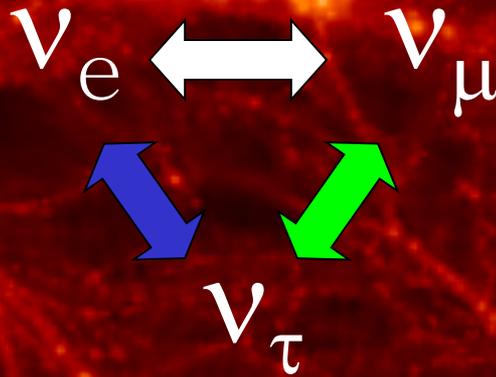


NEUTRINO PHYSICS AND COSMOLOGY



STEEN HANNESTAD, Aarhus University
PASCOS, 6 JUNE 2012

FLAVOUR STATES

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = U \begin{pmatrix} \nu_1(m_1) \\ \nu_2(m_2) \\ \nu_3(m_3) \end{pmatrix}$$

PROPAGATION STATES

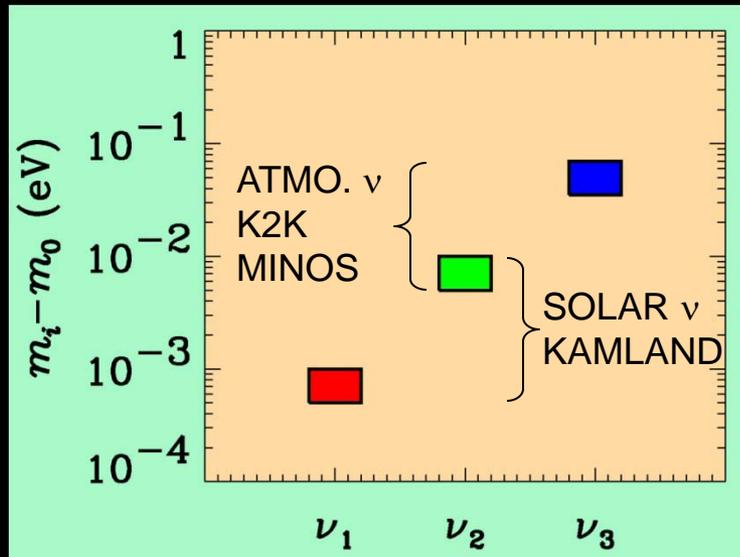
MIXING MATRIX (UNITARY)

$$U = \begin{bmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{12}e^{-i\delta} \\ s_{12}c_{23} - c_{12}s_{23}e^{-i\delta} & c_{12}c_{23} - s_{12}s_{23}e^{-i\delta} & s_{23}e^{-i\delta} \\ s_{12}s_{23} + c_{12}c_{23}e^{-i\delta} & c_{12}s_{23} - s_{12}c_{23}e^{-i\delta} & c_{23}e^{-i\delta} \end{bmatrix}$$

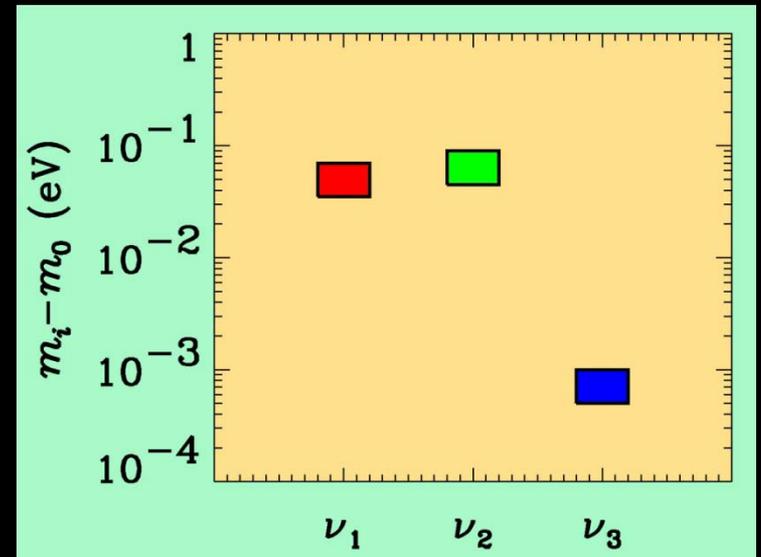
LATE-TIME COSMOLOGY IS (ALMOST) INSENSITIVE TO THE MIXING STRUCTURE

$\cos \theta_{12}$
 $\sin \theta_{12}$

If neutrino masses are hierarchical then oscillation experiments do not give information on the absolute value of neutrino masses



Normal hierarchy



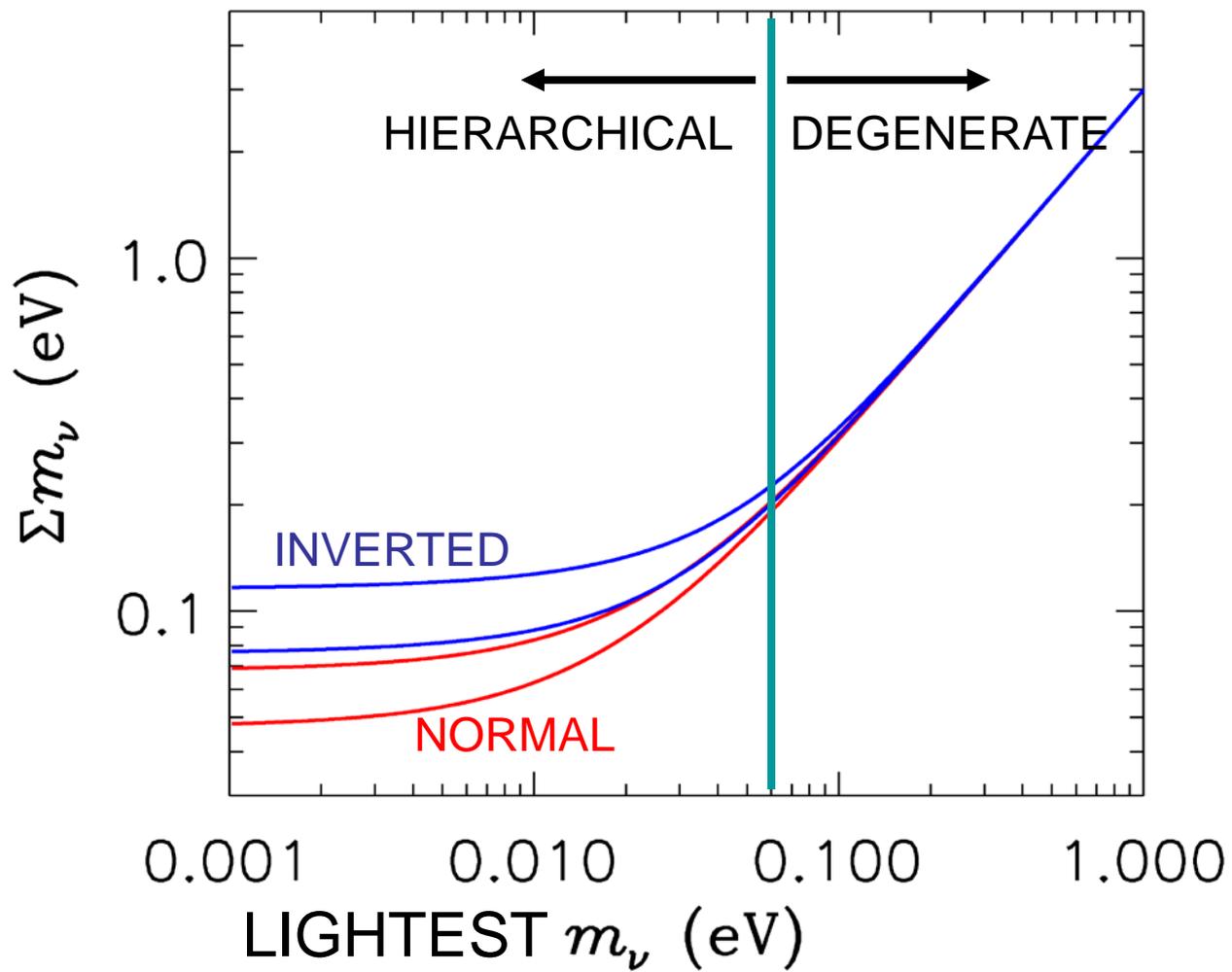
Inverted hierarchy

However, if neutrino masses are degenerate

$$m_0 \gg \delta m_{\text{atmospheric}}$$

no information can be gained from such experiments.

Experiments which rely on either the kinematics of neutrino mass or the spin-flip in neutrinoless double beta decay are the most efficient for measuring m_0



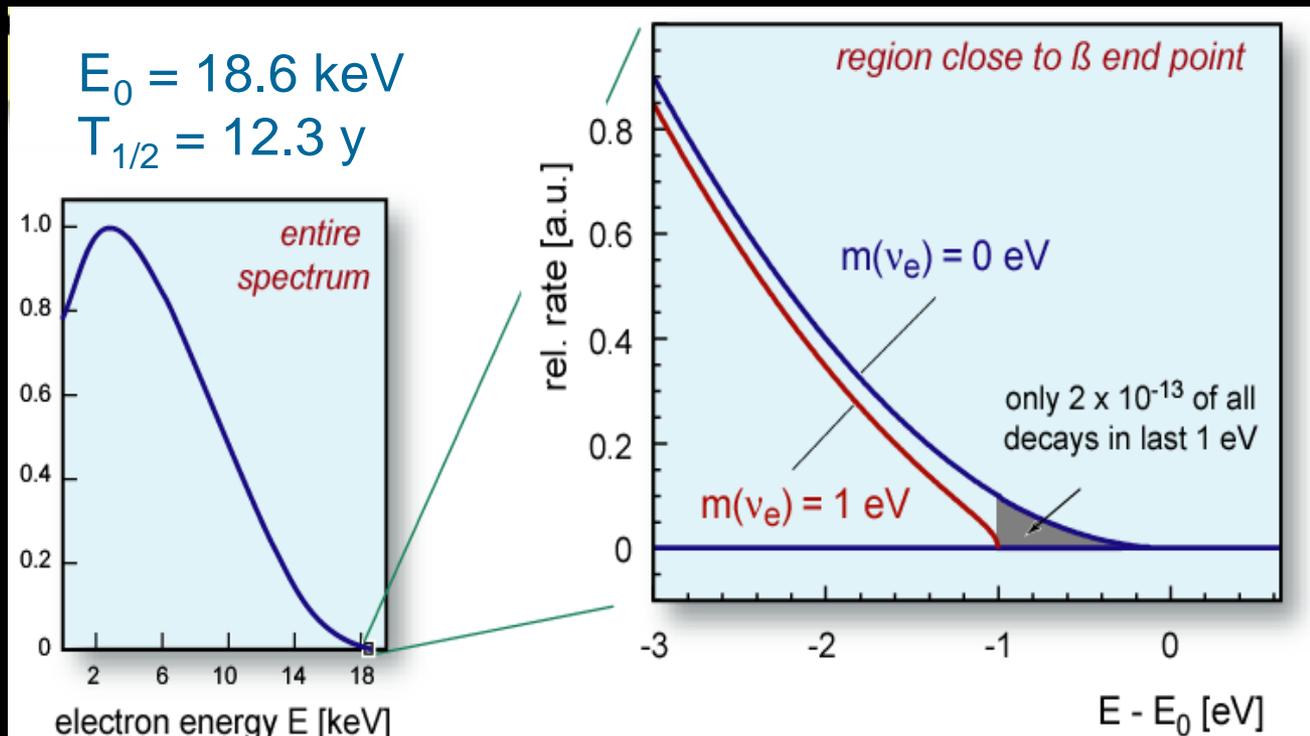
β -decay and neutrino mass

model independent neutrino mass from β -decay kinematics

only assumption: relativistic energy-momentum relation

$$\frac{d\Gamma_i}{dE} = C p (E + m_e) (E_0 - E) \sqrt{(E_0 - E)^2 - m_i^2} F(E) \theta(E_0 - E - m_i)$$

experimental \downarrow observable is m_ν^2



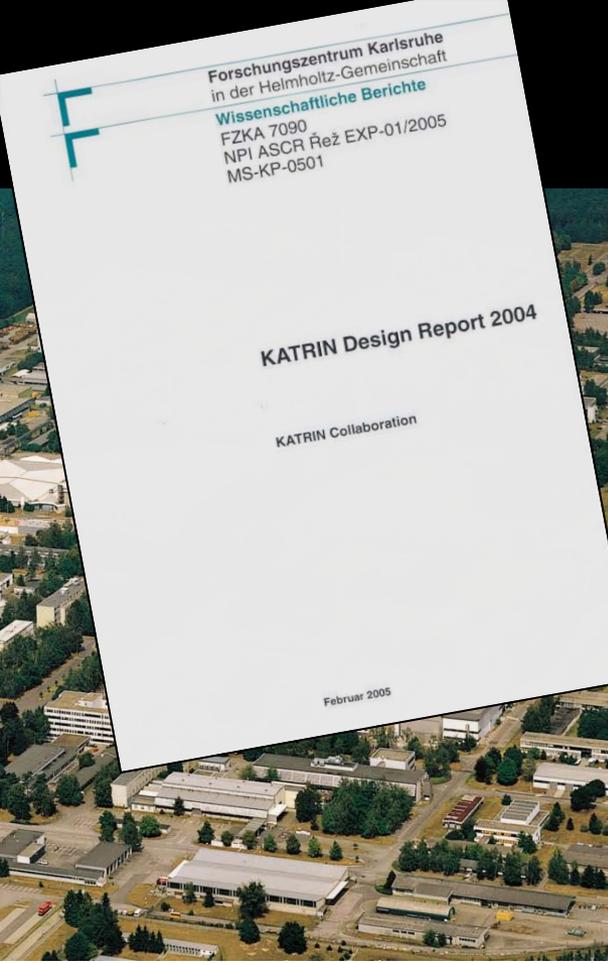
Tritium decay endpoint measurements have provided limits on the electron neutrino mass

$$m_{\nu_e} = \left(\sum |U_{ei}|^2 m_i^2 \right)^{1/2} \leq 2.3 \text{ eV} \quad (95\%)$$

Mainz experiment, final analysis (Kraus et al.)

