

# XV MEXICAN WORKSHOP ON PARTICLES AND FIELDS

## RING INJECTORS LUMINOSITY LIMITS: SPACE CHARGE

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# Beam parameters

The luminosity is a famous parameter in detectors ...

$$L_{del} = t \langle L \rangle \text{ barn}^{-1}$$

$$N_{event} = BR\sigma L_{del}$$

$$L = \frac{N_b^2 k_b \gamma f}{4\pi\beta^* \epsilon_n} F$$

$N_b$  Number of particles per bunch

$K_b$  Number of bunches per beam

$\beta^*$  Beta function

$\gamma$  Relativistic factor

$\epsilon_n$  Normalized emittance

BR Branching Ratio

$f$  collision frequency

LHC Luminosity from  $10^{33}$  to  $10^{34} \text{ cm}^{-2} \text{ s}^{-1}$

Tevatron Max Luminosity  $10^{32} \text{ cm}^{-2} \text{ s}^{-1}$

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Two Mexicans working here

There is a group in Guanajuato  
working in this parameter

- A good luminosity is the difference between wait 1 o 10 years!

LHC Luminosity from  $10^{33}$  to  $10^{34} \text{ cm}^{-2} \text{ s}^{-1}$

Tevatron Max Luminosity  $10^{32} \text{ cm}^{-2} \text{ s}^{-1}$

# Electron cloud issues in the LHC

Humberto Maury – Universidad de Guanajuato

Gerardo Guillermo - CINVESTAV

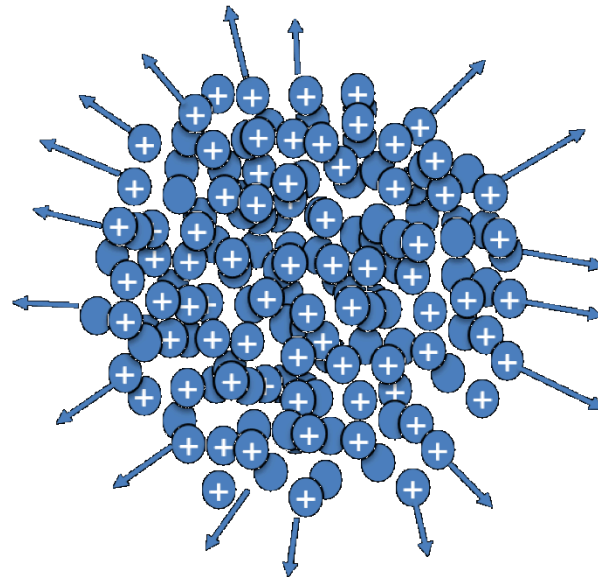
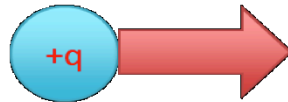
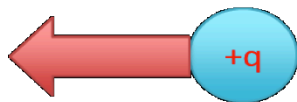
- Electron cloud: a set of electrons created inside the LHC vacuum chamber by *ionization of the residual gas* or by photoemission due to *beam-induced synchrotron radiation*. It can affect the **accelerator performance** and or **degraded beam quality**.
- Effects:
  - pressure increase by several orders of magnitude.
  - Beam instabilities
  - Additional heat load to the cryogenic system.

$$L = \frac{N_b^2 k_b \gamma f}{4\pi\beta^* \epsilon_n} F$$

# Space charge

- Coulomb's force separate the same charge particles from each other
- High intensity beams suffer from instabilities due severe space charge problems

$$L = \frac{N_b^2 k_b \gamma f}{4\pi\beta^* \epsilon_n} F \quad I = \frac{qeN_b}{t}$$



# Beam space charge

$$F = q(E + v \times B)$$

Consider a longitudinally cylindrical beam with constant charge density  $\rho$  and current  $I$ .

The magnetic field creates an opposite force to the electric field

$$F = q\left(E - \frac{v\beta E}{c}\right)$$

$$= q(E - \beta^2 E) = q\frac{E}{\gamma^2}$$



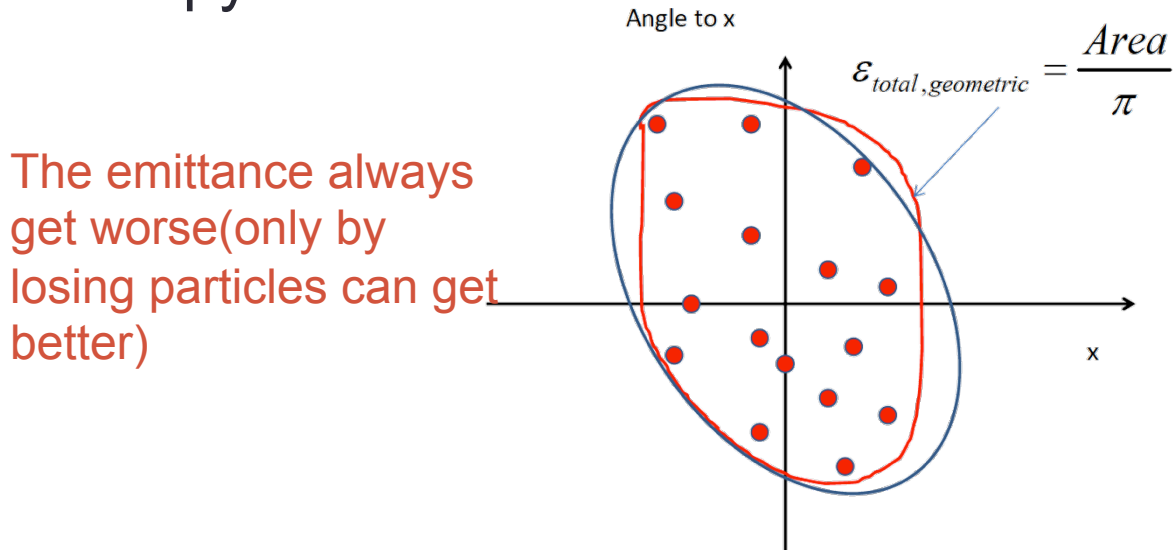
$$E_r = \frac{\rho r}{2\epsilon_0} \quad J = \frac{I}{\pi a^2}$$

$$B_\theta = \frac{\mu_0 J r}{2} = \frac{\mu_0 I r}{2\pi a^2} = \frac{\beta E_r}{c}$$

Energy	$\gamma$ (protons)	$\gamma$ (electrons)
45Kev	1.00004	1.088
50 Mev	1.05328	98.084
160 MeV	1.17052	314.112
1 Gev	2.06574	1957.145
1 TeV	1066.7889	1956952.375

# Emittance

- The region in phase space that the particles in a beam occupy is called the beam emittance

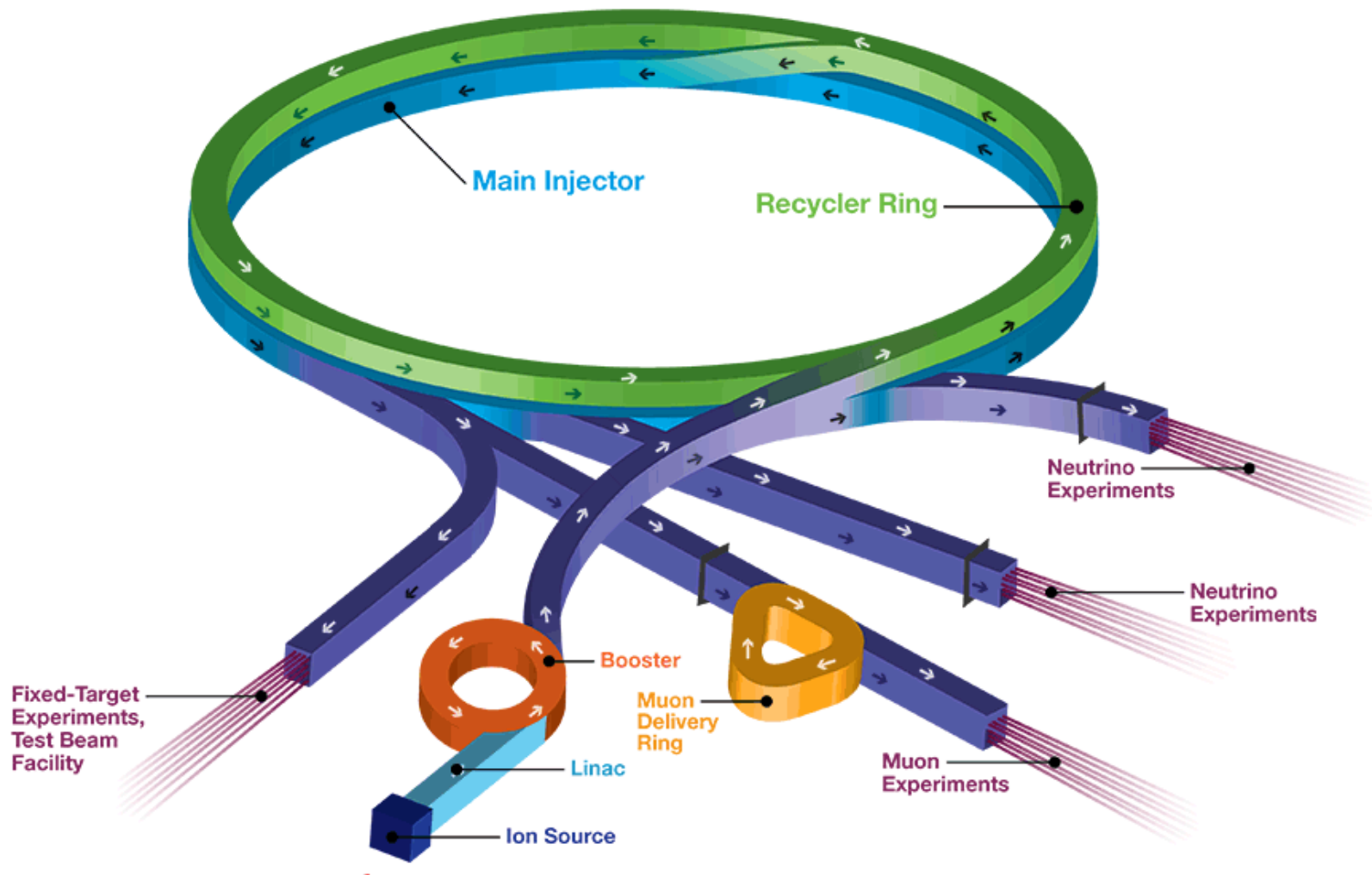


$$\varepsilon = \frac{r}{2c} \sqrt{\frac{kT}{m}} \propto T^{1/2}$$

- Mm.mrad? mrad from  $p_x/p_z$
- The goal in every accelerator is to have the lower beam emittance achievable

