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# Future collider sensitivities to $\nu$ SMEFT interactions

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# Outline

- 1 Motivation: SM Neutrino EFT ( $\nu$ SMEFT)
- 2 Lepton-trijet signals at LHeC
- 3 Lepton collider sensitivities to  $N$  signals

# Masses in the standard model (SM)

- Gauge symmetry breaking

$$[SU(2)_L \times U(1)_Y]_{EW} \xrightarrow{\text{SSB}} U(1)_Q$$

$$\phi = \begin{pmatrix} \phi^+ \\ \phi^0 \\ \phi^0 \end{pmatrix} \xrightarrow{\text{SSB}} \langle\phi\rangle = \begin{pmatrix} 0 \\ v+h \\ \sqrt{2} \end{pmatrix}$$

- Dirac mass in Yukawa  
Lagrangian:

$$-\mathcal{L}_Y \supset \Gamma_\ell^{ij} \overline{L}_L^i \phi \ell_R^j \xrightarrow{\text{SSB}} \frac{\Gamma_\ell^{ij} \nu}{\sqrt{2}} \overline{\ell}_L^i \ell_R^j$$

- Massless neutrinos  $\nu_{eL}, \nu_{\mu L}, \nu_{\tau L}$ ...
- Lepton number is conserved...
- But it needs to be extended to include neutrino masses!

Three Generations of Matter (Fermions) spin $\frac{1}{2}$						Bosons (Forces) spin 1	
mass $\rightarrow$	2.4 MeV	1.27 GeV	171.2 GeV	0	0	91.2 GeV	$>114$ GeV
charge $\rightarrow$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	0	0	0	0
name $\rightarrow$	u up Left	c charm Left	t top Left	g gluon	$\gamma$ photon	$Z^0$ weak force	Higgs boson
Quarks	d down Left	s strange Left	b bottom Left	$\nu_e$ electron neutrino Left	$\nu_\mu$ muon neutrino Left	$\nu_\tau$ tau neutrino Left	$W^\pm$ weak force $\nu_e$ spin 0
Leptons	e electron Left	$\mu$ muon Left	$\tau$ tau Left	$\ell_L^i = e, \mu, \tau$	$L_L = \begin{pmatrix} \nu_e \\ e \end{pmatrix}_L$	$\ell_R^- = \ell_R^-$	

# Seesaw Mechanism (Type I)

- Incorporate sterile  $N_{i,R}$

$$\mathcal{L}_\nu = -\Gamma_{\ell j} \overline{L}_{\ell,L} \epsilon \tilde{\phi}^* N_{j,R} - \frac{1}{2} (N_{i,R})^T C M_{ij} N_{j,R} + h.c.$$

SSB

$$\mathcal{L}_\nu = -\bar{\nu}_{\ell,L} M_{\ell j}^D N_{j,R} - \frac{1}{2} \overline{N_{i,R}^c} M_{ij}^N N_{j,R}$$

$2.4 \text{ MeV}$ $\frac{2}{3}$ <b>u</b> Left up Right	$1.27 \text{ GeV}$ $\frac{2}{3}$ <b>c</b> Left charm Right	$171.2 \text{ GeV}$ $\frac{2}{3}$ <b>t</b> Left top Right
$4.8 \text{ MeV}$ $-\frac{1}{3}$ <b>d</b> Left down Right	$104 \text{ MeV}$ $-\frac{1}{3}$ <b>s</b> Left strange Right	$4.2 \text{ GeV}$ $-\frac{1}{3}$ <b>b</b> Left bottom Right
$<0.0001 \text{ eV}$ $0$ <b><math>\nu_e</math></b> Left electron neutrino Right	$\sim 0.01 \text{ eV}$ $0$ <b><math>\nu_\mu</math></b> Left muon neutrino Right	$\sim 0.04 \text{ eV}$ $0$ <b><math>\nu_\tau</math></b> Left tau neutrino Right
$0.511 \text{ MeV}$ $-1$ <b>e</b> Left electron Right	$105.7 \text{ MeV}$ $-1$ <b><math>\mu</math></b> Left muon Right	$1.777 \text{ GeV}$ $-1$ <b><math>\tau</math></b> Left tau Right

Heavy N  
undetectable

- 6 massive states: Majorana fermions
- 3 Light  $\nu_m$

$$m_\nu \sim (M^D)^2 (M^N)^{-1}$$

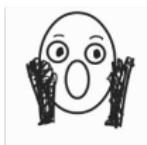
- 3 Heavy N



$$M_N \sim M^N$$

- Mixing of the active-massive states:

$$\nu_{\ell,L} = U_{\ell m} \nu_m + \underline{U_{\ell N}} N$$



$$U_{\ell N} \lesssim 1 \times 10^{-6} \sqrt{\frac{100 \text{ GeV}}{M_N}}$$

TINY MIXINGS!

# $\nu$ SMEFT: Dim=6 simplified scenario [1]

what if there is something more ?

