



# Discrete Dark Matter

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Merida Yucatán, 3<sup>rd</sup> - 8<sup>th</sup> June 2012

# Plan of the Talk

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1. Introduction
2. Stability Mechanism
3. The Model
4. Phenomenology
5. Conclusions

# Flavor and Flavor models

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Horizontal flavor symmetries used to:

## Predict relations between quark masses and mixings

Wilczek and Zee Phys.Lett. B70 (1977) 418

Pakvasa and Sugawara Phys.Lett. B73 (1978) 61

Sartori Phys.Lett. B82 (1979) 255

Wyler Phys.Rev. D19 (1979) 3369

⋮

$$\theta_C \simeq \sqrt{m_d/m_s}$$

Gatto Sartori, Tonin Phys.Lett. B28 (1968) 128-130

Mixing

$$U_{CKM} \sim \begin{bmatrix} 1 & \lambda & \lambda^3 \\ -\lambda & 1 & \lambda^2 \\ \lambda^3 & -\lambda^2 & 1 \end{bmatrix}$$

Small mixing angles

$$\lambda = \sin \theta_C = 0.23$$

# Neutrino masses

There is evidence of solar, atmospheric and reactor neutrino oscillation

Difference mass squared

$$\Delta m_{\text{atm}}^2 \sim 2.5 \cdot 10^{-3} \text{ eV}^2,$$

$$\Delta m_{\text{sol}}^2 \sim 8 \cdot 10^{-5} \text{ eV}^2$$

Mixing angles

$$\theta_{12} \text{ (solar) large}$$

$$\theta_{23} \text{ (atm) large, } \sim \text{maximal}$$

$$\theta_{13} \text{ (T2K, Double Chooz, Daya Bay) small}$$

Forero, Tortola and Valle

arXiv:1205.4018v2 [hep-ph]

## 3-Neutrino oscillation parameters

parameter	best fit $\pm 1\sigma$	$2\sigma$	$3\sigma$
$\Delta m_{21}^2 [10^{-5} \text{eV}^2]$	$7.59^{+0.20}_{-0.18}$	7.24–7.99	7.09–8.19
$\Delta m_{31}^2 [10^{-3} \text{eV}^2]$	$2.50^{+0.09}_{-0.16}$ $-(2.40^{+0.08}_{-0.09})$	2.25 – 2.68 $-(2.23 – 2.58)$	2.14 – 2.76 $-(2.13 – 2.67)$
$\sin^2 \theta_{12}$	$0.312^{+0.017}_{-0.015}$	0.28–0.35	0.27–0.36
$\sin^2 \theta_{23}$	$0.52^{+0.06}_{-0.07}$ $0.52 \pm 0.06$	0.41–0.61 0.42–0.61	0.39–0.64
$\sin^2 \theta_{13}$	$0.013^{+0.007}_{-0.005}$ $0.016^{+0.008}_{-0.006}$	0.004–0.028 0.005–0.031	0.001–0.035 0.001–0.039
$\delta$	$(-0.61^{+0.75}_{-0.65})\pi$ $(-0.41^{+0.65}_{-0.70})\pi$	0 – $2\pi$	0 – $2\pi$

Double CHOOZ experiment, talk by H.De. Kerrect at LowNu2011, <http://workshop.kias.re.kr/lownu11/>

Best measured

Daya Bay:

$$\sin^2 \theta_{13} \sim 0.0235$$

CP measurable??

# DM Stability

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DM is stable

$$\tau_{DM} > \tau_U \sim 10^{18} \text{ sec}$$

$$\tau_{DM} \gtrsim 10^{26} \text{ sec} \quad \leftarrow \text{in most models not to produce } e^+, \bar{p}, \gamma, \dots \text{ fluxes larger than observed}$$

In many models Stability

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In many models Stability assumed by hand

# DM Stability

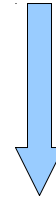
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ad hoc global symmetry assumed, e.g. a  $Z_2$

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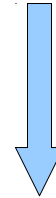
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In many models Stability assumed by hand



