

The profile of non-standard cosmic strings

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XV Latin American Symposium on High Energy Physics
November 4 2024

Kibble Mechanism

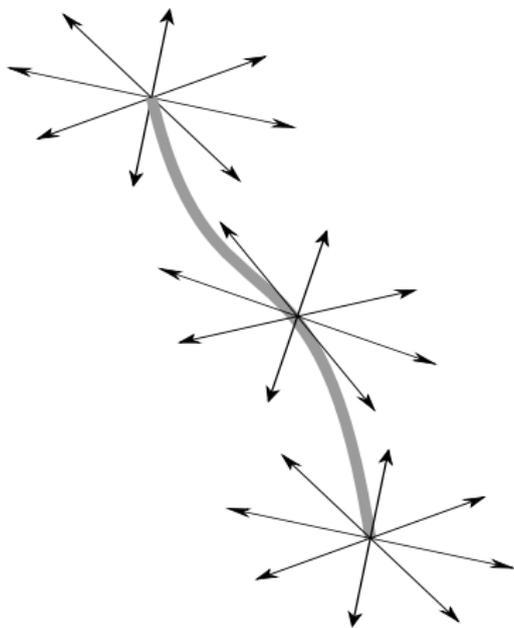
It is generally assumed that phase transitions occurred in the early universe at the late stages of inflation. These transitions could have possibly formed topological defects.

Examples:

- ▶ $\pi_0(\mathcal{M}) \neq I \Rightarrow$ Domain wall
- ▶ $\pi_1(\mathcal{M}) \neq I \Rightarrow$ Vortex (2d), cosmic strings (3d)
- ▶ $\pi_2(\mathcal{M}) \neq I \Rightarrow$ Monopole

\mathcal{M} : Vacuum manifold.

Cosmic Strings



2-dimensional vortices stacked on top of each other,
forming a cosmic string in three dimensions

$U(1)_{B-L}$ exact global symmetry

In the Standard Model $U(1)_{B-L}$ is an **exact** global symmetry. B baryon number, L lepton number.

This is strange, an exact symmetry is only natural when it is local.

We promote $U(1)_{B-L}$ to a local symmetry that couples to the hypercharge.

Gauge symmetry

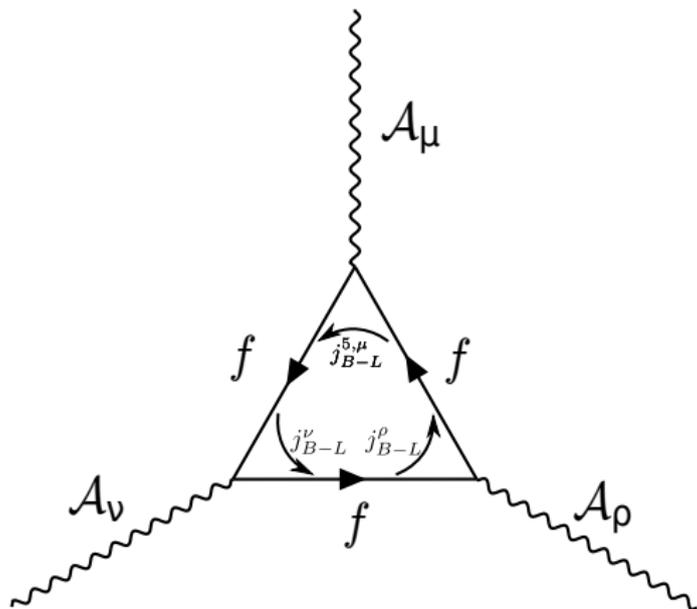
We introduce a new gauge coupling h' and define a new charge as

$$Y' \equiv 2hY + \frac{h'}{2}(B - L),$$

h, h' gauge couplings.

We take the gauge group to be $U(1)_{Y'}$ and we call the gauge field \mathcal{A}_μ .

Gauge Anomaly



In each vertex the quarks of one generation contribute with $B = 4$, and leptons with $L = 3$.
 $B - L \neq 0$.

Gauge anomaly. It is cured by adding a ν_R ($L = 1$) to each generation.