This translates into a limit on the sum of the three mass eigenstates

$$\sum m_i \leq 7 \text{ eV}$$

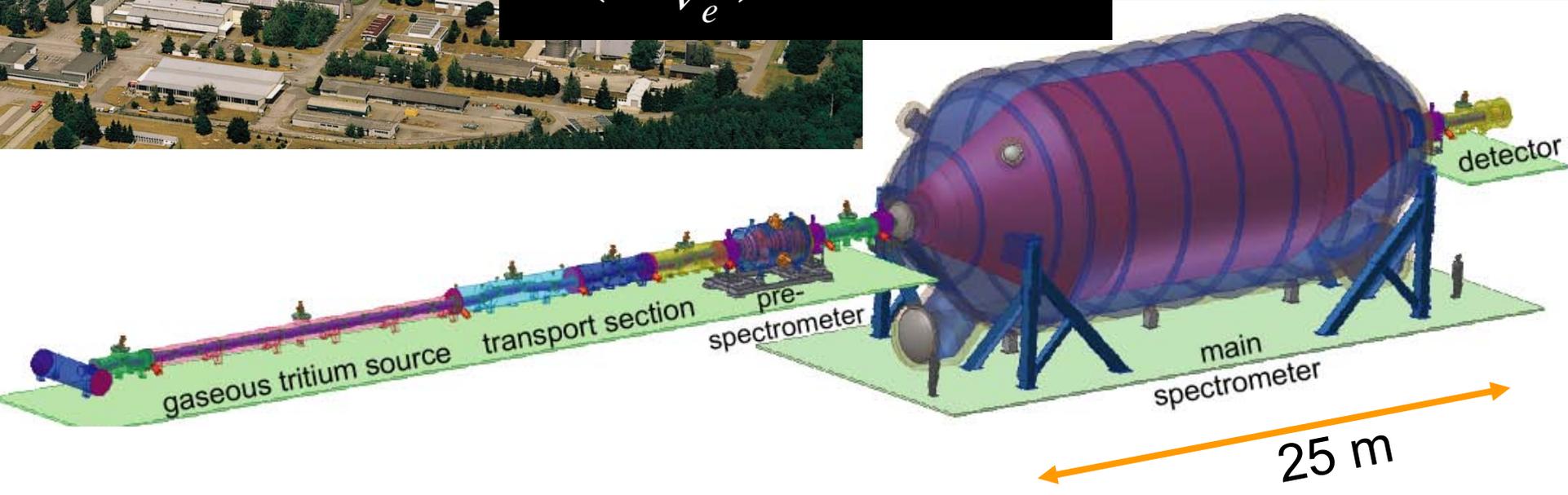


KATRIN experiment



Karlsruhe Tritium Neutrino Experiment
at Forschungszentrum Karlsruhe
Data taking starting 2013

$$\sigma(m_{\nu_e}) \sim 0.2 \text{ eV}$$



NEUTRINO MASS AND ENERGY DENSITY FROM COSMOLOGY

NEUTRINOS AFFECT STRUCTURE FORMATION
BECAUSE THEY ARE A SOURCE OF DARK MATTER
($n \sim 100 \text{ cm}^{-3}$)

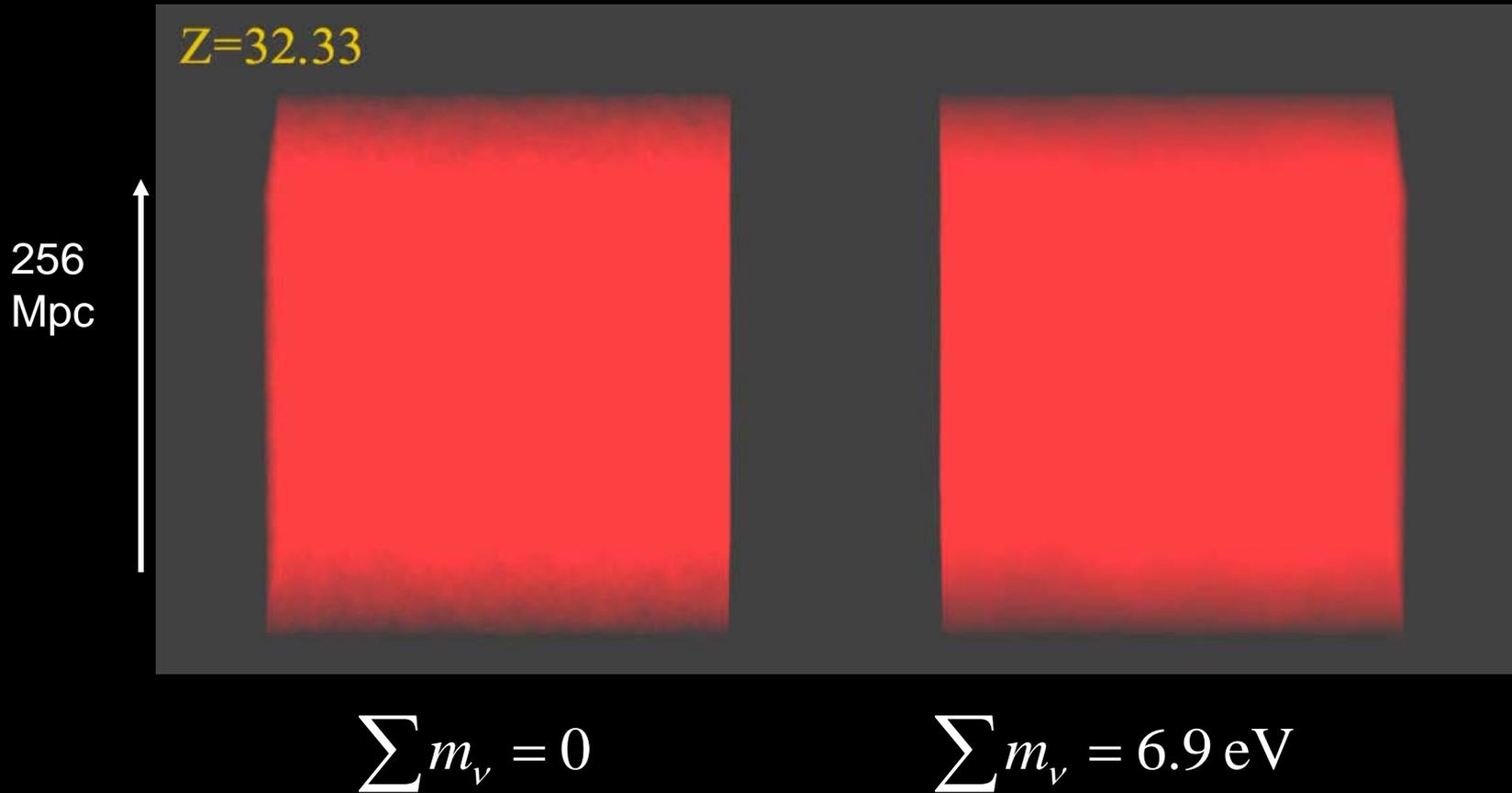
$$\Omega_\nu h^2 = \frac{\sum m_\nu}{93 \text{ eV}} \quad \text{FROM} \quad T_\nu = T_\gamma \left(\frac{4}{11} \right)^{1/3} \approx 2 \text{ K}$$

HOWEVER, eV NEUTRINOS ARE DIFFERENT FROM CDM
BECAUSE THEY FREE STREAM

$$d_{\text{FS}} \sim 1 \text{ Gpc } m_{\text{eV}}^{-1}$$

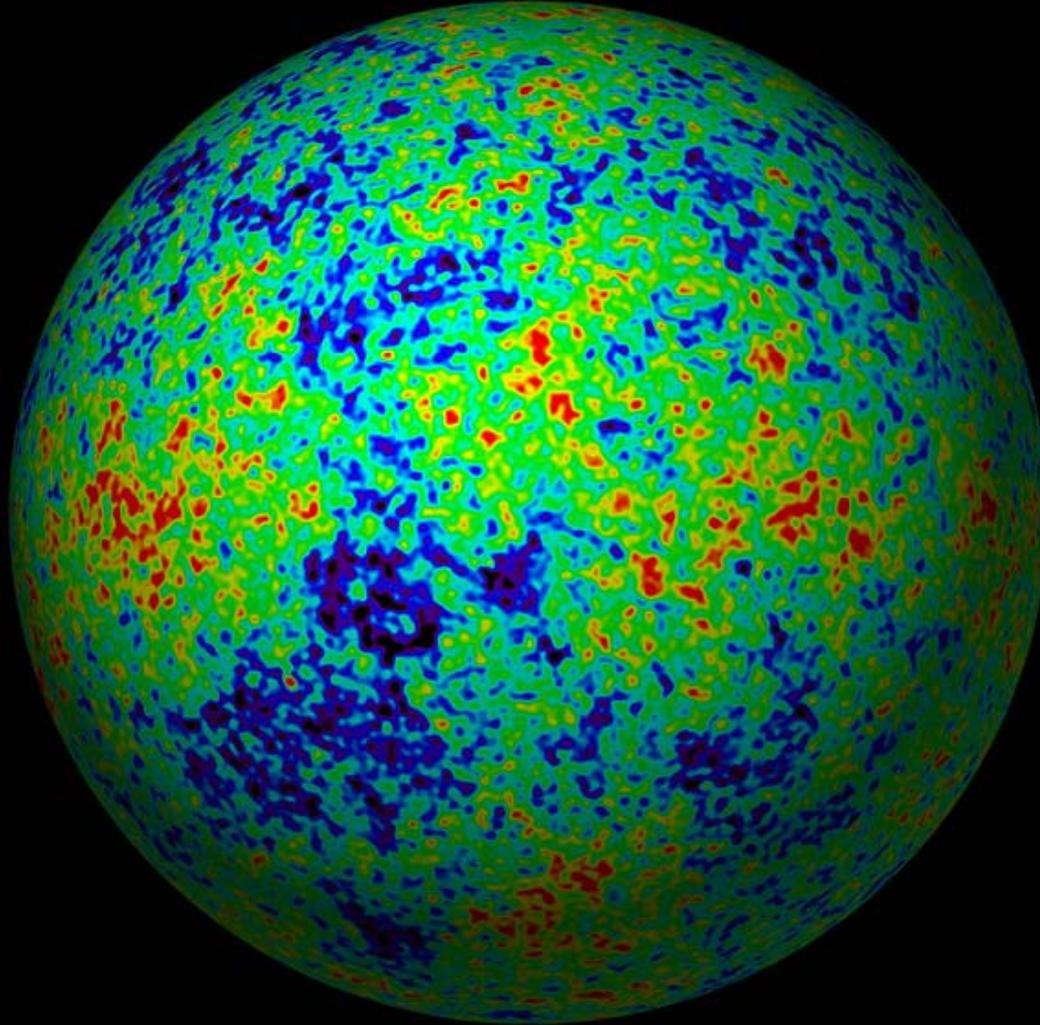
SCALES SMALLER THAN d_{FS} DAMPED AWAY, LEADS TO
SUPPRESSION OF POWER ON SMALL SCALES