- EFT with  $N_R$  and SM fields

$$\mathcal{L} = \mathcal{L}_{SM} + \mathcal{L}_\nu + \mathcal{L}^5 + \mathcal{L}^6 + \dots$$

Encodes BSM physics with  $N_R$  as low-energy degree of freedom

- Discard the mixing term in the renormalizable lagrangian:

$$\mathcal{L}_\nu \supset \Gamma_\ell \overline{L_{\ell,L}} \epsilon \tilde{\phi}^* N_R \rightarrow 0 \sim U_{\ell N} \rightarrow 0$$

- Consider only one massive heavy  $N$  ( $N \equiv N_R$ ) with a Majorana mass: it is a Majorana particle!
- Only dim 5 interaction with ONE  $N$  is  $\mathcal{O}_{N\phi}^{(5)} = \bar{N}_R N_R^c \phi^\dagger \phi$ : reabsorb contribution to  $M_N$  in  $N$  physical mass  $m_N$  (See JHEP 09(2022)079, 2205.13550)

$$\mathcal{L}_{eff} = \mathcal{L}_{SM} + \sum_{d=6}^{\infty} \left( \frac{1}{\Lambda^{d-4}} \sum_{\mathcal{J}} \alpha_{\mathcal{J}} \cancel{\mathcal{O}_{\mathcal{J}}^d} + h.c. \right)$$



[1] F. del Aguila PLB (2009) 0806.0876, Liao PRD (2017) 1612.04527, Bhattacharya PRD (2016) 1505.05264

# Dim= 6 Operators with one heavy $N$ [1]

Higgs dressed mixing

$$\mathcal{O}_{LN\phi} = (\phi^\dagger \phi)(\bar{L}_i N \tilde{\phi})$$

73 couplings counting different flavors!

$$(\alpha_{LN\phi}^{(i)}) \quad SCALAR$$

Boson currents

**NC**  $\mathcal{O}_{NN\phi} = i(\phi^\dagger D_\mu \phi)(\bar{N}\gamma^\mu N) \quad \alpha_Z \quad (\alpha_{NN\phi})$

**CC**  $\mathcal{O}_{NI\phi} = i(\phi^T \epsilon D_\mu \phi)(\bar{N}\gamma^\mu l_i) \quad \alpha_W^{(i)} \quad (\alpha_{NI\phi}^{(i)}) \quad VECTORIAL$

4-fermions ( $4 - f$ )

**CC**  $\mathcal{O}_{duNI} = (\bar{d}_j \gamma^\mu u_j)(\bar{N}\gamma_\mu l_i) \quad \alpha_{duNI}^{(i,j)}$

**SQCD**  $\mathcal{O}_{fNN} = (\bar{f}_i \gamma^\mu f_i)(\bar{N}\gamma_\mu N) \quad \alpha_{fNN}^{(i)} \quad f = u, d, l, Q, L$

**SQCD**  $\mathcal{O}_{QuNL} = (\bar{Q}_i u_i)(\bar{N}l_j) \alpha_{QuNL}^{(i,j)}, \quad \mathcal{O}_{QNLD} = (\bar{Q}_i N)\epsilon(\bar{l}_j d_j) \alpha_{QNLD}^{(i,j)}$

$\mathcal{O}_{LNQd} = (\bar{L}_i N)\epsilon(\bar{Q}_j d_j) \alpha_{LNQd}^{(i,j)}, \quad \mathcal{O}_{LNLI} = (\bar{L}_i N)\epsilon(\bar{l}_j l_j) \alpha_{LNLI}^{(i,j)}$

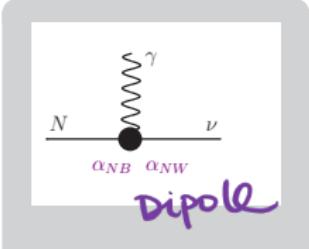
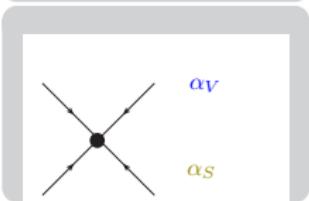
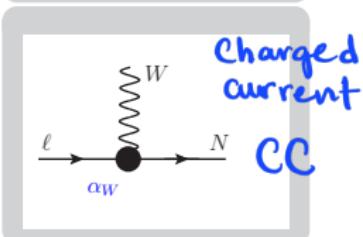
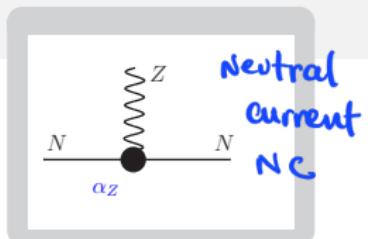
1-loop generated (1 – loop)

$$\mathcal{O}_{NB} = (\bar{L}_i \sigma^{\mu\nu} N)\tilde{\phi} B_{\mu\nu} \quad \alpha_{NB}^{(i)}$$

