
**Exploring isotropic events in pp collisions
using the flattenicity event shape variable
or
searching for hedgehogs at the LHC**

Dr. Leonid Serkin

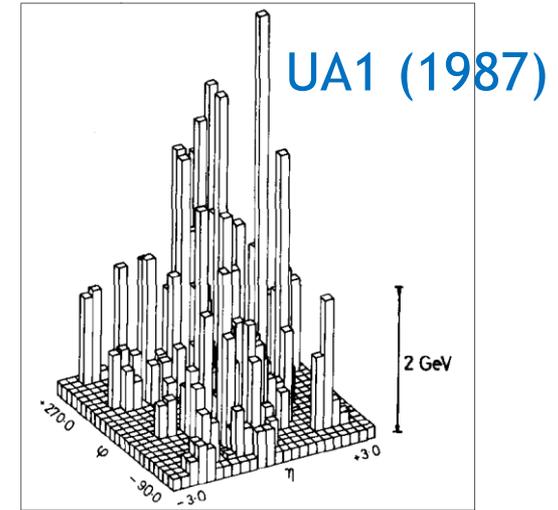
Departamento de Física de Altas Energías
Instituto de Ciencias Nucleares (ICN-UNAM), México

Hedgehogs (erizos) at the LHC?

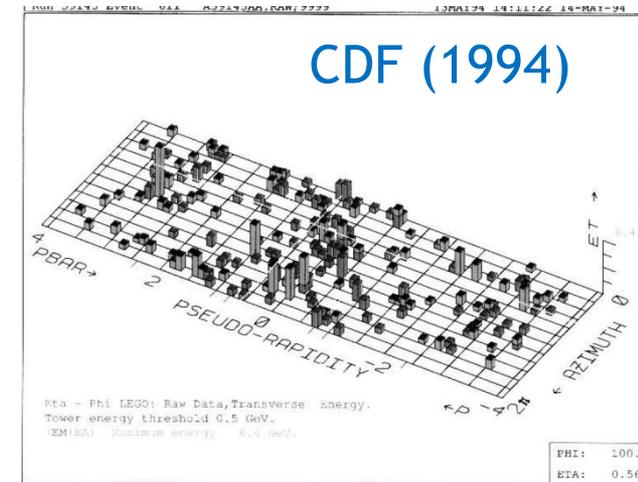


Introduction to “hedgehog-like” events

- Looking for the presence of events with a very **extended structure** of low momentum tracks filling in a **uniform way the pseudorapidity-azimuth** (η - ϕ) space.
- First dedicated analysis of highest transverse energy (E_T) events seen in the UA1 detector at the SppS collider at CERN in proton-antiproton collisions at $\sqrt{s} = 630$ GeV
- Several isotropic events with $E_T \sim 210$ GeV in UA1 observed (even tested for top quark production), no evidence for non-QCD mechanism for these events.
- Similar unusual events observed in p-pbar collisions at $\sqrt{s} = 1.8$ TeV by CDF's Run 1 detector with more than 60 charged particles and $E_T \sim 320$ GeV
- Called “**hedgehog-like**” events by C. Quigg
- Taken for granted that in these events with high E_T perturbative aspects of QCD dominate the event properties: multi-jet events.



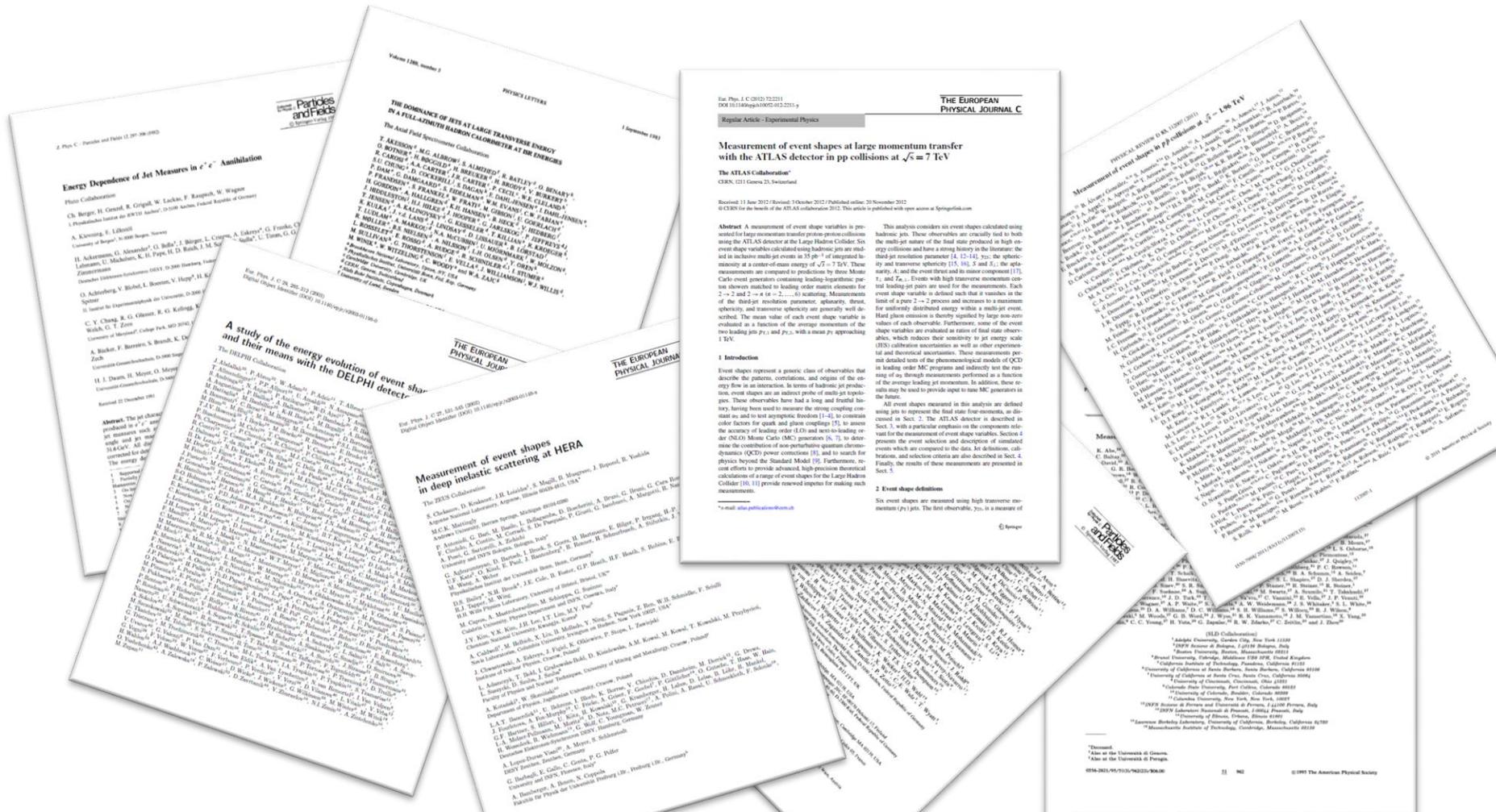
[UA1 Collaboration, Zeit. für Phys. C, V. 36, p. 33 \(1987\)](#)



