

## 3 BODY STOP DECAY WITH GRAVITINO/GOLDSTINO IN THE FINAL STATE

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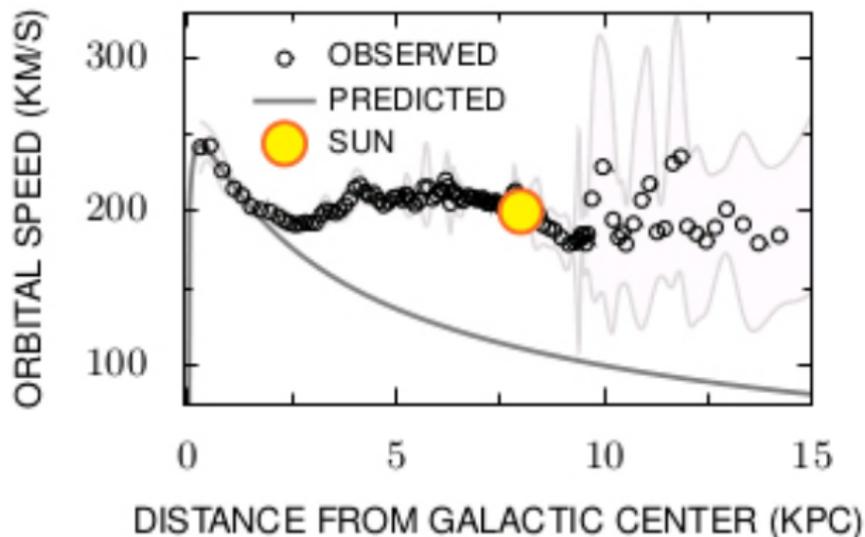
XXIX Reunión Anual de Partículas y Campos



# Outline

- Motivation: Dark Matter (**DM**) and Supersymmetry (**SUSY**),
  - Gravitino Lightest Supersymmetric Particle (**LSP**) and Dark Matter,
  - The Next Lightest Supersymmetric Particle (**NLSP**),
- **3 body Stop decay**,
  - With Gravitino
  - With Goldstino
- Conclusions.

# Dark Matter



$$F_T = ma$$

$$v = \sqrt{\frac{G_N M}{r}}$$

# New Physics: LHC and the Cosmos

- After 30-40 years of Standard Model success (apart from  $\nu$  hints) something new should happen or else...,
- LHC is expected to find Physics Beyond the SM (BSM),
- At the same time, astro/cosmo phenomena also suggest BSM physics may be needed,
- **SUSY is one of the best motivated theories** BSM.

**Supersymmetry** is a symmetry that relates Boson fields degree of freedom with Fermion Fields degree of freedom.

$$|Fermions\rangle = \hat{Q} |Bosons\rangle$$

$$|Bosons\rangle = \hat{Q} |Fermions\rangle$$

There are a lot of SUSY models. We will use the Minimal Supersymmetric Standard Model **MSSM (4D) with  $\mathcal{N} = 1$** .

# The MSSM particle content

	SM	Superpartners
SM Bosons	$W^\pm, Z, \gamma$ gluon Higgs bosons	Wino, Zino, Photino gluino Higgsinos
SM Fermions	quarks leptons neutrinos	squarks sleptons sneutrinos

The particles in the **SM** are distinguished from their superpartners from R-Parity. With R-Parity being preserved the (LSP) cannot decay.

# What is the LSP?

The lightest Supersymmetric (**LSP**) particle is suppose to be stable and electrically neutral and to interact weakly with the particles of the **SM**. These are exactly the characteristic required for **DM**.

- One option is: **Gravitino** ( $\tilde{\Psi}_\mu$ ), there are other ones (**Neutralino**, **Sneutrino**).

# Gravitino $\tilde{\Psi}_\mu$ as LSP in SUGRA models

- One of the candidates for dark matter in Supergravity (**local Supersymmetry**) is the gravitino. However, the exact relation is uncertain.
- Gravitino is a very weakly interacting particle, with coupling  $\simeq 1/M_{Pl} = 0.83 \times 10^{-19} GeV^{-1}$  (in Supergravity).
  - Practically undetectable. (**Except for its gravitational effect.**)
  - The next lightest SUSY particle (NLSP) could be long lived.
- We have many possibilities for the NLSP: neutralino, stau, **stop**, sneutrino. Each with its own distinct phenomenology.

