

New Physics Tests with Long Baseline Neutrino Oscillations

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What are “Long Baseline” (LBL) Neutrino Oscillation Experiments?

No clear definition, but usually we refer to neutrino oscillation experiments which use neutrinos produced by accelerators with baseline larger than $\sim O(100)$ km

In this talk, I will restrict to experiments which satisfy this condition

Outline

- **Brief introduction of neutrino oscillations which can be studied by long-baseline (LBL) neutrino experiments**
- **Current Status and Open Questions**
- **Brief review of sensitivities to oscillation parameters to be studied by near future LBL experiments, focusing on DUNE and Hyper-Kamiokande, within the standard 3 flavor framework**
- **New physics beyond SM (beyond masses and mixing of 3 active neutrinos) to be studied (mainly) by DUNE and HK**
- **Summary**

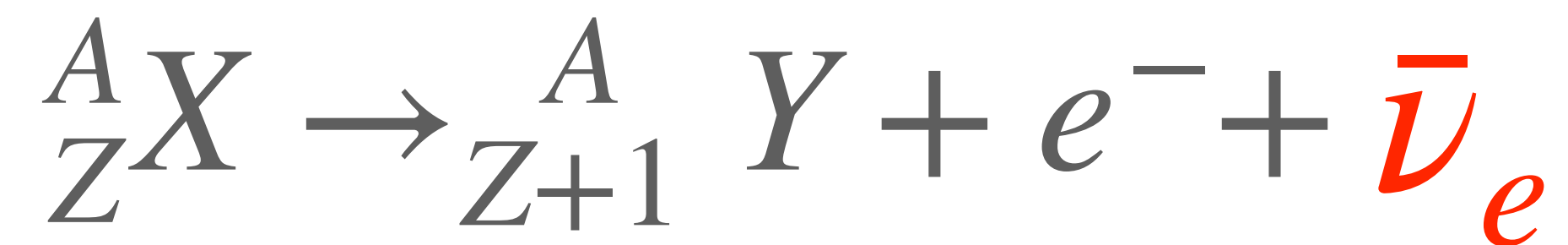
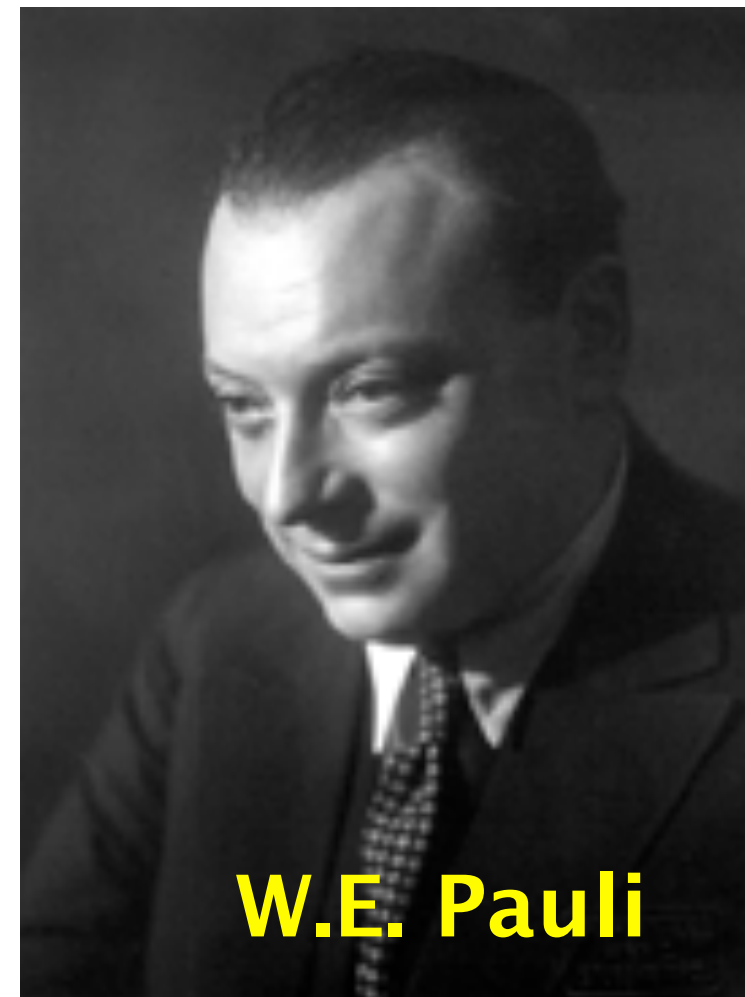
I will focus more on phenomenological aspects, for experimental details, please see talks by Ettore Segreto for DUNE (Friday), Saul Cuen-Rochin for Hyper-K (yesterday), Pedro Ochoa for Short Baseline experiments (today)!

(Very) Brief review of Neutrino Oscillation

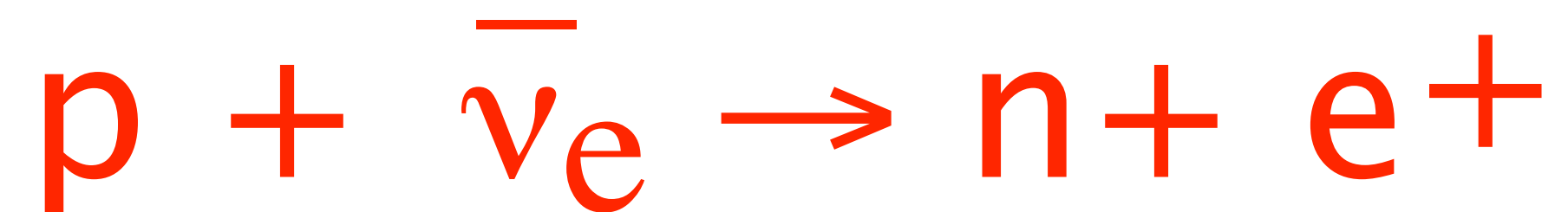
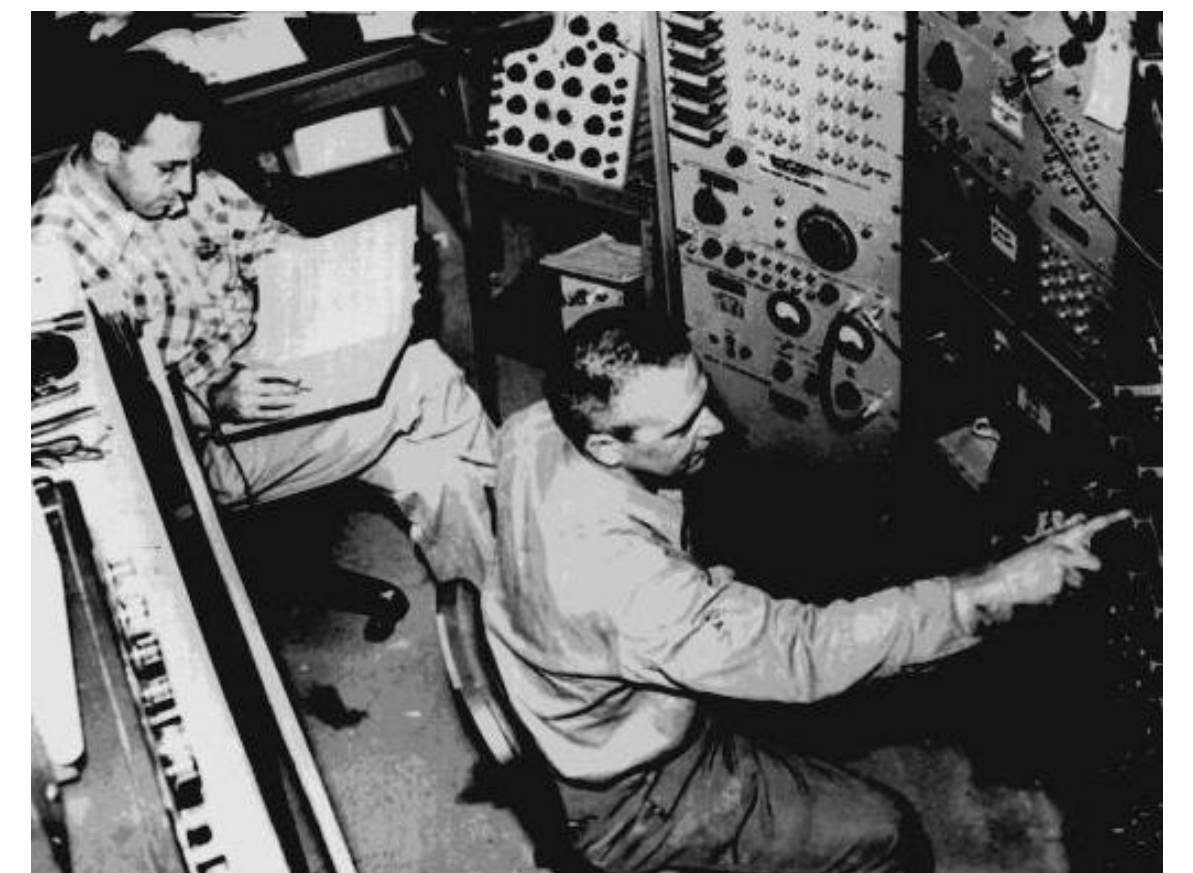
- from theory to experiment -

A bit of History

Neutrino was invented/introduced by W. Pauli in 1930 to explain the problem (of continuous spectra of emitted electrons) observed in beta decays



Discovered/detected for the first time by Rines and Cowan in 1956 by using reactor neutrinos through the IBD (inverse beta decay) reaction



1995

Period (until 1998) after the first detection of neutrino

1956-1998 (~40 years): steady progress from both theoretical and experimental point of view

Theory: possibility of non-zero neutrino masses, concept of neutrino mixing, neutrino oscillation, nature of neutrino, Dirac or Majorana, etc

Experiments: detection of ν_μ , observations of neutrinos from various different sources, detection of supernova (SN1987A) neutrinos, solar neutrino problem, atmospheric neutrino anomaly, etc.

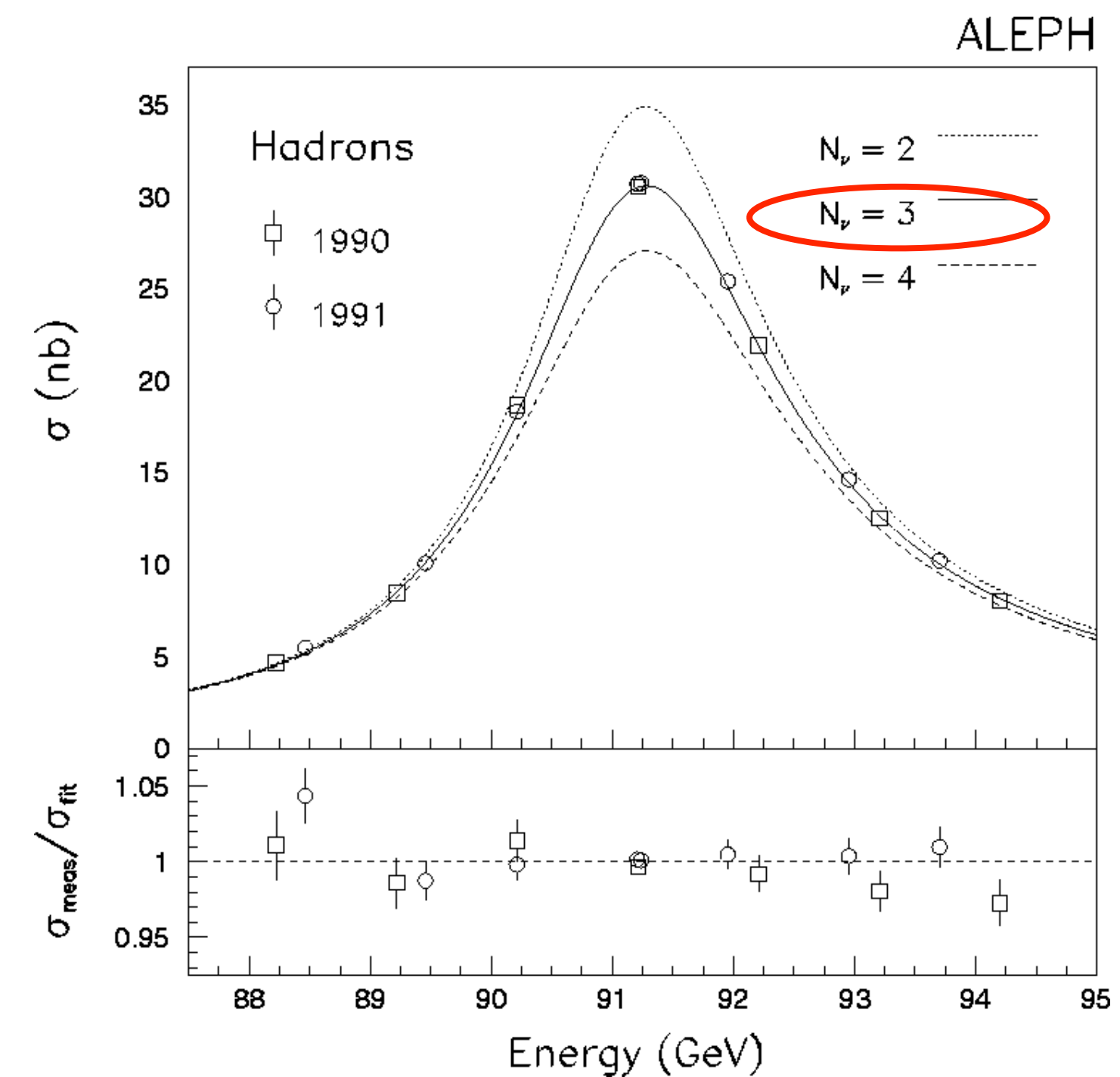
We know that there are three types (flavors) of “active” neutrinos associated to charged leptons, e , μ and τ

$$\begin{pmatrix} \nu_e \\ e^- \end{pmatrix} \quad \begin{pmatrix} \nu_\mu \\ \mu^- \end{pmatrix} \quad \begin{pmatrix} \nu_\tau \\ \tau^- \end{pmatrix}$$

and their anti-particles or anti-neutrinos

$$\begin{pmatrix} \bar{\nu}_e \\ e^+ \end{pmatrix} \quad \begin{pmatrix} \bar{\nu}_\mu \\ \mu^+ \end{pmatrix} \quad \begin{pmatrix} \bar{\nu}_\tau \\ \tau^+ \end{pmatrix}$$

see later for “sterile” neutrino(s)



LEP: $N_\nu = 2.984 \pm 0.012$

from the decay width of Z

During ~15 years of 1998 - 2012

**Very Important Discovery
in Neutrino Physics**

Neutrino Oscillation!

During ~15 years of 1998 - 2012

**Very Important Discovery
in Neutrino Physics**

Neutrino Oscillation!

**1998-2012: “Discovery” Phase (Era) of
(several types of) neutrino oscillations**

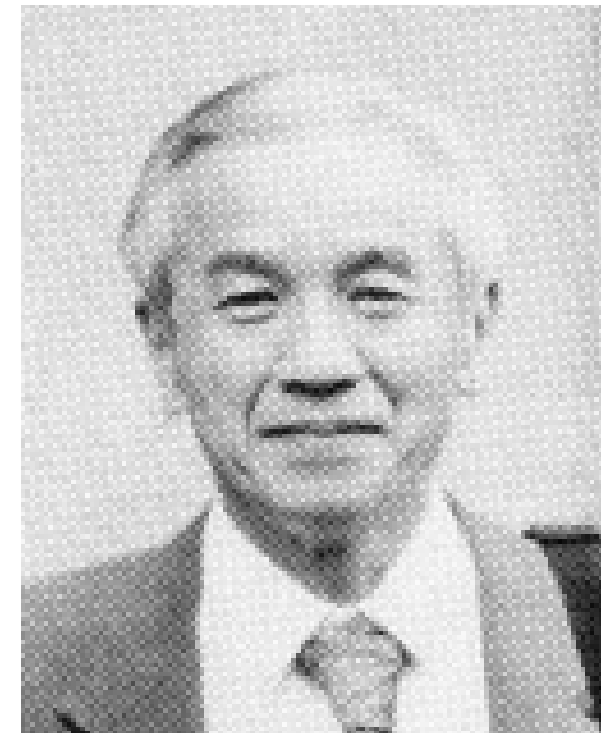
Brief Review of Neutrino Oscillation

from theory point of view

Mixing of Neutrinos



Z. Maki



M. Nakagawa



S. Sakata

1962

If neutrinos have non-zero different masses, assuming only 2 flavors

$$\begin{bmatrix} \nu_e \\ \nu_\mu \end{bmatrix} = \begin{bmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{bmatrix} \begin{bmatrix} \nu_1 \\ \nu_2 \end{bmatrix}$$

flavor eigenstates (pointing to ν_e, ν_μ)

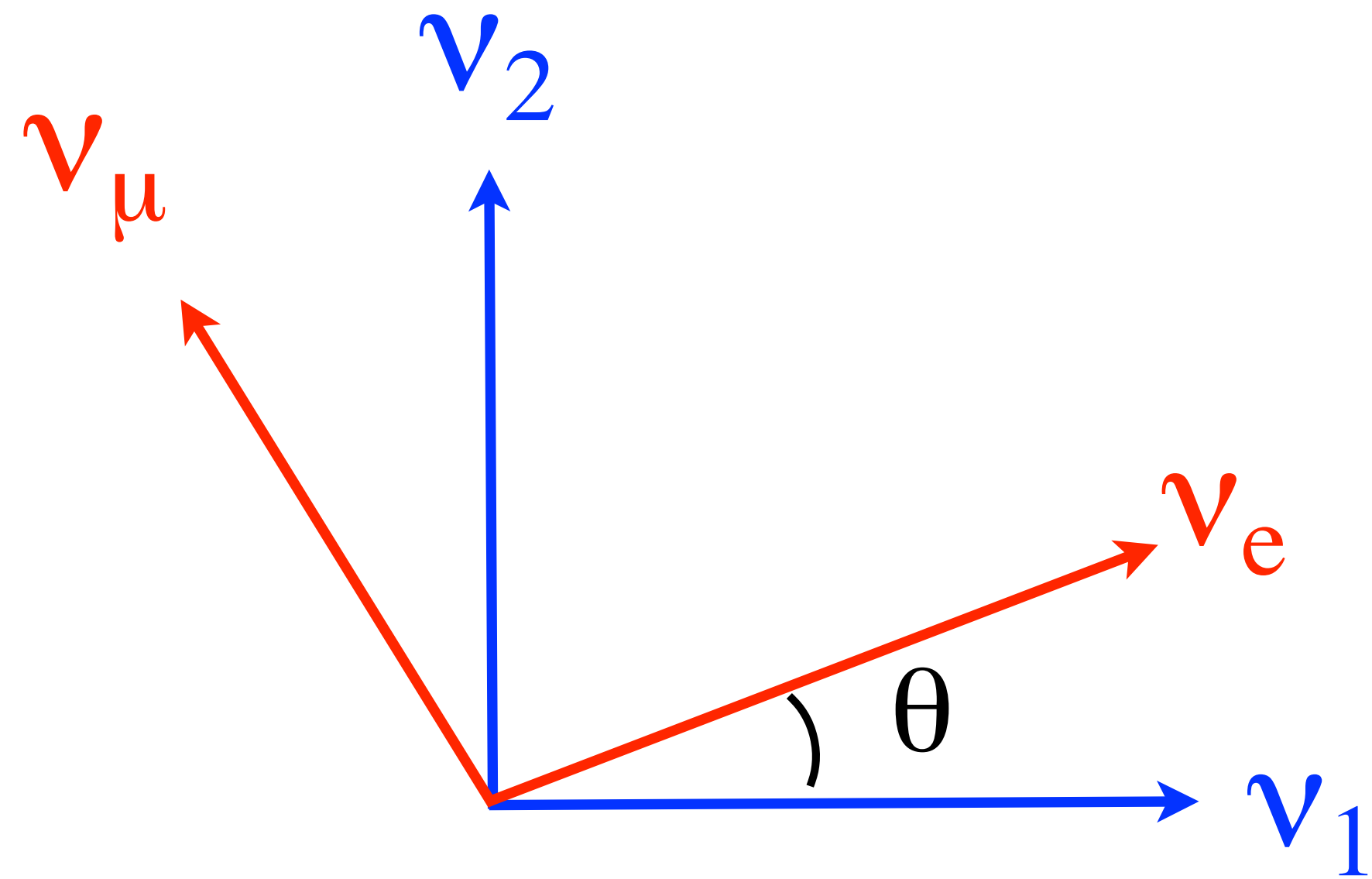
mass eigenstates (pointing to ν_1, ν_2)

θ : mixing angle

$m_1 \neq m_2$

Prog.Theo.Phys. 28 (1962) 870

Mixing of Neutrinos



general neutrino state

$$|\nu\rangle = c_e |\nu_e\rangle + c_\mu |\nu_\mu\rangle$$

$$|\nu\rangle = c_1 |\nu_1\rangle + c_2 |\nu_2\rangle$$

general neutrino state

=

a



+

b



**linear superposition (combination) of
different flavors/masses (states)**

Oscillation Probabilities for 2 flavors in vacuum

For ultra-relativistic neutrino, $E = \sqrt{p^2 + m^2} \sim p + \frac{m^2}{2p} \sim p + \frac{m^2}{2E}$

E: energy, p: momentum, m: mass of neutrino

For the case where the initial state is ν_μ



B. Pontecorvo

$$P(\nu_\mu \rightarrow \nu_e) = \left| \sin \theta \cos \theta e^{-i \frac{m_1^2}{2E} L} + \cos \theta (-\sin \theta) e^{-i \frac{m_2^2}{2E} L} \right|^2$$

$$= \boxed{\sin^2 2\theta} \sin^2 \left[\frac{\Delta m^2}{4E} L \right] \quad \text{: appearance probability}$$

oscillation amplitude

$$P(\nu_\mu \rightarrow \nu_\mu) = 1 - \boxed{\sin^2 2\theta} \sin^2 \left[\frac{\Delta m^2}{4E} L \right] \quad \text{: survival (disappearance) probability}$$

$$\Delta m^2 \equiv m_2^2 - m_1^2 \quad \text{: mass squared difference}$$

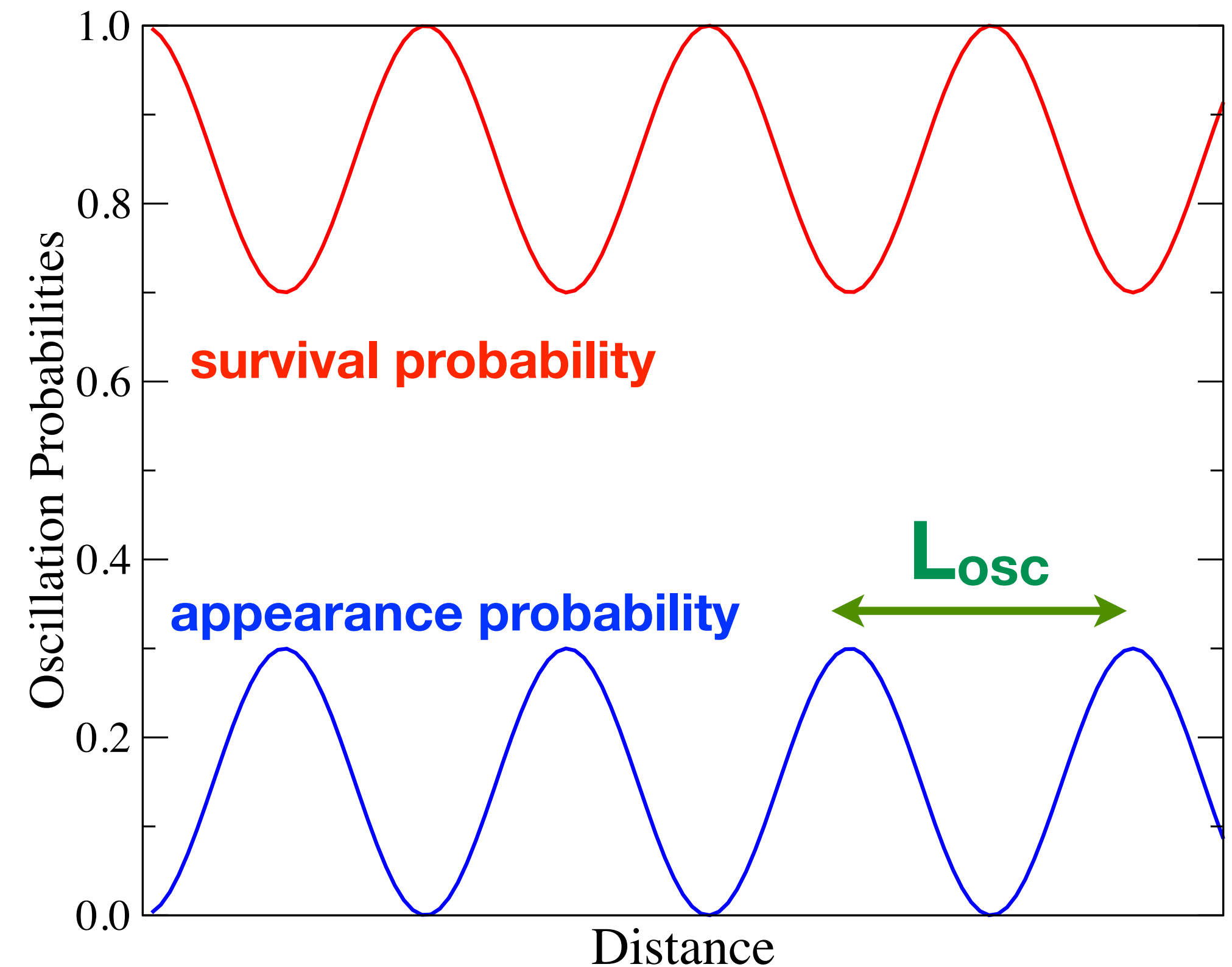
Oscillation Probabilities for 2 flavors in vacuum

$$P(\nu_\mu \rightarrow \nu_e) = \sin^2 2\theta \sin^2 \left[\frac{\Delta m^2}{4E} L \right]$$

appearance probability

$$P(\nu_\mu \rightarrow \nu_\mu) = 1 - \sin^2 2\theta \sin^2 \left[\frac{\Delta m^2}{4E} L \right]$$

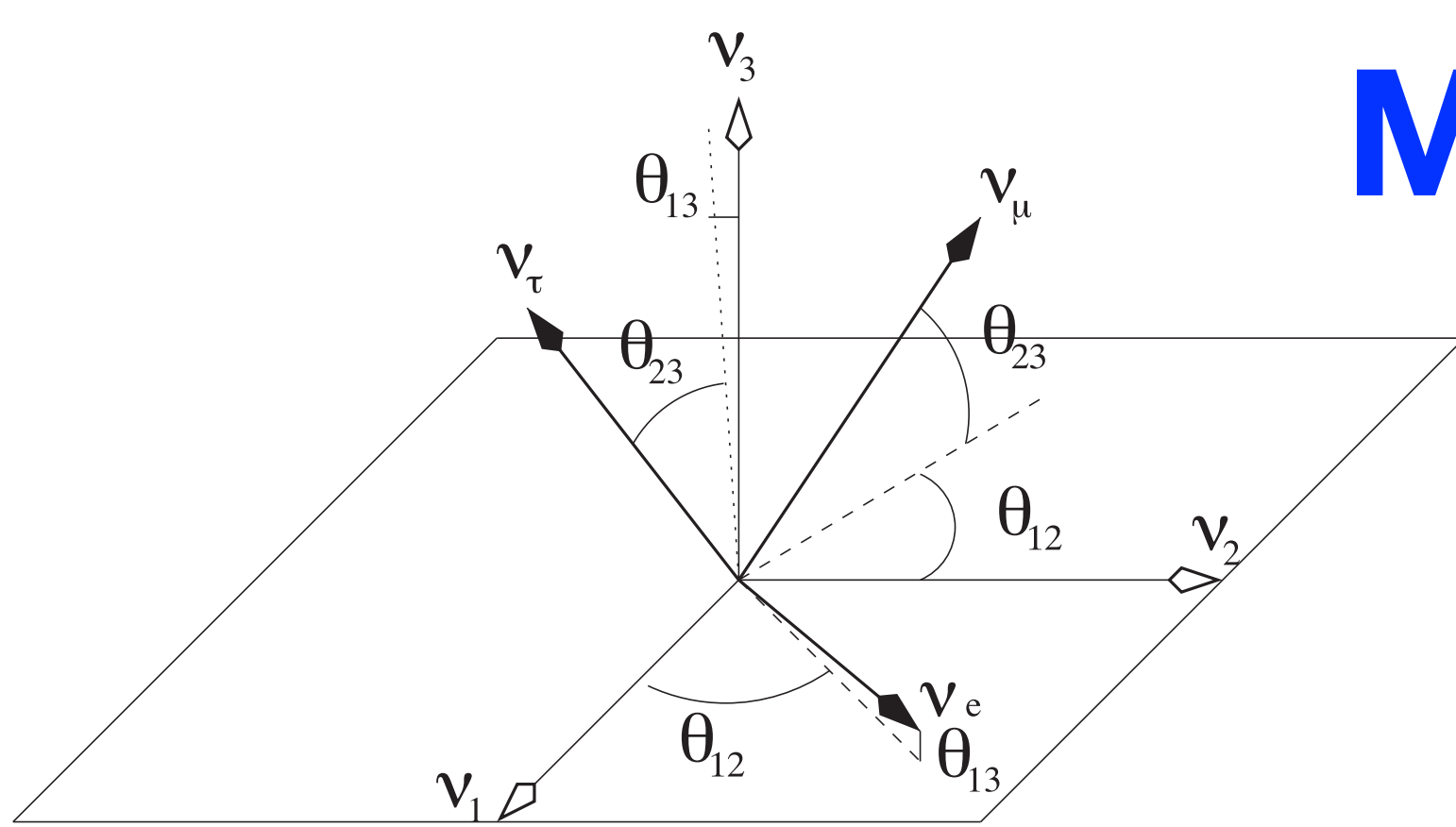
survival probability



$$L_{osc} = \frac{4\pi E}{\Delta m^2} \simeq \frac{\pi}{1.27} \left[\frac{E}{\text{GeV (MeV)}} \right] \left[\frac{\text{eV}^2}{\Delta m^2} \right] \text{ km (m)} : \text{oscillation length}$$

ν oscillation is a powerful tool to probe (indirectly) very tiny neutrino masses

Mixing among 3 flavors of neutrinos



flavor
eigenstates

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix}$$

$$= U_{\text{PMNS}}$$

$$\begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

mass
eigenstates

U_{PMNS} : analogous to CKM matrix

$\theta_{12} \theta_{23} \theta_{13}$ analogous to Euler angles

$$U_{\text{PMNS}} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{bmatrix} \begin{bmatrix} c_{13} & 0 & s_{13}e^{-i\delta_{\text{CP}}} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta_{\text{CP}}} & 0 & c_{13} \end{bmatrix} \begin{bmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

Pontecorvo-Maki-
Nakagawa-Sakata

atmospheric ν osc.

$$c_{ij} \equiv \cos\theta_{ij}, s_{ij} \equiv \sin\theta_{ij}$$

reactor ν osc.

solar ν osc.

For oscillation, 6 indep. parameters: 3 mixing angles, $\theta_{12}, \theta_{23}, \theta_{13}$, 1 CP phase δ_{CP}

and 2 (indep.) mass squared differences

$$\Delta m_{21}^2, \Delta m_{31}^2 (= \Delta m_{32}^2 - \Delta m_{21}^2)$$

Neutrino Oscillation Probabilities in Vacuum

$$P(\alpha \rightarrow \beta) = \left| \sum_j U_{\alpha j}^* U_{\beta j} e^{-i \frac{m_j^2}{2E} L} \right|^2$$
$$= \delta_{\alpha\beta} - 4 \sum_{i>j} \Re[U_{\alpha i}^* U_{\alpha j} U_{\beta i} U_{\beta j}^*] \sin^2 \left(\frac{\Delta m_{ij}^2}{4E} L \right) + 2 \sum_{i>j} \Im[U_{\alpha i}^* U_{\alpha j} U_{\beta i} U_{\beta j}^*] \sin \left(\frac{\Delta m_{ij}^2}{2E} L \right)$$

Oscillation probabilities depends on 6 oscillation parameters

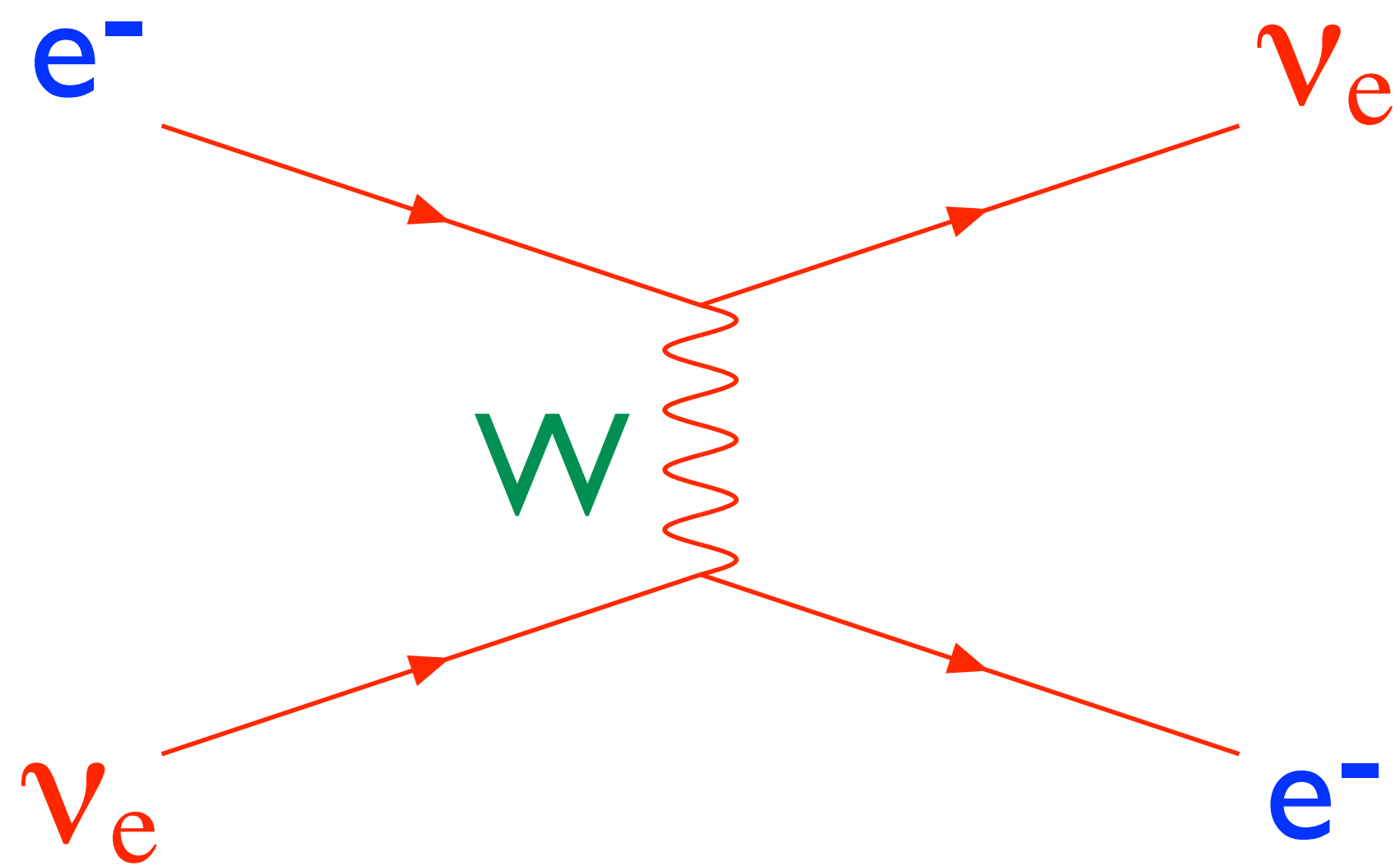
$$\Delta m_{21}^2, \Delta m_{31}^2 (= \Delta m_{32}^2 - \Delta m_{21}^2)$$

$$\theta_{12}, \theta_{23}, \theta_{13}$$

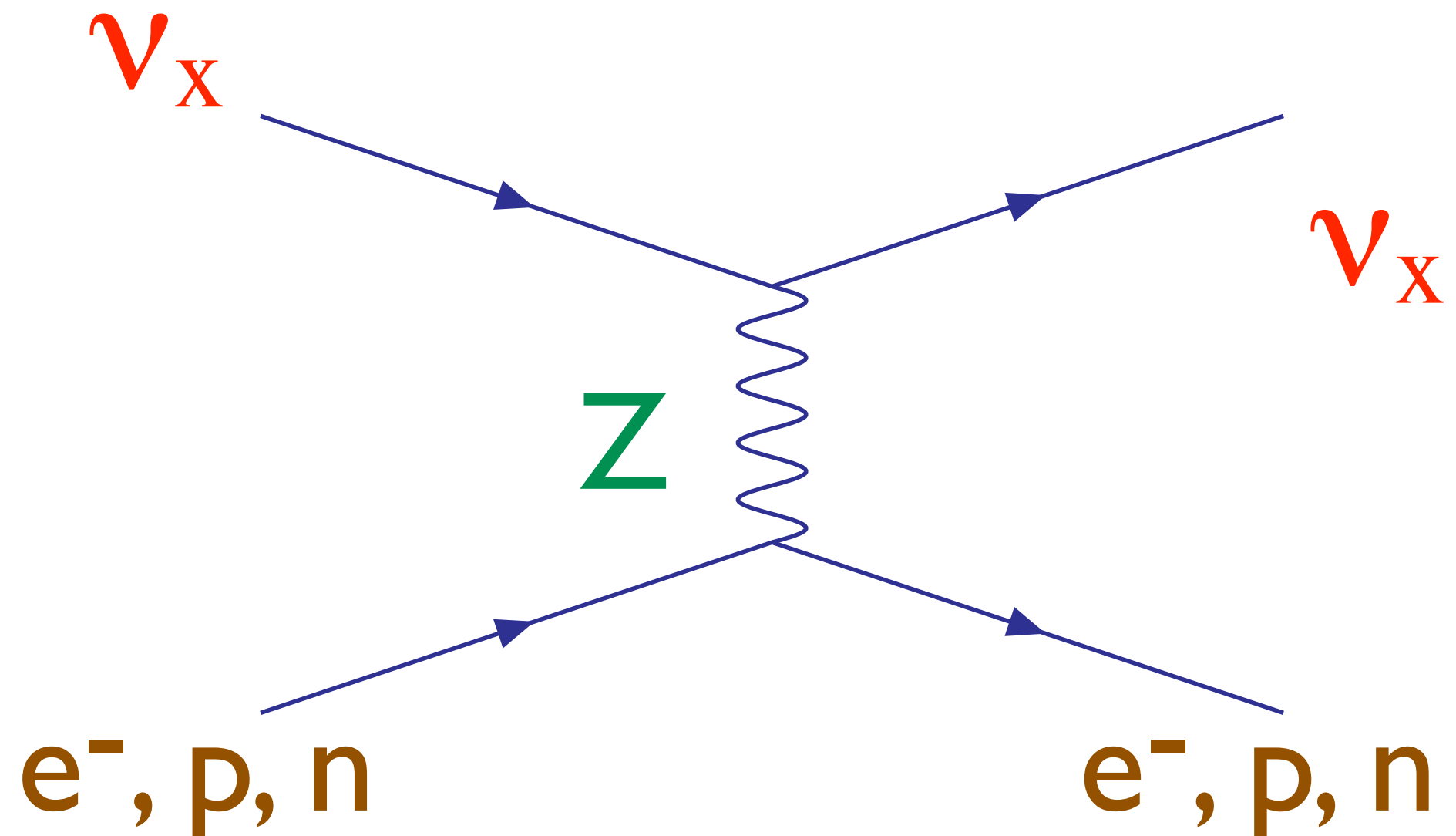
$$\delta_{\text{CP}}$$

Interaction of neutrinos with matter

Charged Current (CC)



Neutral Current (NC)



$$\nu_x = \nu_e, \nu_\mu, \nu_\tau$$

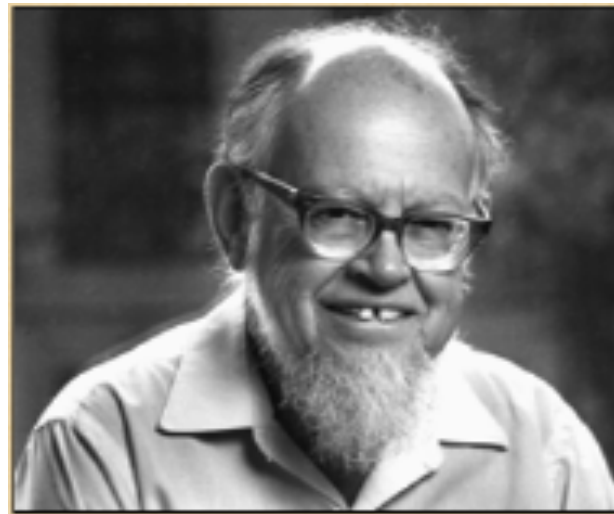
Coherent Effect $\sim O(G_F)$

matter effect modifies the index of refraction for neutrinos
can modify drastically the oscillation probability

analogy: photon gain effective mass in matter

Neutrino Oscillation in Matter

Mikheyev-Smirnov-Wolfenstein (MSW) Effect



L. Wolfenstein

L. Wolfenstein, PRD17 (1978)2369

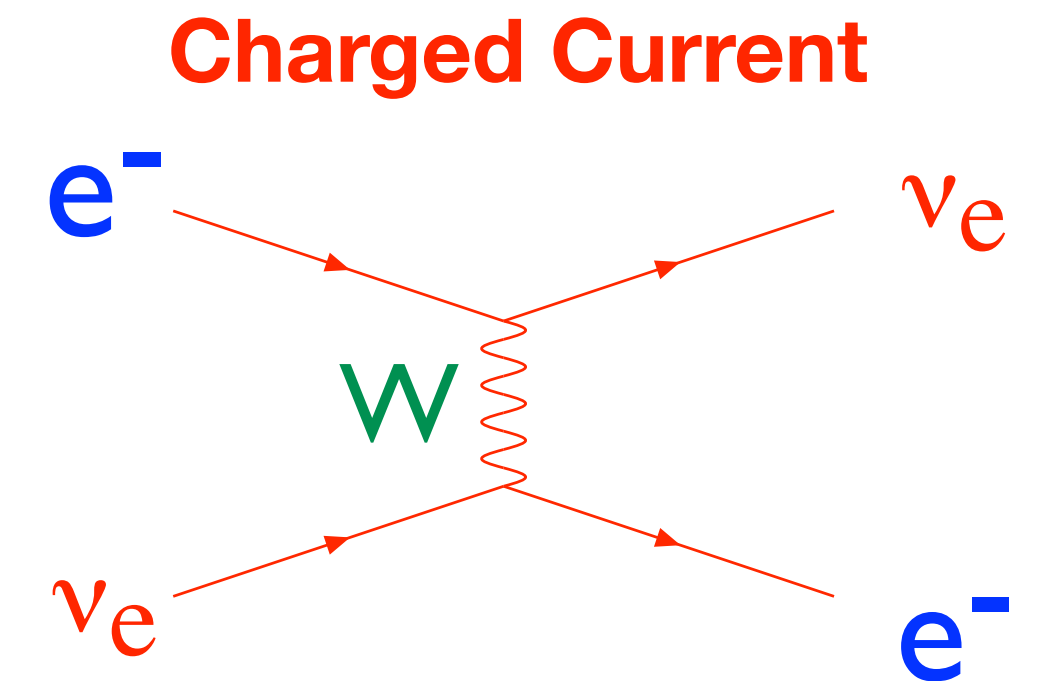


S. P. Mikheyev

S.P.Mikheyev and A. Yu. Smirnov, Sov. J. Nucl. Phys. 42 (1985)913

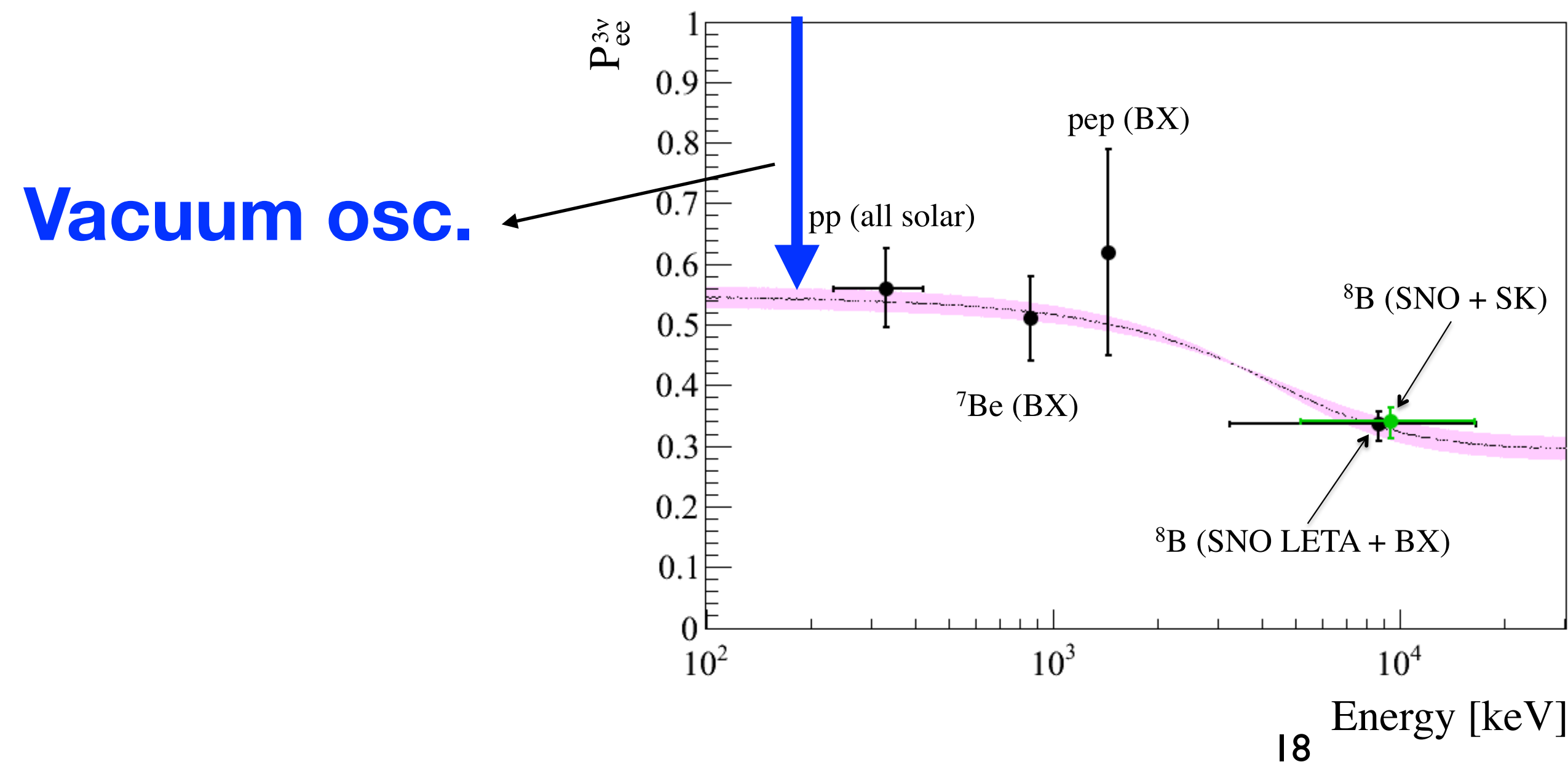


A. Yu. Smirnov



Resonant Enhancement of Neutrino Oscillation in matter

Essential to solve Solar Neutrino Problem



MSW effect (prediction)