[C. Quigg, Il Nuovo Cimento, V. 33C, N. 5 p. 327 \(2010\)](#)

Geometry of the final state: event shapes

- Event shape variables: instrumental in classifying the **geometrical and topological configurations** of the final-state particles produced in high-energy collisions at PETRA, ISR, SppS, SLD, LEP, HERA, Tevatron and the LHC.



- Study the isotropy of the final-state energy distribution by defining the **linearized sphericity tensor of the event**, where the Greek indices denote the x, y, and z components of the momentum of the charged particle i . The eigenvalues must satisfy the normalization condition: $\lambda_1 \geq \lambda_2 \geq \lambda_3$ and $\lambda_1 + \lambda_2 + \lambda_3 = 1$.

$$S^{\alpha\beta} = \frac{\sum_i p_i^\alpha p_i^\beta}{\sum_i |\vec{p}_i|^2},$$

$$A = \frac{3}{2}\lambda_3; \quad S = \frac{3}{2}(\lambda_2 + \lambda_3).$$

- **Aplanarity (A)** serves as a measure of how planar an event is. A balanced pencil-like event corresponds to $A = 0$, and an isotropic event corresponds to $A = 1/2$.
- **Sphericity (S)** quantifies the isotropy of an event, representing the degree to which energy and momentum are evenly distributed in all directions. $S = 0$ denotes a balanced dijet event, and $S = 1$ for an isotropic event.

- **Centrality:** a measure of how much of the event is contained within the central part of the detector; ranges between 0 and 1, where a pencil-like has $C = 0$ and a centrally contained event corresponds to $C = 1$.

$$C = \frac{\sum_i p_{T,i}}{\sum_i E_i},$$

$$T = 1 - \max_{\hat{n}} \frac{\sum_i |\vec{p}_{T,i} \cdot \hat{n}|}{\sum_i |\vec{p}_{T,i}|},$$

- **Transverse thrust:** a widely used event shape ranging from 0 for a pencil-like topology to 1/3 for a circularly symmetric distribution of particles in the transverse plane.

- **Transverse sphericity:** infrared and collinear safe event shape that ranges from $S_0 = 0$ for events with back-to-back multijet final states to $S_0 = 1$ for isotropic event topologies.

$$S_0 = \frac{\pi^2}{4} \min_{\hat{n}_s} \left(\frac{\sum_i |\vec{p}_{T,i} \times \hat{n}_s|}{\sum_i p_{T_i}} \right)^2.$$