## NLSP phenomenology with $\tilde{\Psi}_\mu$ as LSP

To determine viability of each scenario one need to:

- Identify **Gravitino-MSSM** interactions,
- Define the models (**CMSSM**, **NUHM**),
- Calculate **NLSP lifetime**,
- Check consistency with low-energy and collider constraints,
- Verify implications for cosmology.

## Gravitino ( $\tilde{\Psi}_\mu$ ) interactions

- All interactions can be derived from SUGRA lagrangian (Wess-Bagger),
- Most relevant terms are:
  - Coupling with chiral superfields:

$$\mathcal{L}_1 = -\frac{1}{\sqrt{2}M} \tilde{D}_\nu^* \phi_i^* \tilde{\Psi}_\mu \gamma^\nu \gamma^\mu \chi_R^i + h.c. (L \rightarrow R) \quad (1)$$

- Coupling with vector superfields:

$$\mathcal{L}_2 = \frac{i}{8M} \tilde{\Psi}_\mu [\gamma^\nu, \gamma^\rho] \gamma^\mu \lambda^a F_{\nu\rho}^a \quad (2)$$

## 3 body Stop decay

To determine viability of the scenario (NLSP) with  $\tilde{\Psi}_\mu$  as LSP, we need to calculate NLSP life time.

$$\tau = \frac{1}{\Gamma}$$

(3)

The expression for the decay width is (After integration):

$$\frac{d\Gamma}{dxdy} = \frac{m_{\tilde{t}_1}^2}{256\pi^3} |\overline{\mathcal{M}}|^2$$

- Let's focus on the amplitude for the moment

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- Let's focus on the amplitude for the moment
- (Squaring and summing over final polarizations).

$$\tilde{t}_1 \rightarrow b + W + \tilde{\Psi}_\mu$$

We are considering the  $\tilde{t}$  as **NLSP**. In what follows we need to consider the following Feynman diagrams:

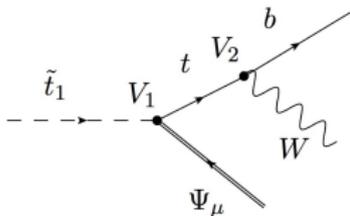


Figure 1. top diagram

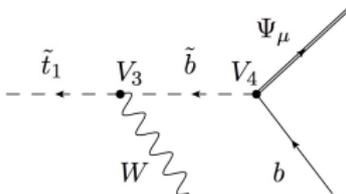


Figure 2. sbottom diagram

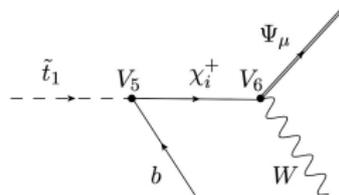


Figure 3. chargino diagram

Where  $V_i \forall i = 1, \dots, 6$  are the interactions vertex.

## 3 body Stop decay

We can write the squared amplitude from the last 3 Feynman diagram.

$$\begin{aligned}
 |\overline{\mathcal{M}}|^2 &= |\mathcal{M}_t|^2 + |\mathcal{M}_{\tilde{b}}|^2 + |\mathcal{M}_{\chi^+}|^2 \\
 &\quad + 2 \operatorname{Re}(\mathcal{M}_t^\dagger \mathcal{M}_{\tilde{b}} + \mathcal{M}_t^\dagger \mathcal{M}_{\chi^+} + \mathcal{M}_{\tilde{b}}^\dagger \mathcal{M}_{\chi^+})
 \end{aligned} \tag{4}$$

In order to keep control of  $|\overline{\mathcal{M}}|^2$  we shall write the chargino amplitude as  $\mathcal{M}_{\chi} = \mathcal{M}_{1\chi} + \mathcal{M}_{2\chi}$ .  
 (Because the huge vertex functions in the process.)