ad hoc global symmetry assumed, e.g. a  $Z_2$

**Some fundamental explanations e.g. GUTS  
and SUSY GUTS**



# Neutrino masses

## 3-Neutrino oscillation parameters

parameter	best fit $\pm 1\sigma$	$2\sigma$	$3\sigma$	
$\Delta m_{21}^2$ [ $10^{-5} \text{eV}^2$ ]	$7.62 \pm 0.19$	7.27–8.01	7.12–8.20	Double CHOOZ experiment Daya Bay, RENO
$\Delta m_{31}^2$ [ $10^{-3} \text{eV}^2$ ]	$2.53^{+0.08}_{-0.10}$ $-(2.40^{+0.10}_{-0.07})$	2.34 – 2.69 $-(2.25 - 2.59)$	2.26 – 2.77 $-(2.15 - 2.68)$	
$\sin^2 \theta_{12}$	$0.320^{+0.015}_{-0.017}$	0.29–0.35	0.27–0.37	Best measured
$\sin^2 \theta_{23}$	$0.49^{+0.08}_{-0.05}$ $0.53^{+0.05}_{-0.07}$	0.41–0.62 0.42–0.62	0.39–0.64	Daya Bay:
$\sin^2 \theta_{13}$	$0.026^{+0.003}_{-0.004}$ $0.027^{+0.003}_{-0.004}$	0.019–0.033 0.020–0.034	0.015–0.036 0.016–0.037	
$\delta$	$(0.83^{+0.54}_{-0.64}) \pi$ $0.07\pi^a$	$0 - 2\pi$	$0 - 2\pi$	CP measurable??

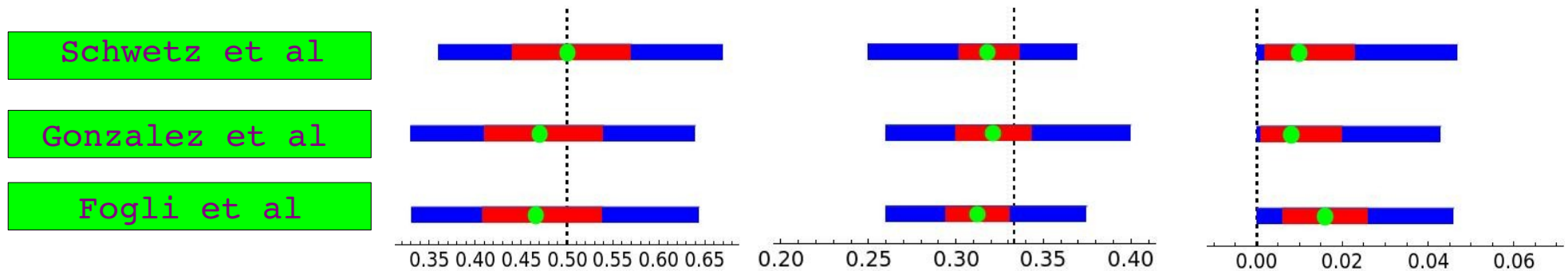
$\sin^2 \theta_{13}$	0.026
	0.027

# TBM mixing

$$U_{\text{HPS}} = \begin{pmatrix} \sqrt{2/3} & 1/\sqrt{3} & 0 \\ -1/\sqrt{6} & 1/\sqrt{3} & -1/\sqrt{2} \\ -1/\sqrt{6} & 1/\sqrt{3} & 1/\sqrt{2} \end{pmatrix}$$

Harrison, Perkins & Scott

$$\sin^2 \theta_{23} = 0.5 \quad \sin^2 \theta_{12} = 1/3 \quad \sin^2 \theta_{13} = 0$$

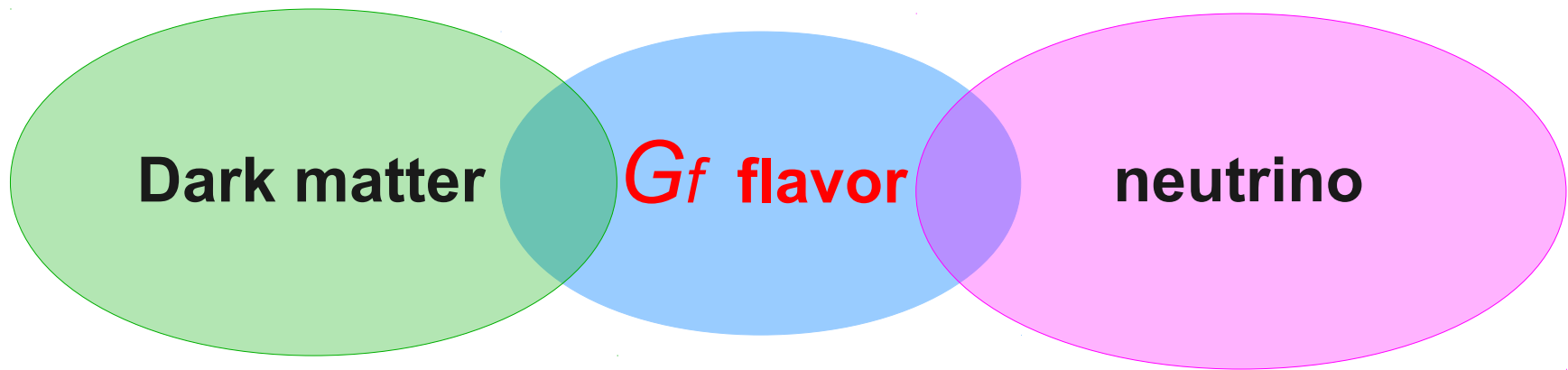


Different ansatz has been studied: mu-tau, trimaximal, tetramaximal, symmetric mixing, hexagon mixing, bimaximal, golden, quark-lepton complementarity...