Characterisation of high-multiplicity events

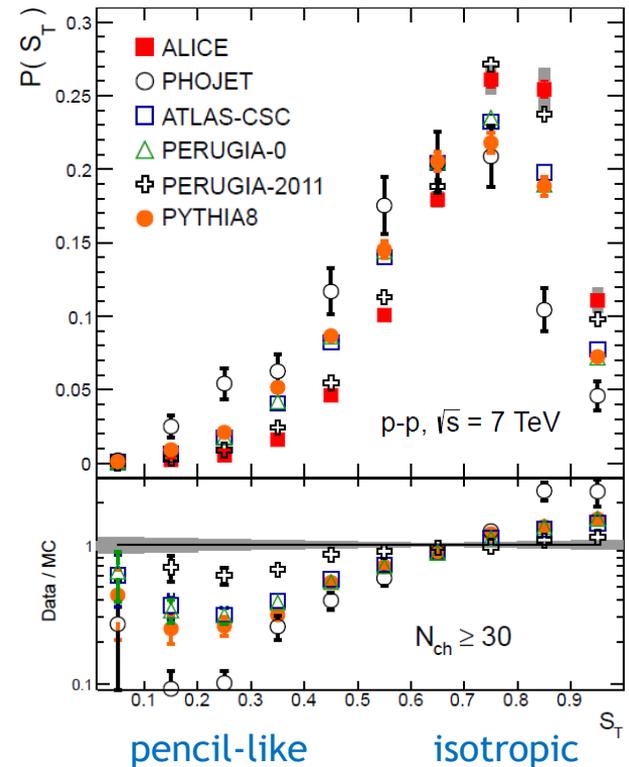
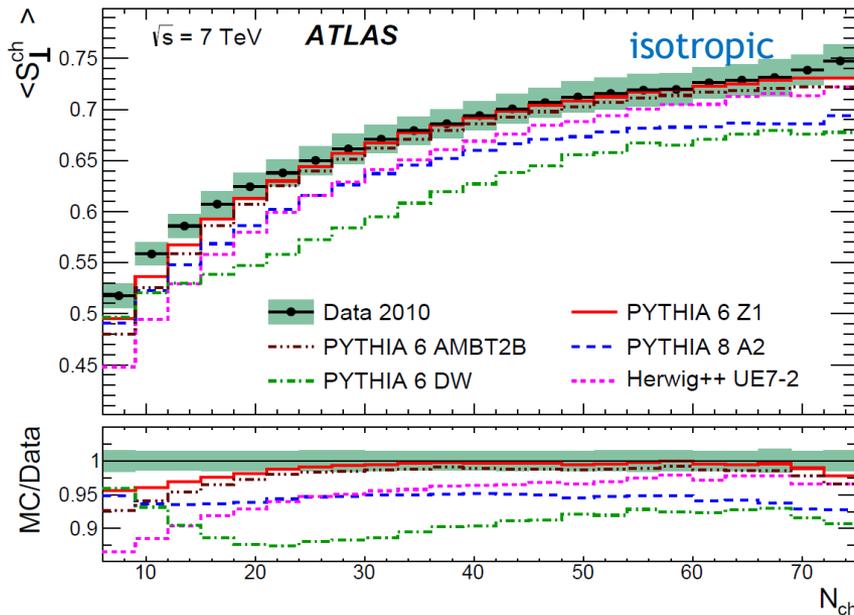
- Attempts to characterise these high-multiplicity events: use of event shapes, i.e. using **transverse sphericity**:

$$S_{\perp} = \frac{2\lambda_2^{xy}}{\lambda_1^{xy} + \lambda_2^{xy}}, \quad S^{xy} = \sum_i \frac{1}{|\vec{p}_{T,i}|^2} \begin{bmatrix} p_{x,i}^2 & p_{x,i} p_{y,i} \\ p_{x,i} p_{y,i} & p_{y,i}^2 \end{bmatrix}$$

- Both ALICE and ATLAS observed an **under-estimation of isotropic events by MC generators at high charged multiplicity ($N_{ch} \geq 30$)**

- ✓ Suggest that a very active underlying event (UE) is needed by the MC event generators in order to explain these high-multiplicity events

ATLAS Collaboration, Phys. Rev. D 88, 032004 (2013)