The amplitudes are:

$$\mathcal{M}_t = C_t P_t(q_1) \bar{\Psi}_\mu p^\mu (A_t + B_t \gamma_5)(q_1 + m_t) \gamma^\rho \epsilon_\rho(k) P_L u(p_2)$$

$$\mathcal{M}_{\tilde{b}_i} = C_{\tilde{b}_i} P_{\tilde{b}_i}(q_2) \bar{\Psi}_\mu q_2^\mu (a_i P_L + b_i P_R) p^\rho \epsilon_\rho(k) P_L u(p_2)$$

$$\mathcal{M}_{1\chi_i^+} = C_{\chi_i^+} P_{\chi_i^+}(q_3) \bar{\Psi}_\mu \gamma^\rho \epsilon_\rho(k) \gamma^\mu (V_i + \Lambda_{i5})(q_3 + m_\chi)(S_i + P_{i5}) u(p_2)$$

$$\mathcal{M}_{2\chi_i^+} = \underline{C}_{\chi_i^+} P_{\chi_i^+} \bar{\Psi}_\mu p^{\rho\mu} (T_i + Q_{i5}) \epsilon_\rho(k) (q_3 + m_\chi)(S_i + P_{i5}) u(p_2)$$

Basically we shall have to compute 4 squared amplitudes and 6 interferences in [4]. ☹

Squared amplitudes can be written as:

$$|\mathcal{M}_{\psi_a}|^2 = C_{\psi_a}^2 |P_{\psi_a}(q_a)|^2 W_{\psi_a\psi_a} \quad (5)$$

where  $\psi_a = (t, \tilde{b}_j, \chi_k^+)$ , and the functions  $W_{\psi_a\psi_a}$  are :

$$W_{\psi_a\psi_a} = \mathbf{w}_{1\psi_a} + m_{\psi_a} \mathbf{w}_{2\psi_a} + m_{\psi_a}^2 \mathbf{w}_{3\psi_a} \quad (6)$$

$\mathbf{w}_{i\psi_a} \forall i = 1, 2, 3, 4$  are functions of the scalar products of the momenta  $p, p_1, p_2, k$ .

The interference terms may be written as follows:

$$\mathcal{M}_{\psi_a}^\dagger \mathcal{M}_{\psi_b} = C_{\psi_a} C_{\psi_b} P_{\psi_a}^*(q_a) P_{\psi_b}(q_b) W_{\psi_a \psi_b} \quad (7)$$

with

$$W_{\psi_a \psi_b} = \mathbf{w}_{1\psi_a \psi_b} + m_{\psi_a} (\mathbf{w}_{2\psi_a \psi_b} + m_{\psi_b} \mathbf{w}_{3\psi_a \psi_b}) + m_{\psi_b} \mathbf{w}_{4\psi_a \psi_b} \quad (8)$$

Finally we will need to compute the 36 w's. 😞

But it is ok, fortunately we have **Mathematica** 😊





With Mathematica help but also with human intuition (**hand Working**), we obtain for the same last squared amplitude:

We have

$$\mathcal{M}_{\chi_i^+}^\dagger = C_{\chi_i^+} P_{\chi_i^+}^*(q_3) \bar{u}(p_2) (S_j - P_j \gamma_5) (\not{q}_3 + m_\chi) (V_j - \Lambda_j \gamma_5) \epsilon_\sigma(k) \Psi^\sigma$$

Squaring and summing over final polarization we obtain:

$$|\overline{\mathcal{M}}_{\chi_i^+}|^2 = C_{\chi_i^+}^2 |P_{\chi_i^+}(q_3)|^2 W_{\chi_i^+ \chi_i^+}$$

where

$$\begin{aligned} W_{\chi_i^+ \chi_i^+} &= \text{Tr} \left[ M_{\rho\sigma} D^{\rho\sigma} (V_i + \Lambda_i \gamma_5) (\not{q}_3 + m_\chi) (S_i + P_i \gamma_5) \not{p}_2 \right. \\ &\quad \left. (S_j - P_j \gamma_5) (\not{q}_3 + m_\chi) (V_j - \Lambda_j \gamma_5) \right] \\ &= w_{1\chi_i^+ \chi_i^+} + m_{\chi_i^+} w_{2\chi_i^+ \chi_i^+} + m_{\chi_i^+}^2 w_{3\chi_i^+ \chi_i^+} \end{aligned}$$