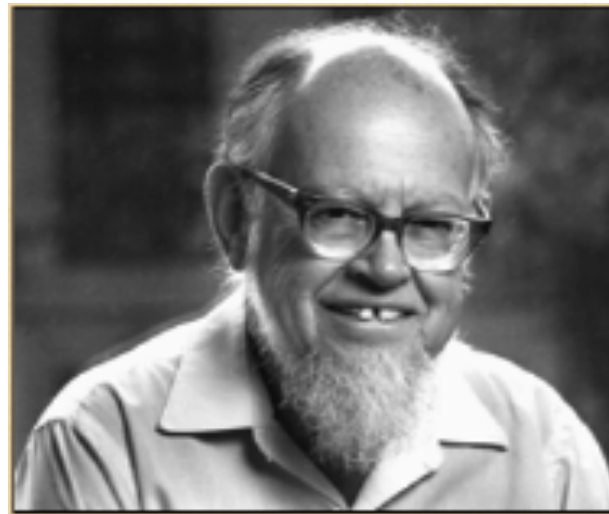
changes index of refraction

ν_e feels extra potential
or gains effective mass

Bellini et al, Borexino, PRD89, 112007 (2014)

Neutrino Oscillation in Matter

Mikheyev-Smirnov-Wolfenstein (MSW) Effect



L. Wolfenstein

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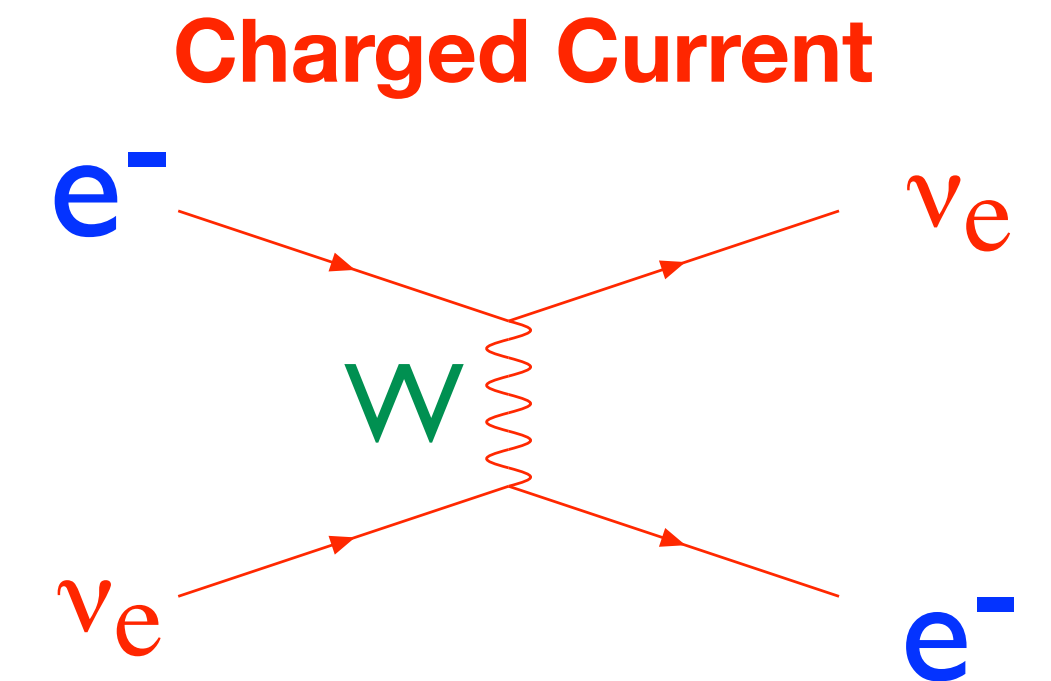


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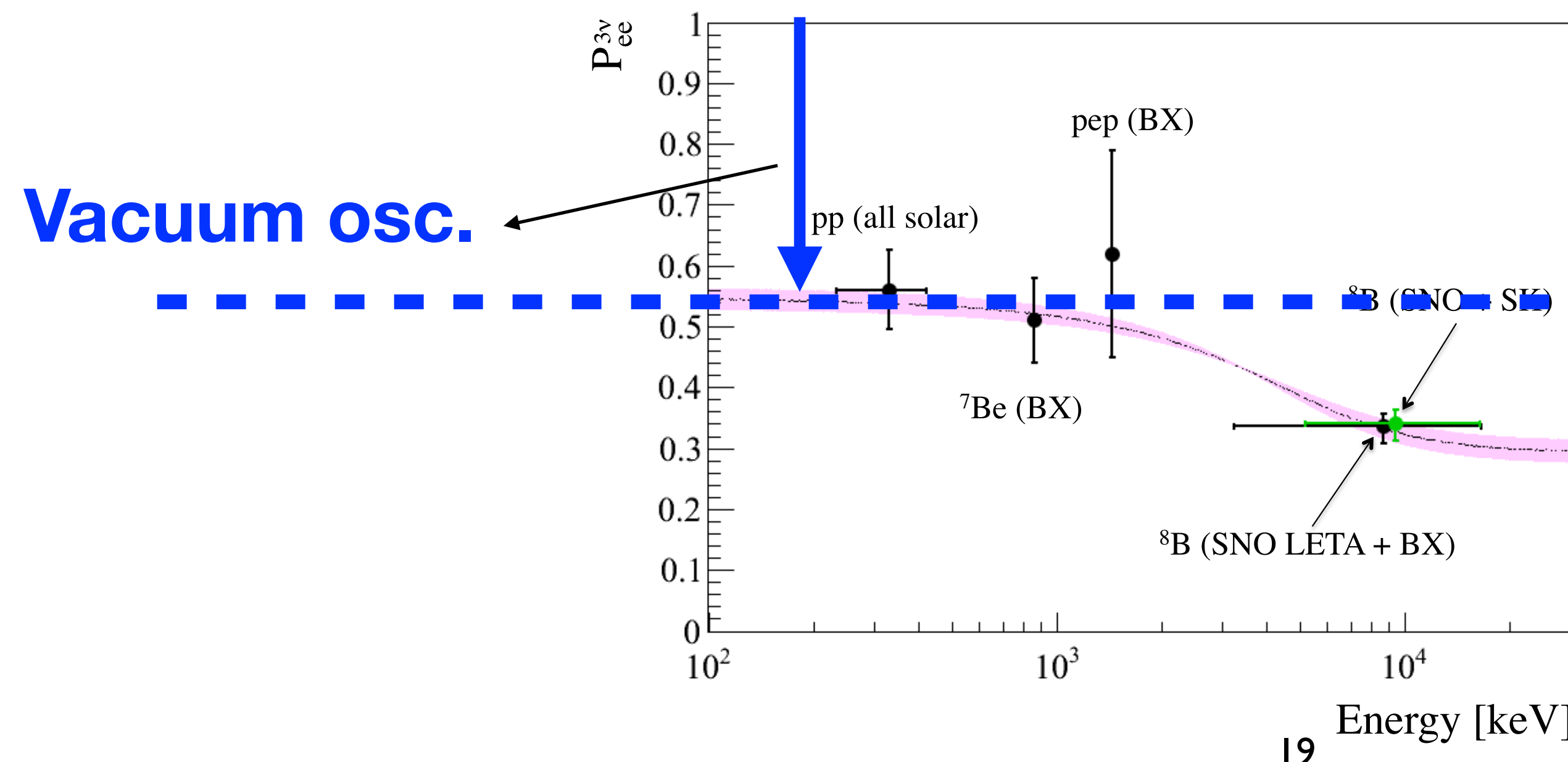


A. Yu. Smirnov



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Neutrino Oscillation Probabilities in Matter

$$P(\alpha \rightarrow \beta) = \left| \sum_j U_{\alpha j}^* U_{\beta j} e^{-i \frac{m_j^2}{2E} L} \right|^2 \quad (\text{Oscillation Probabilities in vacuum})$$

$$= \delta_{\alpha\beta} - 4 \sum_{i>j} \Re[U_{\alpha i}^* U_{\alpha j} U_{\beta i} U_{\beta j}^*] \sin^2 \left(\frac{\Delta m_{ij}^2}{4E} L \right) + 2 \sum_{i>j} \Im[U_{\alpha i}^* U_{\alpha j} U_{\beta i} U_{\beta j}^*] \sin \left(\frac{\Delta m_{ij}^2}{2E} L \right)$$

With constant matter density, we can compute oscillation probabilities in the same way by simply replacing the vacuum mixing matrix elements and mass squared differences to the effective ones in matter,

$$U_{\alpha i} \rightarrow \widetilde{U}_{\alpha i} , \quad \Delta m_{ij}^2 \rightarrow \widetilde{\Delta m_{ij}^2}$$

Neutrino Oscillation Probabilities in Matter

$$P(\alpha \rightarrow \beta) = \left| \sum_j \widetilde{U}_{\alpha j}^* \widetilde{U}_{\beta j} e^{-i \frac{\widetilde{m_j^2}}{2E} L} \right|^2$$

$$= \delta_{\alpha\beta} - 4 \sum_{i>j} \Re[\widetilde{U}_{\alpha i}^* \widetilde{U}_{\alpha j} \widetilde{U}_{\beta i} \widetilde{U}_{\beta j}^*] \sin^2 \left(\frac{\widetilde{\Delta m_{ij}^2}}{4E} L \right) + 2 \sum_{i>j} \Im[\widetilde{U}_{\alpha i}^* \widetilde{U}_{\alpha j} \widetilde{U}_{\beta i} \widetilde{U}_{\beta j}^*] \sin \left(\frac{\widetilde{\Delta m_{ij}^2}}{2E} L \right)$$

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Neutrino Evolution Equation in Matter

$$i \frac{d}{dx} \begin{bmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{bmatrix} = H \begin{bmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{bmatrix}$$

G_F : Fermi Constant

N_e : Electron number density

$$H = U \begin{bmatrix} 0 & 0 & 0 \\ 0 & \frac{\Delta m_{21}^2}{2E} & 0 \\ 0 & 0 & \frac{\Delta m_{31}^2}{2E} \end{bmatrix} U^\dagger + \begin{bmatrix} \sqrt{2} G_F N_e & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

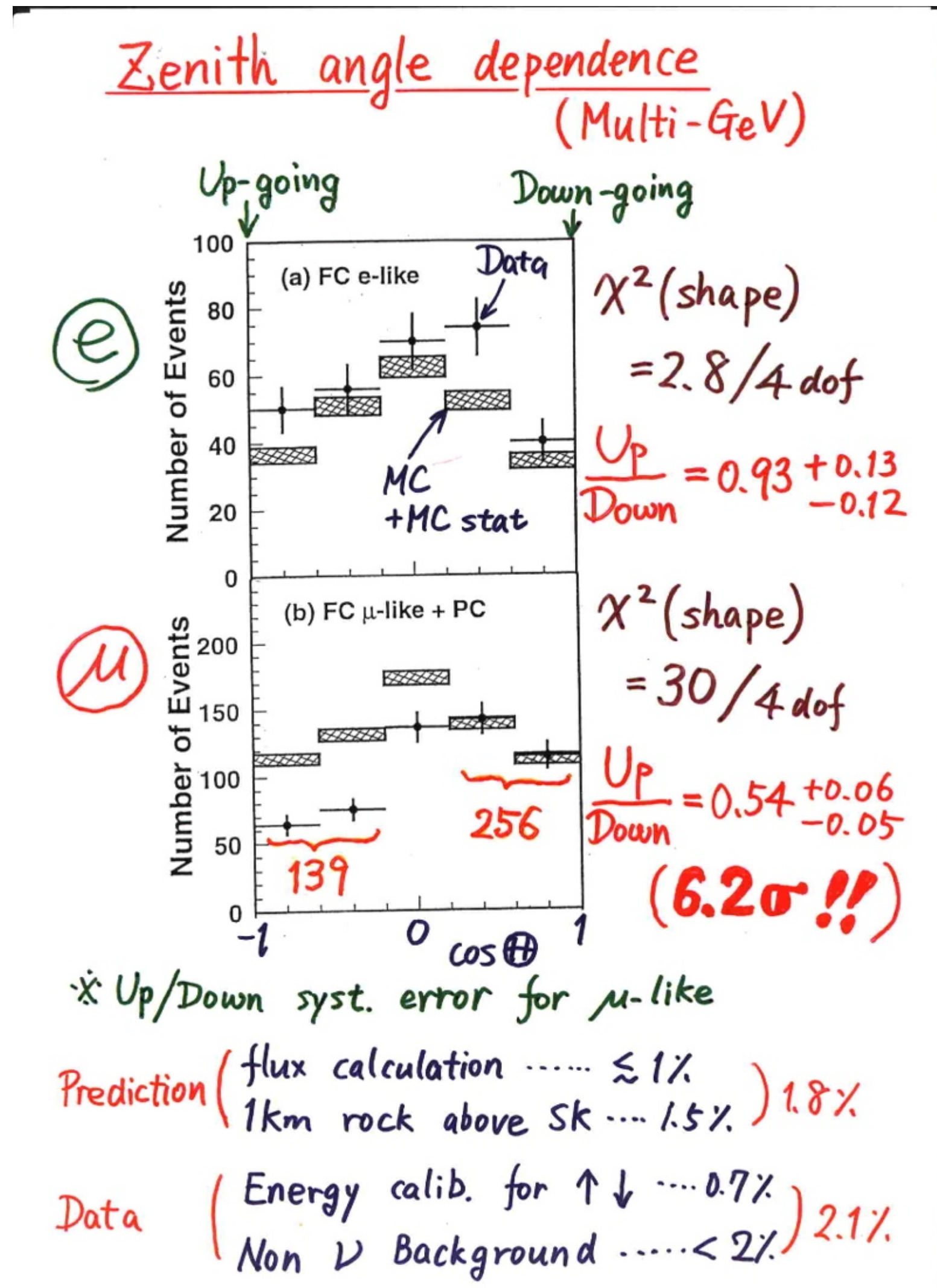
In general, for varying matter (electron) density profile, one needs to solve numerically the evolution equation, or diagonalize the Hamiltonian at each position, to compute the final oscillation probability

Discovery of Neutrino Oscillations

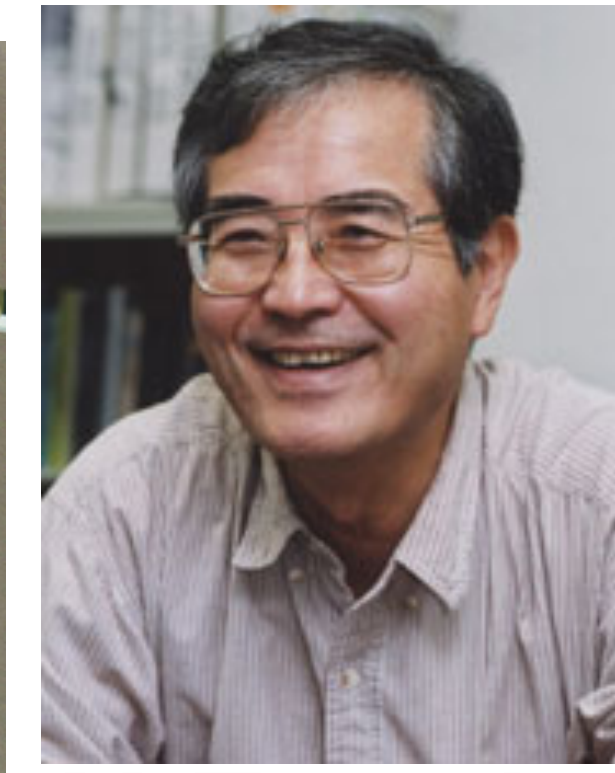
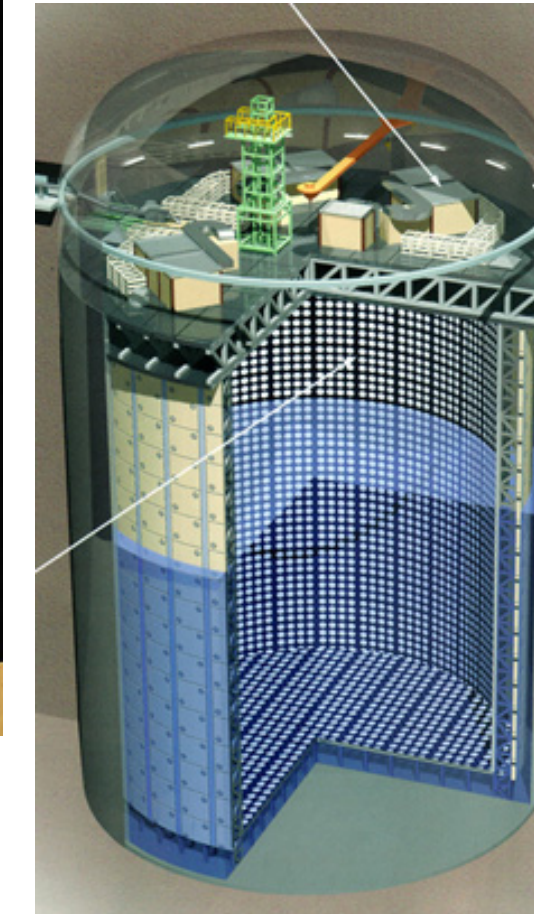
from experimental point of view

Discovery of **Neutrino Oscillation** in 1998

Announced in “Neutrino '98” @Takayama, Japan



T. Kajita



Y. Totsuka
(1942-2008)



Super-Kamiokande
Collaboration

ν_μ



ν_τ

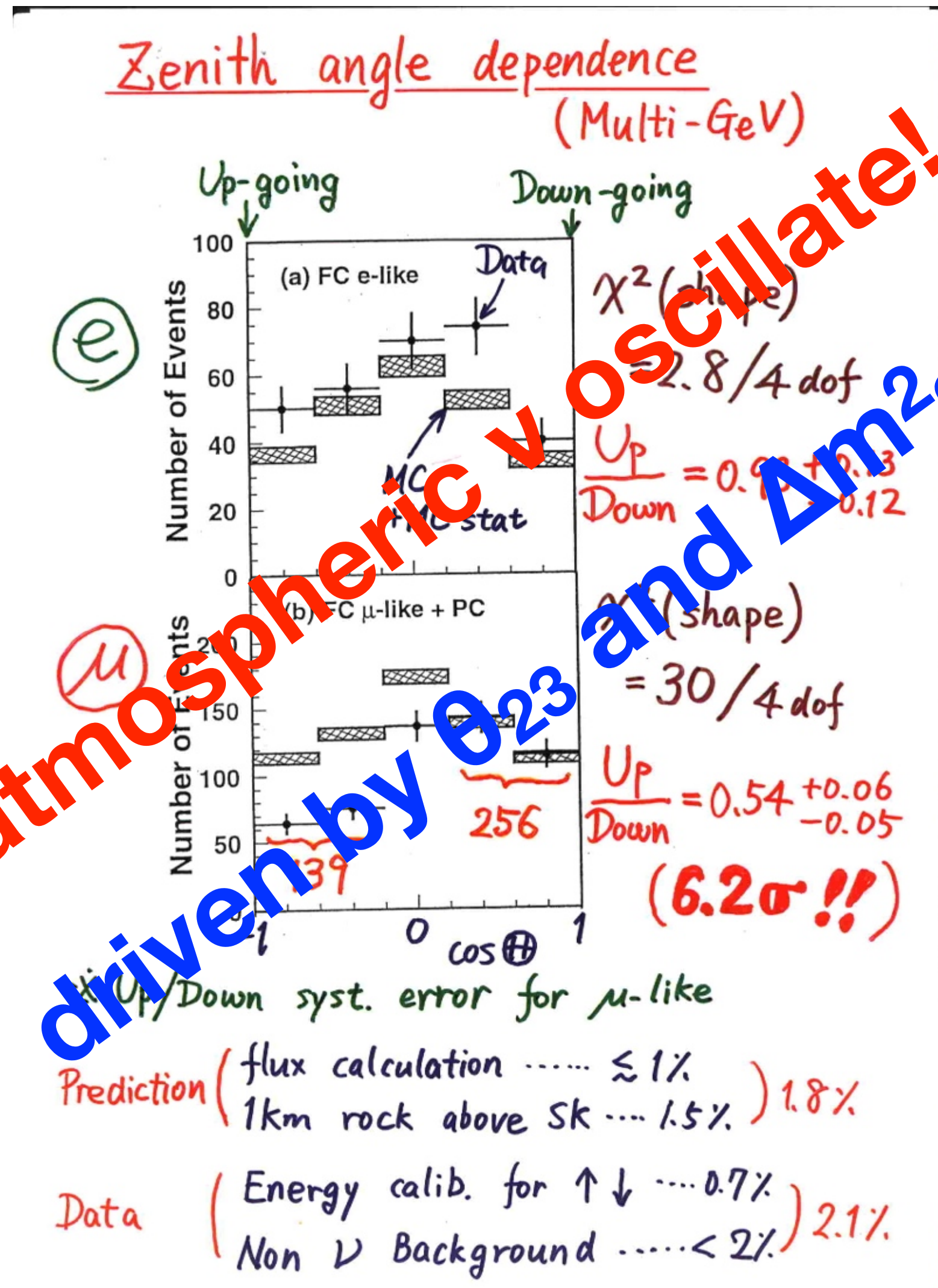
neutrinos change flavors !

$\rightarrow m_\nu \neq 0$

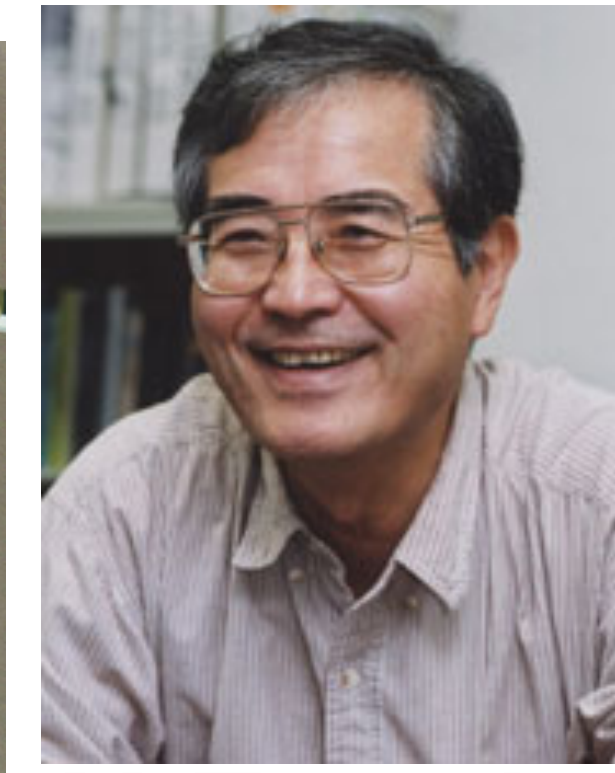
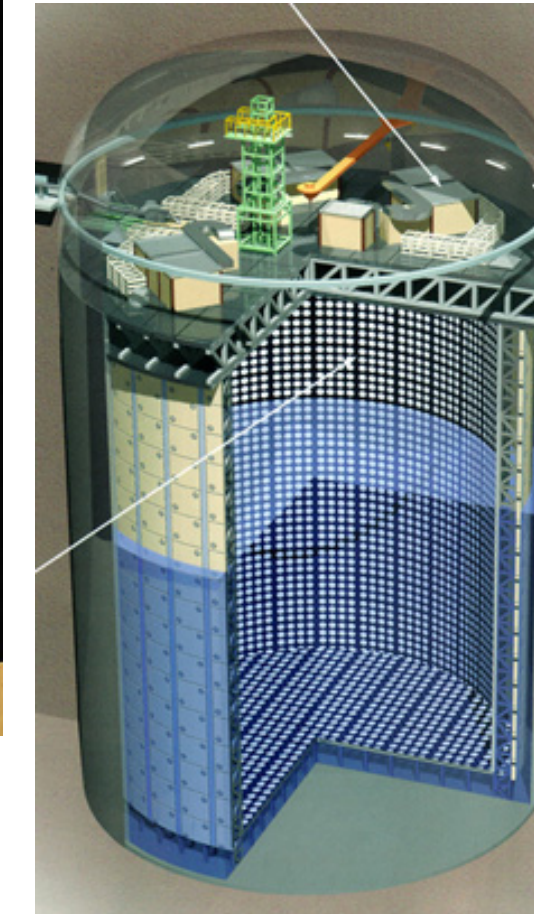
$$P(\nu_\mu \rightarrow \nu_\mu) \sim 1 - \sin^2 2\theta_{23} \sin^2 \left(\frac{\Delta m_{32}^2 L}{4E} \right)$$

Discovery of Neutrino Oscillation in 1998

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Super-Kamiokande
Collaboration



ν_μ



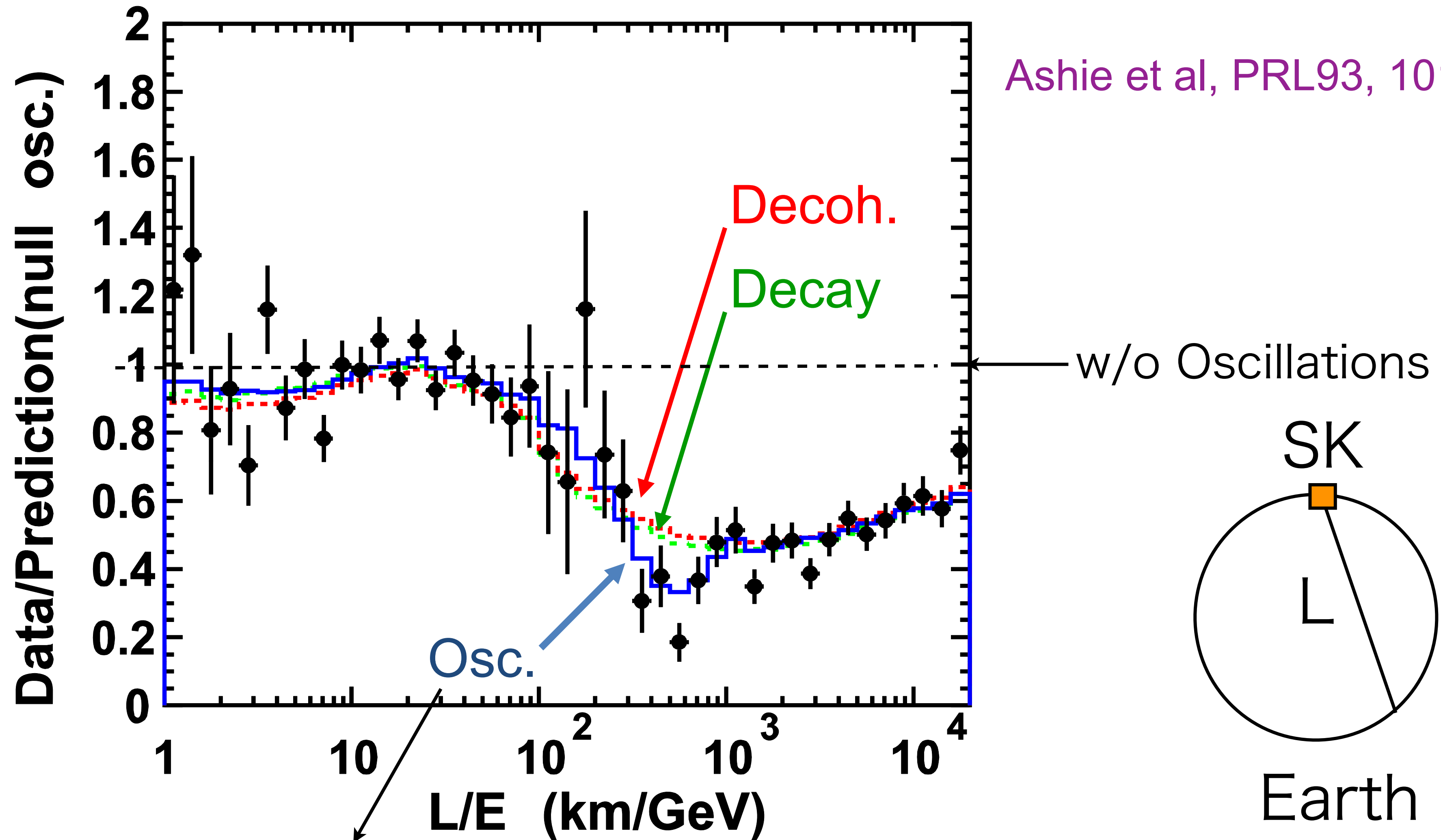
ν_τ

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$$P(\nu_\mu \rightarrow \nu_\mu) \sim 1 - \sin^2 2\theta_{23} \sin^2 \left(\frac{\Delta m_{32}^2 L}{4E} \right)$$

L/E distribution of Super-Kamiokande Atmospheric Neutrinos



$$P(\nu_\mu \rightarrow \nu_\mu) = \sin^2 2\theta \sin \left(\frac{\Delta m^2}{4E} L \right)$$

Solar neutrinos also oscillate!

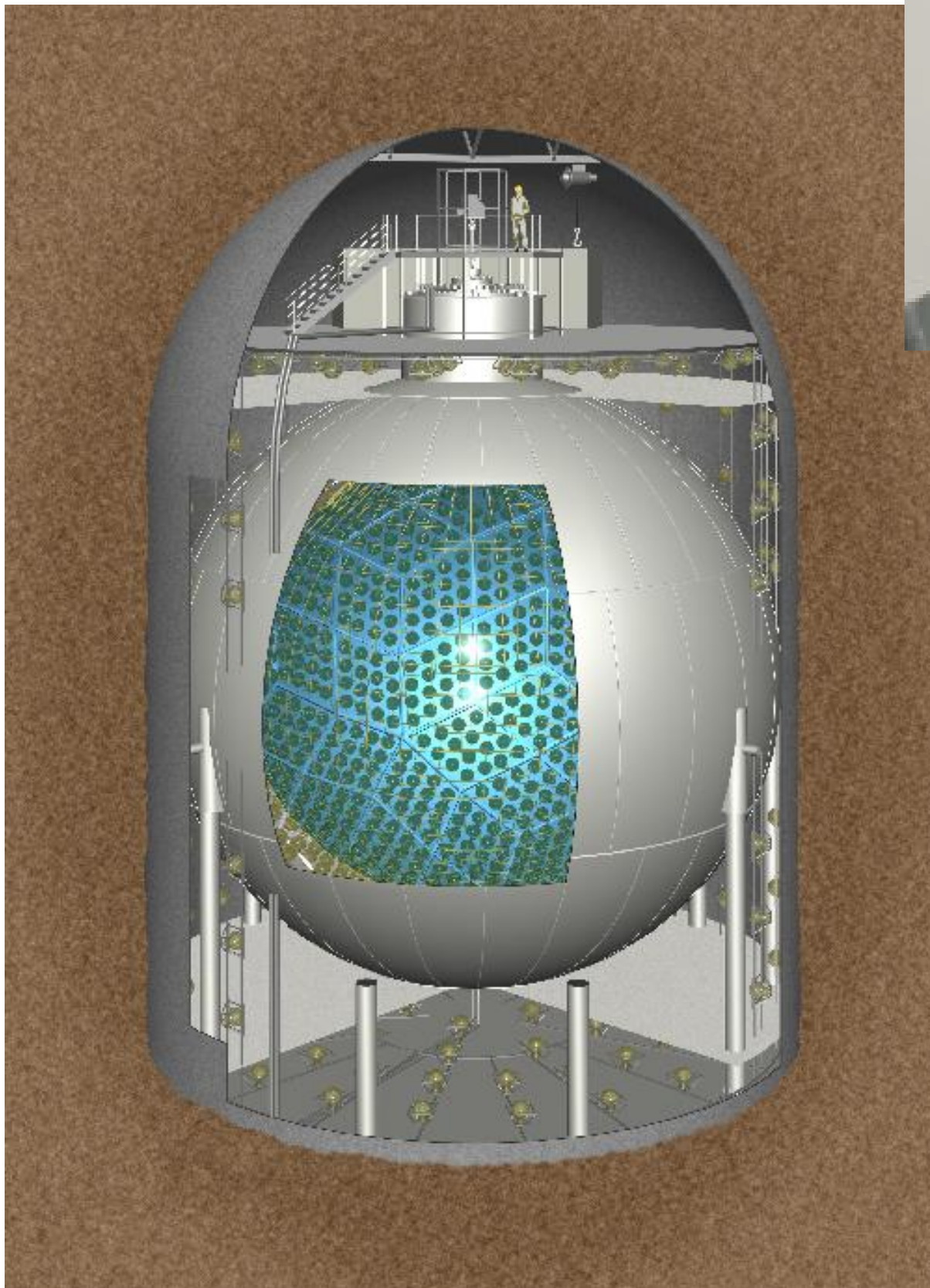
A. McDonald



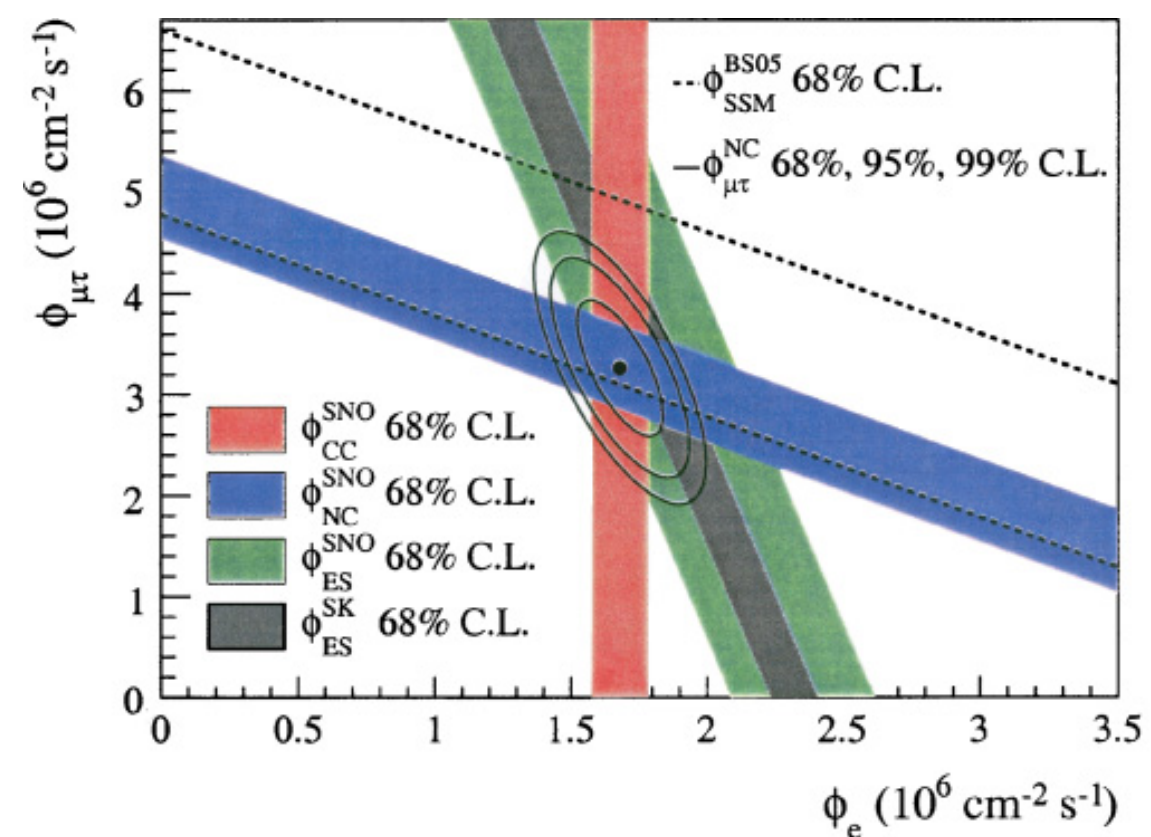
ν_e

$\nu_{\mu, \tau}$

A. Suzuki



$$P(\nu_e \rightarrow \nu_e) \sim \sin^2 \theta_{12}$$



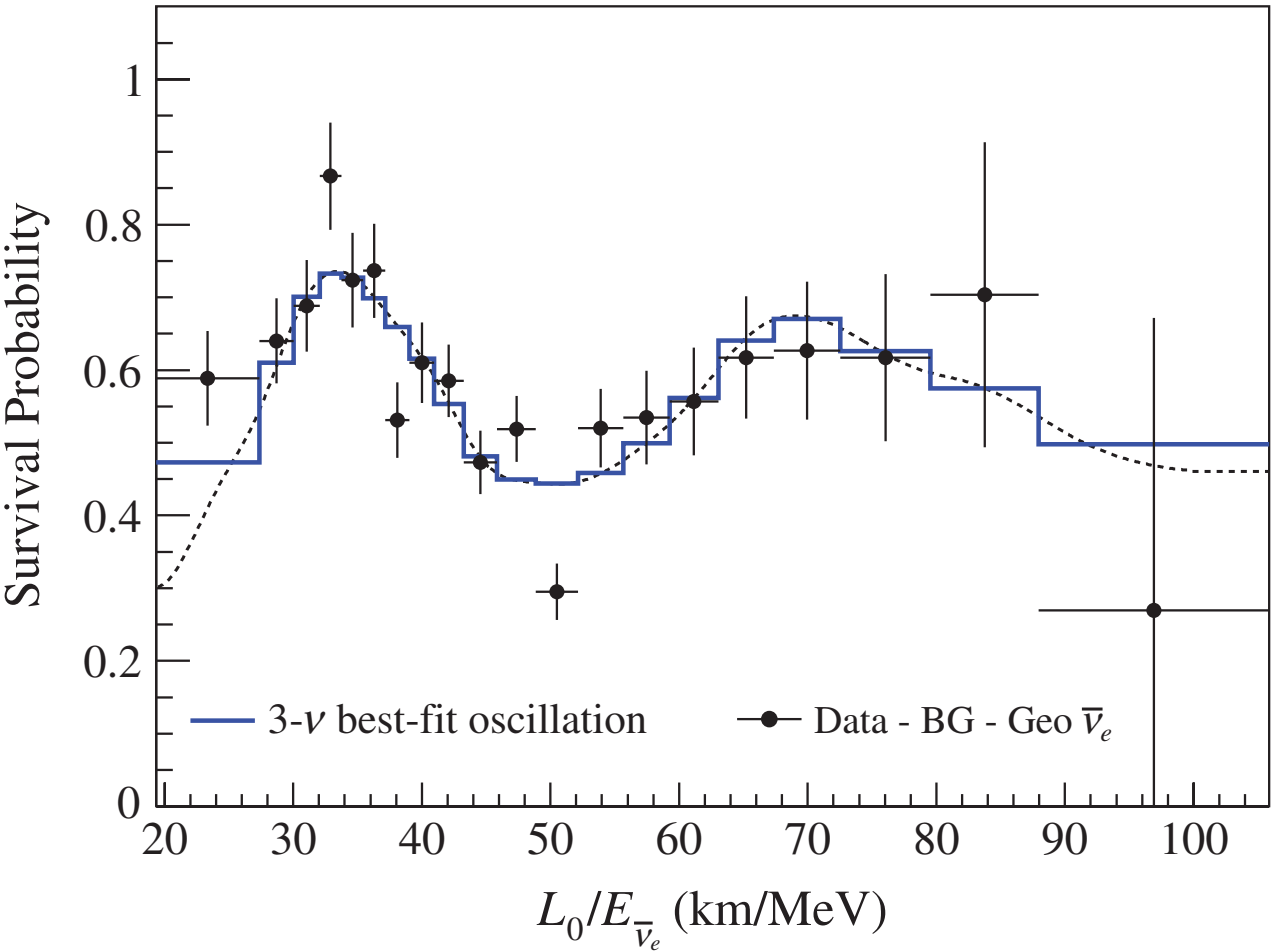
Aharmim et al, PRC72, 055502 (2005)

SNO
solar ν

2002

KamLAND
reactor ν

Gando et al, PRD88, 033001 (2013)



$$P(\bar{\nu}_e \rightarrow \bar{\nu}_e) \sim 1 - \sin^2 2\theta_{12} \sin^2 \left(\frac{\Delta m_{21}^2 L}{4E} \right)$$

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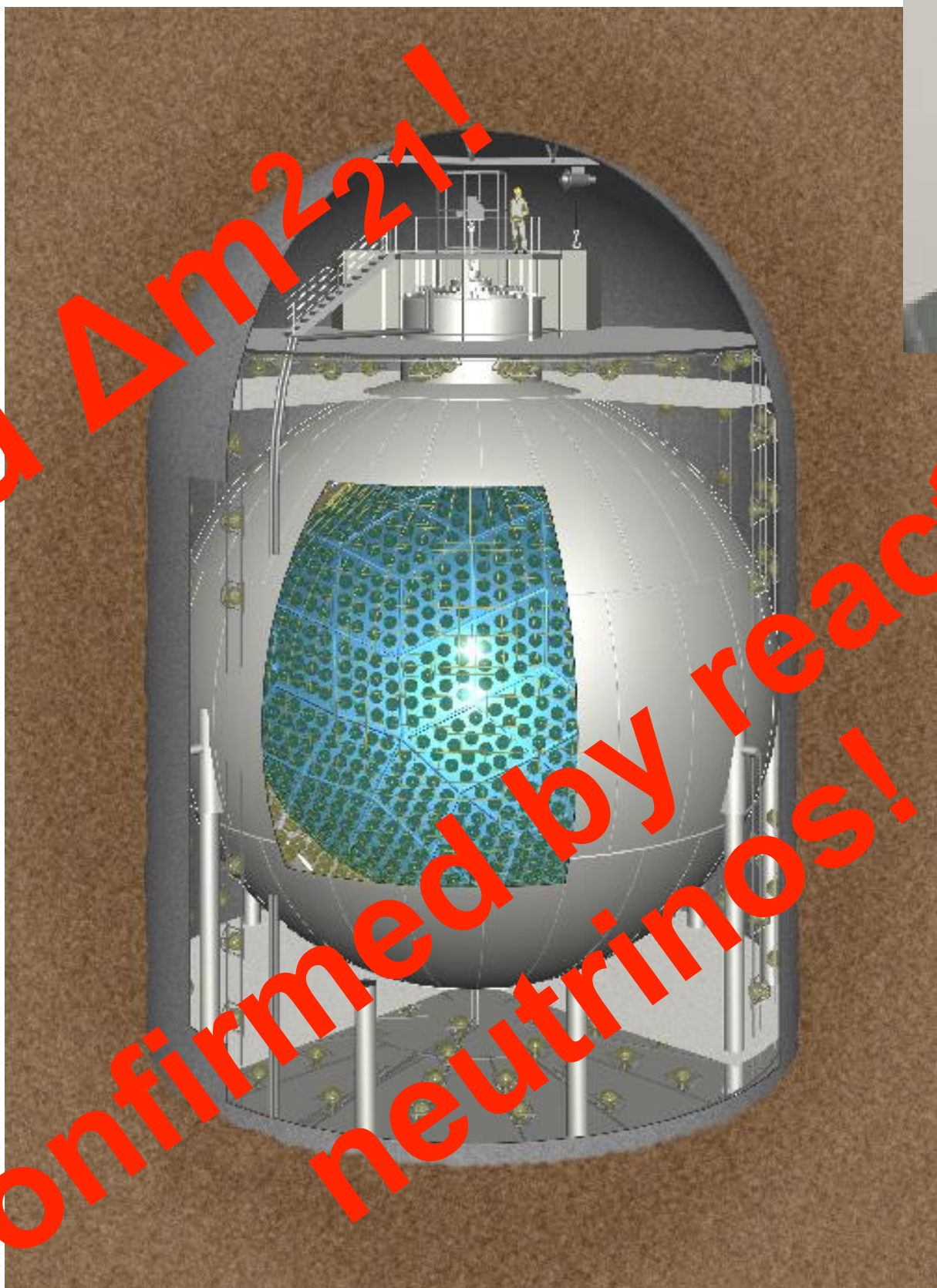
A. McDonald



ν_e

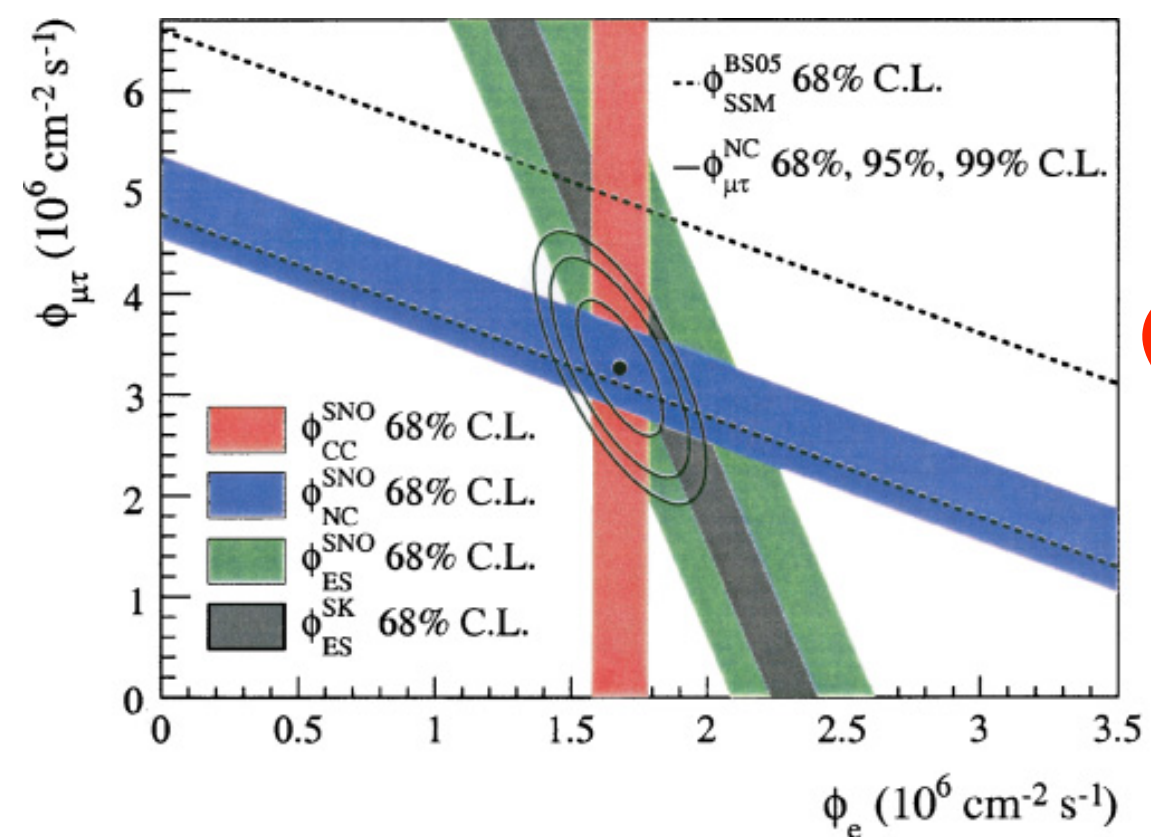
$\nu_{\mu,\tau}$

A. Suzuki



driven by θ_{12} and Δm_{21}^2 !
confirmed by reactor neutrinos!