N-BODY SIMULATIONS OF Λ CDM WITH AND WITHOUT NEUTRINO MASS (768 Mpc³) – GADGET 2



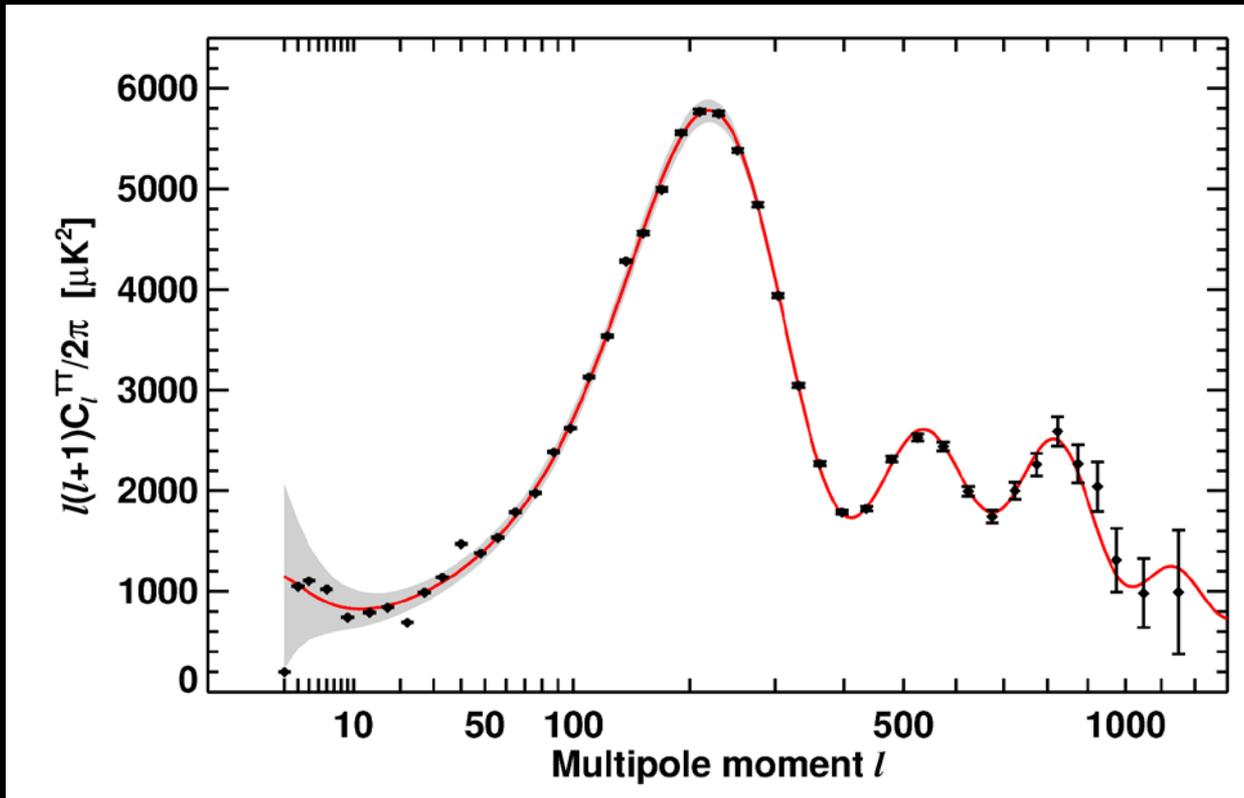
AVAILABLE COSMOLOGICAL DATA

THE COSMIC MICROWAVE BACKGROUND



WMAP TEMPERATURE MAP

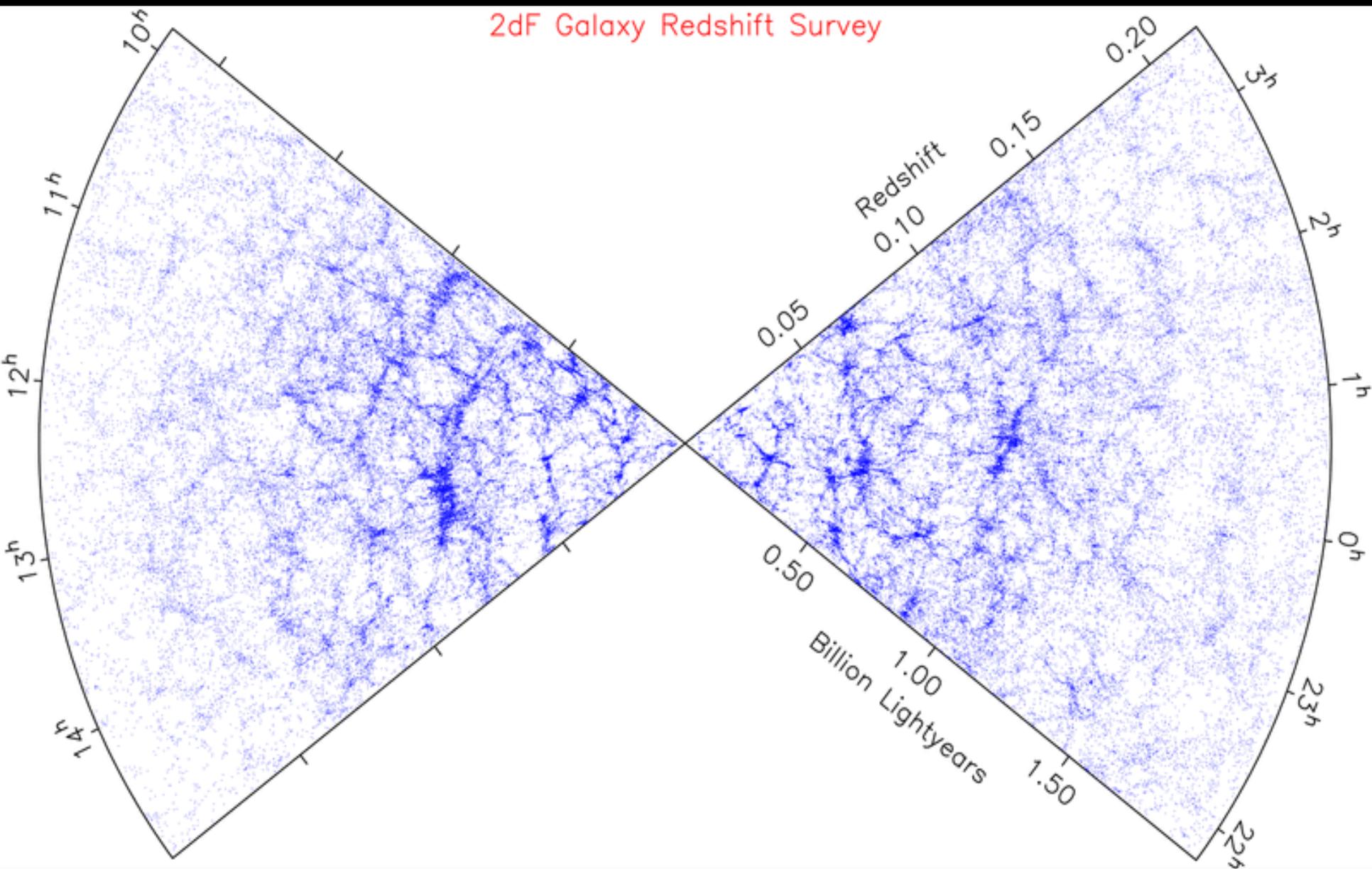
WMAP-7 TEMPERATURE POWER SPECTRUM



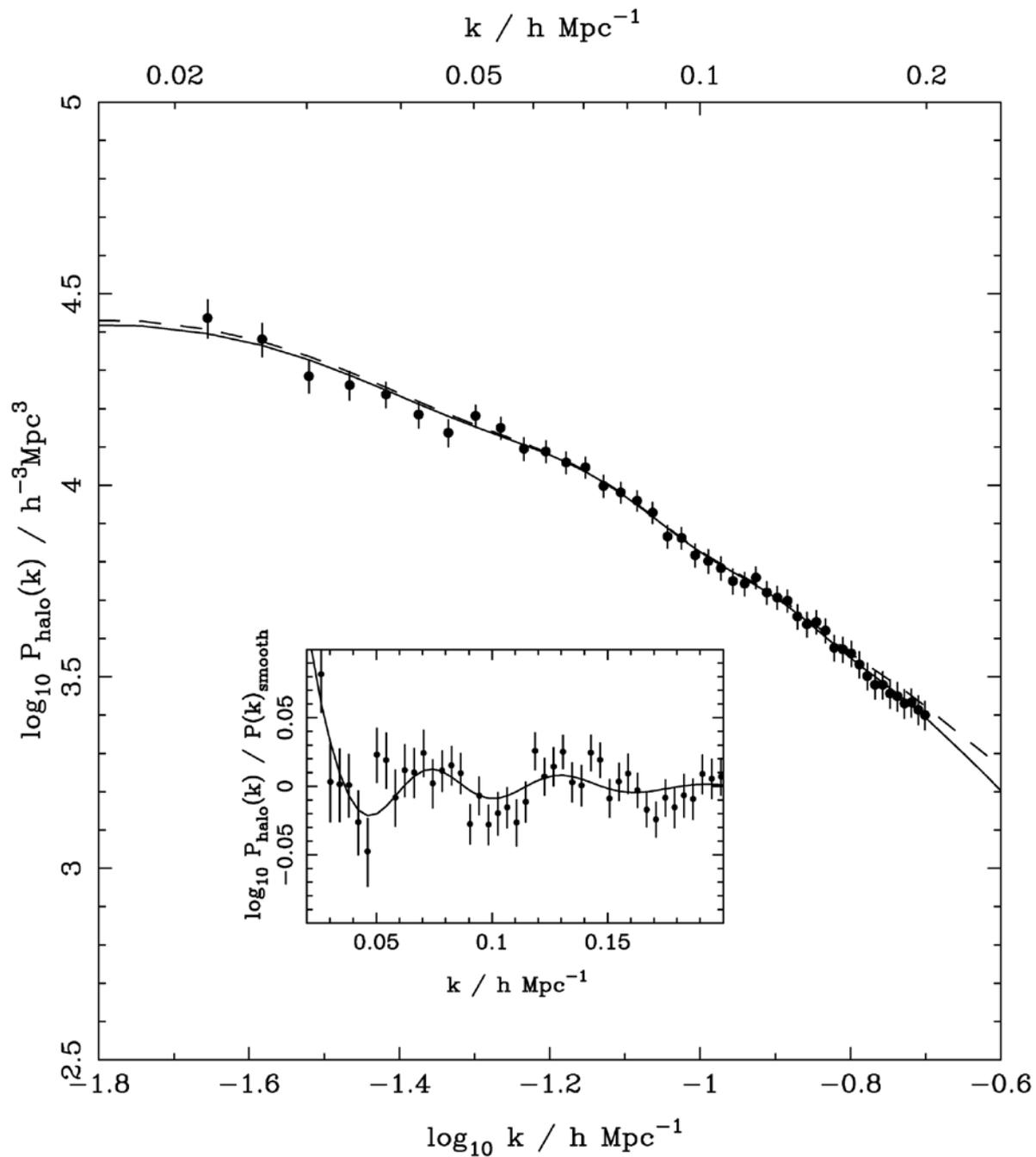
LARSON ET AL, ARXIV 1001.4635

ADDITIONAL DATA ON SMALLER SCALES FROM
ATACAMA COSMOLOGY TELESCOPE (Dunkley et al. 2011)
SOUTH POLE TELESCOPE (Keisler et al. 2011)

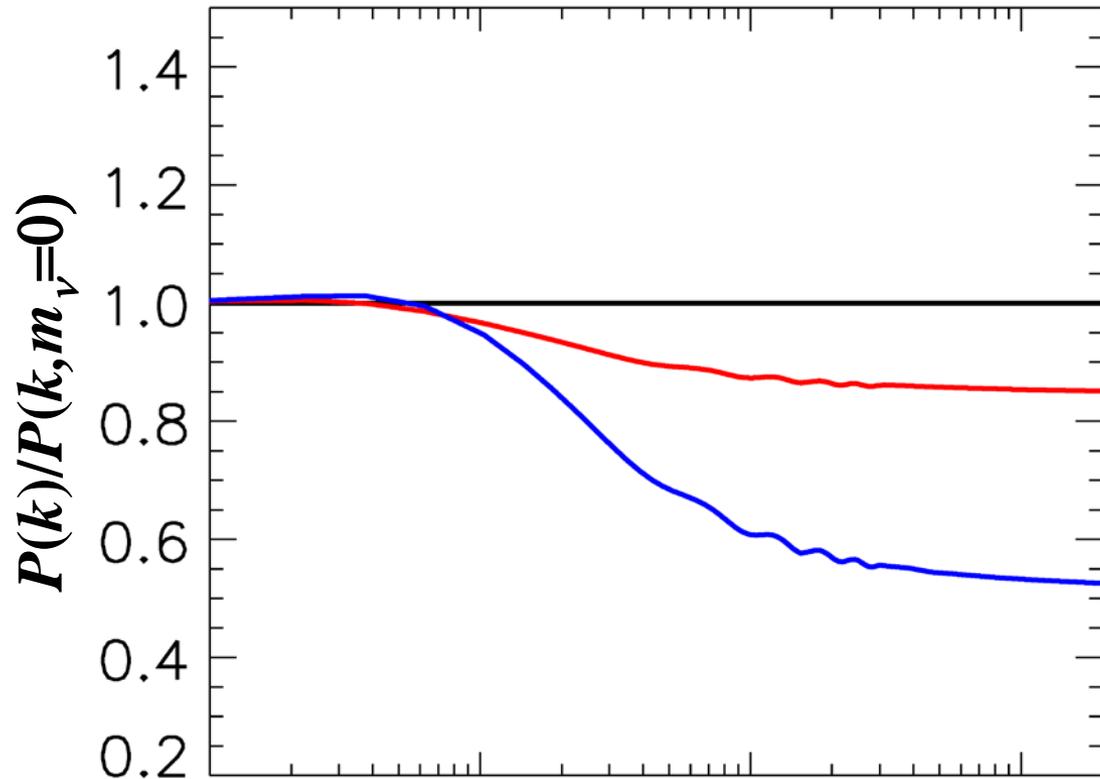
LARGE SCALE STRUCTURE SURVEYS - 2dF AND SDSS



SDSS DR-7
LRG SPECTRUM
(Reid et al '09)



FINITE NEUTRINO MASSES SUPPRESS THE MATTER POWER SPECTRUM ON SCALES SMALLER THAN THE FREE-STREAMING LENGTH



$\Sigma m = 0 \text{ eV}$

$\Sigma m = 0.3 \text{ eV}$

$\Sigma m = 1 \text{ eV}$

$$\frac{\Delta P}{P_{m=0}} (k \gg k_{FS}) \sim -8 \frac{\rho_\nu}{\rho_{TOT}} \frac{1}{k \text{ (h/Mpc)}}$$

NOW, WHAT ABOUT NEUTRINO
PHYSICS?

