# Collider physics II: Jets

## Two aspects of new developments

- Better QCD jet.
  - Smarter jet algorithm.
  - Noise suppression with jet grooming.
- Jet substructure.
  - Boosted top.
  - Higgs.

#### Boston Jet Workshop:

http://jets.physics.harvard.edu/workshop/Main.html

Northwest Terascale workshop

http://www.physics.uoregon.edu/~soper/Jets2011/talks.html

Boost 2011, May, 23-27, Princeton.

http://boost2011.org

Boost 2012, July, 23-27, Valencia, Spain.

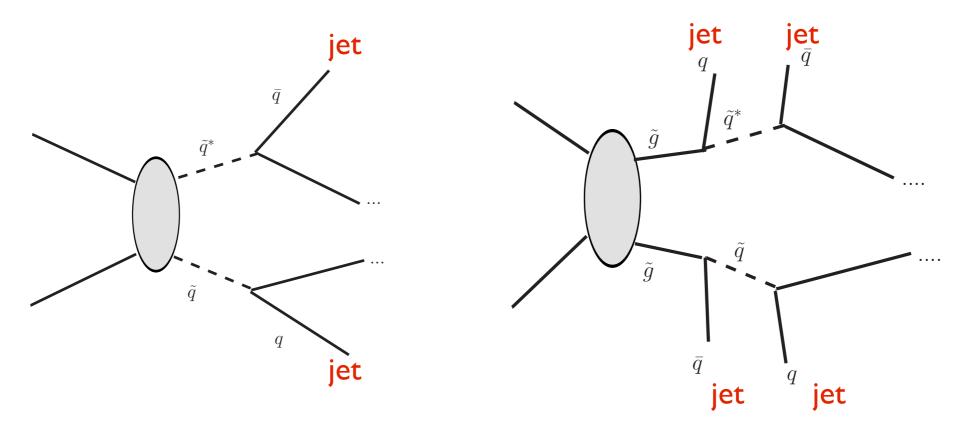
http://ific.uv.es/boost2012/

## Want to play with it?

- Parton level Signal and background:
  - Madgraph, Alpgen, ...
- ME+PS matching, UE, Pileup:
  - Pythia, Herwig, Sherpa, ...
- Some detector effect, in particular, granularity
   0.1x0.1
  - PGS, Delphes, "by hand".
- Jet tools.
  - Fastjet. <a href="http://www.lpthe.jussieu.fr/~salam/fastjet/">http://www.lpthe.jussieu.fr/~salam/fastjet/</a>
  - SpartyJet
    <a href="http://projects.hepforge.org/spartyjet/">http://projects.hepforge.org/spartyjet/</a>

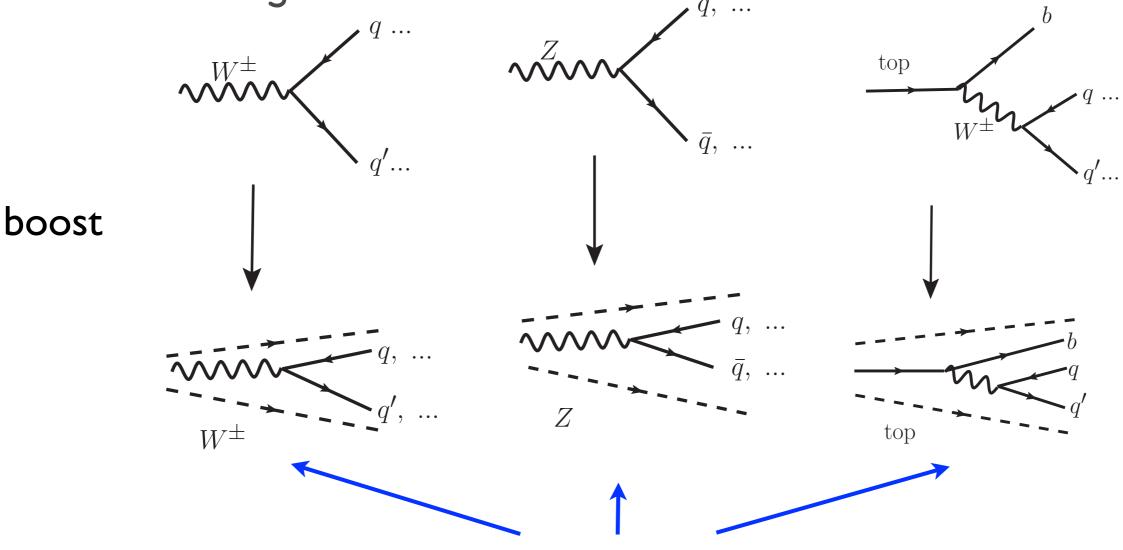
## The importance of jets:

- "Everywhere" at hadron colliders. p p, or,  $p\bar{p}$  initial state.
- Present in (almost) all new physics signals.
  - Many of them only have hadronic channels.



#### Jet look likes

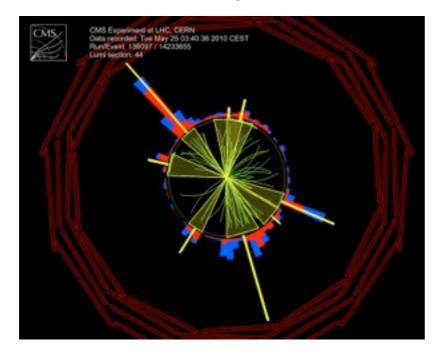
- When produced at TeV-scale energies, they have a large boost.

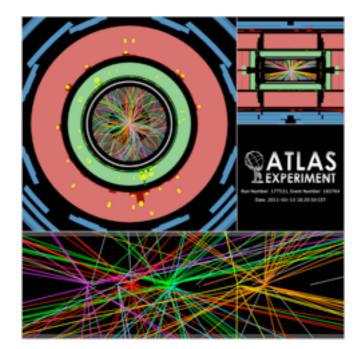


Jets with substructure.

Challenge: distinguishing them from QCD jets (q and g).

## Need new jet tools for the LHC.





- More energetic, bigger, jet at the LHC.

▶ LHC jet: 50 GeV - several TeV

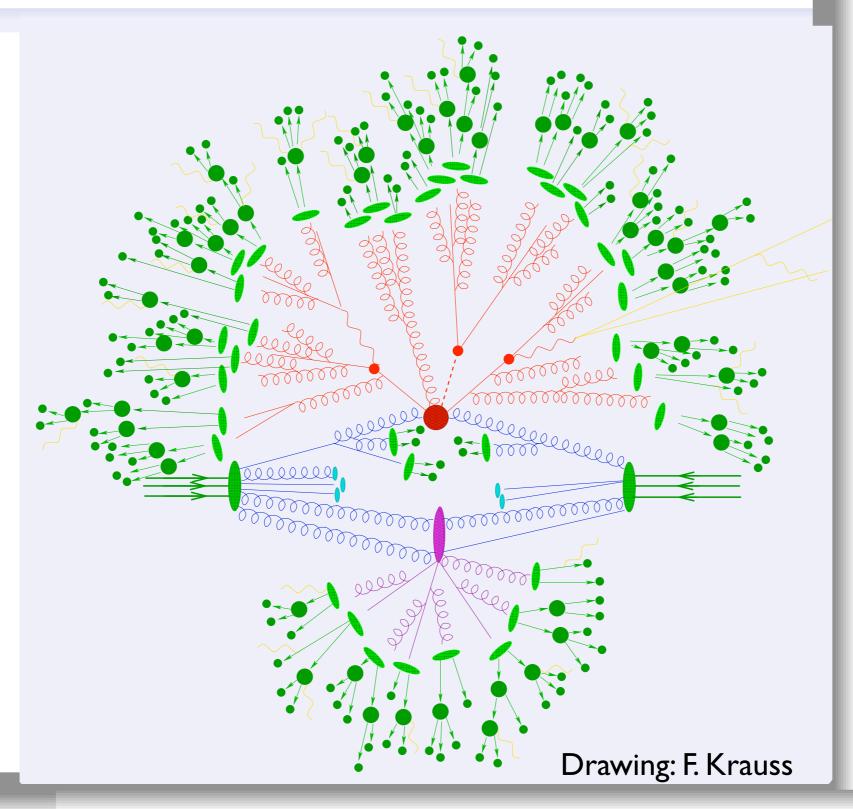
▶ Tevatron jet: 50 - 100s GeV

Much higher "noise" level at the LHC.

**LHC:** I0-100 GeV / rapidity

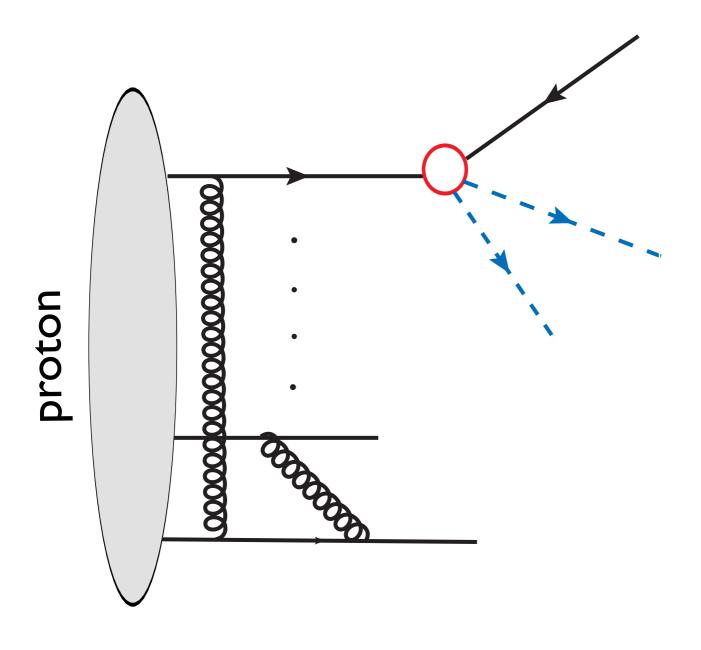
**Tevatron:** 2-10 GeV / rapidity

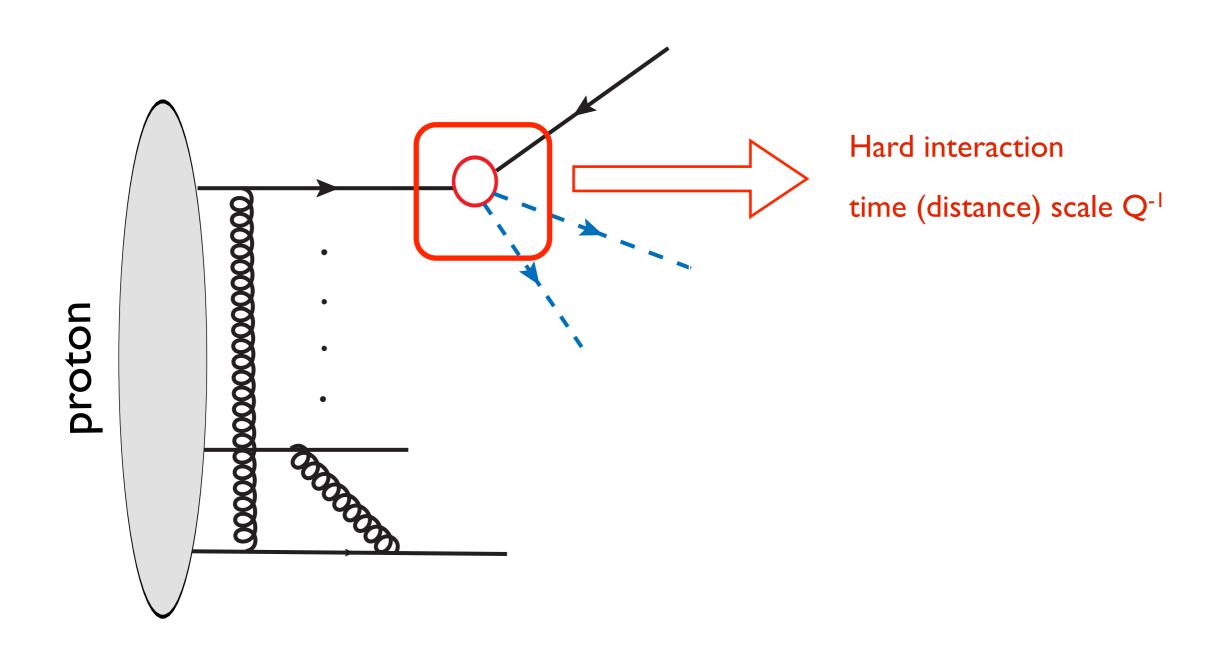
## adron collision

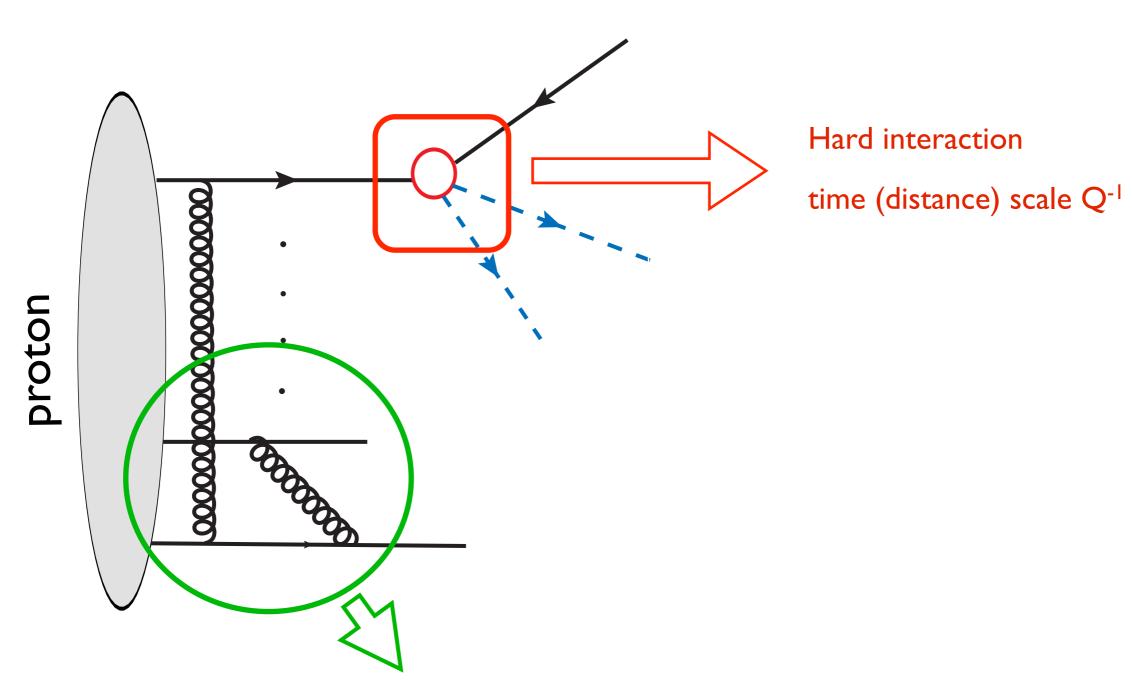


## Why can we calculate at all?

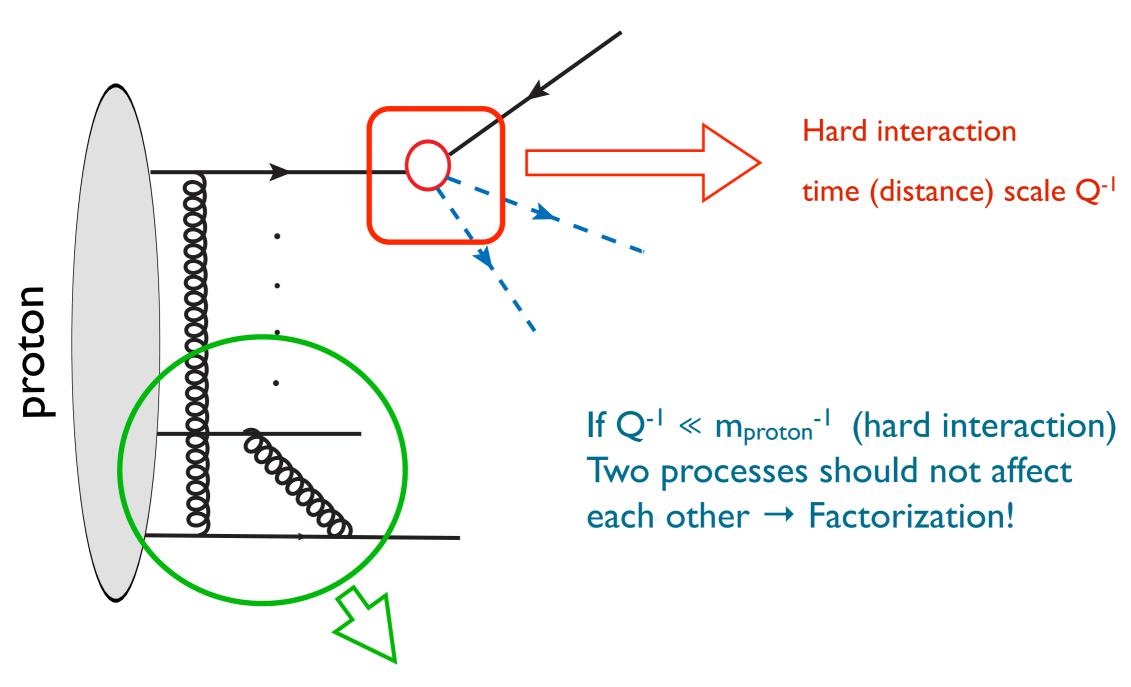
- Perturbatively, we can only calculate with quark and gluon in hard collisions.
- Factorization.
- IRC safety, need proper choice of observable.
  - Soft or collinear radiation should not be able to induce "large" changes in the observable.
  - Description observables.