$$P(\nu_e \rightarrow \nu_e) \sim \sin^2 \theta_{12}$$



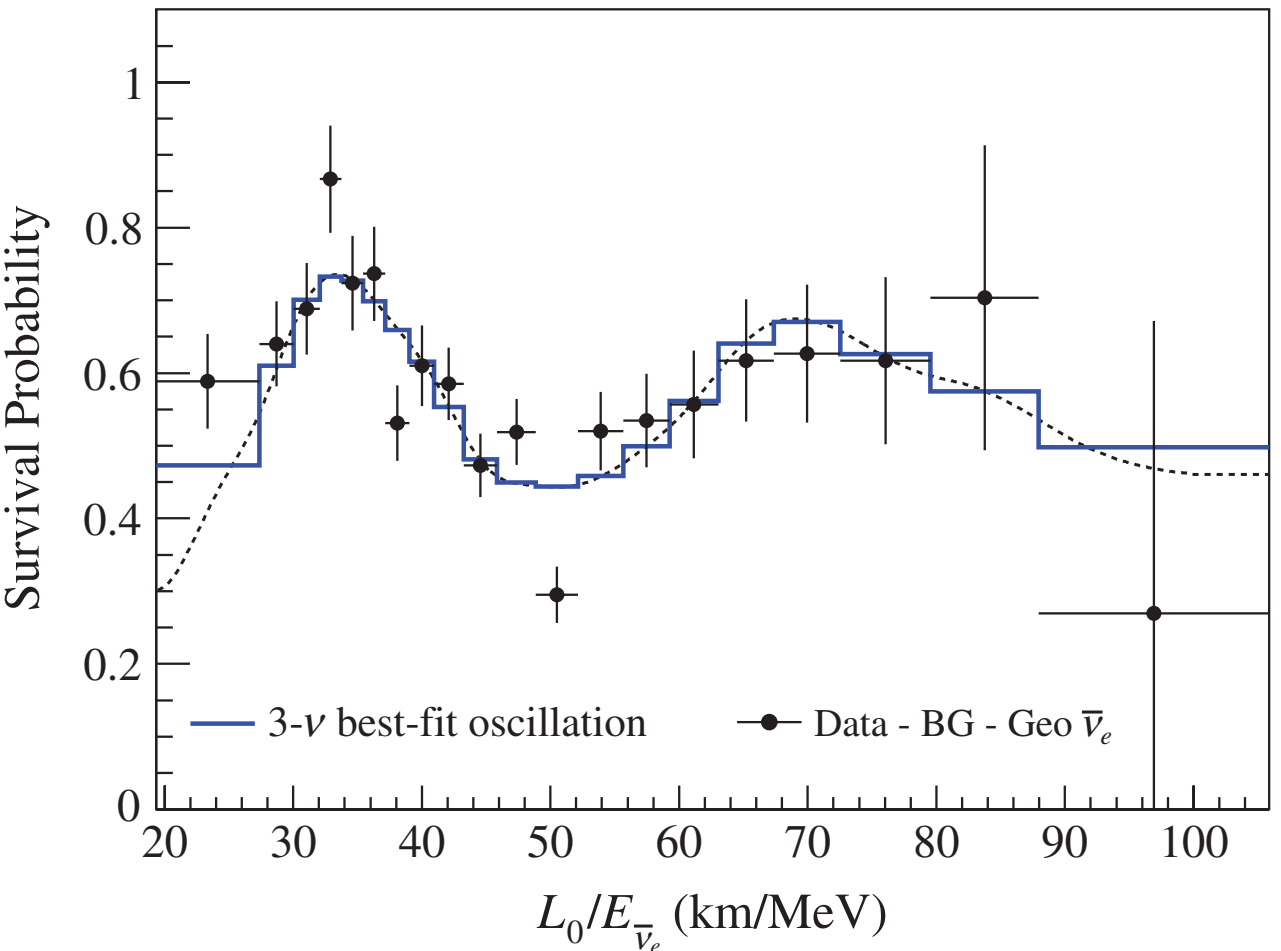
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SNO
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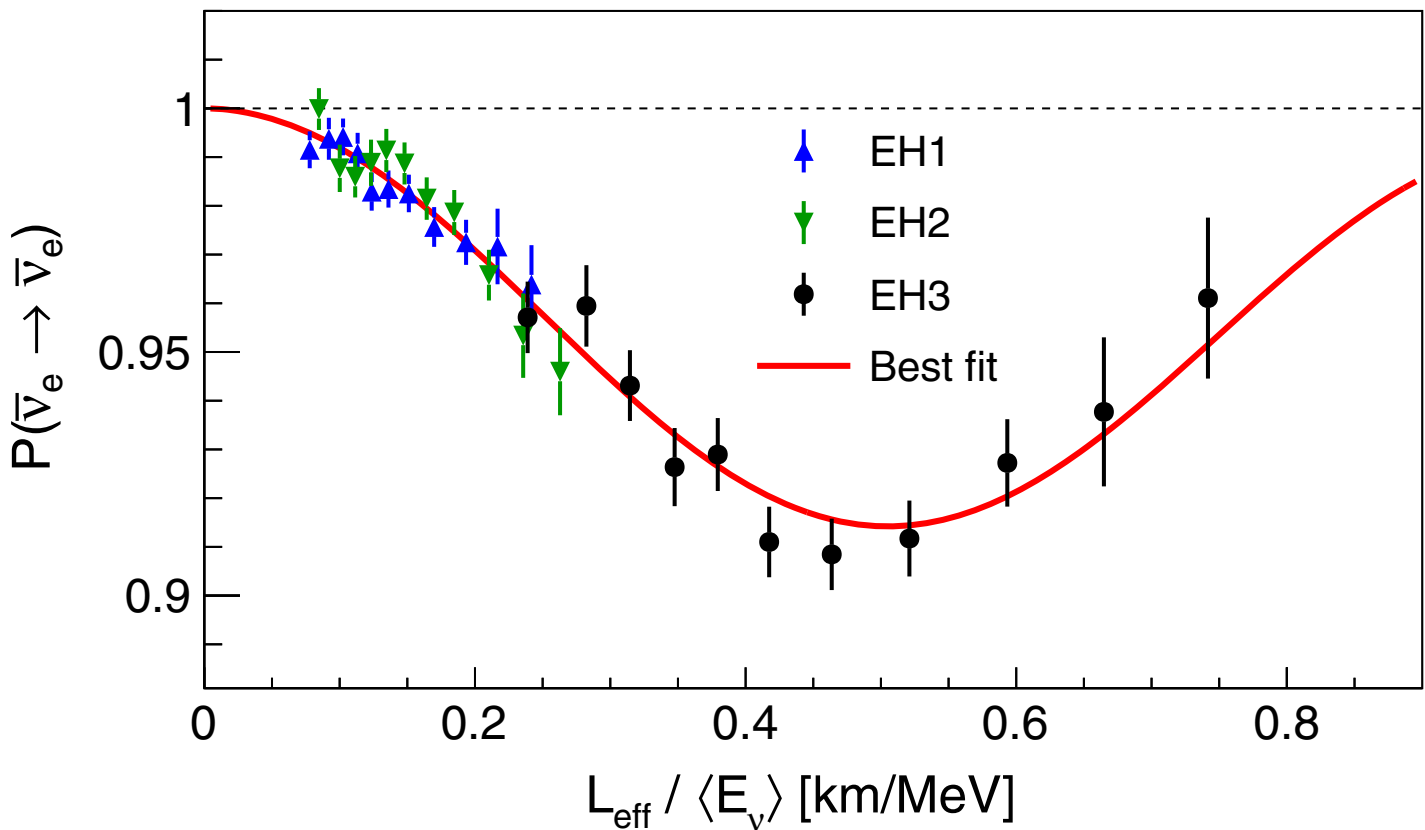
Gando et al, PRD88, 033001 (2013)



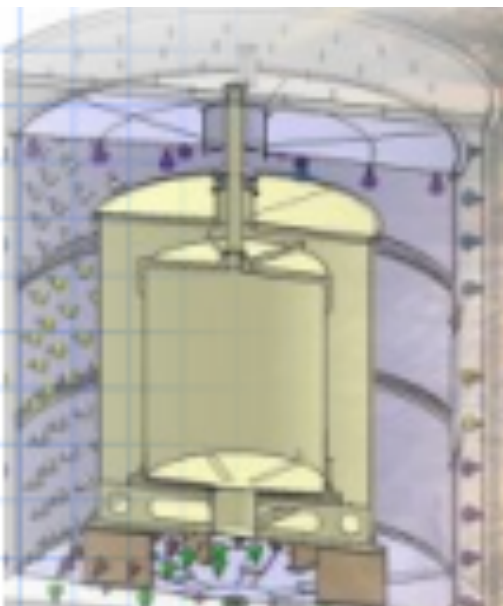
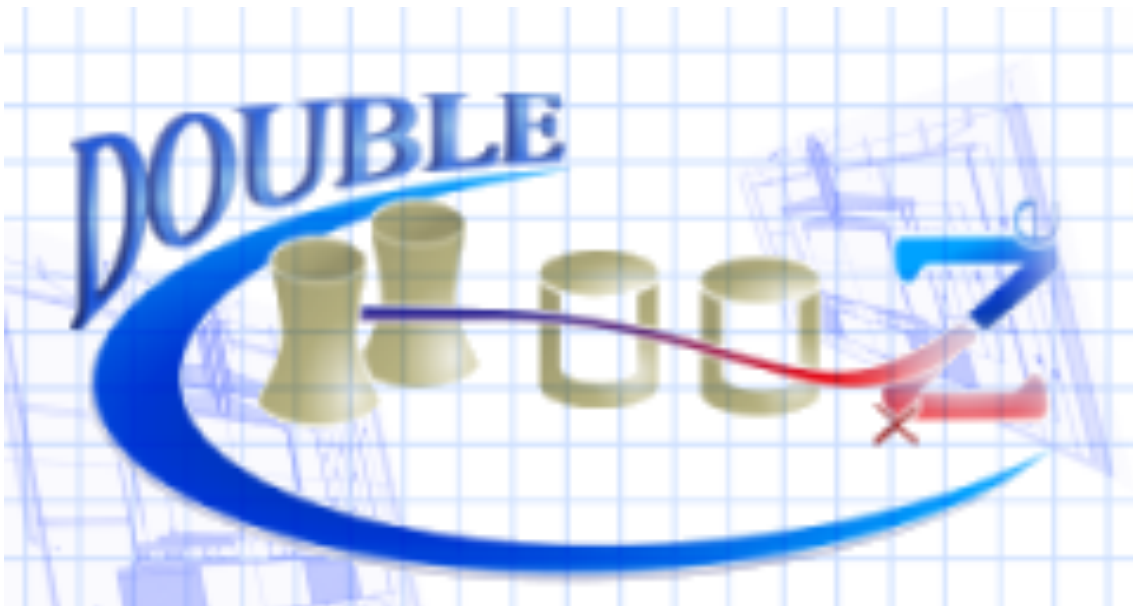
$$P(\bar{\nu}_e \rightarrow \bar{\nu}_e) \sim 1 - \sin^2 2\theta_{12} \sin^2 \left(\frac{\Delta m_{21}^2 L}{4E} \right)$$

Another oscillation channel observed by reactor experiments

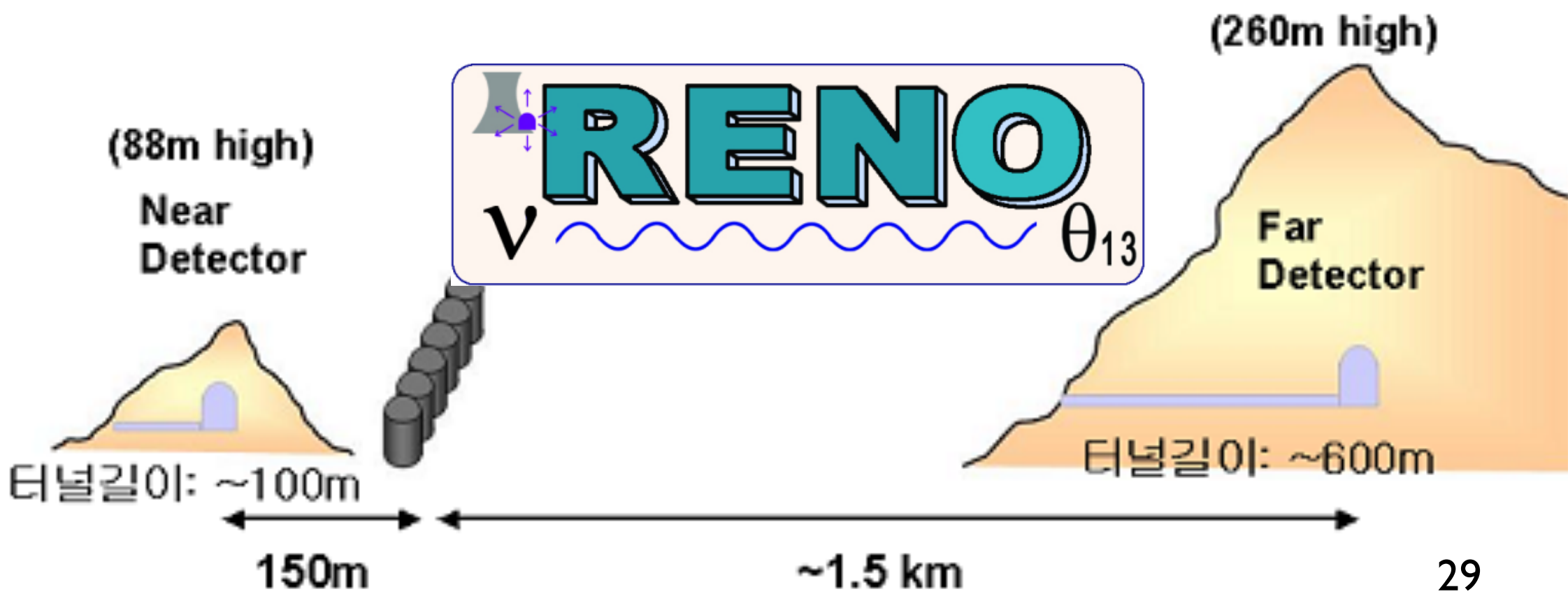
2011-2012 $P(\bar{\nu}_e \rightarrow \bar{\nu}_e) \sim 1 - \sin^2 2\theta_{13} \sin^2 \left(\frac{\Delta m_{31}^2 L}{4E} \right)$



An et al, PRL108, 171803 (2012)



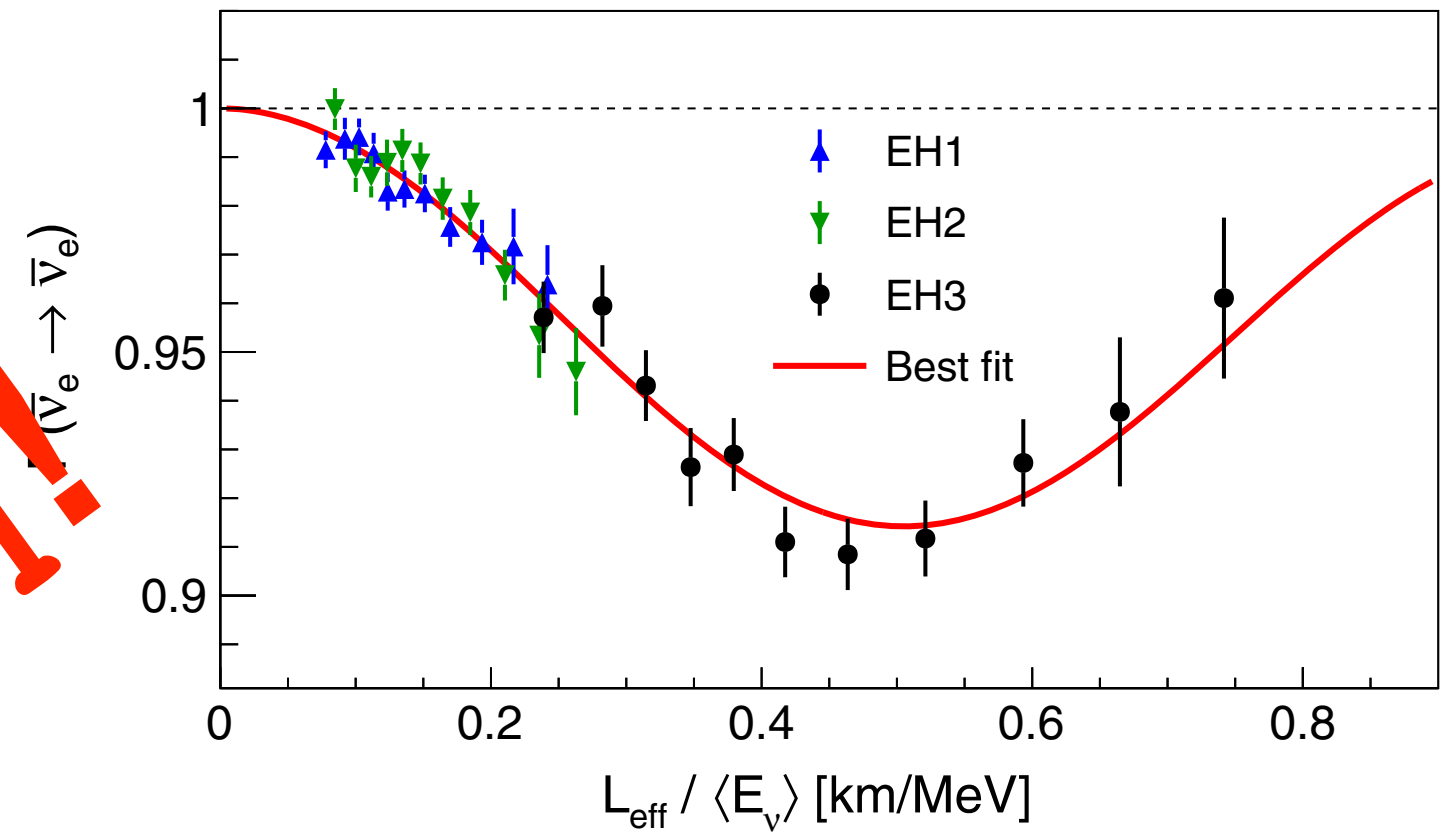
Abe et al, PRL108, 131801 (2012)



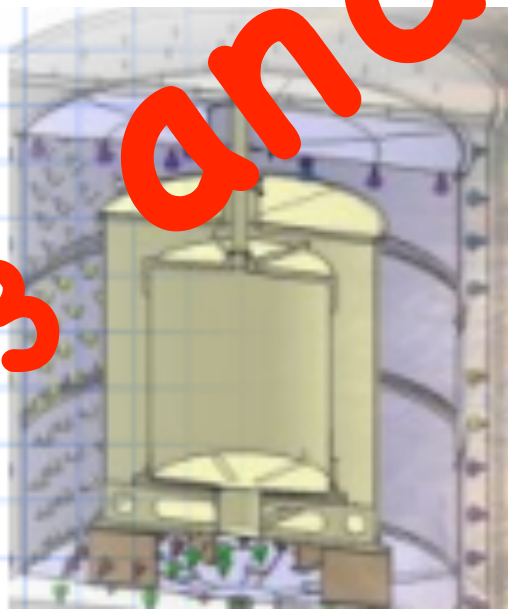
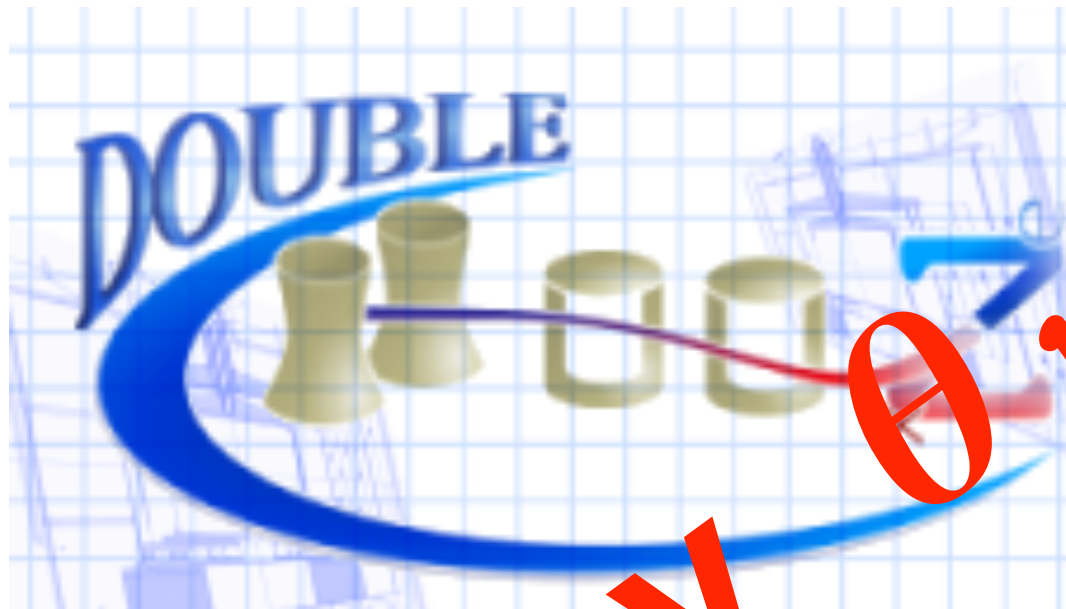
Ahn et al, PRL108, 191802 (2012)

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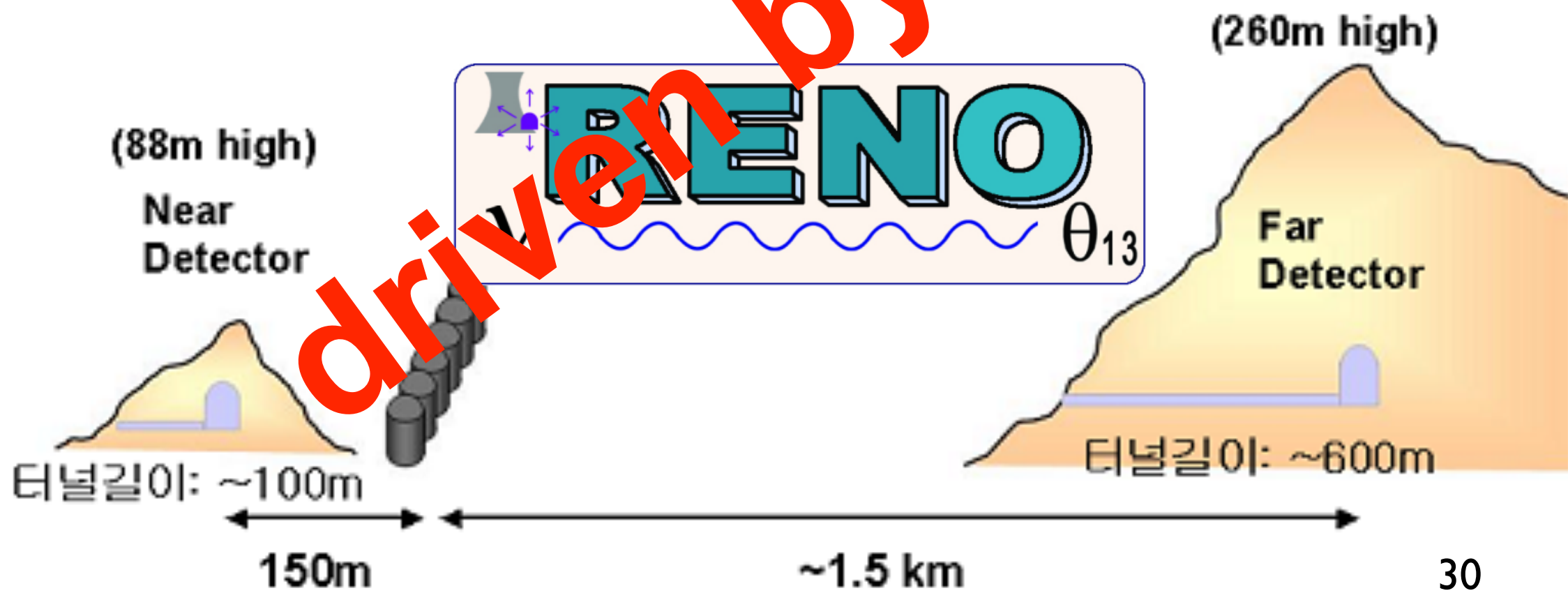


An et al, PRL108, 171803 (2012)



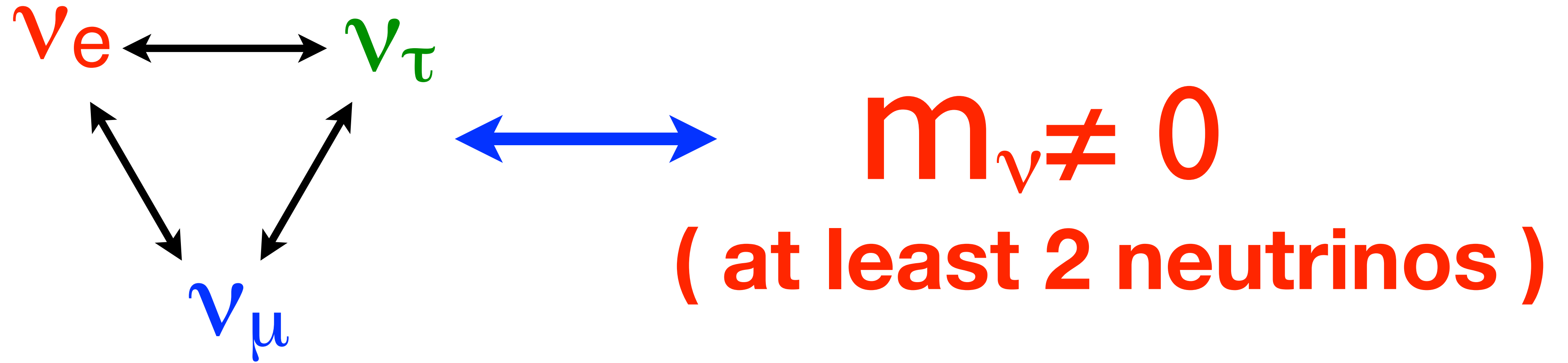
Δm_{31}^2

Abe et al, PRL108, 131801 (2012)



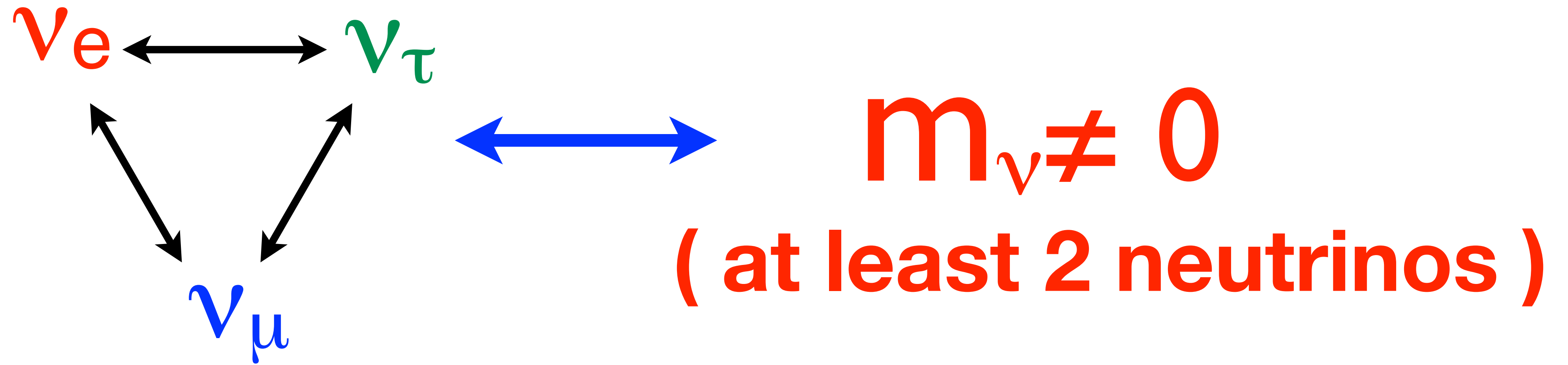
Ahn et al, PRL108, 191802 (2012)

Neutrinos do Oscillate!



So What?

Neutrinos do Oscillate!



So What?

- Strong evidence of physics beyond the Standard Model
- It is likely that by studying phenomena related to tiny neutrino masses, we are probing some higher energy scales beyond SM, e.g., GUT scale, like the scenario suggested in the Seesaw Mechanism

Current Status and Open Questions

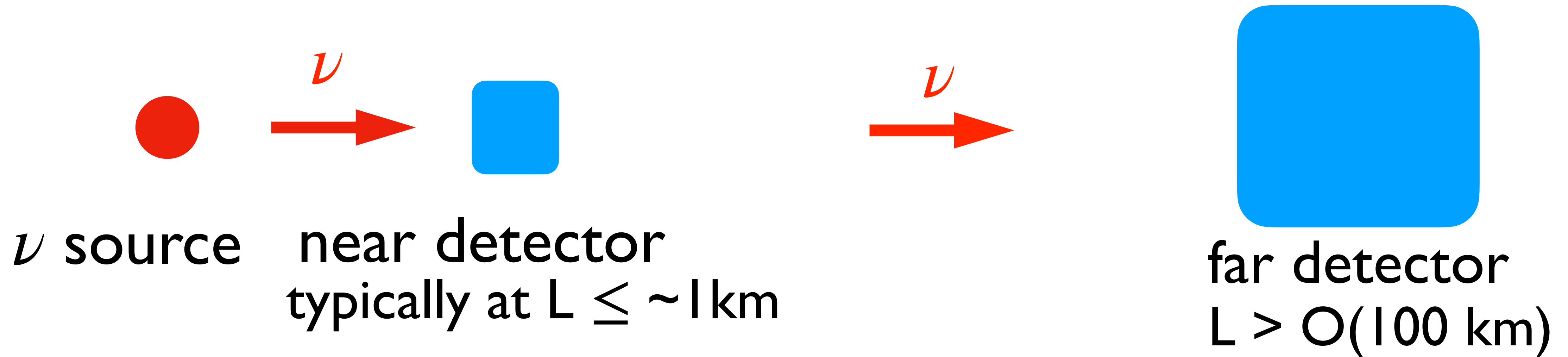
(in the context of LBL oscillation experiments)

Past and currently running “Long Baseline” ν oscillation experiments

- K2K (KEK to Kamioka) : Japan, 1999-2004, Baseline = 250km**
- MINOS (Main Injector Neutrino Oscillation Search): USA, 2005-2016, Baseline = 735 km**
- OPERA (Oscillation Project with Emulsion-tRacking Apparatus): CERN to Gran Sasso Laboratory, 2008-2012, Baseline = 730 km**
- T2K (Tokai to Kamioka): Japan, 2009-present, Baseline = 295 km**
- NOvA (NuMI Off-Axis ν_e Appearance, USA): 2014-present, Baseline = 810 km**

So far, all of them showed results consistent with neutrino oscillation within the standard 3 flavor scheme, no strong disagreement among these experiments

Setup of Near-Far Detectors in LBL experiments



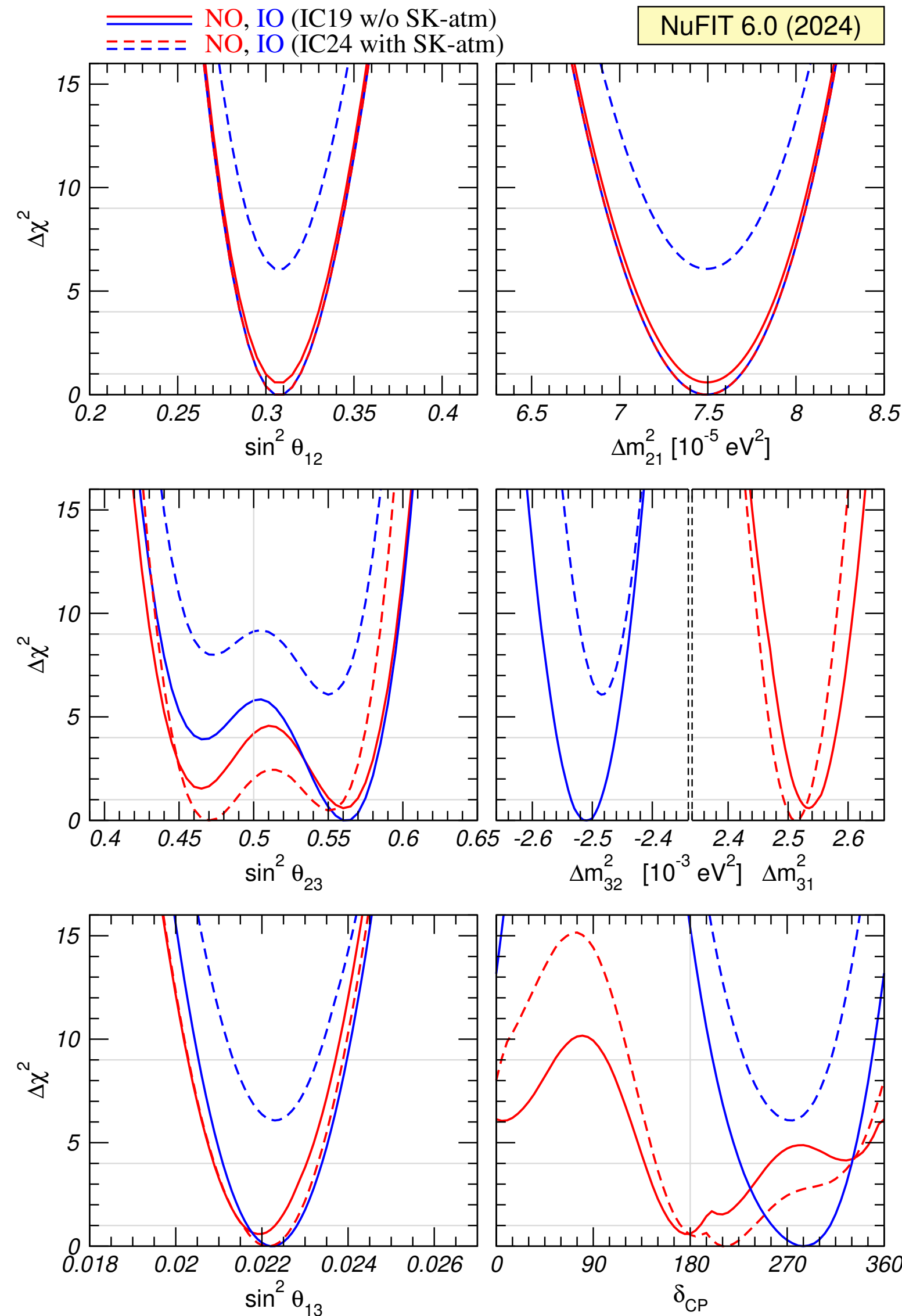
In LBL oscillation experiments, near detector (ND) is mandatory, or essential to predict “unoscillated” neutrino spectra at the far detector (FD), cancelling various systematic uncertainties

This near-far comparison allows us to perform precise analysis/study of oscillation (or effect of any new physics)

Therefore, in general, a LBL oscillation experiment comes with a “short baseline (\sim km)” experiment with its near detector, by which one can study also some physics (including some BSM physics) related to neutrinos

I will focus mainly the oscillation related phenomena which can be studied by “near-far” comparison

Current allowed range of mixing parameters from Global Fit



Based on ν data coming from solar, atmospheric, reactor, accelerator ν experiments (no strong evidence of more than 3 flavors, except for some hints/indications)

1 σ uncertainties of 6 mixing parameters

$\sin^2 \theta_{ij}$ ($ij = 12, 23, 23$) : $\sim 3 - 4 \%$

Δm_{21}^2 : $\sim 3 \%$

$$\Delta m_{ij}^2 \equiv m_i^2 - m_j^2$$

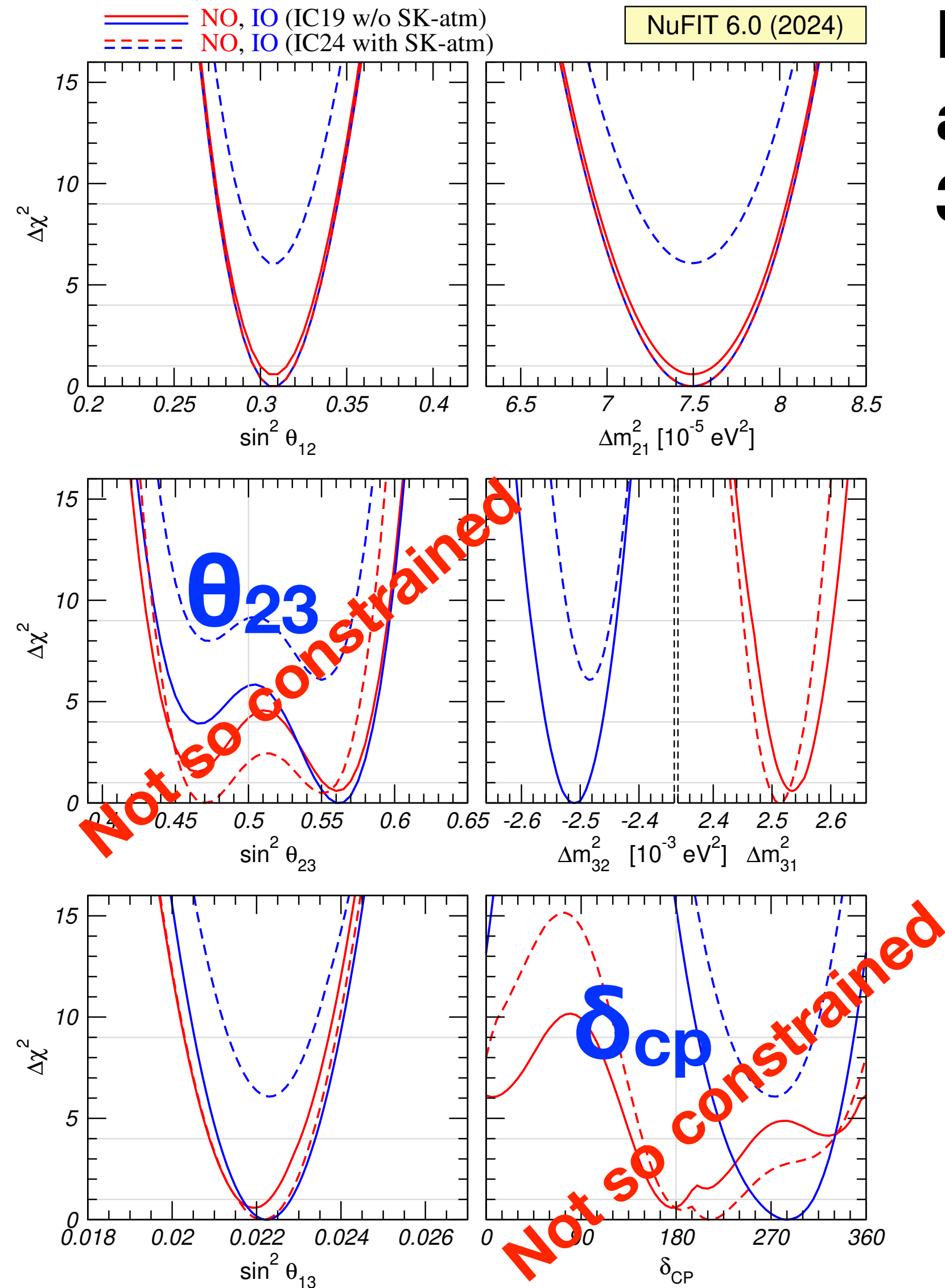
$|\Delta m_{31}^2| \simeq |\Delta m_{32}^2|$: $\sim 1\%$

δ_{CP} : $\sim 30^\circ$ (central value not so stable)

normal mass ordering ($\Delta m_{31}^2 > 0$) is favored at $\sim 2\sigma$

See Mriam Tortola's talk for any details!

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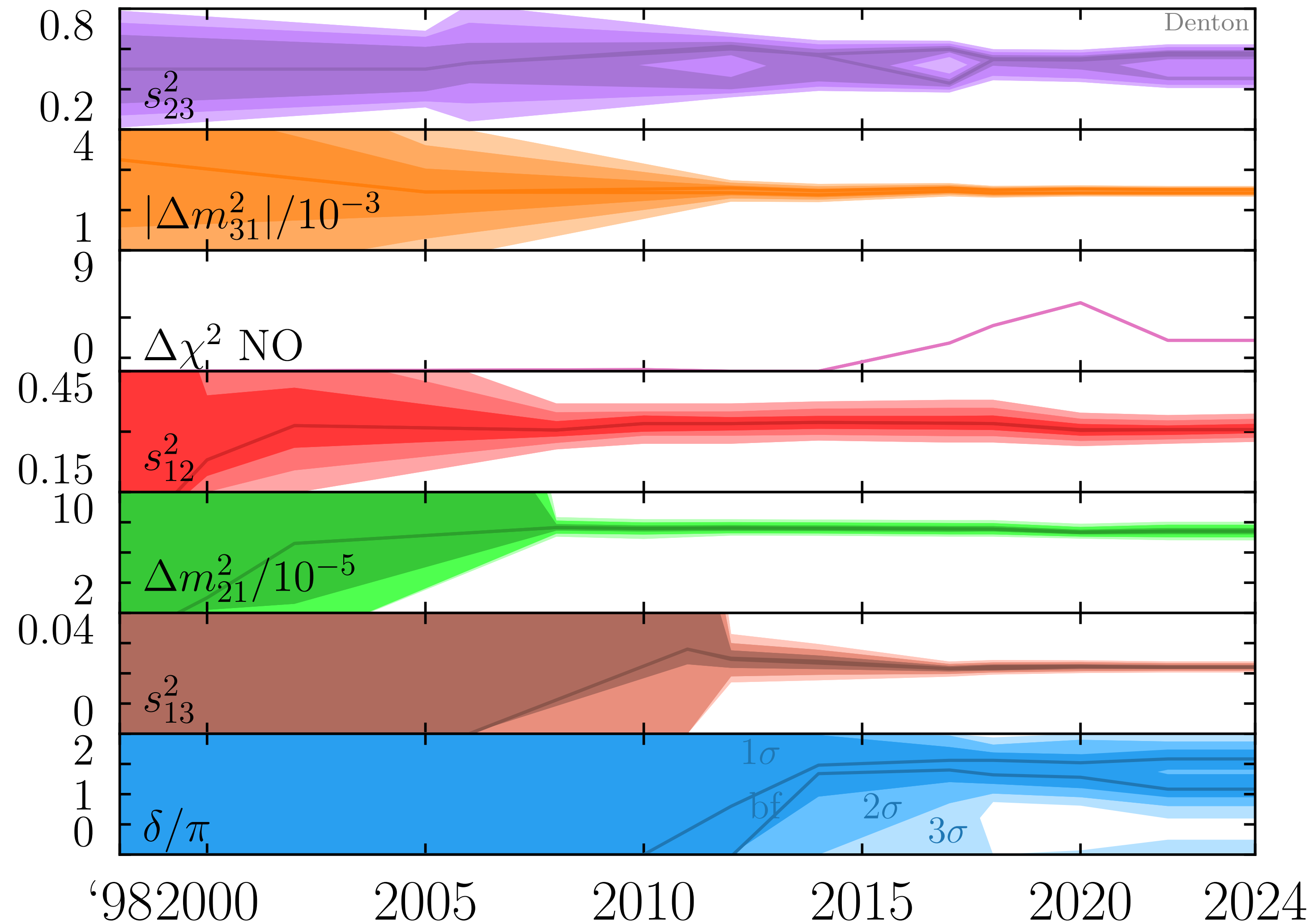
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See Mriam Tortola's talk for any details!

Time evolution of precision of our knowledge about mixing parameters



we are now in
a “precision” era!