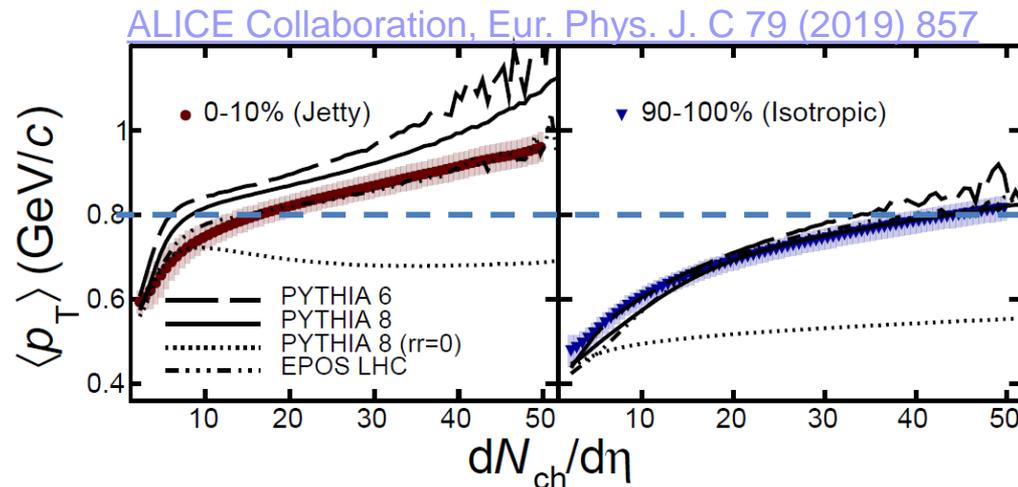


ALICE Collaboration, Eur. Phys. J. C 72 (2012) 2124

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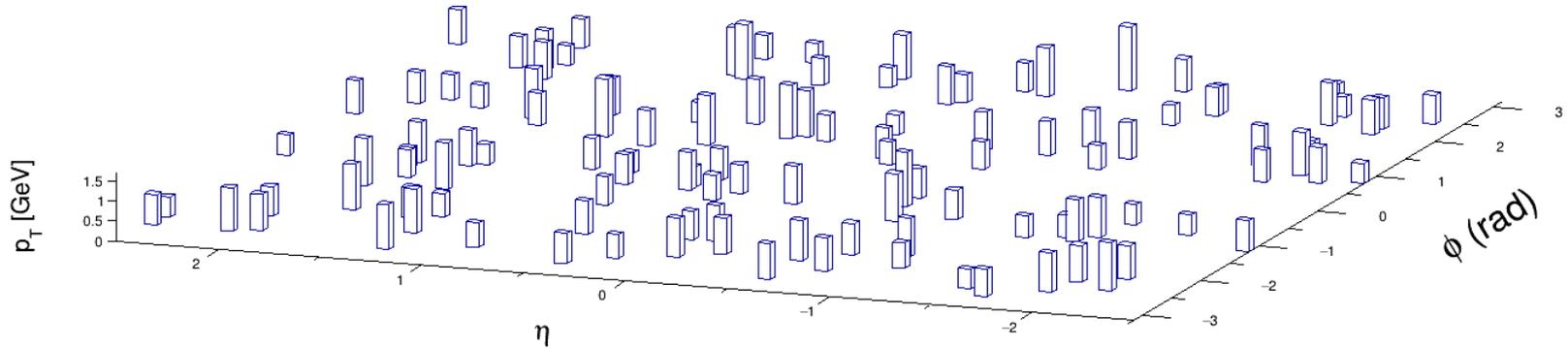


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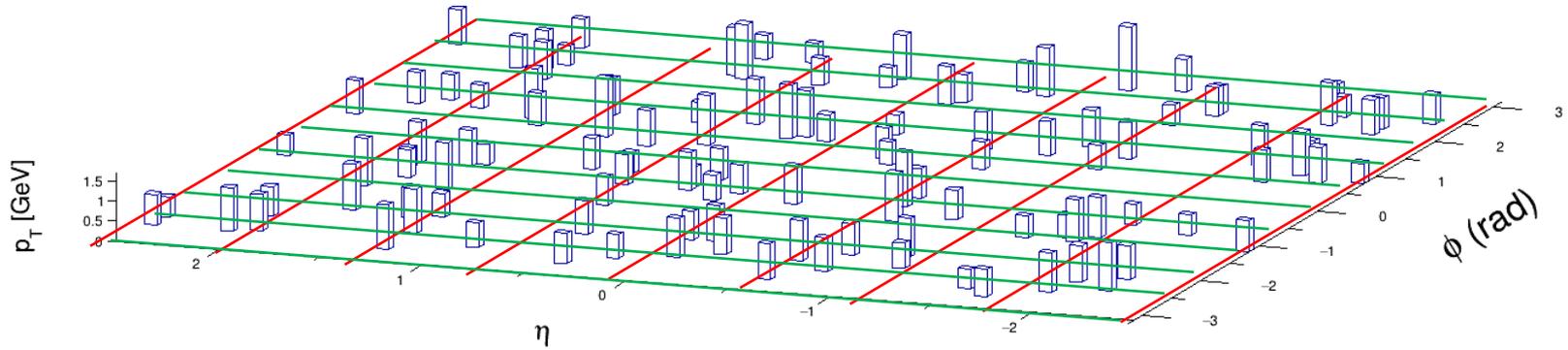
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- Recently, a new event shape parameter, **flattenicity**, was proposed [[A. Ortiz, G. Paic, Rev. Mex. Fis. Suppl. 3 \(2022\) 4, 040911](#)] that allows one to identify and characterise high-multiplicity events with a quasi-isotropic distribution in a wide pseudorapidity range in proton-proton collisions.
- MC event generators are able to model “hedgehog” events, which opens the possibility to study their properties and find a potential way to experimentally trigger these events.

- The idea: find out how uniform the p_T of tracks is distributed in a given event!

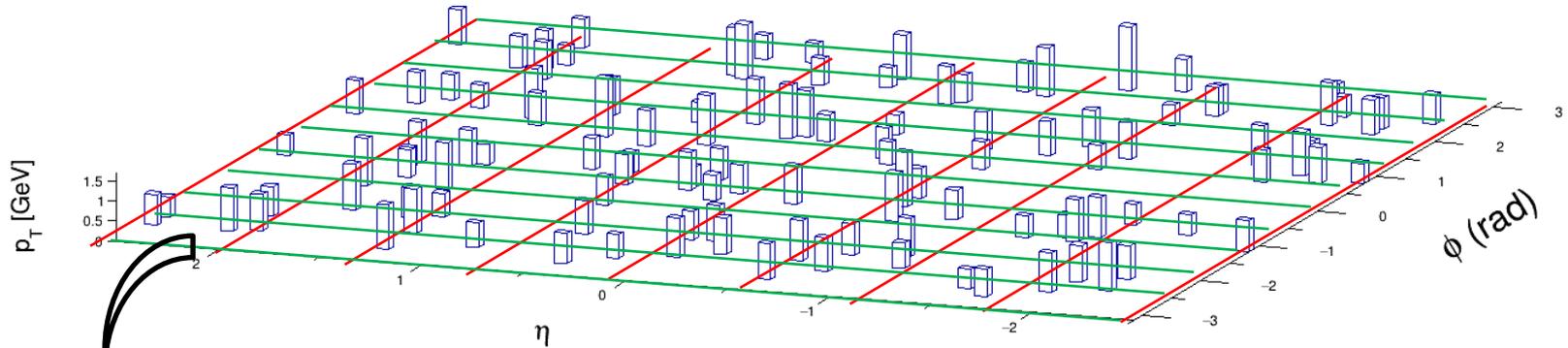


Calculating flattenicity

- Build **10** x **12** grid in (η - ϕ) space:



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In each cell, the average transverse momentum is calculated: p_T^{cell}