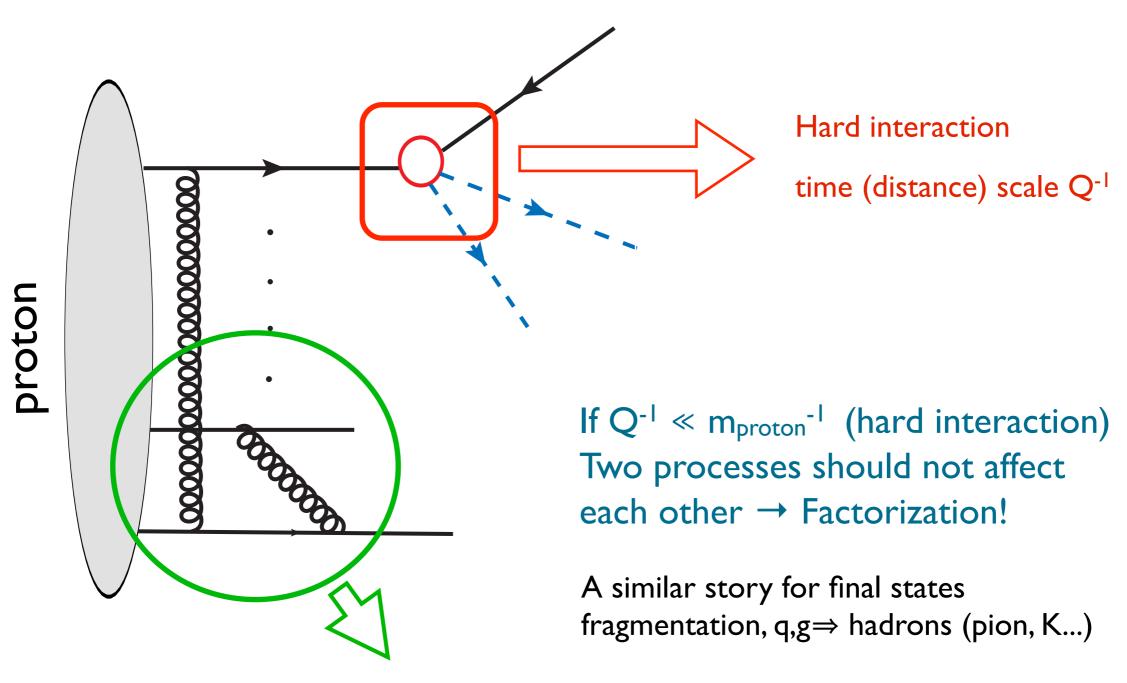




"talking" to the rest of the proton time(distance) scale m<sub>proton</sub>-I



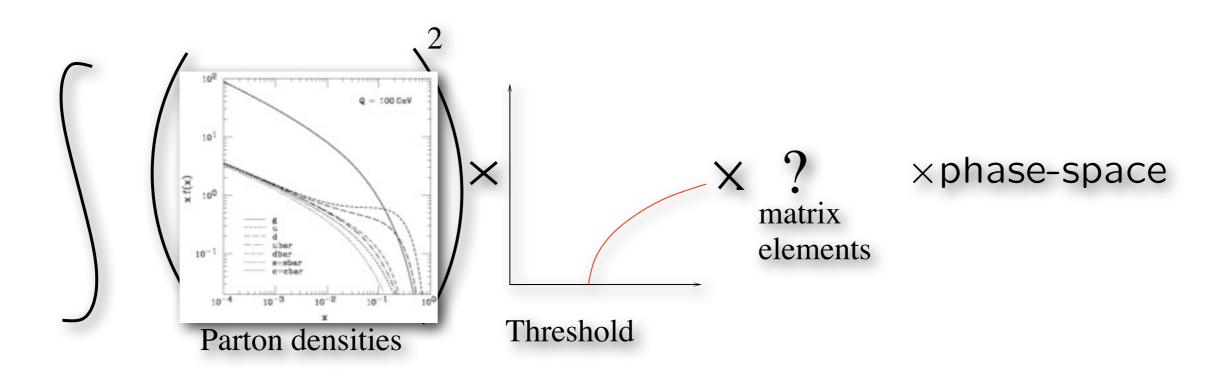
"talking" to the rest of the proton time(distance) scale m<sub>proton</sub>-I



"talking" to the rest of the proton time(distance) scale m<sub>proton</sub>-I

#### Factorization

- Schematics of production at hadron colliders.

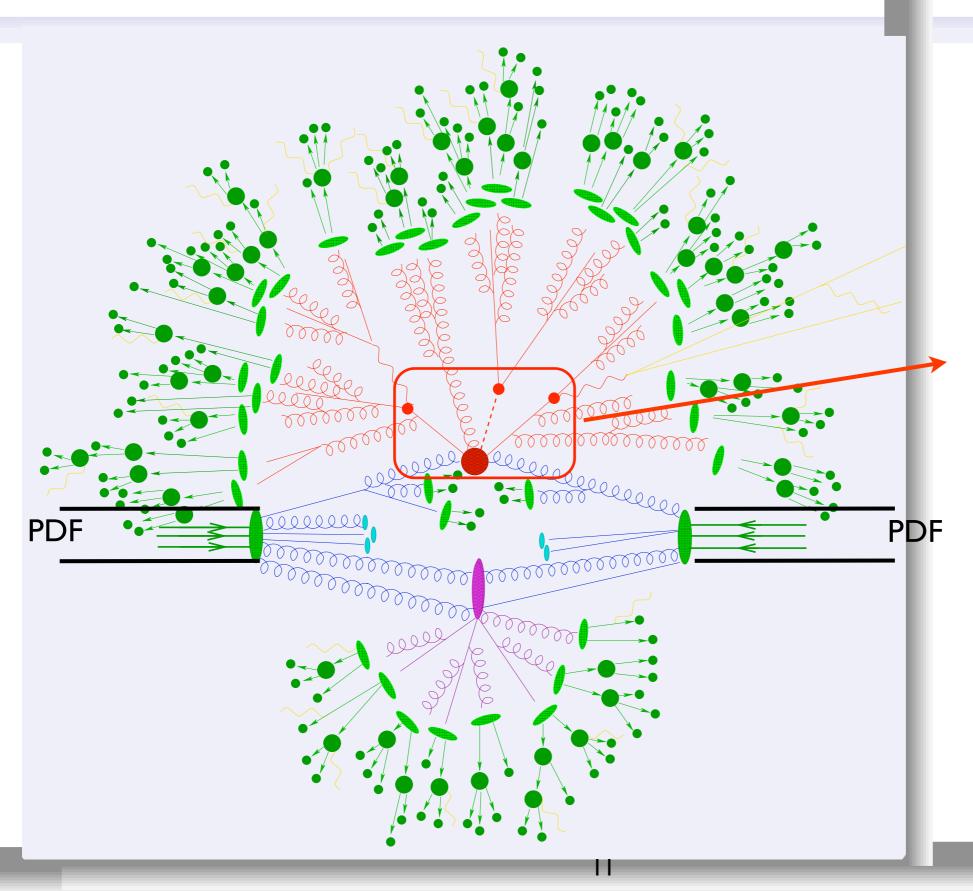


$$a+b\rightarrow ...$$

$$\sigma = \sum_{a,b} \int dx_1 dx_2 f_a(x_1) f_b(x_2) \hat{\sigma}_{\mathbf{x}}$$

Partonic cross section

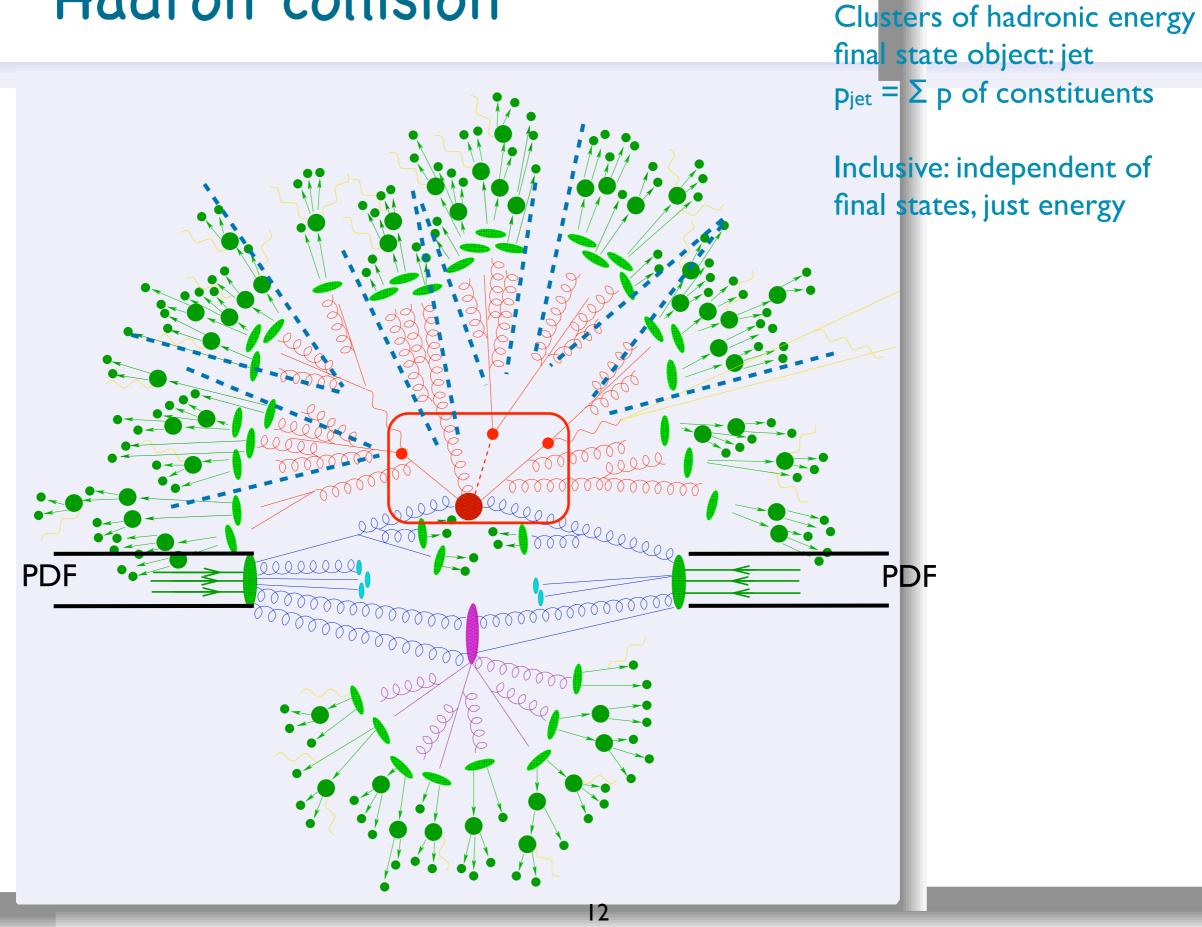
## Hadron collision.



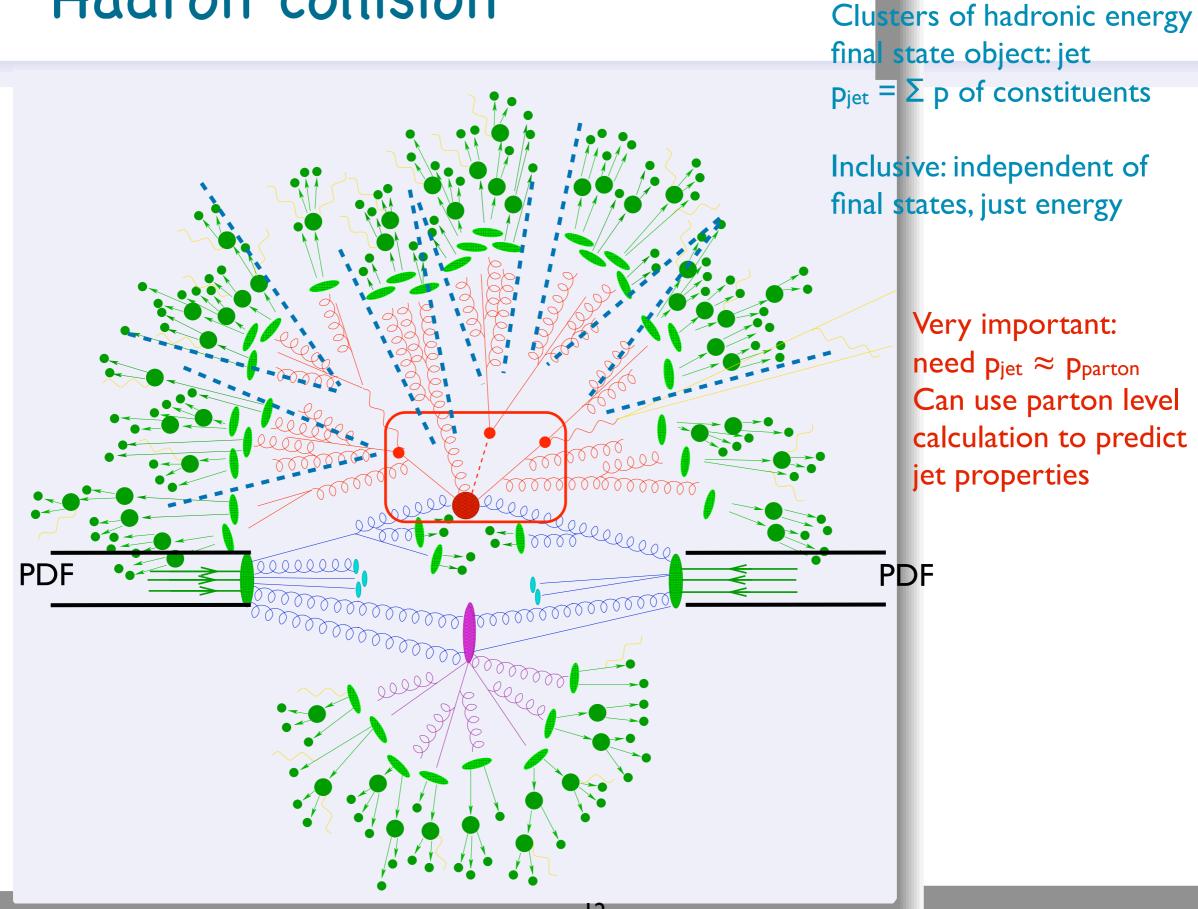
Hard interaction, gg⇒ g h t tbar

⇒h t tbar decay

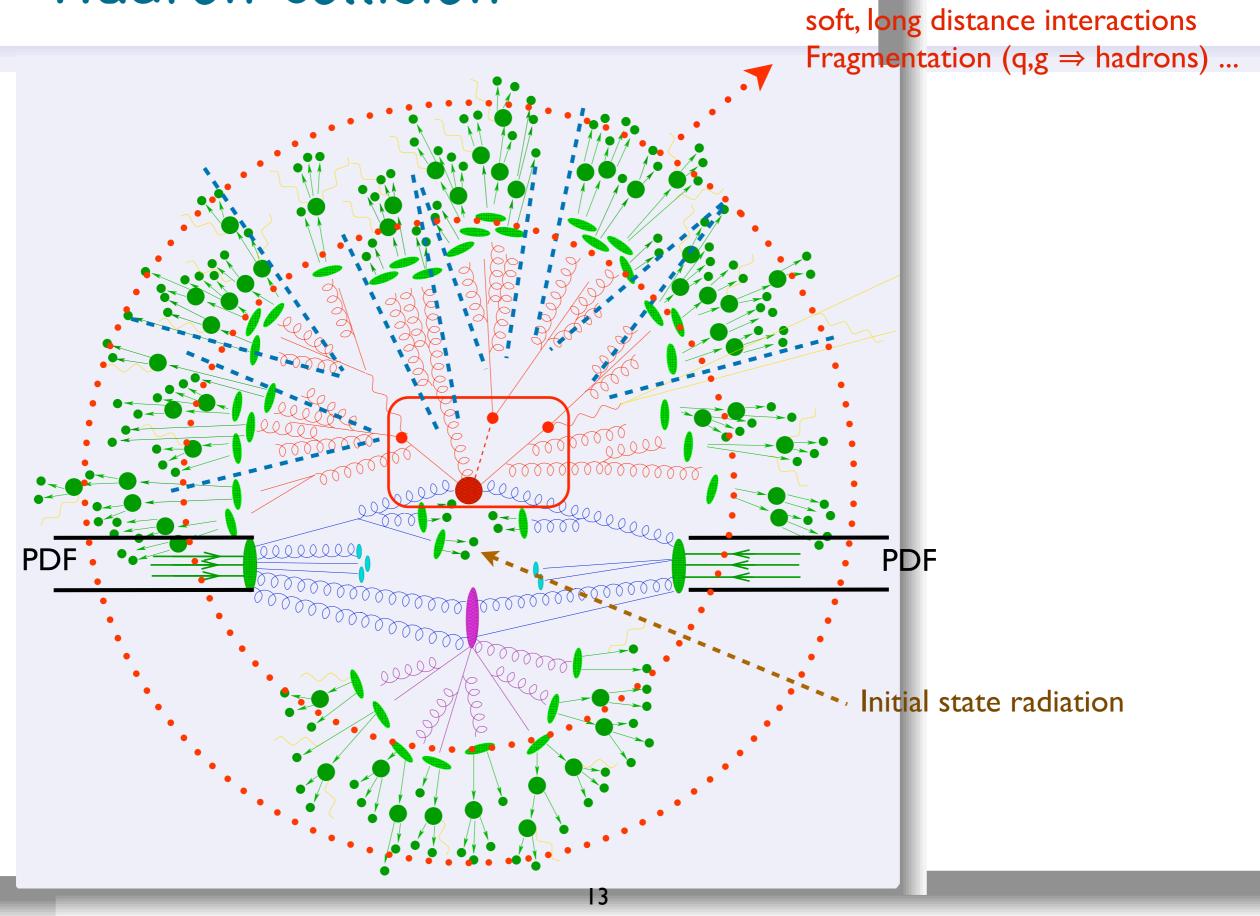
### Hadron collision



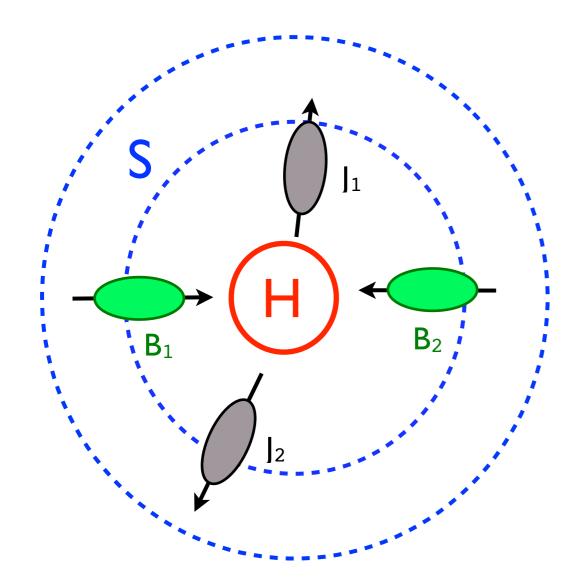
#### Hadron collision



## Hadron collision



#### Factorization

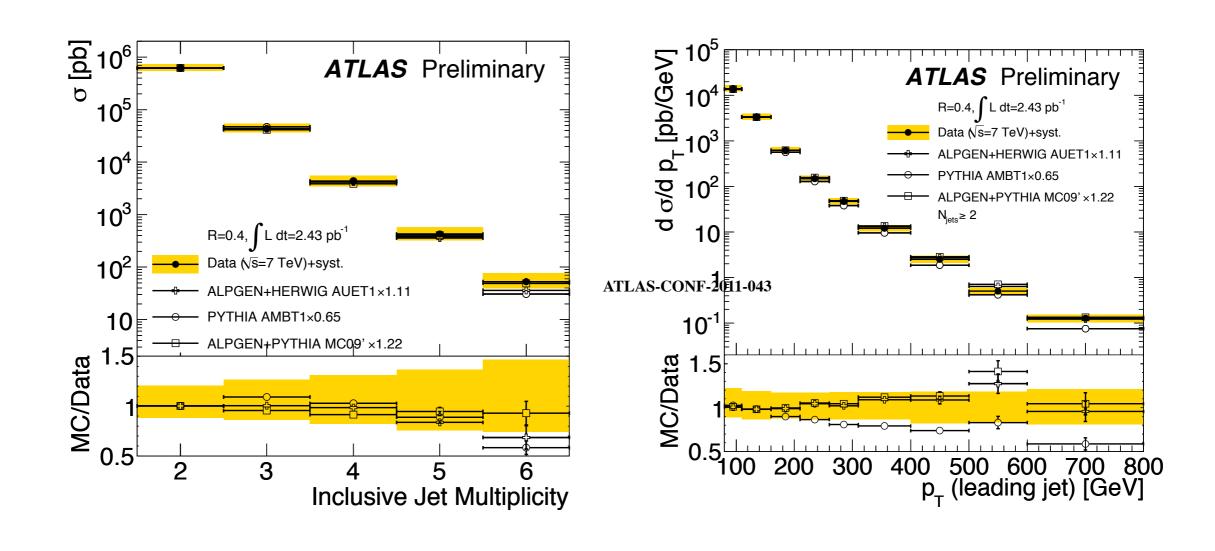


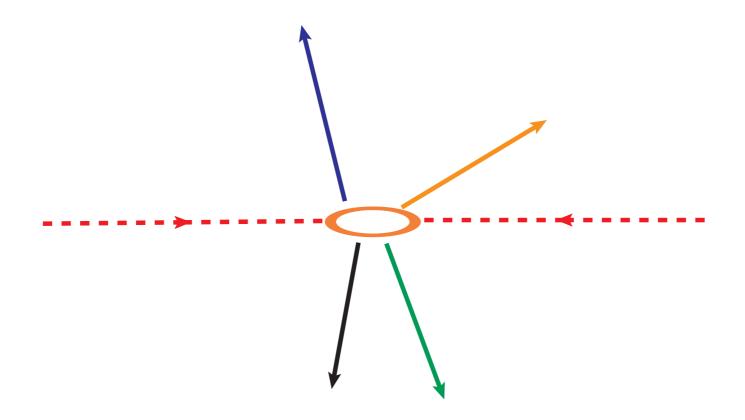
$$\sigma = B_1 \otimes B_2 \otimes H \otimes J_1 \otimes J_2 \otimes S$$