WHAT IS THE PRESENT BOUND ON THE NEUTRINO MASS?

DEPENDS ON DATA SETS USED AND ALLOWED PARAMETERS

THERE ARE MANY ANALYSES IN THE LITERATURE

$$\sum m_\nu \leq 0.44 \text{ eV @ 95 C.L.} \quad \text{USING THE MINIMAL COSMOLOGICAL MODEL}$$

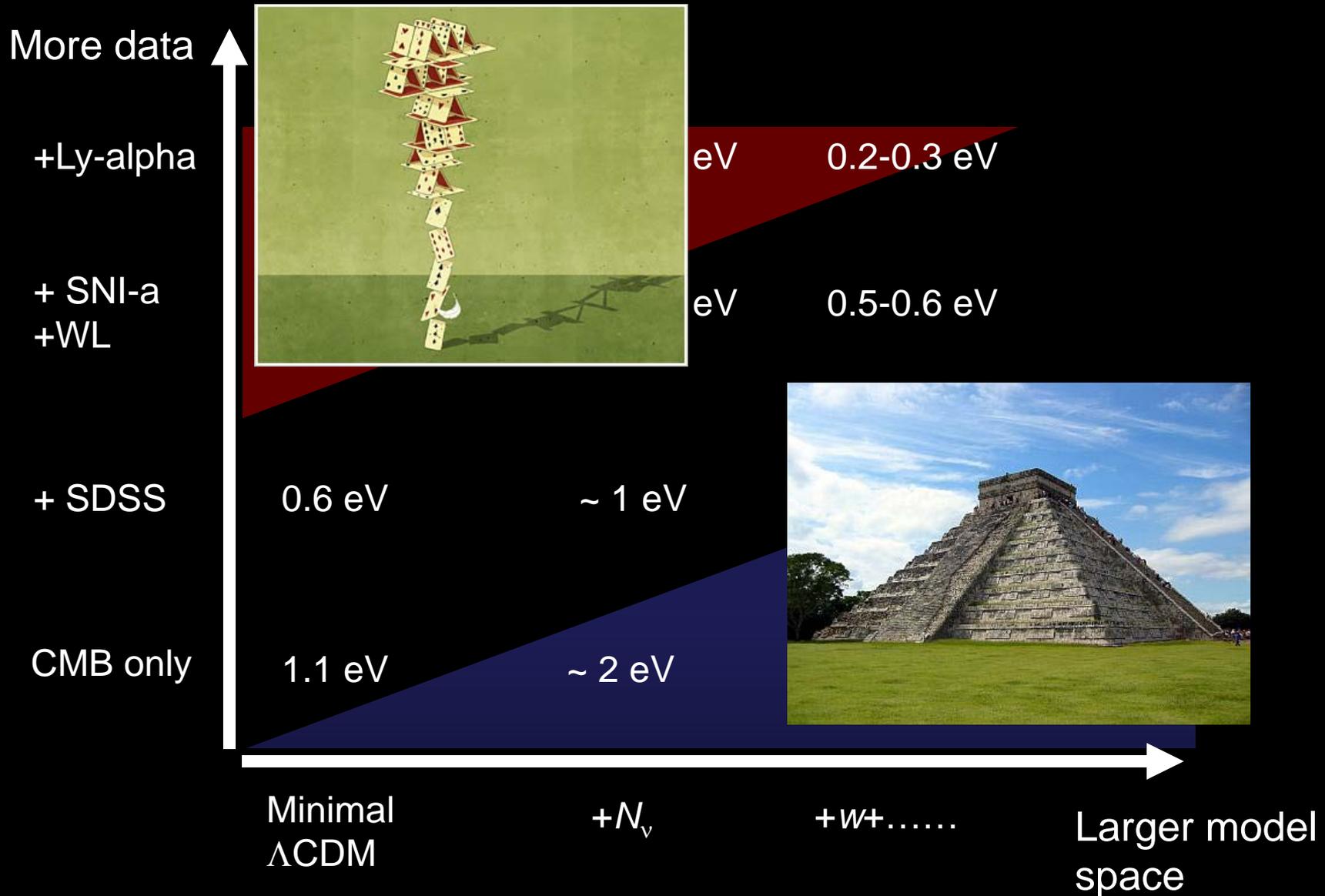
STH, MIRIZZI, RAFFELT, WONG (arxiv:1004:0695)

HAMANN, STH, LESGOURGUES, RAMPF & WONG (arxiv:1003.3999)

JUST ONE EXAMPLE

TALK BY E. GIUSARMA FOR A MORE RECENT ANALYSIS

THE NEUTRINO MASS FROM COSMOLOGY PLOT



Model	Observables	Σm_ν (eV) 95% Bound
$\omega\text{CDM} + \Delta N_{\text{rel}} + m_\nu$	CMB+H0+SN+BAO	≤ 1.5
$\omega\text{CDM} + \Delta N_{\text{rel}} + m_\nu$	CMB+H0+SN+LSSPS	≤ 0.76
$\Lambda\text{CDM} + m_\nu$	CMB+H0+SN+BAO	≤ 0.61
$\Lambda\text{CDM} + m_\nu$	CMB+H0+SN+LSSPS	≤ 0.36
$\Lambda\text{CDM} + m_\nu$	CMB (+SN)	≤ 1.2
$\Lambda\text{CDM} + m_\nu$	CMB+BAO	≤ 0.75
$\Lambda\text{CDM} + m_\nu$	CMB+LSSPS	≤ 0.55
$\Lambda\text{CDM} + m_\nu$	CMB+H0	≤ 0.45

WHAT IS N_ν ?

A MEASURE OF THE ENERGY DENSITY IN NON-INTERACTING RADIATION IN THE EARLY UNIVERSE

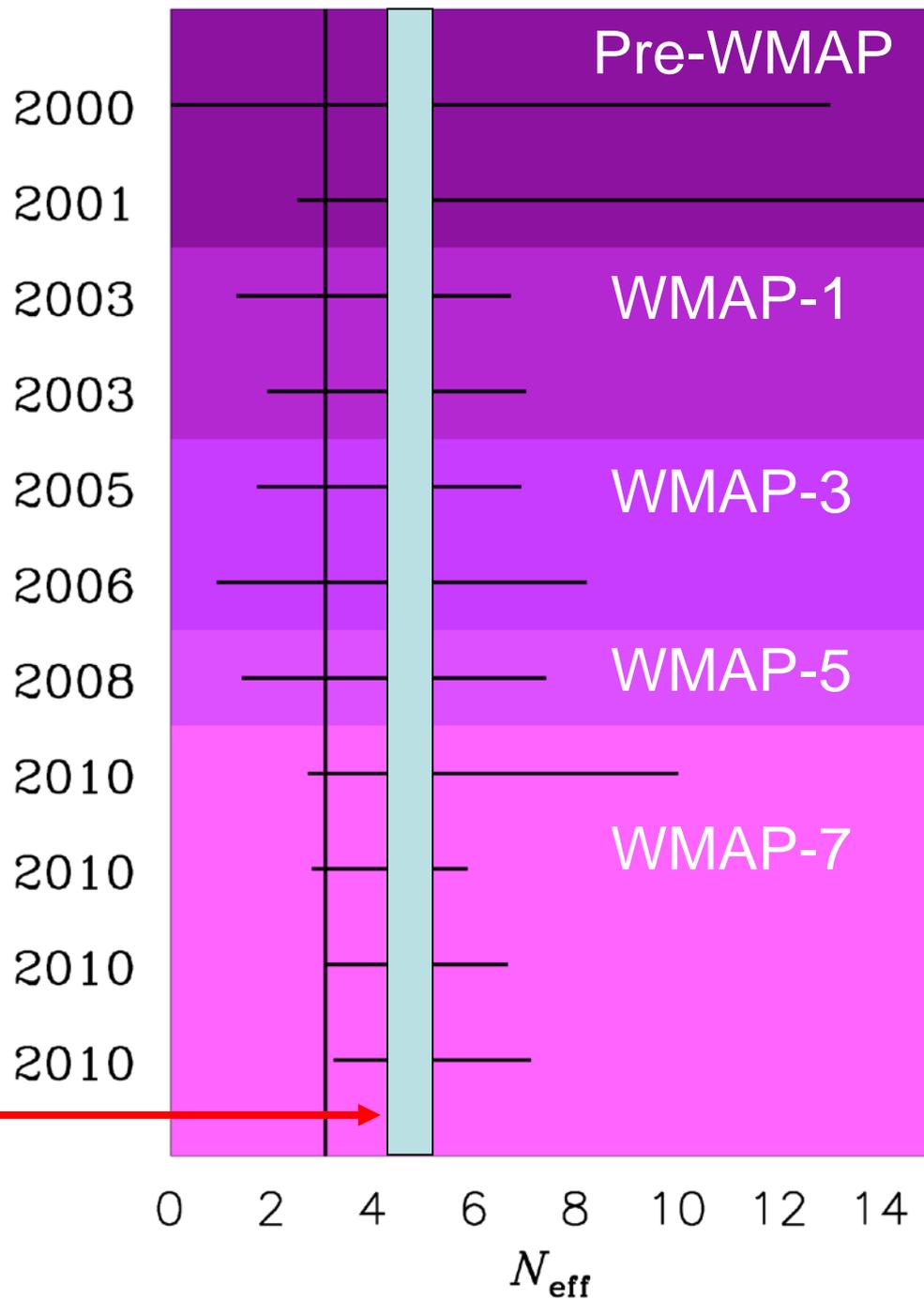
THE STANDARD MODEL PREDICTION IS

$$N_\nu \equiv \frac{\rho}{\rho_{\nu,0}} = 3.046 \quad , \quad \rho_{\nu,0} \equiv \frac{7}{8} \left(\frac{4}{11} \right)^{4/3} \rho_\gamma$$

Mangano et al., hep-ph/0506164

BUT ADDITIONAL LIGHT PARTICLES (STERILE NEUTRINOS, AXIONS, MAJORONS,.....) COULD MAKE IT HIGHER

TIME EVOLUTION OF
THE 95% BOUND ON
 N_{ν}



ESTIMATED PLANCK
SENSITIVITY



MOST RECENT ANALYSIS (THIS WEEK)
 ARCHIDIACONO ET AL. ARXIV:1206.0109

	Baseline model	BaselineSPT model	BaselineSPT-SNIa model
w	-0.76 ± 0.15	-0.85 ± 0.12	-0.85 ± 0.12
N_{eff}	$5.82^{+0.60+2.71}_{-0.84-2.12}$	$4.38^{+0.27+1.07}_{-0.31-0.98}$	$4.29^{+0.26+1.05}_{-0.31-0.96}$
c_{vis}^2	$0.21^{+0.10+0.21}_{-0.10-0.18}$	$0.24^{+0.032+0.17}_{-0.052-0.13}$	$0.25^{+0.03+0.42}_{-0.06-0.13}$
c_{eff}^2	$0.35^{+0.01+0.05}_{-0.02-0.05}$	$0.33^{+0.006+0.024}_{-0.007-0.024}$	$0.33^{+0.01+0.02}_{-0.01-0.03}$
n_s	0.976 ± 0.026	0.982 ± 0.024	0.980 ± 0.024