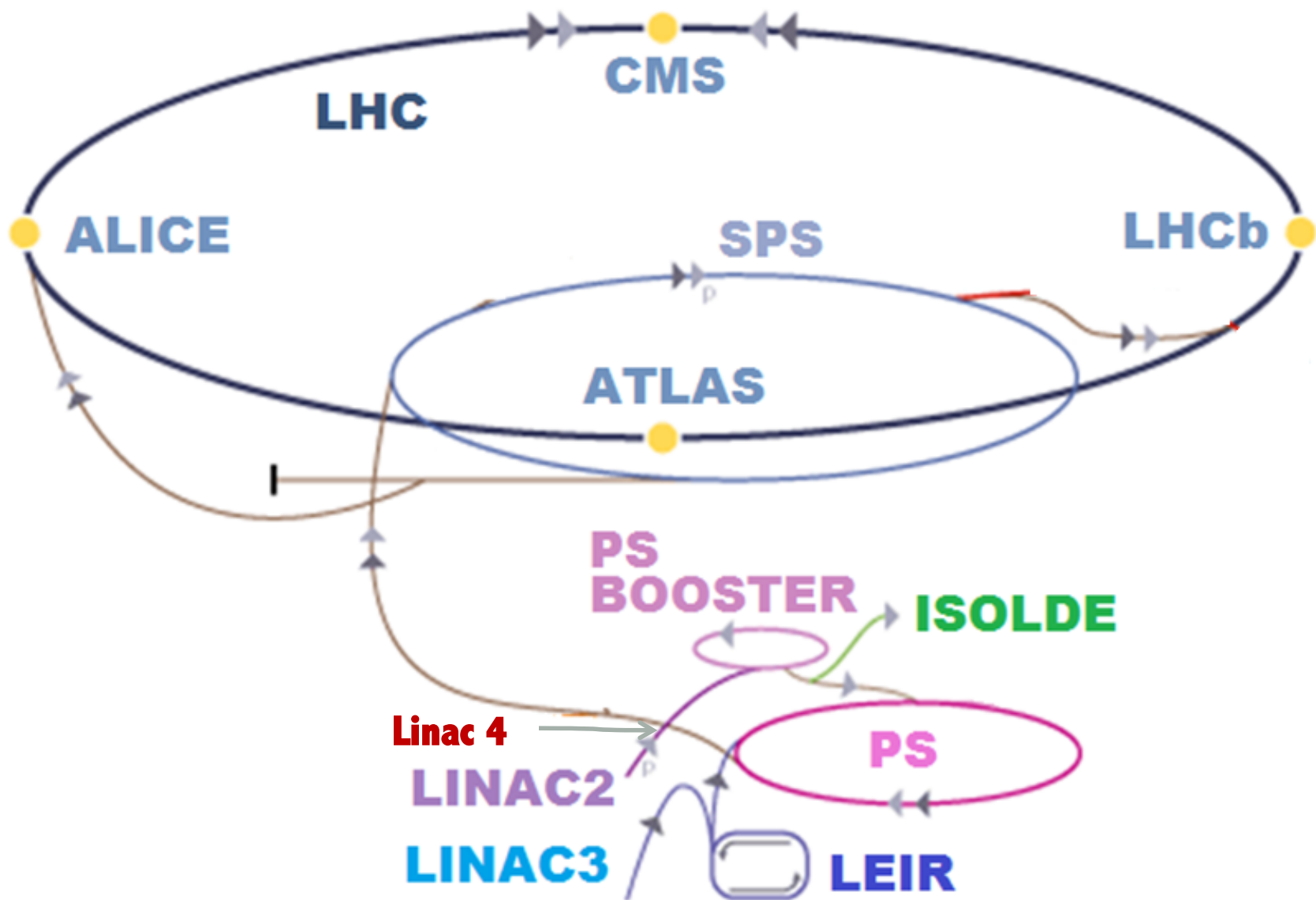
$$Brightness \propto \frac{1}{\varepsilon_y \varepsilon_x}$$

# Fermilab Accelerator Complex





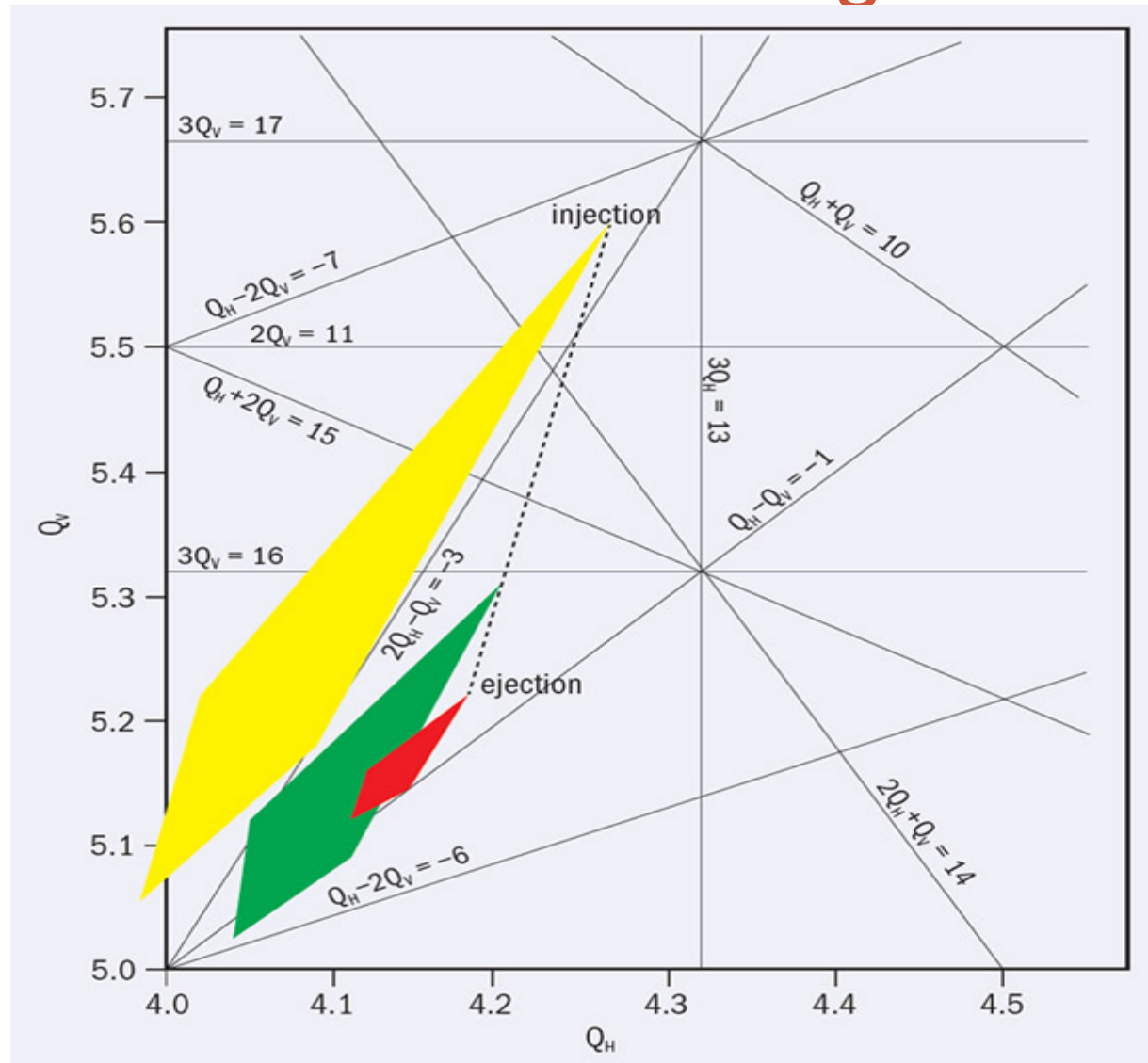
# Cern Accelerator complex



# Why we need Linacs before the Rings?

- The space charge limits the beam intensity inside the ring

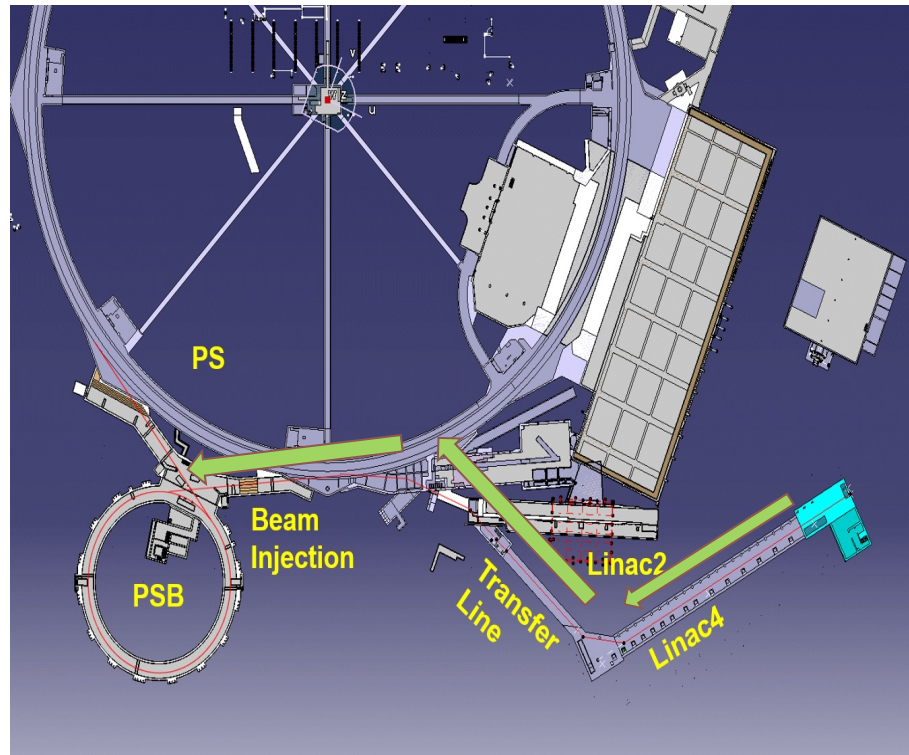
$$\Delta Q \propto \frac{N_b}{\epsilon_n \beta \gamma^2}$$