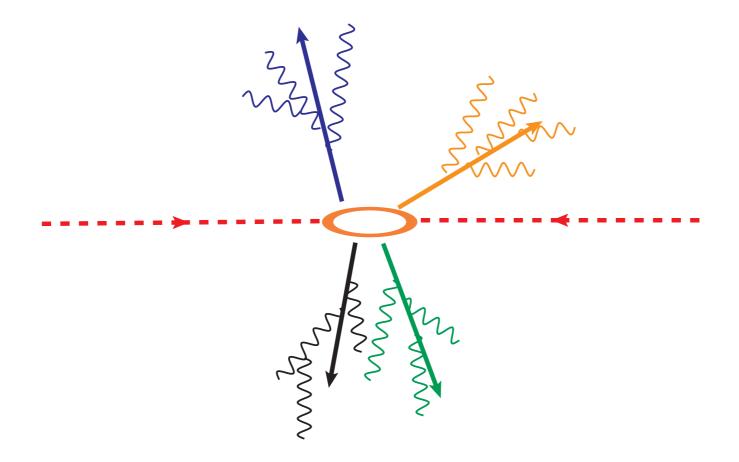
$$B_1 = dx_1 f(x_1), B_2 = dx_2 f(x_2).$$
  
 $\hat{\sigma} = H \otimes J_1 \otimes J_2 \otimes S$ 

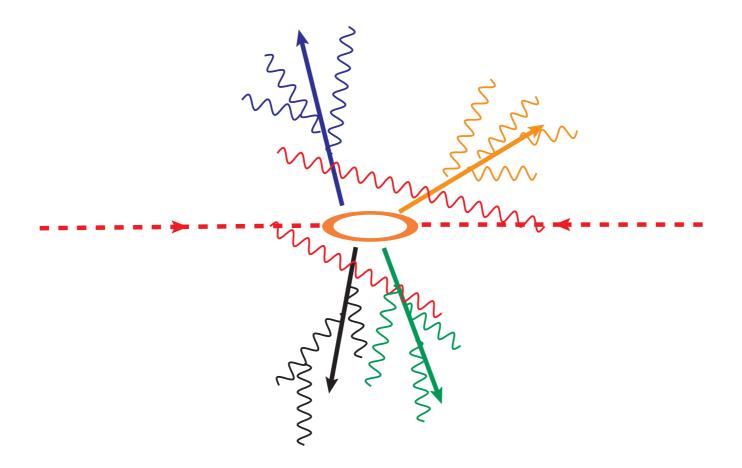
#### Well tested.

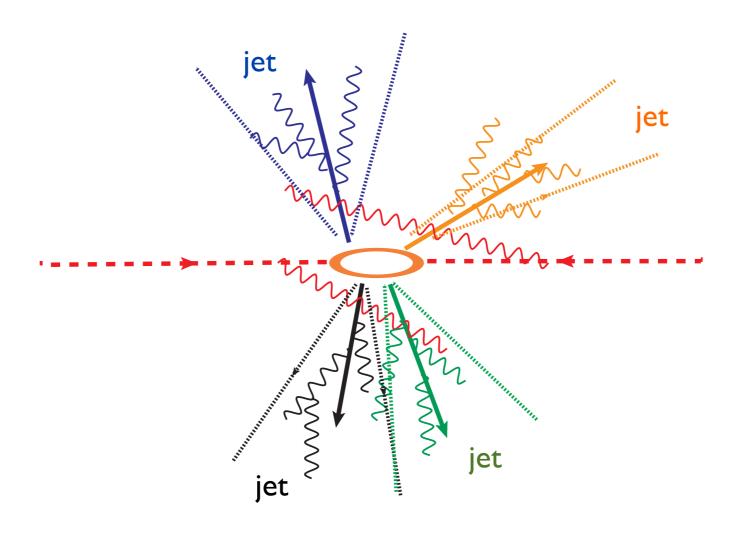
#### ATLAS-CONF-2011-043, 7 TeV, 2.43 pb<sup>-1</sup>



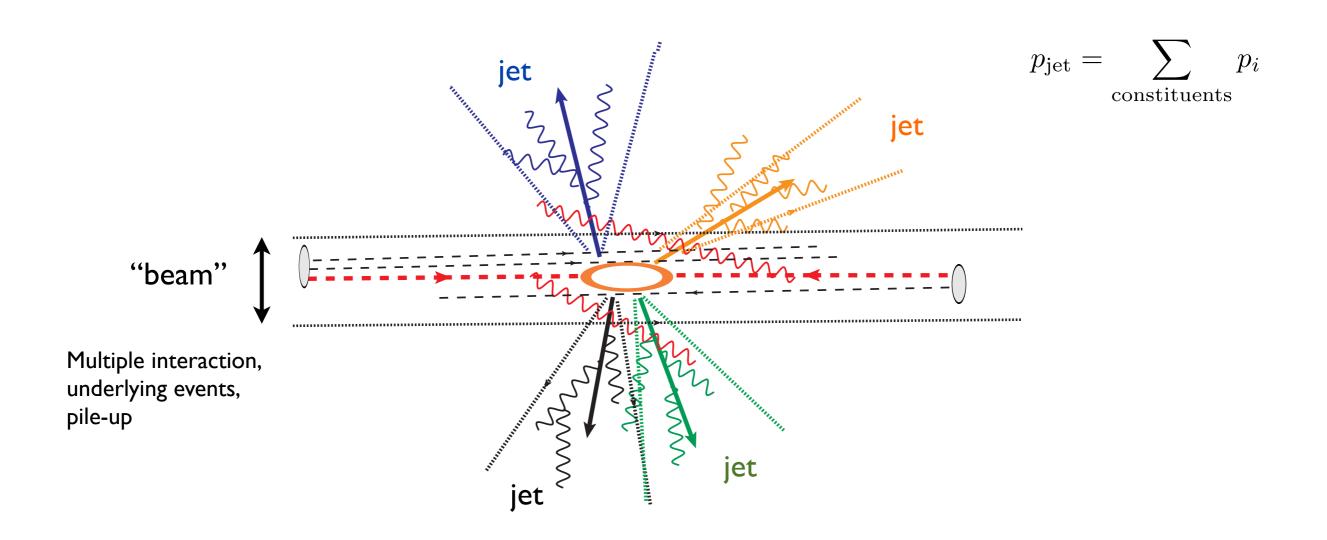


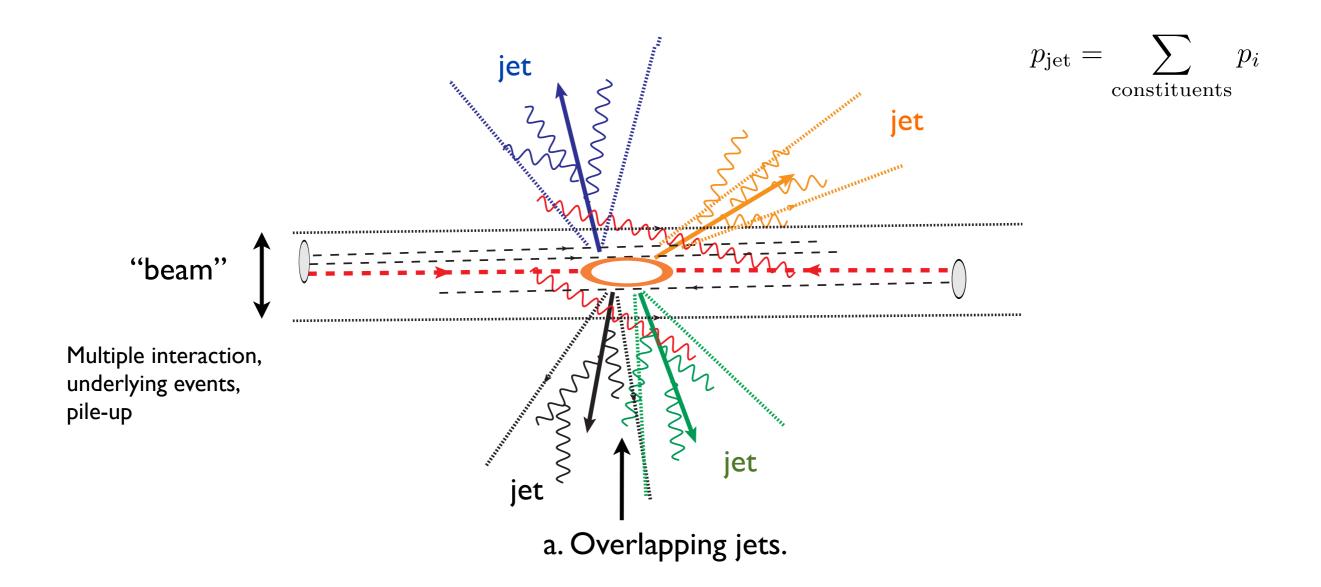


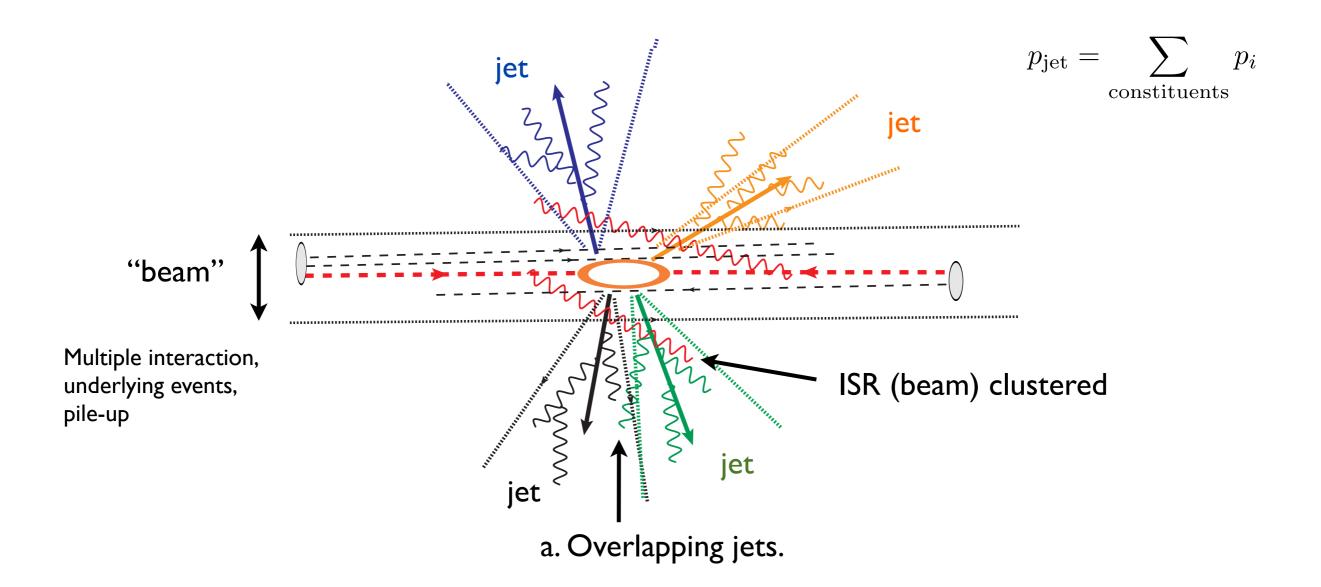


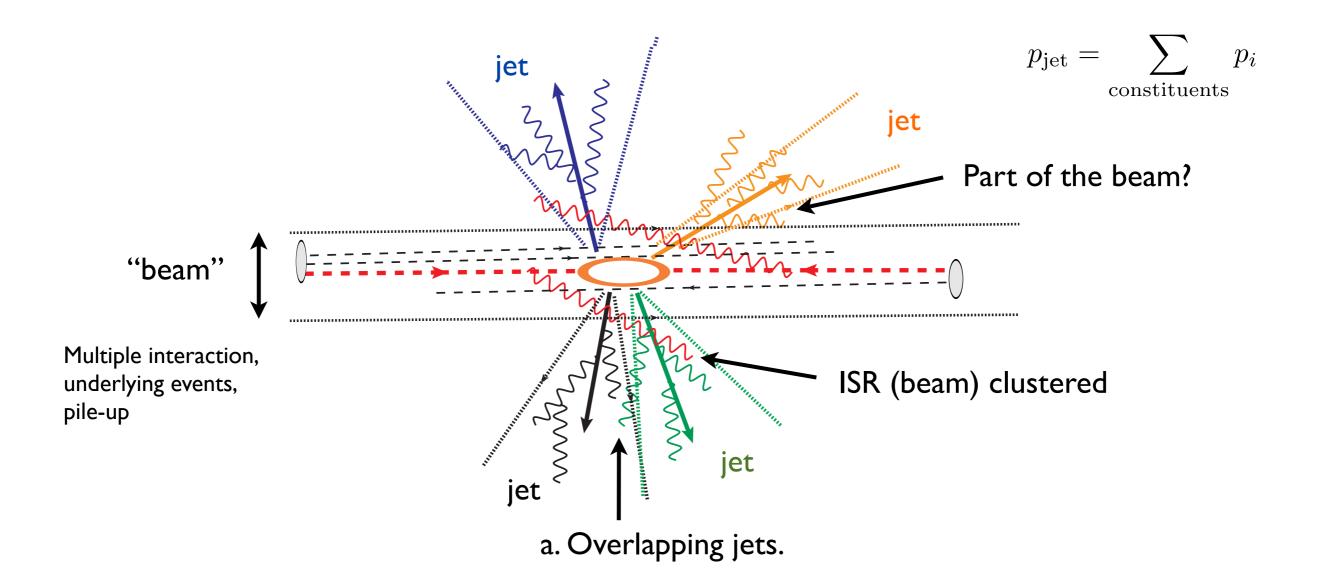


$$p_{\rm jet} = \sum_{\rm constituents} p_i$$

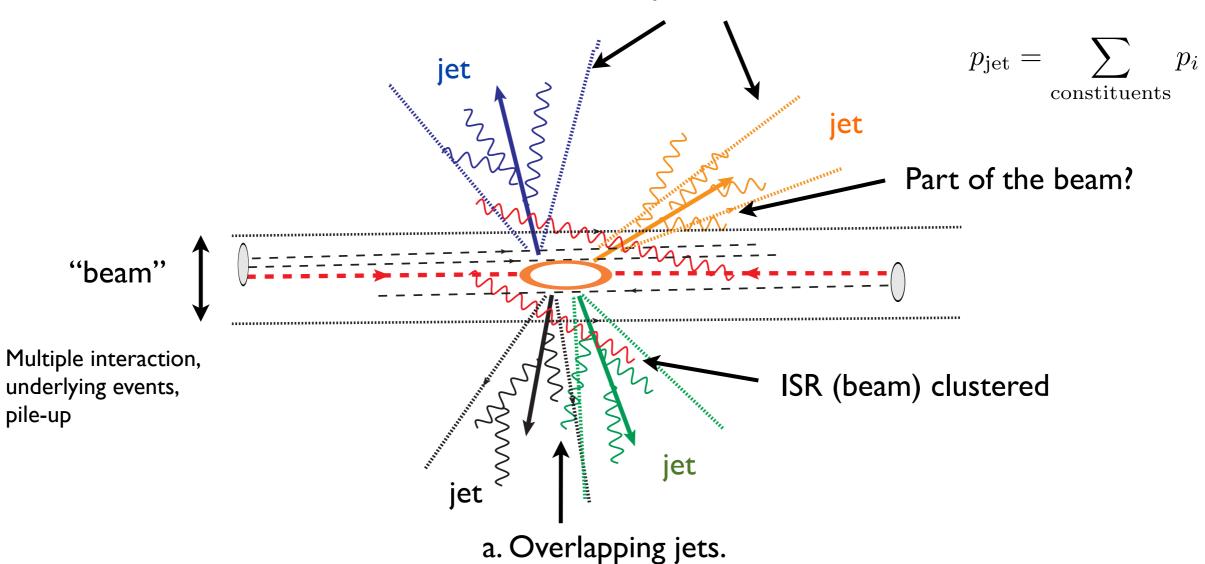




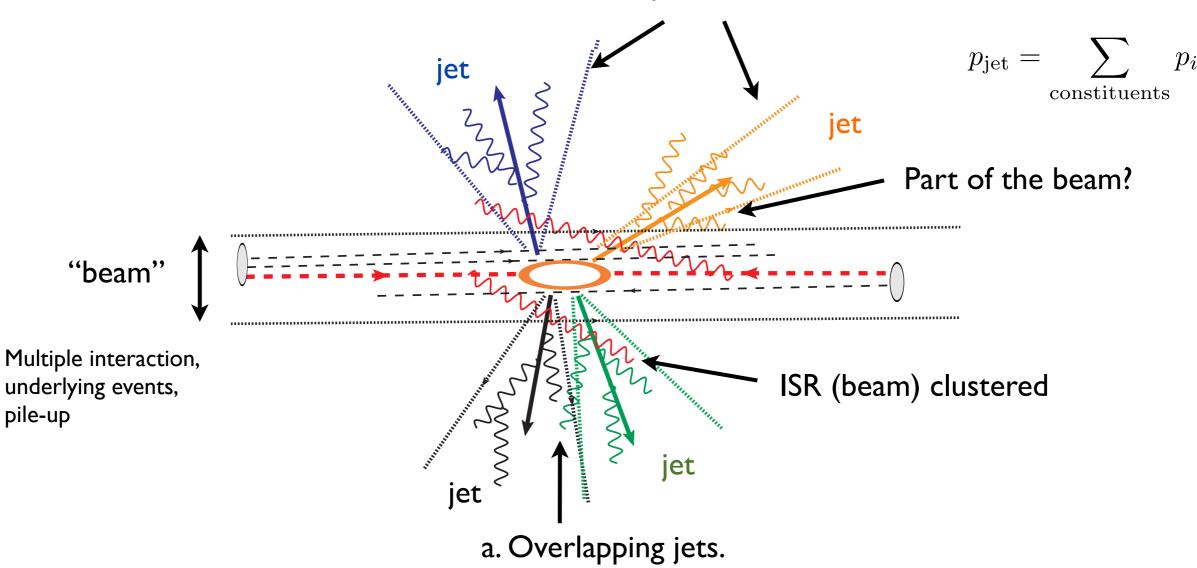








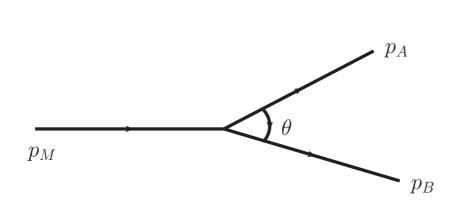
Proper choice of cone size?