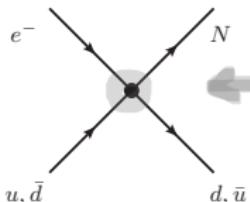
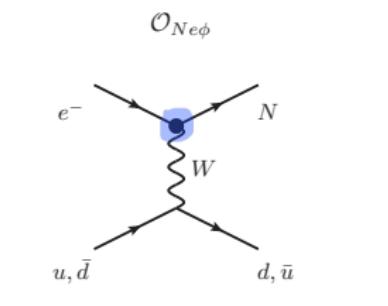
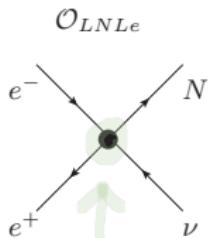
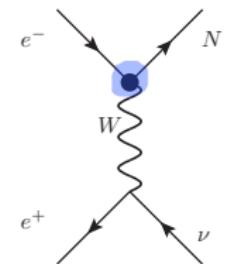
$$\mathcal{O}_{NW} = (\bar{L}_i \sigma^{\mu\nu} \tau^I N)\tilde{\phi} W_{\mu\nu}^I \quad \alpha_{NW}^{(i)} \dots$$

TENSORIAL

$$\alpha^{1-loop} = \frac{\alpha^{tree}}{16\pi^2}$$



# Dim= 6 Operators with one heavy $N$ [1]



Tree-level generated :

•  $\mathcal{O}_{NI\phi}^i = i(\phi^T \epsilon D_\mu \phi)(\bar{N} \gamma^\mu l_i)$

$\mathcal{O}_{duNI}^{i,j} = (\bar{d}_j \gamma^\mu u_j)(\bar{N} \gamma_\mu l_i)$

$\mathcal{O}_{LNQd}^{i,j} = (\bar{L}_i N) \epsilon (\bar{Q}_j d_j)$

$\mathcal{O}_{QuNL}^{i,j} = (\bar{Q}_i u_i)(\bar{N} L_j)$

$\mathcal{O}_{QNLd}^{i,j} = (\bar{Q}_i N) \epsilon (\bar{L}_j d_j)$

$\mathcal{O}_{LNLI}^{i,j} = (\bar{L}_i N) \epsilon (\bar{L}_j l_j)$

[1] F. del Aguila PLB (2009) 0806.0876, Liao PRD (2017) 1612.04527, Bhattacharya PRD (2016) 1505.05264

# Bounds on the couplings $\alpha_{\mathcal{J}}^{(i)}$ ( $\nu$ SMEFT)

Translate existing bounds on seesaw mixings!

## • Effective CC

$$\mathcal{L}_{NI\phi}^{d=6} \supset \frac{-vm_W}{\sqrt{2}} \frac{\alpha_W^{(i)}}{\Lambda^2} \bar{l}_i \gamma^\mu P_R N W_\mu^-$$

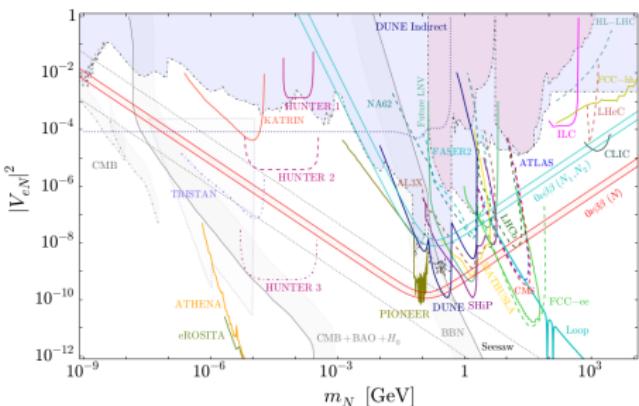
$$U_{l_i N} \simeq \frac{\alpha^{(i)} v^2}{2\Lambda^2}$$

## • seesaw CC

$$\mathcal{L}_{\nu}^{d=4} \supset \frac{-g}{\sqrt{2}} U_{l_i N} \bar{l}_i \gamma^\mu P_L N W_\mu^-$$

$$g = \frac{2m_W}{v}$$

[\*] FIPs Antel et. al. 2305.01715, EPJC (2023)