Since the neutrinos have mass, it is natural to introduce a mechanism to give mass to the neutrinos.

We can introduce masses to ν_L , ν_R , normally through the Higgs mechanism.

To add a mass term solely for ν_R , independently of ν_L , we add a non-standard Higgs field $\chi \in \mathbb{C}$

$$f_{\nu_R} \nu_R^T \chi C^\dagger \nu_R + \text{c.c.},$$

where f_{ν_R} is a Yukawa coupling.

To preserve gauge invariance, the field χ must have a charge $B - L = 2$.

We generate the Majorana-type mass with the Higgs mechanism using a non-standard Higgs field $\chi \in \mathbb{C}$.

We denote the vacuum expectation value of χ as v' .

χ gives a Majorana-type mass to the right-handed neutrino $M = f_{\nu_R} v'$.

χ is added to the Lagrangian with a quartic potential (power counting renormalizable)

$$V' = \frac{m'^2}{2} \chi^* \chi + \frac{\lambda'}{4} (\chi^* \chi)^2.$$

It is natural to include (normalizable, gauge invariant)

$$\frac{\kappa}{2} \Phi^\dagger \Phi \chi^* \chi.$$

We assume that $v' > v$ and f_{ν_R} sufficiently large.

Lagrangian

$$\begin{aligned}\mathcal{L} = & \frac{1}{2}(D^\mu\Phi)^\dagger D_\mu\Phi - \frac{m^2}{2}\Phi^\dagger\Phi - \frac{\lambda}{4}(\Phi^\dagger\Phi)^2 - \frac{\lambda}{4}v^4 \\ & + \frac{1}{2}(d^\mu\chi)^* d_\mu\chi - \frac{m'^2}{2}\chi^*\chi - \frac{\lambda'}{4}(\chi^*\chi)^2 - \frac{\lambda'}{4}v'^4 \\ & - \frac{\kappa}{2}\Phi^\dagger\Phi\chi^*\chi - \frac{\kappa}{2}v^2v'^2 - \frac{1}{4}\mathcal{F}^{\mu\nu}\mathcal{F}_{\mu\nu},\end{aligned}$$

- ▶ $\Phi = (\phi_+, \phi_0)^\top \in \mathbb{C}^2$
- ▶ $D_\mu\Phi = (\partial_\mu + ih\mathcal{A}_\mu)\Phi$
- ▶ $d_\mu\chi = (\partial_\mu + ih'\mathcal{A}_\mu)\chi$
- ▶ $\mathcal{F}_{\mu\nu} = \partial_\mu\mathcal{A}_\nu - \partial_\nu\mathcal{A}_\mu$

For the potential to be bounded from below, we need

$$\lambda > 0, \quad \lambda' > 0, \quad \kappa^2 < \lambda\lambda',$$

and for spontaneous symmetry breaking to occur

$$m^2 = -\kappa v'^2 - \lambda v^2 < 0,$$
$$m'^2 = -\kappa v^2 - \lambda' v'^2 < 0.$$

(Tree level analysis)

Equations of motion

$$\begin{aligned}D^\mu D_\mu \Phi &= -m^2 \Phi - \lambda(\Phi^\dagger \Phi)\Phi - \kappa \Phi \chi^* \chi \\d^\mu d_\mu \chi &= -m'^2 \chi - \lambda'(\chi^* \chi)\chi - \kappa \chi \Phi^\dagger \Phi \\ \partial^\lambda \mathcal{F}_{\lambda\nu} &= -\frac{ih}{2} [(D_\nu \Phi)^\dagger \Phi - \Phi^\dagger (D_\nu \Phi)] \\ &\quad -\frac{ih'}{2} [(d_\nu \chi)^* \chi - \chi^* (d_\nu \chi)]\end{aligned}$$

Ansatz

The Lagrangian has a $U(1)_{Y'}$ symmetry which can “spontaneously break” down to $\mathbb{1}$.

$\mathcal{M} = U(1)_{Y'}/\mathbb{1} = U(1) \Rightarrow \pi_1(U(1)) = \mathbb{Z} \Rightarrow$ cosmic strings.