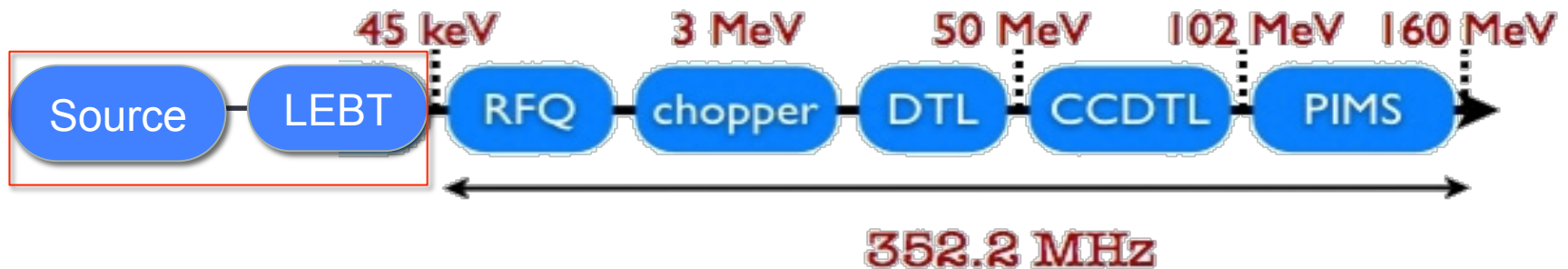
# Linac 4 vs Linac2

$$\Delta Q \propto \frac{N_b}{\epsilon_n \beta \gamma^2}$$

- ◆ H- Beam
- ◆ 160 MeV
- ◆ Lower Emittance than Linac2



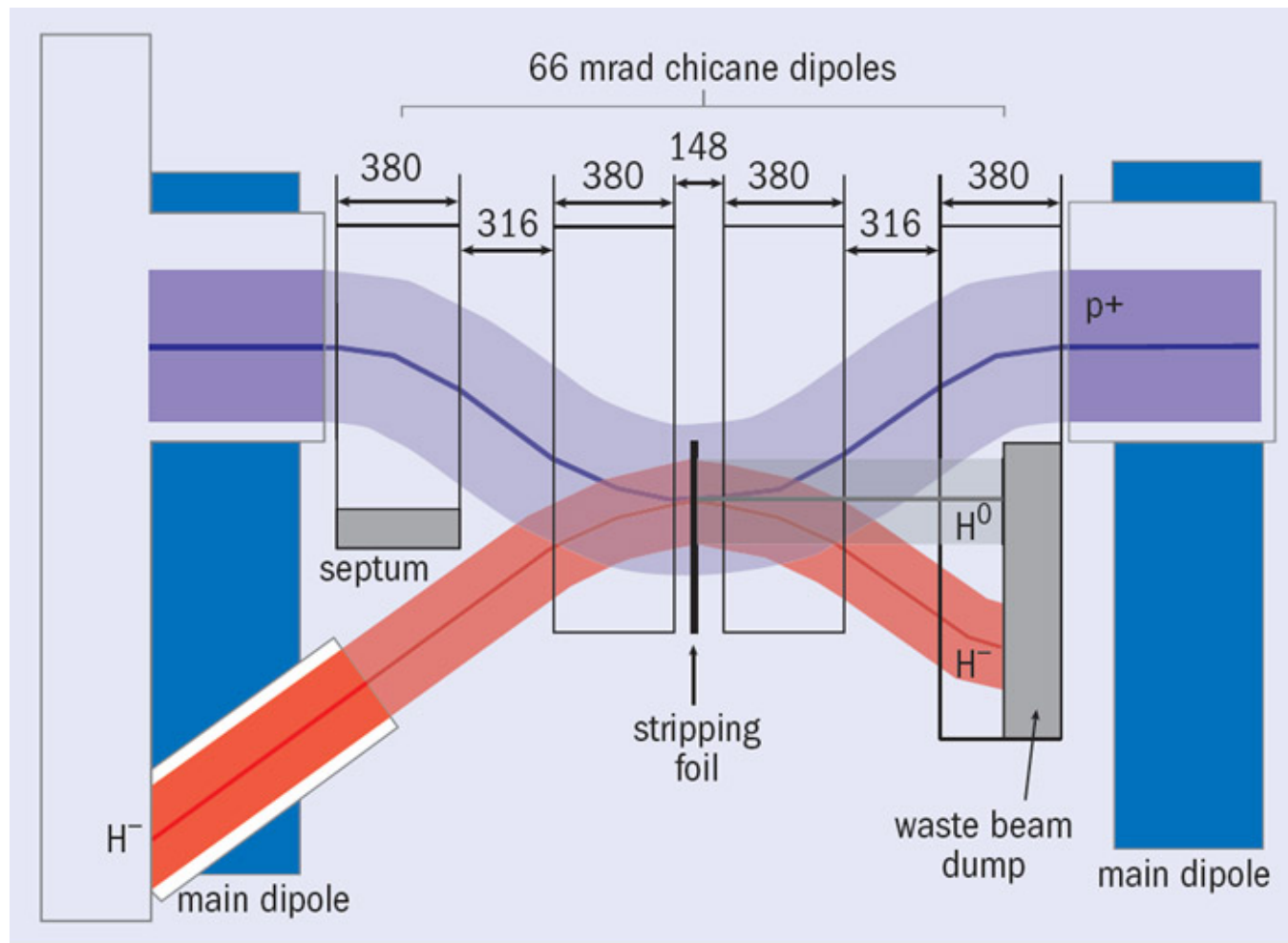
	Linac 4	Linac 2
Ions	H-	P
Energy	160 MeV	50 MeV
Emittance	0.4 mm mrad	1 mm mrad
Frequency	352.2 MHz	202.56 MHz
Beam Current	40 mA	170 mA.
Pulse Length	400 us	100 us



# Why $H^-$ ?

- Because the Space charge repulsion is easier to insert a negative beam inside a positive beam
- In theory the efficiency will be 99% in transform the  $H^-$  in to protons

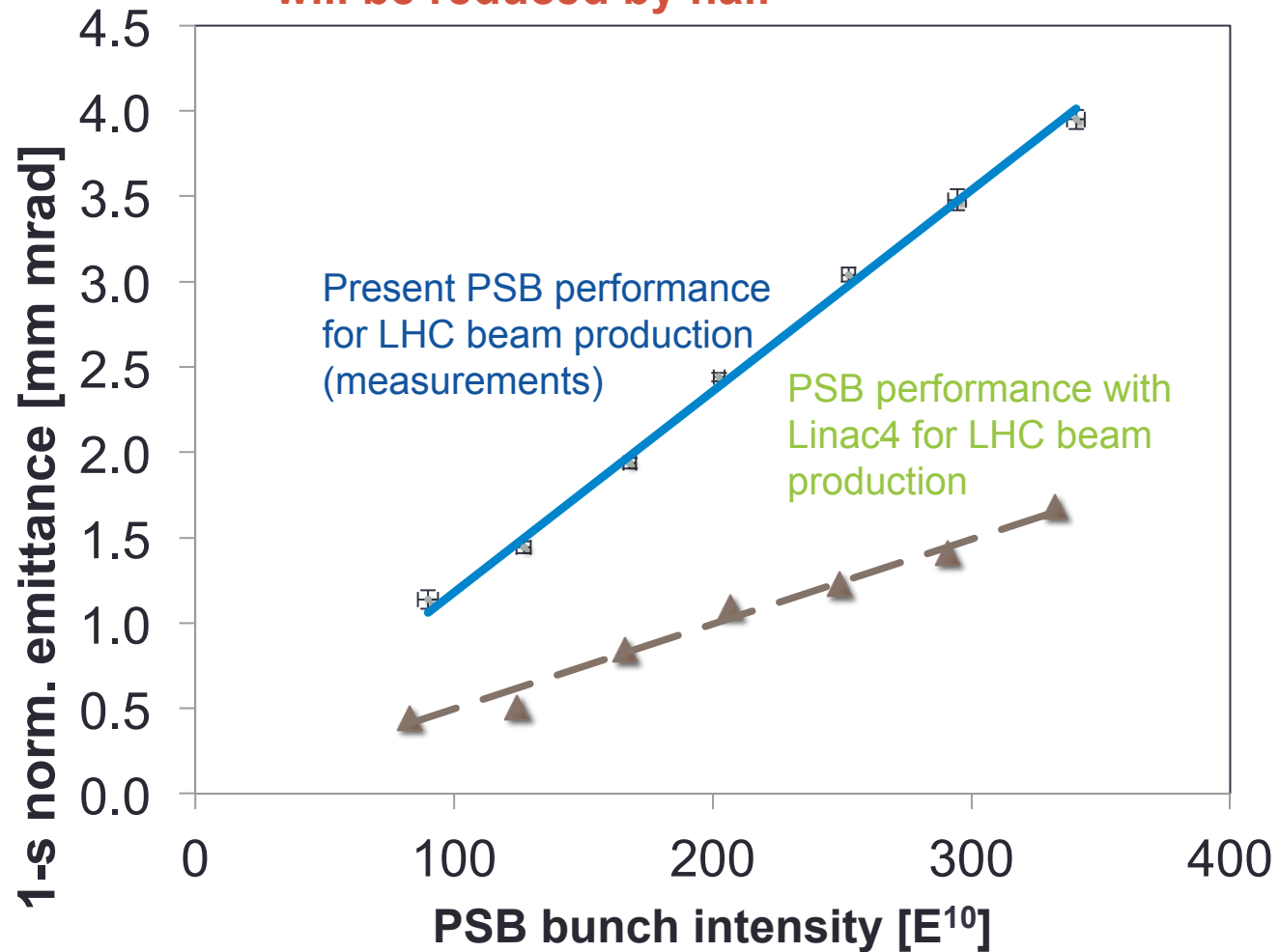
## Schematic of $H^-$ injection into a circular machine.



# PSB Emittance

By inject H- the emittance after the injection will be reduced by half

- LHC beams Brightness out of the PSB are mainly determined by space charge during the injection process



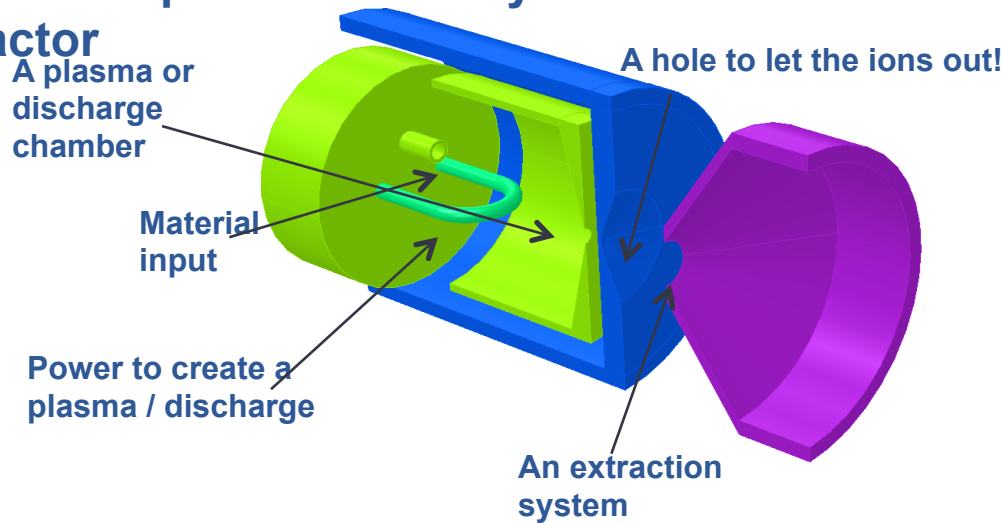
# Where the particles are created?

