



SIMULATION METHODS FOR RF

ALEJANDRO CASTILLA

CERN BE-RF-SRF DCI-UGto. / CAS-ODU Guanajuato, Gto. November 11th – 21st 2015







Outline

- What are numerical simulations for?
- Using math algorithms for RF.
- Volume discretization and its issues.
- Simulations vs measurements.
- Setting up a problem in CST-MWS.
- Other related problems.







Disclaimer

- Great deal of the material for this presentation has been taken from seminars and talks from other people, specially my colleagues:
- Graeme Burt.
- Subashini de Silva.







The Pillbox







Cavity Design

- Accelerator components design
 - RF (radio frequency) cavity design for a variety of applications.
 - Power couplers, higher order mode couplers.
 - Using electromagnetic and mechanical simulators for performance analysis.
 - Limitations:
 - Typically need multiple tools.
 - No good communication available between the tools.









*from S. U. de Silva, ODU.



Design Optimization

*from S. U. de Silva, ODU.

- Aspects of optimization
 - Lower and balanced peak surface fields
 - Stability of the design
 - Cylindrical shape is preferred to reduce flat surfaces
 - Cavity processing
 - Curved end plates for cleaning the cavity
 - Wider separation in Higher Order Mode (HOM) spectrum
 - Multipacting



Numerical Solution of Maxwell's Equations

- Analytical solutions to Maxwell's equations bounded in a cavity are practical for only a few simple cases, instead we solve numerically.
- Most numerical EM codes solve the Helmholtz equation but can be split into two types.

$$\left(\nabla^2 + k^2\right)\Phi = 0$$

Approximate operator Finite Difference Method

Approximate function Finite Element Method

/

*from G. Burt, Lancaster University.





Types of EM solvers

- Finite Difference (Approximate operator)
- Finite Element (Approximate function)
- Boundary Element (uncommon, uses Green's functions)
- Finite Volume (no commercial codes, ignored here)
- Frequency Domain (solve at discrete frequencies)
- Time Domain (solve at time steps)
- Eigenmode (solve for resonant orthonormal eigenmodes of the system)





Yee Cell

Discretise the fields onto a conformal mesh then assume no variation over the unit cell edges.

$$\oint \underline{\mathbf{E}} \cdot \underline{\mathbf{dr}} = -\frac{\partial}{\partial t} \int \underline{\mathbf{B}} \cdot \underline{\mathbf{dS}}$$



Becomes (for each face)

$$\begin{split} B_x \left(t + \frac{1}{2} \delta t, \, x + \delta x, \, y + \frac{1}{2} \delta y, \, z + \frac{1}{2} \delta z \, \right) &= B_x \left(t, \, x + \delta x, \, y + \frac{1}{2} \delta y, \, z + \frac{1}{2} \delta z \, \right) \\ &- \frac{\delta t}{2 \delta y} \left\{ E_z \left(t, \, x + \delta x, \, y + \delta y, \, z + \frac{1}{2} \delta z \, \right) - E_z \left(t, \, x + \delta x, \, y, \, z + \frac{1}{2} \delta z \, \right) \right\} \\ &^{*} \text{from G. Burt, Lancaster University.} &+ \frac{\delta t}{2 \delta z} \left\{ E_y \left(t, \, x + \delta x, \, y + \frac{1}{2} \delta y, \, z + \delta z \, \right) - E_y \left(t, \, x + \delta x, \, y + \frac{1}{2} \delta y, \, z \right) \right\} \end{split}$$

A. Castilla, MEPAS2.0 Gto. Mex. $11^{th} - 21^{st}$ Nov. 2015

Surface Fields

- As E and H fields are solved on separate grids each a half mesh step apart you can only solve one field at the boundary
- The other field has to be interpolated which can lead to errors







EM & Volume Discretisation

• The volume is discretized using Hexahedral (simplest) or Tetrahedral cells (better approximation).



Hexahedral







EM & Volume Discretisation

- Calculation of resonant modes and rf properties of complex electromagnetic structures.
- Solve Maxwell's Equations:
 - Using finite element method (FIT).





400 MHz, rf-dipole crabbing cavity (531,000 total tetrahedrons)



500 MHz, $\beta_0 = 1$ double-spoke cavity (168,000 total tetrahedrons)





How many points are required to define a wavelength?



*from G. Burt, Lancaster University.





How mesh size effects simulation



The accuracy of your results is dependent on the mesh density. In order to test your code you should increase the mesh with various runs until the results do not vary with mesh size.





How mesh size effects simulation



Beware! The run time of your simulation also increases.