Albright, Dueck, Rodejohann 1004.2798

# DM - neutrino

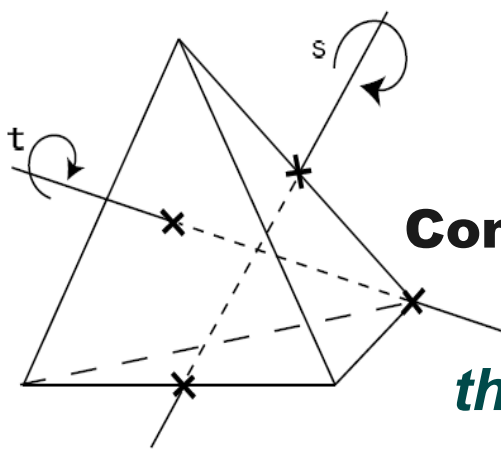
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Talk by M. Lindner

# A4 Symmetry

the discrete group even permutations four objects



$$S^2 = T^3 = (ST)^3 = 1$$

Contains **4 Irreducible** representations

*three singlets 1, 1', 1''*

*one triplet 3*

$$S = \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{pmatrix}$$

$$T = \begin{pmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \end{pmatrix}$$

# A4 Symmetry

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The generators are :

$S$  and  $T$

$$S^2 = T^3 = (ST)^3 = \mathcal{I}.$$

1, 1', 1'' and 3

1	$S = 1$	$T = 1$
1'	$S = 1$	$T = e^{i4\pi/3} \equiv \omega^2$
1''	$S = 1$	$T = e^{i2\pi/3} \equiv \omega$

S diagonal basis

$$S = \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{pmatrix}$$

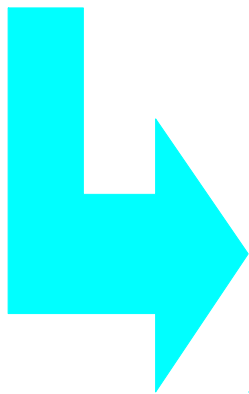
$$T = \begin{pmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \end{pmatrix}$$

# A4 spontaneously broken

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Z3 in the charged sector

Z2 in the neutrino sector



TBM



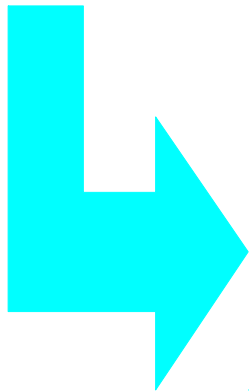
# A4 spontaneously broken

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Z3 in the ~~charged~~ sector

Z2 in the neutrino sector

**stabilize the DM**



~~TBM~~



# A4 spontaneously broken

---

**Z2** in the charged sector    **Z2** in the neutrino sector

**stabilize the DM**



Hirsch, Morisi, Peinado and Valle  
Phys. Rev. D 82, 116003 (2010)

**1, 1', 1''**

**3**



# The mechanism

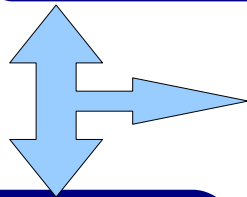
SM + 3 Higgs SU(2) doublets , 4 right handed neutrinos

Hirsch, Morisi, Peinado and Valle  
Phys. Rev. D 82, 116003 (2010)

	$L_e$	$L_\mu$	$L_\tau$	$l_e^c$	$l_\mu^c$	$l_\tau^c$	$N_T$	$N_4$	$H$	$\eta$
$SU(2)$	2	2	2	1	1	1	1	1	2	2
$A_4$	1	1'	1''	1	1''	1'	3	1	1	3

The alignment

$$\langle \eta \rangle \sim (1, 0, 0)$$



$$S = \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{pmatrix}$$

$A_4 \rightarrow Z_2$



$$\begin{pmatrix} \eta_1 \\ \eta_2 \\ \eta_3 \end{pmatrix}$$



$$\begin{pmatrix} \eta_1 \\ -\eta_2 \\ -\eta_3 \end{pmatrix}$$

# Z<sub>2</sub> residual symmetry

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$$\langle \eta \rangle \sim (1, 0, 0)$$

$$H = \begin{pmatrix} \tilde{H}_0^+ \\ (v_h + \tilde{H}_0 + i\tilde{A}_0)/\sqrt{2} \end{pmatrix}, \quad \eta_1 = \begin{pmatrix} \tilde{H}_1^+ \\ (v_\eta + \tilde{H}_1 + i\tilde{A}_1)/\sqrt{2} \end{pmatrix}$$