Denton et al (SNOWMASS Report), arXiv:2212.00809, updated in 2024 by P. Denton

Best Fitted values of mixing parameters from PDG2024

$$\sin^2 \theta_{12} = 0.307 \pm 0.013 \quad \Delta m_{21}^2 = (7.53 \pm 0.18) \times 10^{-5} \text{ eV}^2$$

$$\sin^2 \theta_{13} = (2.19 \pm 0.07) \times 10^{-2}$$

Normal Order

$$\Delta m_{32}^2 = (2.455 \pm 0.028) \times 10^{-3} \text{ eV}^2 \quad \sin^2 \theta_{23} = 0.558^{+0.015}_{-0.021}$$

Inverted Order

$$\Delta m_{32}^2 = (-2.529 \pm 0.029) \times 10^{-3} \text{ eV}^2 \quad \sin^2 \theta_{23} = 0.553^{+0.016}_{-0.024}$$

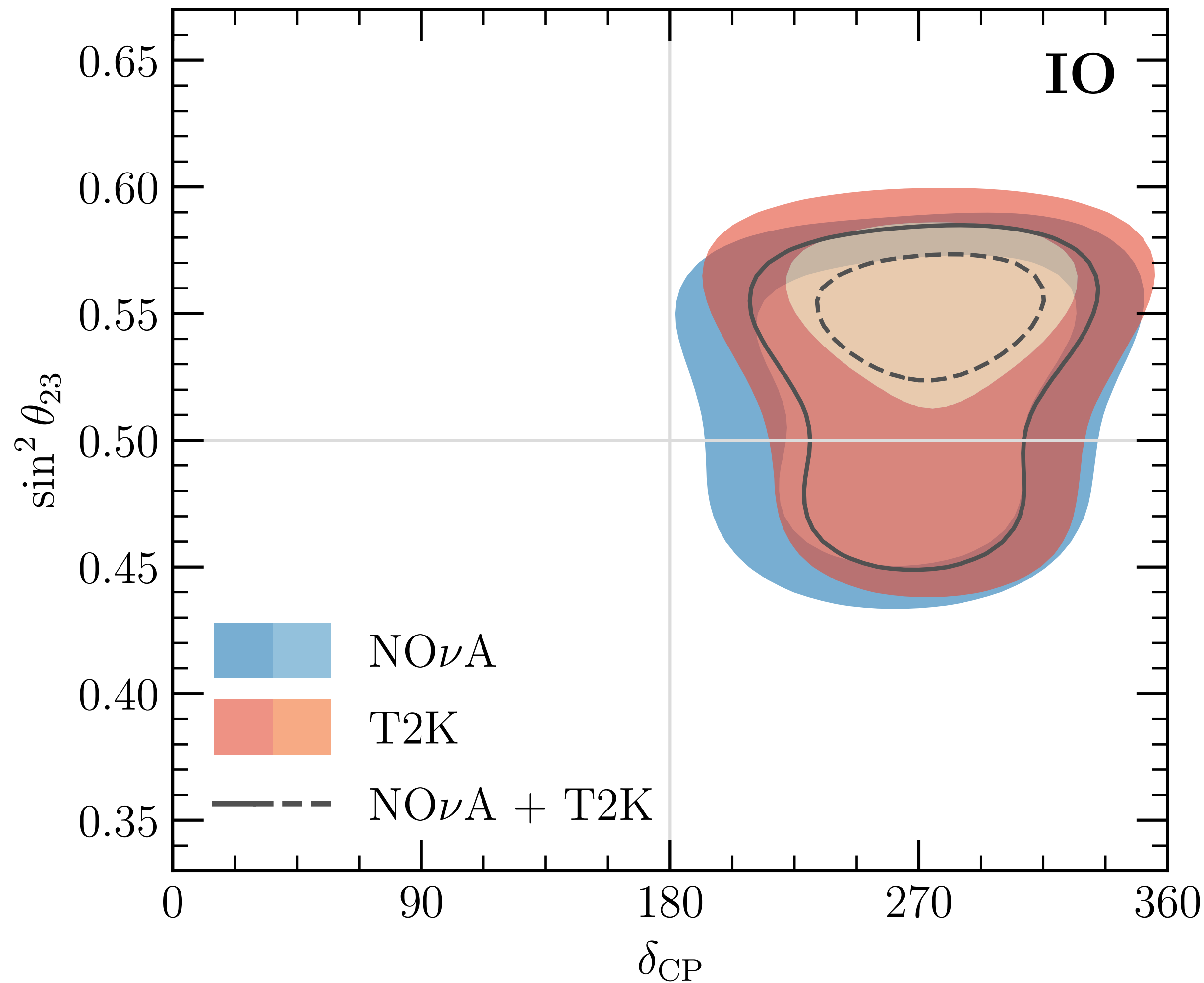
$$\delta_{CP} = 1.19 \pm 0.22\pi \text{ rad}$$

~ a few % precisions, except for CP phase and Mass Ordering

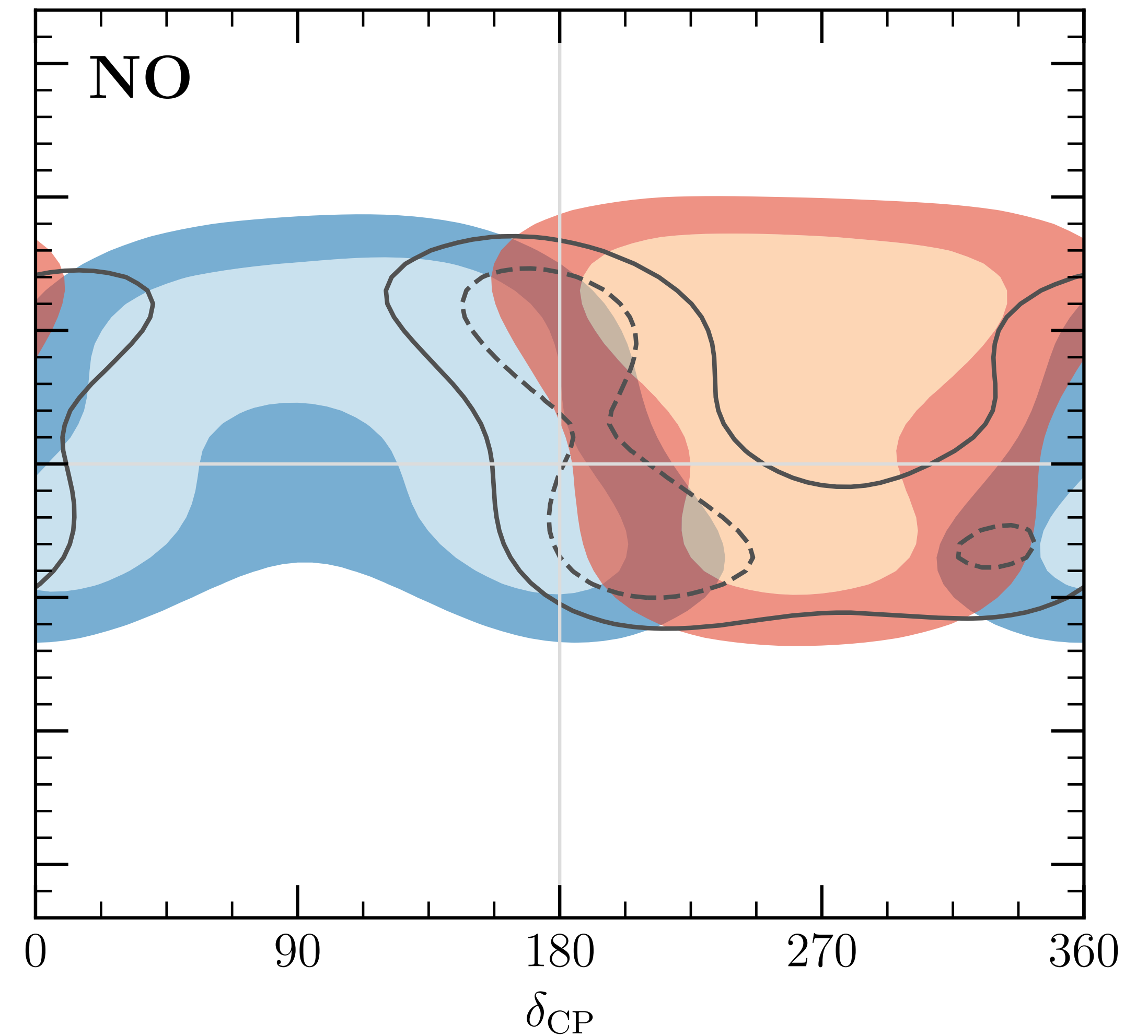
S. Navas et al. (PDG2024), Phys. Rev. D 110, 03001 (2024)

We do not know very well the value of CP phase

Inverted Ordering

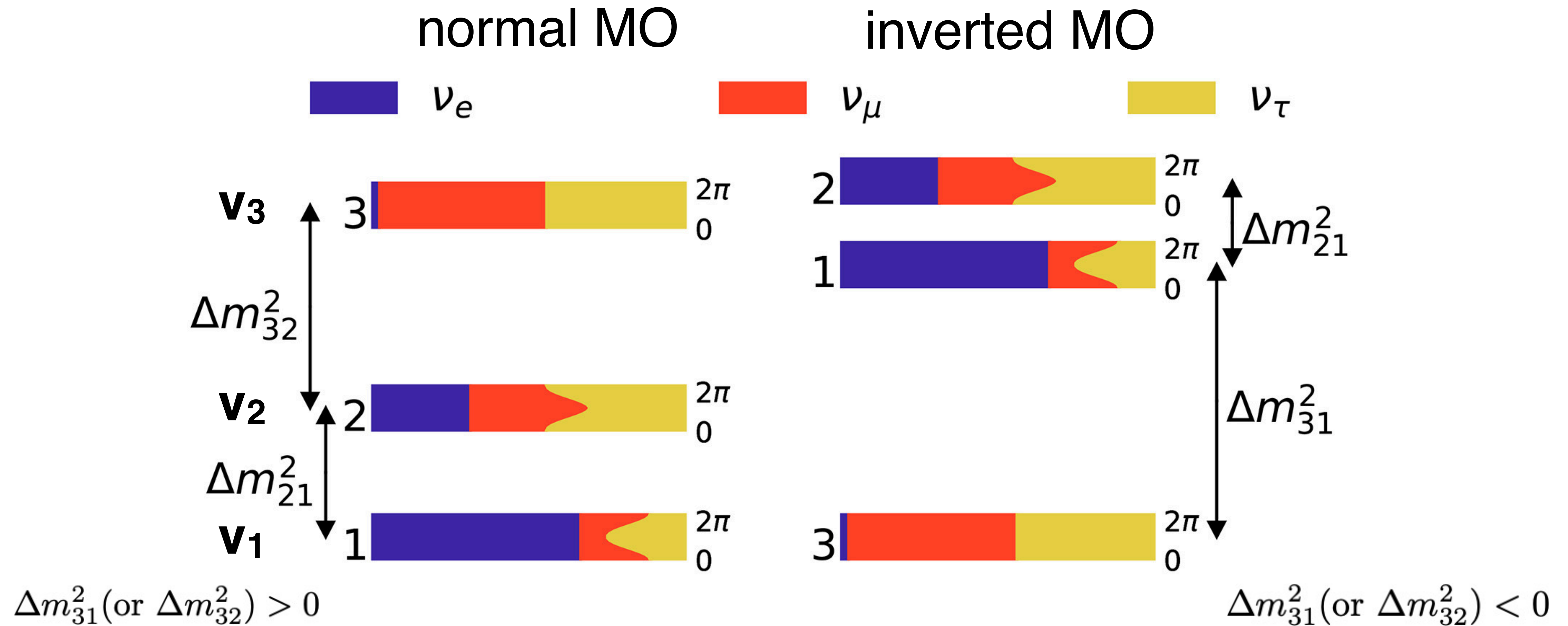


Normal Ordering



NuFit6.0 Esteban et al, arXiv:2410.05380

We still do not know the neutrino mass ordering (MO)








Salas et al, Front.Astron.Space.Sci 5, 36(2018)

Normal MO is currently favored only at $\sim 2\text{-}3\sigma$, not yet conclusive

Open Questions in Neutrino Sector

- **Why neutrino masses are very small? How to understand mixing pattern?**
- **Neutrinos are Dirac or Majorana particles?**
- **Is CP (Charge Conjugation) symmetry violated?**
- **Mass Ordering (MO), Normal or Inverted?**
- **Octant of θ_{23} , larger than $\pi/4$ or not?**
- **Are there more than 3 neutrinos (sterile ν) ?**
- **Do neutrinos have some new BSM (Beyond Standard Model) properties such as non-standard interactions (NSI), magnetic moment, instabilities (decay), decoherence, etc?**

Open Questions in Neutrino Sector

- Why neutrino masses are very small? How to understand mixing pattern?
- Neutrinos are Dirac or Majorana particles?
- Is CP (Charge Conjugation) symmetry violated?  **Hyper-K/DUNE**
- Mass Ordering (MO), Normal or Inverted?  **JUNO/HK/DUNE**
- Octant of θ_{23} , larger than $\pi/4$ or not?  **Hyper-K/DUNE**
- Are there more than 3 neutrinos (sterile ν) ?  **JUNO/HK/DUNE**
- Do neutrinos have some new BSM (Beyond Standard Model) properties such as non-standard interactions (NSI), magnetic moment, instability (decay), decoherence, etc?  **JUNO/HK/DUNE**

So far, in neutrino sector, there is no strong evidence of new physics beyond SM (beyond mass and mixing), apart from some indication/hint like LSND anomaly, or some mild “tension” between some experiments

So we need to look for hint for new physics in future experiments, in particular, in the context of new oscillation experiments, JUNO, Hyper-Kamiokande and DUNE

Near Future Long-Baseline Neutrino Oscillation Experiments: Hyper-Kamiokande and DUNE

Please also see talks by

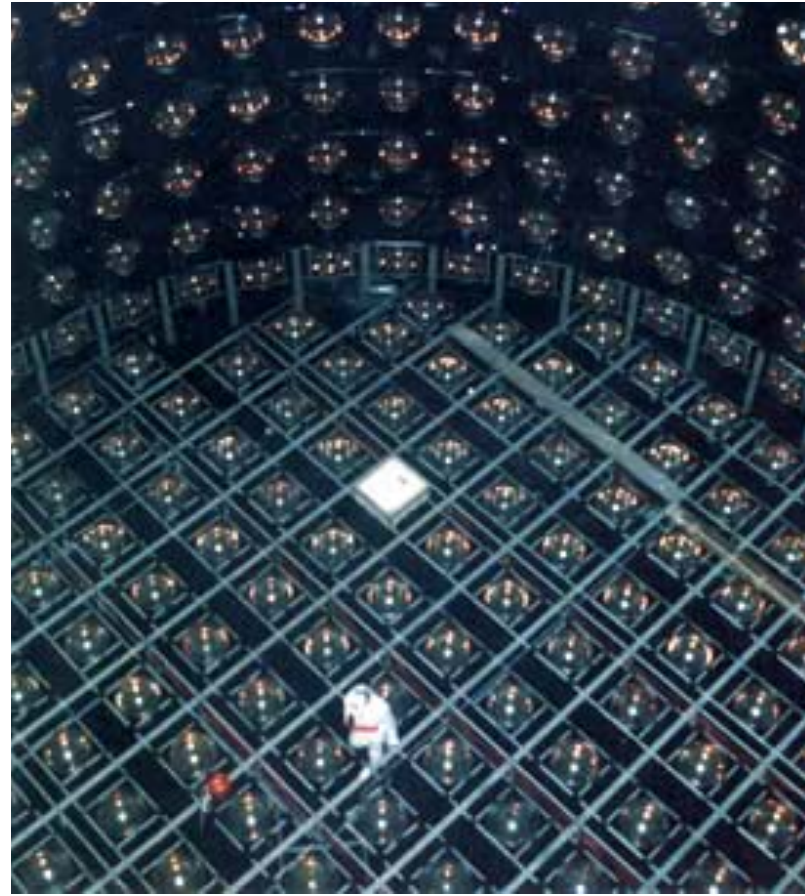
Saul Cuen-Rochin for Hyper-Kamiokande (yesterday)

Pedro Ochoa Ricoux for Short Baseline Oscillation Experiments (today)

Ettore Segreto for DUNE (Friday)

Hyper-Kamiokande

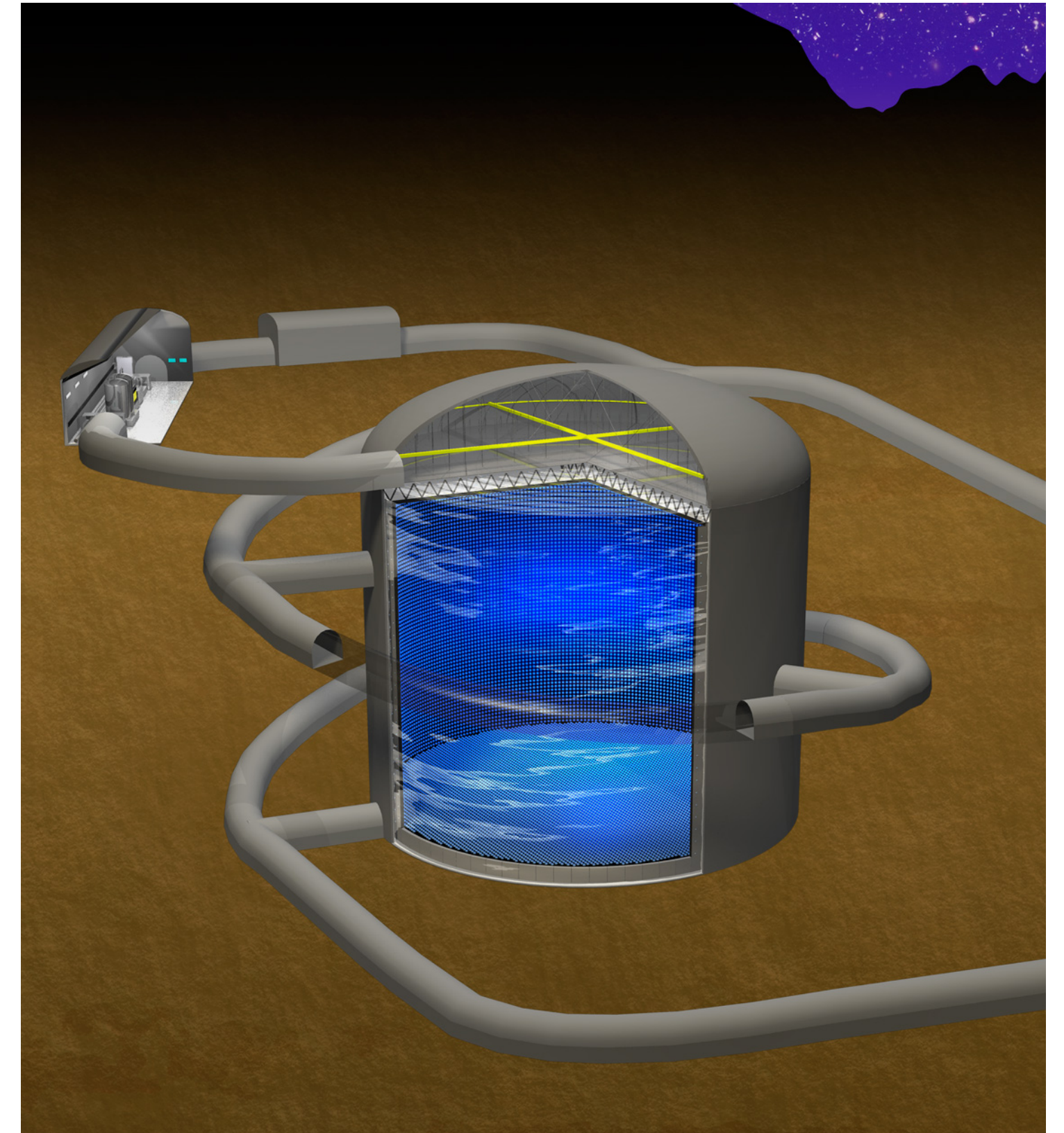
3rd Generation Water Cherenkov Detector in Kamioka



Kamiokande (1983-1996)
0.68 kton, Detection of
Neutrinos from SN1987A



Super-Kamiokande (1996-ongoing):
22.5 kton, Discovery of Neutrino Oscillation
in 1998



Hyper-Kamiokande (will start in 2027)
188 kton (~8 times SK)
Observation of CP violation, Nucleon Decay,
Supernova, New Physics?

Hyper-Kamiokande is in the Construction Phase

Expected to start data taking in 2027

Cavern now excavated to 37m depth (over halfway)



Photograph taken
June 2024

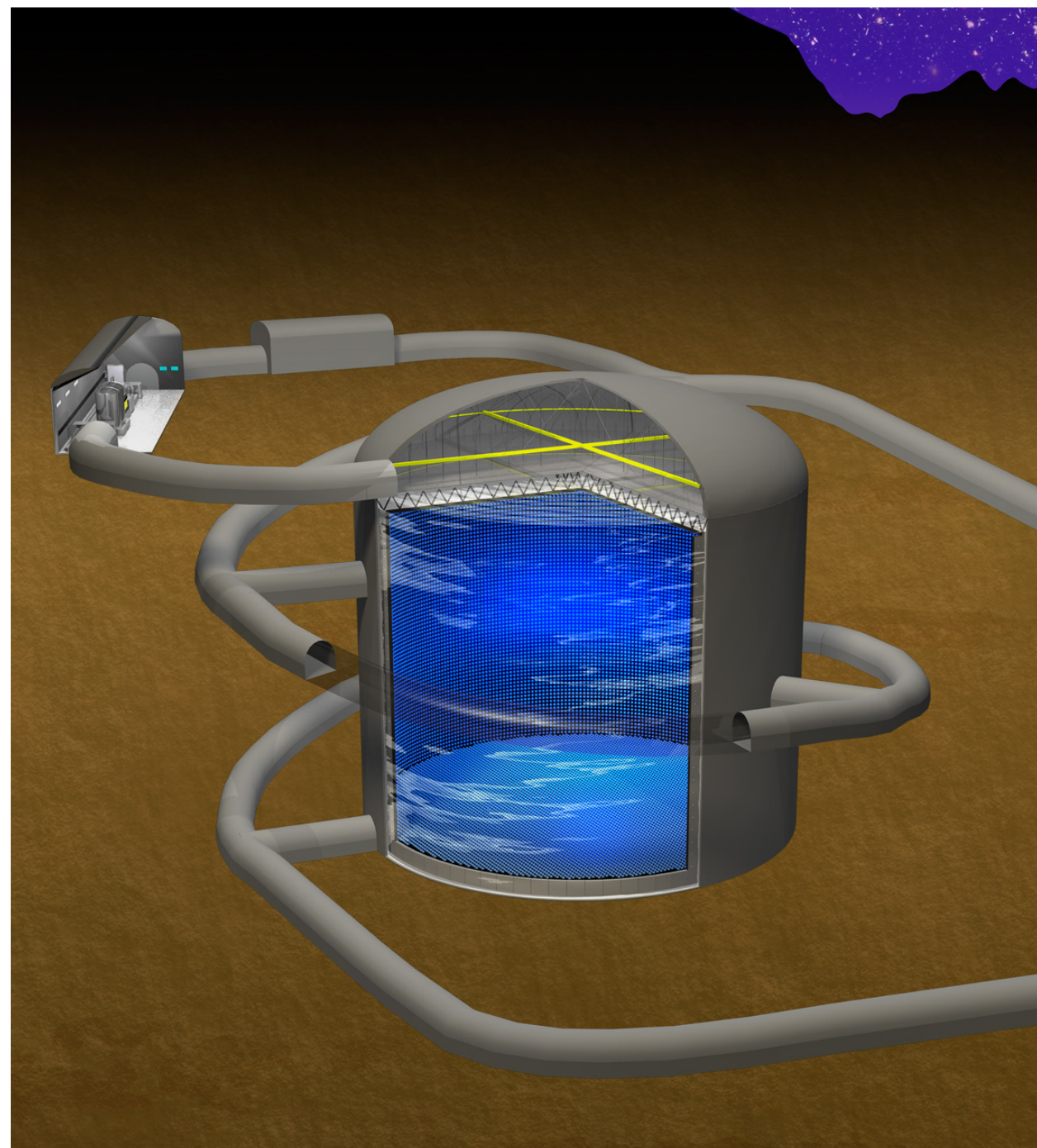
22

Slide shown by Jeanne Wilson @ NOW2024 workshop (September 2024)

Experimental Setup of HK's LBL Oscillation Study by using JPARC Neutrino Beam

L = 295 km

J-PARC



often called "T2HK" (Tokai to HK)
experiment/setup (not an official name)

$\nu_e/\bar{\nu}_e$

$\nu_\mu/\bar{\nu}_\mu$

near detector

L = 280 m

ND280

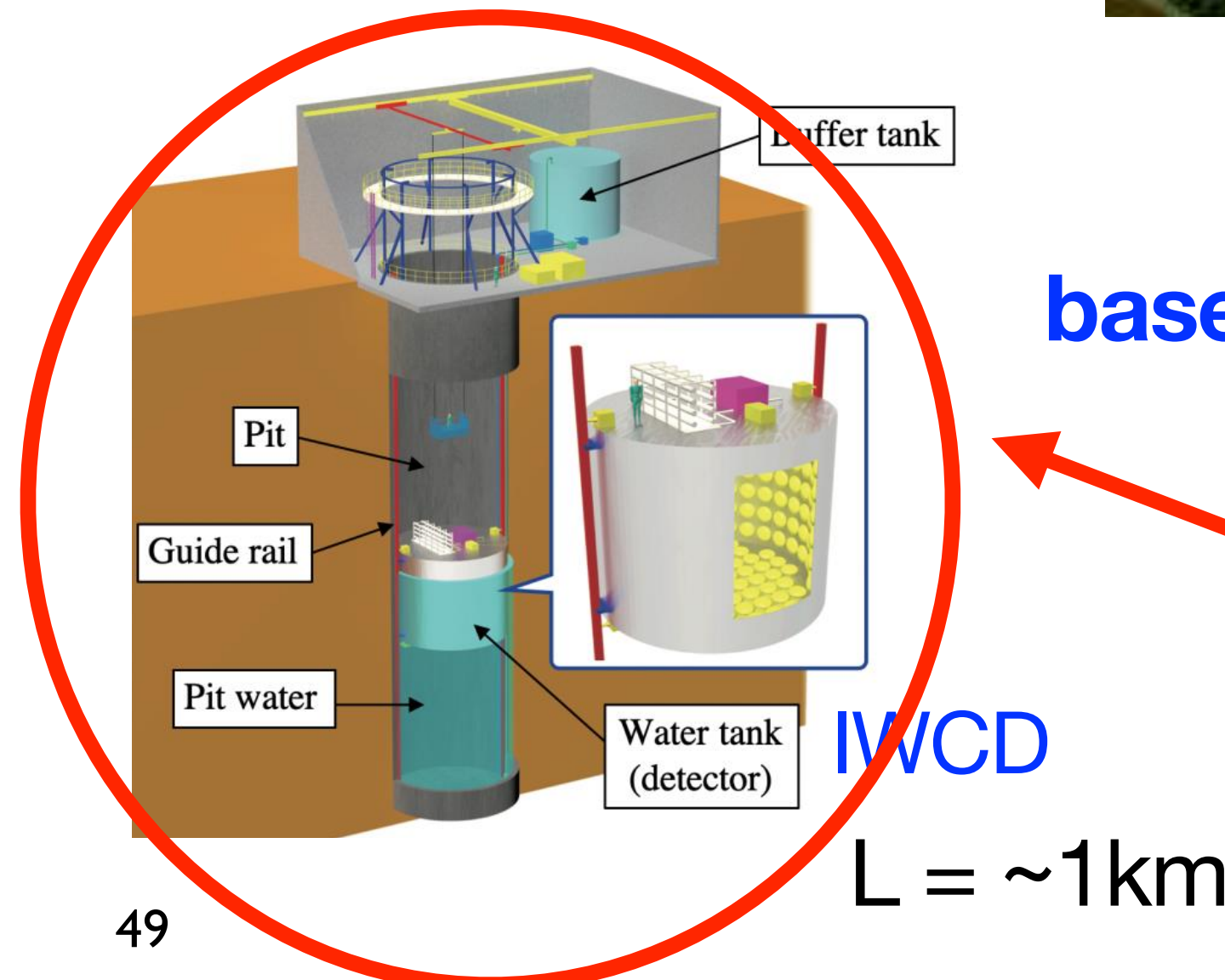
$\nu_\mu/\bar{\nu}_\mu$



1.3 MW ν beam

based on off-axis (2.5°) beam

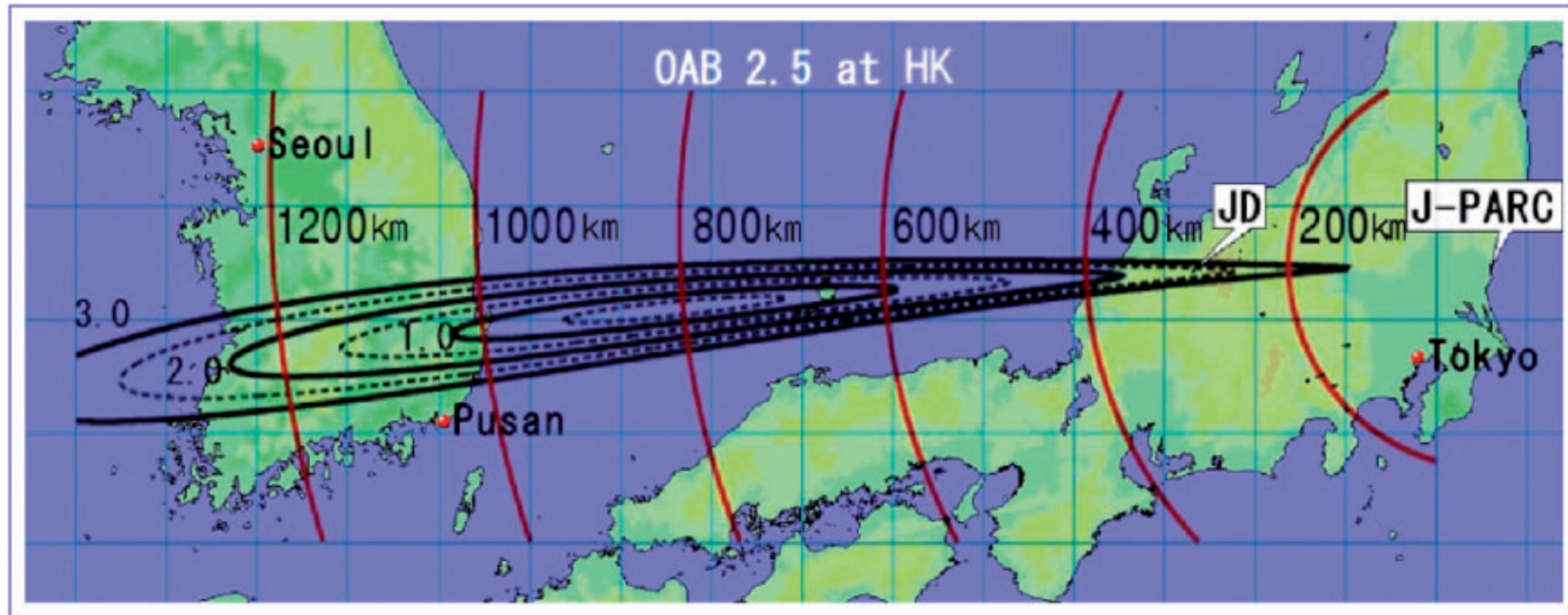
near detector



INWCD

L = ~1km

Possibility to construct another identical detector in Korea with a baseline ~ 1000 km, is under consideration/discussion



map showing baseline and off-axis angles of the beam from J-PARC

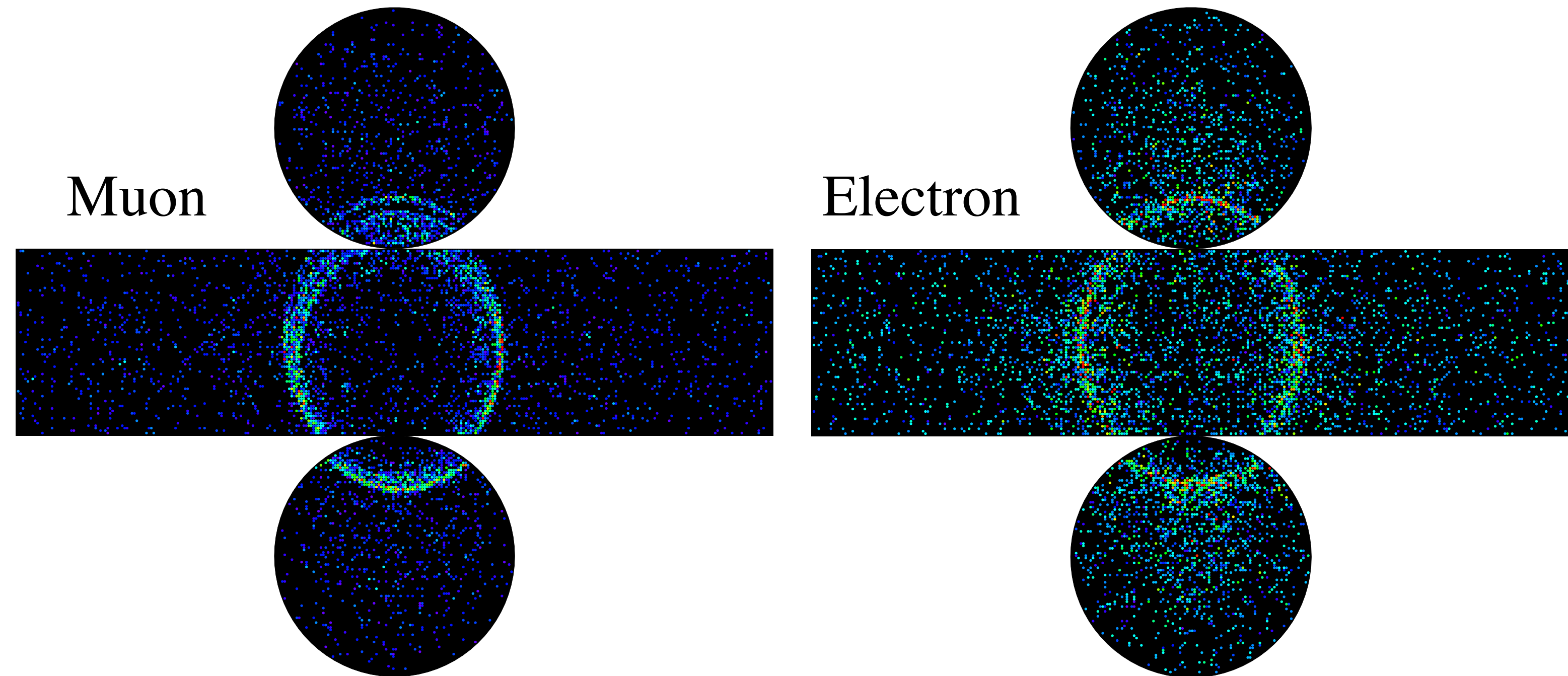
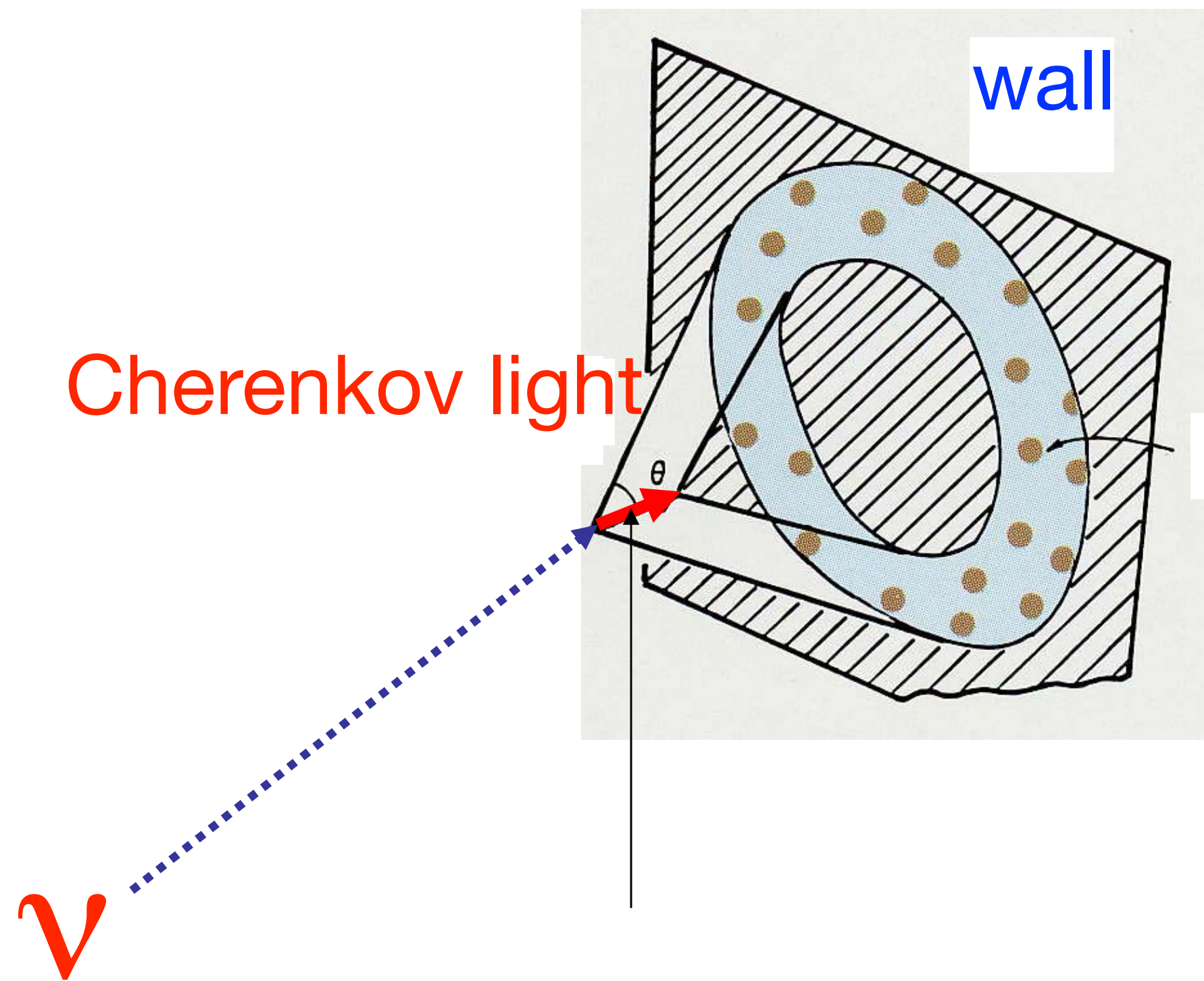
This setup is often called “T2HKK” (Tokai to HK and Korea), not an official name

ν_μ and ν_e can be distinguished in the Water Cherenkov detector

$$n + \nu_\mu \rightarrow p + \mu^-$$

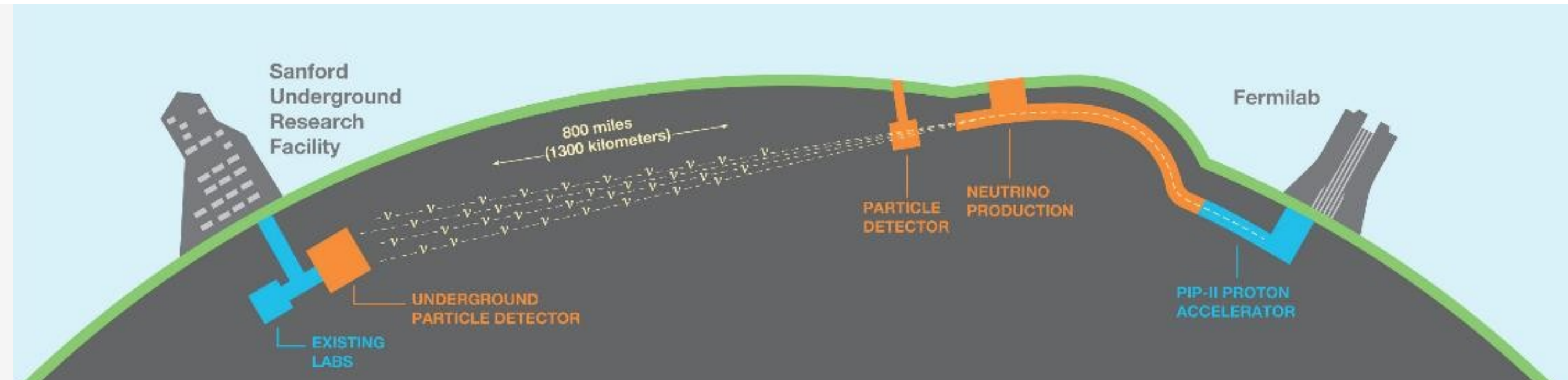
Charged Current Interaction

$$n + \nu_e \rightarrow p + e^-$$



if $v_{\text{particle}} > \text{speed of light in matter} = c/n$ ($n=1.33$ for water)

DUNE (Deep Underground Neutrino Experiment) Project



- Wideband (anti)neutrino beamline with $>2\text{MW}$ intensity
- Underground, modular LArTPC Far Detector with ≥ 40 kt fiducial mass
- Movable LArTPC Near Detector with muon spectrometer and separate on-axis detector
- Global collaboration of >1400 scientists and engineers



$L = 1285 \text{ km}$

5

DUNE - Neutrino24 - Chris Marshall



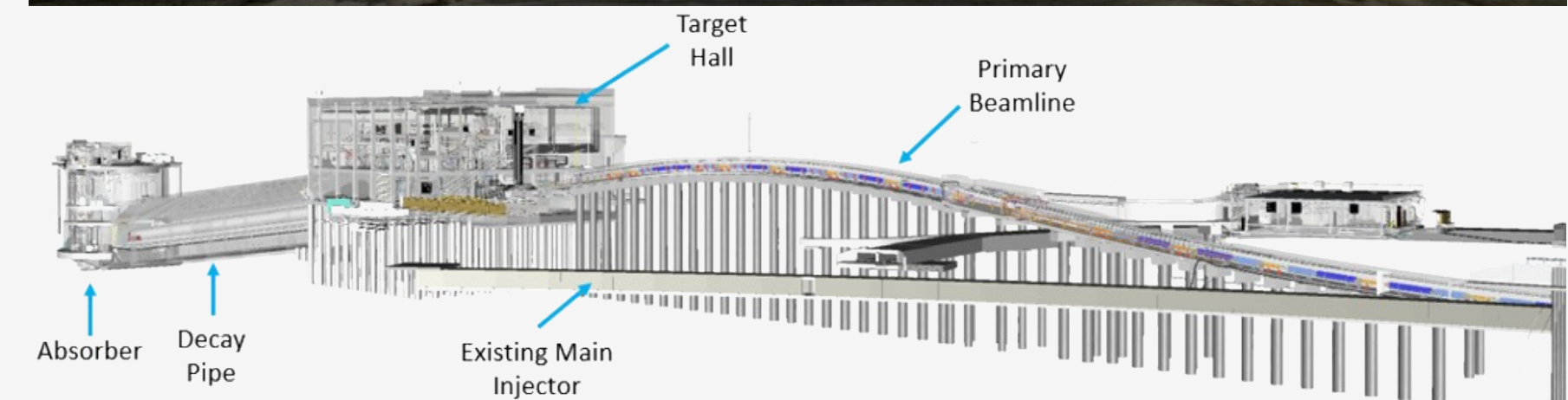
See the talk by Ettore Segreto

Talk by C. Marshall @ Neutrino 2024

DUNE (Deep Underground Neutrino Experiment) Project

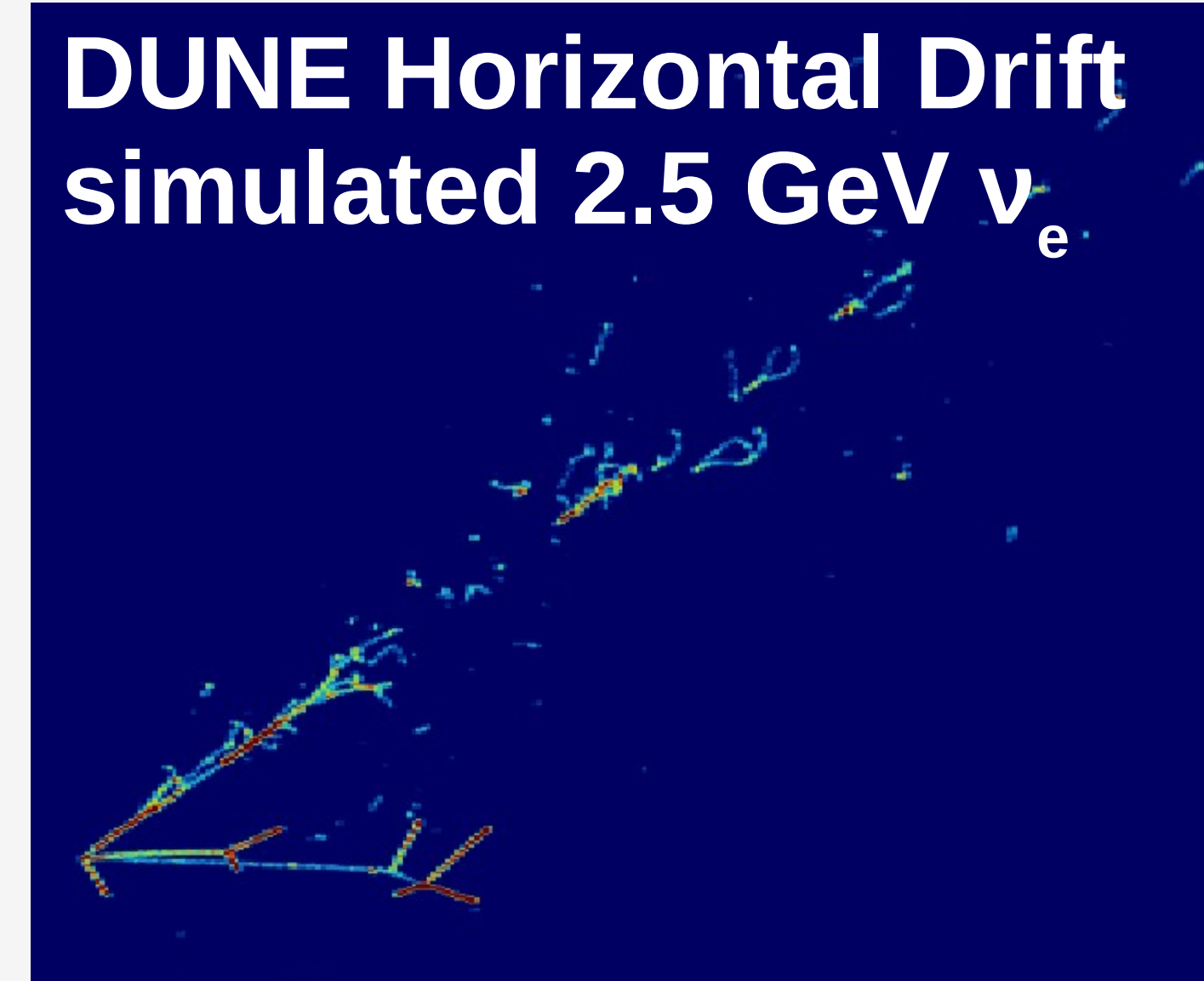
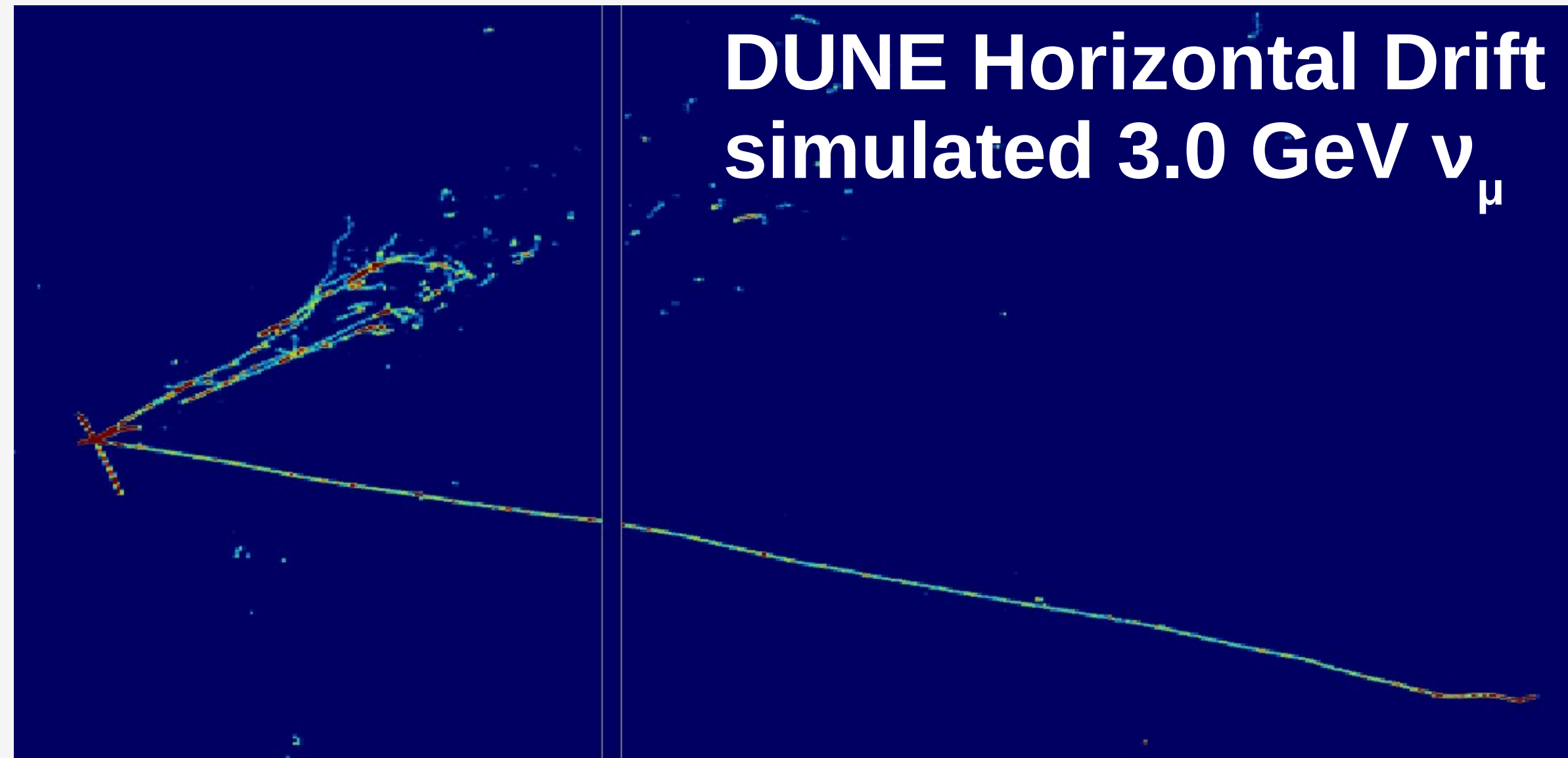
Long-baseline oscillations as part of a broad physics program

- Large, sensitive underground detectors are excellent to:
 - Observe supernova burst neutrinos
 - Measure solar and atmospheric neutrinos
 - Search for new physics (nucleon decays, cosmogenic dark matter, etc.)
- Intense beams with capable near detectors are excellent to:
 - Search for new physics produced in the beamline
 - Search for new physics in rare interactions (i.e. neutrino tridents)



DUNE detector is based on Liquid Argon Time Projection Chamber

LArTPC: flavor & energy reco over a broad range of topologies



- 60% of interactions at DUNE energy have final state pions → LArTPC enables precise hadron reconstruction
- Excellent e/μ and e/γ separation