We only consider the component ϕ_0 of the Higgs field Φ . Cylindrically symmetric ansatz (const. in z)

$$\phi_0(r, \varphi) = \phi(r) e^{in\varphi}$$

$$\chi(r, \varphi) = \xi(r) e^{in'\varphi}, \quad n, n' \text{ winding numbers}$$

$$\mathcal{A}(r) = \frac{a(r)}{r} \hat{\varphi}.$$

Equations of motion

$$\partial_r^2 \phi + \frac{1}{r} \partial_r \phi - \frac{(n + ha)^2}{r^2} \phi - m^2 \phi - \lambda \phi^3 - \kappa \phi \xi^2 = 0$$

$$\partial_r^2 \xi + \frac{1}{r} \partial_r \xi - \frac{(n' + h'a)^2}{r^2} \xi - m'^2 \xi - \lambda' \xi^3 - \kappa \xi \phi^2 = 0$$

$$\partial_r^2 a - \frac{1}{r} \partial_r a - h(n + ha)\phi^2 - h'(n' + h'a)\xi^2 = 0.$$

Boundary conditions ($n, n' \neq 0$)

$$\phi(0) = 0, \quad \lim_{r \rightarrow \infty} \phi(r) = v$$

$$\xi(0) = 0, \quad \lim_{r \rightarrow \infty} \xi(r) = v'$$

$$a(0) = 0, \quad \lim_{r \rightarrow \infty} a(r) = -\frac{n}{h} = -\frac{n'}{h'}.$$

Boundary value problem, numerical solutions with the damped Newton method.

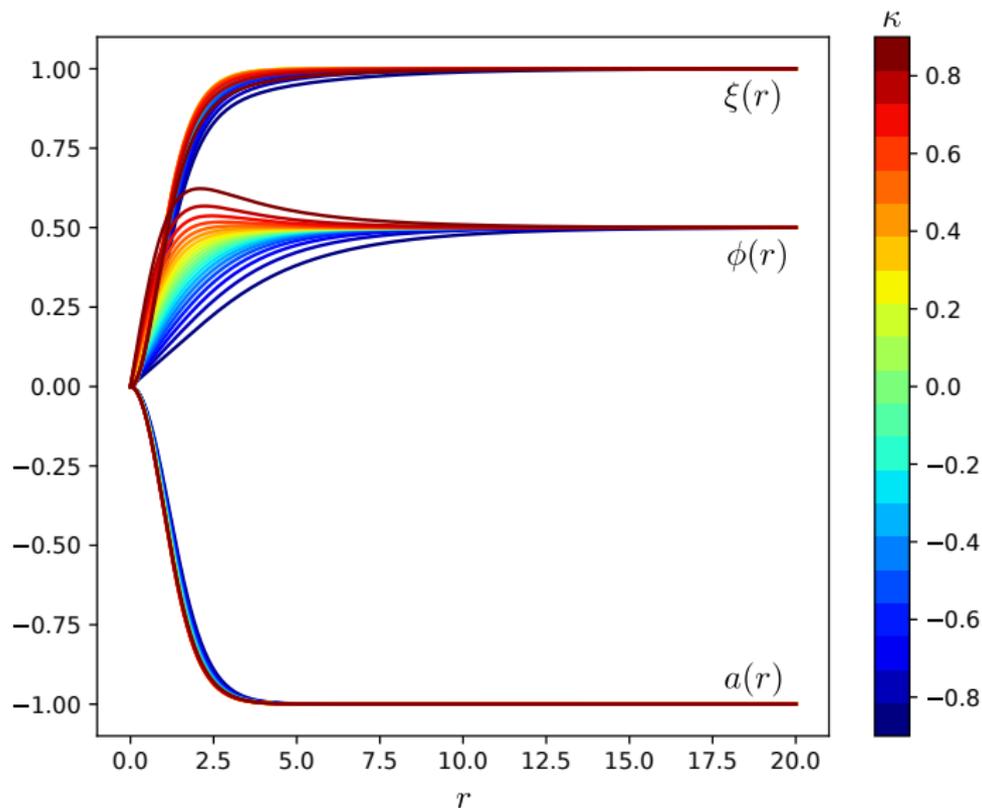
Solutions uniquely defined by inserting v , v' , λ , λ' , h , h' , n and n' .