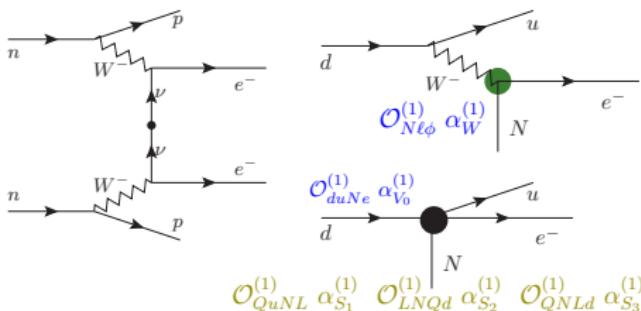


- $\alpha_{0\nu\beta\beta}^{\text{bound}} \lesssim 3.2 \times 10^{-2} \left(\frac{m_N}{100\text{GeV}}\right)^{1/2}$

on first family operators

- Neutrinoless double beta decay:

$$\text{KamLAND-Zen } \tau_{0\nu\beta\beta} \geq 1.1 \times 10^{26} \text{ yr}$$



[\*\*] Also see Fernández-Martínez 2304.06772, JHEP(2023) and R.Beltrán 2302.03216, JHEP (2023)

# Our agnostic benchmark: every operator ON

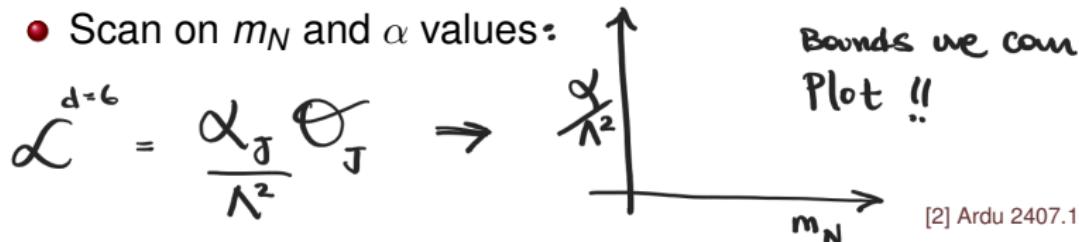
Why??

- ...Different operators mix under renormalization between scales [2]
- Allow  $N$  production and decay to depend on different physics



We consider

- Operators contributing to  $0\nu\beta\beta$ -decay (first family) set to  $\alpha_{0\nu\beta\beta}^{\text{bound}} \lesssim 3.2 \times 10^{-2} \left(\frac{m_N}{100\text{GeV}}\right)^{1/2}$
- Every other operator set to the same numerical value  $\alpha$ : mostly second and third families flavors...
- Scan on  $m_N$  and  $\alpha$  values:

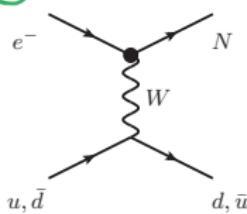


[2] Ardu 2407.16751, JHEP (2024)

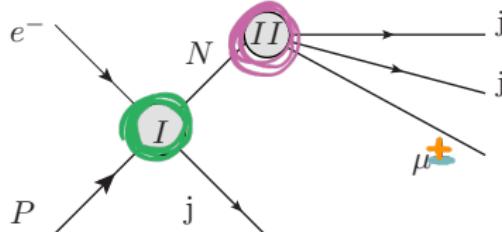
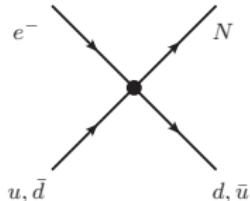
# Lepton-trijet signals at the LHeC [3]

- Lepton Flavor violation:  $p e^- \rightarrow j N \rightarrow j \mu^- jj$
- Lepton Number violation:  $p e^- \rightarrow j N \rightarrow j \mu^+ jj$   
(and flavor)