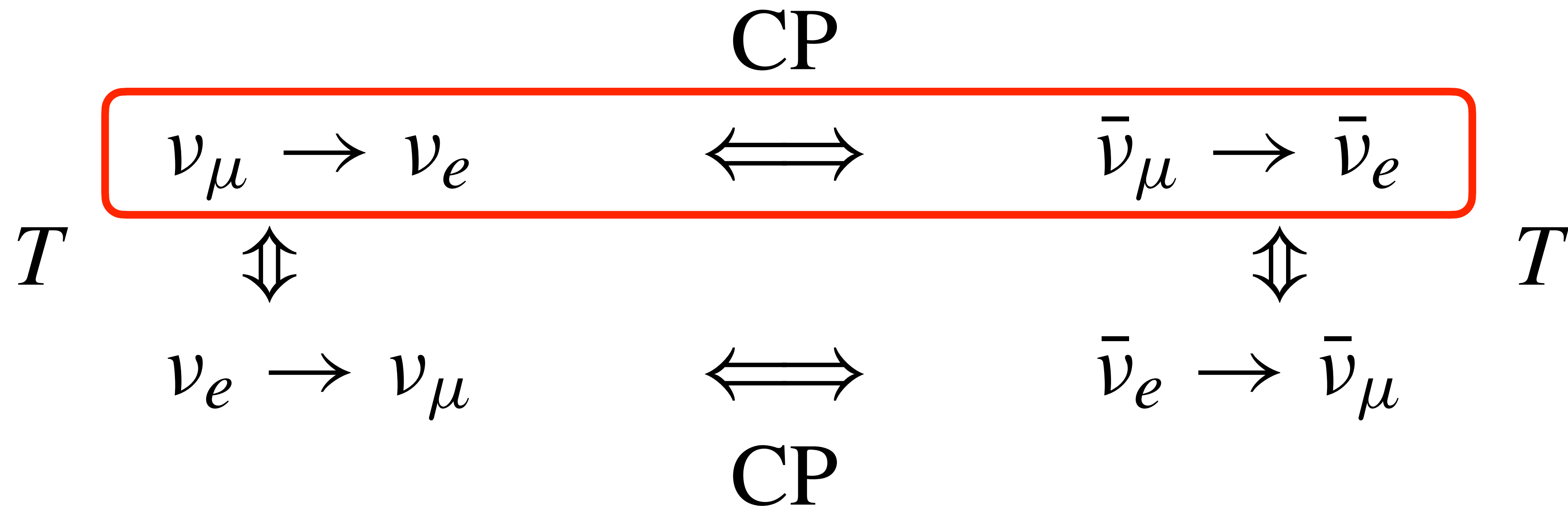
Test of CP Violation by Long-Baseline Neutrino Oscillation Experiments

Test of CP (Charge Conjugation) Symmetry

One of the fundamental symmetries in Nature

May shed some light on matter-antimatter asymmetry in the Universe

studying oscillation between muon and electron neutrinos is the easiest way



Compare oscillation probabilities of CP conjugate channels

Note: if CP is violated, T (time reversal) is also violated due to CPT invariance

Probability of $\nu_\mu \rightarrow \nu_e$ oscillation in vacuum

$$P(\nu_\mu \rightarrow \nu_e) = \left| U_{e1} U_{\mu 1}^* e^{-i \frac{m_1^2}{2E} L} + U_{e2} U_{\mu 2}^* e^{-i \frac{m_2^2}{2E} L} + U_{e3} U_{\mu 3}^* e^{-i \frac{m_3^2}{2E} L} \right|^2$$

ν_1 ν_2 ν_3

$$\approx \left| \sqrt{P_{\text{atm}}} e^{-i(\Delta_{32} + \delta_{\text{CP}})} + \sqrt{P_{\text{sol}}} \right|^2$$

HN, Parke & Valle, arXiv:0710.0554 [hep-ph]

$$= P_{\text{atm}} + \underbrace{2\sqrt{P_{\text{atm}}} \sqrt{P_{\text{sol}}} \cos(\Delta_{32} + \delta_{\text{CP}})}_{\text{interference term}} + P_{\text{sol}}$$

where $\Delta_{ij} \equiv \frac{\Delta m_{ij}^2}{4E} L$

$$\sqrt{P_{\text{atm}}} \equiv \sin \theta_{23} \sin 2\theta_{13} \sin \Delta_{31}$$

atmospheric term

interference term

$$\sqrt{P_{\text{sol}}} \equiv \cos \theta_{23} \cos \theta_{13} \sin 2\theta_{12} \sin \Delta_{21}$$

solar term

for $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ we should consider $U \rightarrow U^*$ or $\delta_{\text{CP}} \rightarrow -\delta_{\text{CP}}$

For HK (or DUNE), $\sin \Delta_{21} \sim \Delta_{21} (\sim |\Delta_{31}|/30) \longrightarrow$ osc. is driven by $\Delta m_{32}^2 \sim \Delta m_{31}^2$

In matter, mixing parameters get modified $\theta_{ij} \rightarrow \theta_{ij}^{\text{m}}, \Delta_{ij} \rightarrow \Delta_{ij}^{\text{m}}$ but the same formula applies

Observation of CP Violation (CPV) in vacuum

$$\Delta P_{\text{CPV}} \equiv P(\nu_\alpha \rightarrow \nu_\beta) - P(\bar{\nu}_\alpha \rightarrow \bar{\nu}_\beta) = -16J_{\alpha\beta} \sin \Delta_{12} \sin \Delta_{23} \sin \Delta_{31},$$

where $\Delta_{ij} \equiv \frac{\Delta m_{ij}^2}{2E} L$

$$J_{\alpha\beta} \equiv \Im[U_{\alpha 1} U_{\alpha 2}^* U_{\beta 1} U_{\beta 2}^*] = \pm J_\nu, \quad J_\nu \equiv s_{12} c_{12} s_{23} c_{23} s_{13} c_{13}^2 \sin \delta_{\text{CP}},$$

+(-) sign is for cyclic (anti-cyclic) permutation of $\alpha, \beta = e, \mu, \tau$

parametrization independent measure of CPV (Jarlskog invariant)

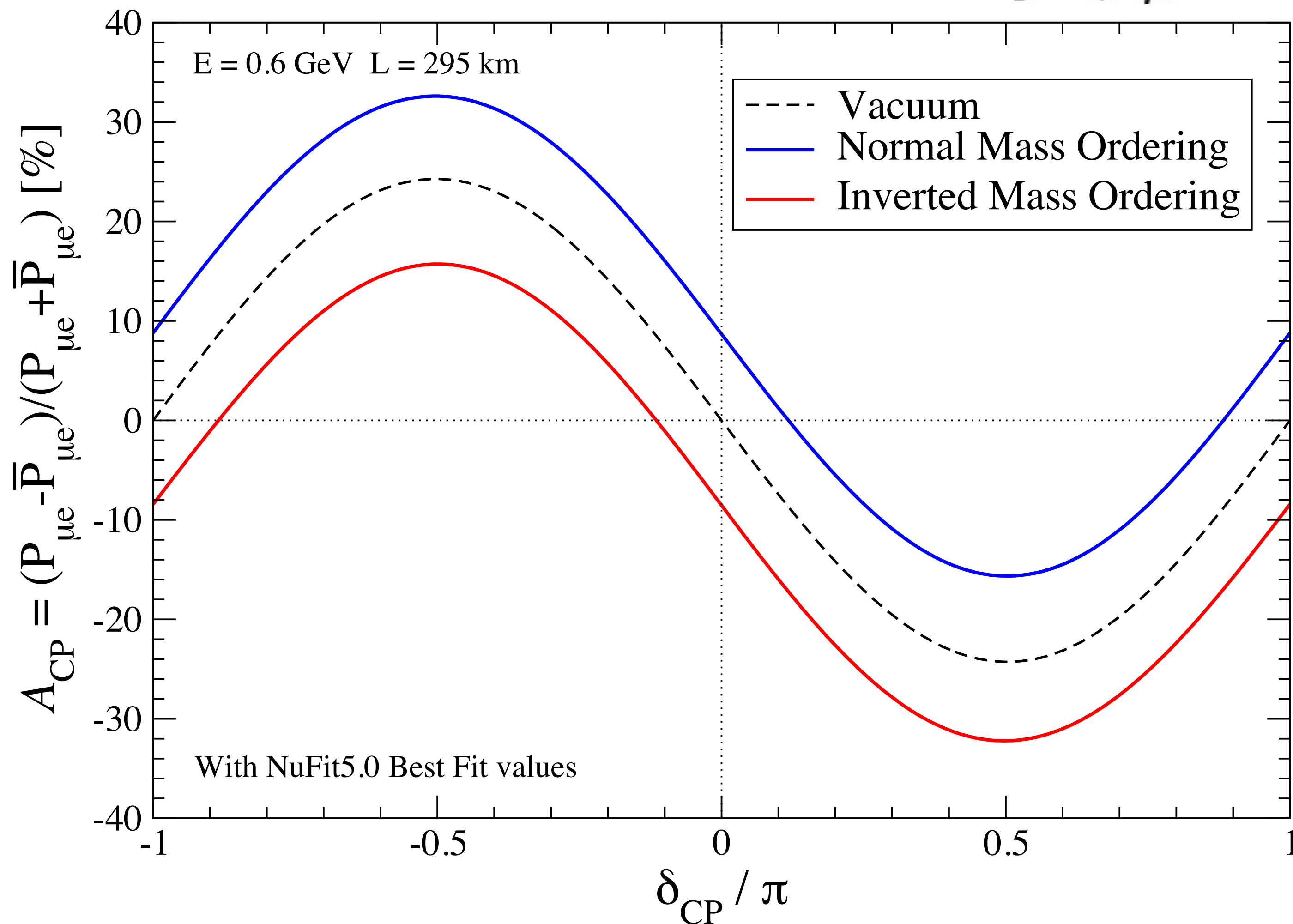
from current data, $J_\nu^{\text{max}} = J_\nu(\sin \delta_{\text{CP}} = 1) \simeq 0.033$

CPV \leftrightarrow all ν masses must be non-degenerate, all $\theta_{12}, \theta_{23}, \theta_{13} \neq 0$ and $\sin \delta_{\text{CP}} \neq 0$

CP asymmetry $A_{\text{CP}} \equiv \frac{[P(\nu_\mu \rightarrow \nu_e) - P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)]}{[P(\nu_\mu \rightarrow \nu_e) + P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)]} \propto \sin \delta_{\text{CP}}$ **would be useful**

CP asymmetry

$$A_{\text{CP}} \equiv \frac{[P(\nu_\mu \rightarrow \nu_e) - P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)]}{[P(\nu_\mu \rightarrow \nu_e) + P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)]} \propto \sin \delta_{\text{CP}}$$



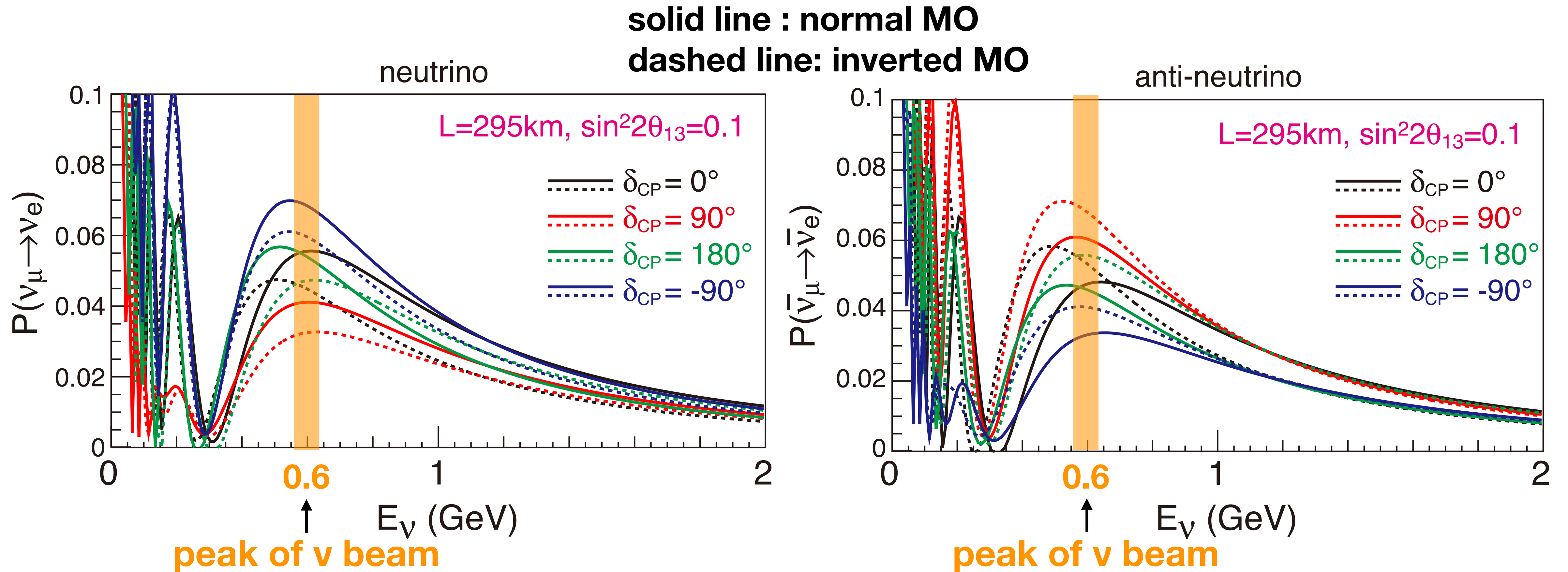
CP asymmetry can be as large as ~30%

matter effect (predictable)

Due to matter effect, $A_{\text{CP}} \neq 0$
even for $\sin \delta_{\text{CP}} = 0$

CP asymmetry could, in principle, tell us the presence of CPV in the lepton sector even if some unknown new physics (NSI, non-unitarity, etc) is the source of CPV!

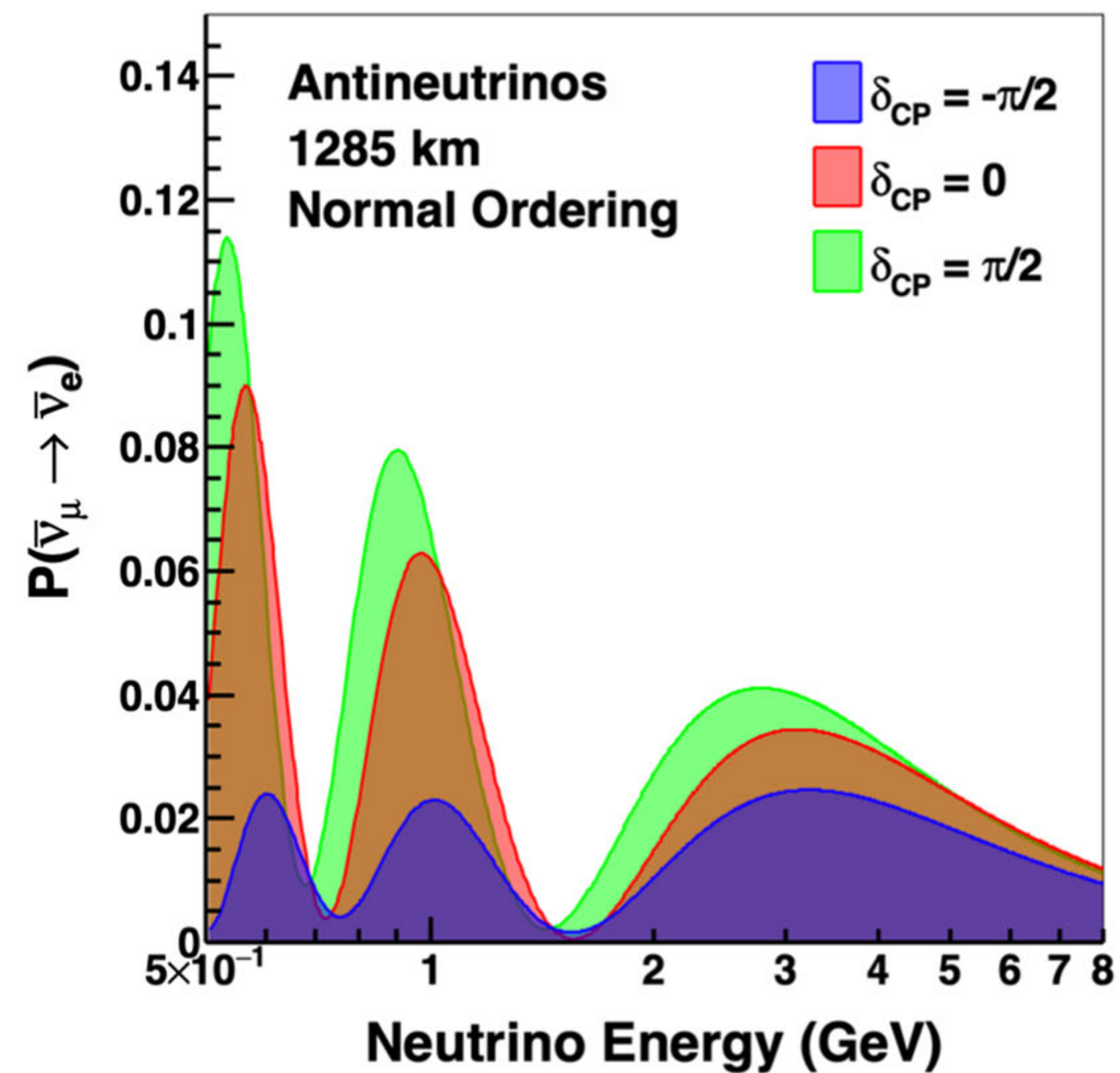
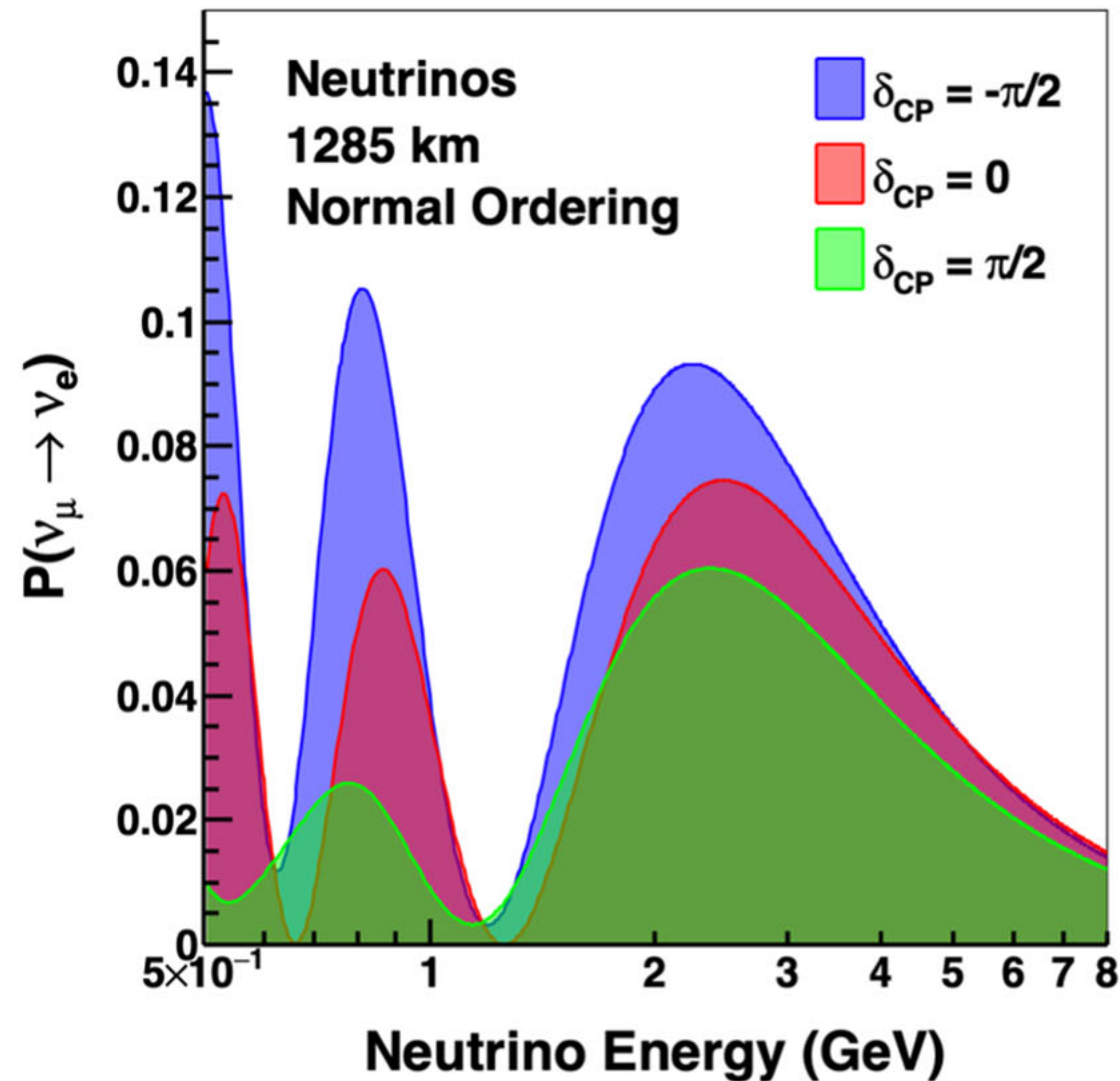
Appearance Probabilities for T2HK (Tokai to Hyper-K)



HK Design Report, arXiv:1805.04163v2 [hep-ex]

CP phase affects oscillation amplitudes and also positions of the peaks and dips of oscillations

Appearance Probabilities for DUNE (L ~ 1300 km)

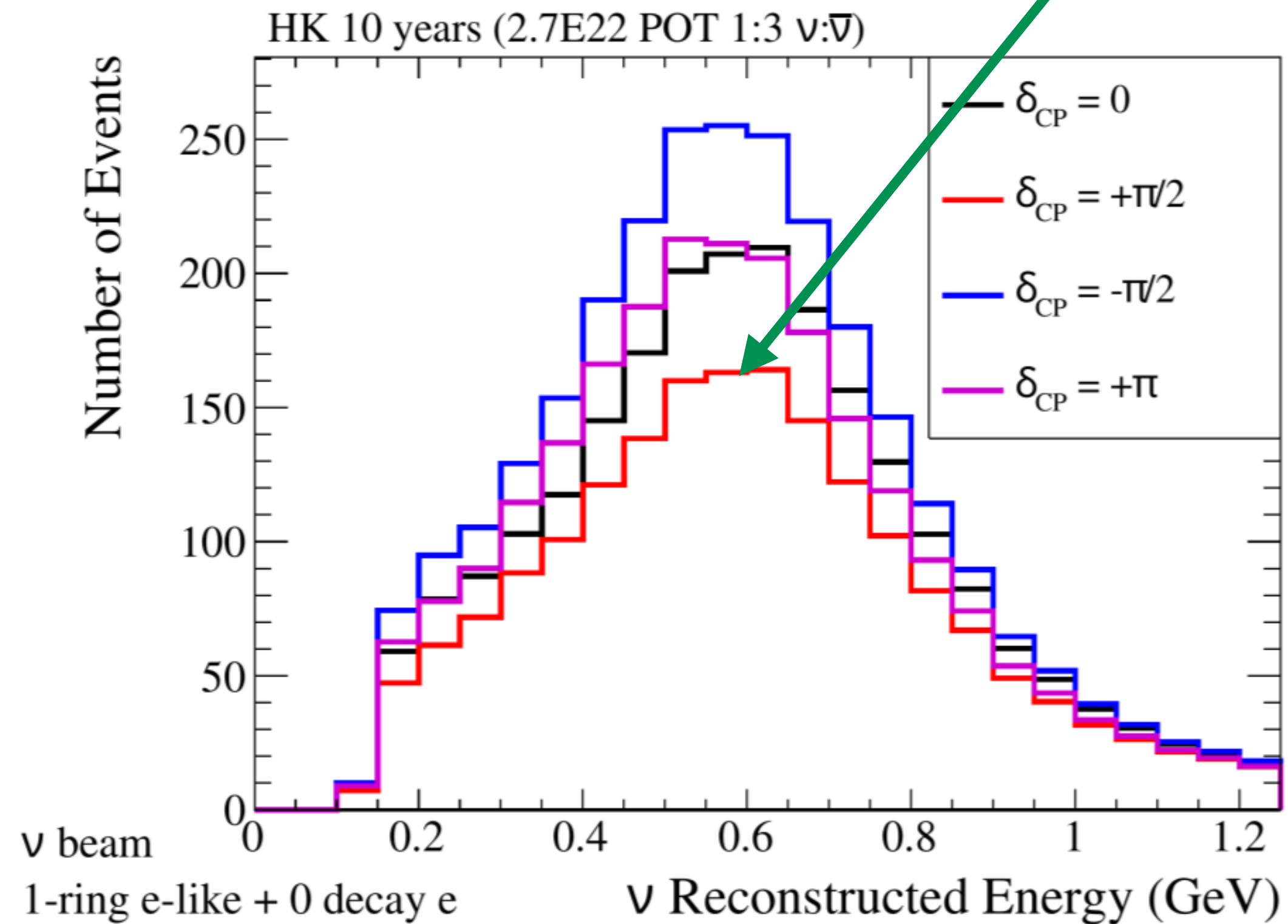


Abi et al, Eur. Phys. J. C80, 978 (2020)

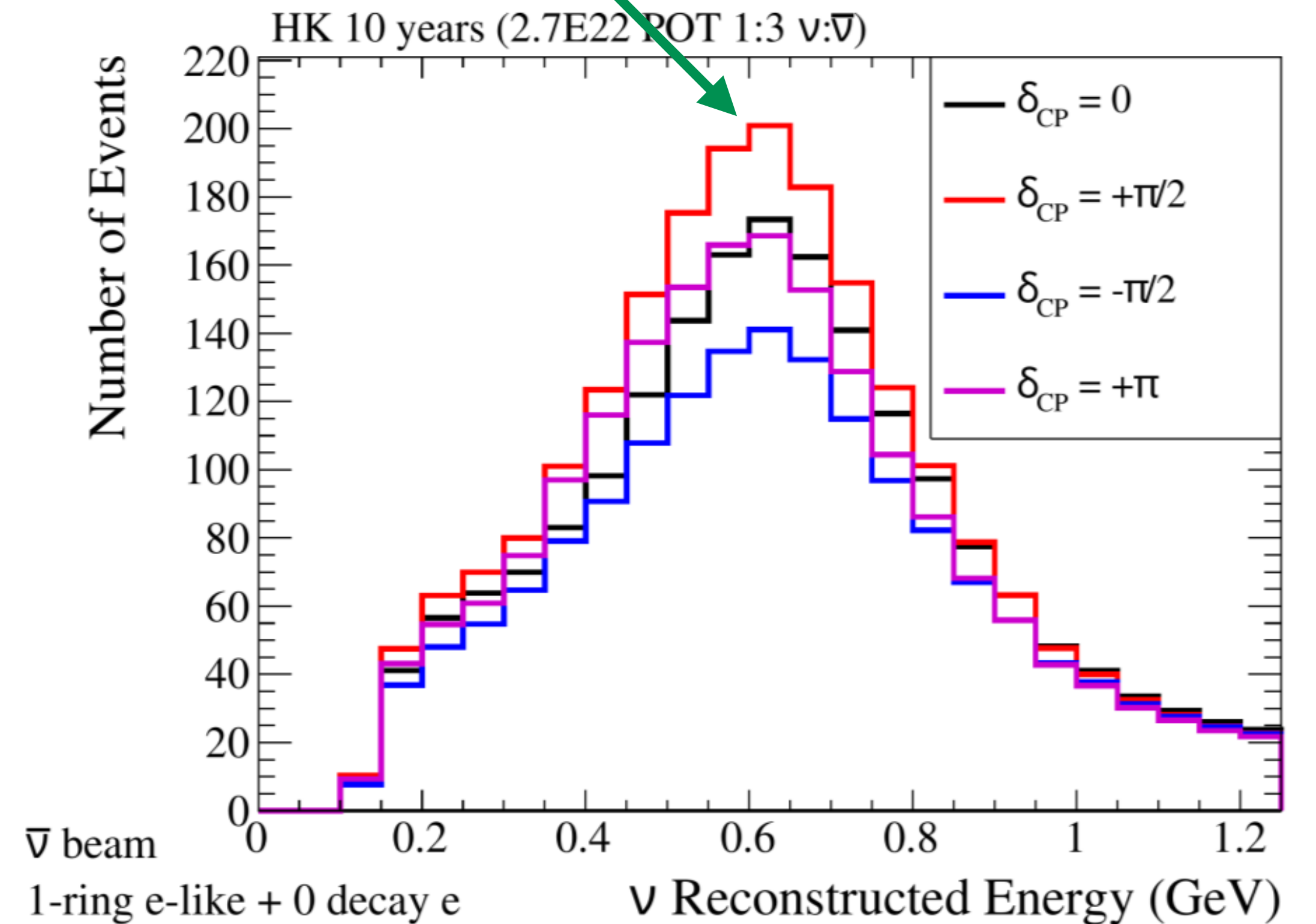
Large differences in probability for neutrino and anti-neutrinos comes mainly from the matter effect

Expected Event Number Distributions at Hyper-K

Large Asymmetry



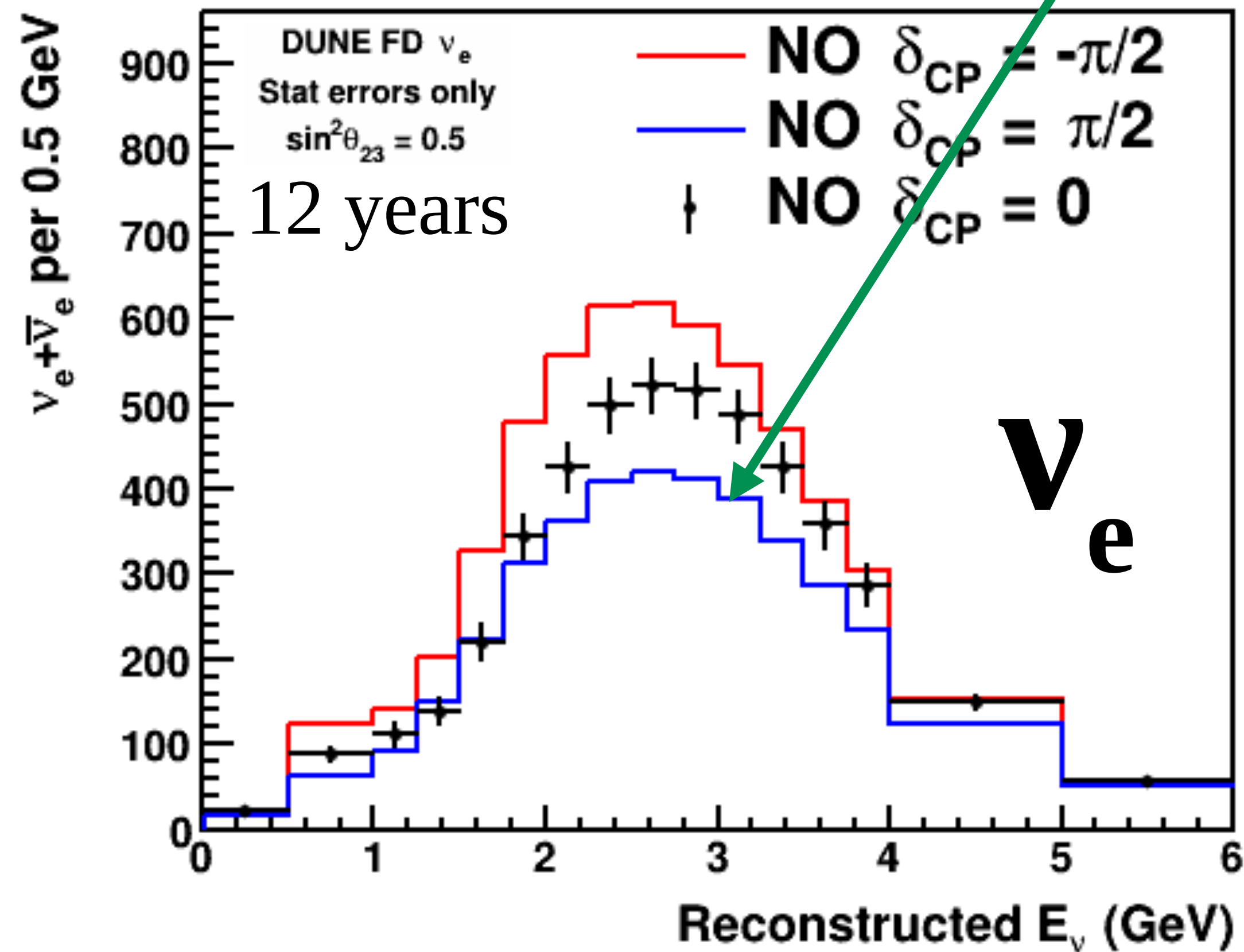
Neutrino



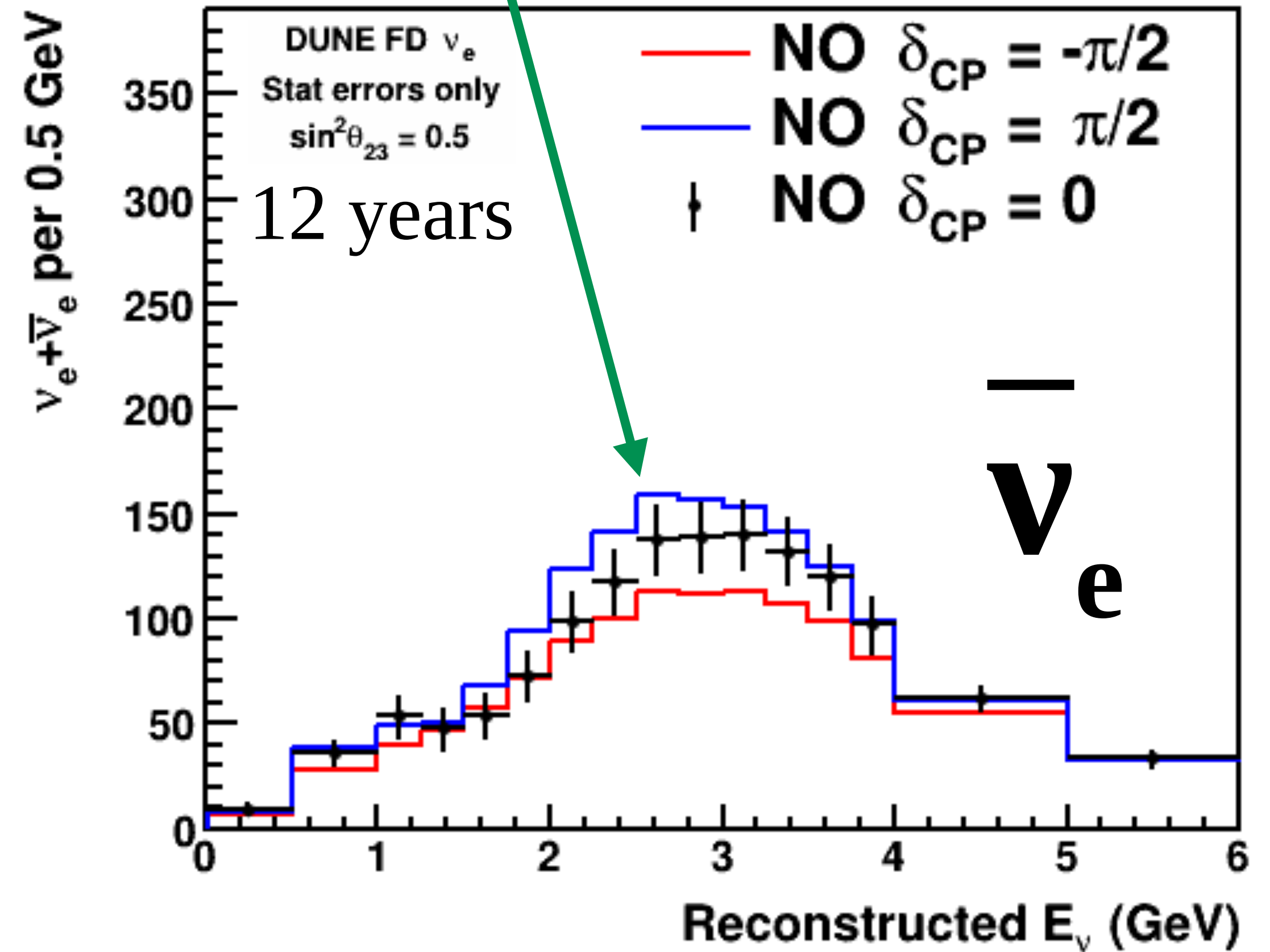
Anti-Neutrino

Expected Event Number Distributions at DUNE

Large Asymmetry



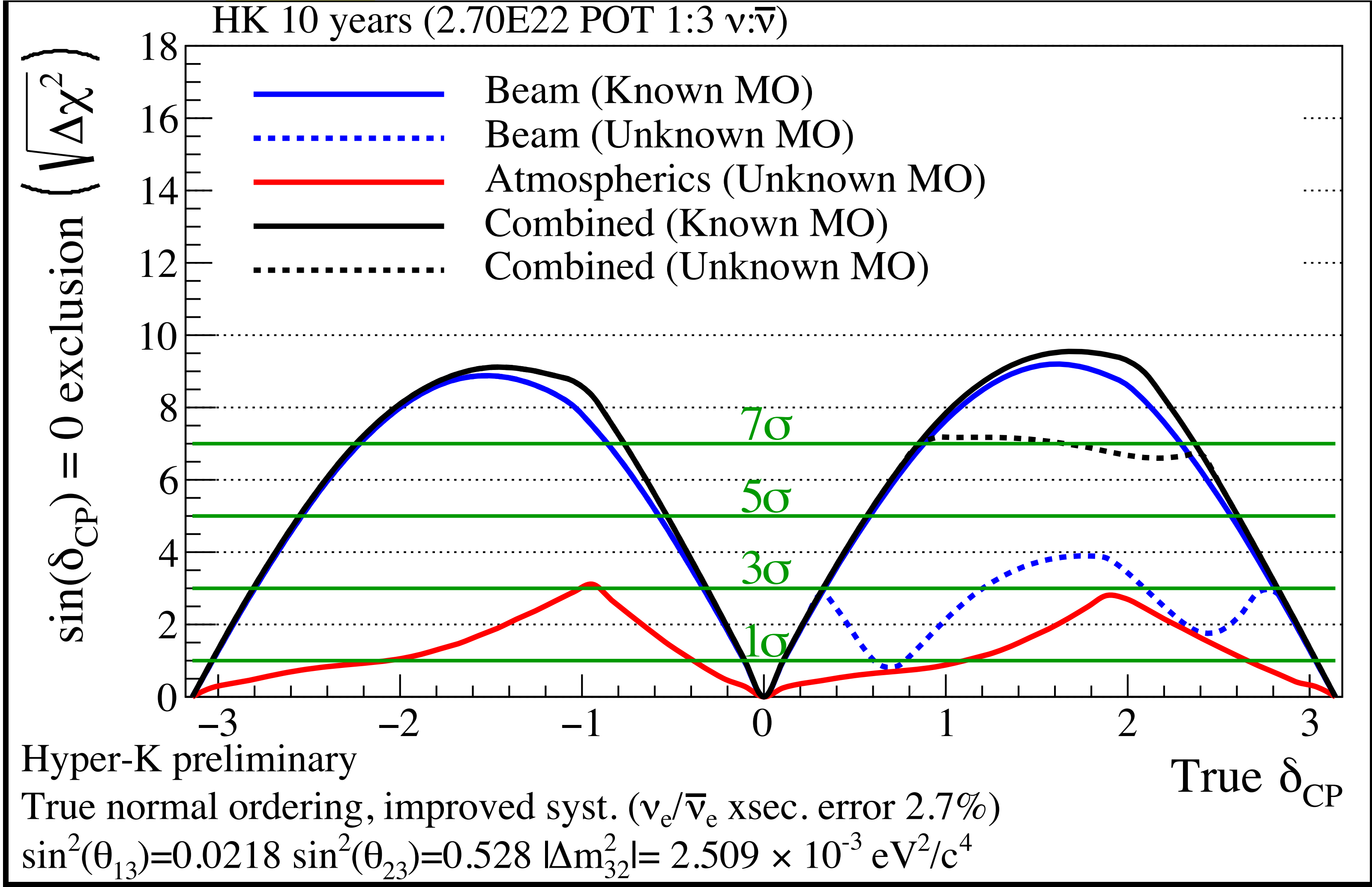
Neutrino



Anti-Neutrino

HK's ability to exclude the CP conserving case $\sin \delta_{\text{CP}} = 0$

Assumption: True Mass Ordering = Normal Ordering

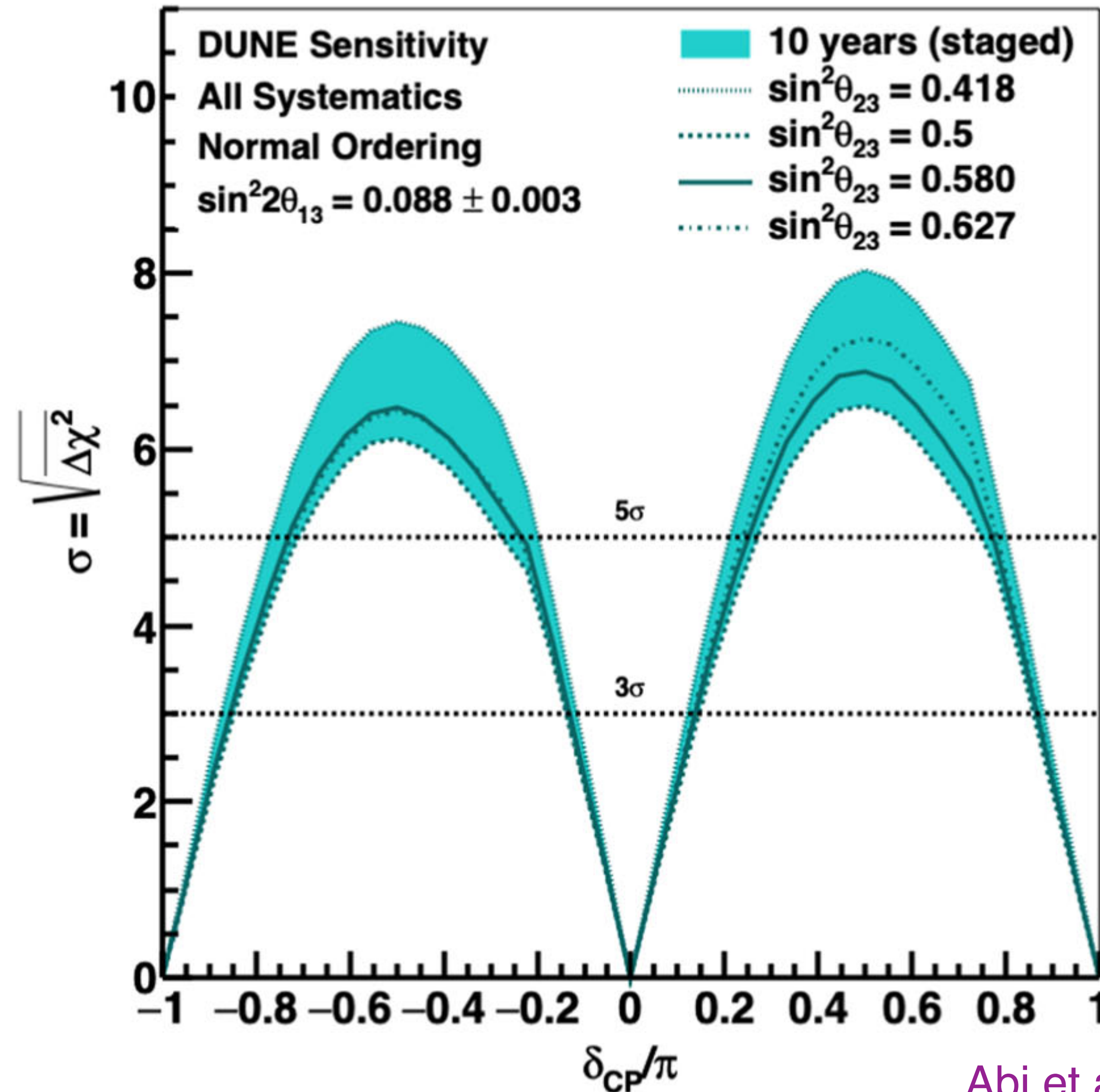


T2K+NOvA may reach at most $\sim 3\sigma$ for some values of CP phase

↓

Significant Improvement

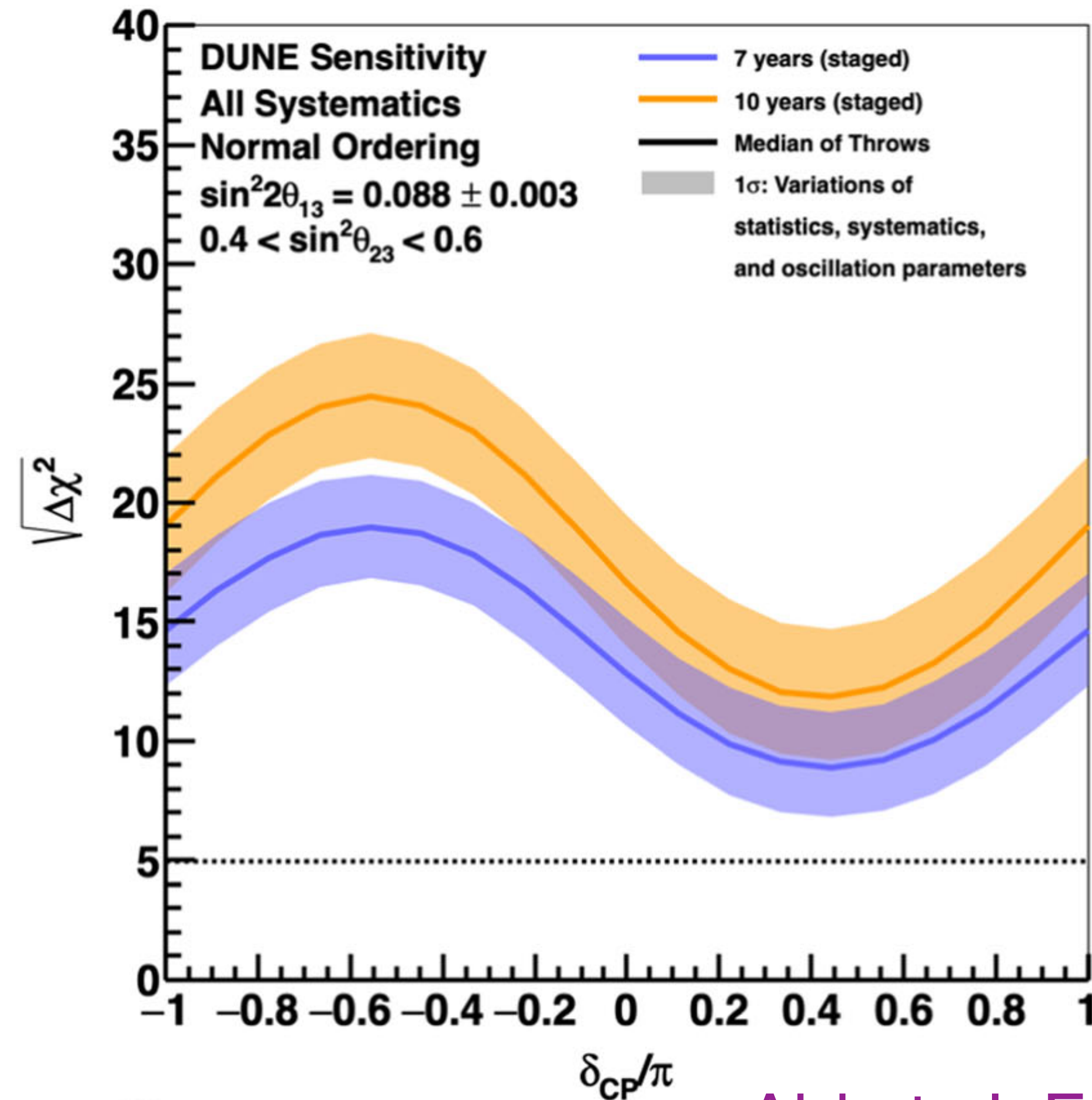
DUNE's ability to exclude the CP conserving case $\sin \delta_{\text{CP}} = 0$



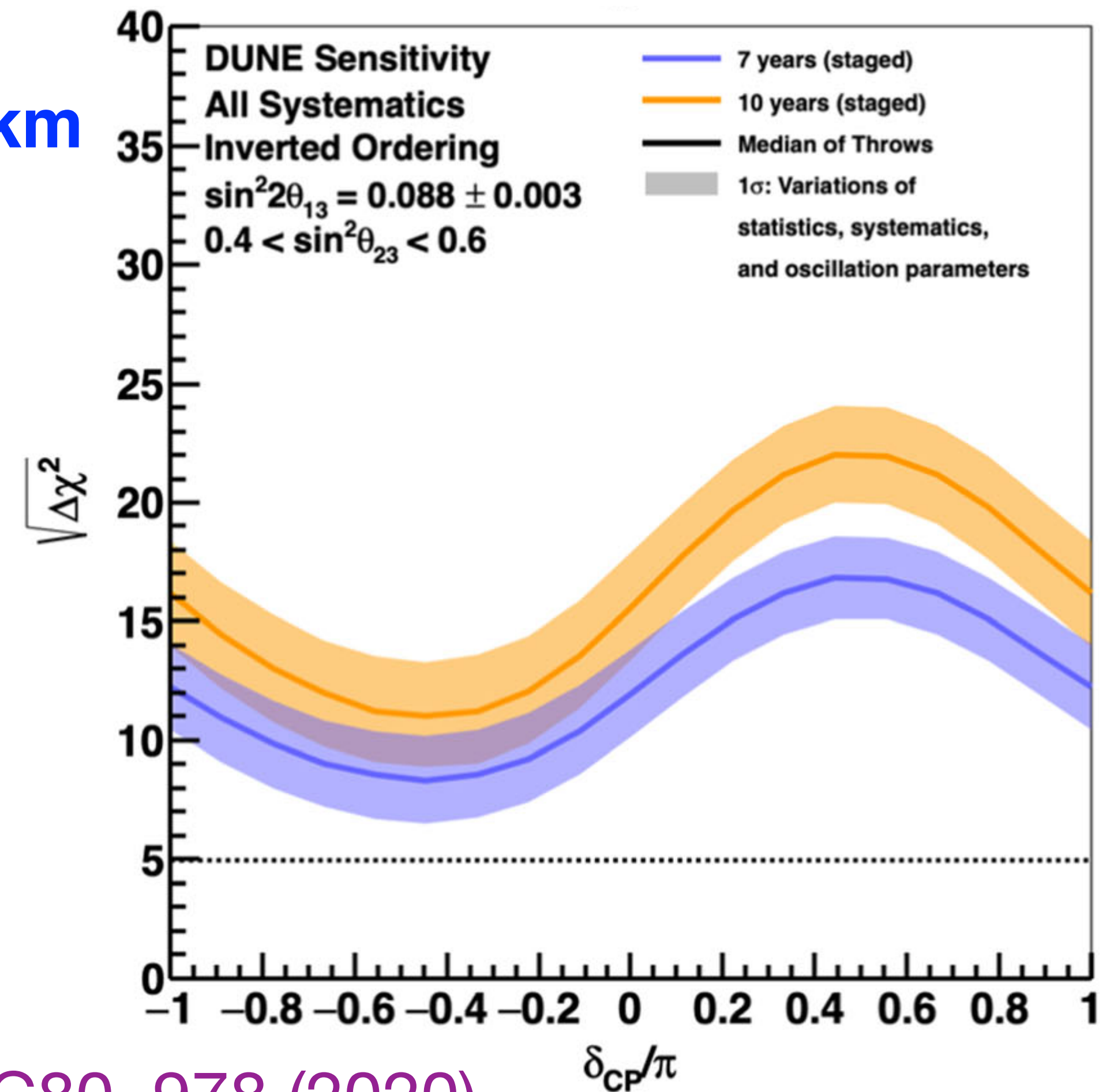
Abi et al, Eur. Phys. J. C.80, 978 (2020)

Determination Neutrino Mass Ordering by Long-Baseline Neutrino Oscillation Experiments

HK LBL is not powerful, but DUNE LBL is quite powerful to determine MO thanks to the larger matter effect due to longer baseline!