We choose $v' > v$.

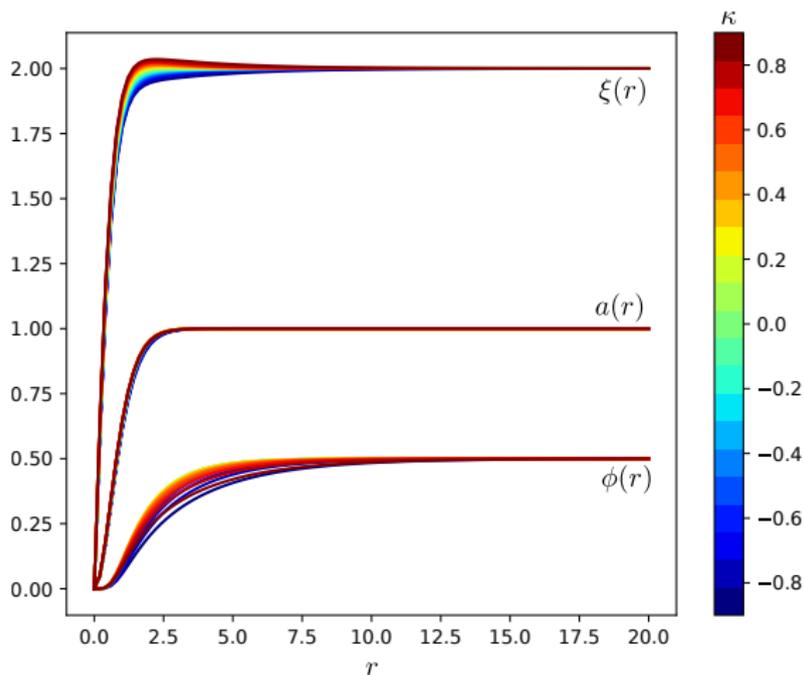
$v^{\text{phys}} = 246 \text{ GeV}$ is used to convert all dim'less variables to physical units.