- To best preserve  $p_{\rm jet} \simeq p_{\rm [initial\ parton]}$  we would like to:
  - Use "smart" jet shapes.
  - Reduce "noise".

What do jets look like?

## Parton splitting, collinear limit



Relevant kinematical variables

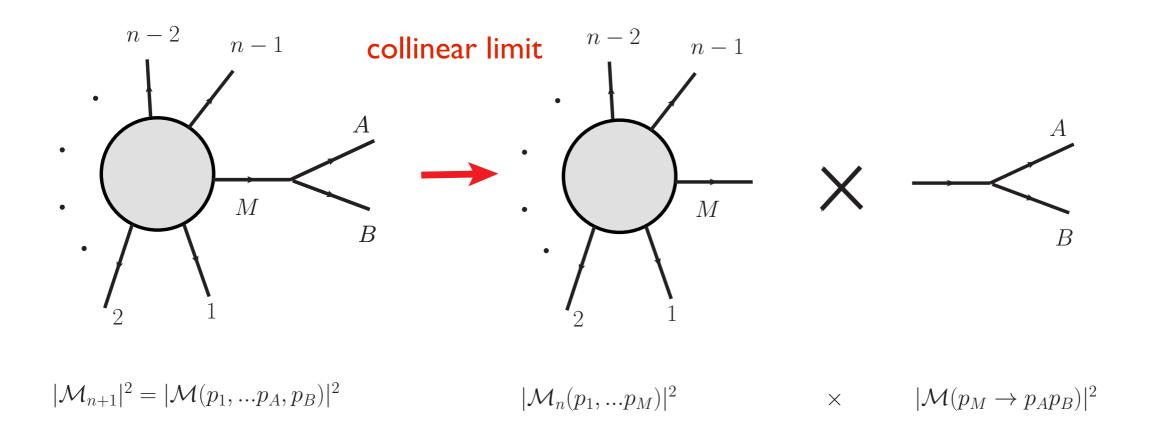
$$t = p_M^2 = (p_A + p_B)^2$$

$$z = \frac{E_A}{E_M}$$

$$\phi$$

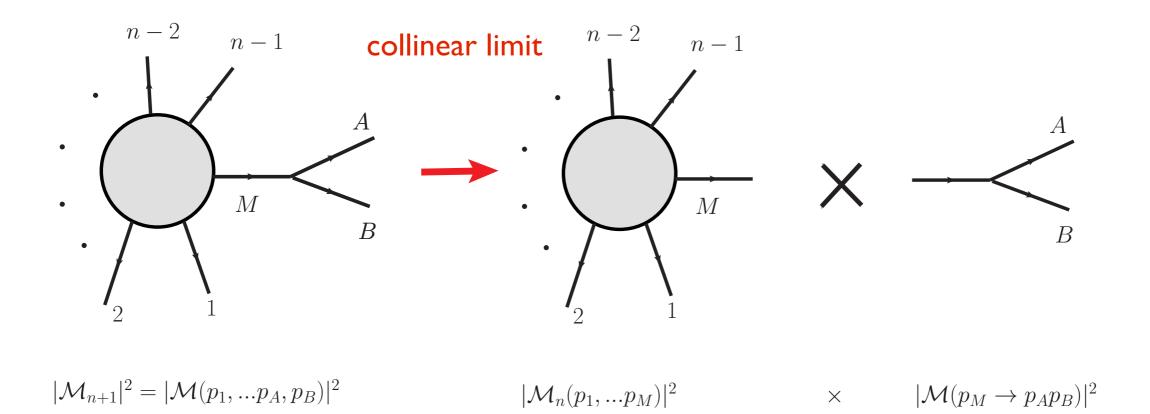
The main feature of radiation can be seen by considering the Collinear limit:  $\theta \Rightarrow 0$ ,  $t \ll E_M^2$ 

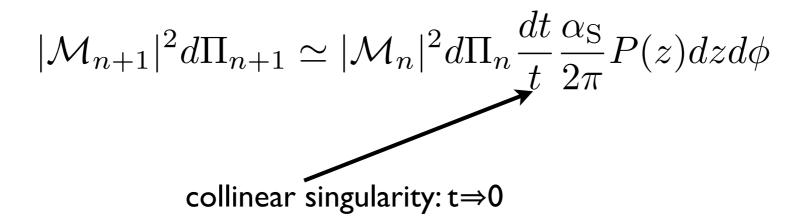
#### Collinear factorization



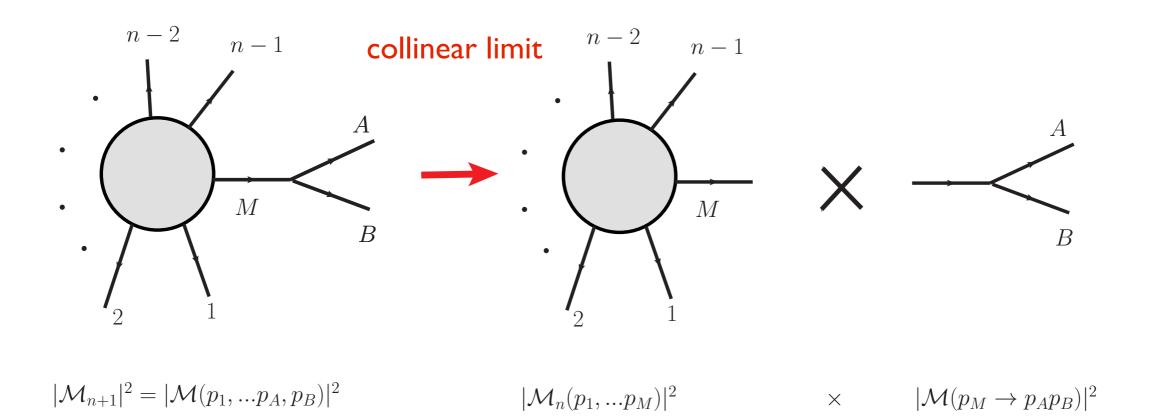
$$|\mathcal{M}_{n+1}|^2 d\Pi_{n+1} \simeq |\mathcal{M}_n|^2 d\Pi_n \frac{dt}{t} \frac{\alpha_S}{2\pi} P(z) dz d\phi$$

#### Collinear factorization





#### Collinear factorization



$$|\mathcal{M}_{n+1}|^2d\Pi_{n+1}\simeq |\mathcal{M}_n|^2d\Pi_n\frac{dt}{t}\frac{\alpha_{\mathrm{S}}}{2\pi}P(z)dzd\phi$$
 collinear singularity:  $\mathbf{t}\Rightarrow \mathbf{0}$  
$$P(z)\propto |\mathcal{M}(p_M\to p_Ap_B)|^2$$

Splitting function IR singularity: z⇒0, I

## Splitting function, IR singular as $z \Rightarrow 0$ , 1

$$P_{q \to qg}(z) = C_F \frac{1+z^2}{1-z},$$

$$P_{g \to gg}(z) = C_A \left[ \frac{1-z}{z} + \frac{z}{1-z} + z(1-z) \right]$$

$$P_{g \to q\bar{q}}(z) = T_R \left[ z^2 + (1-z)^2 \right],$$

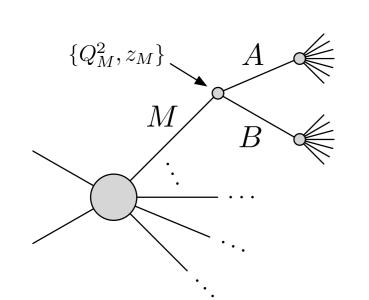
#### Combining with

$$|\mathcal{M}_{n+1}|^2 d\Pi_{n+1} \simeq |\mathcal{M}_n|^2 d\Pi_n \frac{dt}{t} \frac{\alpha_S}{2\pi} P(z) dz d\phi$$

Radiation wants to be collinear and soft

### Shape of a jet: parton shower

 From the initial parton, a jet is built up by many radiations (splittings).



$$d\sigma_{M\to A+B}^{\rm QCD} = \frac{dQ_M^2}{2\pi} \frac{1}{Q_M^2} dz \frac{\alpha(\mu)}{2\pi} P_{M\to AB}(z) \Delta(\mu_{\rm start}, \mu)$$

Prefers collinear radiation

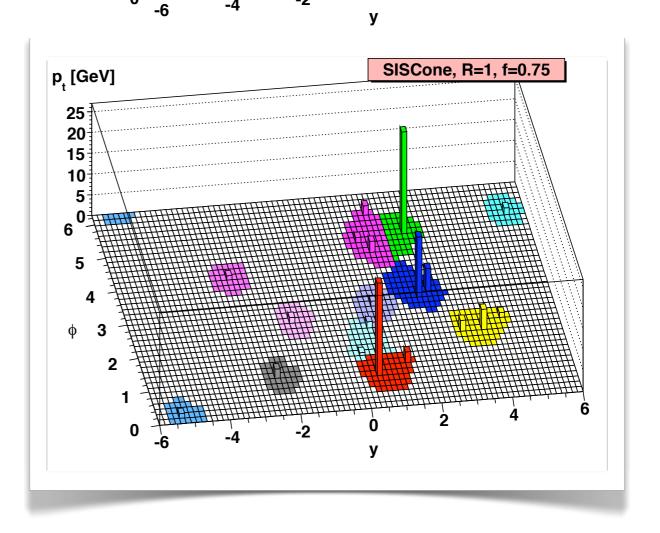
 $O_{M^2} = t$ 

 $P \sim (z)^{-1}$  prefers soft radiation

- QCD jet: a cluster of radiation
- a) relatively soft
- b) close to the direction of  $P_M$
- c) approximately symmetrical around P<sub>M</sub>

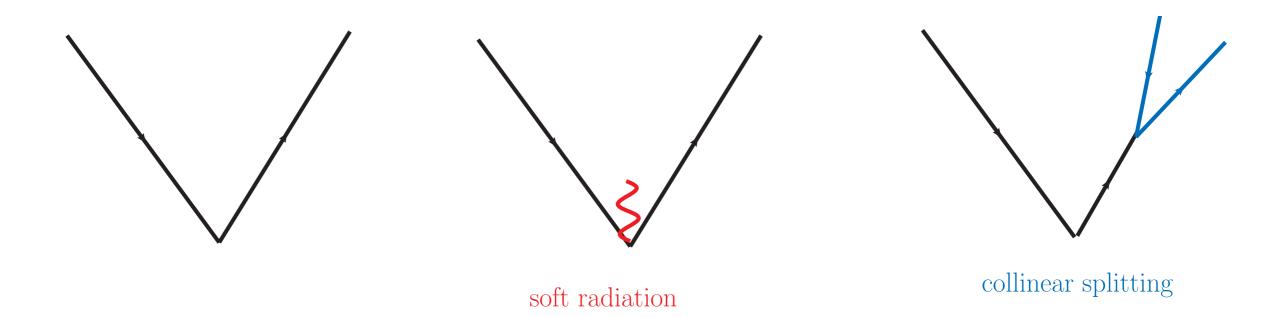
### Jet Algorithms.

A set of vectors {p<sub>i</sub>} Calorimeter towers...

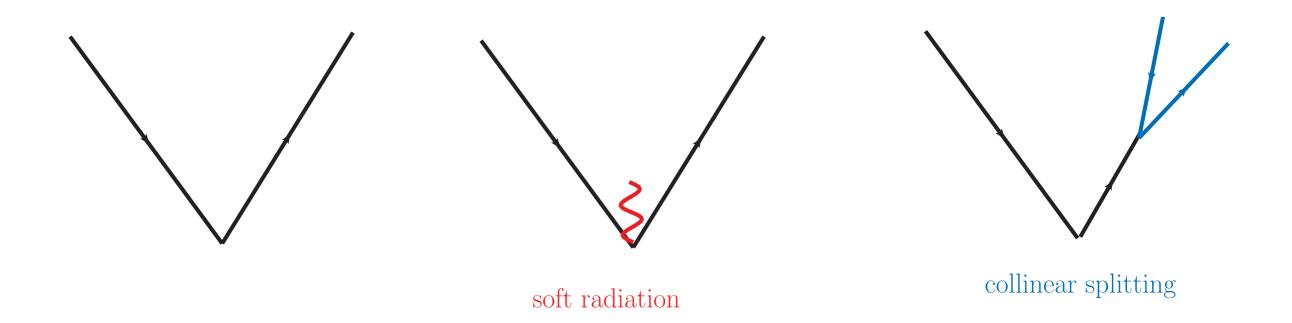


- Two type of decisions, based on two types criteria:
  - What to cluster.
  - When to stop cluster.
- Choice of the criteria determines the properties of the jets.

## First consideration: IRC safety

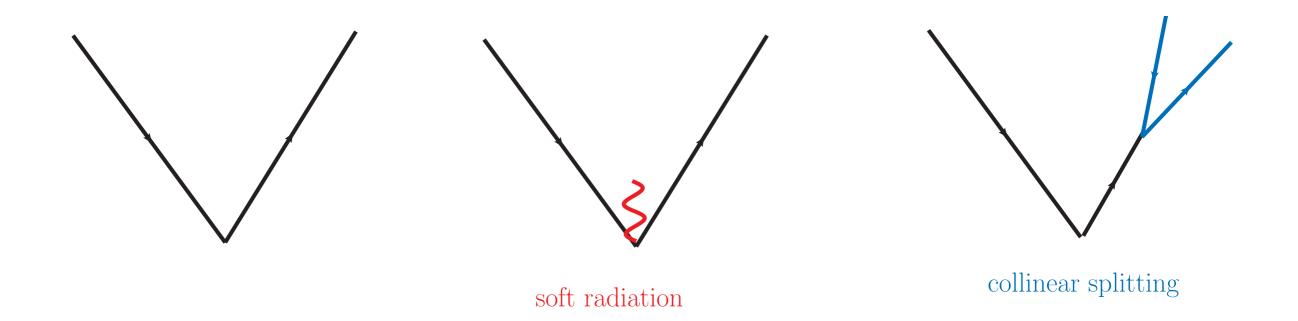


### First consideration: IRC safety



- Soft or collinear radiation should not be able to induce "large" changes in the observable.
- Otherwise we cannot compute and compare with experiments.

### First consideration: IRC safety



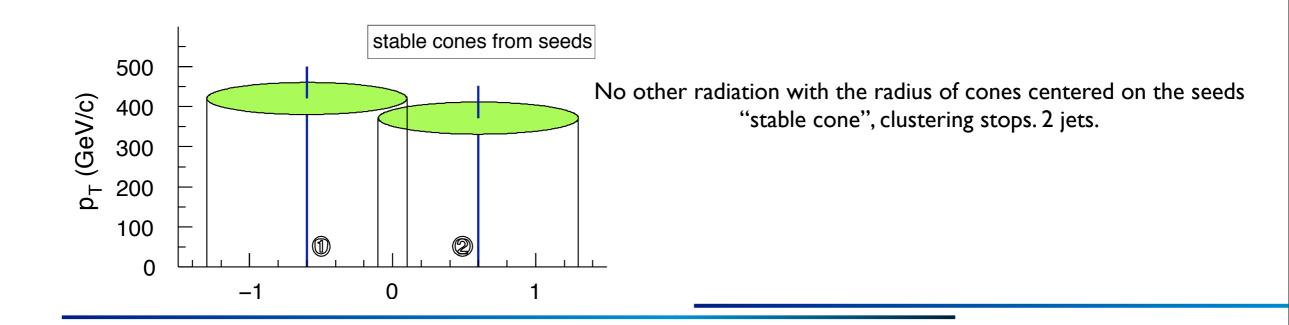
### All of these should be 2 jet events!

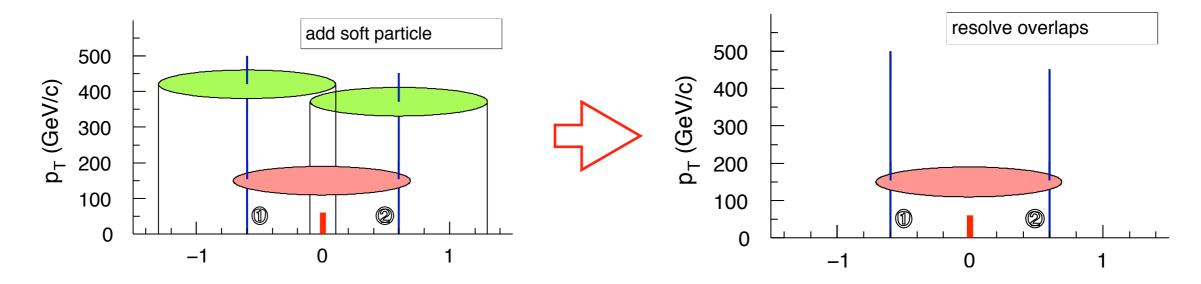
- Soft or collinear radiation should not be able to induce "large" changes in the observable.
- Otherwise we cannot compute and compare with experiments.