A STERILE NEUTRINO IS PERHAPS THE MOST OBVIOUS CANDIDATE FOR AN EXPLANATION OF THE EXTRA ENERGY DENSITY

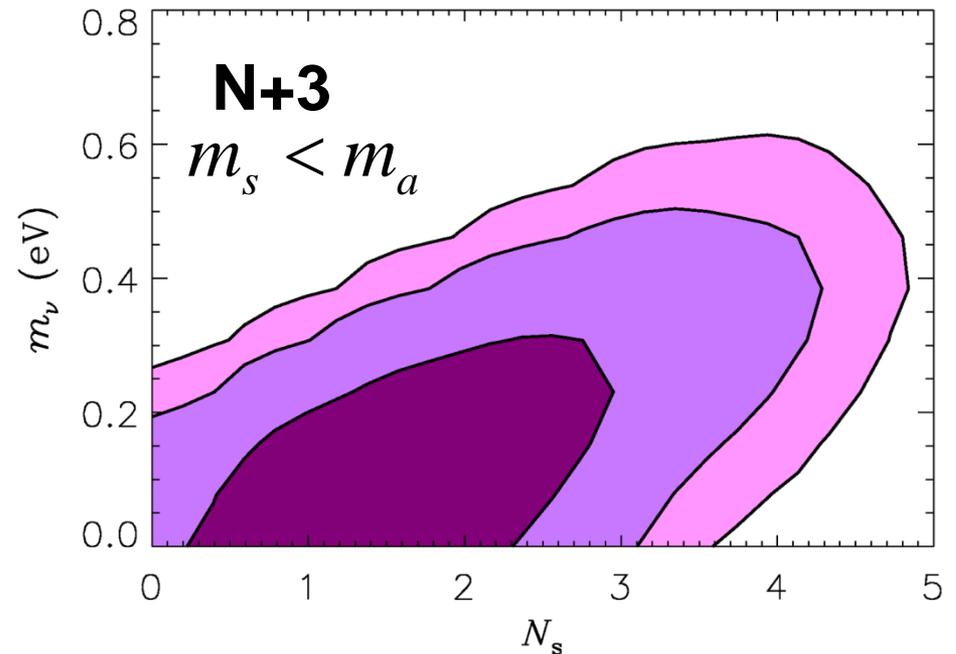
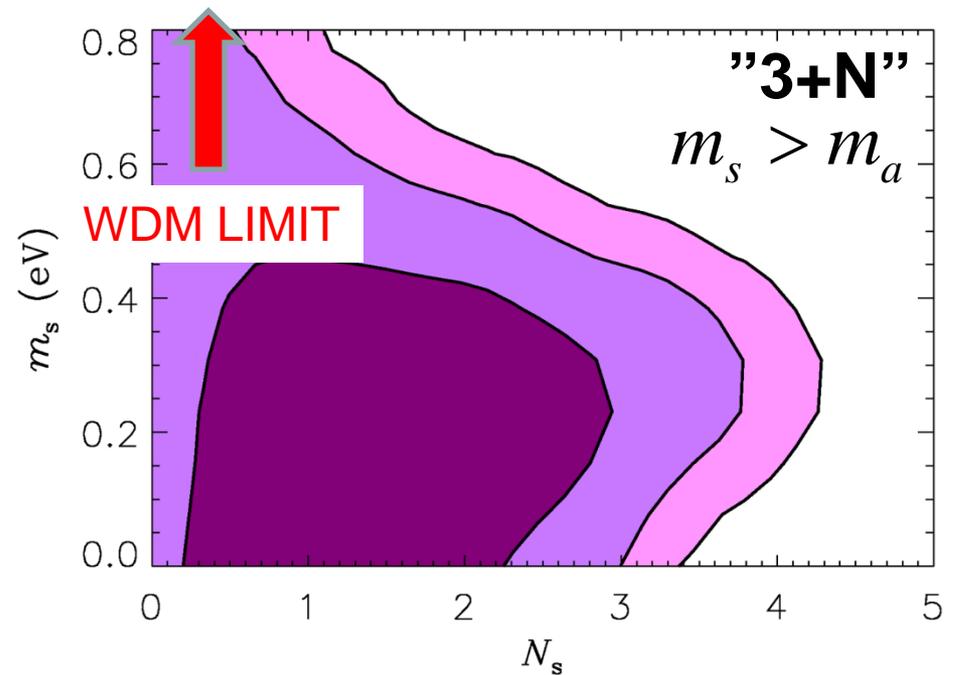
ASSUMING A NUMBER OF ADDITIONAL STERILE STATES OF APPROXIMATELY EQUAL MASS, TWO QUALITATIVELY DIFFERENT HIERARCHIES EMERGE



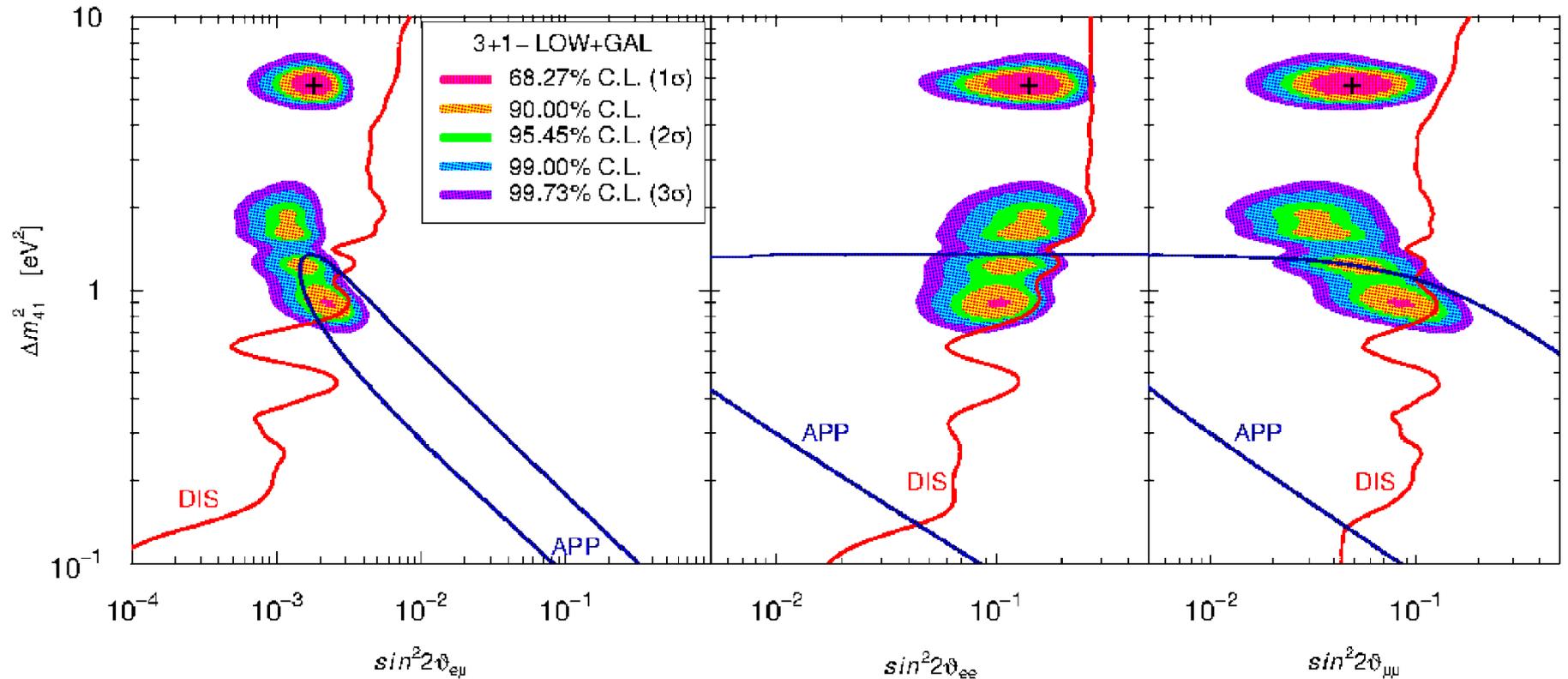
Hamann, STH, Raffelt, Tamborra,
Wong, arxiv:1006.5276 (PRL)

COSMOLOGY AT PRESENT
NOT ONLY MARGINALLY
PREFERS EXTRA ENERGY
DENSITY, BUT ALSO ALLOWS
FOR QUITE HIGH NEUTRINO
MASSES!

See also
Dodelson et al. 2006
Melchiorri et al. 2009
Acero & Lesgourgues 2009



THERE ARE A NUMBER OF HINTS FROM EXPERIMENTS THAT A FOUR eV-MASS STERILE STATE MIGHT BE NEEDED:
LSND, MiniBoone, reactor anomaly, Gallium (see talk by De Gouvea)



Giunti & Laveder 2011 (and many other recent analyses)

HOW DO THESE TWO HINTS FIT TOGETHER? CAN THEY BE EXPLAINED BY THE SAME PHYSICS?

SHORT ANSWER: IT IS DIFFICULT WITHOUT MODIFYING COSMOLOGY

3 standard + 1 sterile

$$m_s < 0.48 \text{ eV} \quad (95 \text{ \% C.I.})$$

Hamann et al. 2010

Global oscillations
best-fit:

$$m_s \geq 1 \text{ eV}$$

Kopp, Maltoni & Schwetz 2011

3 standard + 2 sterile

$$m_{s1} + m_{s2} < 0.9 \text{ eV} \quad (95 \text{ \% C.I.})$$

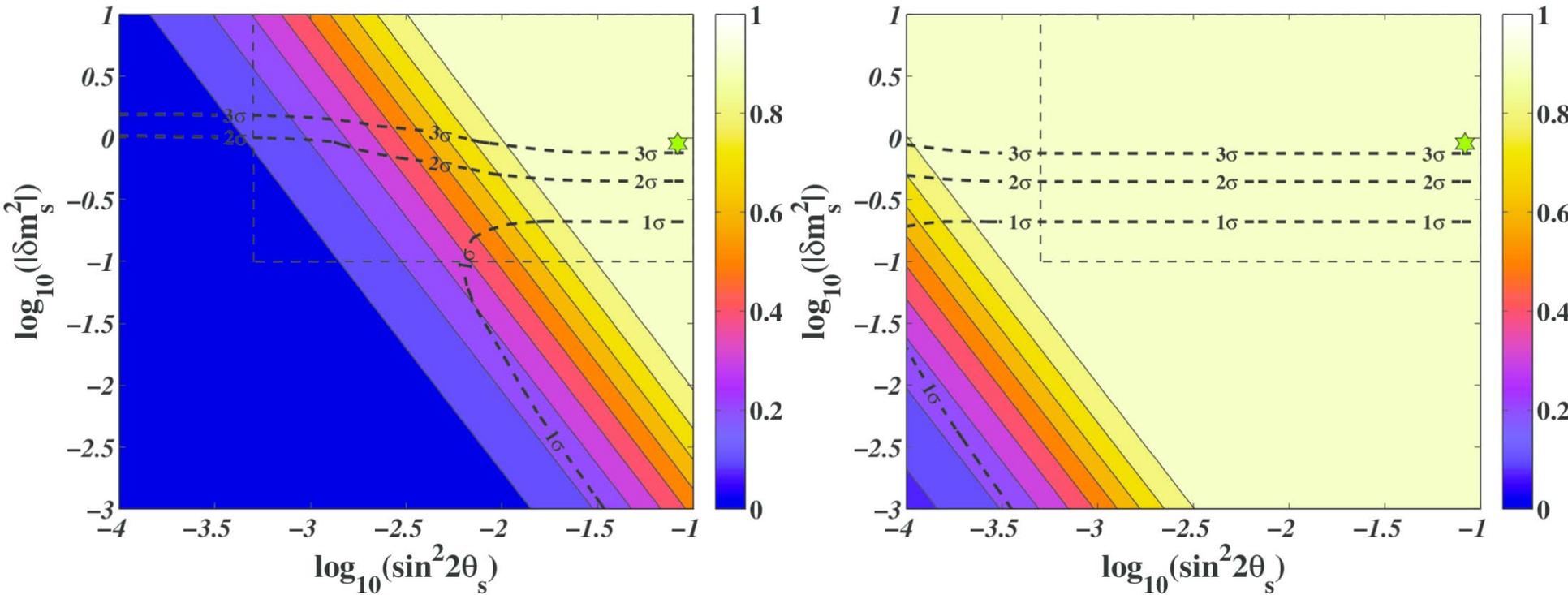
Global oscillations
best-fit:

$$m_{s1} \geq 0.7 \text{ eV}$$
$$m_{s2} \geq 0.9 \text{ eV}$$

MODIFYING FOR EXAMPLE THE DARK ENERGY EQUATION OF STATE CAN HELP, BUT THE 3+2 MODEL IS STRONGLY DISFAVOURLED

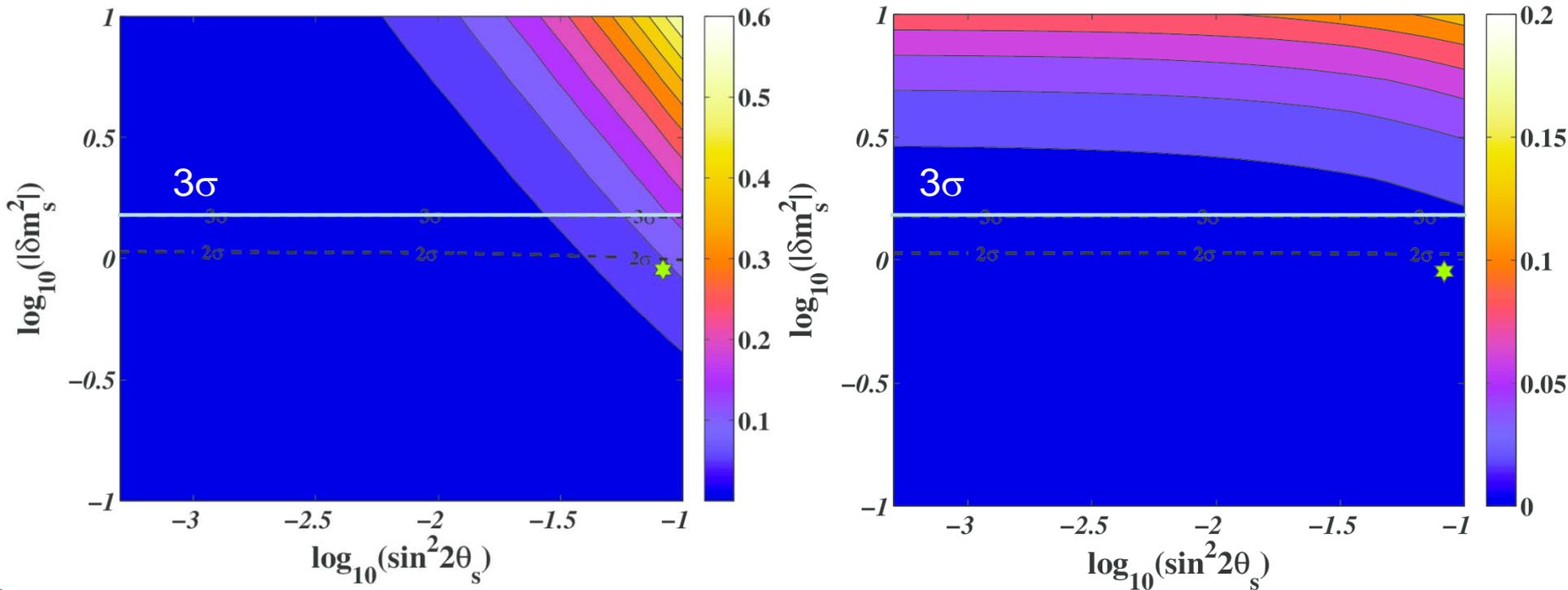
A LARGE PRIMORDIAL LEPTON ASYMMETRY CAN RECONCILE THE DATA (STH, Tamborra, Tram 2012) (Talk by Thomas Tram)