Runtime is roughly proportional to the number of mesh cells in the simulation, or the number of cells per dimension cubed, N³

CERN





Mesh Stability



Number of mesh elements





A cunning trick







Perfect Boundary Approximations

- Corrections can be applied to the Yee Algorithm to account for a single cut across a cell.
- This is known as the Perfect Boundary Approximation (CST) or Dey-Mitra Algorithm (VORPAL).
- Not an exact solution so has some issues.
- The cut reduces the cell size so Courant conditions require smaller time steps.







Mesh refinement



One drawback of a conformal mesh is you cannot refine the mesh at critical points without refining the mesh along a cross pattern in all directions.





750 MHz CC Trimming Results



- df/dz per total length
- calculated: -0.46769 MHz/mm
- measured: -0.46299 MHz/mm

Measured



Mode	f (MHz)	Q	Loss (dB)
1	749.492	5600	-53
2	1058.027	6900	-37
3	1370.410	1200	-16
4	1377.506	2000	-19





Real results-Resonant frequency

The particle have a set separation and should all arrive at the same phase hence the cavity frequency must be known. The results start to converge at about 40 lines per wavelength.







Real results-Magnetic field

The surface magnetic field can cause a superconducting cavity to become normal conducting. The mesh density doesn't just effect the resonant frequency it can also effect fields.







Real results- Voltage

In particle physics the cavity voltage is the Electric field seen by a particle travelling at the speed of light integrated over the cavity length.









Symmetry Planes

- Most RF structures have axis of symmetry (both in field and geometry)
- We can make use of image charges and currents in walls to make our simulations smaller by applying boundary conditions to these symmetry planes.







Setting up a Pillbox in CST Microwave Studio

Required Steps

- Choose Units and background material
- Draw Geometry
- Set Boundary conditions and symmetry planes
- Set frequency Range
- Set mesh
- Set up Ports if required
- Add any monitors
- Run the simulation
- Post-processing







Getting Started

i 🗈 📂 星 🍋 😤	भ २ २	Untitled_0 - CST STUDIO SUITE - [Educ	_ 🗇 🗙			
File Home Mod	deling Simulation	on Post Processing View	۵ () -			
Paste Copy Cipboard	Units Problem Type	Image: Solver_ Simulation Image: Optimizer P ar. Sweep Solver_ Simulation Image: Optimizer ar.				
avigation Tree	Dimension					
Jong Forums Jong Forums Jong Forums Jong Forums Jong Forums Jong Forum Jong Forum	m cm mm um nm ft in mil Frequency Hz KHz MHz GHz THz PHz					
Eady		30 Schematic Parameter List × Messages ✓ Name Expression Value Description Type <p< th=""><th>x x taster=1.000 PEC mm GHz ns K</th></p<>	x x taster=1.000 PEC mm GHz ns K			
			17:23			
A. Castilla, MEPAS2.0 Gto. Mex. 11 th – 21 st Nov. 2015 *from G. Burt, Lancaster University.						











A. Castilla, MEPAS2.0 Gto. Mex. 11th – 21st Nov. 2015 *from G. B





CERN

A. Castilla, MEPAS2.0 Gto. Mex. 11th – 21st Nov. 2015 *from G. Bur























CERN

A. Castilla, MEPAS2.0 Gto. Mex. 11th – 21st Nov. 2015 *fr



















A. Castilla, MEPAS2.0 Gto. Mex. 11th – 21st Nov. 2015 *from G.





🥿 🛯 0 X∄ N S P L







ERN

A. Castilla, MEPAS2.0 Gto. Mex. 11th – 21st Nov. 2015 *from G. Burt, Lancaster University.











CERNY





w A 0 X∄ NE S PE





- 🖿 🔐 🐯 🏗 🌜



ERM

A. Castilla, MEPAS2.0 Gto. Mex. 11th – 21st Nov. 2015 *from G. Burt, Lancaster University.





w X N S L 01



A. Castilla, MEPAS2.0 Gto. Mex. 11th – 21st Nov. 2015 *from G. Burt, Lancaster University.



- 🖻 🔐 😚 🏗 🍕

H



S w L 1 X≣ N P 0



A. Castilla, MEPAS2.0 Gto. Mex. 11th – 21st Nov. 2015 *from G. Burt, Lancaster University.



07/11/2015

- 🖻 🔐 😵 🛍 🌜

Wake Fields and Wake Potentials

- Any variation in the cavity profile, material, or material properties will perturb the configuration
- Beam loses part of its energy to establish EM (wake) fields that remain after the passage of the beam
- Wake duration depends on the geometry and material of the structure
 - Wakes persist for duration of bunch passage
 - Wakes last longer than the time between bunches

$$W_{z}(\vec{r},\vec{r}',s) = -\frac{1}{q} \int_{z_{1}}^{z_{2}} dz [E_{z}(\vec{r},z,t)]_{t=(z+s)/c}$$

$$W_{\perp}(\vec{r},\vec{r}',s) = \frac{1}{q} \int_{z_1}^{z_2} dz \left[\vec{E}_{\perp} + c(\hat{z} \times \vec{B})\right]_{t=(z+s)/c}$$

*from S. U. de Silva, ODU.