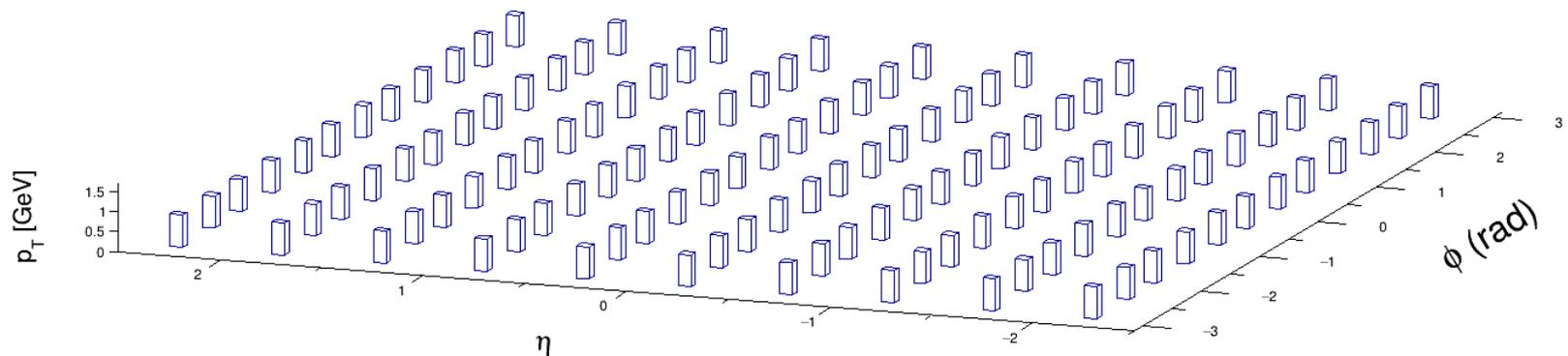
- Event-by-event, the relative standard deviation of the p_T^{cell} distribution is obtained.
- Events with isotropic distribution of particles (“hedgehogs”) are expected to have $\rho = 1$.

$$\rho = 1 - \frac{\sqrt{\sum_{i=1}^{i=120} \left(p_T^{\text{cell},i} - \langle p_T^{\text{cells}} \rangle \right)^2 / N_{\text{cell}}^2}}{\langle p_T^{\text{cells}} \rangle},$$

$\rho = 1$

Simulation: $N_{\text{ch}} = 120, \langle p_T \rangle = 0.8 \text{ GeV}$

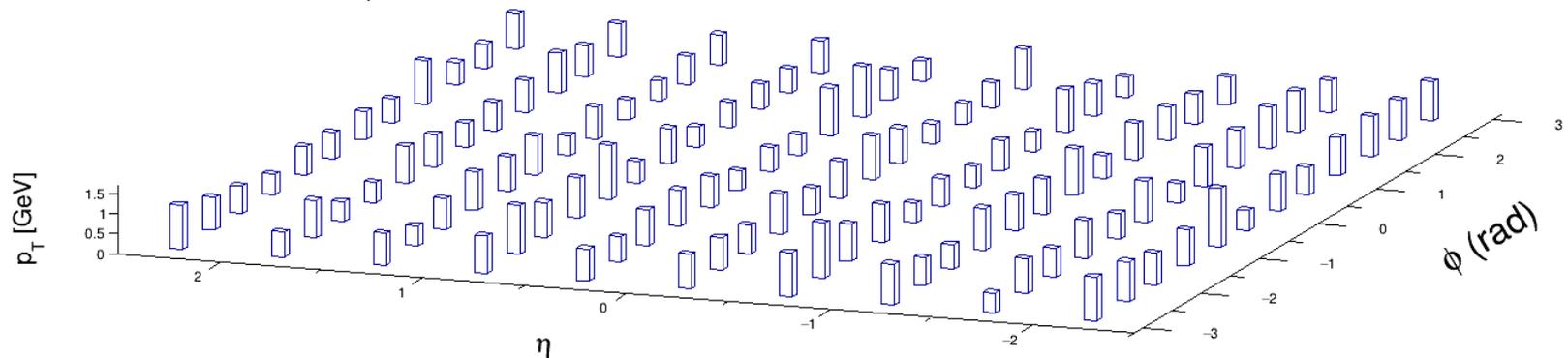
$A = 0.10, C = 0.42, S = 0.20, S_0 = 0.76, T = 0.27, \rho = 1.00$