with

$$w_{1\chi_i^+ \chi_i^+} = -\frac{8\Sigma_{ij1}h_2}{3m_W^2 m_{\tilde{G}}^2} \left( (m_{\tilde{G}}^2 + f_3) \left( 2(m_{\tilde{G}}^2 + m_W^2) + 4f_3 - q_3 \right) + f_2 \left( -2m_{\tilde{G}}^2 - 2f_3 + q_3 \right) - 2f_1 (m_{\tilde{G}}^2 + f_3) \right)$$

$$w_{2\chi_i^+ \chi_i^+} = -\frac{8(\Sigma_{ij1} + \Sigma_{ij2})h_2}{3m_W^2 m_{\tilde{G}}^2} (m_{\tilde{G}}^2 - f_1 - f_2 + 2f_3 + m_W^2)$$

$$w_{3\chi_i^+ \chi_i^+} = -\frac{8\Sigma_{ij3}h_2}{3m_W^2 m_{\tilde{G}}^2} (m_{\tilde{G}}^2 - f_2 + f_3)$$

with  $h_2 = (2m_W^2 m_{\tilde{G}}^2 + (f_3)^2)$  and also we have used the substitutions:

$$\Sigma_{ij1} = (S_i S_j + P_i P_j)(V_i V_j - \Lambda_i \Lambda_j) - (S_i P_j + P_i S_j)(\Lambda_i V_j - V_i \Lambda_j)$$

$$\Sigma_{ij2} = (S_i S_j + P_i P_j)(V_i V_j - \Lambda_i \Lambda_j) + (S_i P_j + P_i S_j)(\Lambda_i V_j - V_i \Lambda_j)$$

$$\Sigma_{ij3} = (S_i S_j + P_i P_j)(V_i V_j + \Lambda_i \Lambda_j) + (S_i P_j + P_i S_j)(\Lambda_i V_j + V_i \Lambda_j)$$

# Goldstino Approximation

In spontaneously broken SUSY models, the massless gravitino field  $\tilde{\Psi}_\mu$  acquires mass by absorbing goldstino modes. For the case  $\sqrt{s} \gg m_{\tilde{G}}$ , the wave function of the gravitino of helicity  $\pm \frac{1}{2}$  components is approximately proportional to  $p_\mu/m_{\tilde{G}}$  where  $p_\mu$  is a momentum of the gravitino. In this case the helicity  $\pm \frac{1}{2}$  component of the gravitino field can be written as:

$$\tilde{\Psi}_\mu \sim \sqrt{\frac{2}{3}} \frac{1}{m_{\tilde{G}}} \partial_\mu \Psi \quad (9)$$

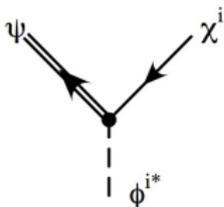
# Goldstino Approximation

$\Psi$  represents the spin  $\frac{1}{2}$  fermionic field which can be interpreted as the goldstino. Substituting [9] into gravitino interaction lagrangian, one can obtain the effective interaction lagrangian for the goldstino components  $\Psi$ .

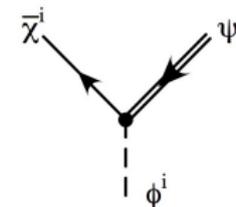
We would like to explore in which case the Goldstino is a good approximation to the Gravitino.

# Goldstino Approximation

From the Feynman diagram we can obtain the amplitudes for the stop decay in the case that we have a Goldstino in the final state.