### Seeded cone

- Starting with a set of seeds (momenta which are "more likely" to be the centers of the jets).
- Draw a cone of certain size around each seed.
- Within each cone, add up all momenta. Use the new direct as the new seed.
- Iterate this process until we end up with stable cones.

### Seeded Cone, IR unsafe

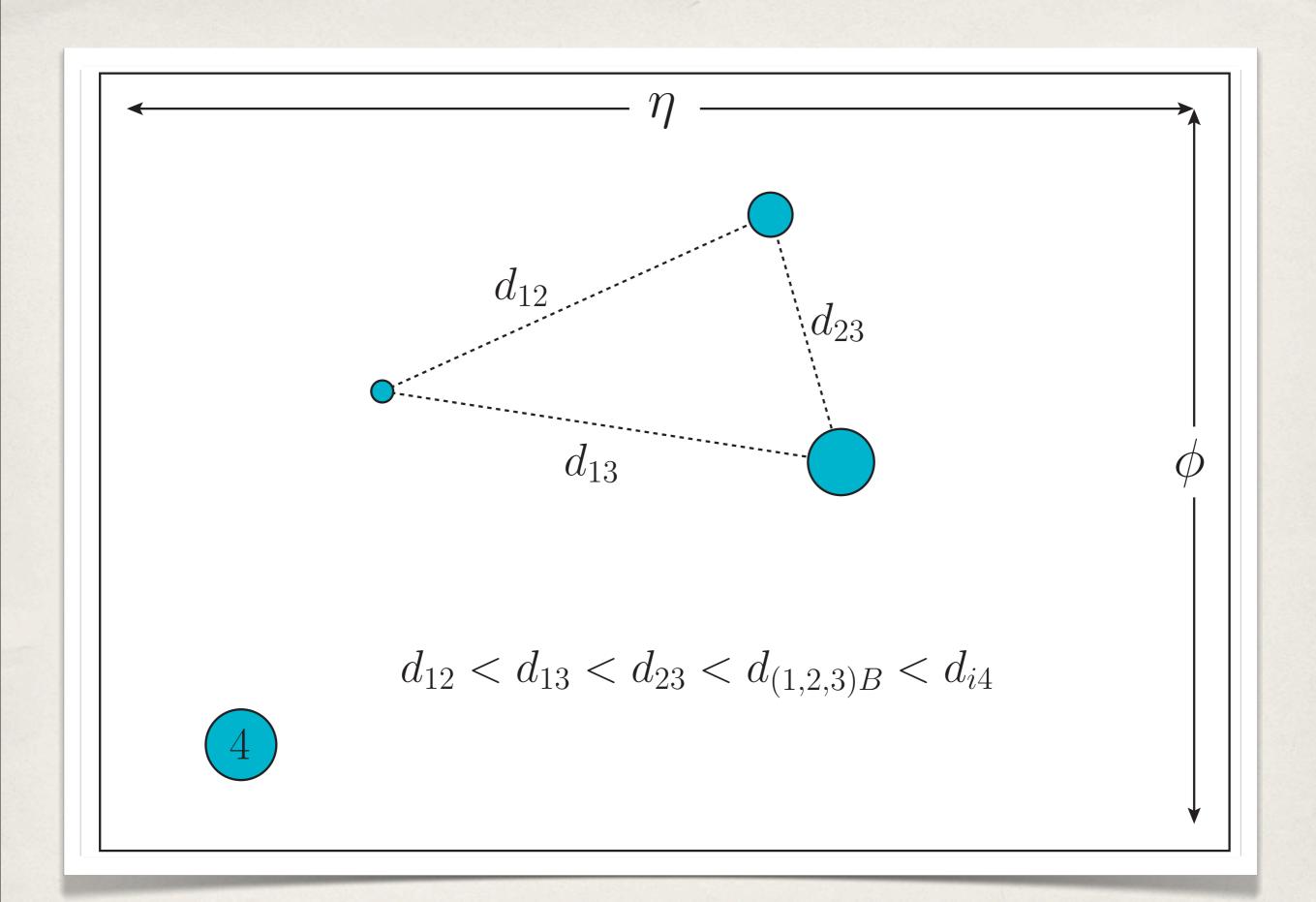


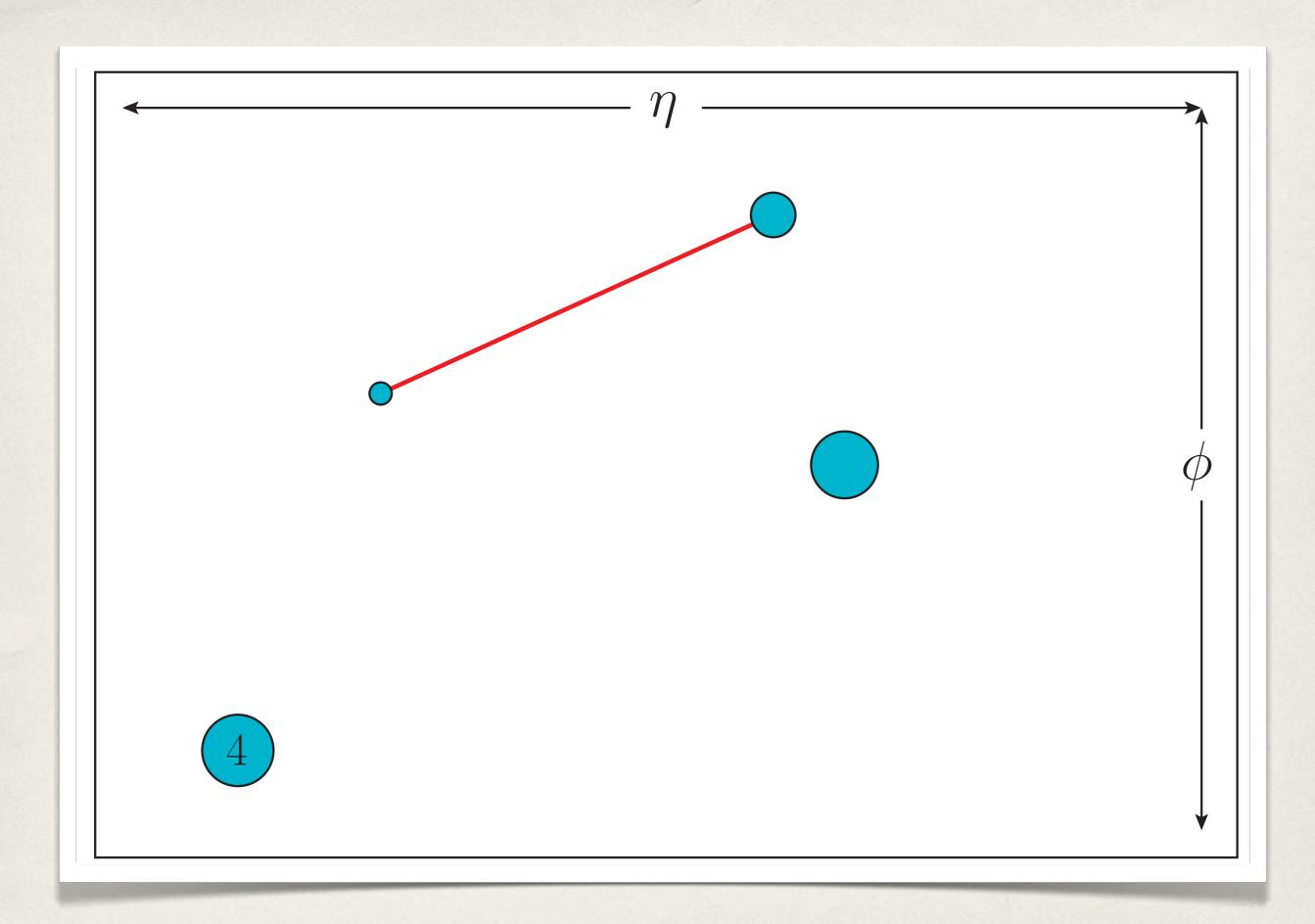


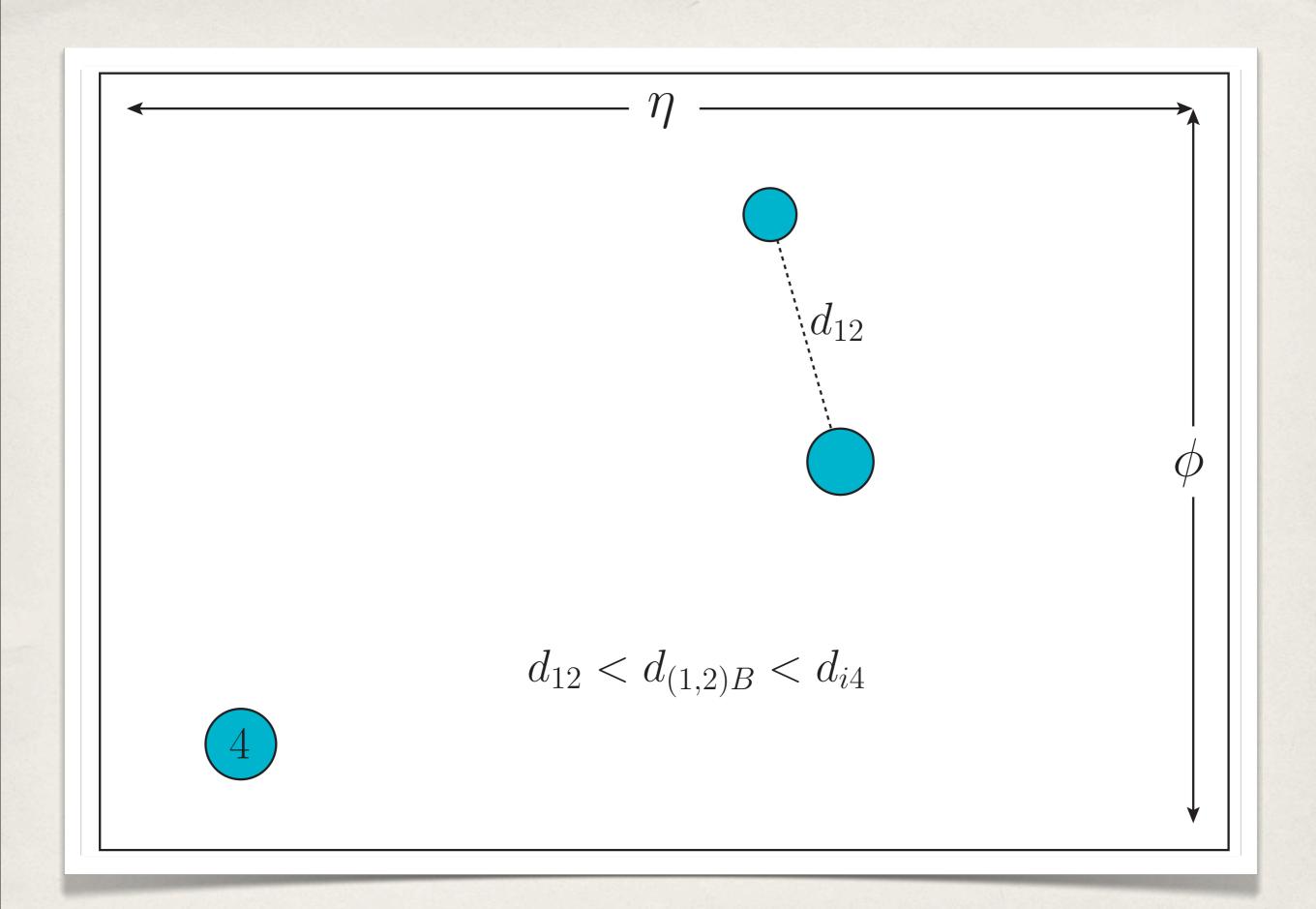
an event with 2 jets becomes an event with one jet because of a soft radiation

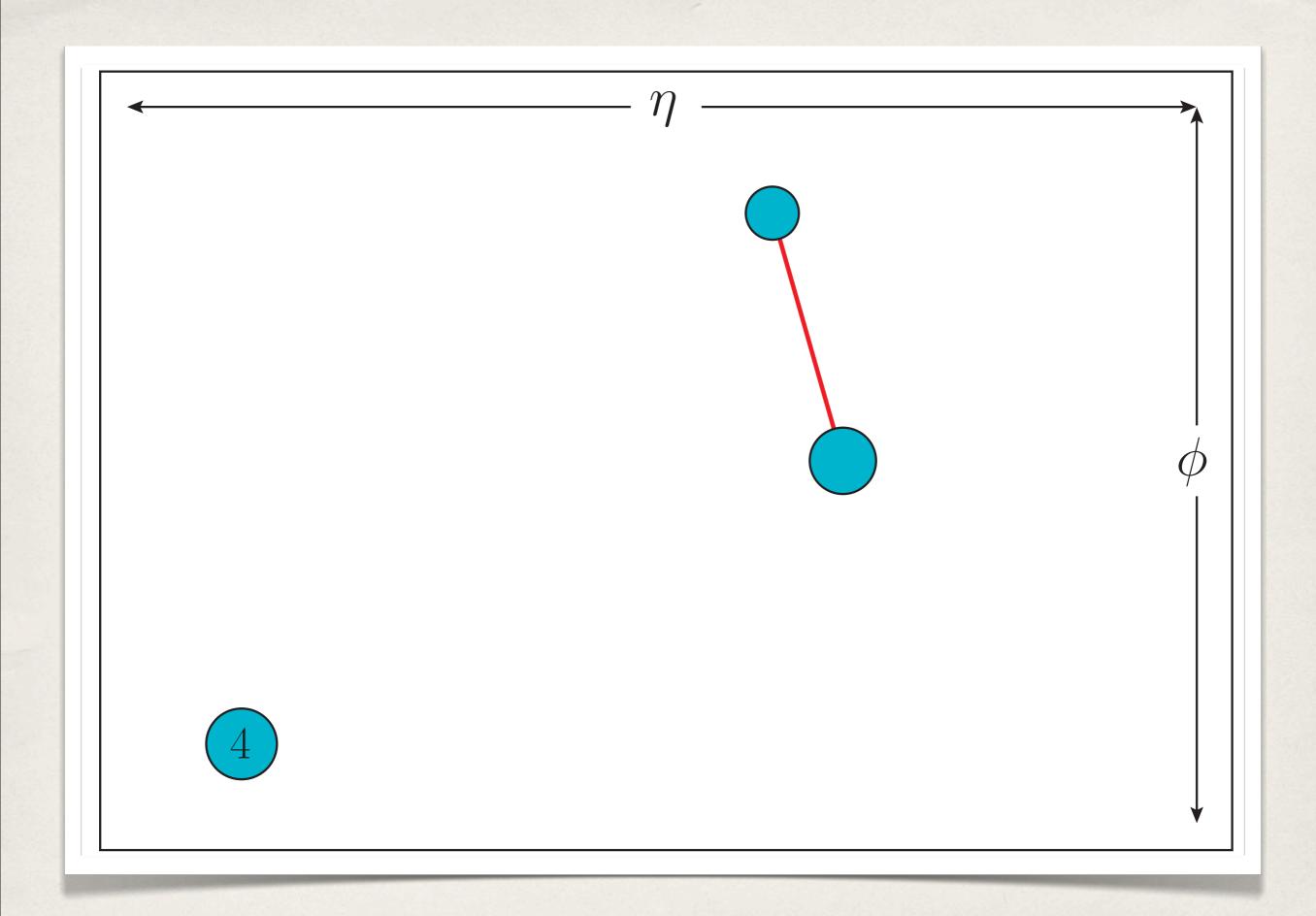
### Sequential recombination jet algorithm

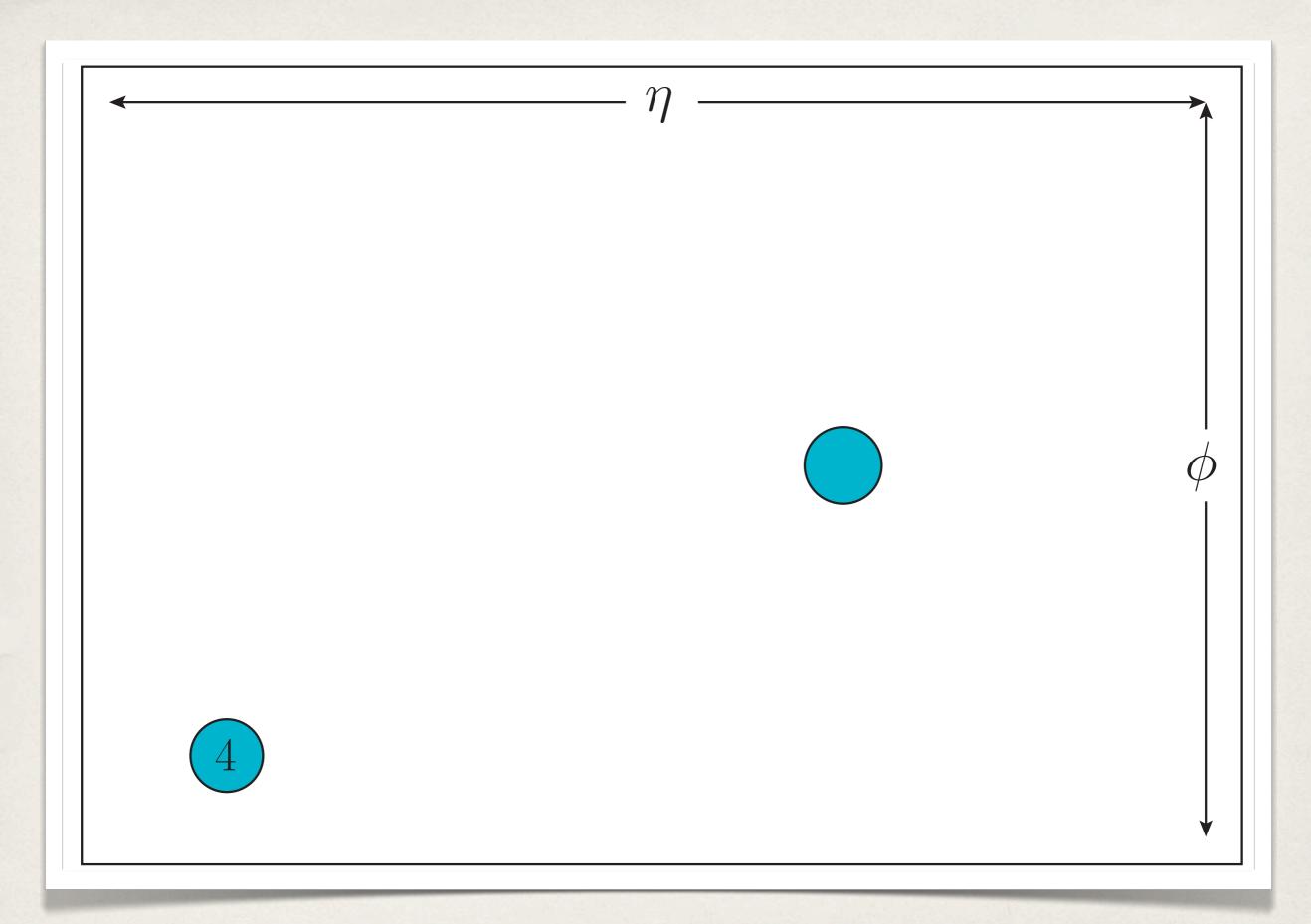
- Basic ingredients of a "sequential" jet algorithm.
- Two types of "distances"
  - Jet-jet distance:  $d_{ij}$  "when to cluster"
  - ullet Jet-beam distance:  $d_{iB}$  "when to stop clustering"
- Pair wise comparison of all distances
  - If smallest distance at any stage in clustering is jet-jet, add together corresponding four-momenta, else take jet with smallest jet-beam distance and set it aside.
  - Repeat till all jets are set aside.