- The maximum  $N_b$  will be at the beam source output
- After been created the value  $C$  will be almost constant
- As we get closer to the ion source more physics need to be included in simulations to predict results

$$C \propto \frac{N_b}{\varepsilon_n}$$

# Source and Beam Extraction

The beam is formed by the particles in the plasma taken by the extractor



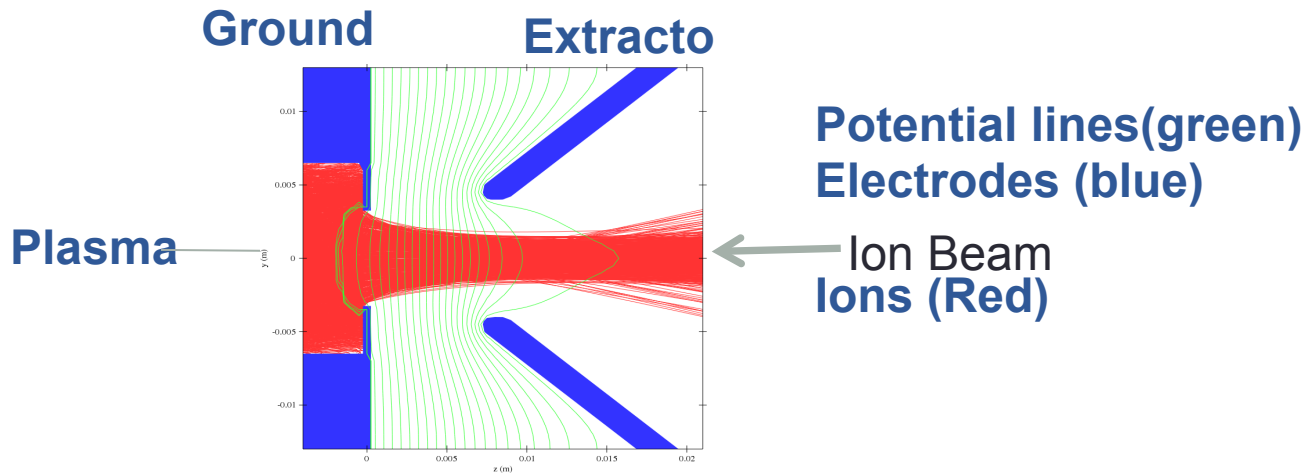
$$j = \frac{4\epsilon_0}{9} \sqrt{\frac{2e}{m}} \frac{V^{3/2}}{d^2}$$

Child–Langmuir law

The beam energy is calculated by the difference of potential

$$E = q(V_{source} - V_{ground})$$

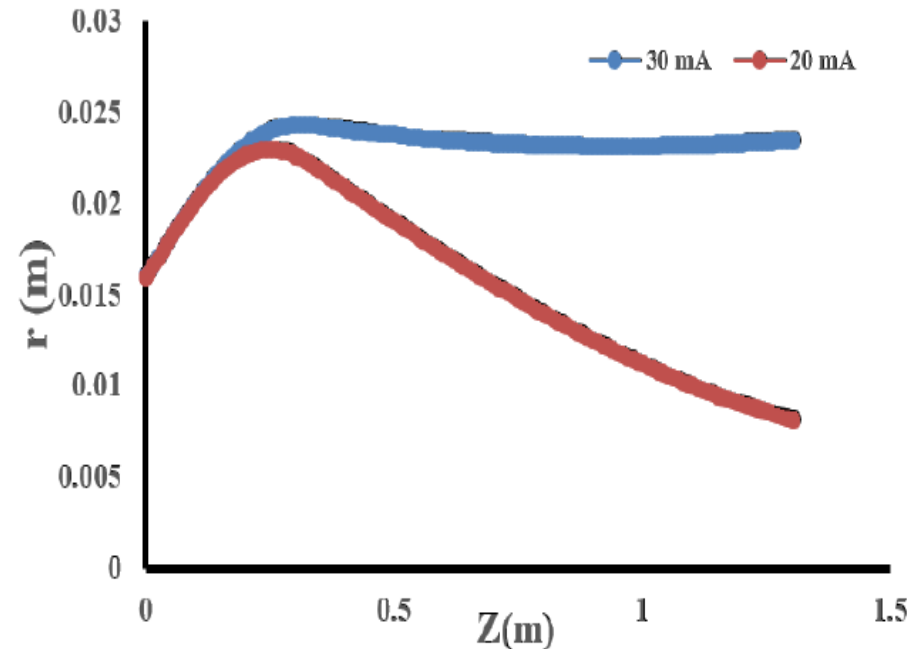
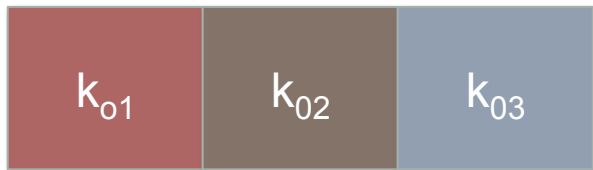
Plasma extraction potential (meniscus)



# Beam transport under Space charge

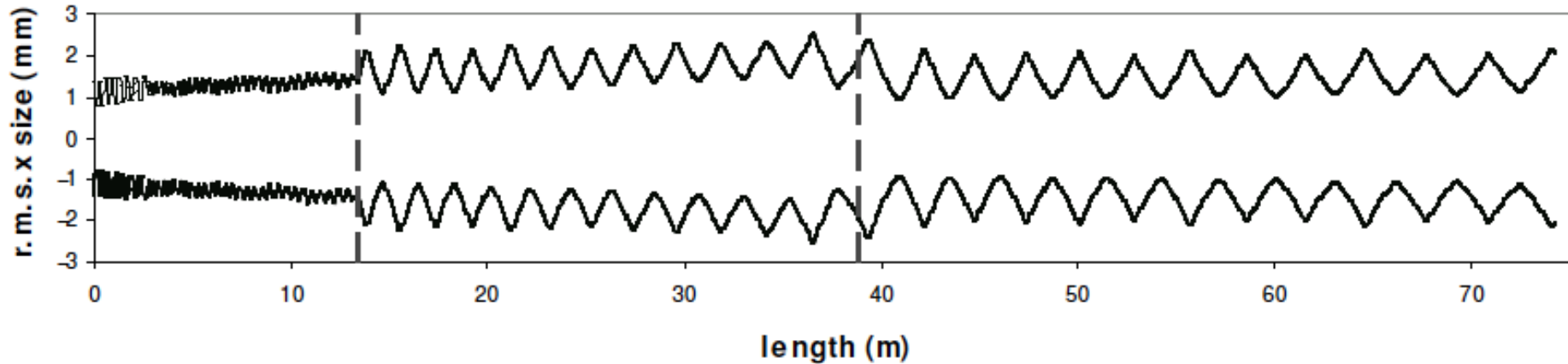
- The envelope of a cylindrically symmetric beam ( $r$ ) transported along the  $z$ -axis can be described by the differential equation:
  - $k_0$  is the focusing strength
  - $K_0$  is the space charge term

$$\frac{d^2 r}{dz^2} + k_0^2 r + \frac{\epsilon^2}{r^3} - \frac{K_0}{r} = 0$$





# Beam transport simulations

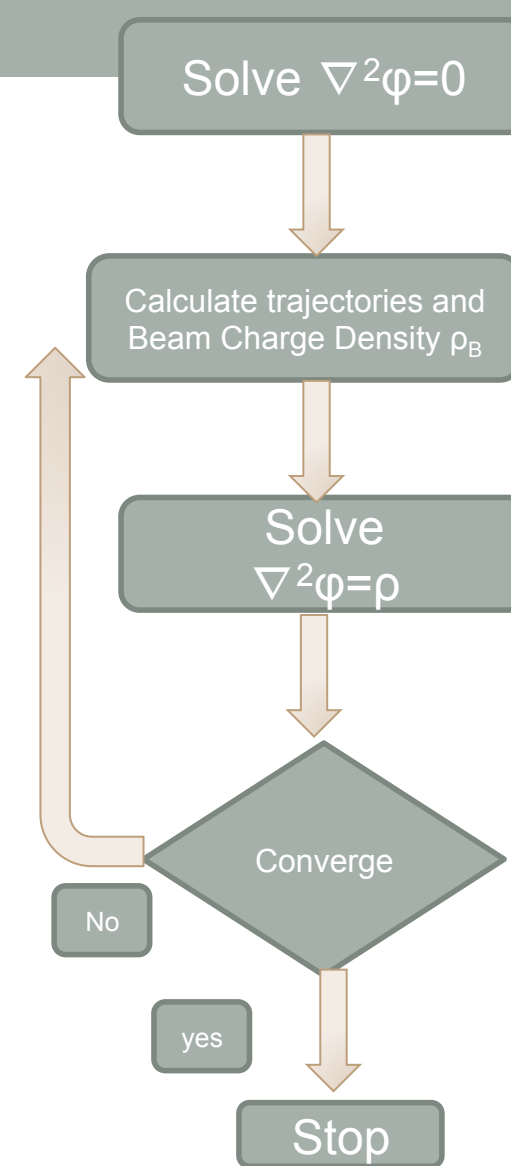
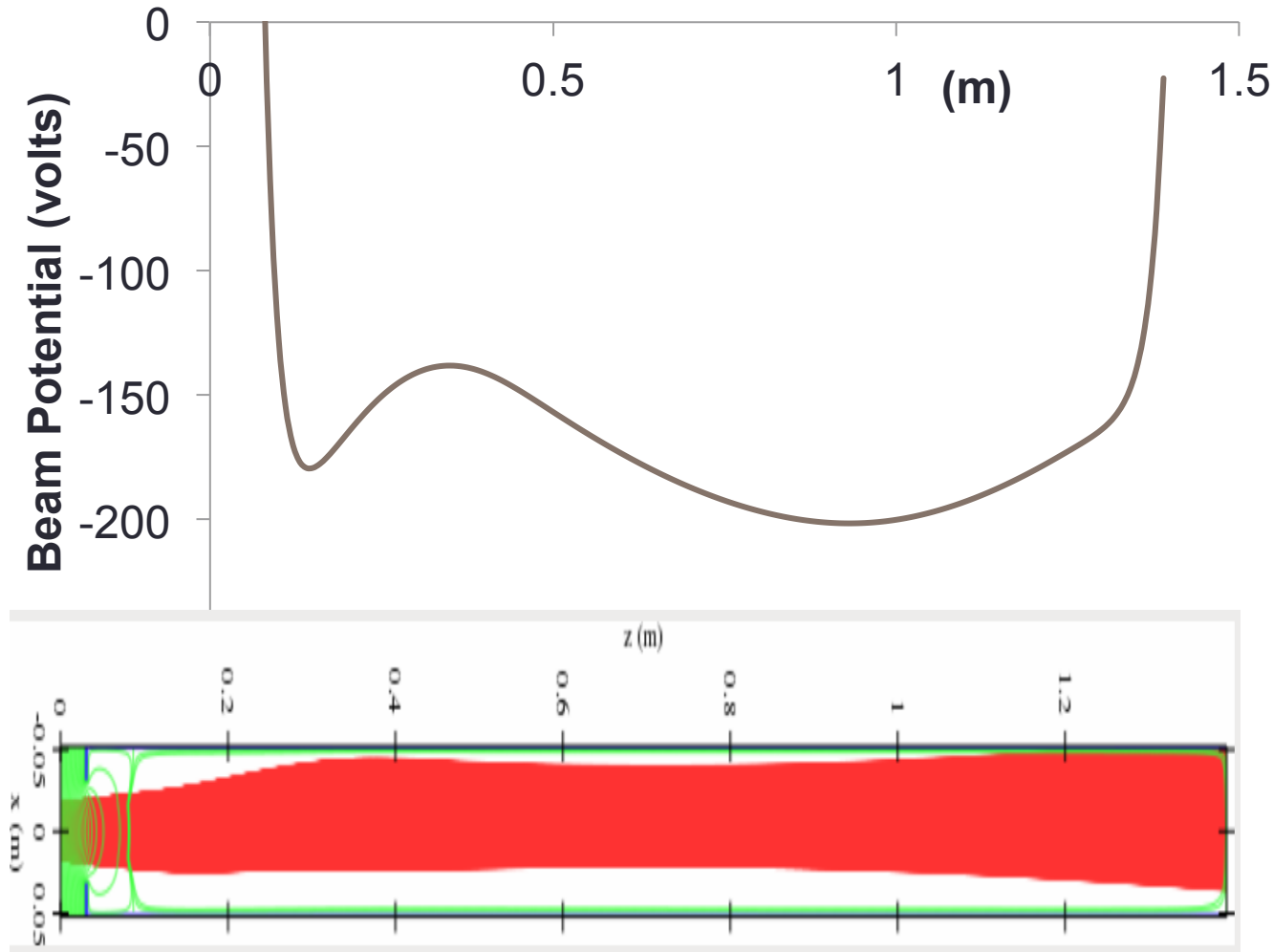