L ~ 1300 km



Abi et al, Eur. Phys. J. C80, 978 (2020)

DUNE alone can determine MO at more than 5 σ !

Test of New Physics by Long-Baseline Neutrino Oscillation Experiments

**New Physics = neutrino property beyond the
standard framework of 3 massive neutrinos**

**For some New Physics effects which can be studied in
coherent neutrino-nucleus elastic scattering,
see the talk by Diego Aristizábal (Friday) !**

Effect of New Physics is not expected to be so large

Current Situation: Apart from some experimental data (such as LNSD), almost all the data can be explained quite well by neutrino oscillations (induced by masses and mixing) in the standard 3 flavor framework.

In general, if there is some new physics effect, such effect should not be so large or should be subdominant

More precision is needed!

Examples of “New Physics” effect which can manifest in LBL neutrino oscillations

NSI (Non-standard Interactions) of neutrinos

Presense of extra (sterile) neutrino

Decay of neutrinos due to New Physics

Violation of unitarity, or non-unitarity

Decoherence effect

Lorentz Violation, and so on

Examples of “New Physics” effect which can manifest in LBL neutrino oscillations

NSI (Non-standard Interactions) of neutrinos

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Decay of neutrinos due to New Physics

Violation of unitarity, or non-unitarity

Decoherence effect

Lorentz Violation, and so on

Phenomenological Approache

In most cases, New Physics (NP) effects can be manifested or parameterized by some effective NP parameters, in model independent (or less model dependent) way, which allows us to take phenomenological approache without explicitly considering some specific models

In this presentation, I will follow this approach, focusing on phenomenological aspects/consequences

Test for NSI (Non-Standard Interactions) of neutrinos with matter in long baseline oscillation experiments

Non-Standard Interactions (NSI) of Neutrinos

NSI can be generally described by

$$\mathcal{L}_{\text{NSI, CC}} = -2\sqrt{2}G_F \sum_{f,f',\alpha,\beta} \varepsilon_{\alpha\beta}^{ff',P} (\bar{\ell}_{\alpha} \gamma_{\mu} P_L \nu_{\beta}) (\bar{f} \gamma^{\mu} P f') + \text{h.c.} \quad : \text{CC NSI} \quad \text{Strongly contained by meson/muon decays}$$

$$\mathcal{L}_{\text{NSI, NC}} = -2\sqrt{2}G_F \sum_{f,P,\alpha,\beta} \varepsilon_{\alpha\beta}^{f,P} (\bar{\ell}_{\alpha} \gamma_{\mu} P_L \nu_{\beta}) (\bar{f} \gamma^{\mu} P f) + \text{h.c.} \quad : \text{NC NSI}$$

where $\alpha, \beta = e, \mu, \tau$, $f, f' = \text{SM charged fermions}$, $\ell = \text{SM charged leptons}$

$$\varepsilon_{\alpha\beta}^{f,V} \equiv \varepsilon_{\alpha\beta}^{f,L} + \varepsilon_{\alpha\beta}^{f,R}, \quad \varepsilon_{\alpha\beta}^{f,A} \equiv \varepsilon_{\alpha\beta}^{f,L} - \varepsilon_{\alpha\beta}^{f,R} \quad (\text{vector and axial NSI coefficients})$$

we define the effective NSI parameters as

$$\varepsilon_{\alpha\beta} \equiv \sum_{f=e,u,d} \varepsilon_{\alpha\beta}^f \frac{N_f}{N_e} = \sum_{f=e,u,d} (\varepsilon_{\alpha\beta}^{fL} + \varepsilon_{\alpha\beta}^{fR}) \frac{N_f}{N_e} \simeq \varepsilon_{\alpha\beta}^e + 3\varepsilon_{\alpha\beta}^u + 3\varepsilon_{\alpha\beta}^d \quad \text{for Earth matter}$$

Neutrino Evolution Equation in Matter **with NSI effect**

$$i \frac{d}{dx} \begin{bmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{bmatrix} = H \begin{bmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{bmatrix}$$
$$H = U \begin{bmatrix} 0 & 0 & 0 \\ 0 & \frac{\Delta m_{21}^2}{2E} & 0 \\ 0 & 0 & \frac{\Delta m_{31}^2}{2E} \end{bmatrix} U^\dagger + \sqrt{2} G_F N_e \begin{bmatrix} 1 + \varepsilon_{ee} & \varepsilon_{e\mu} & \varepsilon_{e\tau} \\ \varepsilon_{\mu e}^* & \varepsilon_{\mu\mu} & \varepsilon_{\mu\tau} \\ \varepsilon_{\tau e}^* & \varepsilon_{\tau\mu}^* & \varepsilon_{\tau\tau} \end{bmatrix}$$

G_F : Fermi Constant

N_e : Electron number density

Neutrino Evolution Equation in Matter **with NSI effect**

$$i \frac{d}{dx} \begin{bmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{bmatrix} = H \begin{bmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{bmatrix}$$

Off diagonal elements, $\varepsilon_{\alpha\beta}$ ($\alpha \neq \beta$), can induce additional mixing(-like) effects
 $\text{Im}[\varepsilon_{\alpha\beta}]$ is a new source of CP violation

$$H = U \begin{bmatrix} 0 & 0 & 0 \\ 0 & \frac{\Delta m_{21}^2}{2E} & 0 \\ 0 & 0 & \frac{\Delta m_{31}^2}{2E} \end{bmatrix} U^\dagger + \sqrt{2} G_F N_e \begin{bmatrix} 1 + \varepsilon_{ee} & \varepsilon_{e\mu} & \varepsilon_{e\tau} \\ \varepsilon_{\mu e}^* & \varepsilon_{\mu\mu} & \varepsilon_{\mu\tau} \\ \varepsilon_{\tau e}^* & \varepsilon_{\tau\mu}^* & \varepsilon_{\tau\tau} \end{bmatrix}$$

G_F : Fermi Constant

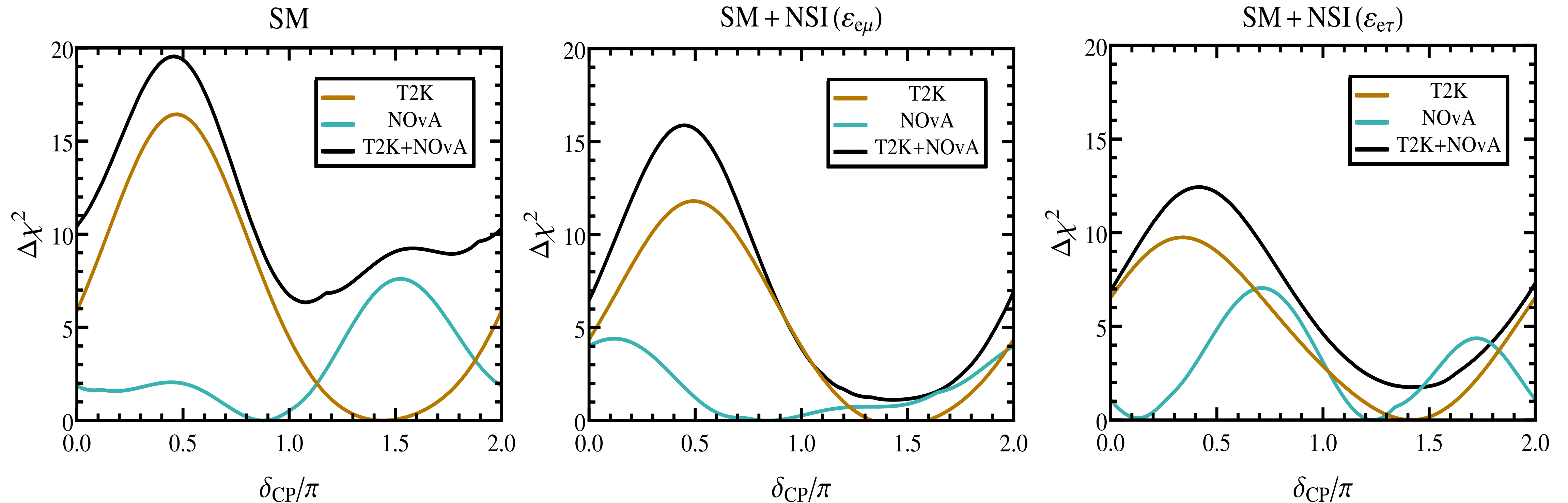
N_e : Electron number density

Diagonal elements, $\varepsilon_{\alpha\alpha}$, can induce new potential and modify the resonance condition

Some indication (hint) of NSI?

For Normal Ordering, T2K and NOvA results are in some tension with each other which could be alleviated if we include NSI effect

some tension (mismatch) of preferred value of CP phase between T2K and NOvA

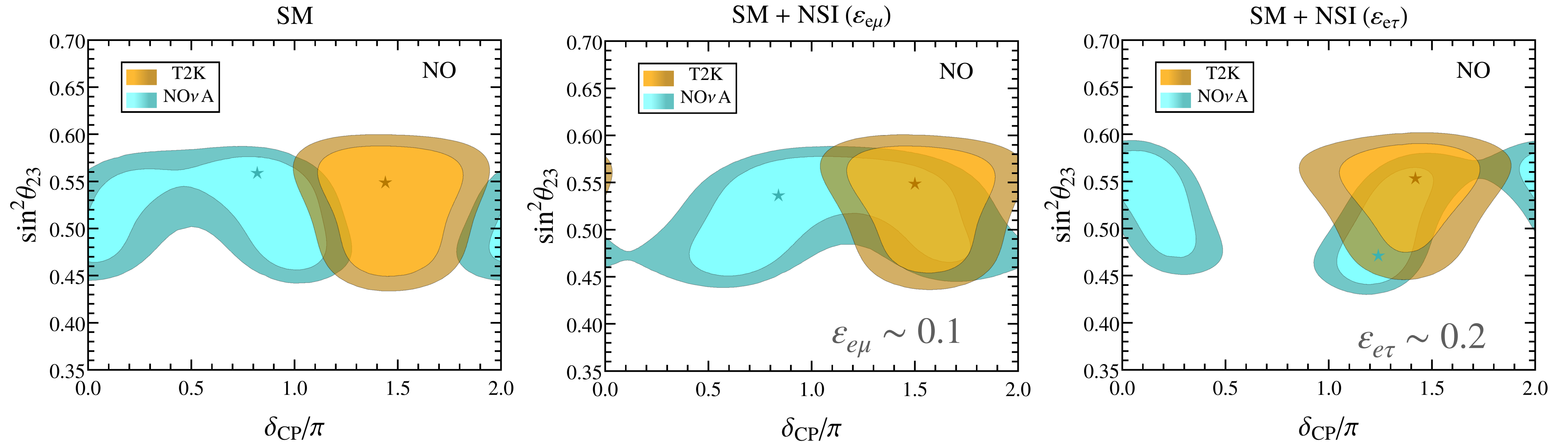


S. S. Chatterjee and A. Palazzo, arXiv:2409.10599 [hep-ph]

Some indication (hint) of NSI?

For Normal Ordering, T2K and NOvA results are in some tension with each other which could be alleviated if we include NSI effect

Including NSI, T2K and NOvA data indicate the similar values of CP phase

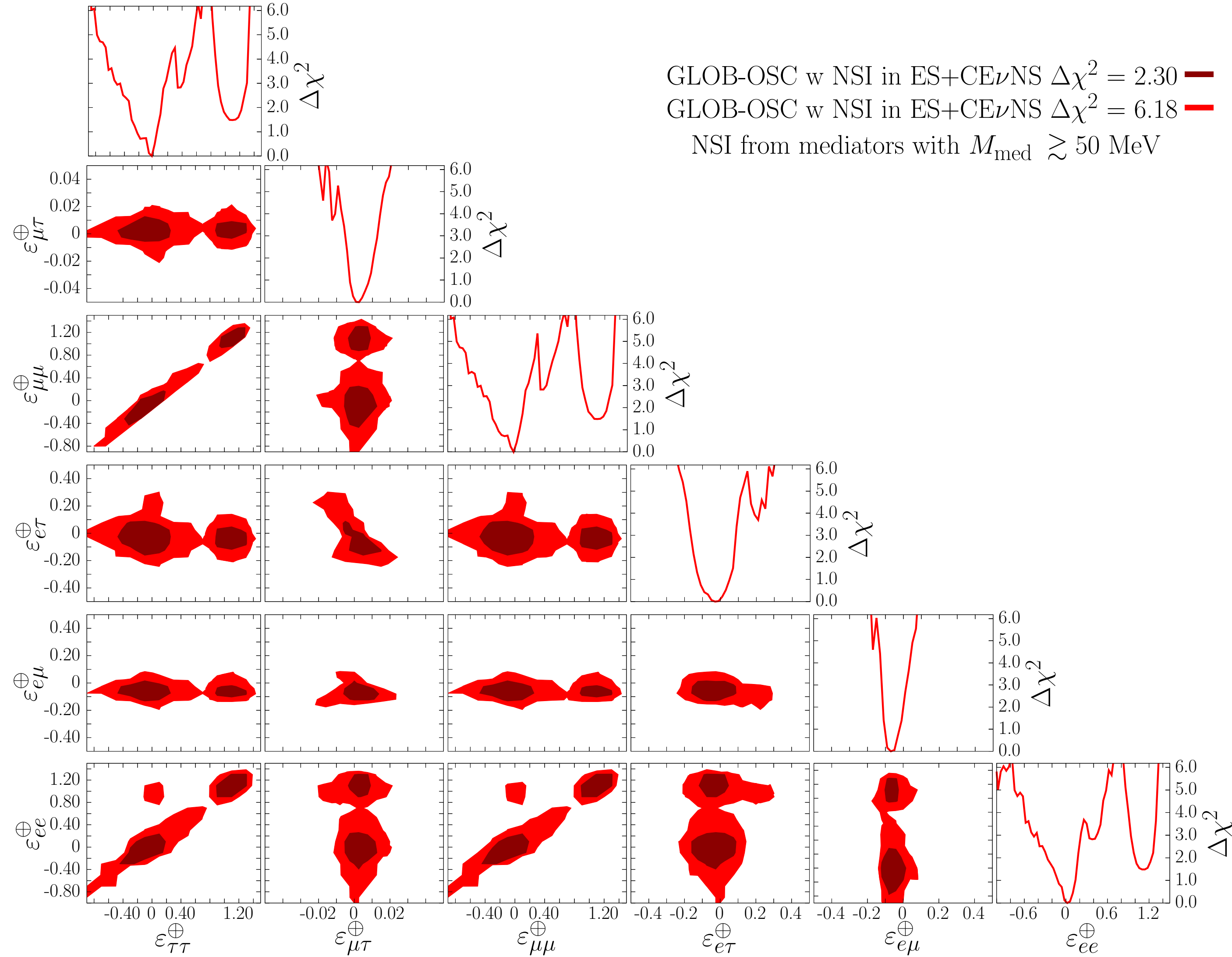


non-zero NSI is favored at $\sim 2\sigma$

S. S. Chatterjee and A. Palazzo, arXiv:2409.10599 [hep-ph]

See also Denton et al, PRL126, 051801 (2021) [arXiv: 2008.01110 [hep-ph]]

Current Bounds on the effective NSI in Earth Matter relevant for LBL experiments



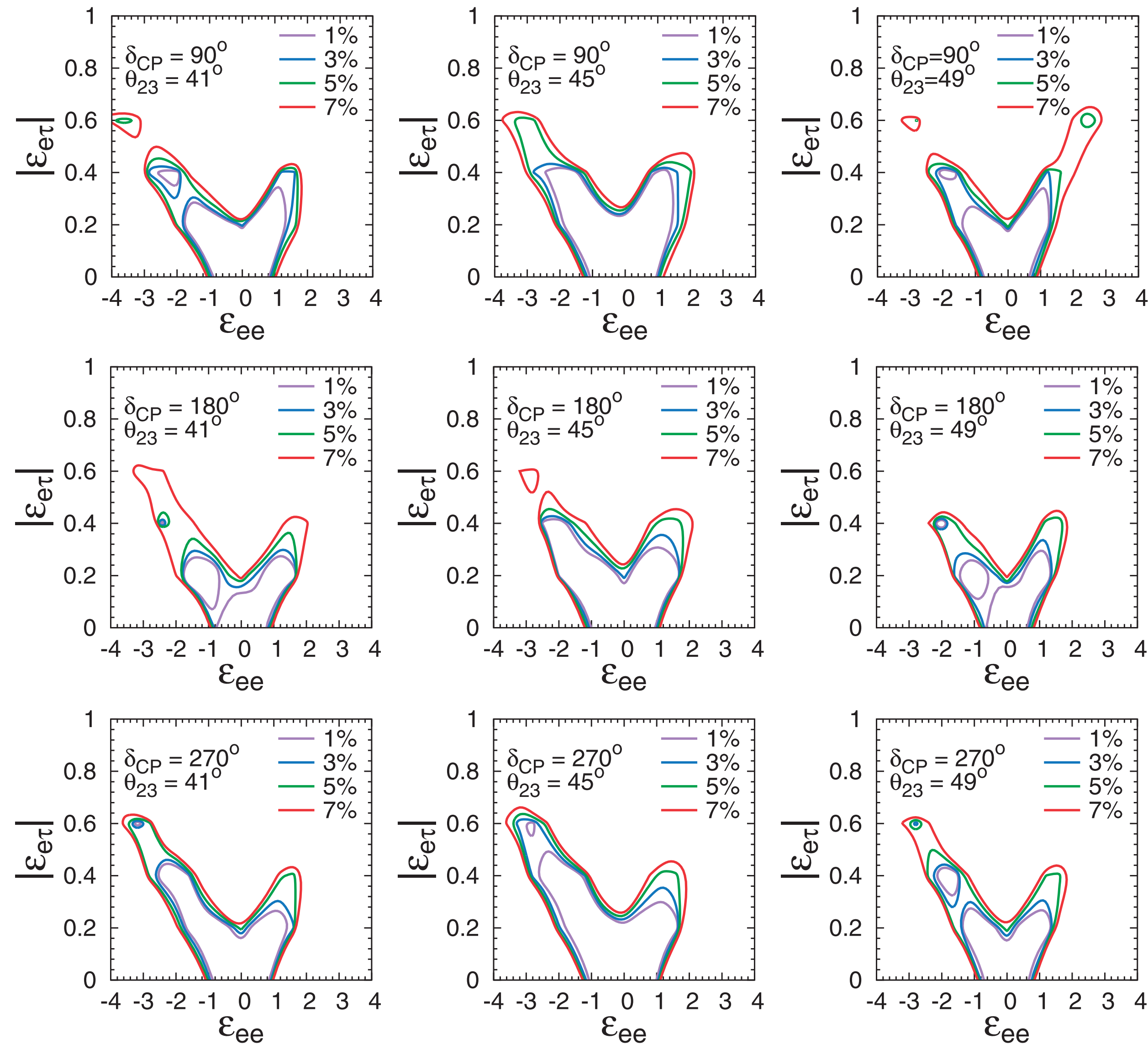
Coloma et al, JHEP08, 032 (2023) [arXiv:2305.07698 [hep-ph]]

Current Bounds on the effective NSI in Earth Matter relevant for LBL experiments

Allowed ranges at $\begin{smallmatrix} 90\% \text{ CL} \\ (99\% \text{ CL}) \end{smallmatrix}$ marginalized			
GLOB-OSC w/o NSI in ES		GLOB-OSC w NSI in ES + CE ν NS	
$\varepsilon_{ee}^{\oplus} - \varepsilon_{\mu\mu}^{\oplus}$	$[-3.1, -2.8] \oplus [-2.1, -1.88] \oplus [-0.15, +0.17]$ $([-4.8, -1.6] \oplus [-0.40, +2.6])$	$\varepsilon_{ee}^{\oplus}$	$[-0.19, +0.20] \oplus [+0.95, +1.3]$ $([-0.23, +0.25] \oplus [+0.81, +1.3])$
$\varepsilon_{\tau\tau}^{\oplus} - \varepsilon_{\mu\mu}^{\oplus}$	$[-0.0215, +0.0122]$ $([-0.075, +0.080])$	$\varepsilon_{\mu\mu}^{\oplus}$	$[-0.43, +0.14] \oplus [+0.91, +1.3]$ $([-0.29, +0.20] \oplus [+0.83, +1.4])$
$\varepsilon_{e\mu}^{\oplus}$	$[-0.11, -0.021] \oplus [+0.045, +0.135]$ $([-0.32, +0.40])$	$\varepsilon_{\tau\tau}^{\oplus}$	$[-0.43, +0.14] \oplus [+0.91, +1.3]$ $([-0.29, +0.20] \oplus [+0.83, +1.4])$
$\varepsilon_{\mu\tau}^{\oplus}$	$[-0.22, +0.088]$ $([-0.49, +0.45])$	$\varepsilon_{e\mu}^{\oplus}$	$[-0.12, +0.011]$ $([-0.18, +0.08])$
$\varepsilon_{\mu\tau}^{\oplus}$	$[-0.0063, +0.013]$ $([-0.043, +0.039])$	$\varepsilon_{e\tau}^{\oplus}$	$[-0.16, +0.083]$ $([-0.25, +0.33])$
		$\varepsilon_{\mu\tau}^{\oplus}$	$[-0.0047, +0.012]$ $([-0.020, +0.021])$

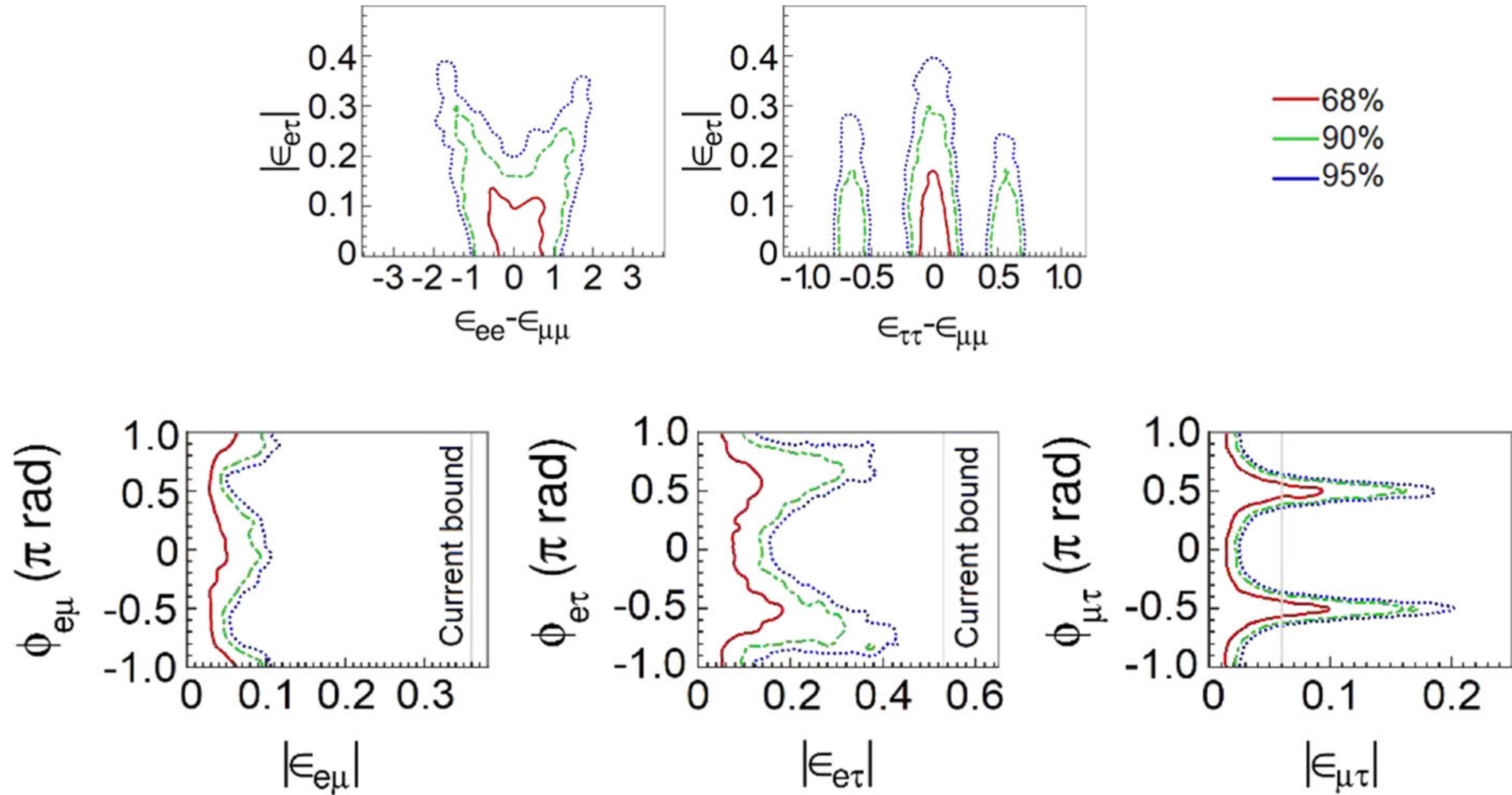
Coloma et al, JHEP08, 032 (2023) [arXiv:2305.07698 [hep-ph]]

Expected sensitivity to constrain NSI by Hyper-K + another detector at Korea



Abe et al, PTEP 2018, 063C01 [arXiv:1611.06118 [hep-ex]]

Expected sensitivity to constrain NSI by DUNE



Abi et al (DUNE Collab.), Eur. Phys. J. C81, 322 (2021) [arXiv:2008.12769 [hep-ex]]

Some remarks for NSI in LBL experiments

To enhance sensitivities to NSI, synergy among different experiments, Hyper-K, DUNE, JUNO, solar, atmospheric neutrinos, etc, would be important

If the hint for non-zero NSI implied by T2K+NOvA results is true, with much larger statistics, Hyper-K and DUNE are expected to confirm (or exclude) such a scenario

Interesting difference between Hyper-K and DUNE
Hyper-K: small matter (NSI) effect ($L = 295\text{km}$)
DUNE: larger matter (NSI) effect ($L = 1285\text{ km}$)

Test for sterile neutrinos in long baseline neutrino oscillation experiments

Neutrino Evolution Equation for 3+1 model

Let us consider so called 3+1 (3 active + 1 sterile neutrinos) model

$$i \frac{d}{dx} \begin{bmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \\ \nu_s \end{bmatrix} = (H_0 + V_m) \begin{bmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \\ \nu_s \end{bmatrix}$$

$$V_m = \begin{bmatrix} V_e + V_n & 0 & 0 & 0 \\ 0 & V_n & 0 & 0 \\ 0 & 0 & V_n & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

$$V_e \equiv \sqrt{2} G_F n_e, \quad V_n \equiv -\frac{\sqrt{2}}{2} G_F n_e,$$

$$H_0 = U_{3+1} \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & \frac{\Delta m_{21}^2}{2E} & 0 & 0 \\ 0 & 0 & \frac{\Delta m_{31}^2}{2E} & 0 \\ 0 & 0 & 0 & \frac{\Delta m_{41}^2}{2E} \end{bmatrix} U_{3+1}^\dagger$$

$$U_{3+1} \equiv R_{34}(\theta_{34}) R_{24}(\theta_{24}, \delta_{24}) R_{14}(\theta_{14}, \delta_{14}) R_{23}(\theta_{23}) R_{13}(\theta_{13}, \delta_{13}) R_{12}(\theta_{12})$$

What is the qualitative impact of sterile neutrino?

1) Further reduction of (active) neutrinos in the disappearance mode

$\nu_\mu \rightarrow \nu_\mu$ can occur or be induced through the mixing θ_{24}

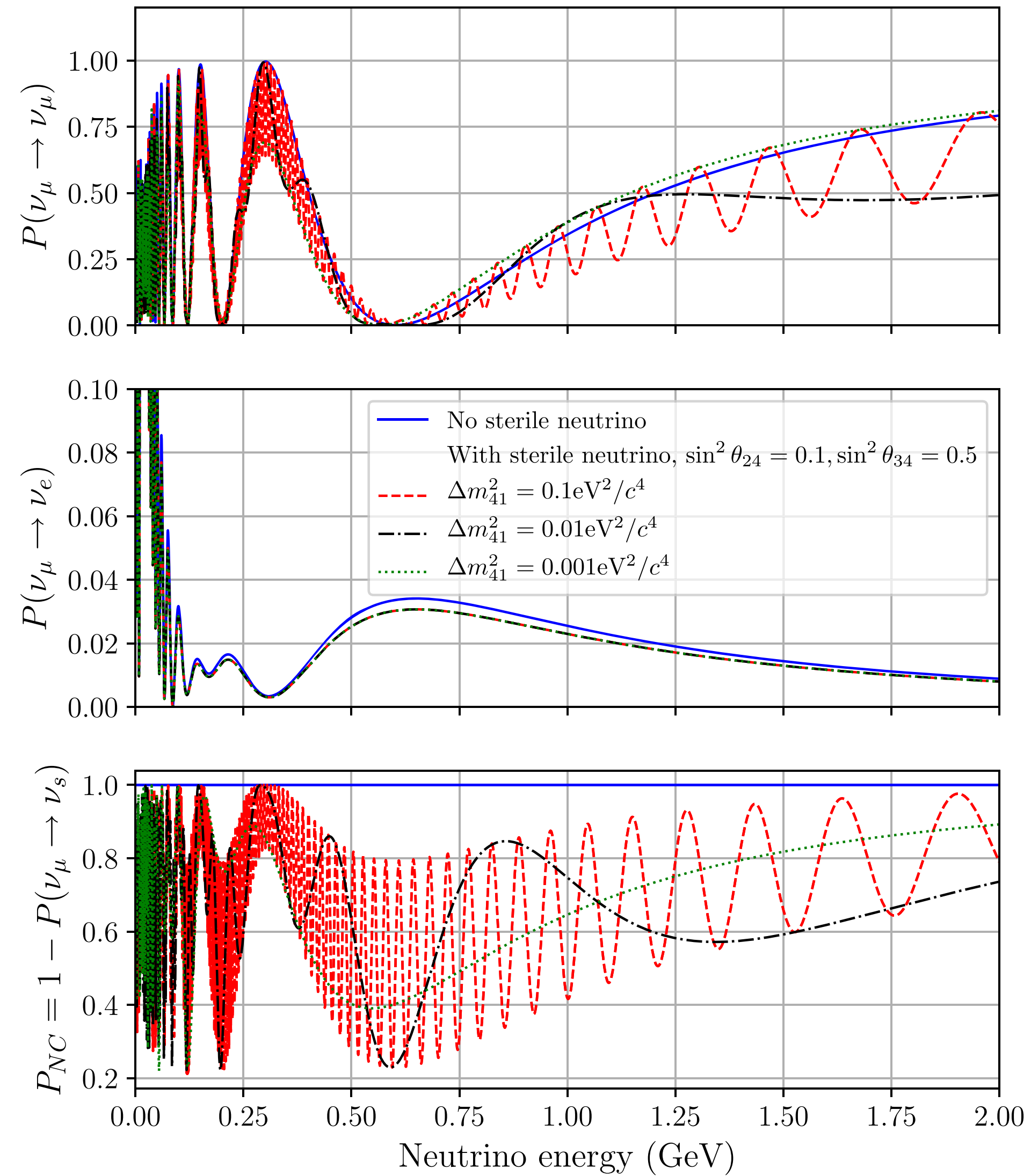
2) Additional (new) contribution in the appearance mode through the oscillation due to mixing and new mass eigenstate (mass squared differences)

$\nu_\mu \rightarrow \nu_e$ can occur or be induced through the simultaneous presence of mixing θ_{24} and θ_{14}

3) Reduction of NC (neutral current) induced events due to oscillation of active neutrinos into sterile ones

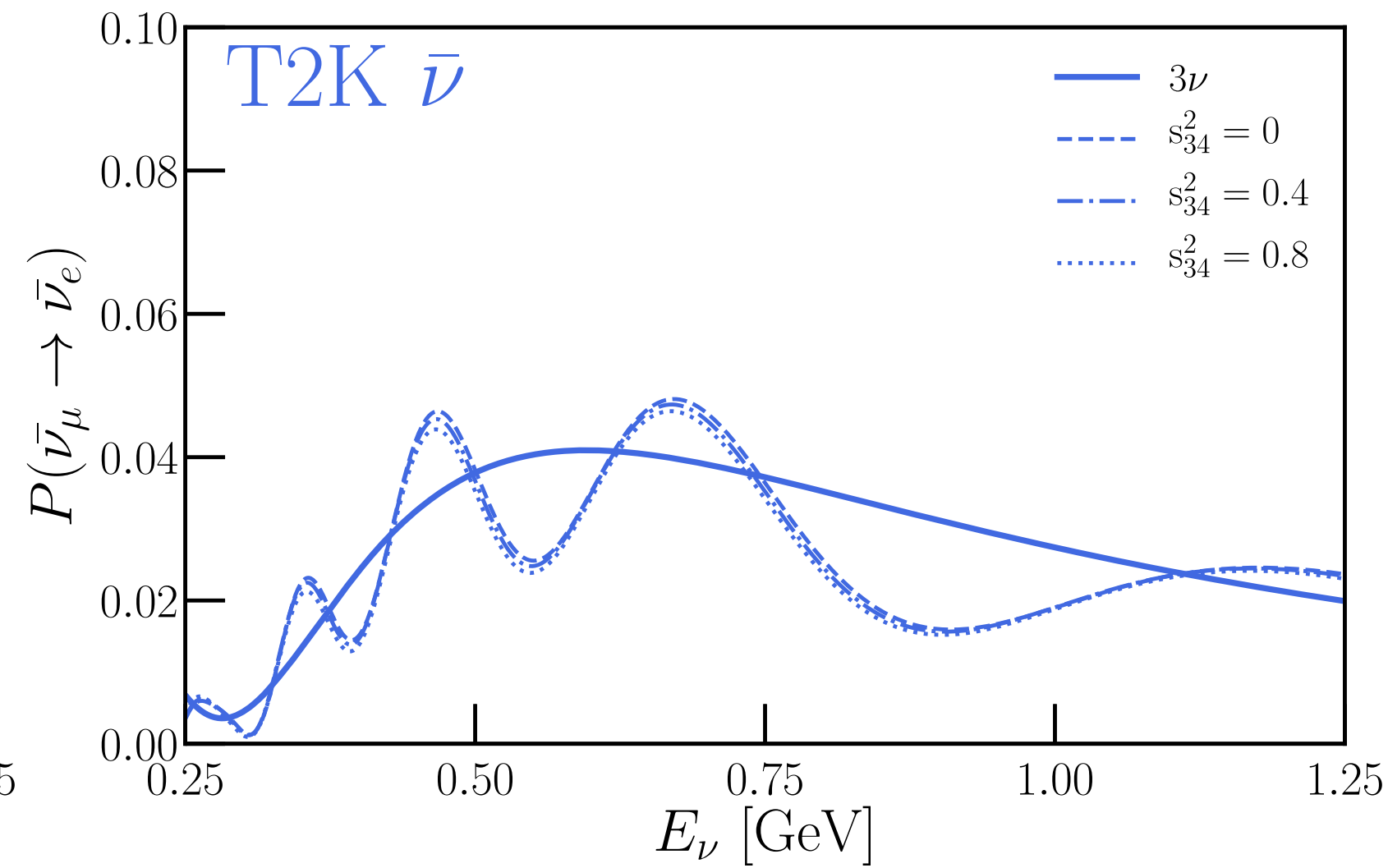
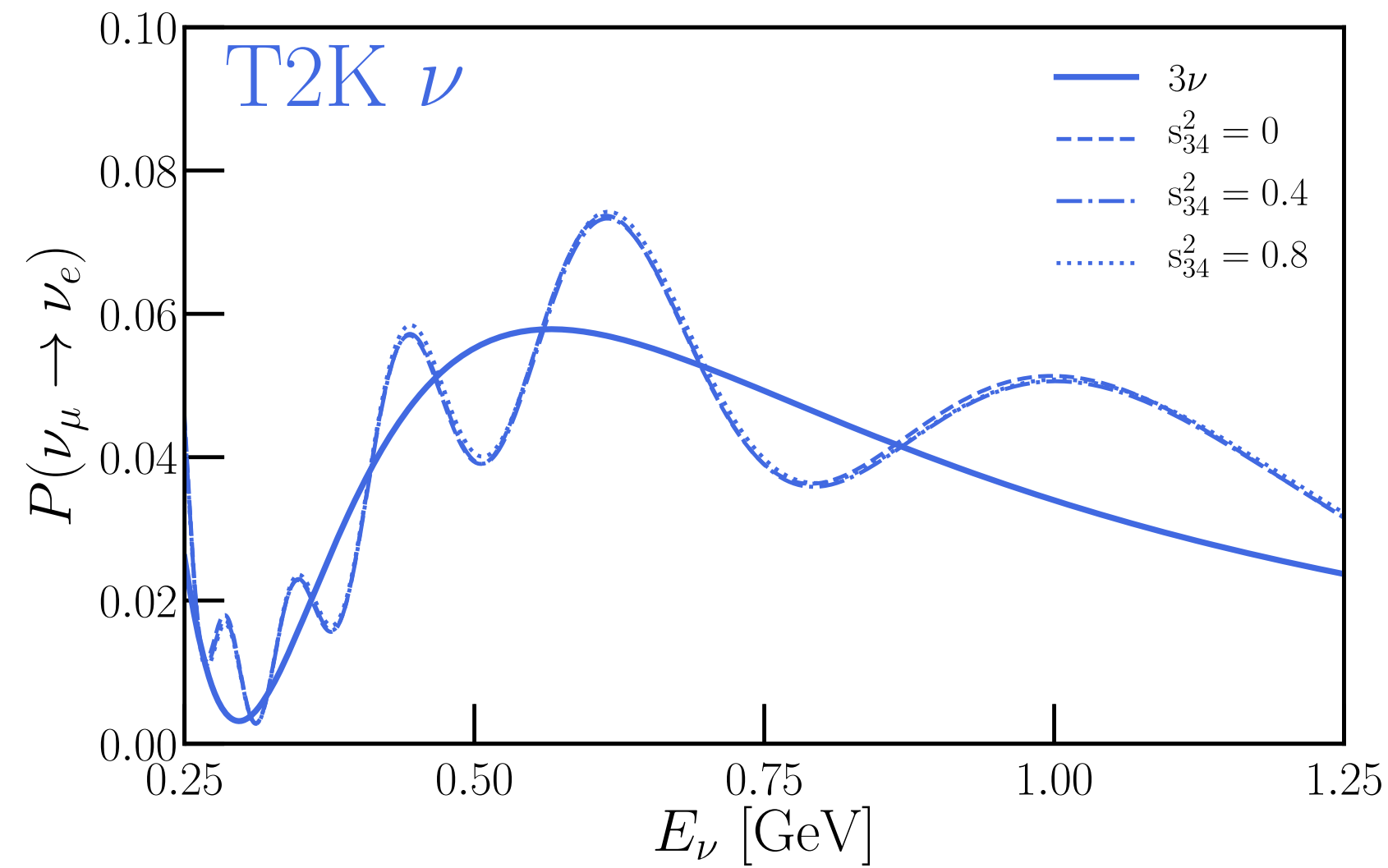
$\nu_\mu \rightarrow \nu_s$

Some example of oscillation probabilities in the 3+1 model for L = 295km (T2K/HK)



Abe et al (T2K Collab.), PRD99, 071103(R) (2019) [arXiv:1902.06529 [hep-ex]]

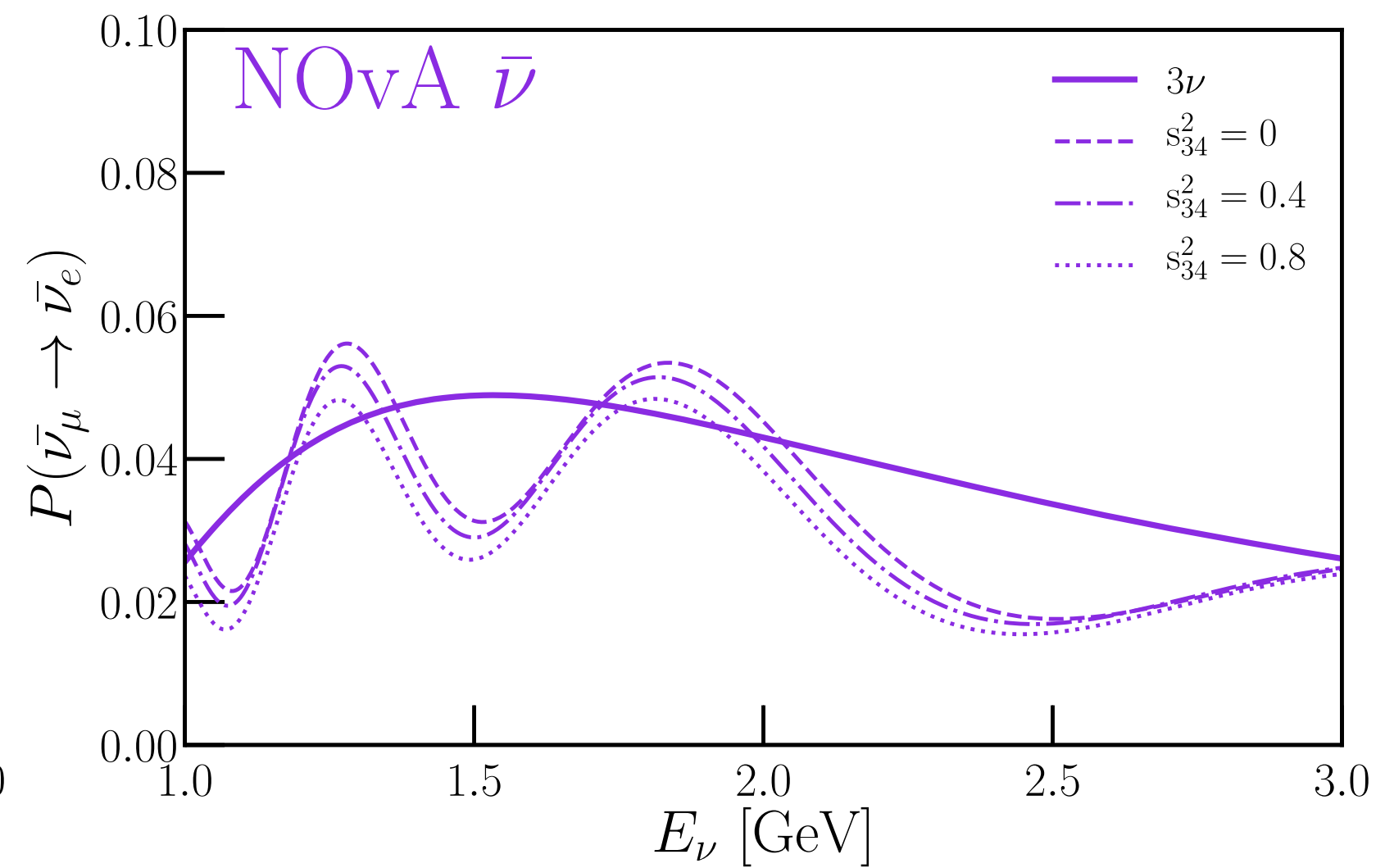
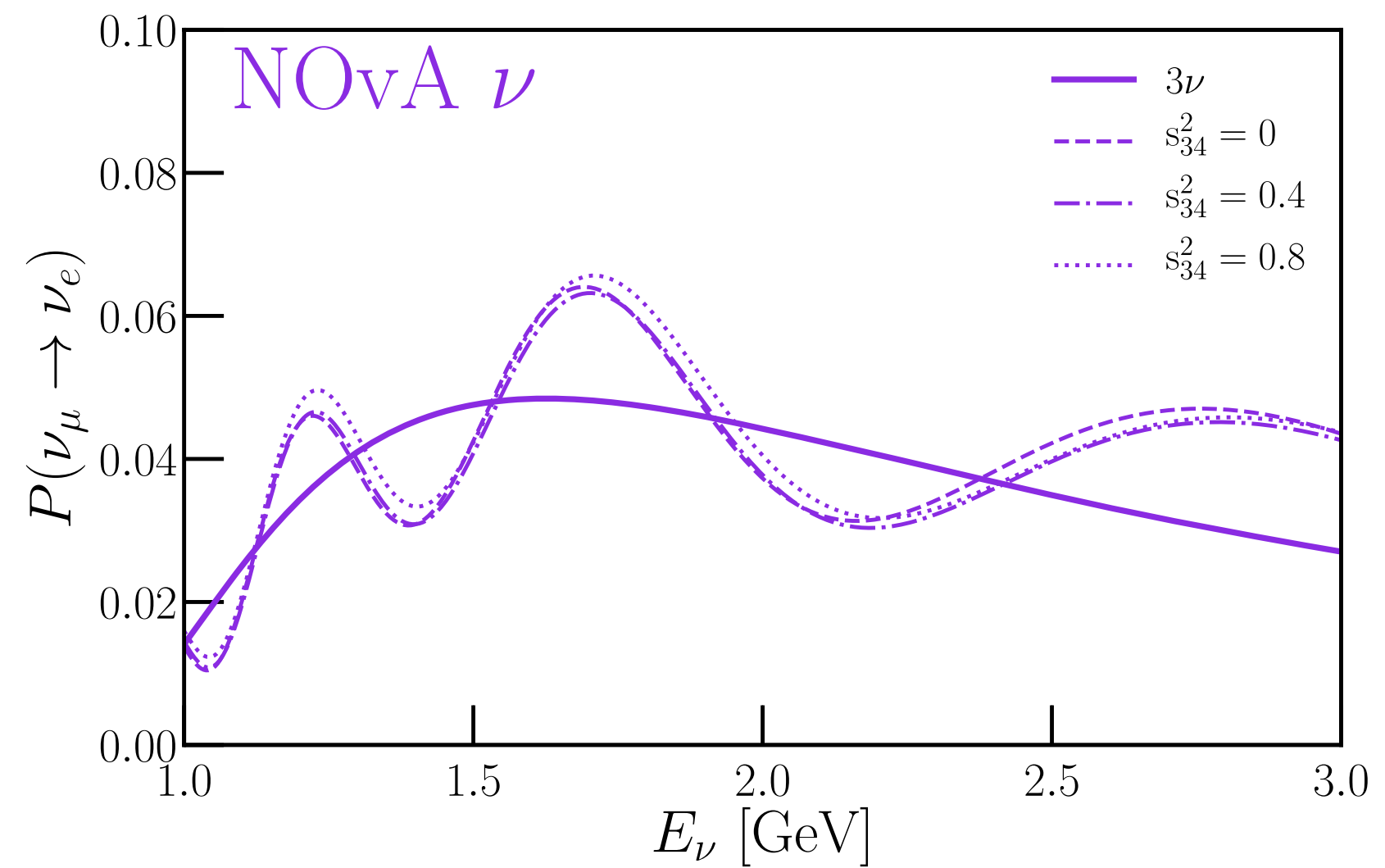
Some example of oscillation probabilities in the 3+1 model for L = 295/810 km for T2K/NOvA