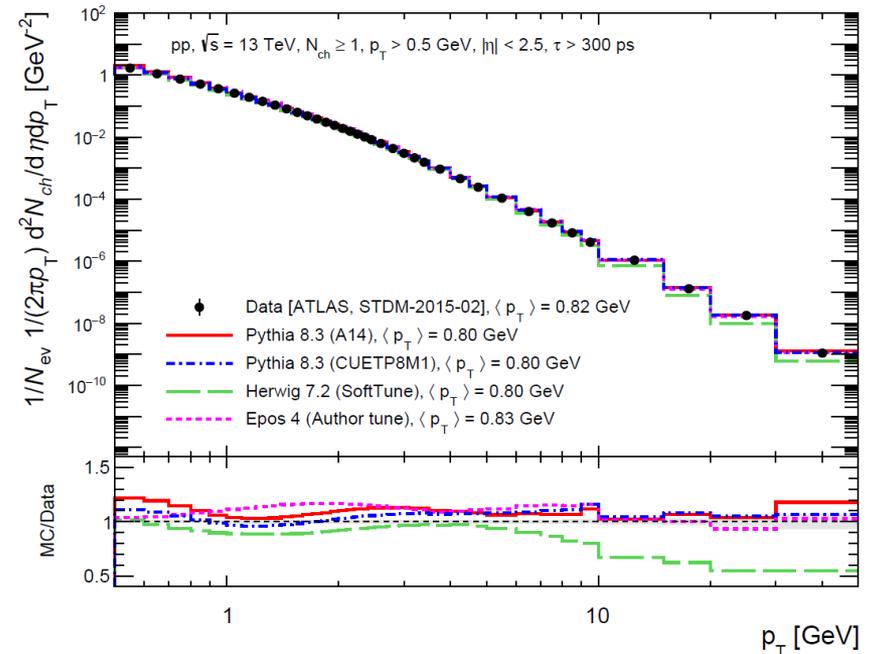
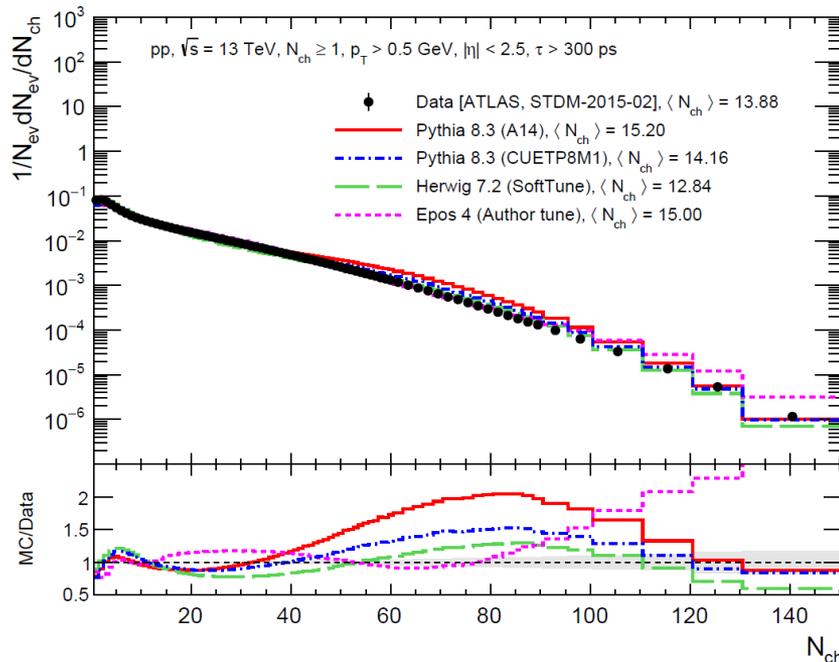
$\rho = 0.98$

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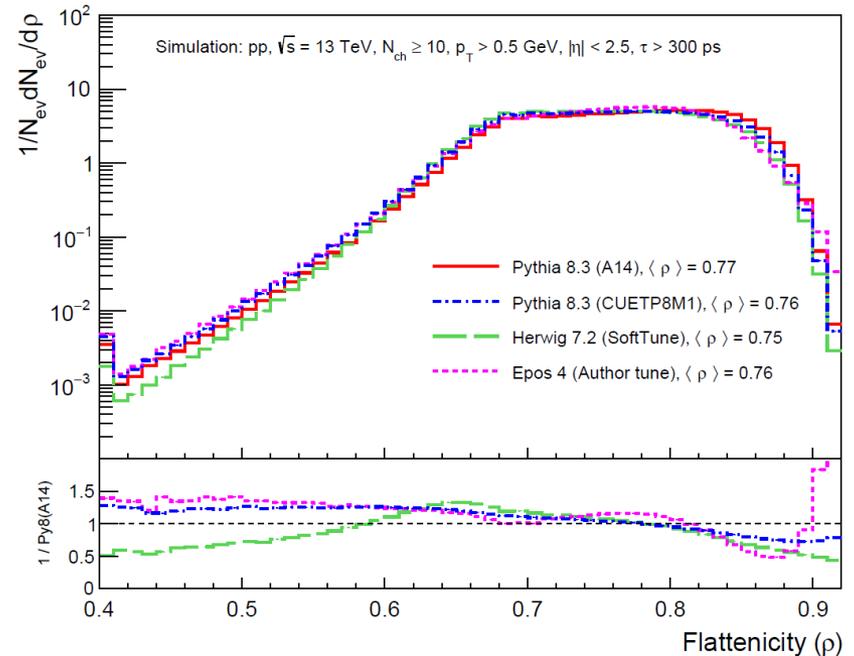
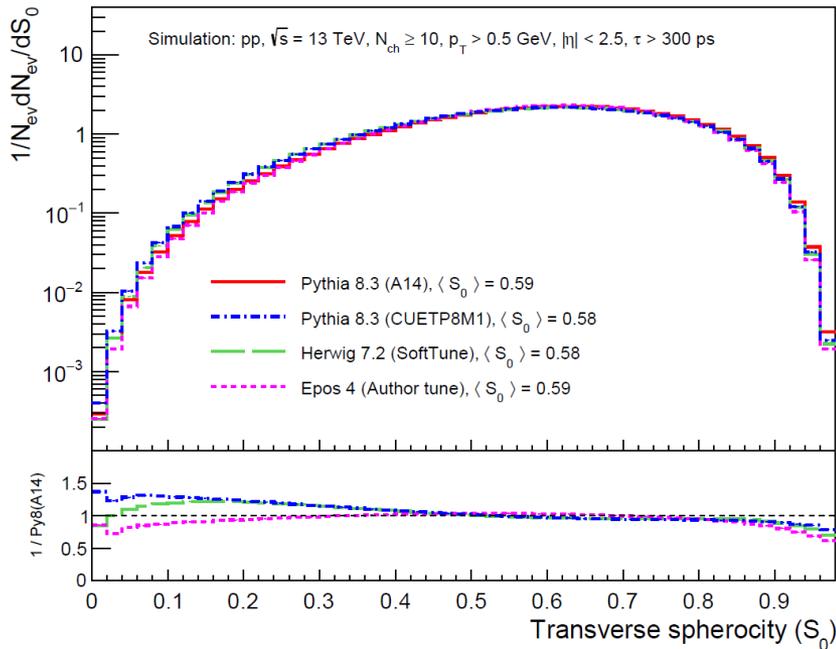
$A = 0.09, C = 0.41, S = 0.19, S_0 = 0.76, T = 0.29, \rho = 0.98$