Calculation Method

A charged particle bunch introduces an electric current density \vec{J} . Combining Ampere's and Faraday's laws

$$\nabla \times (\nabla \times \vec{E}) + \mu \varepsilon \, \frac{\partial^2 \vec{E}}{\partial t^2} + \mu \sigma_{eff} \frac{\partial \vec{E}}{\partial t} = -\mu \frac{\partial \vec{J}}{\partial t}$$

The domain is then discretized into curved tetrahedral elements and $\int E d\tau$ is represented as an expansion in hierarchical Whitney vector basis functions $N_i(x)$

$$\int E d\tau = \sum_{i=1}^{N_p} e_i(t) \cdot N_i(x)$$

*from S. U. de Silva, ODU.







Wake-Field Simulation

• Determine wake potential, impedance and loss factors



Multipacting

For Nb: $E_I > 150 \ eV$ and $E_{II} < 2000 \ eV$



In terms of the cyclotron freq.:

$$\frac{2f}{2n-1} = \frac{eB}{2\pi m}$$

A. Castilla, MEPAS2.0 Gto. Mex. 11th – 21st Nov. 2015

• Multipacting Condition: -Large amount of secondary electrons emitted.

• Resonant Condition:

-Sustainable resonant trajectories. -Impact energies (SEY) >1.





Multipacting

n = multipacting order.





Multipacting Analysis

- Important for maintaining operation gradients, avoiding thermal breakdowns.
- Using SLAC's TRACK3P code from the ACE3P suit for numerical



Extras





CST (Computer Simulation Technology) Suite

- Microwave Studio 3D EM simulation of high frequency components
 - Eigenmode solver, Frequency domain solver
- Particle Studio analysis of charged particle dynamics in 3D electromagnetic fields
 - Stationary particle tracking solver, Wake-field solver, Particle in cell (PIC)
- Mphysics Studio thermal and mechanical stress analysis
 - Structural mechanics solver, Thermal transient / stationary solvers
- Other packages: EM Studio, Cable Studio, PCB Studio, Design Studio
- Is a commercial software suite (CST AG, Germany)
 - With GUI
 - Supports distributed computing
 - Currently runs on stand alone computers

*from S. U. de Silva, ODU.







 ACE3P (Advanced Computational Electromagnetics 3D Parallel) Suite



- From Advanced Computations Department at SLAC National Accelerator Laboratory
- Modules:

Frequency Domain:	Omega3P	– Eigensolver (Damping)	
	S3P	– S-Parameter	
<u>Time Domain</u> :	ТЗР	 Wakefields & Transients 	
Particle Tracking:	Track3P	 Multipacting & Dark Current 	
<u>EM Particle-in-cell</u> : Pic3P		 – RF Guns & Sources (e.g. Klystron) 	
<u>Multi-physics</u> :	TEM3P	– EM, Thermal & Structural Effects	

Courtesy: K. Ko, C. Ng, Z. Li - SLAC



- **Cubit / Trelis** Model and mesh generation
 - Cubit Sandia National Laboratories
 - Trelis Computational Simulation Software, LLC (csimsoft)
- **NERSC** For computation
 - National Energy Research Scientific
 Computing Center: Scientific computing
 facility for Office of Science, U.S.DOE situated
 at Berkeley National Laboratory
- Paraview Visualization
 - Open-source, multi-platform data analysis and visualization application













- Mechanical and thermal analysis
 - ANSYS with HFSS ANSYS Inc.
 - For structural analysis of cavities and cryomodule components
 - Challenges: Extracting deformed structural model to be used in CST or other EM simulation software Astronomy 2 Type: Stress Intensity 2 Type: Stress Intensity 2 Type: Stress Intensity 2
- Cavity integration into cryomodule
 - With ancilliary components, support structures including production details
 - Using CAD software NX by Siemens

*from S. U. de Silva, ODU.







- Beam dynamics study
 - ASTRA (A Space-charge TRacking Algorithm) DESY, Germany
 - Space charge tracking algorithm
 - ELEGANT Argonne National Laboratory
 - 6-D (x, x', y, y', z, ΔE) tracking with matrices and/or canonical integrators, and supports a variety of time-dependent elements
 - Etc.
- Use a large data set of EM 3D field data generated by CST Microwave Studio or Superfish/Poisson (LANL)

*from S. U. de Silva, ODU.