For Inverted Mass Ordering

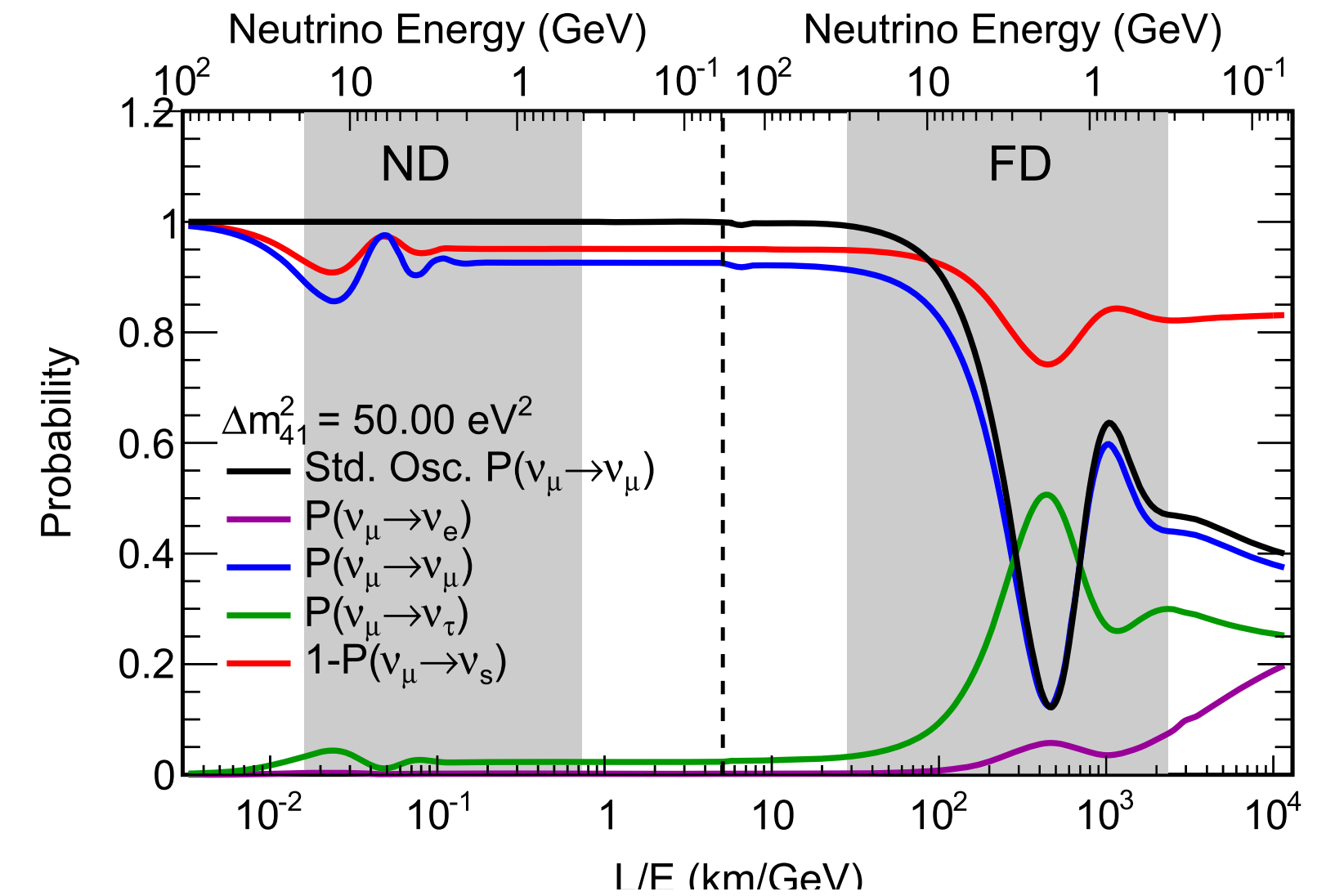
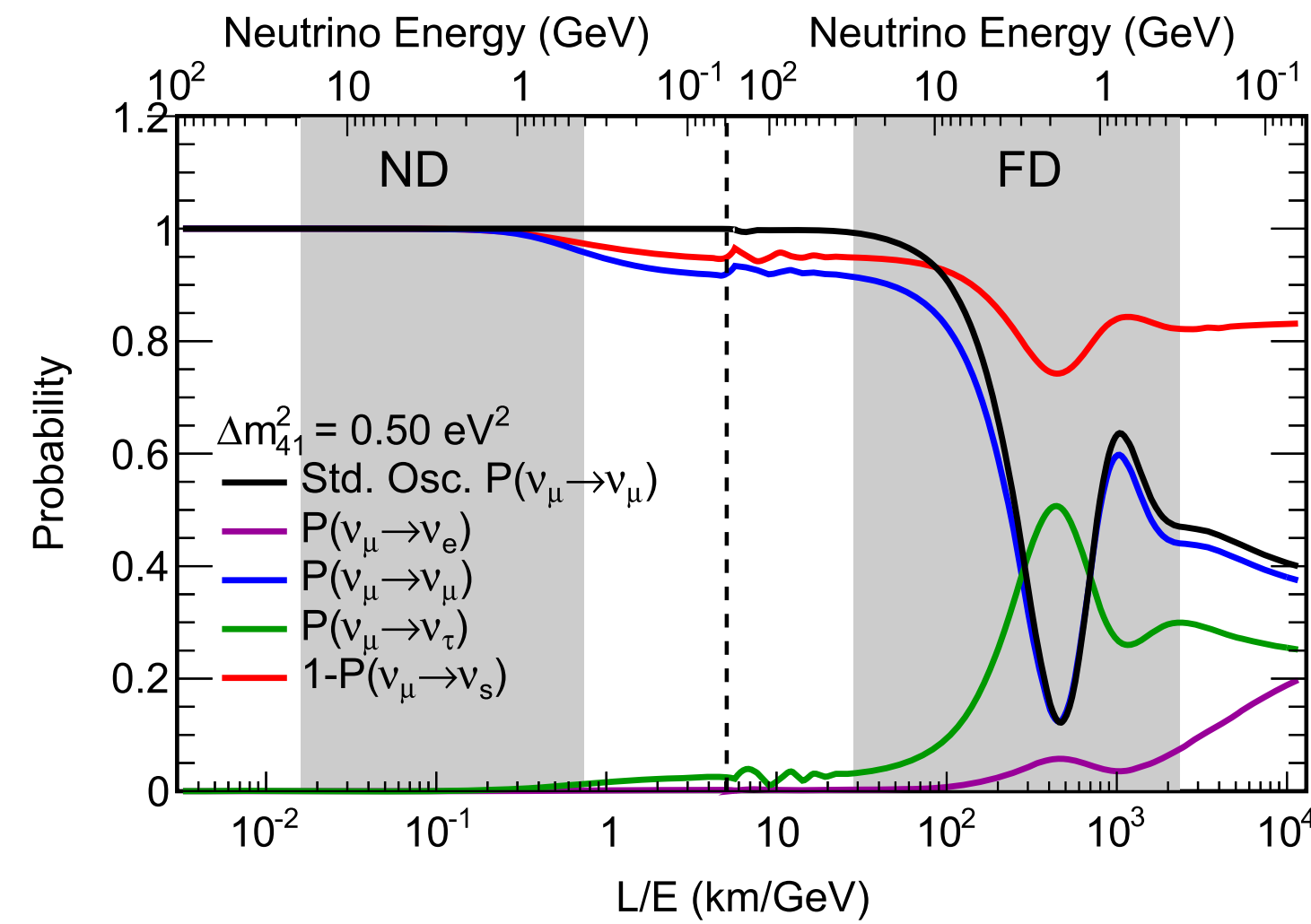
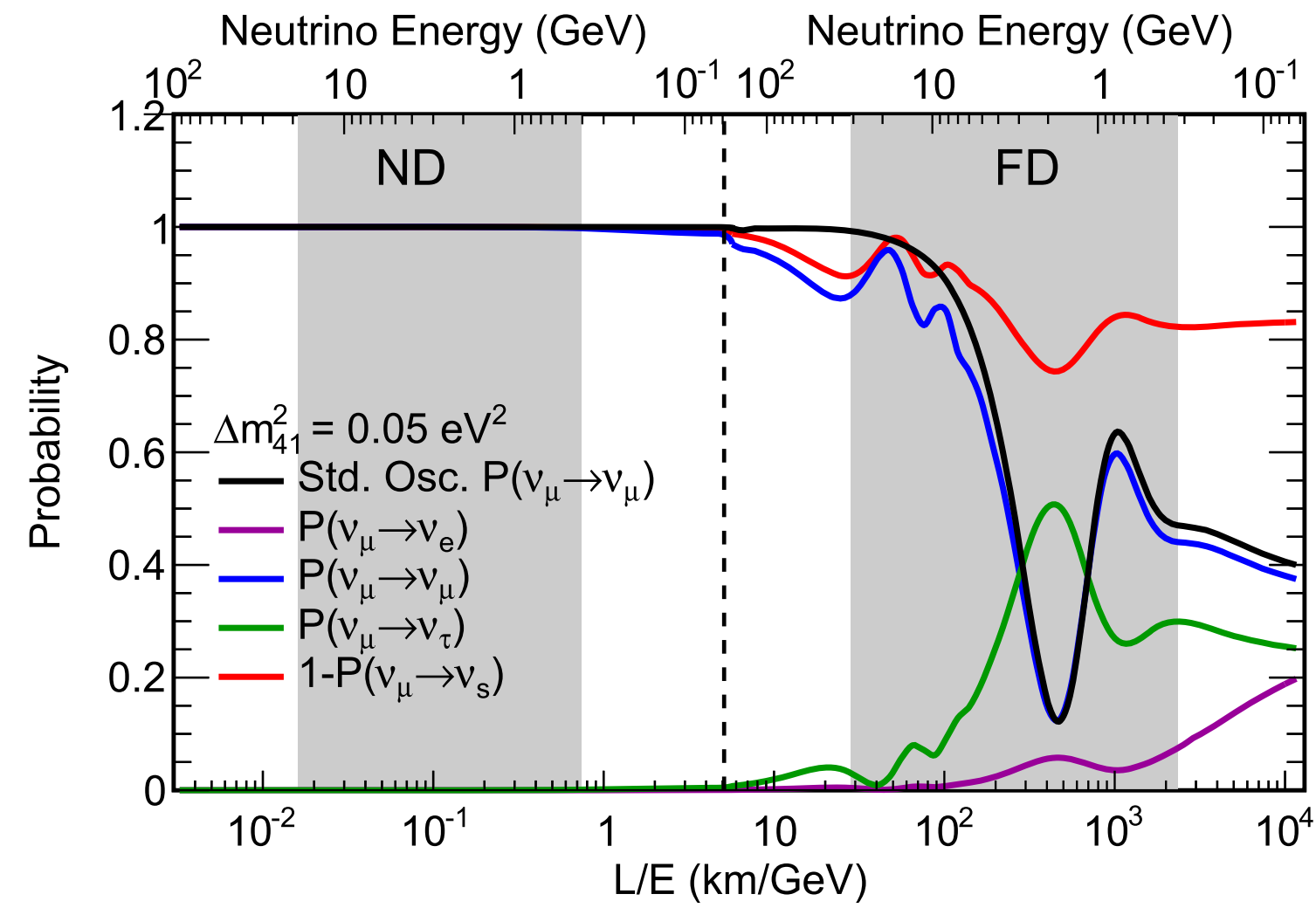
$$\Delta m_{31}^2 = -2.39 \times 10^{-3} \text{ eV}^2$$

$$\Delta m_{41}^2 = -0.011 \text{ eV}^2$$



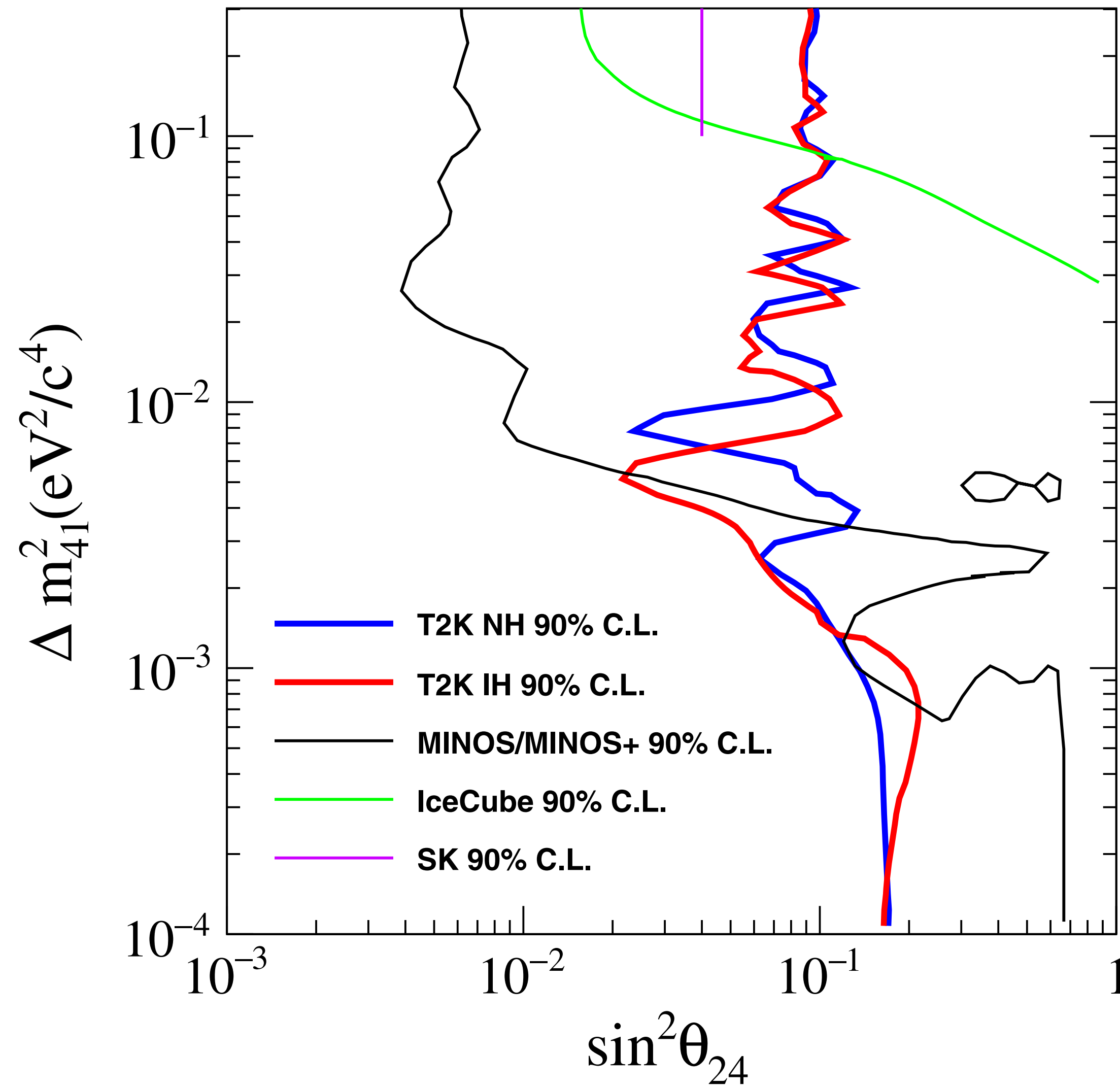
Gouvea, Sahches and Kelly, PRD 106, 055025 (2022) [arXiv:2204.09130 [hep-ph]]

Some example of oscillation probabilities in the 3+1 model for L = 1285km (DUNE)



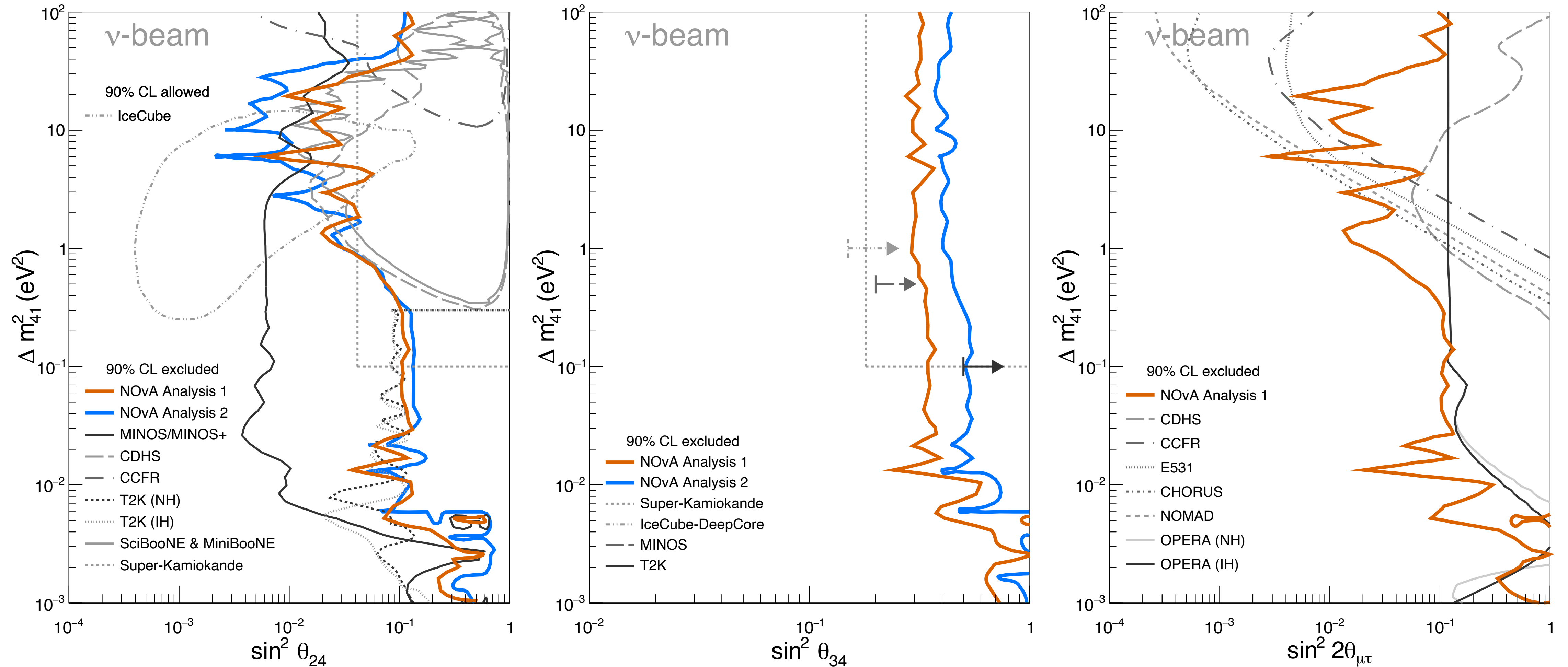
Abi et al (DUNE Collab.), Eur. Phys. J. C81, 322 (2021) [arXiv:2008.12769 [hep-ex]]

Current Bounds for light sterile neutrinos by T2K



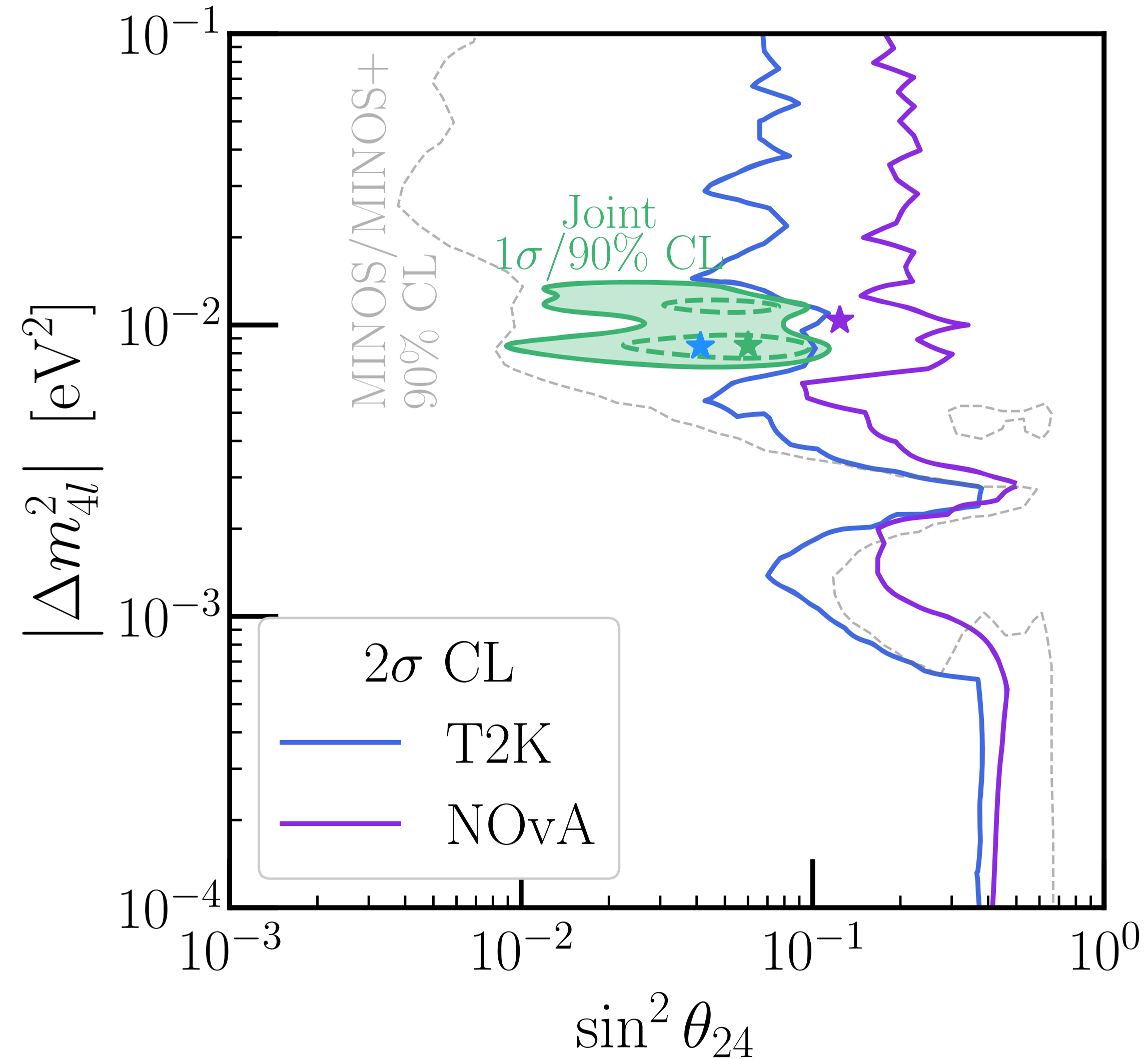
Abe et al (T2K Collab.), PRD99, 071103(R) (2019) [arXiv:1902.06529 [hep-ex]]

Current Bounds for light sterile neutrinos by NOvA



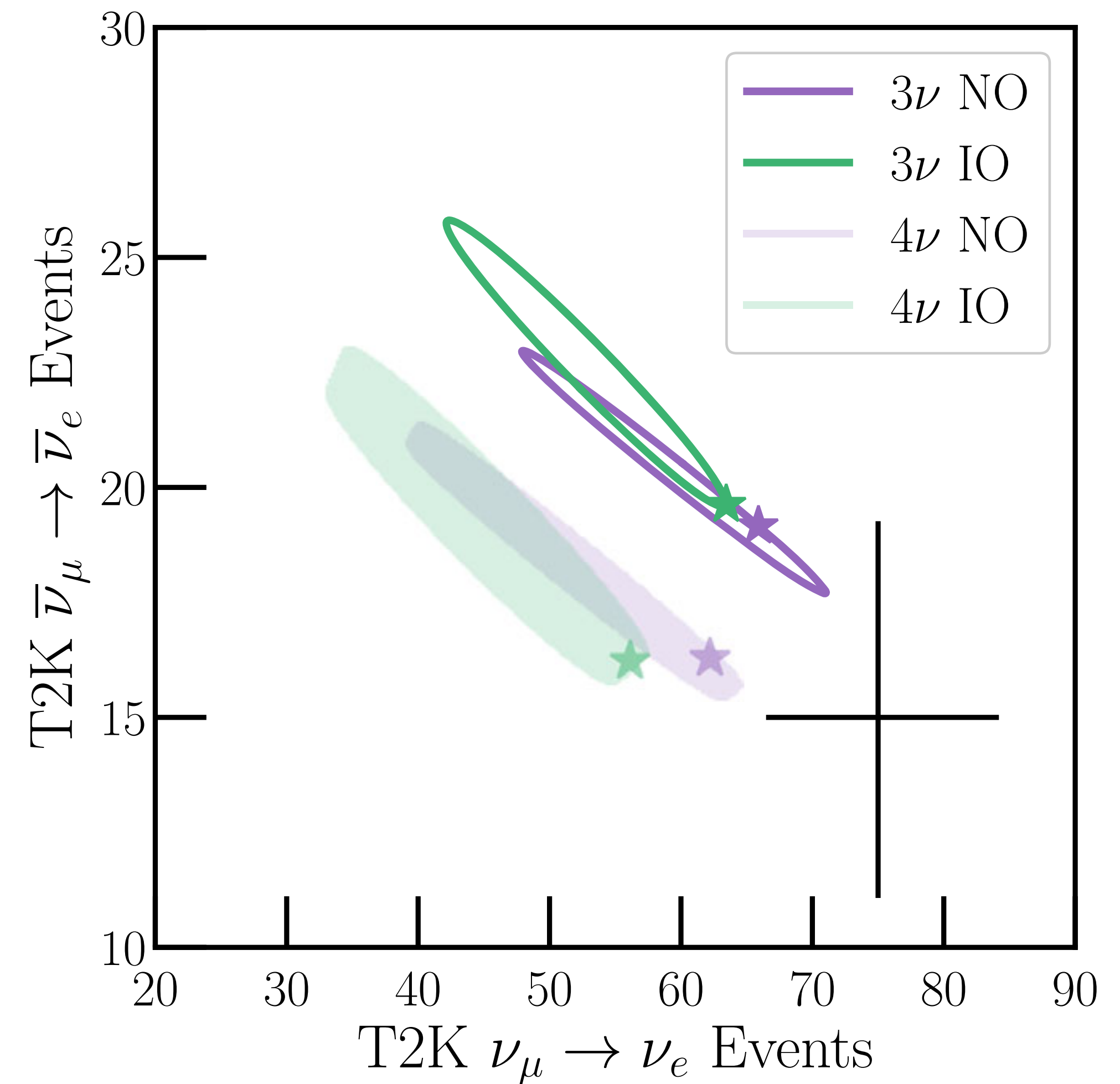
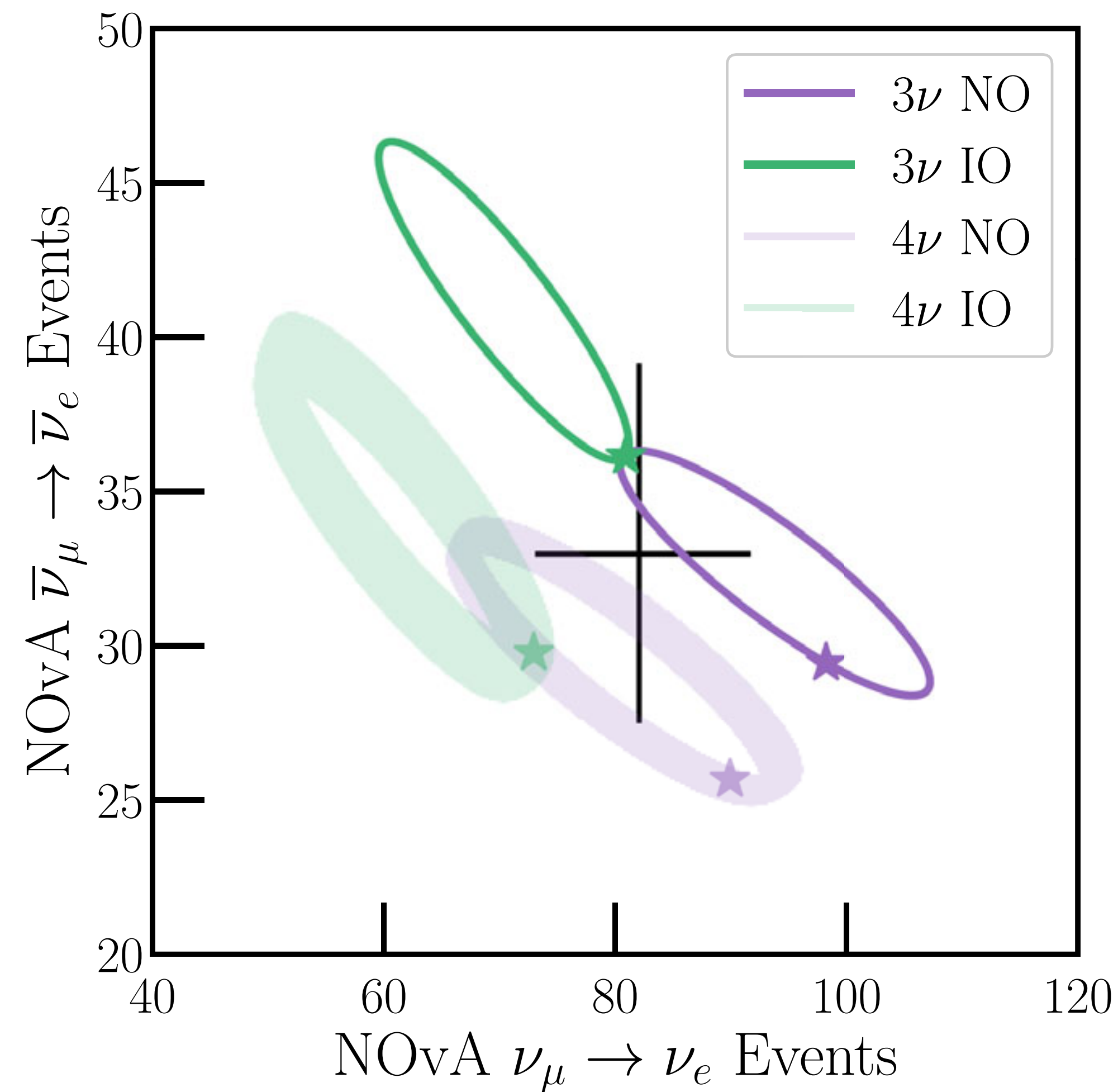
Acero et al (NOvA Collab.), arXiv:2409.04553 [hep-ex]

Light Sterile Neutrino favored by NOvA and T2K



Gouvea, Sahches and Kelly, PRD 106, 055025 (2022) [arXiv:2204.09130 [hep-ph]]

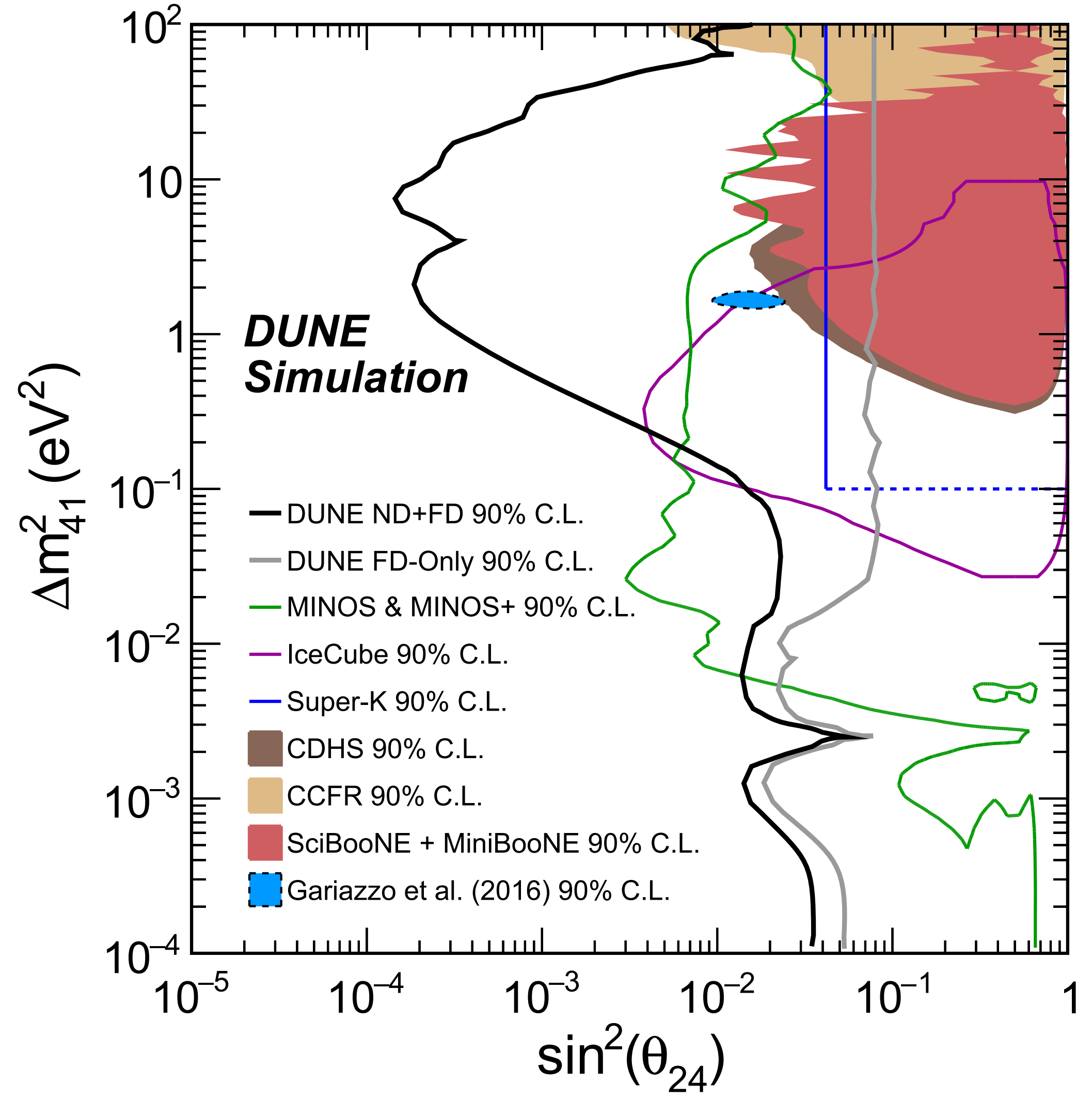
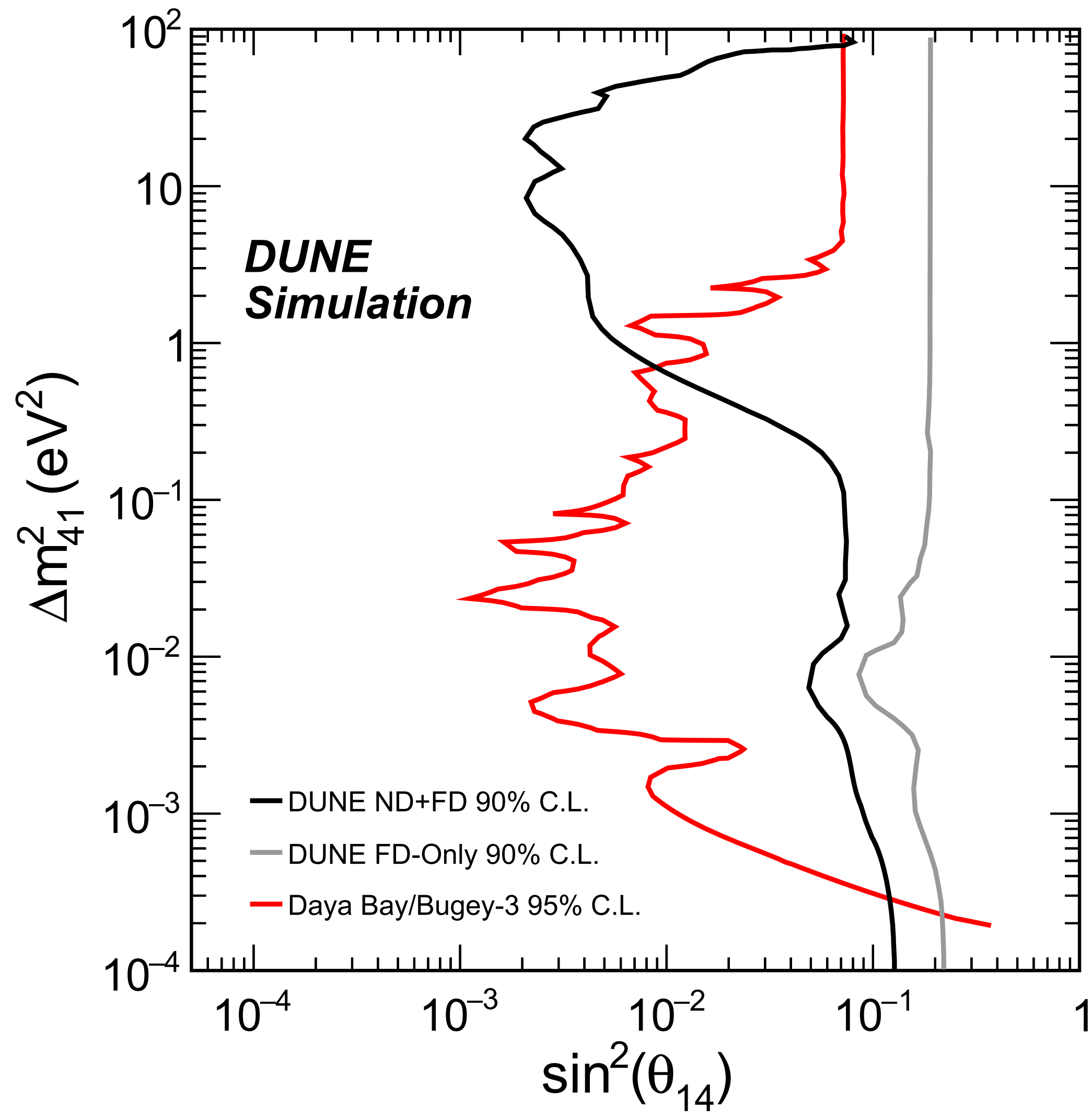
Light Sterile Neutrino favored by NOvA and T2K



Tension between NOvA and T2K can be somewhat ($\sim 2\sigma$) alleviated by adding 1 sterile neutrino, or by 3+1 model

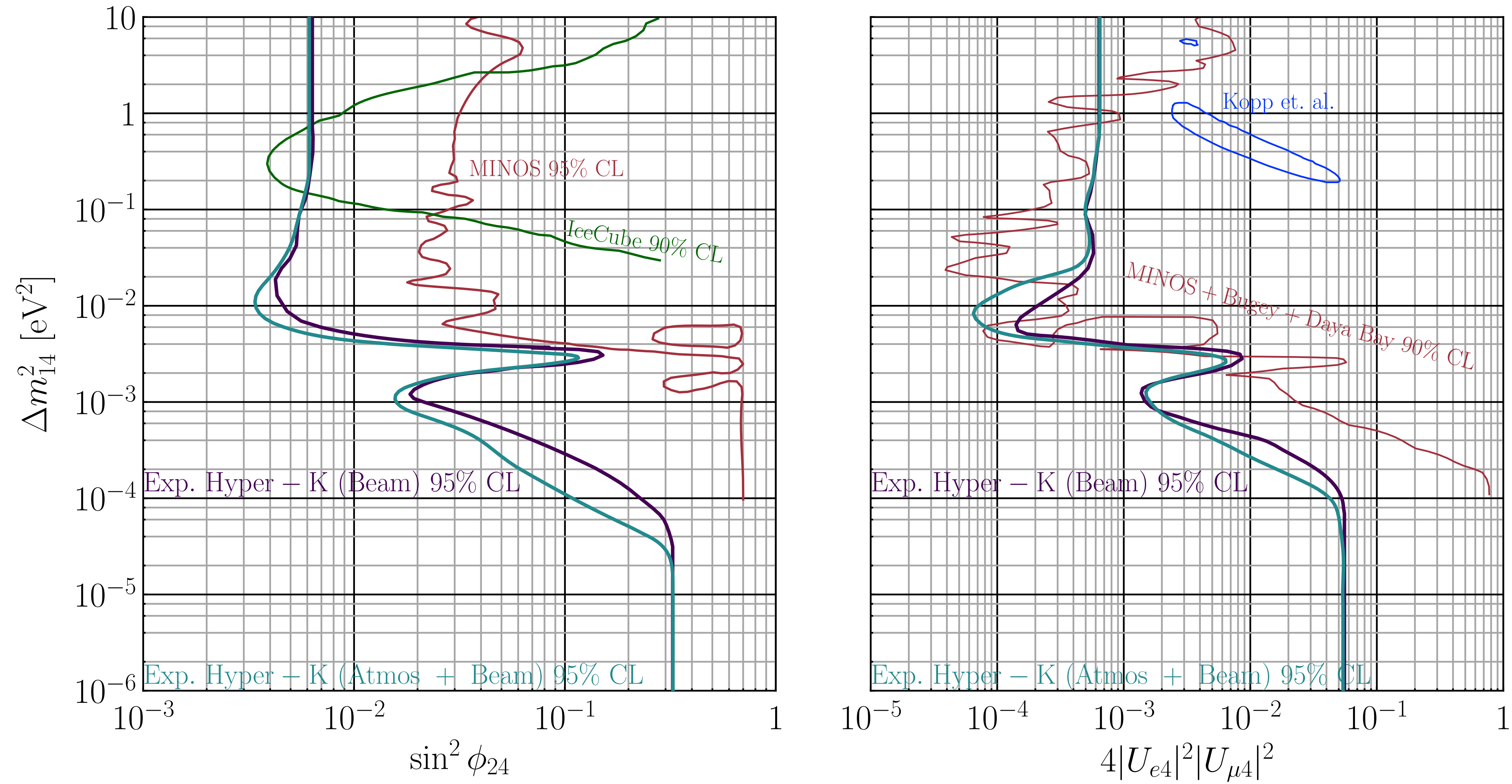
Gouvea, Sahches and Kelly, PRD 106, 055025 (2022) [arXiv:2204.09130 [hep-ph]]

Test of Sterile Neutrino by DUNE



Abi et al (DUNE Collab.), Eur. Phys. J. C81, 322 (2021) [arXiv:2008.12769 [hep-ex]]

Test of Light Sterile Neutrino by Hyper-K



Kelly, PRD95, 115009 (2017) [arXiv:1703.00448 [hep-ph]]

Some remarks for sterile neutrino in LBL experiments

Hyper-K and DUNE, with much larger statistics, would improve the current bounds

If the hint for the presence of sterile neutrino implied by T2K+NOvA results is true, with much larger statistics, Hyper-K and DUNE are expected to confirm (or exclude) such a scenario

Test of Neutrino Decay in LBL experiments

Invisible Decay

For simplicity, let us consider “invisible” decay mode like

$$\nu_i \rightarrow \nu_s + \chi \quad (i = 1, 2 \text{ or } 3)$$

where one of the mass eigenstates ν_i ($i = 1, 2 \text{ or } 3$) decays into sterile neutrino plus some massless particle which would also be non-detectable

Then energy eigen value is given by,

$$E_i = \frac{m_i^2}{2E} - i\frac{\Gamma_i}{2} \quad \frac{1}{\Gamma_i} = \frac{E}{m_i} \tau_i : \text{Lorentz dilated life time}$$

Neutrino Evolution Equation in Matter **with decay effect**

$$i \frac{d}{dx} \begin{bmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{bmatrix} = H \begin{bmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{bmatrix}$$
$$H = U \frac{1}{2E} \left(\begin{bmatrix} 0 & 0 & 0 \\ 0 & \Delta m_{21}^2 & 0 \\ 0 & 0 & \Delta m_{31}^2 \end{bmatrix} - i \frac{m_3}{\tau_3} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix} \right) U^\dagger + \sqrt{2} G_F n_e \begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

assuming that ν_3 can decay into sterile state ν_s like $\nu_3 \rightarrow \nu_s + \chi$