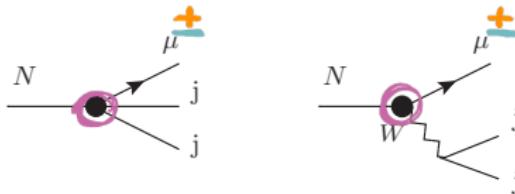
**I**  
 $\mathcal{O}_{Ne\phi}$



$\mathcal{O}_{duNe}, \mathcal{O}_{QuNL}, \mathcal{O}_{LNQd}, \mathcal{O}_{QNLd}$



$N$  production  
affected by  
0v $\beta\beta$ -decay  
bound

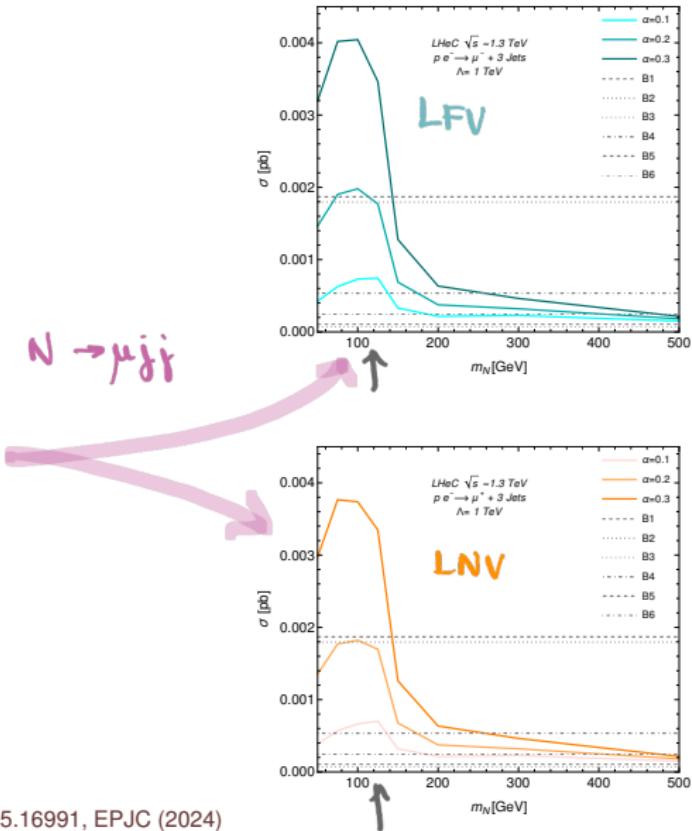
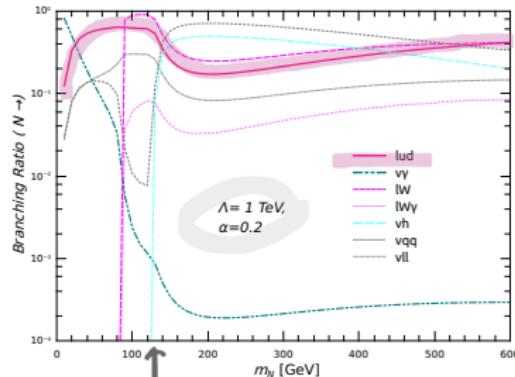
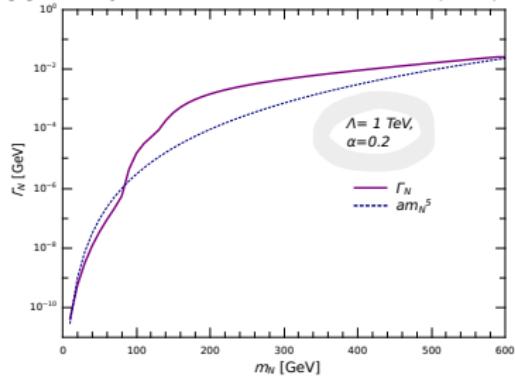


$N$  decay to  
muons is  
less  
constrained

[3] G. Zapata, T.Urruzola, O.A. Sampayo, L. Duarte 2305.16991, EPJC (2024)

# Lepton-trijet signals at the LHeC [3]

[4] N decays: L.Duarte 1603.08052, EPJC (2016)

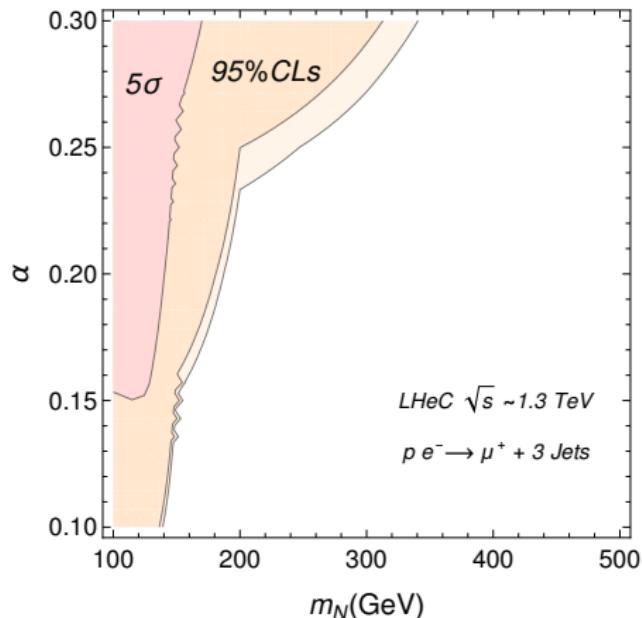
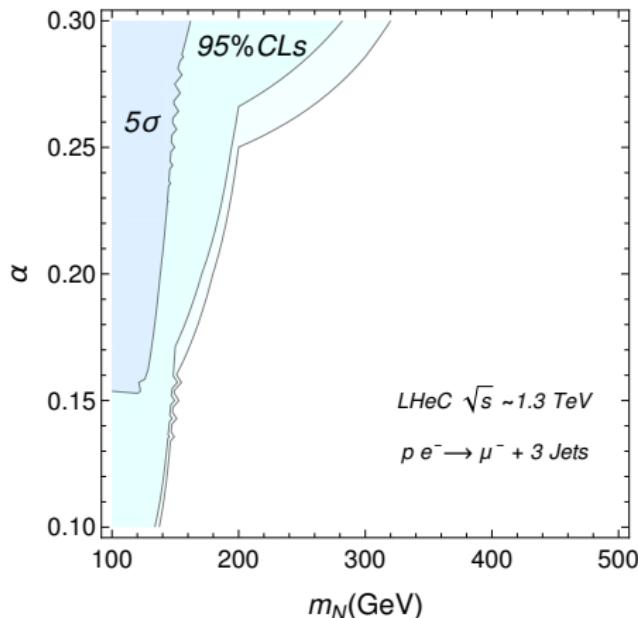