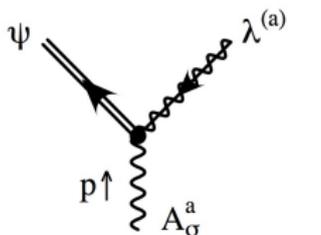
$$\frac{m_\chi^2 - m_\phi^2}{2\sqrt{3}Mm_{3/2}} (1 + \gamma_5)$$



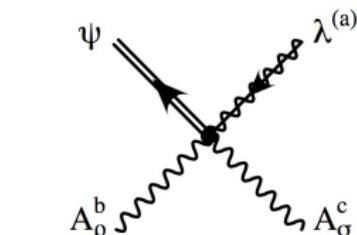
$$\frac{m_\chi^2 - m_\phi^2}{2\sqrt{3}Mm_{3/2}} (1 - \gamma_5)$$

# Goldstino Approximation

Because we are considering the same decay  $\tilde{t} \rightarrow b + W + \Psi$ , we will have to compute 21 amplitudes. Although they are far simpler, compare with the gravitino case. 😊



$$\frac{-im_\lambda}{2\sqrt{6}Mm_{3/2}} [\gamma_\rho, \gamma_\sigma] p^\rho$$



$$\frac{-m_\lambda}{2\sqrt{6}Mm_{3/2}} g f^{abc} [\gamma_\rho, \gamma_\sigma]$$

## Numerical Results

It is more illustrative get some graphs from all these large analytical results.

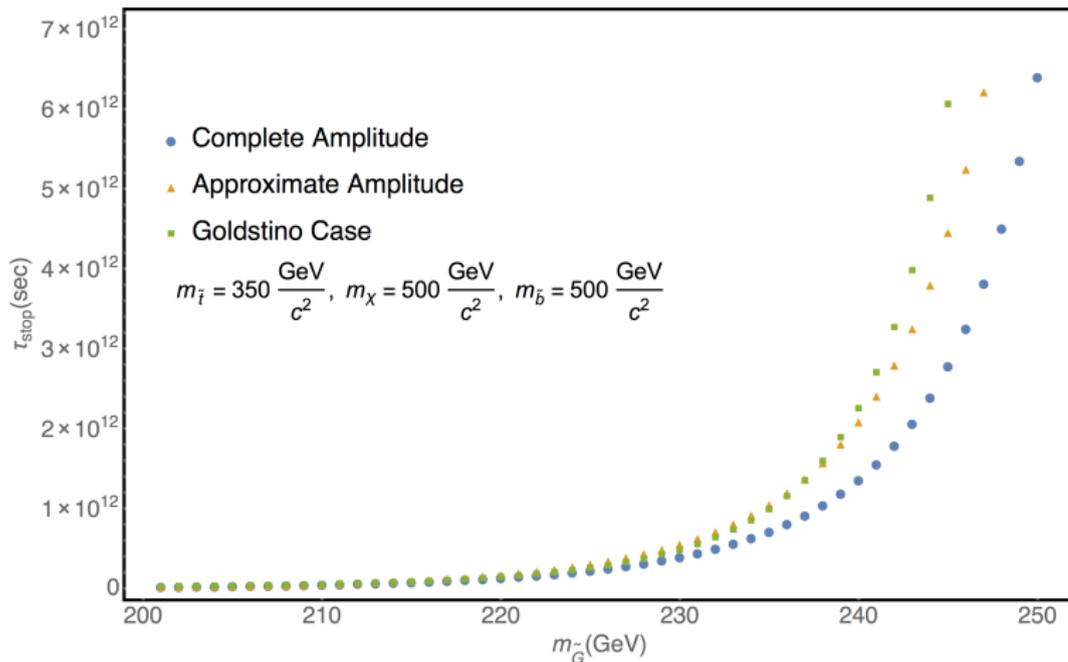
We need to integrate the decay width

$$\frac{d\Gamma}{dxdy} = \frac{m_{\tilde{t}_1}^2}{256\pi^3} |\overline{\mathcal{M}}|^2$$