- ◆ Envelope code where a set of matrix represent the magnets in the accelerator

$$X = RY = R(n) \dots R(2)R(1)Y$$

- ◆ They are really fast (to obtain the solution it takes a few seconds), and can cover all the accelerator chain in a normal computer without problem

# Ray tracing codes



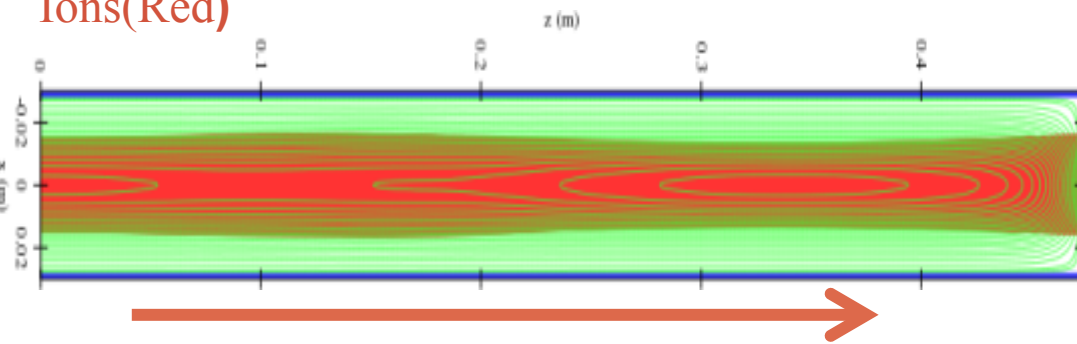
◆ Is more accurate but the simulation time and resource consumption is higher

# Space charge compensation

- The vacuum is not perfect inside the beam pipe
- Range of pressure from  $5 \times 10^{-7}$  mbar to  $1 \times 10^{-5}$  mbar
- The beam ionizes residual gas atoms
- The ionized particles from opposite charge are trapped by the beam potential and same charge particles are expelled to the walls

Full space charge beam transport

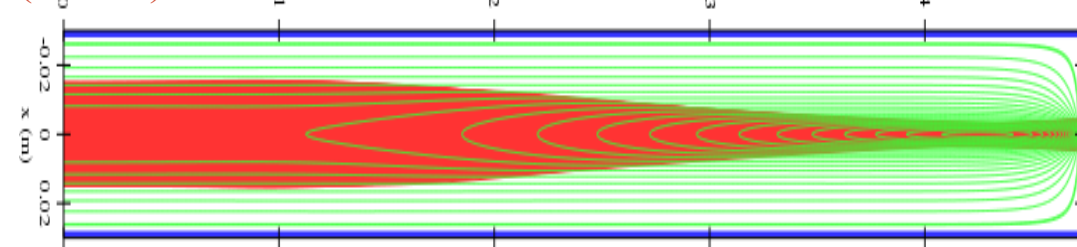
Ions (Red)



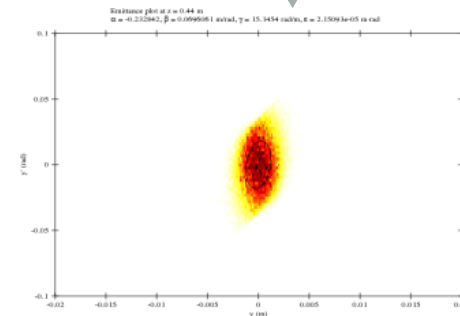
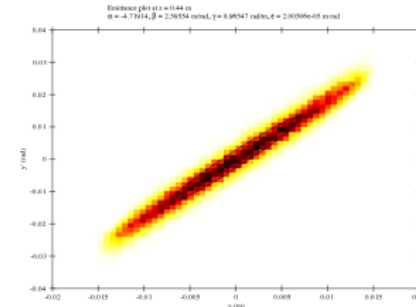
Beam Direction

80% compensation

Potential lines  
(Green)



$$\rho = \rho_{beam} - \rho_{secondary}$$

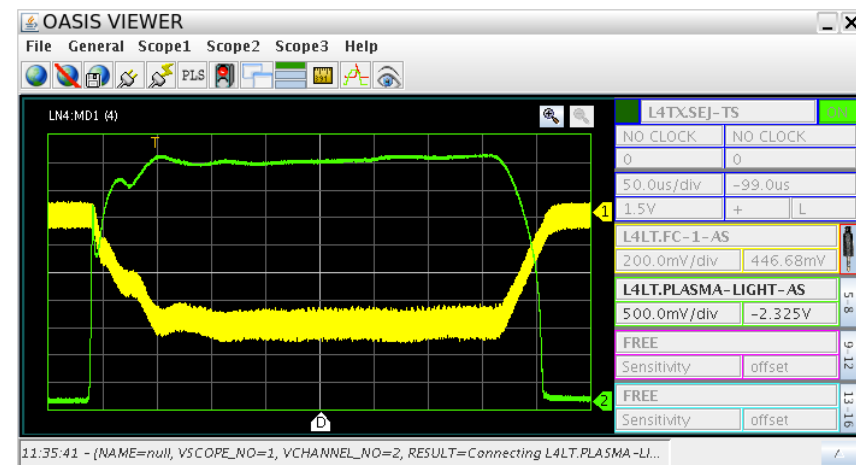
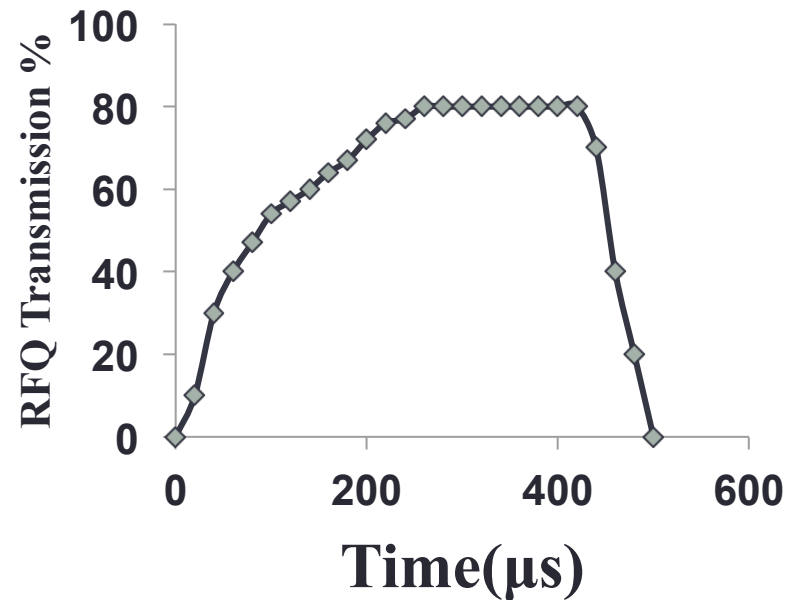