[3] G. Zapata, T. Urruzola, O.A. Sampayo, L. Duarte, 2305.16991, EPJC (2024)

# $\nu$ SMEFT Sensitivity prospects for LHeC: [3]

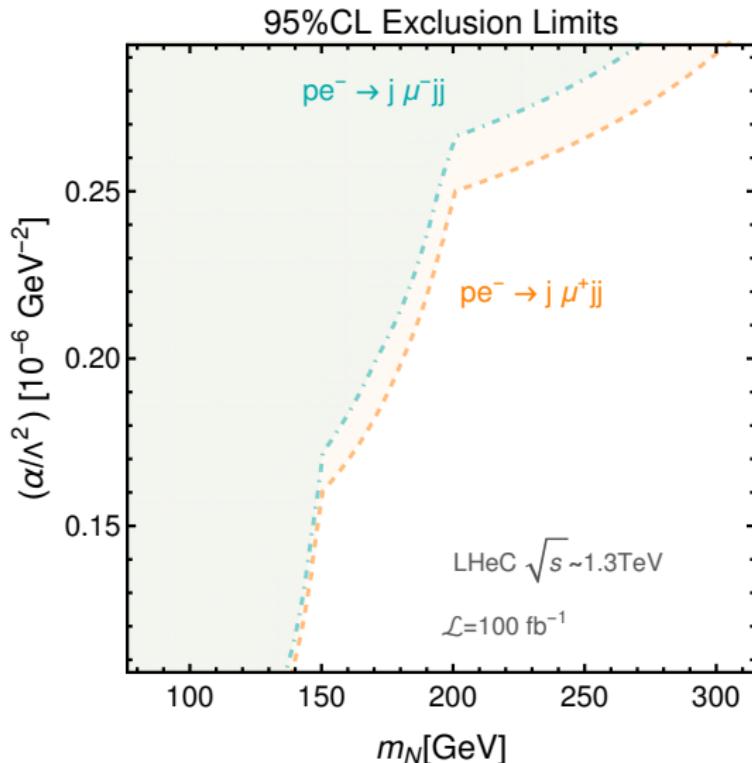
5 $\sigma$ -Discovery and 95% CLs limits at the LHeC:  $\mathcal{L} = 100 \text{ fb}^{-1}$  ( $\Lambda = 1 \text{ TeV}$ ) from lepton-trijet signals. (BDT analysis)

Bounds affect (mostly) to 2nd. family couplings



[3] G. Zapata, T. Urruzola, O.A. Sampayo, L. Duarte 2305.16991, EPJC (2024)

# $\nu$ SMEFT Sensitivity prospects for LHeC: [3]

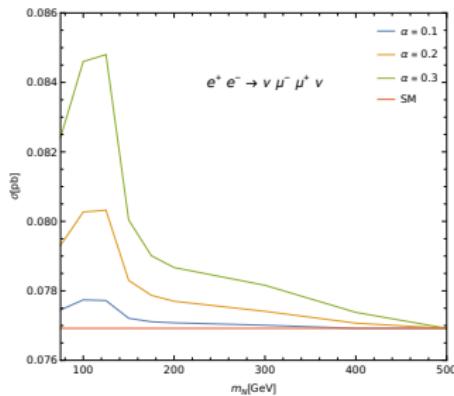
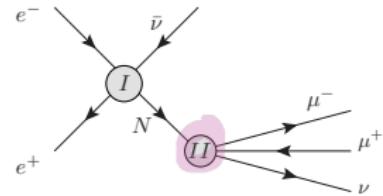


[3] G. Zapata, T.Urruzola, O.A. Sampayo, L. Duarte 2305.16991, EPJC (2024)

# Lepton collider $\nu$ SMEFT sensitivity prospects [4] Work in progress

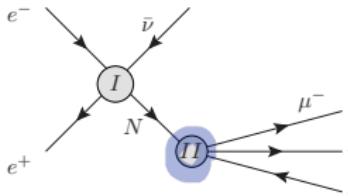
- Single  $N$  production and leptonic decay