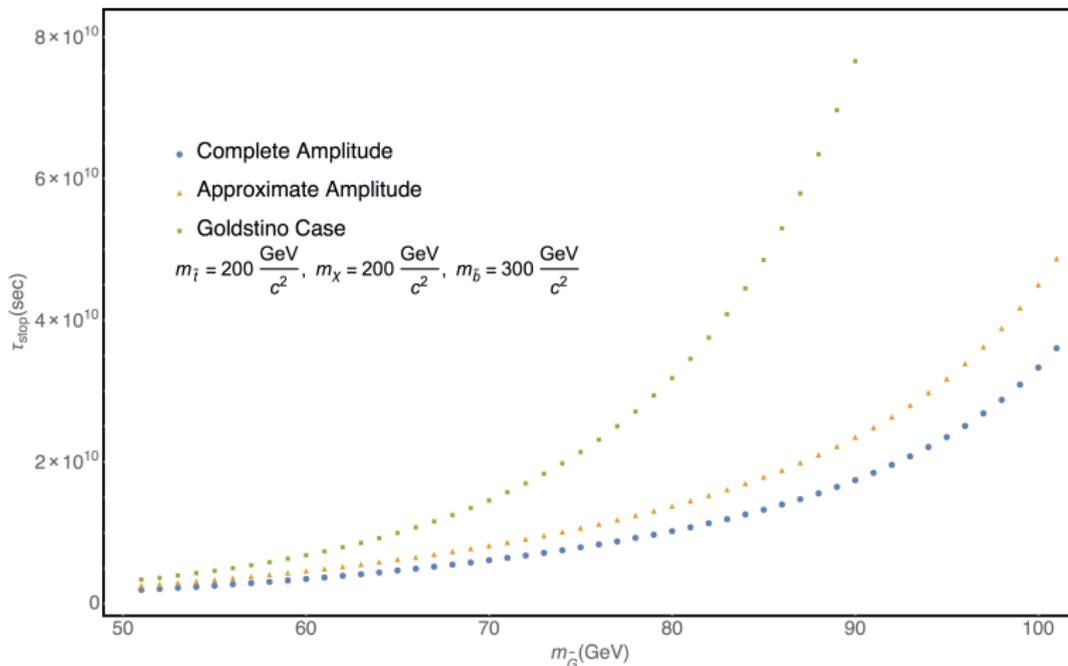
the integration limits are:  $2\mu_G < x < 1 + \mu_G - \mu_W$  and  $y_- < y < y_+$ , where

$$y_{\pm} = \frac{1 + \mu_G + \mu_W - x}{2(1 + \mu_G - x)} [(2 - x) \pm (x - 4\mu_G)^{1/2}]$$

# Numerical Results



# Numerical Results



## Conclusions

- Amplitude approximations in previous work is not so bad, but now we have the complete result, that refine the range of the stop's life-time.
- Gravitino LSP is an interesting and viable scenario,
- Also possible that stop may be the NLSP,
- A distinctive signature of such scenario is the large life-time of the stop  $\simeq 10^8 - 10^{12}$  secs., which has interesting implications for nucleosynthesis and collider physics.
- Goldstino is good approximation in the low gravitino mass limit.

# THANKS..

## Why is SUSY attractive?

- Offers the possibility to stabilize the Higgs mass and induce radiatively
- Improves Unification and o.k. with proton decay,
- Favors a light Higgs boson, in agreement with precision analysis,
- New sources of flavor and CP violation may help to get
- R-parity  $\rightarrow$  Lightest SUSY particle is stable (LSP),
- LSP is a good **Dark matter** candidate.
- It could be the low limit energy of a fundamental theory of Quantum Gravity.

# The MSSM

The minimal extension of the Standard Model (SM) consistent with SUSY (MSSM), is based on:

- Gauge supermultiplets
  - SM Gauge Group  $\rightarrow$  gauge bosons (and gauginos),
- Chiral supermultiplets
  - 3 families of fermions (and sfermions),
  - Two Higgs doublets (and Higgsinos),
- Soft-breaking of SUSY,
  - gaugino and scalar masses,
  - bilinear and trilinear terms,
- R-parity distinguish SM and their superpartners  $\rightarrow$  LSP is stable and good DM candidate.

## The models (a): CMSSM

Models at TeV scale are derived from SUGRA models through RGE,

- CMSSM = Constrained Minimal Supersymmetric Standard Model.
- In the CMSSM one takes (at  $M_{pl}$ ):
  - Universal scalar masses ( $=\tilde{m}_0$ )
  - redUniversal gaugino masses ( $=\tilde{m}_{1/2}$ )
  - Universal trilinear terms ( $=A_0$ )
- Also  $\tan\beta = v_2/v_1$  and  $sgn(\mu)$ .
- Use RGE to get weak-scale parameters.