# Compensation time

- The space charge compensation is time dependent

$$\tau = \frac{1}{v_b (\sigma_{H_2}(E)n_{H_2} + \sigma_x(E)n_x)}$$

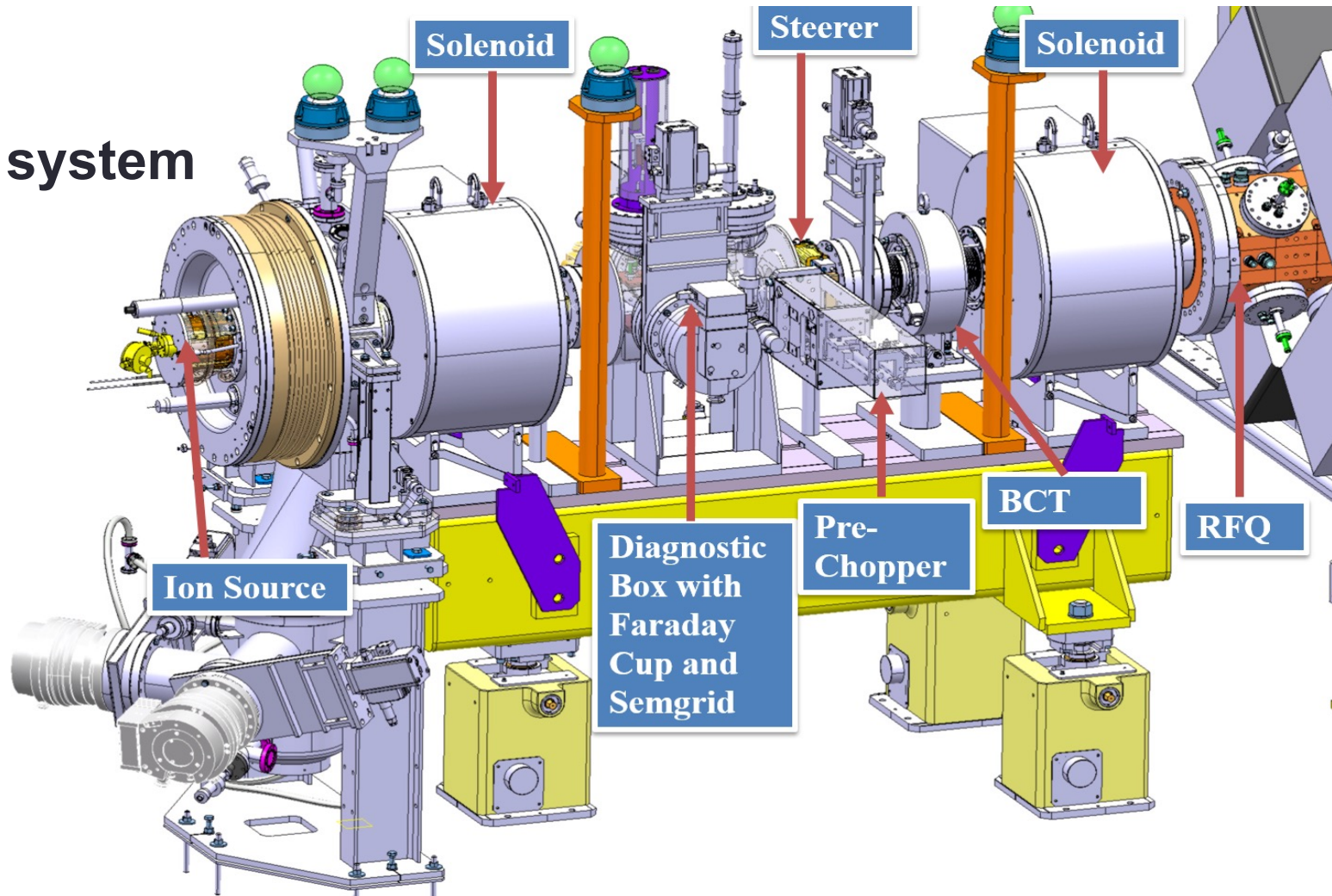
- Beam pulse **500  $\mu\text{s}$**
- Baseline  **$1 \times 10^{-6}$  mbar**



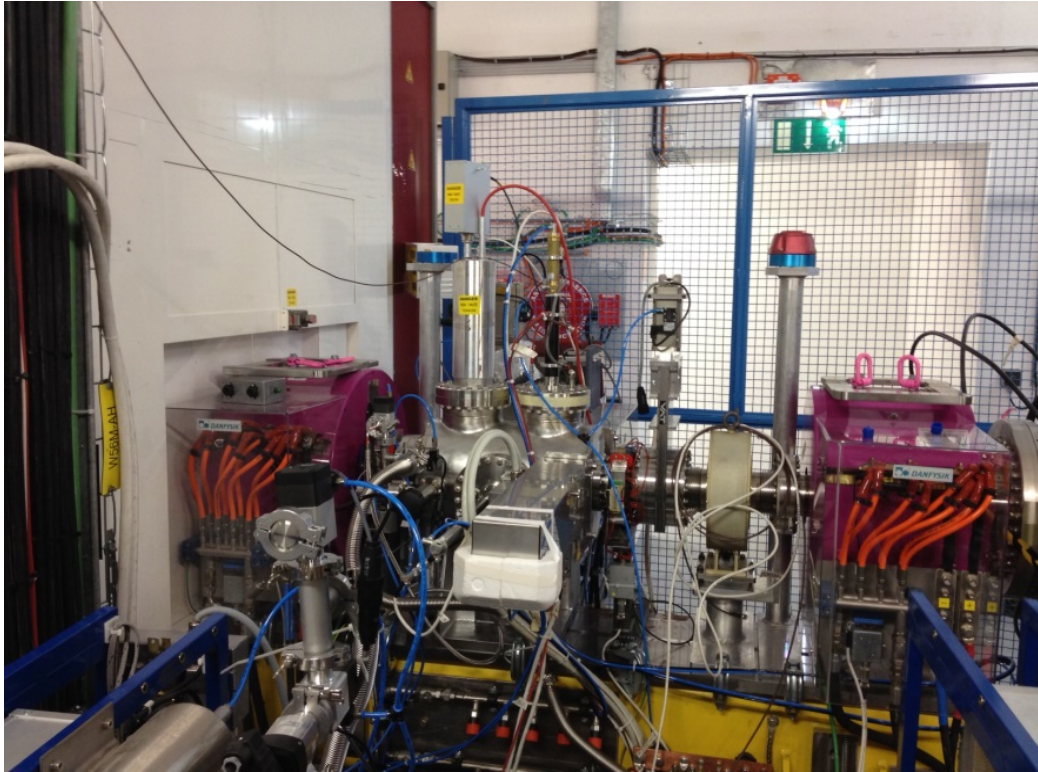
The beam properties are not constant in time and is necessary to use advanced codes to simulate this effect.

# Linac4 Low energy beam Transport (LEBT)

- Source
- Multi step extraction system
- LEBT
- RFQ



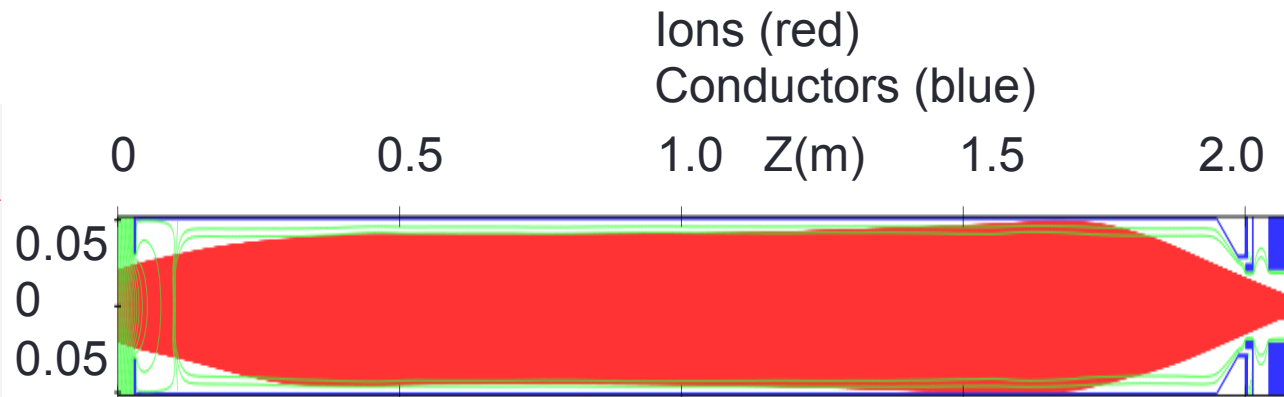
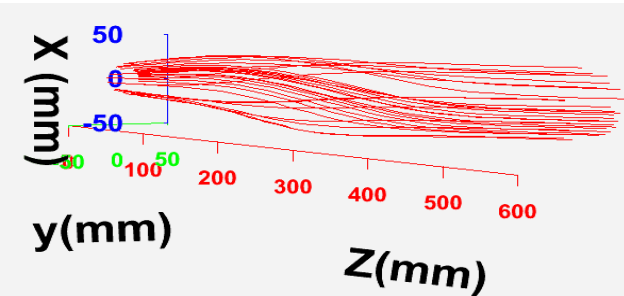
# Linac4 LEBT elements



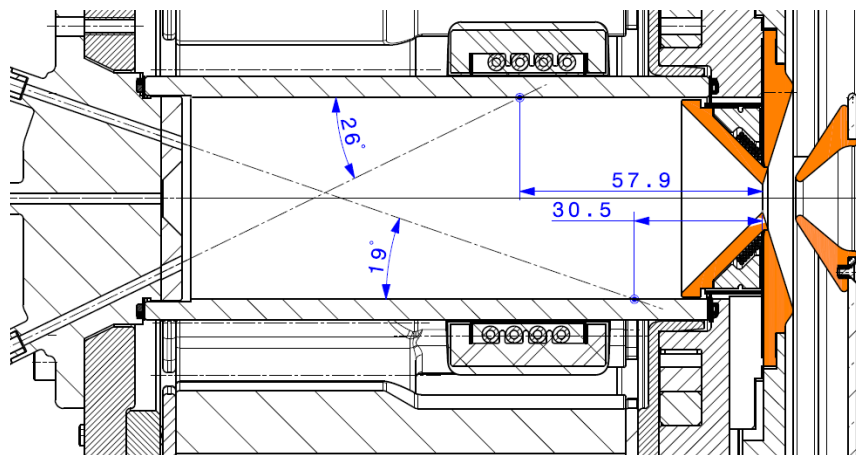
The system include:

- 2XSolenoid
  - Beam focusing
  - Matching
- 4XSteerers
  - Correct beam center alignment
- Gas Injection
  - Controlling space charge compensation degree
- Faraday Cup
  - Beam current measurement
- The beam is unbunched in this stage.
- 

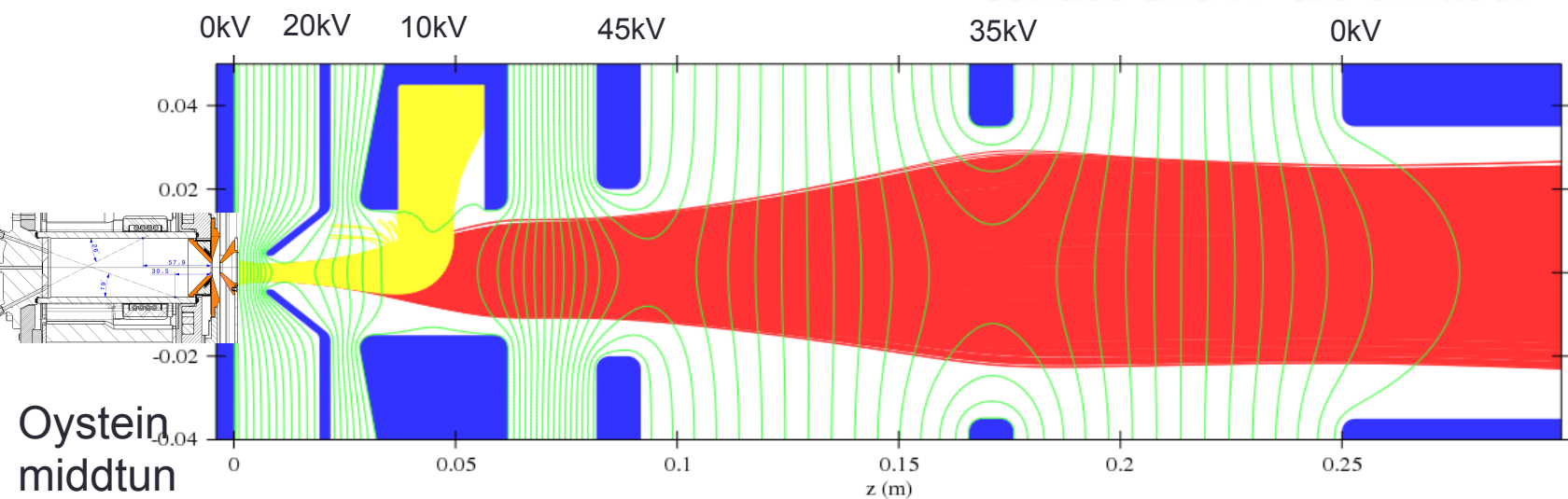
Solenoid Effect in the beam



# Linac4 Ion Source and extraction system



- Plasma is created using 2MHz RF in a solenoid coil.
- The H<sup>-</sup> is produced in the plasma volume and surfaces
- A surface near the extraction is coated with cesium, evaporated from an oven at the back of the source.
- The plasma ions strike the cesium surface and H<sup>-</sup> are emitted.