- $e^+e^- \rightarrow \nu\mu^+\mu^-\nu$

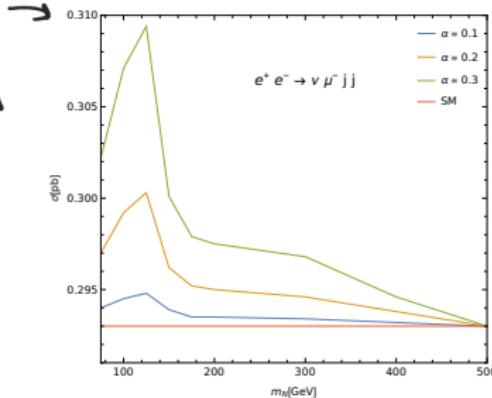


- Single  $N$  production and semi-leptonic decay

- $e^+e^- \rightarrow \nu\mu^-jj$

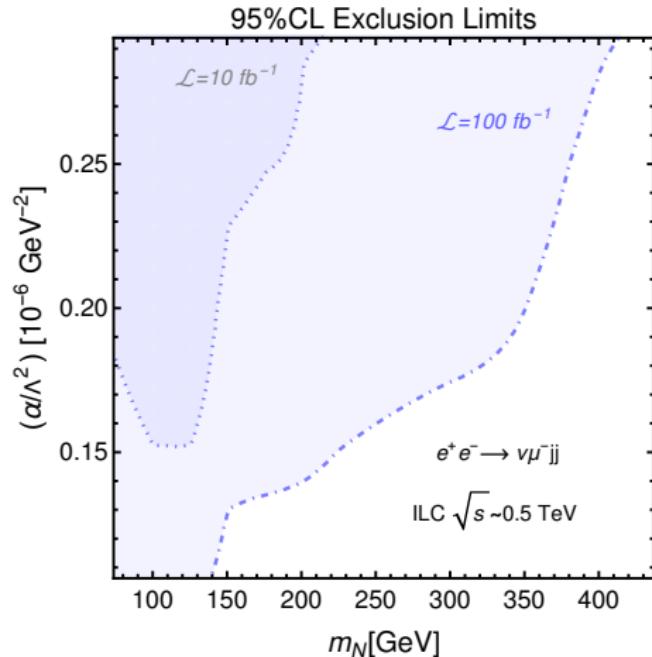
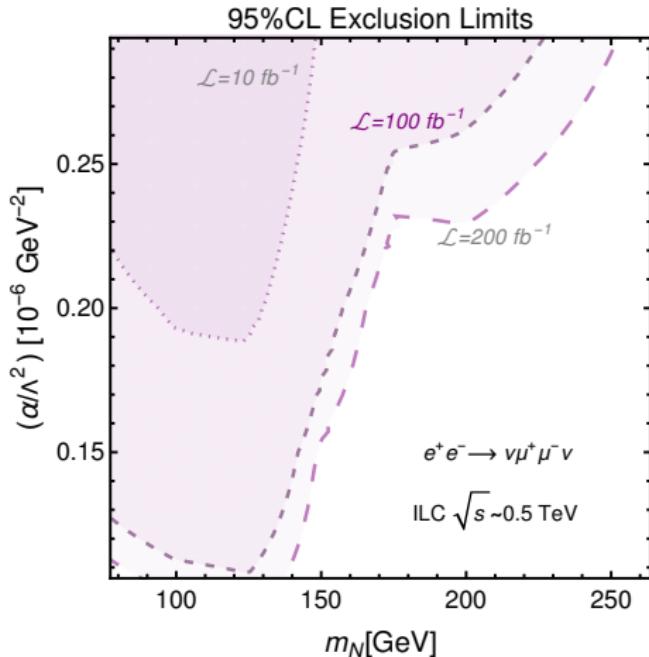


*Much bigger cross section*



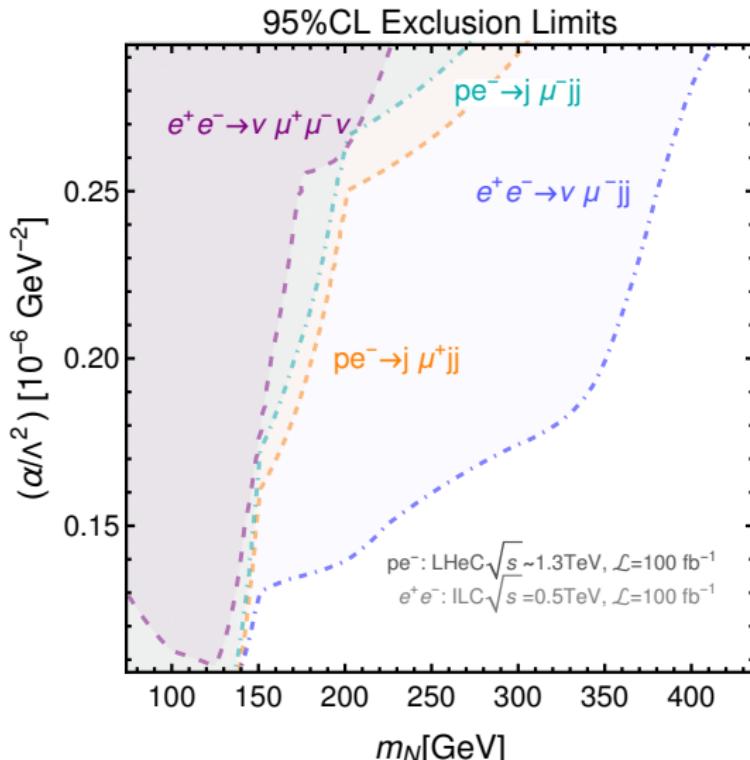
# Lepton collider $\nu$ SMEFT sensitivity prospects [4] Work in progress