Z<sub>2</sub> even

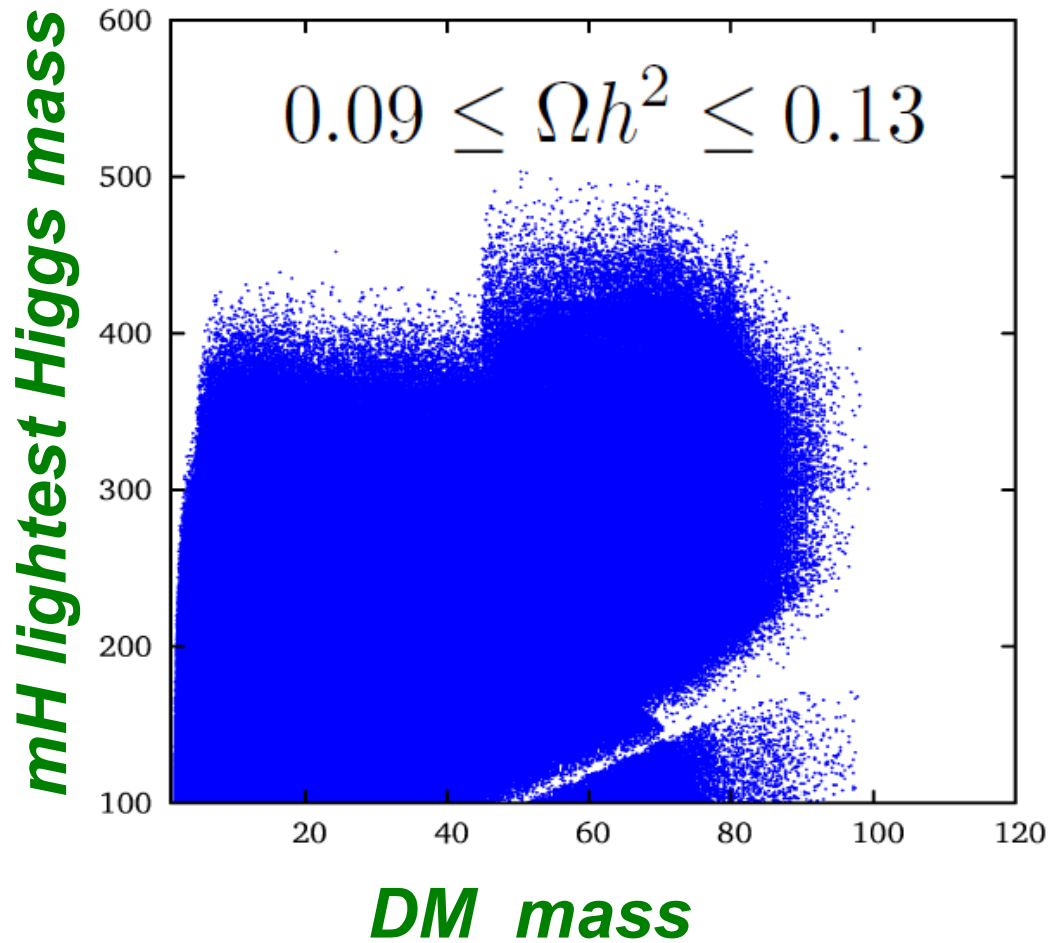
$$\eta_2 = \begin{pmatrix} \tilde{H}_2^+ \\ (\tilde{H}_2 + i\tilde{A}_2)/\sqrt{2} \end{pmatrix}, \quad \eta_3 = \begin{pmatrix} \tilde{H}_3^+ \\ (\tilde{H}_3 + i\tilde{A}_3)/\sqrt{2} \end{pmatrix}$$

Z<sub>2</sub> odd

**Dark Matter Stability**

# The mechanism

Hirsch, Morisi, Peinado and Valle  
Phys. Rev. D 82, 116003 (2010)



$$IH : m_3 = 0$$

$$0.03 \text{ eV} < m_{\nu_{bb}} < 0.05 \text{ eV}$$

$$\theta_{13} = 0$$

# Constraints

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- Relic Density
- Collider bounds
- EW precision
- Vacuum stability
- ...

# The Model

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Is it possible to have non trivial rep for charged leptons (and quarks)?