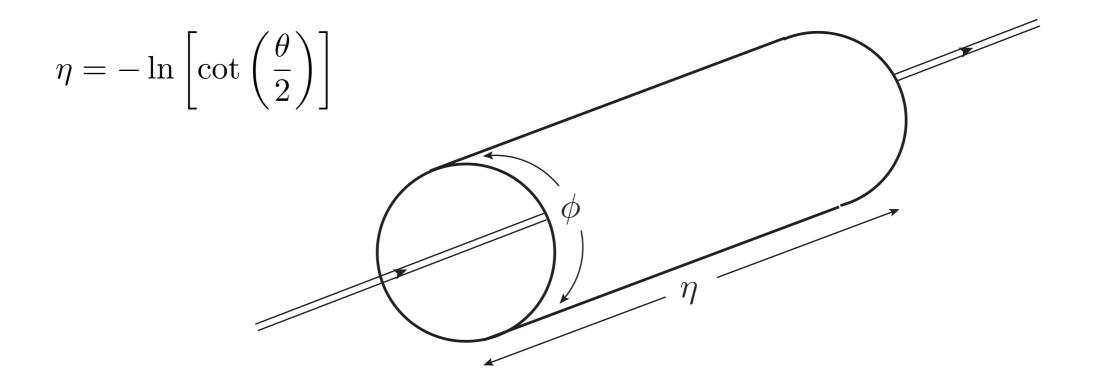






Done!

### Coordinate System



Distance measure:  $(\Delta R)^2 \equiv (\Delta \eta)^2 + (\Delta \phi)^2$ 

# Recombination Algorithms, $p_{TB}$

k<sub>T</sub> algorithm

algorithm 
$$Approximat$$
 
$$d_{ij} = \min(p_{Ti}^2, p_{Tj}^2) \left(\frac{\Delta R}{R_0}\right)^2, \ d_{iB} = p_{Ti}^2$$
 A

C/A algorithm

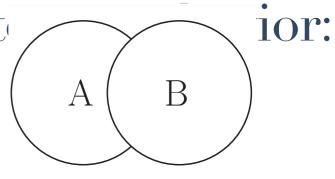
$$d_{ij} = \left(\frac{\Delta R}{R_0}\right)^2, \ d_{iB} = 1$$

anti-k<sub>T</sub> algorithm

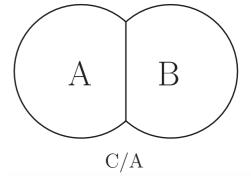
$$d_{ij} = \min(p_{Ti}^{-2}, p_{Tj}^{-2}) \left(\frac{\Delta R}{R_0}\right)^2, \ d_{iB} = p_{Ti}^{-2}$$

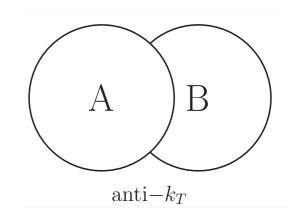
$$(\Delta R)^2 \equiv (\Delta \eta)^2 + (\Delta \phi)^2$$



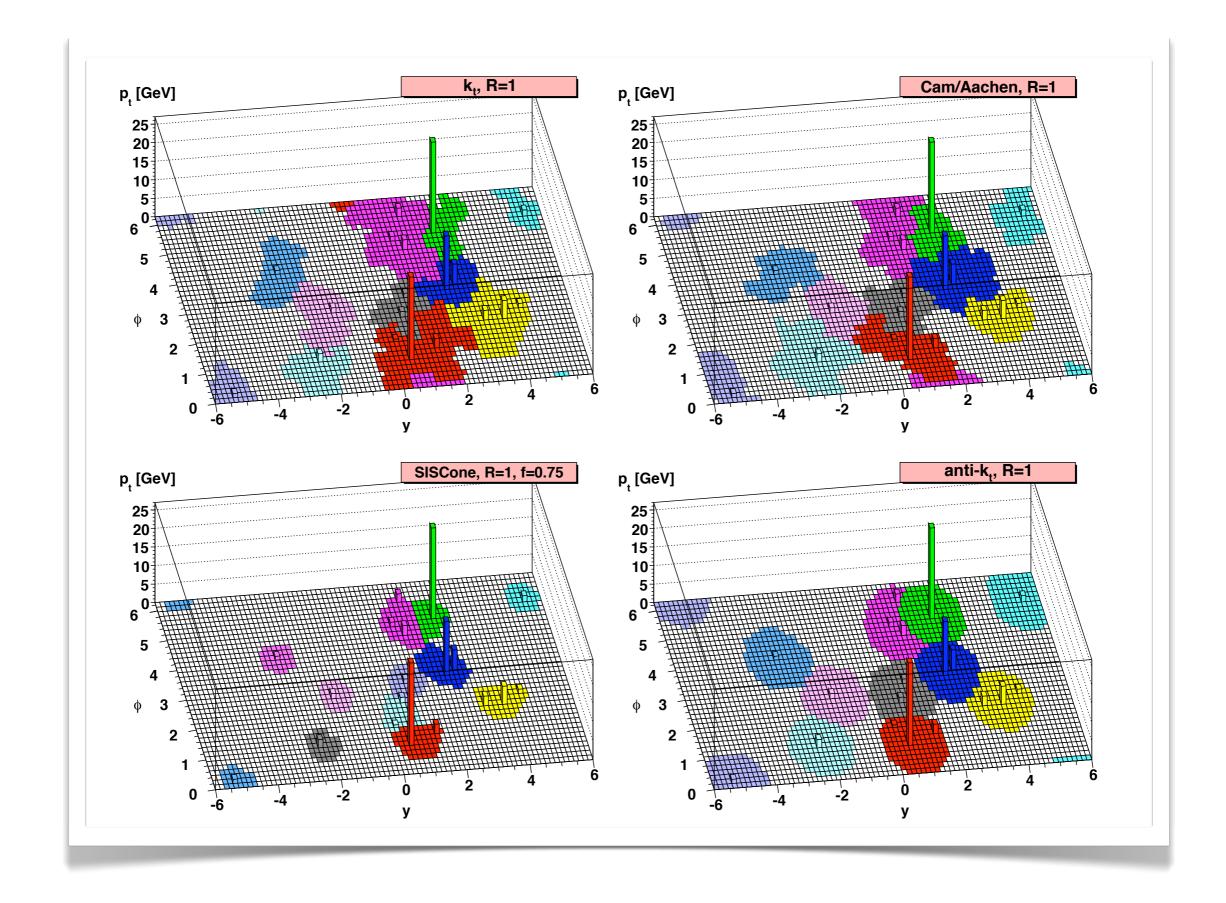


Annroximate Je



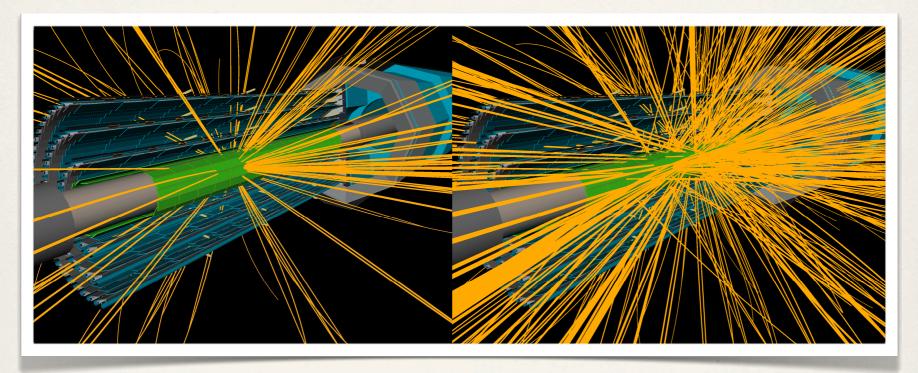


$$p_T^A > p_T^B$$



### Messy environment

\* Example: here's an event with 500 GeV dijets (left), and the same event with fifty pileup events (right).



- We'll encounter this level of pileup next year,
  - \* Somehow we're going to have to find new physics in this mess!

Some "clean up" procedure, filtering, pruning, trimming.

### Jet energy/momentum errors

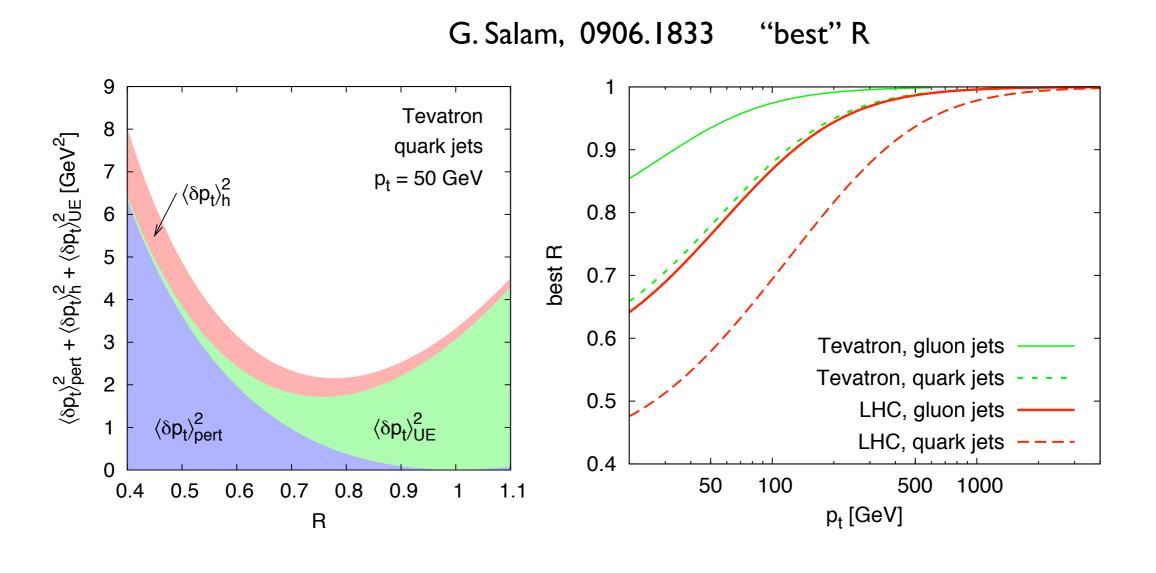
Lost Radiation (outside of the cone)

$$\langle \delta p_t \rangle_{\text{pert}} = \int \frac{d\theta^2}{\theta^2} \int dz \, \underbrace{p_t \left( \max[z, 1-z] - 1 \right)}_{\delta p_t} \frac{\alpha_s \left( \theta \left( 1-z \right) p_t \right)}{2\pi} P_{qq}(z) \, \Theta \left( \theta - f_{\text{alg}}(z) R \right),$$

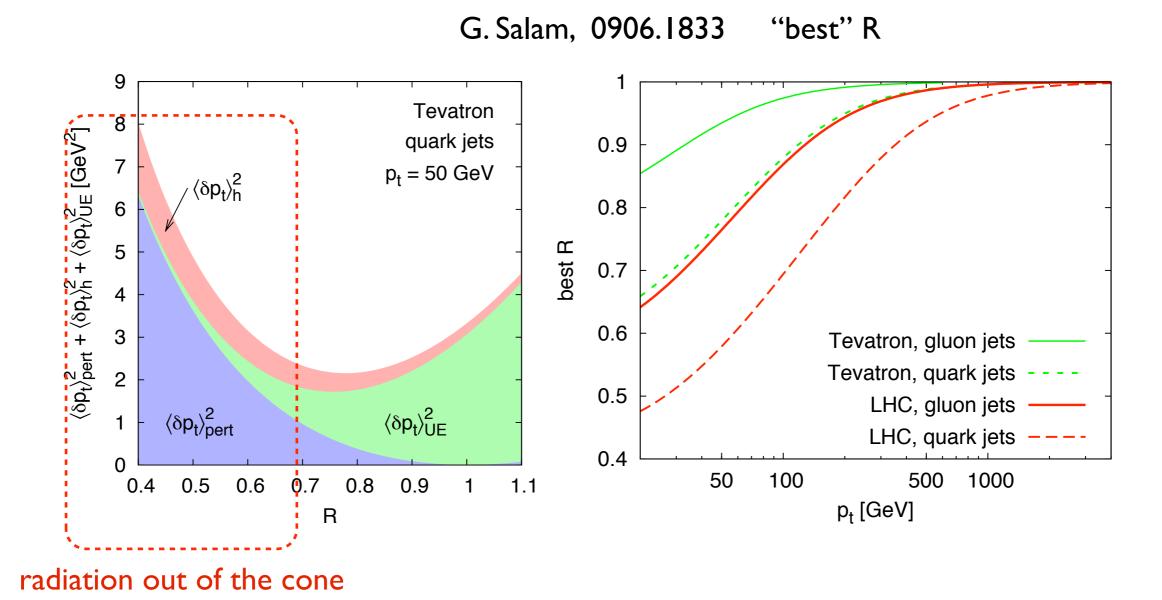
$$\Rightarrow \frac{\langle \delta p_t \rangle_{\text{pert}}}{p_t} = \frac{\alpha_s}{\pi} L_i \ln R + \mathcal{O}(\alpha_s)$$

$$\langle \delta p_t \rangle_{\text{UE}} \simeq \Lambda_{\text{UE}} R J_1(R) = \Lambda_{\text{UE}} \left( \frac{R^2}{2} - \frac{R^4}{8} + \dots \right)$$

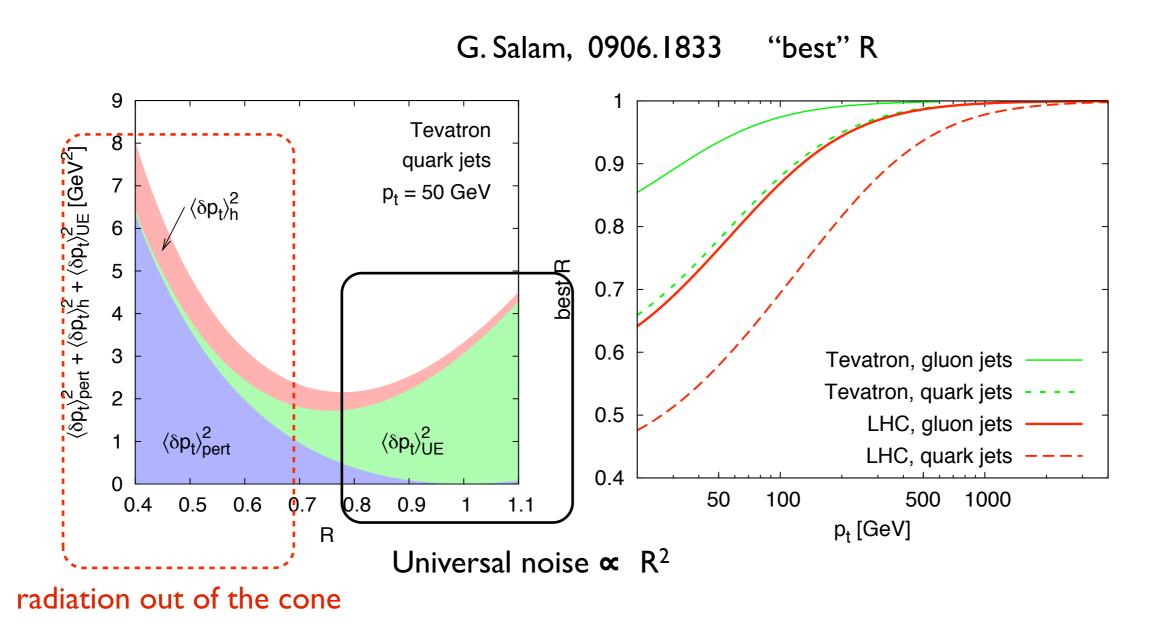
# Shape of jets.



## Shape of jets.

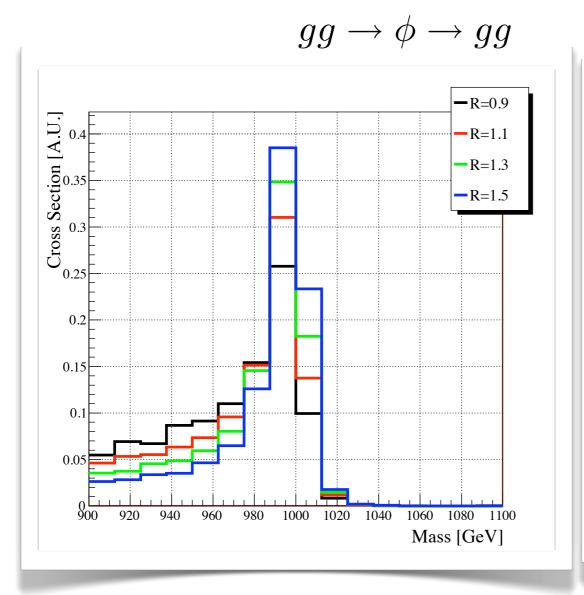


## Shape of jets.

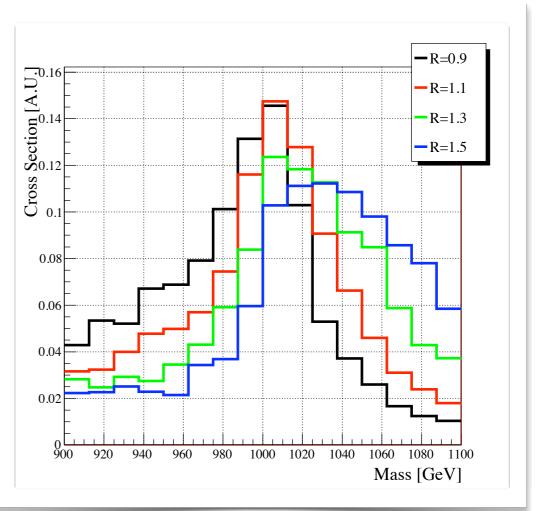


### Going beyond anti-KT: "noise" control

 Noise: Initial state radiation (ISR), multiple interaction (MI), underlying events (UE), pile-up (PU).



$$m_{\phi} = 1 \text{ TeV}$$



FSR only

Including ISR, MI, UE, pile-up

Room for improvement!