STERILE NEUTRINO THERMALISATION WITH ZERO LEPTON ASYMMETRY



STH, Tamborra, Tram 2012

STERILE NEUTRINO THERMALISATION WITH LARGE LEPTON ASYMMETRY

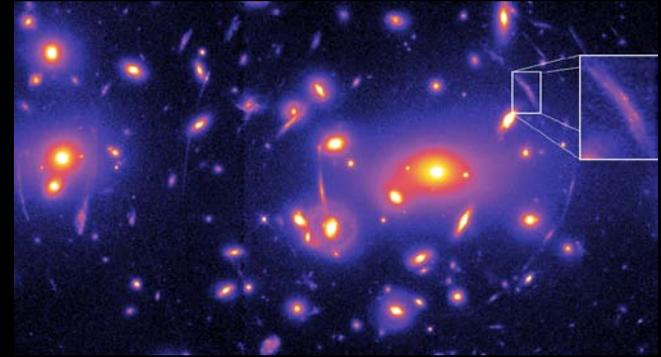
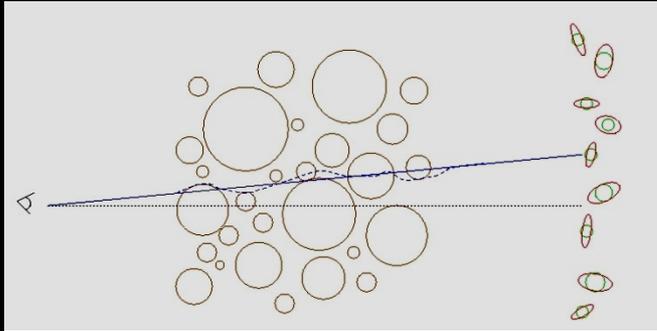


STH, Tamborra, Tram 2012

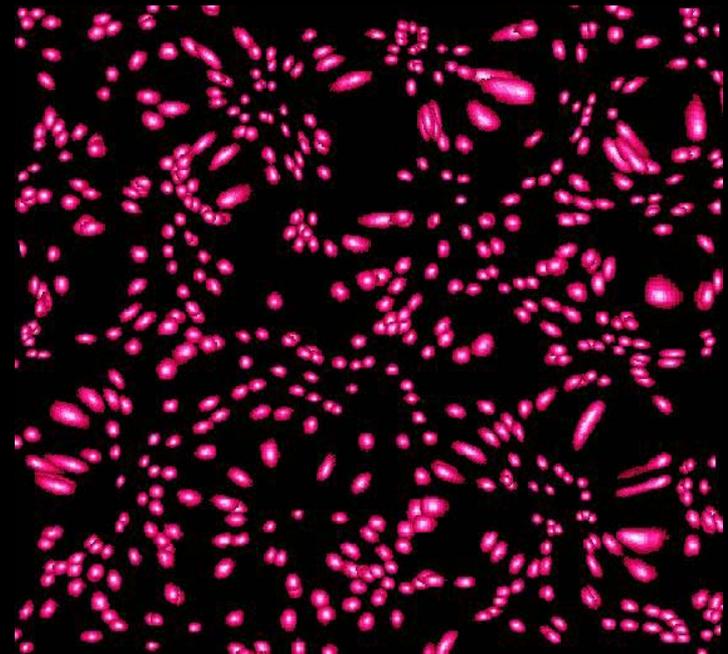
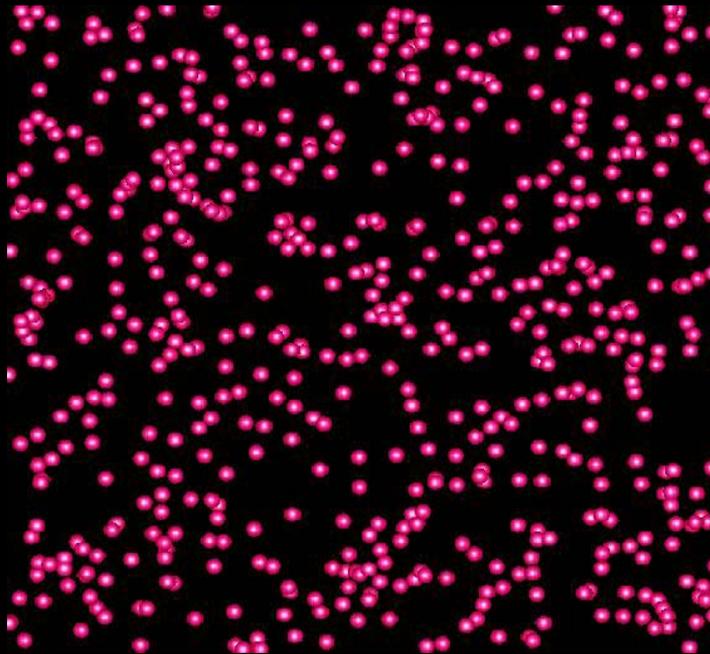
WHAT IS IN STORE FOR THE FUTURE?

- BETTER CMB TEMPERATURE AND POLARIZATION MEASUREMENTS (PLANCK)
- LARGE SCALE STRUCTURE SURVEYS AT HIGHER REDSHIFT AND IN LARGER VOLUMES
- MEASUREMENTS OF WEAK GRAVITATIONAL LENSING ON LARGE SCALES

WEAK LENSING – A POWERFUL PROBE FOR THE FUTURE



Distortion of background images by foreground matter



Unlensed

Lensed

FROM A WEAK LENSING SURVEY THE ANGULAR POWER SPECTRUM CAN BE CONSTRUCTED, JUST LIKE IN THE CASE OF CMB

$$C_\ell = \frac{9}{16} H_0^4 \Omega_m^2 \int_0^{\chi_H} \left[\frac{g(\chi)}{a\chi} \right]^2 P(\ell/r, \chi) d\chi$$

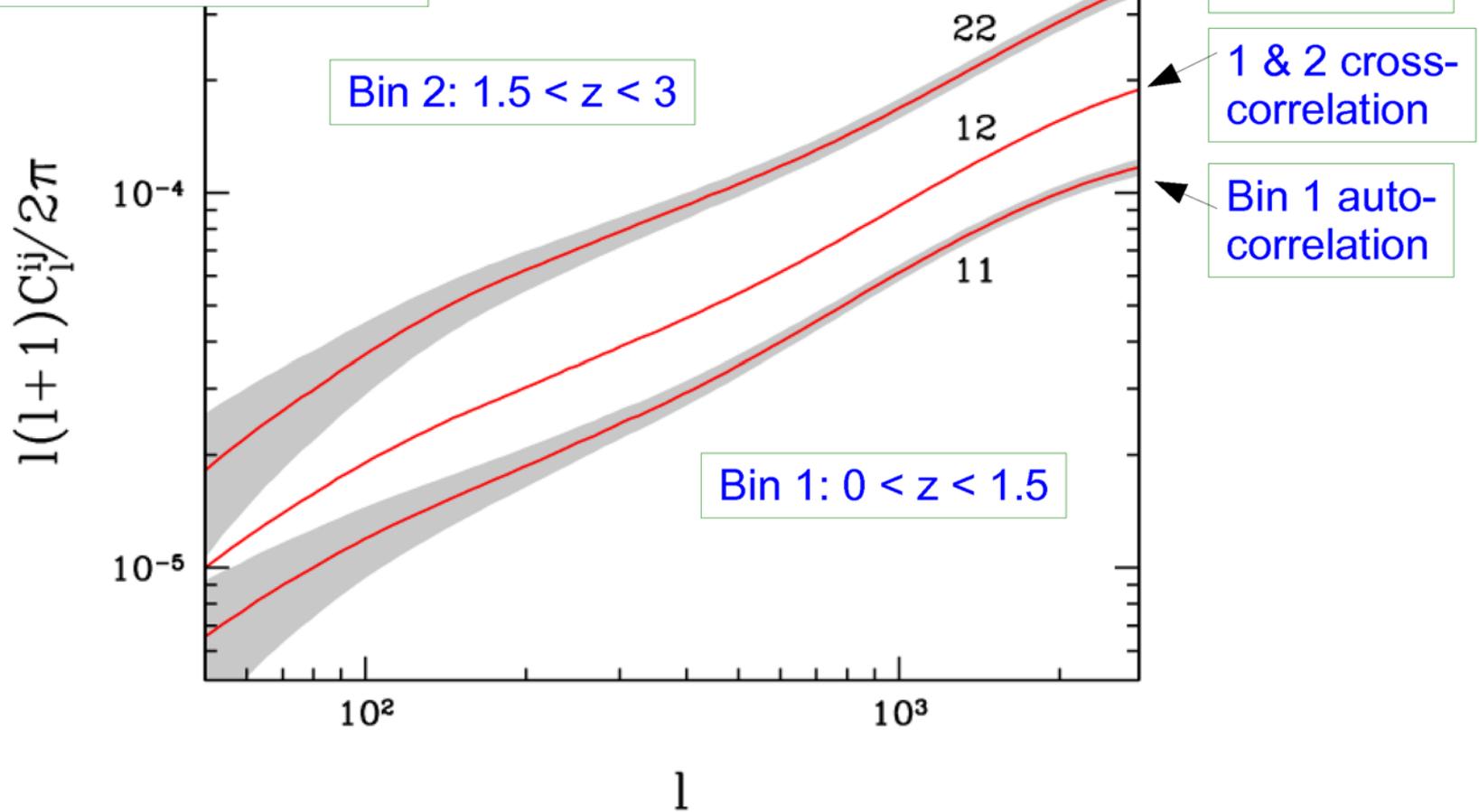
$P(\ell/r, \chi)$ MATTER POWER SPECTRUM (NON-LINEAR)

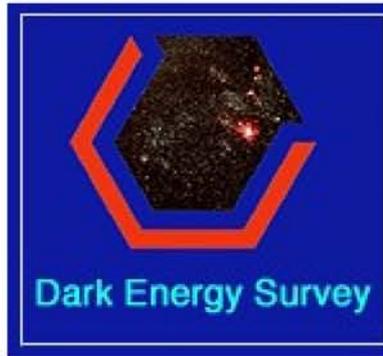
$$g(\chi) = 2 \int_0^{\chi_H} n(\chi') \frac{\chi(\chi' - \chi)}{\chi'} d\chi'$$

WEIGHT FUNCTION
DESCRIBING LENSING
PROBABILITY

(SEE FOR INSTANCE JAIN & SELJAK '96, ABAZAJIAN & DODELSON '03, SIMPSON & BRIDLE '04)