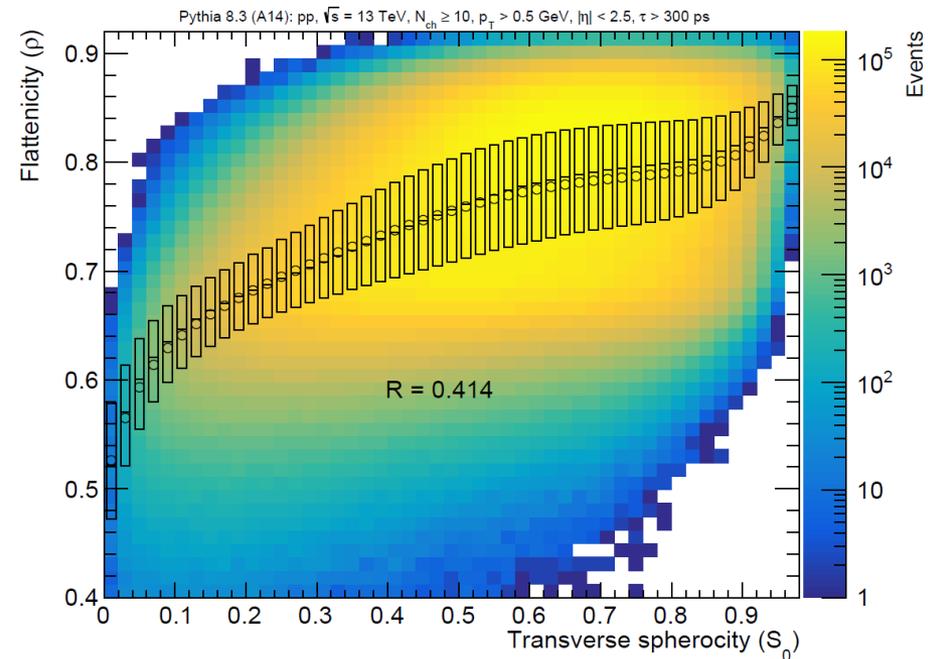
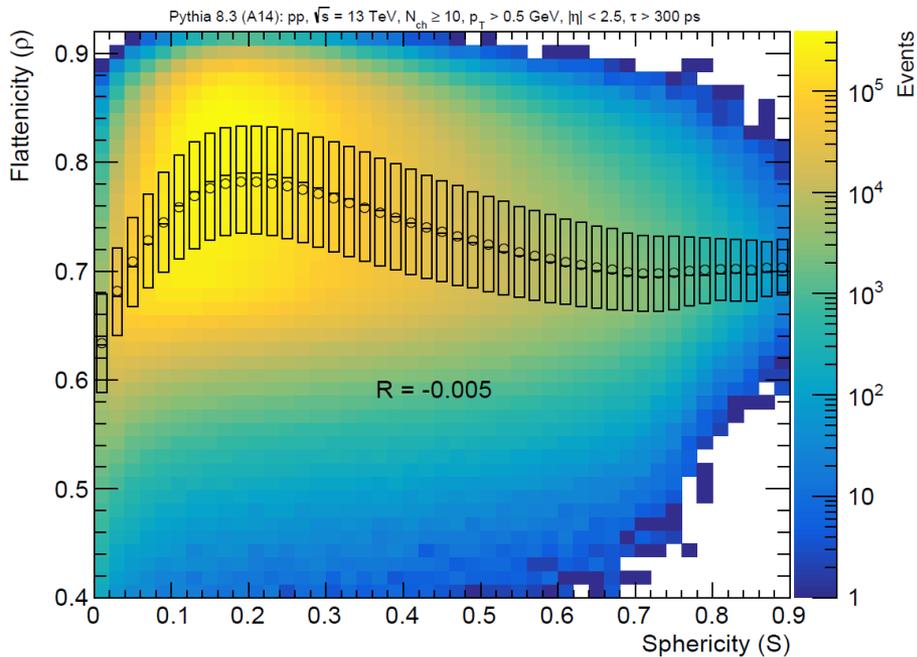
- Two sets of inelastic events, including non-diffractive and diffractive components, were simulated using **Pythia 8.309**: ATLAS A14 tune and CMS CUETP8M1 tune.
- **Herwig 7.2.0** with SoftTune based on the MMHT2014 LO PDF
- Recently released **EPOS 4.0.0** framework using authors tune
- First, **revise the performance** of these MC models in reproducing the 13 TeV pp collision data.