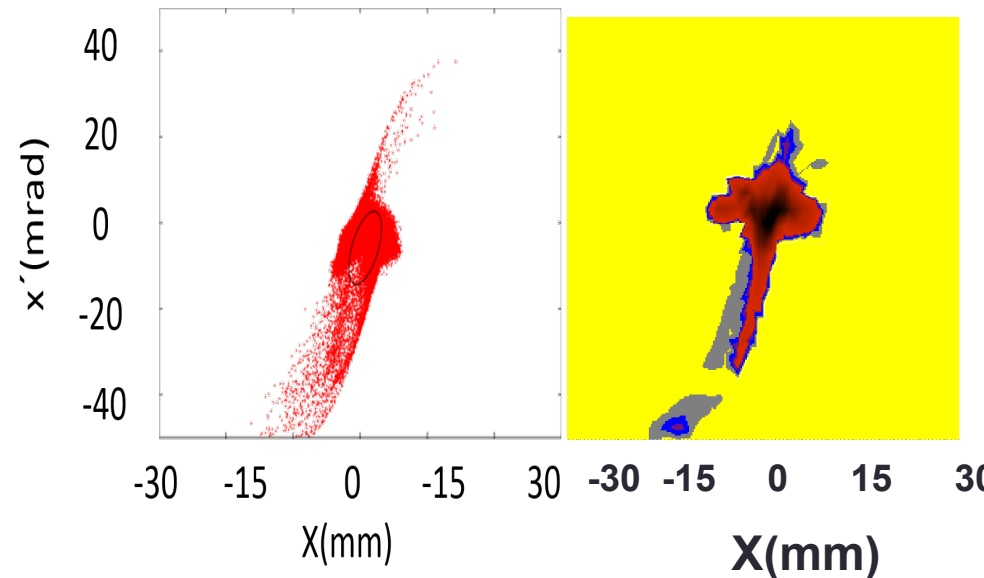
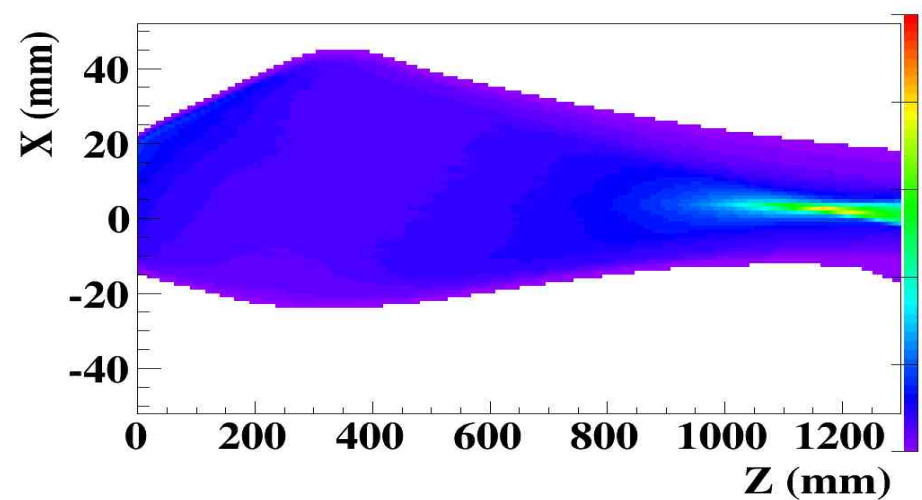


- Electrons (yellow) are extracted along with negative ions (red).

# Linac4 source simulation using Ray tracing code

➤ Beam Current 35 mA

Simulation    Measurements



Emittance mm.mrad 1 rms (norm) :    **0.29**

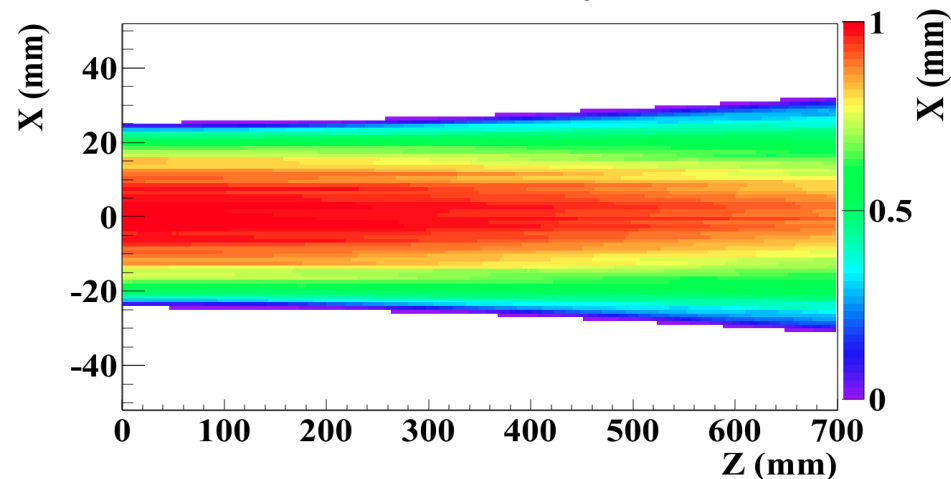
**0.55**

The absolute value of the emittance is almost 200% bigger in measurements

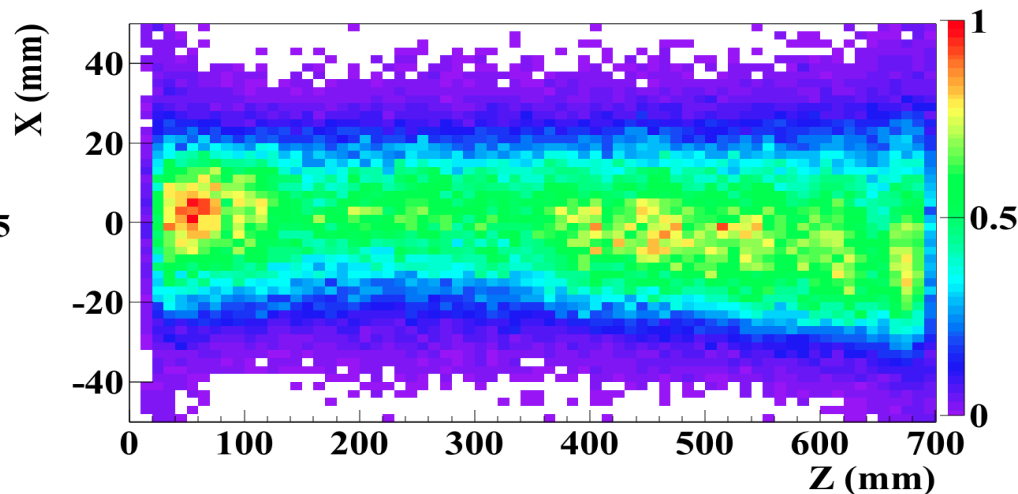


# Particle in Cell codes (PIC)

## Beam density



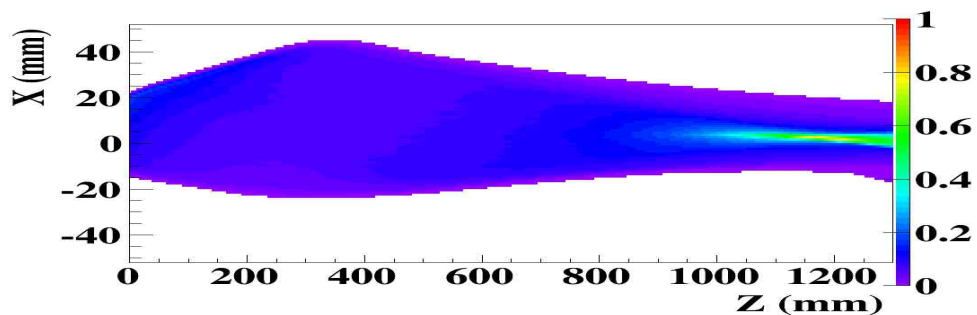
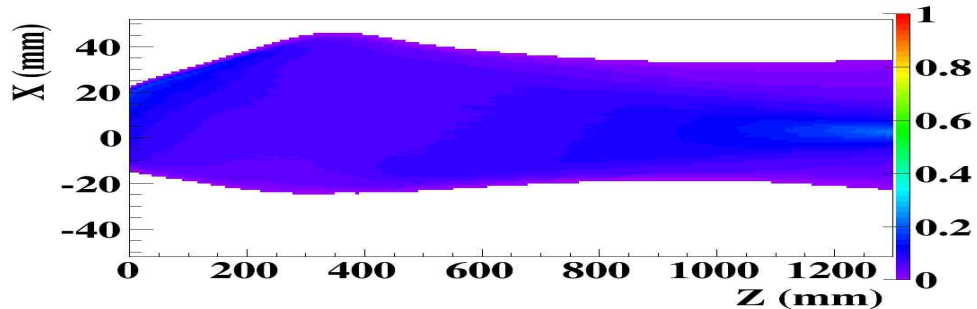
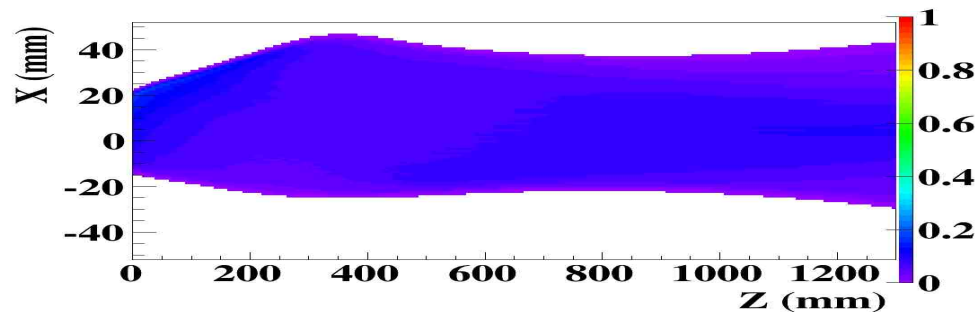
## Secondary ions density