**G:**  $r_a$  and  $r_b$  with  $\dim(r_{a,b}) > 1$

$G \supset Z_N$  **DM stability**

$$\Delta(54) \sim (Z_3 \times Z_3) \rtimes S_3$$

triplets                      Four       $\mathbf{2}_{1,2,3,4}$                       Two singlets                       $\mathbf{1}_{\pm}$

$$\mathbf{2}_k \times \mathbf{2}_k = \mathbf{1}_+ + \mathbf{1}_- + \mathbf{2}_k$$

$$P \equiv (Z_3 \times Z_3)$$

$$\mathbf{2}_1 \times \mathbf{2}_2 = \mathbf{2}_3 + \mathbf{2}_4$$

$$\mathbf{2}_3 \sim (\chi_1, \chi_2)$$

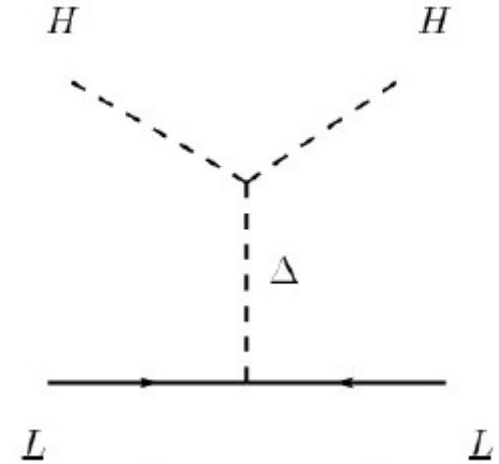
$$\chi_1 (\omega^2, \omega)$$

$$\chi_2 (\omega, \omega^2)$$

# The Model

S. Boucenna, S. Morisi, E. Peinado, Yusuke Shimizu and J. W. F. Valle  
 arXiv:1204.4733 [hep-ph]

	$\bar{L}_e$	$\bar{L}_D$	$e_R$	$l_D$	$H$	$\chi$	$\eta$	$\Delta$
$SU(2)$	2	2	1	1	2	2	2	3
$\Delta(54)$	$1_+$	$2_1$	$1_+$	$2_1$	$1_+$	$2_1$	$2_3$	$2_1$



$$\langle \Delta \rangle \sim (1, 1) \text{ and } \langle \chi_1 \rangle \neq \langle \chi_2 \rangle$$

$$r = \langle \chi_2 \rangle / \langle \chi_1 \rangle$$

$$M_\ell = \begin{pmatrix} a & br & b \\ cr & d & e \\ c & e & dr \end{pmatrix}$$

$$M_\nu \propto \begin{pmatrix} 0 & \delta & \delta \\ \delta & \alpha & 0 \\ \delta & 0 & \alpha \end{pmatrix}$$

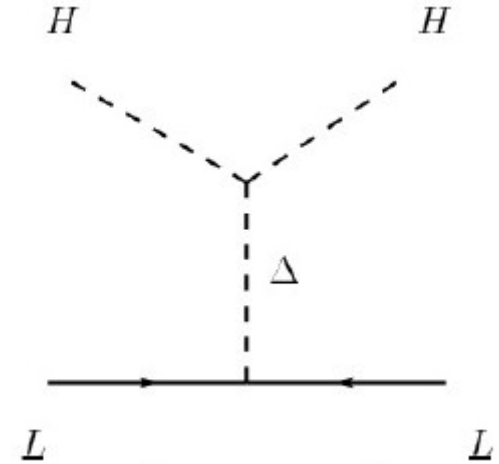
**Mass sum rule**

$$m_1^\nu + m_2^\nu = m_3^\nu$$

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**Mass sum rule**

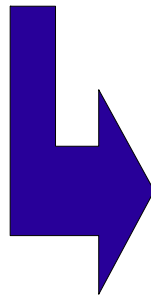
L. Dorame, D. Meloni, S. Morisi, EP and J. Valle,  
 1111.5614  
 J. Barry and W. Rodejohann, Nucl.Phys. B842, 33  
 (2011), 1007.5217

# The Model

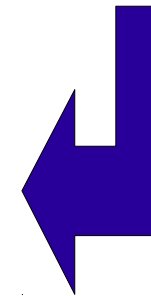
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	$Q_{1,2}$	$Q_3$	$(u_R, c_R)$	$t_R$	$d_R$	$s_R$	$b_R$
$SU(2)$	2	2	1	1	1	1	1
$\Delta(54)$	$\mathbf{2}_1$	$\mathbf{1}_+$	$\mathbf{2}_1$	$\mathbf{1}_+$	$\mathbf{1}_-$	$\mathbf{1}_+$	$\mathbf{1}_+$

$$M_d = \begin{pmatrix} ra_d & rb_d & rd_d \\ -a_d & b_d & dd \\ 0 & c_d & ed \end{pmatrix}, \quad M_u = \begin{pmatrix} ra_u & b_u & du \\ b_u & a_u & rdu \\ c_u & rc_u & eu \end{pmatrix}$$