### Jet trimming.

D. Krohn, J. Thaler, LTW, arXiv:0912.1342

- Introducing a "cut" on soft radiation.
  - Discard "stuff" below the cut after jet clustering.
- Our implementation.
  - Cluster all calorimeter data using any algorithm
  - Take the constituents of each jet and recluster with smaller radius Rsub (Rsub = 0.2 seems to work well).
  - Discard the subjet i if  $p_{Ti} < f_{\mathrm{cut}} \cdot \Lambda_{\mathrm{hard}}$  — ISR argument.
- Best choice of the hard scattering scale and fcut.
  - Process dependent.
  - Can be optimized experimentally.

### Why is it possible to gain?

- MI, UE, and pile-up are incoherent soft background. They can be effectively removed with a cut on soft radiation.
- Both FSR (want to keep) and ISR (want to discard) have soft radiation, but
  - ISR:  $d\sigma \propto \frac{dp_{\mathrm{T}}^{\mathrm{ISR}}}{p_{\mathrm{T}}^{\mathrm{ISR}}}$  no direction correlation.
  - FSR is controlled by both collinear and soft singularities:

$$d\sigma \propto \frac{d(\Delta R)}{\Delta R} \times \frac{dp_{\mathrm{T}}^{\mathrm{FSR}}}{p_{\mathrm{T}}^{\mathrm{FSR}}}$$

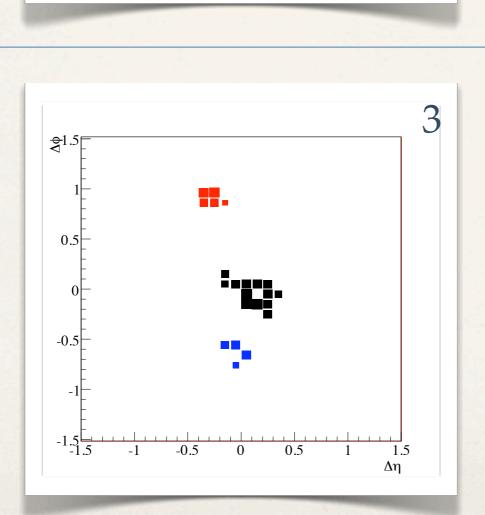
- Tends to be clustered into subjet, and kept.
- Therefore, a soft cut on subjet relative to the jet energy flow could enhance FSR relative to ISR.



1.5 Δη

0.5

# Start



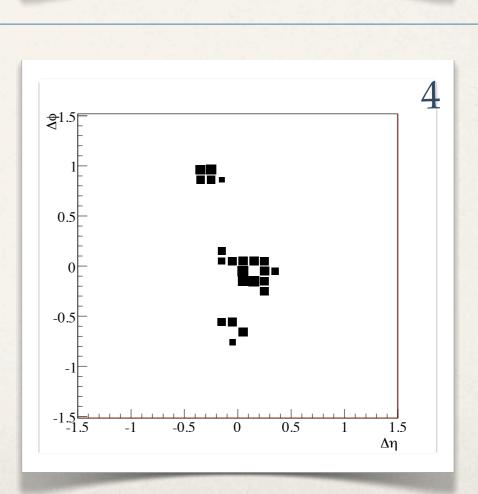
-0.5

1

1.5 Δη

0.5

0



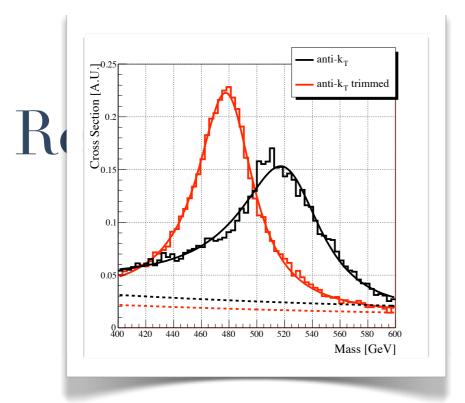
-0.5

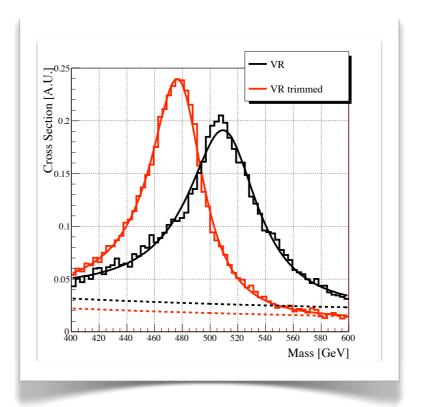
Discard soft subjets

Reassemble

### Simple test case: di-jet resonance

$$gg \rightarrow \phi \rightarrow gg$$



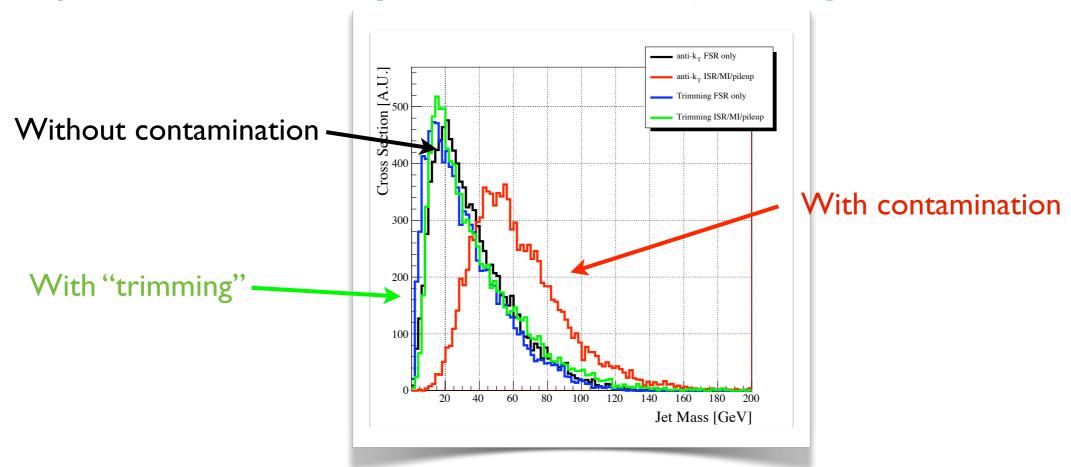


	Improvement	$f_{\rm cut}, N_{\rm cut}$	$R_{ m sub}$	$R_0, \rho$	$\Gamma [{ m GeV}]$	$M [{ m GeV}]$
anti- $k_T$	-	-	-	1.0*	71	522
anti- $k_T$ $(N)$	40%	5*	$0.2^*$	$1.5^*$	62	499
anti- $k_T$ $(f, p_T)$	59%	$3 \times 10^{-2*}$	0.2	1.5	52	475
anti- $k_T$ $(f, H)$	61%	$1 \times 10^{-2*}$	0.2	1.5	50	478
VR	30%	-	-	$200^* \text{ GeV}$	62	511
VR(N)	53%	5	0.2	$275^* \text{ GeV}$	53	498
$VR(f, p_T)$	68%	$3 \times 10^{-2}$	0.2	$300^* \text{ GeV}$	49	475
VR(f, H)	73%	$1 \times 10^{-2}$	0.2	$300^* \text{ GeV}$	47	478

We provide plugins fully compatible with Fastjet.

http://jthaler.net/jets/VR\_Jets.html
http://jthaler.net/jets/Jet\_Trimming.html

### Jet mass: help from new jet algorithm



More faithful (smaller) jet mass for the background.

• Effect of radiation contamination on the jet mass

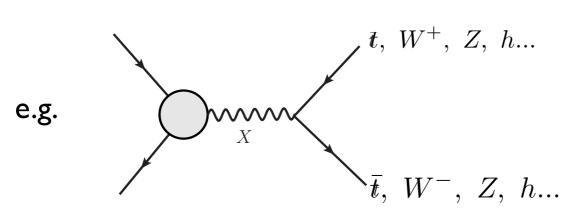
$$\langle \delta M^2 \rangle \simeq (\Lambda_{\rm soft} + p_{\rm T}^{\rm ISR}) p_{\rm T}^j \left( \frac{(\Delta R)^4}{4} + \dots \right)$$

 Trimming gives large improvement by reducing effective jet size significantly.

# Jet substructure

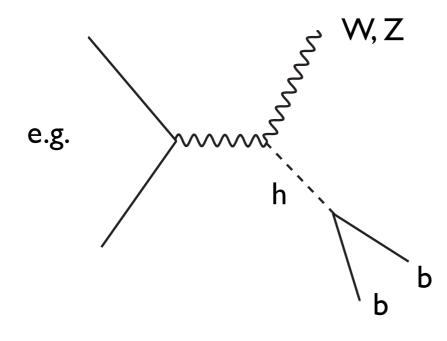
### When to consider substructure

Have to consider the boosted objects.



For example, boost tops
Brooijmans; Lillie, Randall, LTW; Thaler, LTW;
D. Kaplan, K. Reherman, M. Schwartz, B. Tweedie;
L. Almeida, S. Lee, G. Perez, G. Sterman, I. Sung, J. Virzi
S. Chekanov and J. Proudfoot.

It is beneficial to consider the boosted objects.



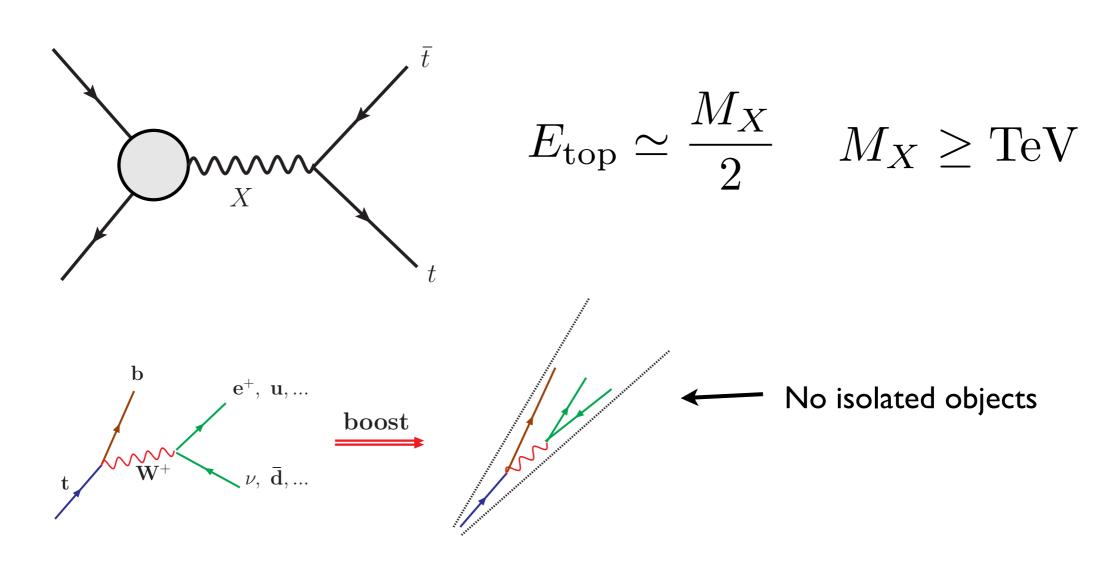
Lower combinatorics, SM background boost differently.

Butterworth, Davidson, Bubin, Salam

For a summary of recent developments: C. Vermilion, 1001.1335

# For example, boosted top quark.

Heavy resonance decay.

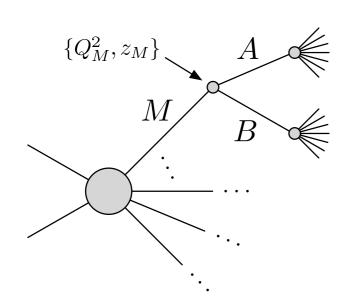


- •For  $m_{t\bar{t}}>$  3 TeV, > 90% events with at least one top fully collimated.
- •Large fraction of events "2-object"-like. QCD  $b\bar{b}$ , jj background.
- •A few % with lepton isolation

Lillie, Randall, and Wang, JHEP 0709:074, 2007

### Shape of a jet: parton shower

 From the initial parton, a jet is built up by many radiations.



$$d\sigma_{M\to A+B}^{\rm QCD} = \frac{dQ_M^2}{2\pi} \frac{1}{Q_M^2} dz \frac{\alpha(\mu)}{2\pi} P_{M\to AB}(z) \Delta(\mu_{\rm start}, \mu)$$

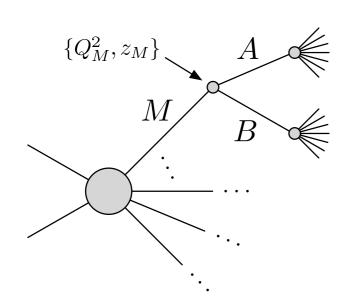
Prefers collinear radiation

 $P \sim (z)^{-1}$  prefers soft radiation

- QCD jet: a cluster of radiation
- a) relatively soft
- b) close to the direction of P<sub>M</sub>
- c) approximately symmetrical around P<sub>M</sub>

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QCD jet: a cluster of radiation

- a) relatively soft
- b) close to the direction of P<sub>M</sub>
- c) approximately symmetrical around P<sub>M</sub>

 $Q_{M^2}$  (first splitting) = virtuality or "mass" of orginal parton ≈ jet mass

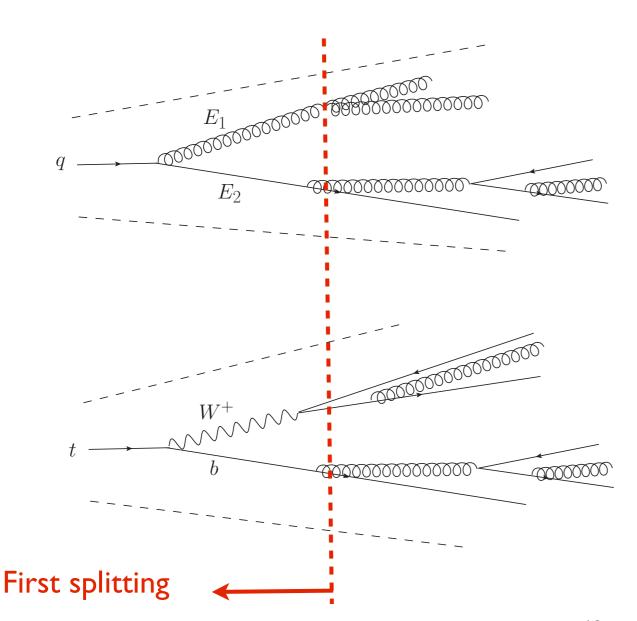
For QCD jets 
$$\frac{d\sigma}{dm_{jet}^2} \propto \frac{1}{m_{
m jet}^2}$$

### (hadronic) Top tagging at the LHC

Fully collimated tops look like QCD jets.

Basic distinction:

- QCD: radiation.
- Top decay:  $t \to bW(\to qq')$  3 hard objects.



### Zooming in near the first splitting

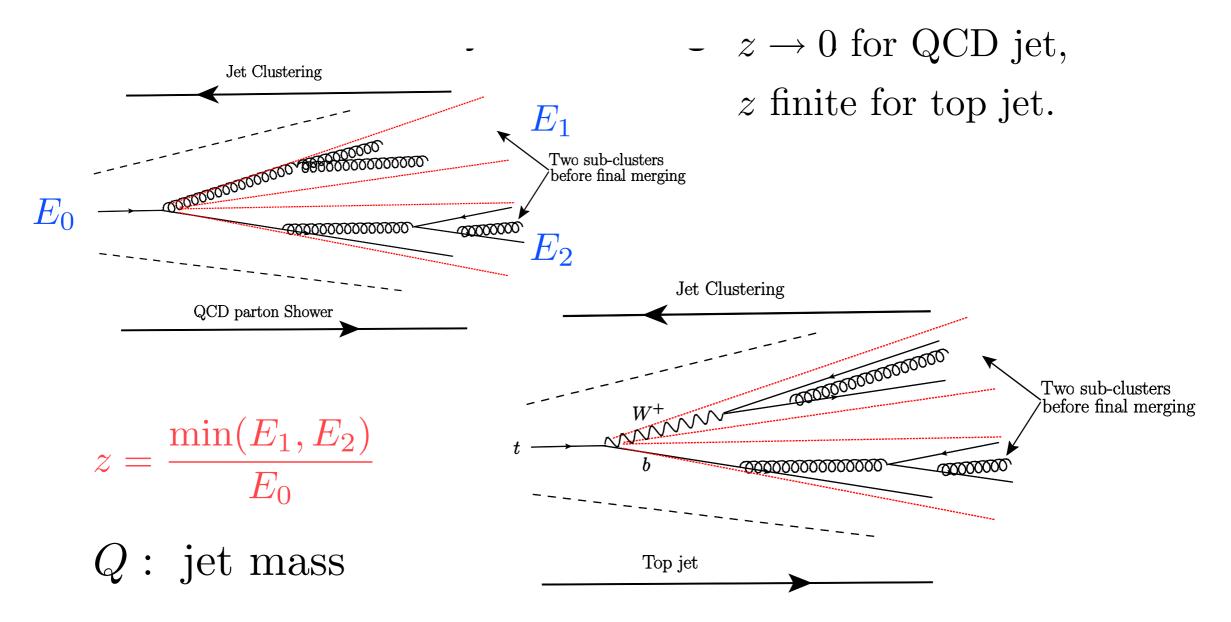
QCD. Soft radiation: 
$$z = \frac{\min(E_1, E_2)}{E_1 + E_2} \rightarrow 0$$

Jet mass: 
$$d\sigma \propto \frac{1}{m_{
m jet}^2}$$

Top. Decay: 
$$z = \frac{\operatorname{Min}(E_{\mathrm{W}}, E_b)}{E_{\mathrm{W}} + E_b} \to \operatorname{finite}$$

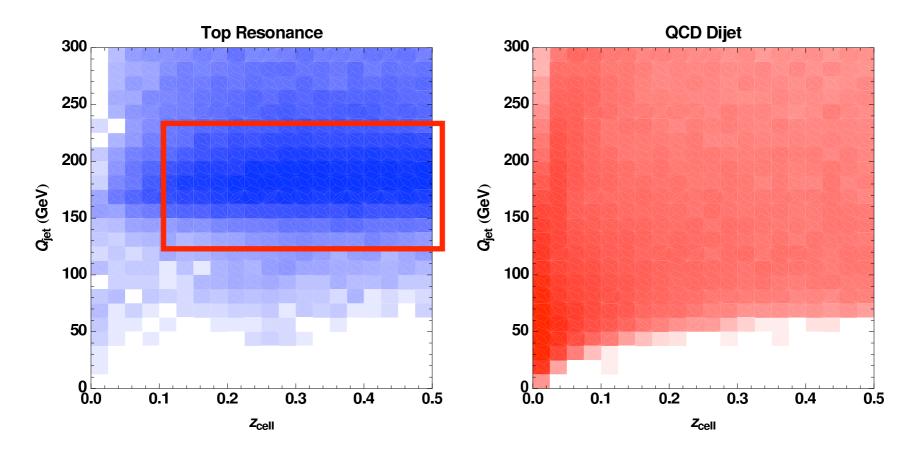
Jet mass: 
$$m_{\rm jet} \simeq m_{\rm top}$$

# Building amiches jet formation: inside jets.



 The jet clustering history is approximately the inverse of the parton shower.