Exclusion limits at the ILC: cut based analysis we already proposed in [5]



[5] G. Zapata, T. Urruzola, O. Sampayo and L. Duarte, 2201.02480, EPJC (2022)

# Future collider $\nu$ SMEFT sensitivity prospects [4] Work in progress



[4] L. Duarte, D. Chalencon, T. Urruzola 25XX.XXXXX: Work in progress

# Take home message

- $\nu$ SMEFT: model independent info on new physics contributions to heavy  $N$  (HNL) phenomenology (beyond seesaw mixing!)
- 95% CLs exclusion limits in  $\mathcal{O}(EW)$   $m_N - \alpha$  plane show future LHeC and ILC (or FCC-ee) could constrain the effective couplings (muon family) to a region as tight as the bounds that are currently considered for  $m_N \lesssim \mathcal{O}(10)$  GeV

(See Fernández-Martínez 2304.06772, JHEP(2023) and R.Beltrán 2302.03216, JHEP (2023))

- Lots of parameter space to be explored yet!

| Thanks for your attention!

Curiosity? lucia.duarte@fcien.edu.uy

# $\nu$ SMEFT: (Backup)

- EFT with  $N_R^i$  and SM fields

$$\mathcal{L} = \mathcal{L}_{SM} + \mathcal{L}_\nu + \mathcal{L}^5 + \mathcal{L}^6 + \dots$$

- Non-renormalizable operators (dim > 5) [1]:

$$\mathcal{O}_W^{(5)} = \sum_{\ell\ell'} \frac{(\alpha_W)_{\ell\ell'}}{\Lambda} \bar{L}_{\ell,L} \tilde{\phi}^* \tilde{\phi}^\dagger L_{\ell',L} + h.c. \quad (\mathcal{O}_{LH})$$

Weinberg operator  
 $\nu_L$  Majorana mass

$$\mathcal{O}_{N\phi}^{(5)} = \sum_{ij} \frac{(\alpha_{N\phi})_{ij}}{\Lambda} \bar{N}_{i,R} N_{j,R}^c \phi^\dagger \phi + h.c. \quad (\mathcal{O}_{NNH})$$

+  $N_R$  Majorana mass  
 $N$

$$\mathcal{O}_{NB}^{(5)} = \sum_{i \neq j} \frac{(\alpha_{NB})_{ij}}{\Lambda} \bar{N}_{i,R} \sigma_{\mu\nu} N_{j,R}^c B^{\mu\nu} + h.c. \quad (\mathcal{O}_{NNB})$$

$N$  dipole  
 Coupling

[\*] See: Graesser PRD(2007) 0704.0438, Aparici (PRD 2009) 0904.3244 and Caputo (JHEP 2017) 1704.08721,

See Joel Jones's talk!

Delgado JHEP 09(2022)079, 2205.13550

+ 2311.17989 JHEP(2024)

# Dim= 6 operators: renormalizable UV-realizations

$$\mathcal{L}^{\text{tree}} \supset \frac{1}{\Lambda^2} \sum_{i,j} \left\{ -\alpha_W^{(i)} \frac{v m_W}{\sqrt{2}} \bar{l}_i \gamma^\nu P_R N W_\mu^- \right.$$

$$+ \alpha_{duNI}^{(i,j)} (\bar{u}_j \gamma^\nu P_R d_j \bar{l}_i \gamma_\nu P_R N)$$

$$+ \alpha_{LNLI}^{(i,j)} (\bar{\nu}_i P_R N \bar{l}_j P_R l_j - \bar{\nu}_j P_R l_j \bar{l}_i P_R N)$$

$$+ \alpha_{QuNL}^{(i,j)} (\bar{u}_j P_L d_j \bar{l}_i P_R N + \bar{u}_j P_L u_j \bar{\nu}_i P_R N)$$

$$+ \alpha_{LNQd}^{(i,j)} (\bar{d}_j P_R d_j \bar{\nu}_i P_R N - \bar{u}_j P_R d_j \bar{l}_i P_R N)$$

$$+ \alpha_{QNLd}^{(i,j)} (\bar{u}_i P_R N \bar{l}_j P_R d_j - \bar{d}_i P_R N \bar{\nu}_j P_R d_j)$$

$$+ \text{h.c.} \}$$



UV-mediator :



charged and  
Neutral SCALARS

SCALAR LEPTOQUARKS

- A renormalizable UV-completion is needed for Majorana N 4f vertices to work in MadGraph5

See also: G.Zapata Eur.Phys.J.C 82(2022)6, 2201.02480 and G. Cottin JHEP 09(2021)039, 2105.13851