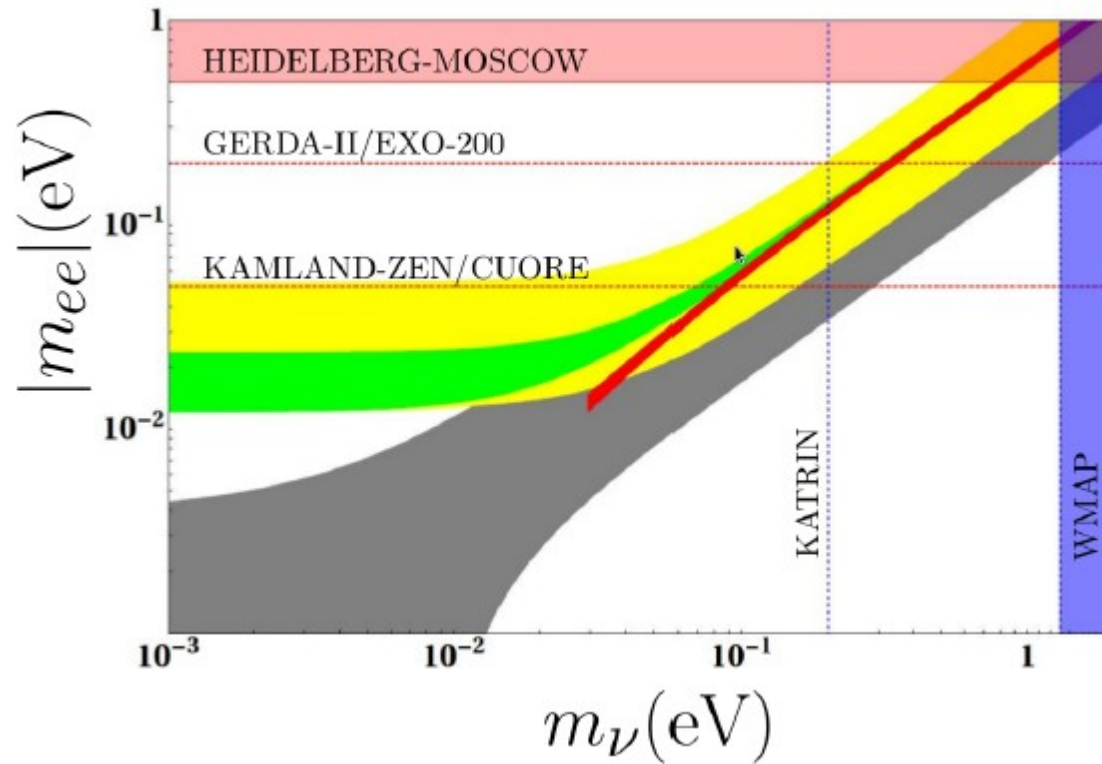
$$0.1 < r < 0.2$$





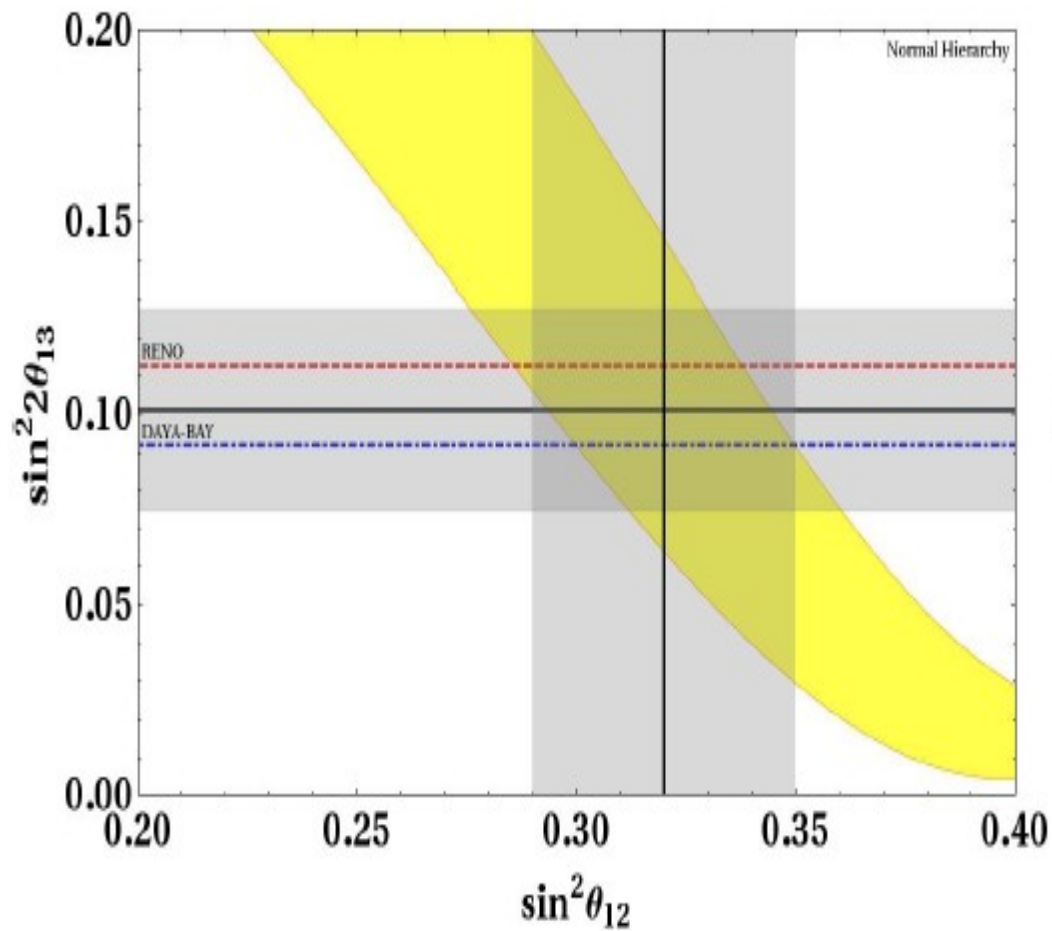
# Correlations

$$m_1^\nu + m_2^\nu = m_3^\nu$$

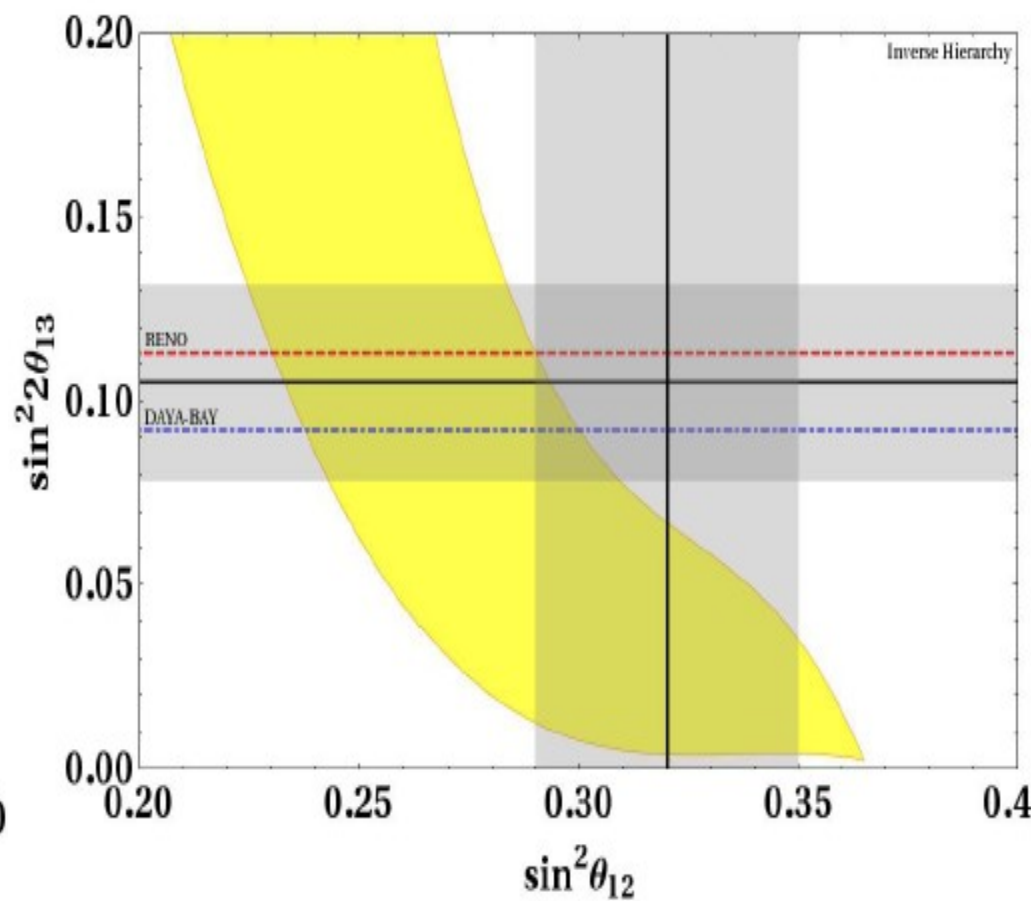


# Correlations

NI