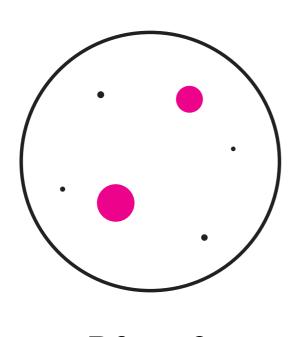
### Top jets vs QCD jets



 Combined cuts on jet mass and z can enhance further the signal with respect to the background.

### More jet shape variables.

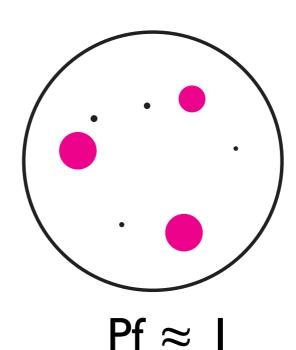
- Top decay is more like 3-body. Span a "plane" perpendicular to the jet axis.
  - Transverse sphericity, or planar flow



$$Pf \approx 0$$

$$I_w^{kl} = \sum_i w_i \frac{p_{i,k}}{w_i} \frac{p_{i,l}}{w_i}$$

 $\lambda_1, \ \lambda_2: \ 2 \text{ eigenvalues of } I_w^{kl}$ 

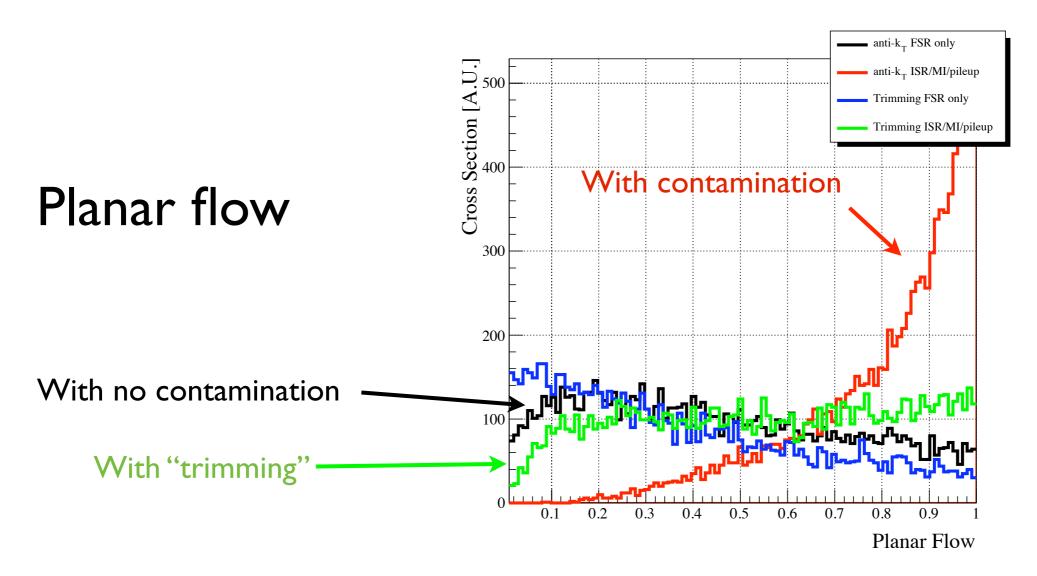


$$Pf = \frac{4\lambda_1\lambda_2}{(\lambda_1 + \lambda_2)^2}$$

Thaler and LTW, arXiv:0806.0023.

51Almeida, Lee, Perez, Sterman, Sung, Virzi, arXiv:0807.0234

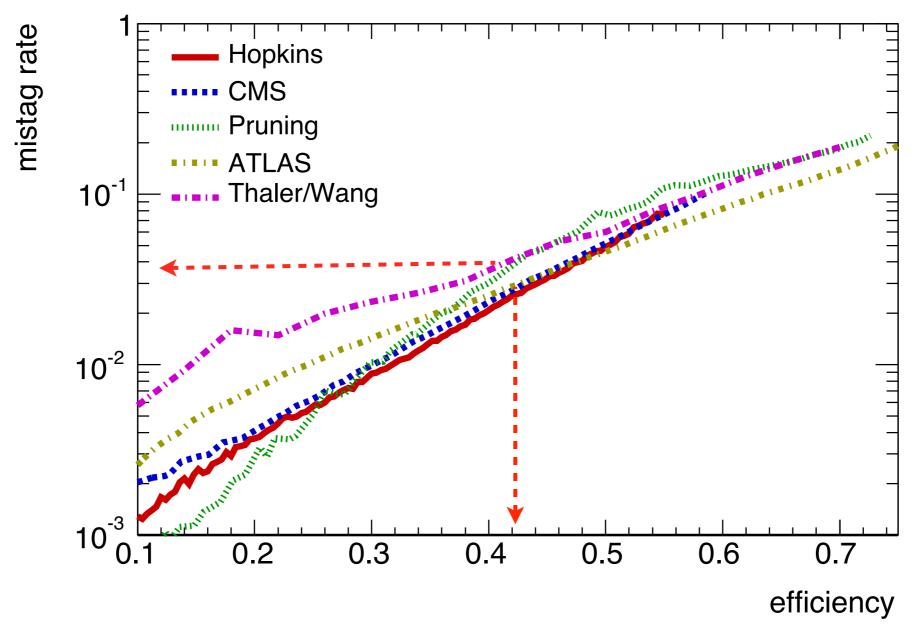
### Grooming gives better jet shape



- Can be used to further improve top tagging. An additional factor of several possible.
- Interesting to compare with improved QCD calculation, using modern technologies such as SCET.

### Various top taggers

Boost 2010 proceeding, 1012.5421



G. Brooijmans, arXiv:0802.3715;

CMS Coll. CMS PAS JME-09-001 J. Thaler, LTW, arXiv:0806.0023

D. Kaplan, K. Reherman, M. Schwartz, B. Tweedie, arXiv: 0806.0848.

L. Almeida, S. Lee, G. Perez, G. Sterman, I. Sung, J. Virzi, arXiv:0807.0243

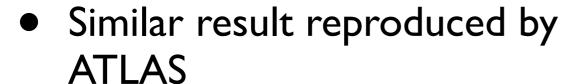
L. Almeida, S. Lee, G. Perez, G. Sterman, I. Sung, arXiv: 1006.2035

Barger, Huang, 1102.3183

53

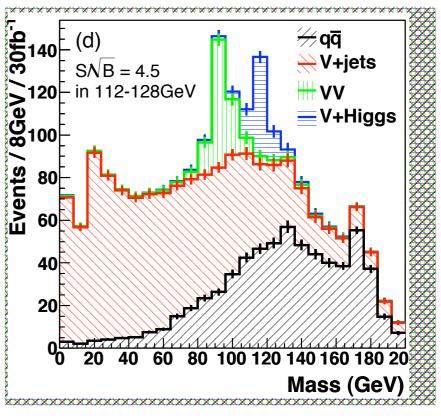
- Considere ထို ဦစီoosted Higgs.
  - Better at the Better at the
  - backgroudssuch as ttbar
     boost diffeneratly.60 80 100 120 140 160 180 20
     Mass (GeV)

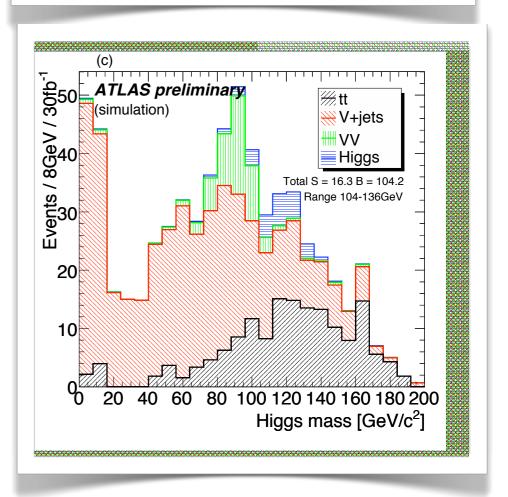
 $4.5(8.2)\sigma$  with 14 TeV and 30(100)  $fb^{-1}$ 



 $3.7\sigma$  with 14 TeV and 30  $fb^{-1}$ 

ATL-PHYS-PUB-2009-088





### New developments: N-jettiness

Stewart, Tackmann, Waalewijn, 1004.2489

$$\mathcal{T}_N = \sum_k |ec{p}_{kT}| \min\{d_a(p_k), d_b(p_k), d_1(p_k), d_2(p_k), \ldots, d_N(p_k)\}$$

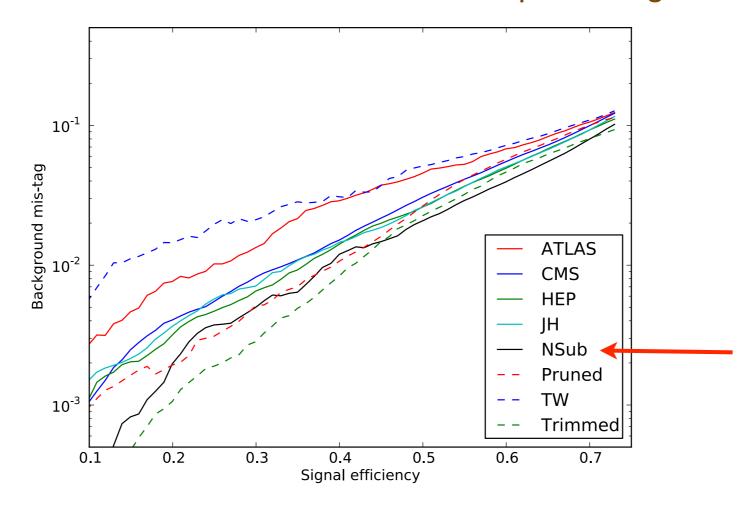
$$\equiv \mathcal{T}_N^a + \mathcal{T}_N^b + \mathcal{T}_N^1 + \cdots + \mathcal{T}_N^N$$

$$\downarrow \text{Soft} \qquad \qquad \downarrow \text{Soft} \qquad \qquad \downarrow \text{Soft} \qquad \qquad \downarrow \text{Soft} \qquad \qquad \downarrow \text{Jet } a \qquad$$

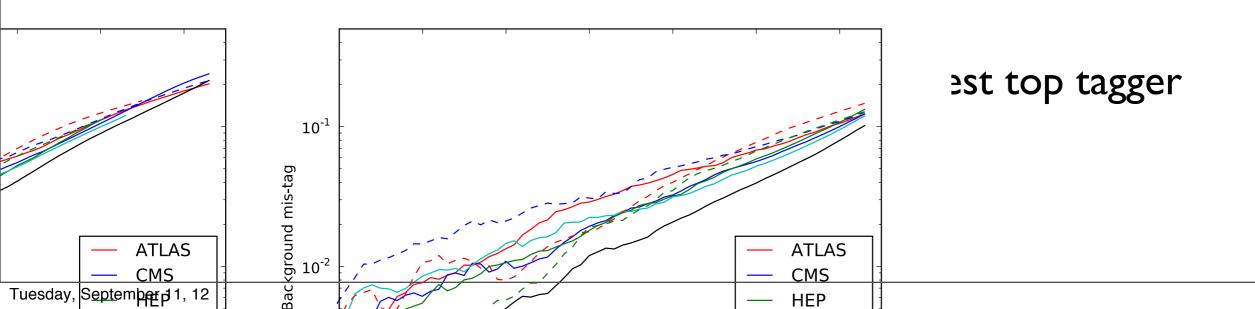
- Using event shape instead of clustered jets.
- Allowing better QCD (SCET) treatments.
- Example: application in jet veto in Higgs searches.

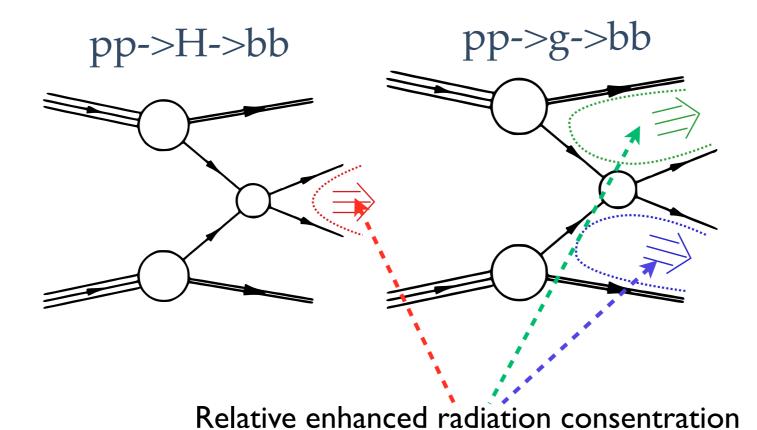
### N-subjettiness

### Boost 2011 proceeding



Using the N-jettiness idea, but applies to number of





- Using more global information.
- Applications to other channels as well.

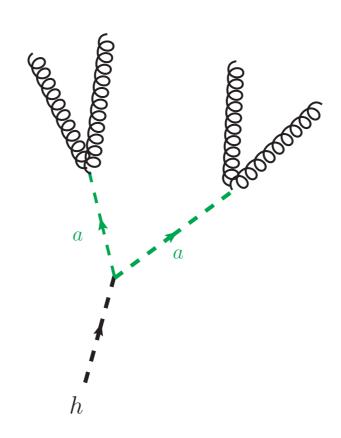
e.g., ttbar at Dzero, Haas Boston Jet Workshop

## Unbury the Higgs.

$$h \to aa \to gggg$$
, "buried"!

### For example:

B. Bellazzini, C. Csaki, A. Falkowski, A. Weiler, arXiv:0910.3210, arXiv:0906.3026



Soft gluon jets, considered impossible.

$$h \to aa \to c\bar{c}c\bar{c}$$
, "charmful"?  $h \to aa \to 4\tau, \ 4b, \ \bar{b}b\bar{\tau}\tau$  58

For example:

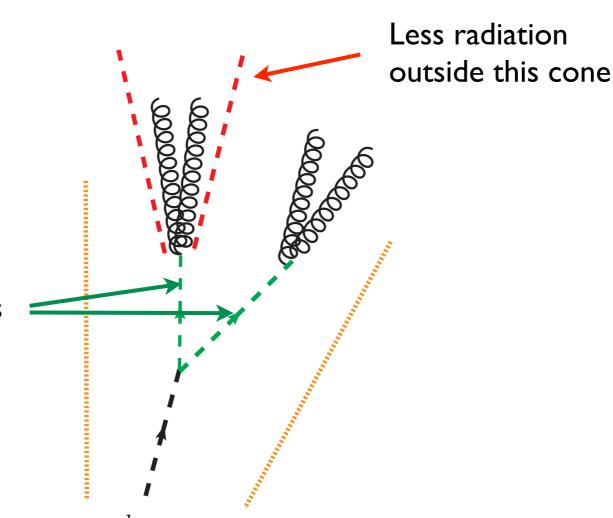
P. Graham, A. Pierce, J. Wacker, hep-ph/0605162 M. Carena, T. Han, G. Huang, C. Wagner, arXiv:0712.2466

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Two "equal "clusters

Boosting the Higgs.

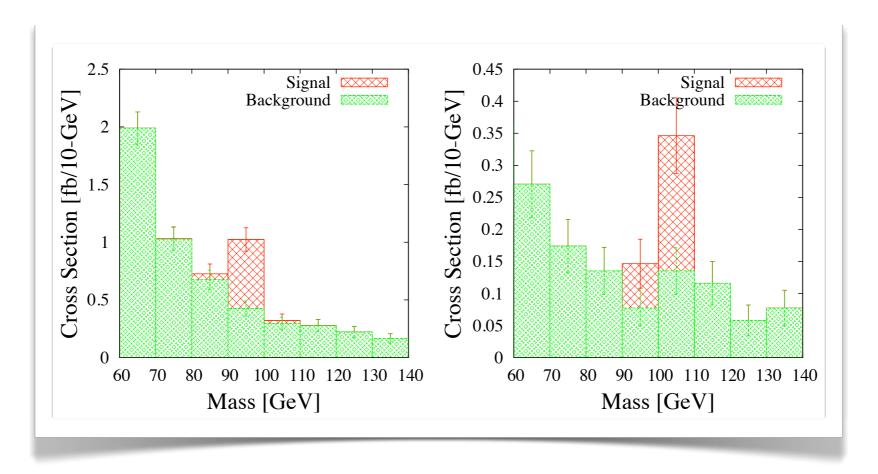
$$h \to aa \to c\bar{c}c\bar{c}$$
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For example:

P. Graham, A. Pierce, J. Wacker, hep-ph/0605162 M. Carena, T. Han, G. Huang, C. Wagner, arXiv:0712.2466

### Encouraging results.

 $> 5\sigma \text{ at } 100 \text{ fb}^{-1}$ 



W/Z+h ttbar+h

Chen, Nojiri, Sreethawong, 1006.1151 Falkowski, Krohn, Shelton, Thalapillil, and LTW, 1006.1650

### Substructure can also be useful for

- From top/W/Z/Higgs from NP decay, early LHC prospects.
  - Resonance ttbar.
  - **SUSY.** Kribs, Martin, Roy, Spannowsky, 0912.4731, 1006.1656
  - Top partner to Higgs. Kribs, Martin, and Roy, 1012.2886
  - **Z'** to WW, Zh... Cui, Han, Schwartz, 1012.2077 Katz, Son, Tweedie, 1010.5253
- Boosted NP particles.
  - Neutralino + RPV
     Butterworth, Ellis, Raklev, Salam, 0906.0728
  - Boosted gluino from squark. Fan, Krohn, Mosteiro, Thalapillil, 1102.0302