## The models (b): NUHM

- NUHM = Non-universal Higgs Masses Model.
- Same parameters as in CMSSM, except that the Higgs masses  $m_{1,2}$  are not equal to  $m_0$ .
- We can trade  $m_{1,2}$  with  $\mu$  and  $m_A$ , as our free parameters through the electroweak symmetry breaking condition.
- Thus the NUHM parameters are:  $m_0, m_{1/2}, A_0, \tan \beta = v_2/v_1, \mu$  and  $m_A$ .

# NLSP scenarios and Constraints

Several constraints are required for consistency of this scenario. SUSY parameters must satisfy:

- LHC limits on Higgs mass ( $m_h = 125$  GeV),
- Current bounds on  $b \rightarrow s + \gamma$ ,
- Correct induced radiative EWSB,
- LHC limits on stable charged particles, e.g.  $m_{\tilde{\tau}} \geq 200$  GeV.

# Stop mass matrix

$$\widetilde{\mathcal{M}}_t^2 = \begin{pmatrix} M_{LL}^2 & M_{LR}^2 \\ M_{LR}^{2\dagger} & M_{RR}^2 \end{pmatrix}, \quad (10)$$

where

$$\begin{aligned} M_{LL}^2 &= M_{\tilde{t}_L}^2 + m_t^2 + \frac{1}{6} \cos 2\beta (4m_w^2 - m_z^2), \\ M_{RR}^2 &= M_{\tilde{t}_R}^2 + m_t^2 + \frac{2}{3} \cos 2\beta \sin^2 \theta_w m_z^2, \\ M_{LR}^2 &= A_t v \sin \beta / \sqrt{2} - m_t \mu \cot \beta, \end{aligned} \quad (11)$$

1

<sup>1</sup>J. L. Diaz-Cruz, J. R. Ellis, K. A. Olive and Y. Santoso, "On the feasibility of a stop NLSP in gravitino dark matter scenarios," JHEP **0705**, 003 (2007) [arXiv:hp-ph/0701229].

# Stop mass matrix

The stop mass eigenvalues are given by:

$$m_{\tilde{t}_1}^2 = m_t^2 + \frac{1}{2}(M_{\tilde{t}_L}^2 + M_{\tilde{t}_R}^2) + \frac{1}{4}m_Z^2 \cos 2\beta - \frac{\Delta}{2} \quad (12)$$

$$m_{\tilde{t}_2}^2 = m_t^2 + \frac{1}{2}(M_{\tilde{t}_L}^2 + M_{\tilde{t}_R}^2) + \frac{1}{4}m_Z^2 \cos 2\beta + \frac{\Delta}{2} \quad (13)$$

where:

$$\Delta^2 = M_{\tilde{t}_L}^2 - M_{\tilde{t}_R}^2 + \frac{1}{6} \cos 2\beta (8m_W^2 - 5m_Z^2) + 4m_t(A_t - \mu \cot \beta).$$

The mixing angle to go from the weak  $(\tilde{t}_L, \tilde{t}_R)$  to the mass eigenstates  $(\tilde{t}_1, \tilde{t}_2)$ , is given by:  $\tan \theta_{\tilde{t}} = (m_{\tilde{t}_1}^2 - M_{LL}^2)/M_{LR}^2$ .

## A.1 Relevant interactions

Stop-top-gravitino interactions:

$$\tilde{t}_1^*(p)\bar{\Psi}_\mu t \rightarrow -\frac{1}{\sqrt{2}M}\gamma^\nu\gamma^\mu p_\nu(\sin\theta_{\tilde{t}}P_R + \cos\theta_{\tilde{t}}P_L) \quad (14)$$

and similar expression holds for the Bottom-sbottom-gravitino interaction.

Chargino-W-gravitino:

$$\chi_i^-\bar{\Psi}_\mu W^-(k) \rightarrow -\frac{m_W}{M}\gamma^\nu\gamma^\mu(A_{Li}P_R + A_{Ri}P_L) \quad (15)$$

where:  $A_{Li} = V_{i2} \sin \beta$ ,  $A_{Ri} = V_{i2} \cos \beta$ , and  $U, V$  are the matrices that diagonalize the charginos.