IH



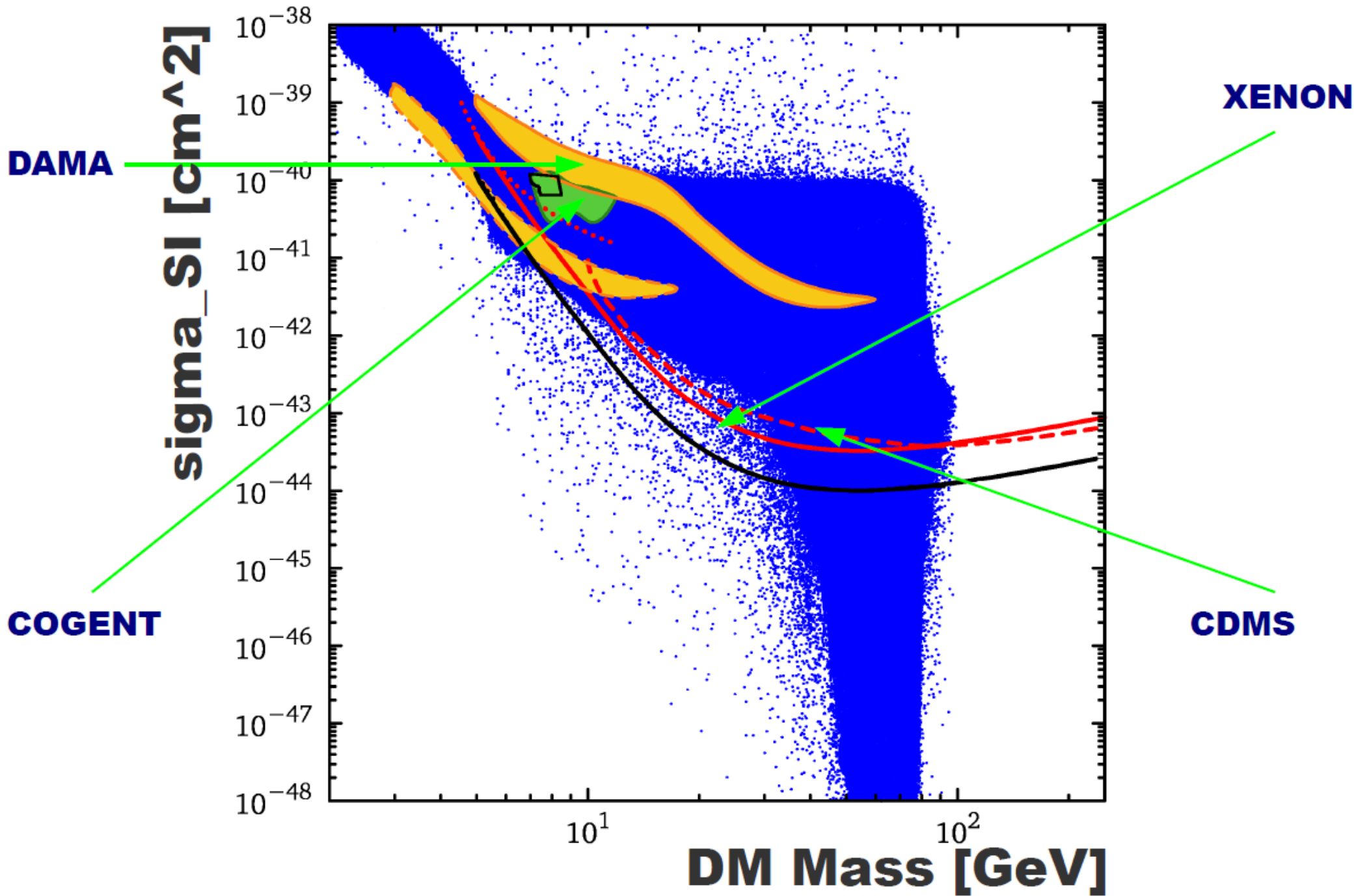
# Conclusions

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**Non-Abelian Flavor Symmetries** are useful to explain the patterns of masses and mixings of neutrinos: **Reduce** the **number of** free **parameters** in the SM

{ **Predictive** }

We show that are also **useful** to explain the **DM** in the Universe:  
Also with a rich phenomenology



... Direct Detection