Shear power spectra
for 2 tomography bins

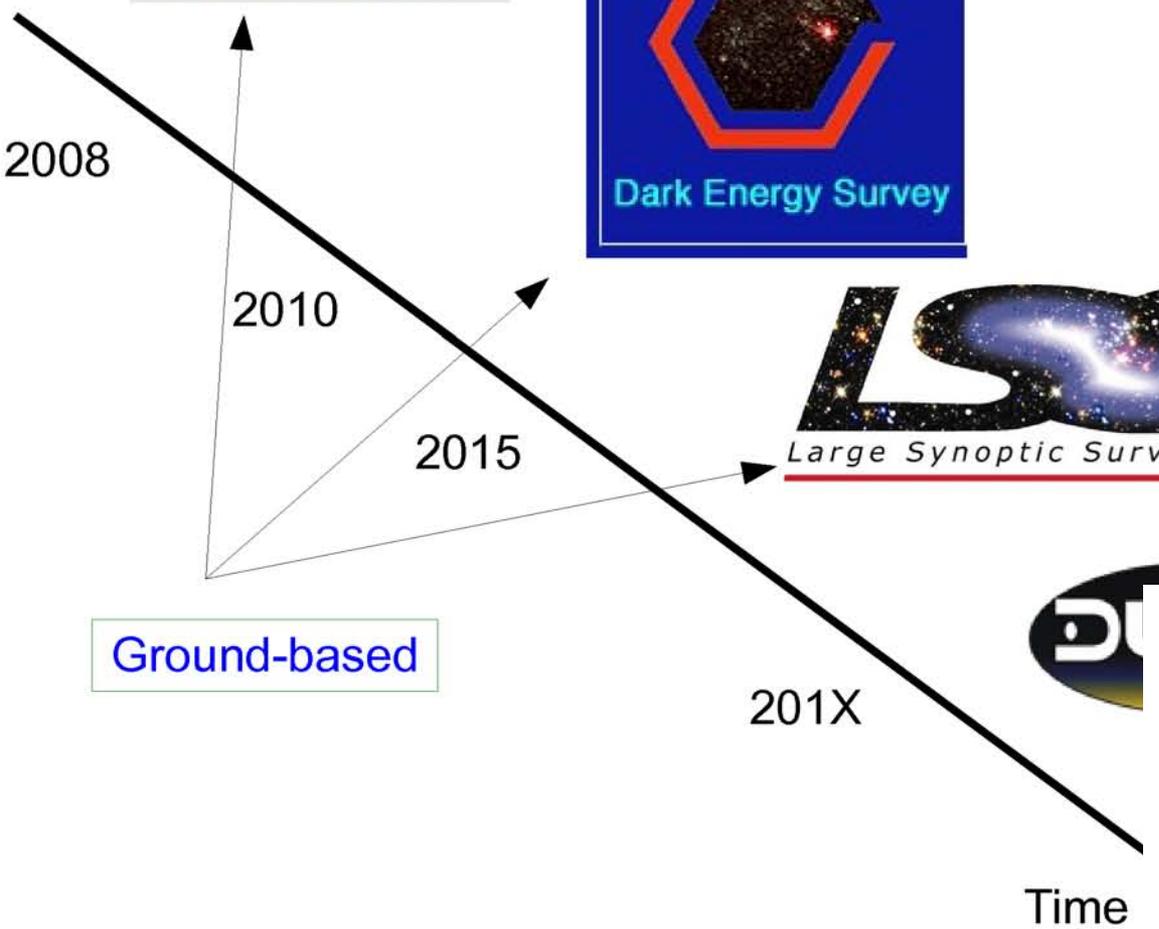




Future surveys
with lensing capacity

Space-based

Ground-based



2008

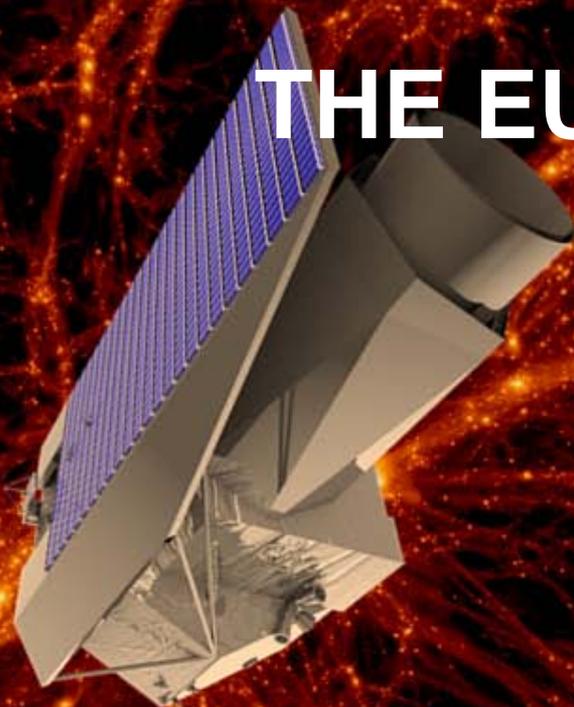
2010

2015

201X

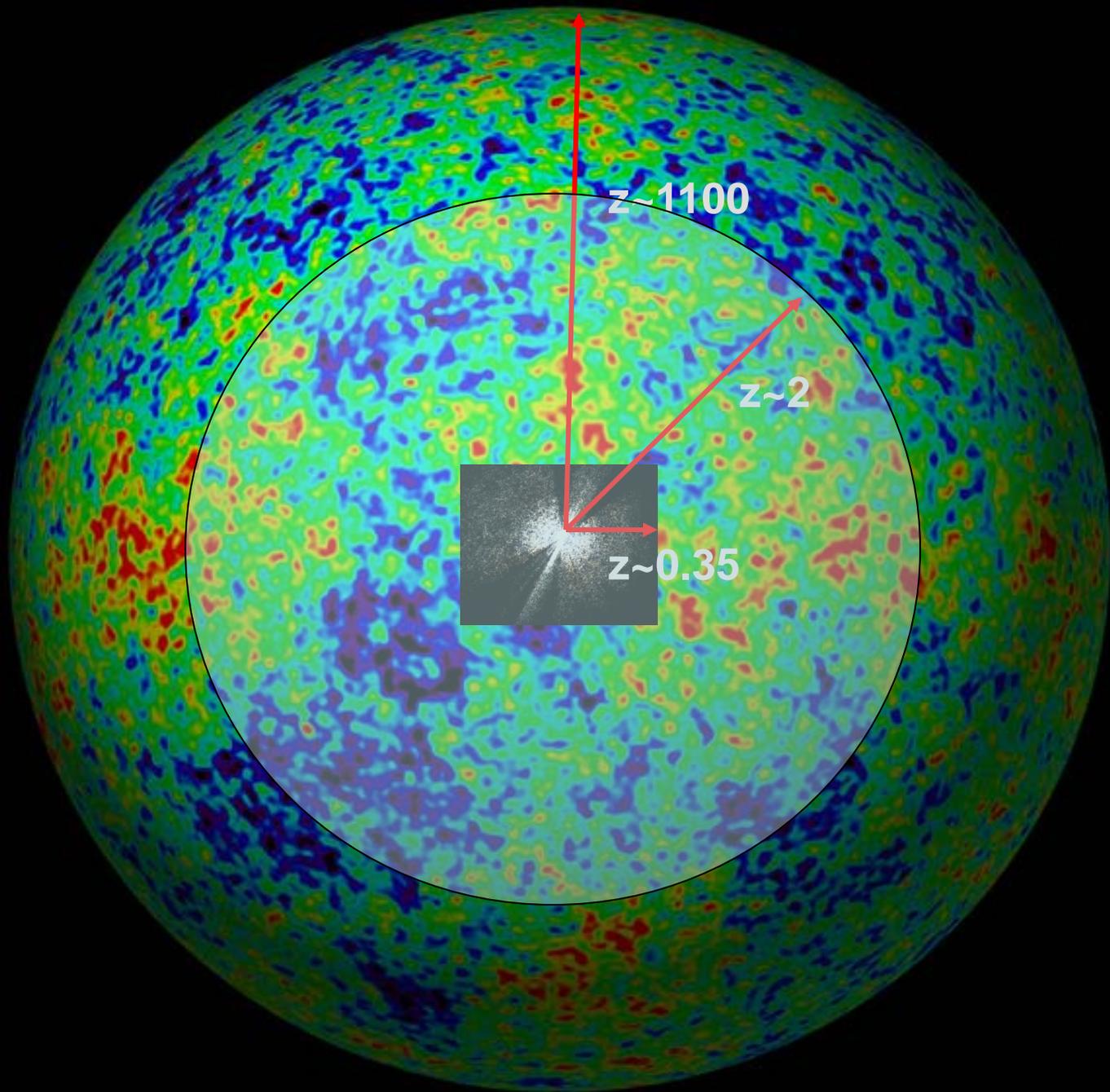
Time

THE EUCLID MISSION



EUCLID WILL FEATURE:

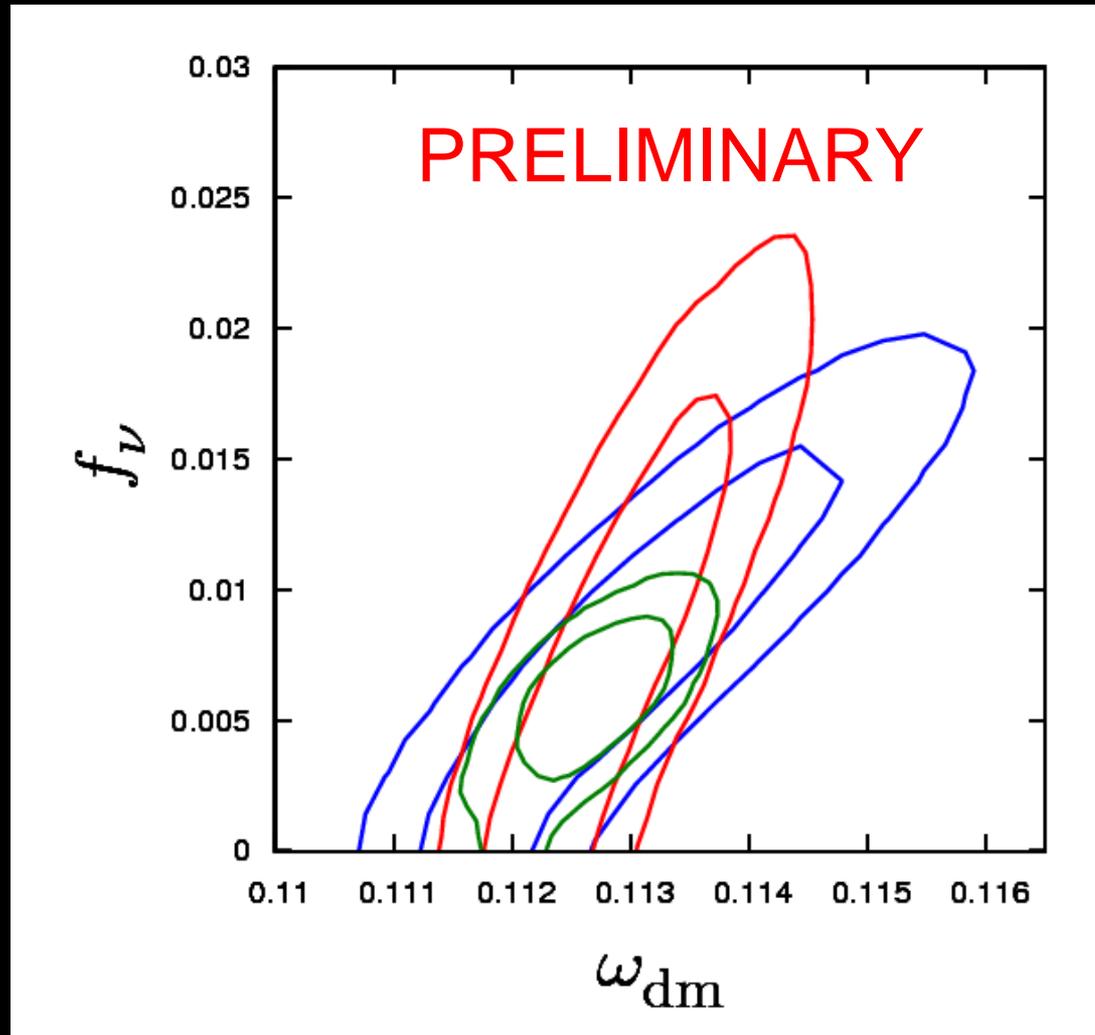
- A WEAK LENSING MEASUREMENT OUT TO $z \sim 2$, COVERING APPROXIMATELY 20,000 deg^2 (THIS WILL BE MAINLY PHOTOMETRIC)
- A GALAXY SURVEY OF ABOUT $\text{few} \times 10^7$ GALAXIES (75 x SDSS)
- A WEAK LENSING BASED CLUSTER SURVEY