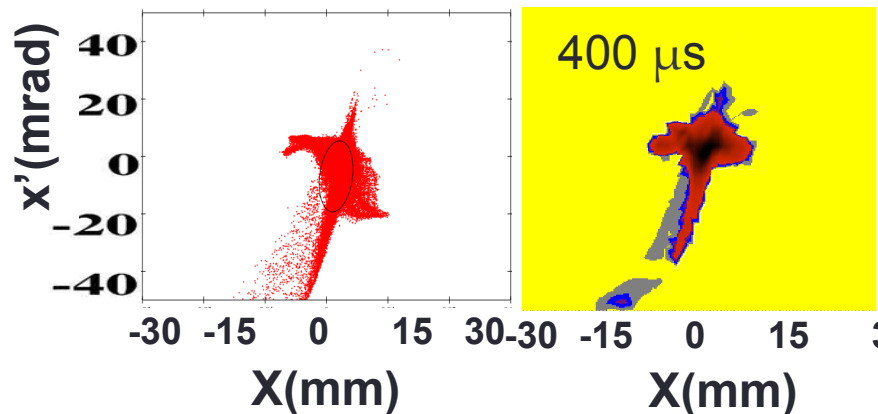
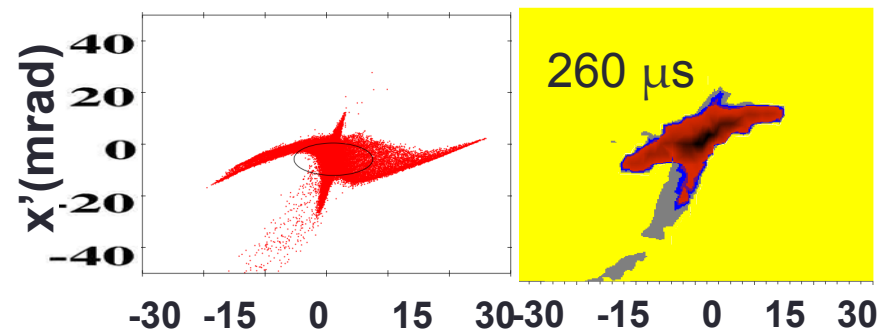
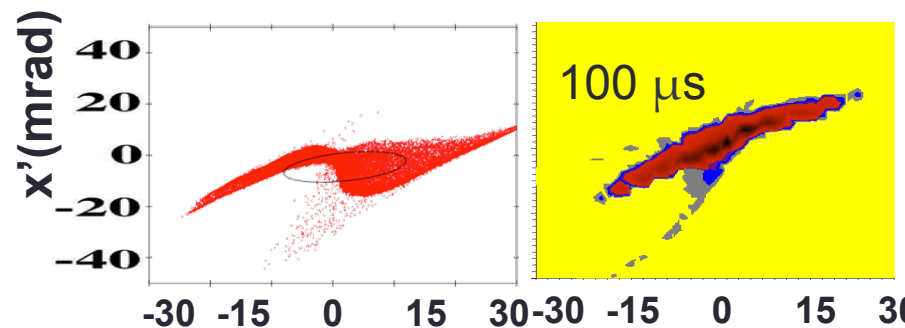
- ◆ The interaction between the beam and the residual gas inside the vacuum pipe generates secondary ions
- ◆ The secondary ions play a major role in the beam transport
- ◆ To simulate 1 meter the simulation time goes from 1 day to 3 months

# Space Charge compensation using H<sub>2</sub>

- Pressure  $1.2 \times 10^{-6}$  mbar
- Current 35 mA

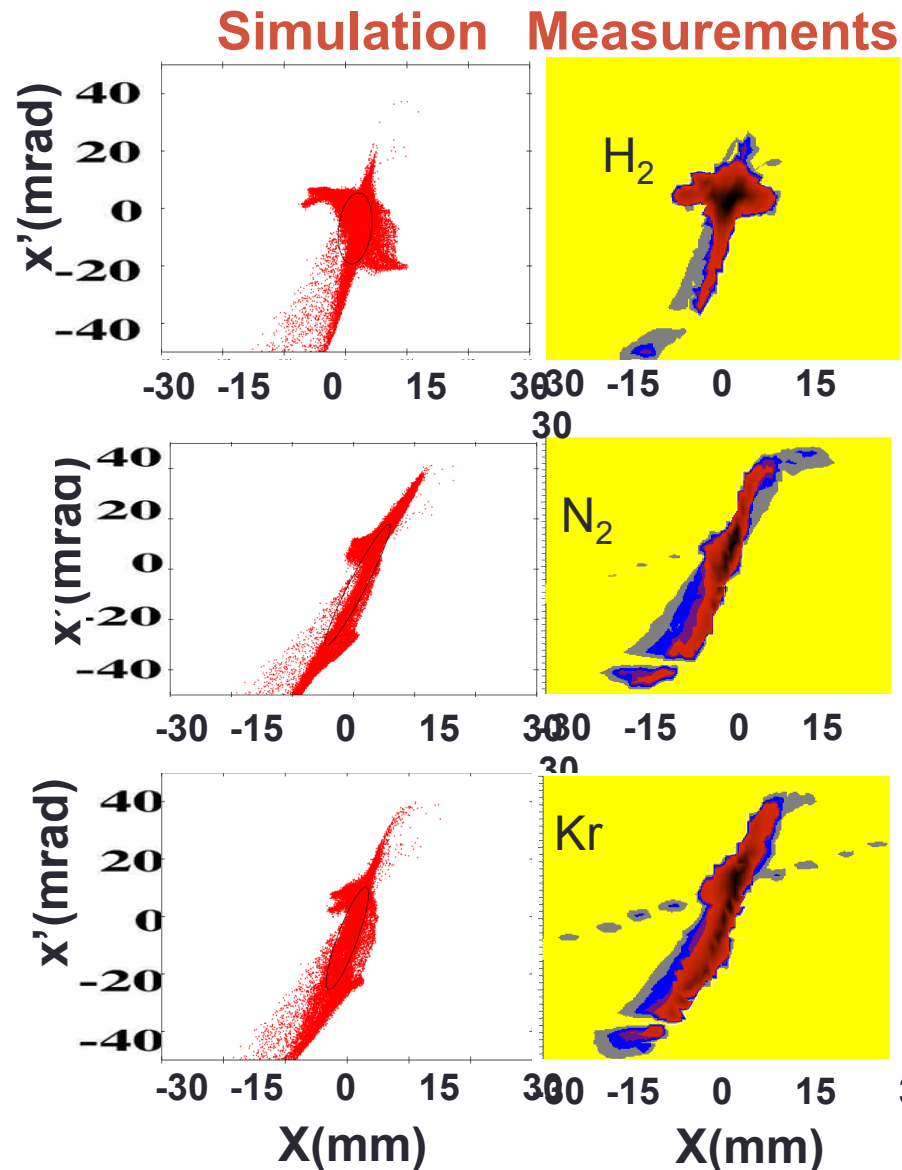
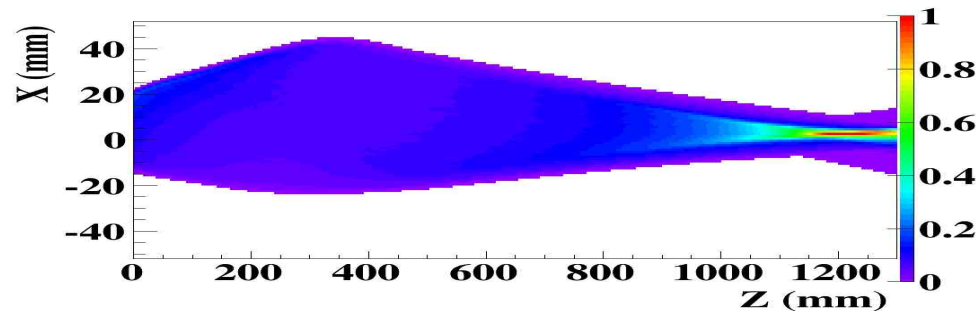
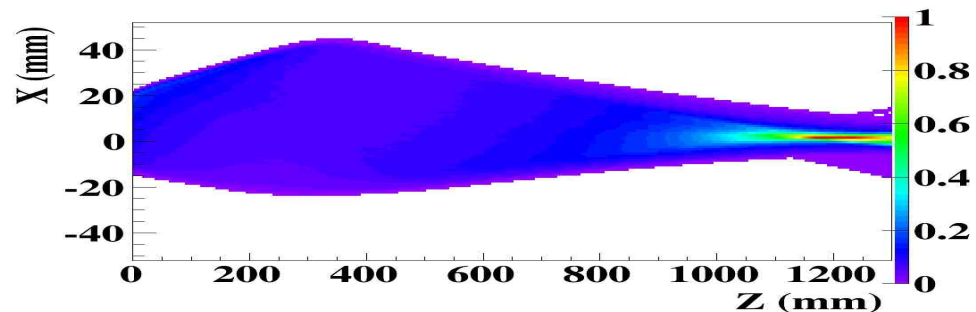
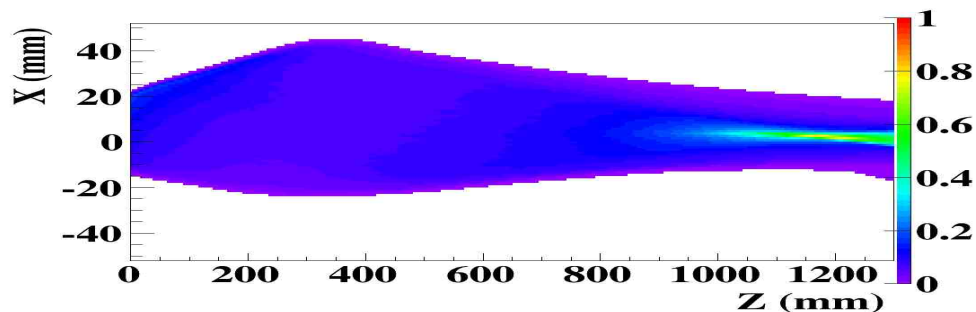


## Simulation Measurements



# Compensation using different gases

- $H_2$   $N_2$  and Kr
- Several pressures were used



# Summary

**The beam space charge in the injectors is one of the biggest challenge to reach a higher luminosity in beam colliders**

**At CERN, Linac4 is under construction to mitigate this problem and duplicate the Luminosity.**

**The goal of produce 80 mA in the Linac4 source continue to be a problem**

**A new method to take into account secondary ions created by the beam has been developed**

**The simulation results from the Linac4 beam source agree with the measurements like not other code available today.**

**Some improvements has been made to the beam source at linac4 thanks to the results of the simulations**

# Thank you!

## Disfruten la playa

Acknowledgement

Richard Scrivens

Ildefonso León

Guillermo Contreras

CONACYT

And the Linac4 collaboration