We display the profile radius r , where $r = 1$ corresponds in physical units to

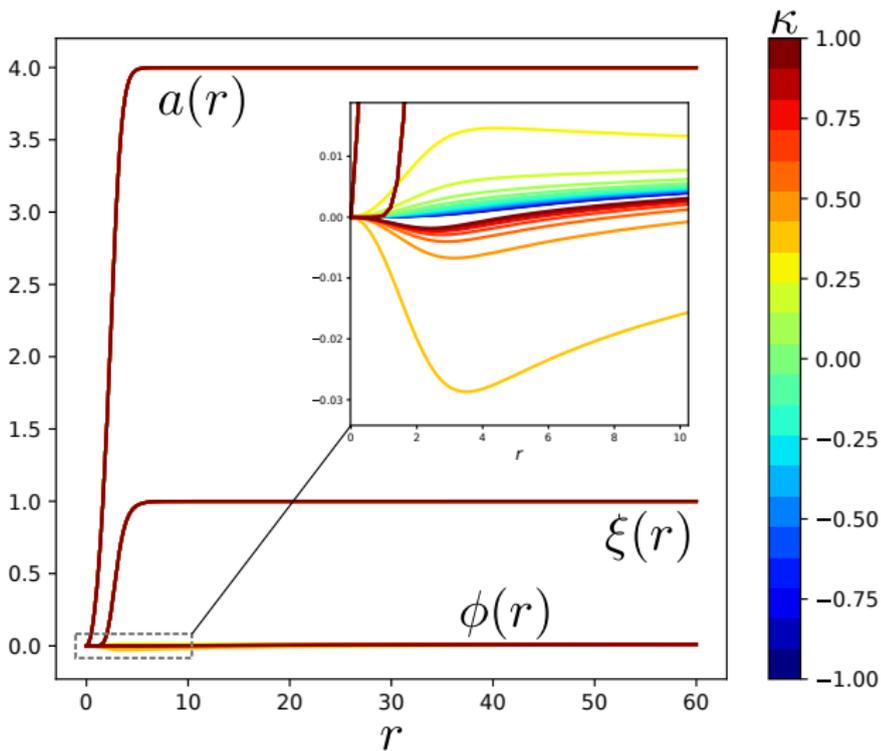
$$v \cdot 0.0008 \text{ fm.}$$



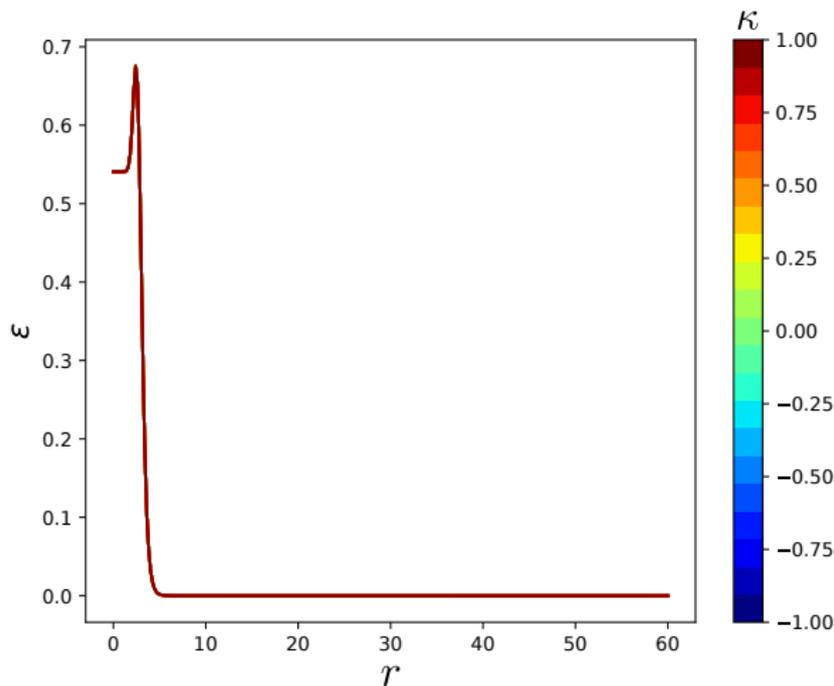
$$\nu = 0.5, \nu' = 1, n = 1, n' = 2, h = 1, h' = 2, \\ \lambda = \lambda' = 1.$$



$\nu = 0.5$, $\nu' = 2$, $n = -5$, $n' = -1$, $h = 5$, $h' = 1$,
 $\lambda = \lambda' = 1$. This is an example from the SO(10)
 GUT [Buchmüller/Greub/Minkowski, '91].



Coaxial string solution, cf. [Bogomol'nyi, 1975] with $n = -2$, $h = 0.5$, $n' = 10$, $h' = -2.5$, $\lambda = 1$, $\lambda' = 1$, $v = 0.01$, $v' = 1$.



Energy density, $\nu = 0.01$, $\nu' = 1$, $n = -2$, $n' = 10$,
 $h = 0.5$, $h' = -2.5$, $\lambda = \lambda' = 1$, in units of
 $4.79 \times 10^{19} \text{ GeV}/\text{fm}^3$.

By integrating over the area the energy density, we find that the string tension is of the order of

$$\mu \sim 10^{10} \text{ GeV}^2 = 10^{25} \frac{\text{kg}}{\text{pc}}.$$

Therefore

$$G\mu \sim 10^{-28},$$

where $G = \frac{1}{(1.2 \times 10^{19} \text{ GeV})^2}$.

The LIGO/Virgo collaboration set constraints to the string tension

$$G\mu \lesssim 4 \times 10^{-15}.$$

Summary

In this BSM model, motivated from the exactness of $U(1)_{B-L}$, we added

- ▶ A new Abelian gauge field \mathcal{A}_μ
- ▶ A right-handed neutrino ν_R
- ▶ A new Higgs field $\chi \in \mathbb{C}$

A non-standard type of cosmic strings is possible.

Overshoot and coaxial string solutions.

At large distances, they do not affect known physics.