EUCLID WL

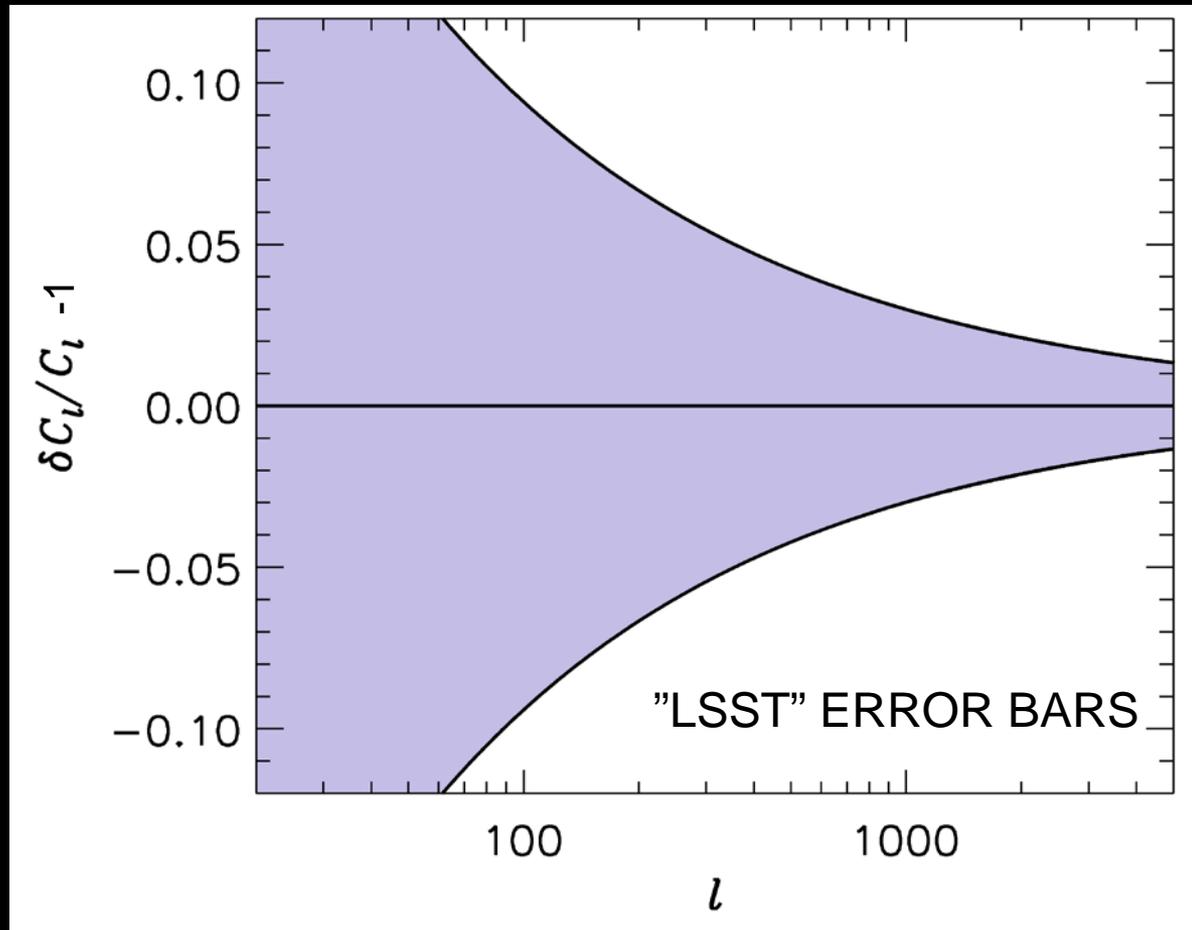
	Planck	+Wide-1	+Wide-5	+Deep-1	+Deep-5
$\sigma(\sum m_\nu)$ (eV)	0.48	0.15	0.043	0.39	0.047
$\sigma(\Omega_{\text{de}})$	0.08	0.020	0.0068	0.036	0.0099
$\sigma(\Omega_b h^2)$	0.00028	0.00016	0.00013	0.00024	0.00014
$\sigma(\Omega_c h^2)$	0.0026	0.0017	0.0015	0.0019	0.0015
$\sigma(w_0)$	0.83	0.093	0.034	0.35	0.045
$\sigma(w_a)$	4.0	0.39	0.081	1.7	0.063
$\sigma(\tau)$	0.0046	0.0043	0.0042	0.0045	0.0043
$\sigma(n_s)$	0.0089	0.0056	0.0028	0.0074	0.0047
$\sigma(\alpha_s)$	0.024	0.013	0.0061	0.020	0.012
$\sigma(\sigma_8)$	0.084	0.019	0.0076	0.030	0.0092
$\sigma(N_{\text{eff}})$	0.19	0.11	0.067	0.14	0.093

HAMANN, STH, WONG 2012: COMBINING THE EUCLID WL AND GALAXY SURVEYS WILL ALLOW FOR AT LEAST A 2σ DETECTION OF THE NORMAL HIERARCHY



THIS SOUNDS GREAT, BUT UNFORTUNATELY THE THEORETICIANS
CANNOT JUST LEAN BACK AND WAIT FOR FANTASTIC NEW DATA
TO ARRIVE.....

FUTURE SURVEYS LIKE EUCLID WILL PROBE THE POWER SPECTRUM TO ~ 1 -2 PERCENT PRECISION



WE SHOULD BE ABLE TO CALCULATE THE POWER SPECTRUM TO AT LEAST THE SAME PRECISION!

IN ORDER TO CALCULATE THE POWER SPECTRUM TO 1% ON THESE SCALES, A LARGE NUMBER OF EFFECTS MUST BE TAKEN INTO ACCOUNT

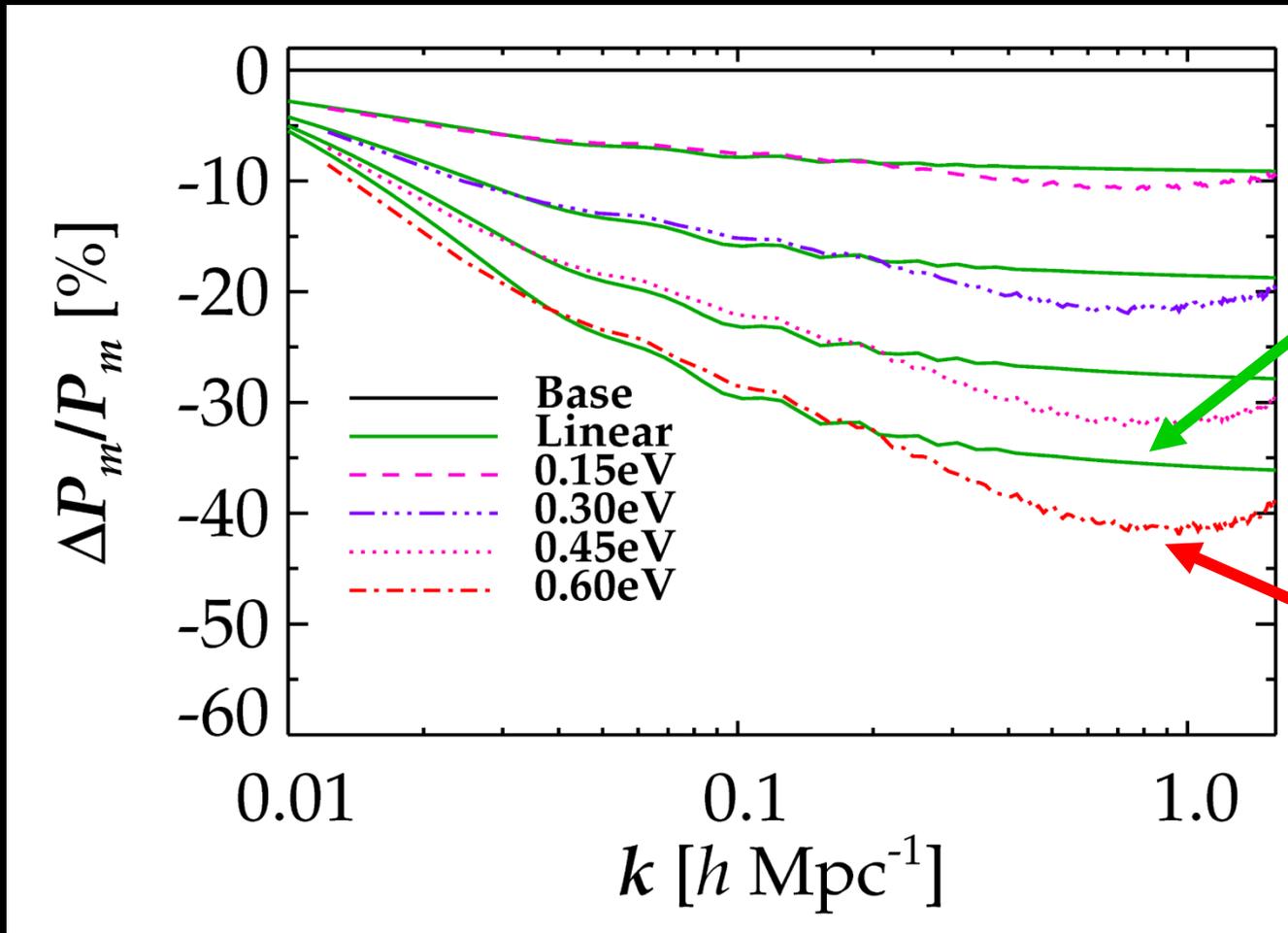
- BARYONIC PHYSICS - STAR FORMATION, SN FEEDBACK,.....

- NEUTRINOS, EVEN WITH NORMAL HIERARCHY

- NON-LINEAR GRAVITY

-

NON-LINEAR EVOLUTION PROVIDES AN ADDITIONAL SUPPRESSION OF FLUCTUATION POWER IN MODELS WITH MASSIVE NEUTRINOS



LINEAR THEORY

$$\frac{\Delta P}{P} \sim -8 \frac{\Omega_\nu}{\Omega_m}$$

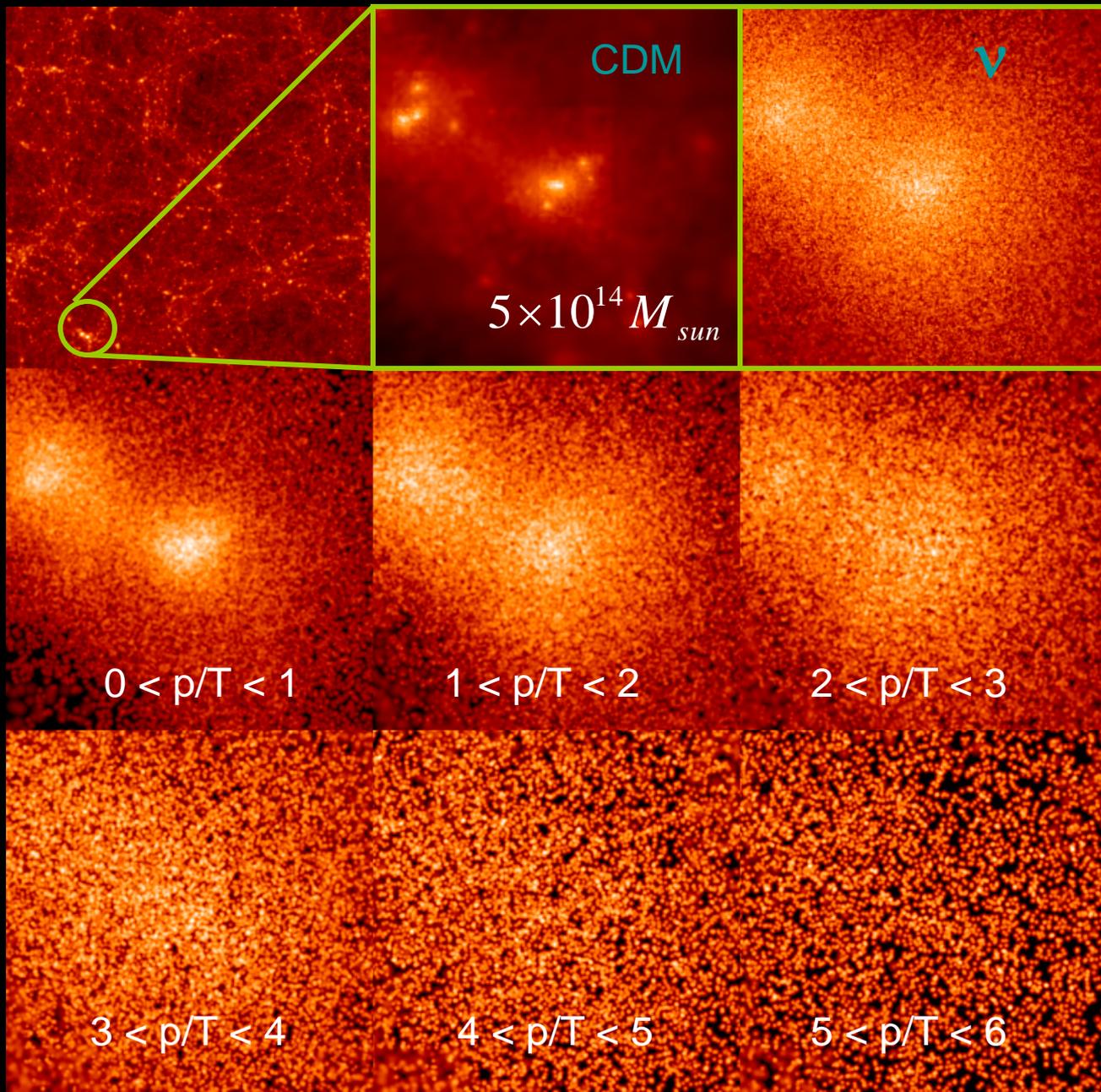
FULL NON-LINEAR

$$\frac{\Delta P}{P} \sim -9.6 \frac{\Omega_\nu}{\Omega_m}$$

Brandbyge, STH, Haugbølle, Thomsen '08
 Brandbyge & STH '09, '10, Viel, Haehnelt, Springel '10
 STH, Haugbølle & Schultz '12, Wagner, Verde & Jimenez '12

INDIVIDUAL HALO PROPERTIES

$512 h^{-1} \text{ Mpc}$



$$\sum m_\nu = 0.6 \text{ eV}$$

CONCLUSIONS

- NEUTRINO PHYSICS IS PERHAPS THE PRIME EXAMPLE OF HOW TO USE COSMOLOGY TO DO PARTICLE PHYSICS
- THE BOUND ON NEUTRINO MASSES IS SIGNIFICANTLY STRONGER THAN WHAT CAN BE OBTAINED FROM DIRECT EXPERIMENTS, ALBEIT MUCH MORE MODEL DEPENDENT
- COSMOLOGICAL DATA MIGHT ACTUALLY BE POINTING TO PHYSICS BEYOND THE STANDARD MODEL IN THE FORM OF STERILE NEUTRINOS
- NEW DATA FROM PLANCK AND EUCLID WILL PROVIDE A POSITIVE DETECTION OF A NON-ZERO NEUTRINO MASS