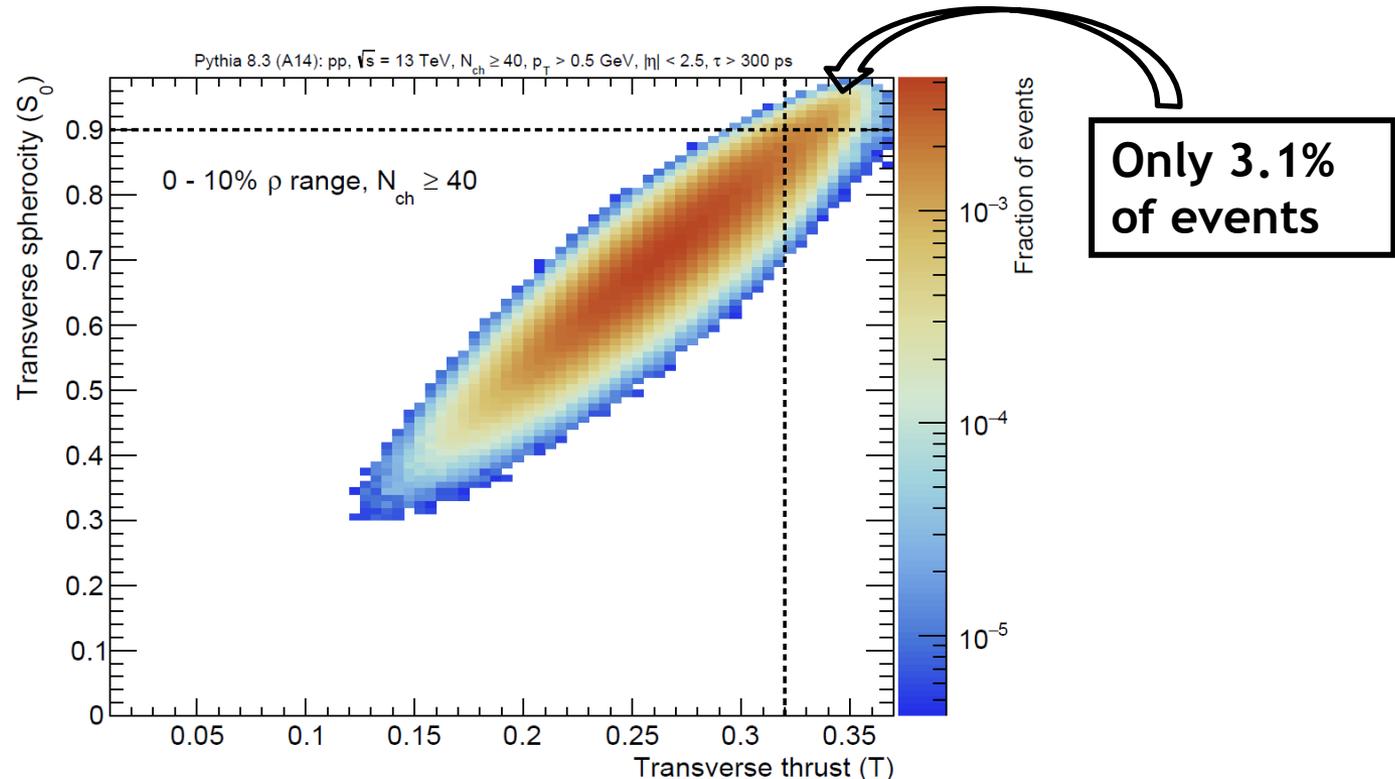
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- Then, **compare transverse sphericity and flattenicity** for the 4 MC settings



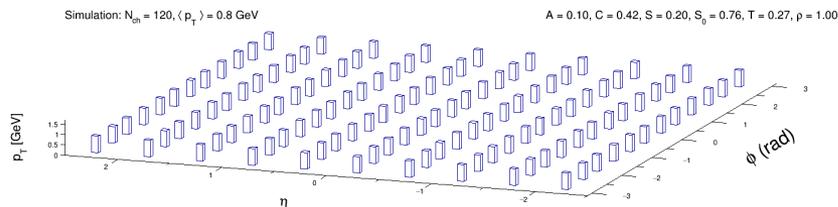
- To demonstrate flattenicity's value in identifying isotropic events and its complementary information about the global shape of an event, we study its correlation with other event shape variables.
- Overall, there is clear indication that while flattenicity is related to other event shape variables, it **provides distinct and complementary** info of the isotropy of events



- Classify the **top 10%** of events in the distributions of flattenicity, transverse sphericity, and transverse thrust for each multiplicity class as **isotropic events**.
- Our observation is that for the highest charged-particle multiplicity class, only 3.1% of events meet all the three criteria: clearly indicates that **flattenicity selects a different subset** of events as compared to widely used S_0 and T.



- Hedgehog events **have never been seriously studied** in pp collisions at the LHC. These events are “rare” – but as rare as a top-quark–pair production!
- Flattenicity - the new event structure parameter - allows one to identify the hedgehog events and observe the evolution of events from jetty to hedgehog type.
- When compared to other event shape variables widely used in the literature, such as transverse sphericity, we found that flattenicity is able to **identify** a subset of isotropic events with **hedgehog-like structures**.
- Our results will be submitted to a journal asap, while experimental measurements using flattenicity are on their way!
- Next steps: analyze hedgehog events in data, so stay tuned!



Muchas gracias
por su atención!