G_F : Fermi Constant

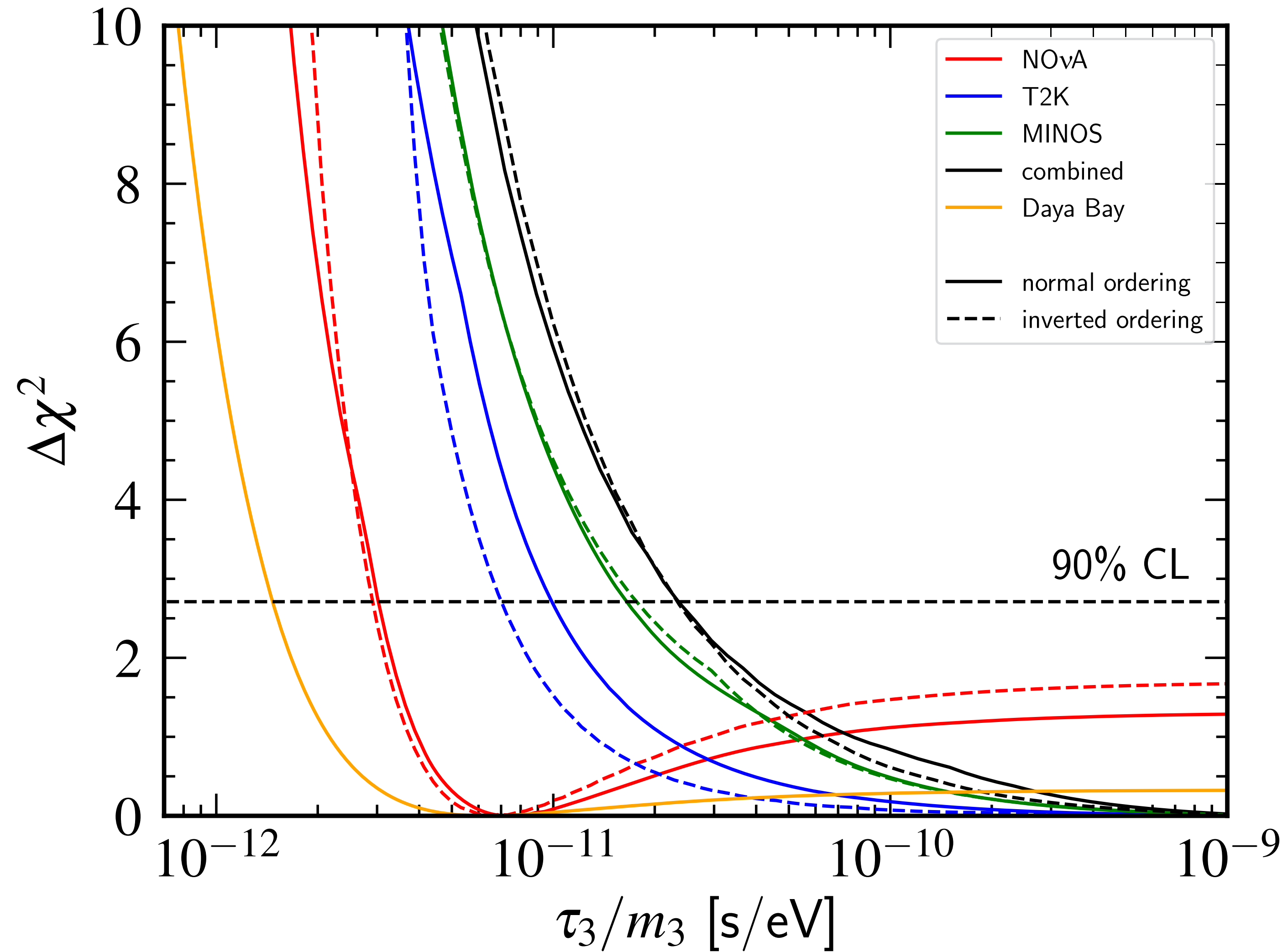
n_e : Electron number density

**Roughly speaking, the large decay effect
is expected if τ/m is $\sim L/E$ or**

For example, if $\sim L/E$ is 1000km/1GeV,

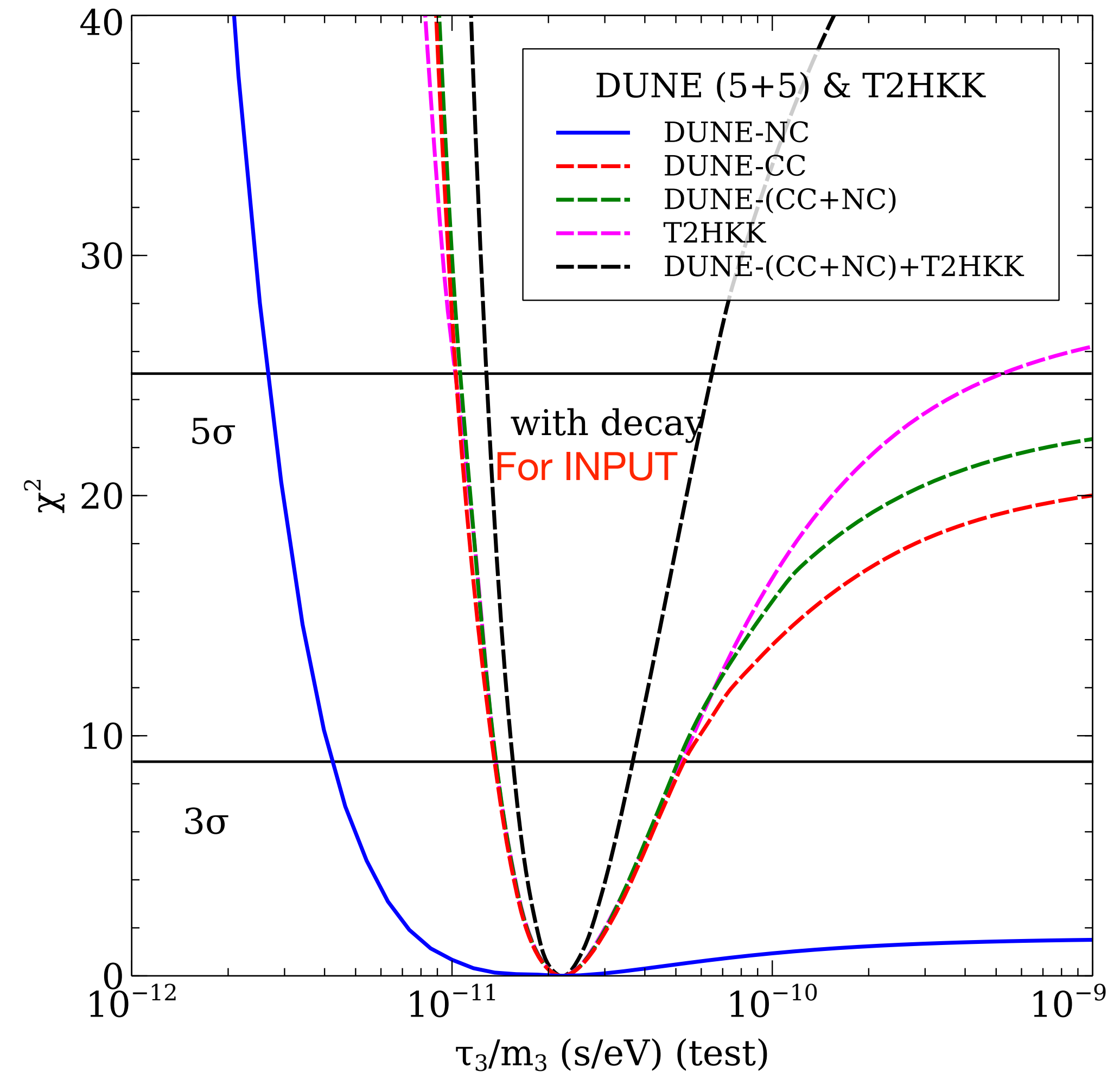
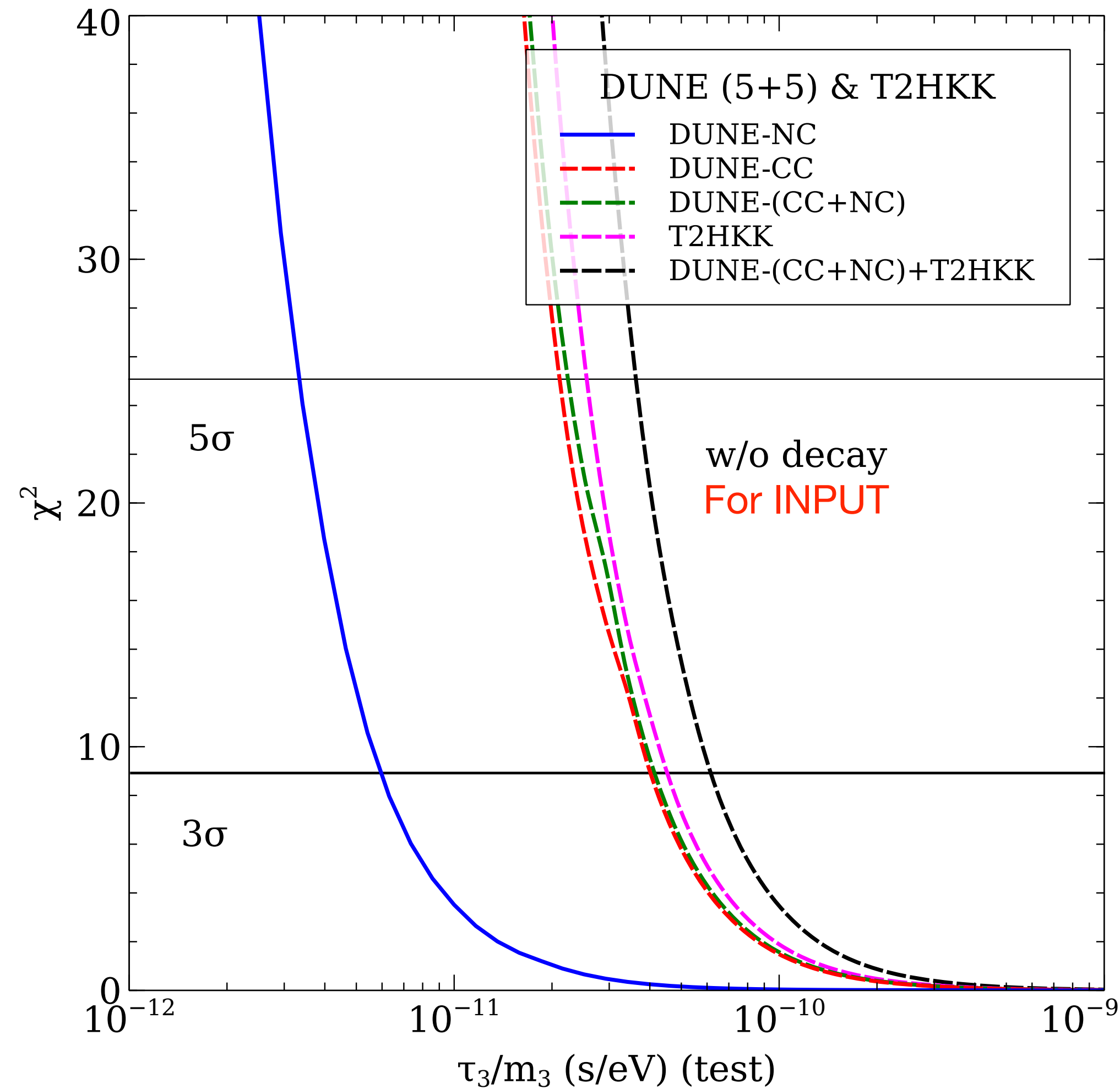
$$\frac{\tau}{m} = \frac{L}{E} \sim \frac{10^3 \text{km}}{1 \text{ GeV}} \sim 3.3 \times 10^{-12} \frac{\text{s}}{\text{eV}}$$

Current bounds by NOvA/T2K/MINOS and Daya Bay



Ternes & Pagliaroli, PRD109, L071701 (2024) [arXiv: 2401.14316 [hep-ph]]

Expected sensitivity by DUNE and T2HKK



Dey & Dutta, JHEP09, 035 (2024) [arXiv: 2402.13235 [hep-ph]]

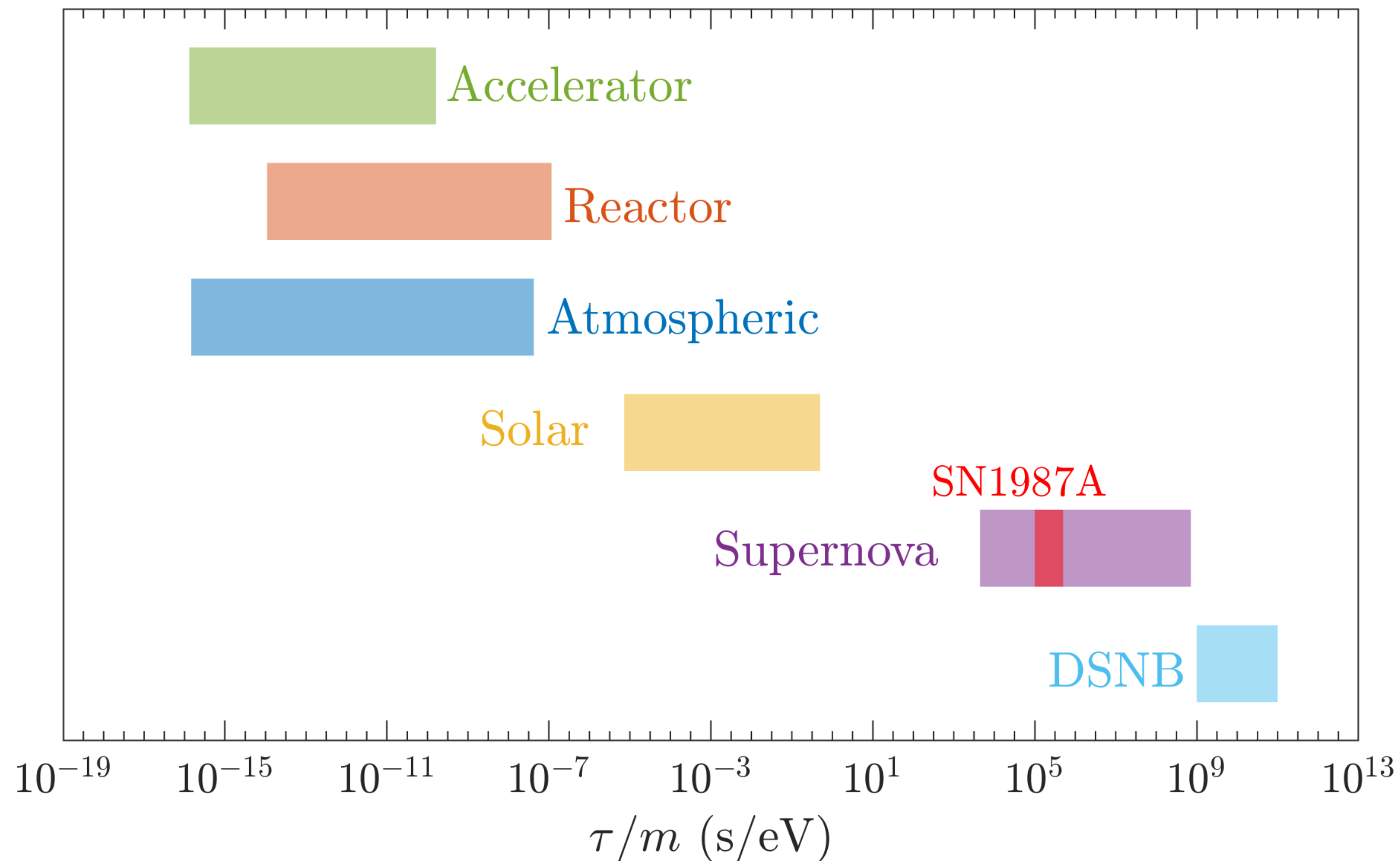
Expected sensitivity by DUNE and T2HKK

Experiment	90% C.L. (3σ) bound on τ_3/m_3 (s/eV) on τ_3/m_3 (s/eV)	ref.
SK+MINOS	$2.9(0.54) \times 10^{-10}$	ref. [31]
T2K + NO ν A	$2.3(1.5) \times 10^{-12}$	ref. [33]
T2K+NO ν A+MINOS	$2.4(2.4) \times 10^{-11}$	ref. [34]
DUNE - CC	$4.50(2.38) \times 10^{-11}$	ref. [37]
DUNE - (CC+NC) (5+5)	$5.1(2.7) \times 10^{-11}$	ref. [38]
T2HKK	$8.41 \times 10^{-11}(4.39 \times 10^{-11})$	This work
DUNE - (CC+NC) (5+5)	$7.74(4.22) \times 10^{-11}$	This work
DUNE - (CC+NC) (5+5)+T2HKK	$1.12 \times 10^{-10}(6.21 \times 10^{-11})$	This work
ESSnuSB (540 km)	$4.22(1.68) \times 10^{-11}$	ref. [40]
ESSnuB (360 km)	$4.95(2.64) \times 10^{-11}$	ref. [40]
JUNO	$9.3(4.7) \times 10^{-11}$	ref. [42]
INO	$1.51(0.566) \times 10^{-10}$	ref. [54]
KM3NeT-ORCA	$2.5(1.4) \times 10^{-10}$	ref. [16]
T2HK	$4.43(2.72) \times 10^{-11}$	ref. [41]
T2HKK	$1.01 \times 10^{-10}(4.36 \times 10^{-11})$	ref. [41]
T2HKK+ESSnuSB	$1.064 \times 10^{-10}(5.53 \times 10^{-11})$	ref. [41]
ESSnuSB	$3.69(2.43) \times 10^{-11}$	ref. [41]
T2HK+ESSnuSB	$1.01 \times 10^{-10}(4.36 \times 10^{-11})$	ref. [41]

Dey & Dutta, JHEP09, 035 (2024) [arXiv: 2402.13235 [hep-ph]]

But accelerator would not provide the best bound

typical sensitivities to the lifetime to mass ratio for neutrino from different sources



Ivanez-Ballester & Volpe, PLB847, 138252 (2023) [arXiv: 2307.03549 [hep-ph]]

Larger the L/E, in general, provides better sensitivity

However, solar/supernova neutrinos can not provide good sensitivity to the decay of ν_3

Some remarks for neutrino decay in LBL experiments

Hyper-K and DUNE, with much larger statistics, would improve the current bounds for some decay modes

Test of Unitarity in LBL experiments

Unitarity Test

For 3 flavor of mixed neutrinos

$$\begin{bmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{bmatrix} = U \begin{bmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{bmatrix} = \begin{bmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} \end{bmatrix} \begin{bmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{bmatrix}$$

mixing matrix U is unitary if

$$UU^\dagger = U^\dagger U = 1 \quad 9 \text{ indep. eqs.}$$

$$|U_{\alpha 1}|^2 + |U_{\alpha 2}|^2 + |U_{\alpha 3}|^2 = 1 \quad (\alpha = e, \mu, \tau)$$

or

$$|U_{ei}|^2 + |U_{\mu i}|^2 + |U_{\tau i}|^2 = 1 \quad (i = 1, 2, 3)$$

normalization
(3 eqs.)

$$U_{\alpha 1}U_{\beta 1}^* + U_{\alpha 2}U_{\beta 2}^* + U_{\alpha 3}U_{\beta 3}^* = 0 \quad (\alpha, \beta = e, \mu, \tau, \alpha \neq \beta)$$

or

$$U_{ei}U_{ej}^* + U_{\mu i}U_{\mu j}^* + U_{\tau i}U_{\tau j}^* = 0 \quad (i, j = 1, 2, 3, i \neq j)$$

closure
of unitarity
triangle
(6R eqs.)

Unitarity Test

Where the Non-Unitarity (NU) effect can manifest?

See e.g. Antusch et al, JHEP10, 084 (2006)

- **Decay Processes**

W decay

Invisible Z decay

Universality test

Rare charged lepton decay

- **Neutrino Oscillation**

Disappearance mode

Appearance mode

In this talk we focus on
NU effect for oscillation

Non-Unitarity implies the presence of extra neutrino state(s)

Let us consider n extra sterile states

$$U_{(3+n) \times (3+n)} = \begin{bmatrix} U_{3 \times 3} & W \\ Z & V \end{bmatrix}$$

$$U_{(3+n) \times (3+n)}^\dagger U_{(3+n) \times (3+n)} = U_{(3+n) \times (3+n)} U_{(3+n) \times (3+n)}^\dagger = 1$$

then we expect that $U_{3 \times 3}^\dagger U_{3 \times 3} \neq 1, U_{3 \times 3} U_{3 \times 3}^\dagger \neq 1$

Non-unitarity can be parametrized as follows

Miranda et al, PRL117, 061804 (2016)

$$U = \begin{bmatrix} \alpha_{11} & 0 & 0 \\ \alpha_{21} & \alpha_{22} & 0 \\ \alpha_{31} & \alpha_{32} & \alpha_{33} \end{bmatrix} U_0$$

$\alpha_{ii} : \text{real}$
 $\alpha_{ij} (i \neq j) : \text{complex}$
 $\alpha_{ii} \sim 1, |\alpha_{ij}| (i \neq j) \ll 1$

non-unitary if the triangular α matrix is not $\mathbb{1}$

standard 3x3 unitary matrix

$\alpha_{ij} \neq \delta_{ij}$ implies unitarity violation

$$\begin{aligned} |U_{e1}|^2 + |U_{e2}|^2 + |U_{e3}|^2 &= \alpha_{11}^2 \\ |U_{\mu1}|^2 + |U_{\mu2}|^2 + |U_{\mu3}|^2 &= \alpha_{22}^2 + |\alpha_{21}|^2 \\ |U_{\tau1}|^2 + |U_{\tau2}|^2 + |U_{\tau3}|^2 &= \alpha_{33}^2 + |\alpha_{32}|^2 + |\alpha_{31}|^2 \end{aligned}$$

normalization (if =1 or not?)

$$\begin{aligned} U_{e1}^* U_{\mu1} + U_{e2}^* U_{\mu2} + U_{e3}^* U_{\mu3} &= \alpha_{11} \alpha_{21} \\ U_{e1}^* U_{\tau1} + U_{e2}^* U_{\tau2} + U_{e3}^* U_{\tau3} &= \alpha_{11} \alpha_{32} \\ U_{\mu1}^* U_{\tau1} + U_{\mu2}^* U_{\tau2} + U_{\mu3}^* U_{\tau3} &= \alpha_{21}^* \alpha_{31} + \alpha_{22}^* \alpha_{32} \end{aligned}$$

closure (of the unitarity triangle)
(if = 0 or not?)

Cauchy-Schwartz Inequalities

If $U = U_{3 \times 3}$ is a part of complete unitary matrix $U_{(3+n) \times (3+n)}$ elements of U must satisfy the following conditions

$$\left| \sum_{i=1}^3 U_{\alpha i} U_{\beta i}^* \right|^2 \leq \left(1 - \sum_{i=1}^3 |U_{\alpha i}|^2 \right) \left(1 - \sum_{i=1}^3 |U_{\beta i}|^2 \right)$$

This condition is important to constrain the closure relations or off diagonal elements α_{ij} ($i \neq j$)

Remark: some works do not (intentionally) take into account this condition

Neutrino Evolution Equation in Matter **with Non-Unitarity effect**

$$i \frac{d}{dx} \begin{bmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{bmatrix} = H \begin{bmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{bmatrix}$$
$$H = \begin{bmatrix} 0 & 0 & 0 \\ 0 & \frac{\Delta m_{21}^2}{2E} & 0 \\ 0 & 0 & \frac{\Delta m_{31}^2}{2E} \end{bmatrix} + \sqrt{2} G_F U^\dagger \begin{bmatrix} N_e - N_n/2 & 0 & 0 \\ 0 & -N_n/2 & 0 \\ 0 & 0 & -N_n/2 \end{bmatrix} U$$

G_F : Fermi Constant

$N_e(N_n)$: Electron (neutron) number density

Neutrino Evolution Equation in Matter **with Non-Unitarity effect**

$$i \frac{d}{dx} \begin{bmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{bmatrix} = H \begin{bmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{bmatrix}$$

Off diagonal elements, α_{ij} ($i \neq j$), can induce additional mixing(-like) effects
 $\text{Im}[\alpha_{ij}]$ is a new source of CP violation

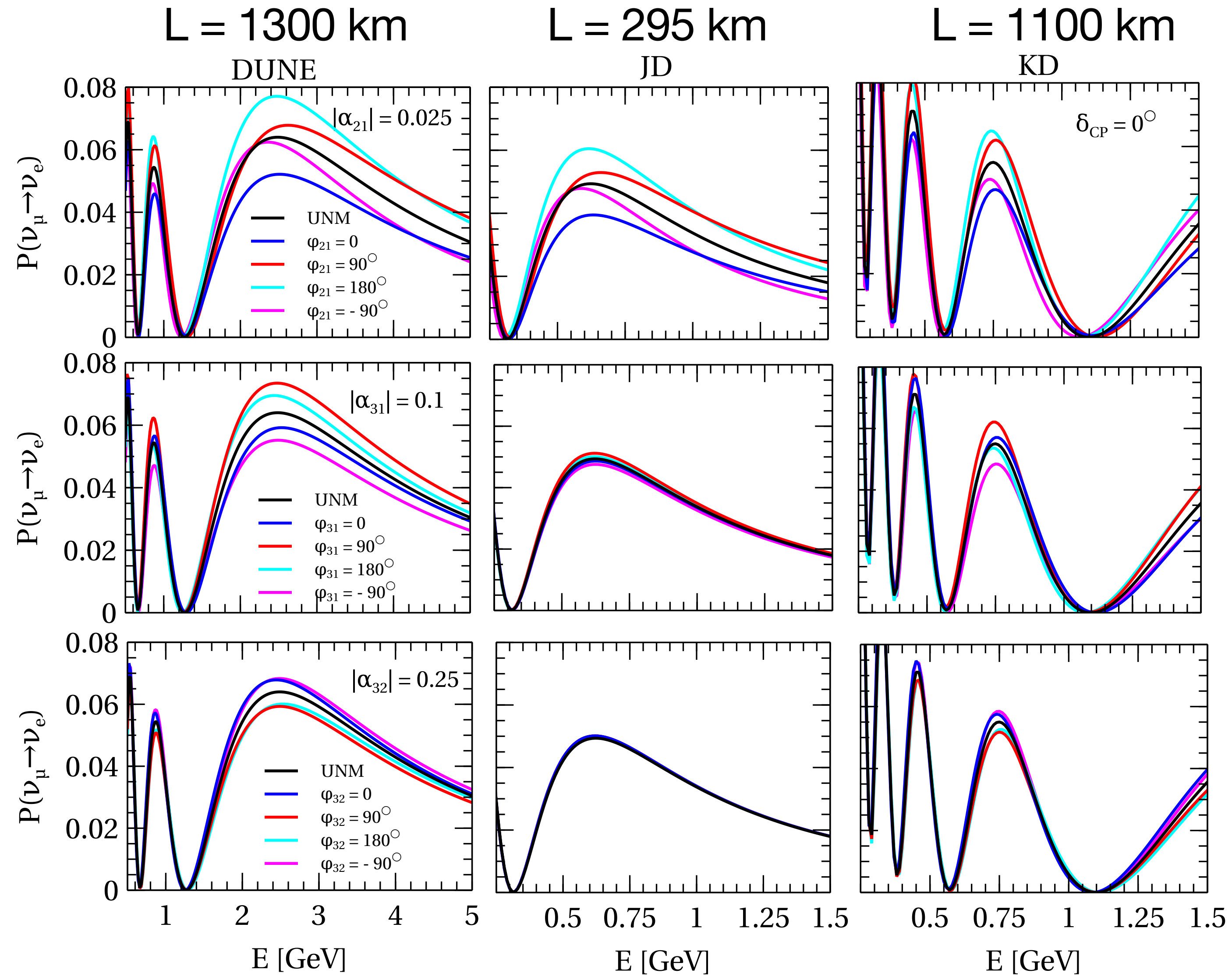
$$H = \begin{bmatrix} 0 & 0 & 0 \\ 0 & \frac{\Delta m_{21}^2}{2E} & 0 \\ 0 & 0 & \frac{\Delta m_{31}^2}{2E} \end{bmatrix} + \sqrt{2} G_F U^\dagger \begin{bmatrix} N_e - N_n/2 & 0 & 0 \\ 0 & -N_n/2 & 0 \\ 0 & 0 & -N_n/2 \end{bmatrix} U$$

Diagonal elements, α_{ii} , if different from 1, can modify the resonance condition

G_F : Fermi Constant

$N_e(N_n)$: Electron (neutron) number density

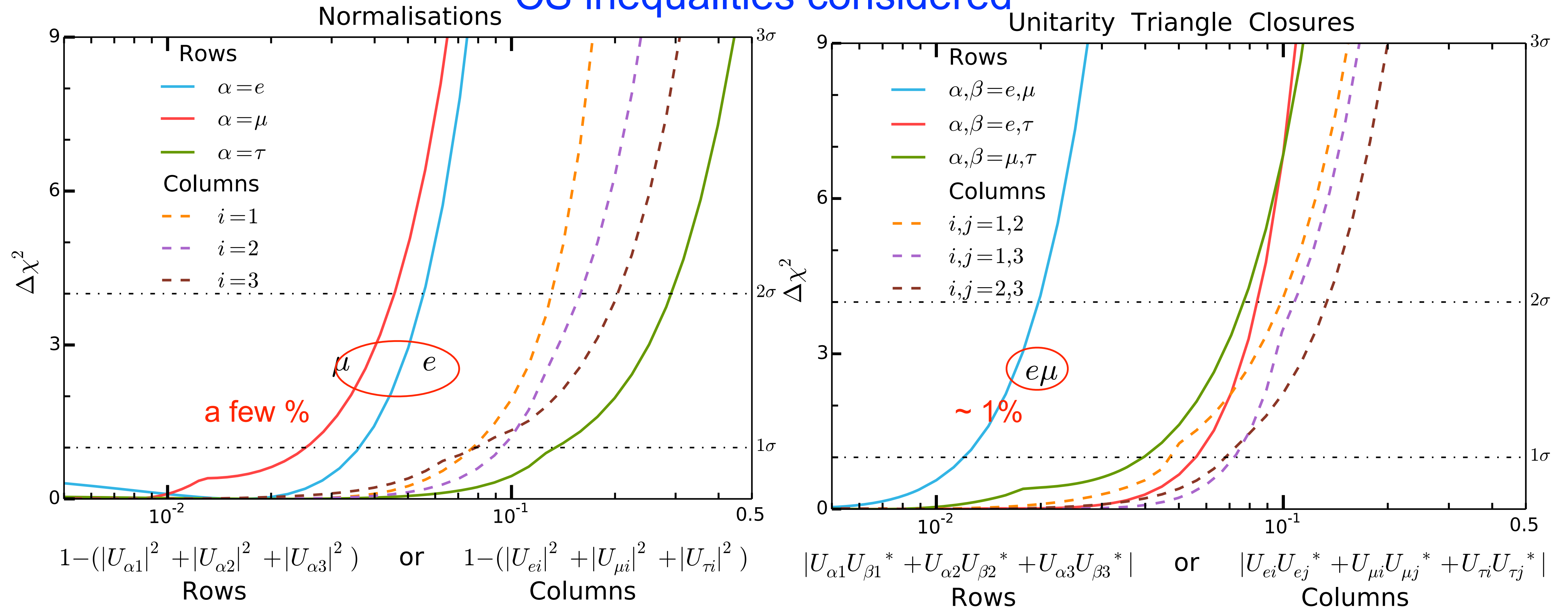
Some example of oscillation probabilities with Non-Unitarity effects for LBL experiments



Agarwalla et al, JHEP07, 121 (2022) [arXiv:2111.00329 [hep-ex]]

Current (around ~2016) limits on Non-Unitarity

CS inequalities considered

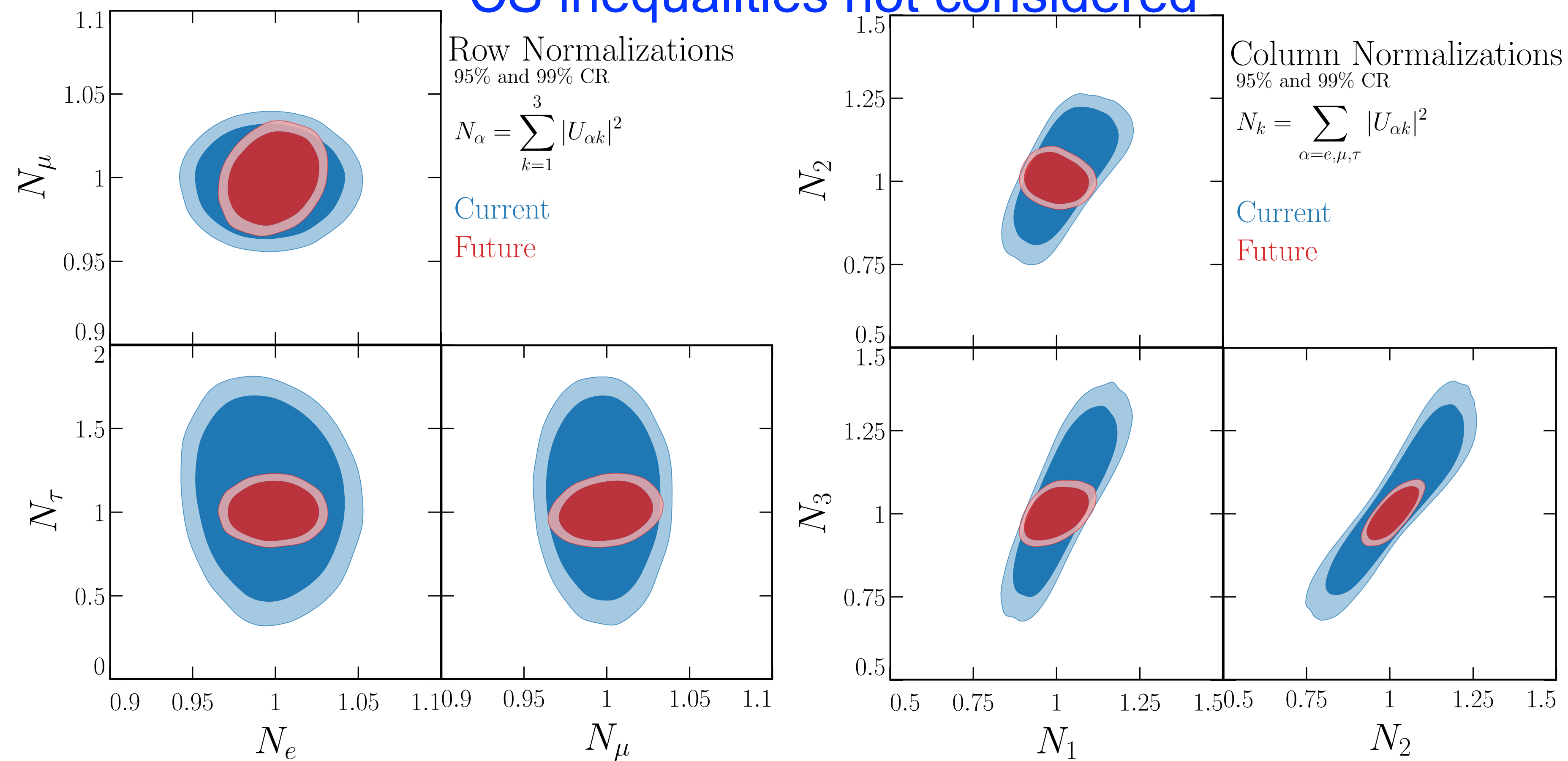


normalization bounds are limited by flux uncertainty

Parke and Ross-Lonergan, PRD93, 113009 (2016)

Current and Future bounds on Non-Unitarity for Normalizations

CS inequalities not considered



$$N_\alpha \equiv |U_{\alpha 1}|^2 + |U_{\alpha 2}|^2 + |U_{\alpha 3}|^2 (\alpha = e, \mu, \tau)$$

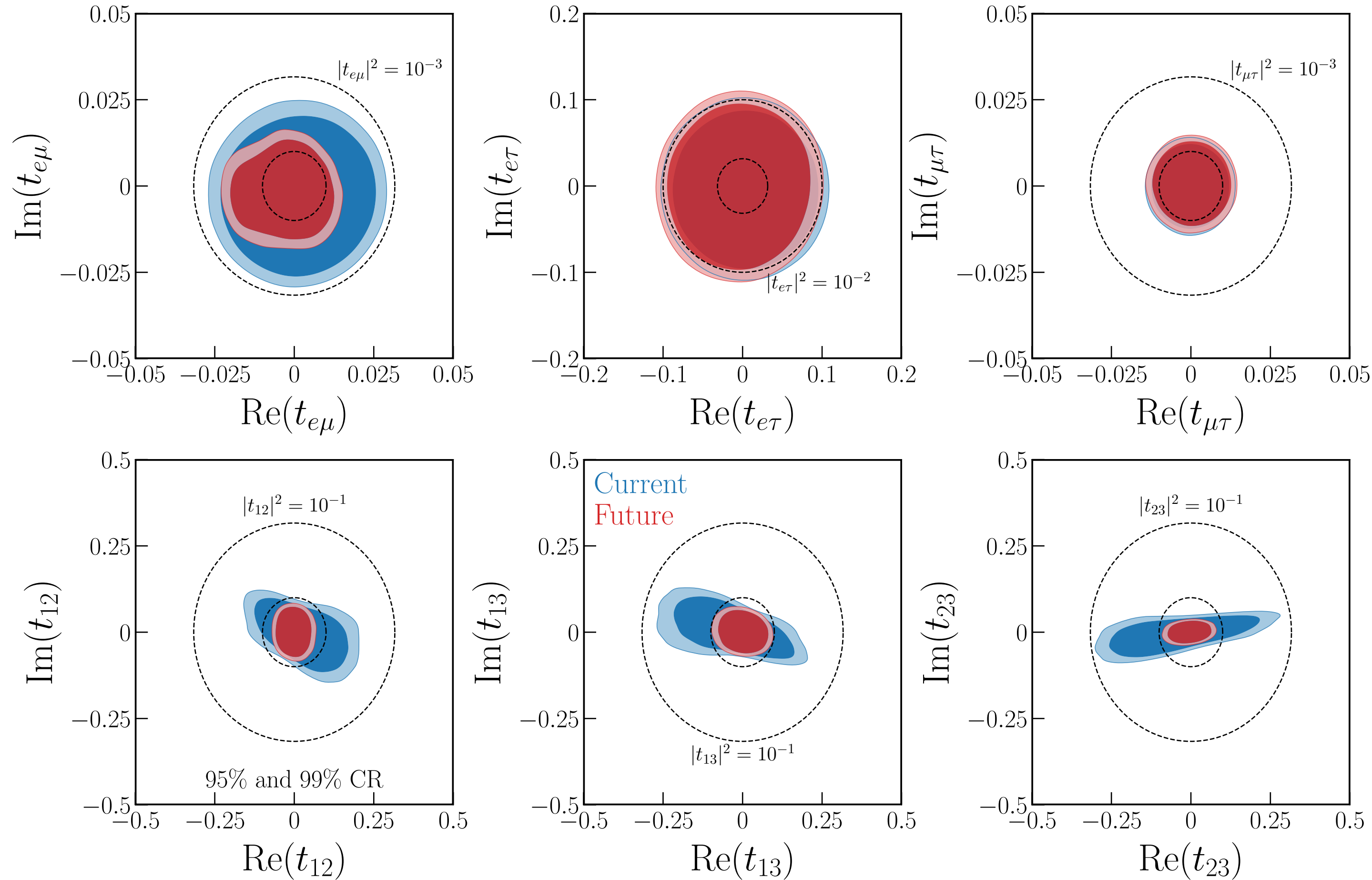
$$N_k \equiv |U_{ek}|^2 + |U_{\mu k}|^2 + |U_{\tau k}|^2 (k = 1, 2, 3)$$

Future case includes JUNO, HK, DUNE and IceCube (upgrade)

Ellis et al., JHEP12.068 (2020) [arXiv:2008.01088 [hep-ph]]

Current and Future bounds on Non-Unitarity for Closures

CS inequalities not considered



$$t_{\alpha\beta} \equiv U_{\alpha 1}^* U_{\beta 1} + U_{\alpha 2}^* U_{\beta 2} + U_{\alpha 3}^* U_{\beta 3} \quad (\alpha, \beta = e, \mu, \tau, \alpha \neq \beta)$$

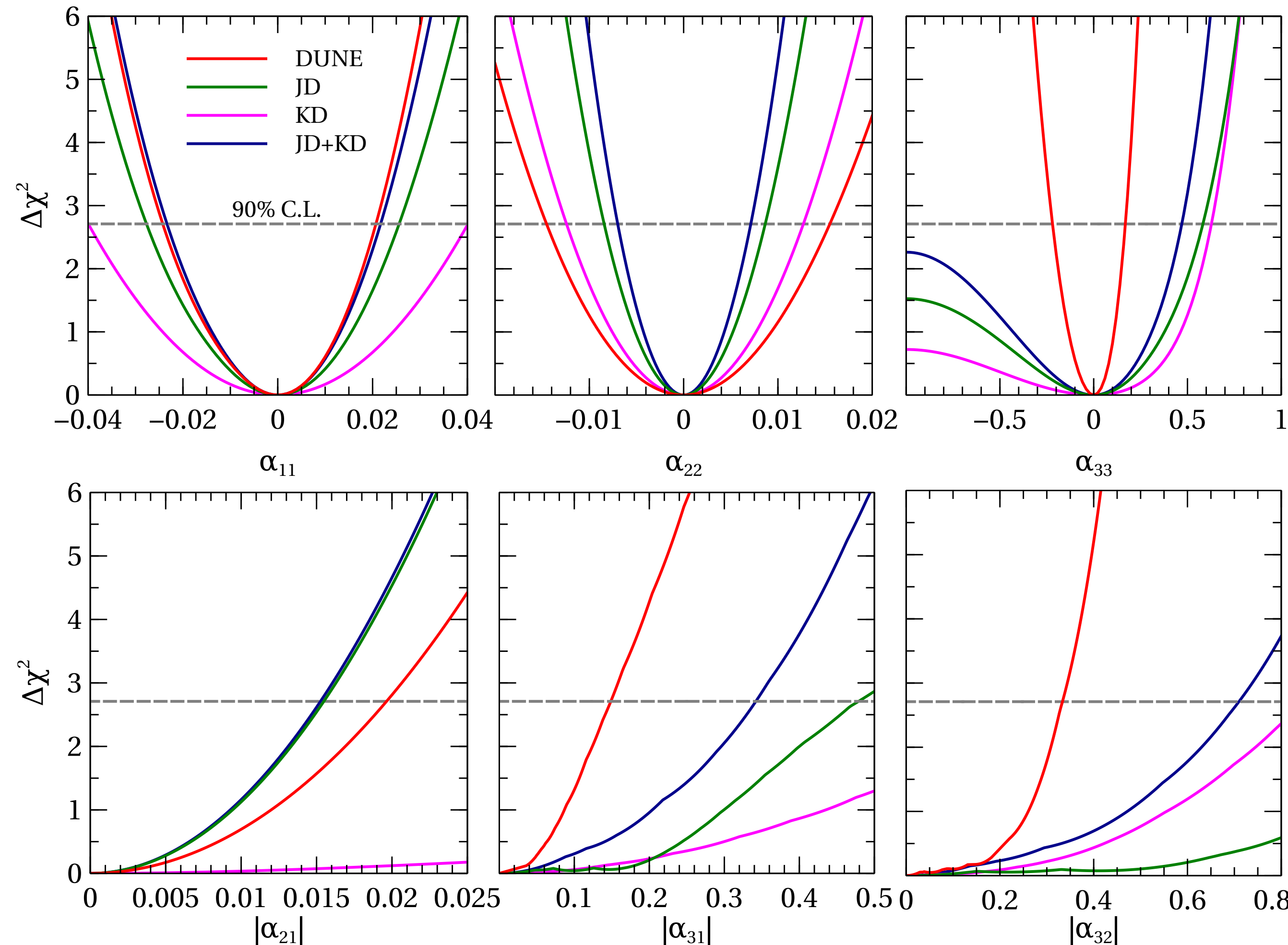
$$t_{ij} \equiv U_{ei}^* U_{ej} + U_{\mu i}^* U_{\mu j} + U_{\tau i}^* U_{\tau j} \quad (i, j = 1, 2, 3, i \neq j)$$

Future case includes JUNO, HK, DUNE and IceCube (upgrade)

Ellis et al., JHEP12.068 (2020) [arXiv:2008.01088 [hep-ph]]

Future bounds on Non-Unitarity by DUNE, T2HK, T2HKK

CS inequalities not considered



JD = T2HK (295 km)

KD = HK detector in
Korea only (1100km)

Agarwalla et al, JHEP07, 121 (2022) [arXiv:2111.00329 [hep-ex]]

Some remarks for Unitarity test in LBL experiments

Hyper-K and DUNE (JUNO), with much larger statistics, would improve the current bounds

But, in my opinion, to improve more bounds on Non-Unitarity, the most important/crucial systematics are uncertainties on flux and the detection cross sections as they affect directly the normalization relations (and also closure relations through CS inequalities), therefore, they must be improved!

See C.S. Fong, HN, Minakata, JHEP02, 114(2017) [arXiv:1609.08623 [hep-ph]]

Summary

- **1. In last ~25 years, neutrino oscillation is very well established and we are now in the era of precision neutrino physics where long-baseline (LBL) oscillation experiments are playing important roles**
- **2. But there are still several fundamental open questions which can be studied by the future LBL experiments**
- **3. Near future LBL experiments like Hyper-K and DUNE can address the questions related to CP phase, θ_{23} and Δm_{32}^2 (related to MO)**
- **4. LBL experiments will be study further new physics effects coming from NSI, sterile neutrino, decay, decoherence, etc**
- **5. We are looking forward to have very interesting and important progress in the coming decade!**

Concluding Remarks

- **During ~15 years of 1998 - 2012**
 - **discovery phase in neutrino physics-**
- **~2013 - present: Steady progress (precision era) but no big new discovery (not yet) related to neutrino**
- **2025 - future: Operation of new generation experiments, JUNO, Hyper-K, DUNE, etc,**
 - New Discovery, some surprise?**

Thank you very much for your attention!

¡Muchas gracias por su atención!

Backup Slides

Current allowed range of mixing parameters from Global Fit

		Normal Ordering (best fit)		Inverted Ordering ($\Delta\chi^2 = 6.1$)	
		bfp $\pm 1\sigma$	3σ range	bfp $\pm 1\sigma$	3σ range
IC24 with SK atmospheric data	$\sin^2 \theta_{12}$	$0.308^{+0.012}_{-0.011}$	$0.275 \rightarrow 0.345$	$0.308^{+0.012}_{-0.011}$	$0.275 \rightarrow 0.345$
	$\theta_{12}/^\circ$	$33.68^{+0.73}_{-0.70}$	$31.63 \rightarrow 35.95$	$33.68^{+0.73}_{-0.70}$	$31.63 \rightarrow 35.95$
	$\sin^2 \theta_{23}$	$0.470^{+0.017}_{-0.013}$	$0.435 \rightarrow 0.585$	$0.550^{+0.012}_{-0.015}$	$0.440 \rightarrow 0.584$
	$\theta_{23}/^\circ$	$43.3^{+1.0}_{-0.8}$	$41.3 \rightarrow 49.9$	$47.9^{+0.7}_{-0.9}$	$41.5 \rightarrow 49.8$
	$\sin^2 \theta_{13}$	$0.02215^{+0.00056}_{-0.00058}$	$0.02030 \rightarrow 0.02388$	$0.02231^{+0.00056}_{-0.00056}$	$0.02060 \rightarrow 0.02409$
	$\theta_{13}/^\circ$	$8.56^{+0.11}_{-0.11}$	$8.19 \rightarrow 8.89$	$8.59^{+0.11}_{-0.11}$	$8.25 \rightarrow 8.93$
	$\delta_{\text{CP}}/^\circ$	212^{+26}_{-41}	$124 \rightarrow 364$	274^{+22}_{-25}	$201 \rightarrow 335$
	$\frac{\Delta m_{21}^2}{10^{-5} \text{ eV}^2}$	$7.49^{+0.19}_{-0.19}$	$6.92 \rightarrow 8.05$	$7.49^{+0.19}_{-0.19}$	$6.92 \rightarrow 8.05$
	$\frac{\Delta m_{3\ell}^2}{10^{-3} \text{ eV}^2}$	$+2.513^{+0.021}_{-0.019}$	$+2.451 \rightarrow +2.578$	$-2.484^{+0.020}_{-0.020}$	$-2.547 \rightarrow -2.421$

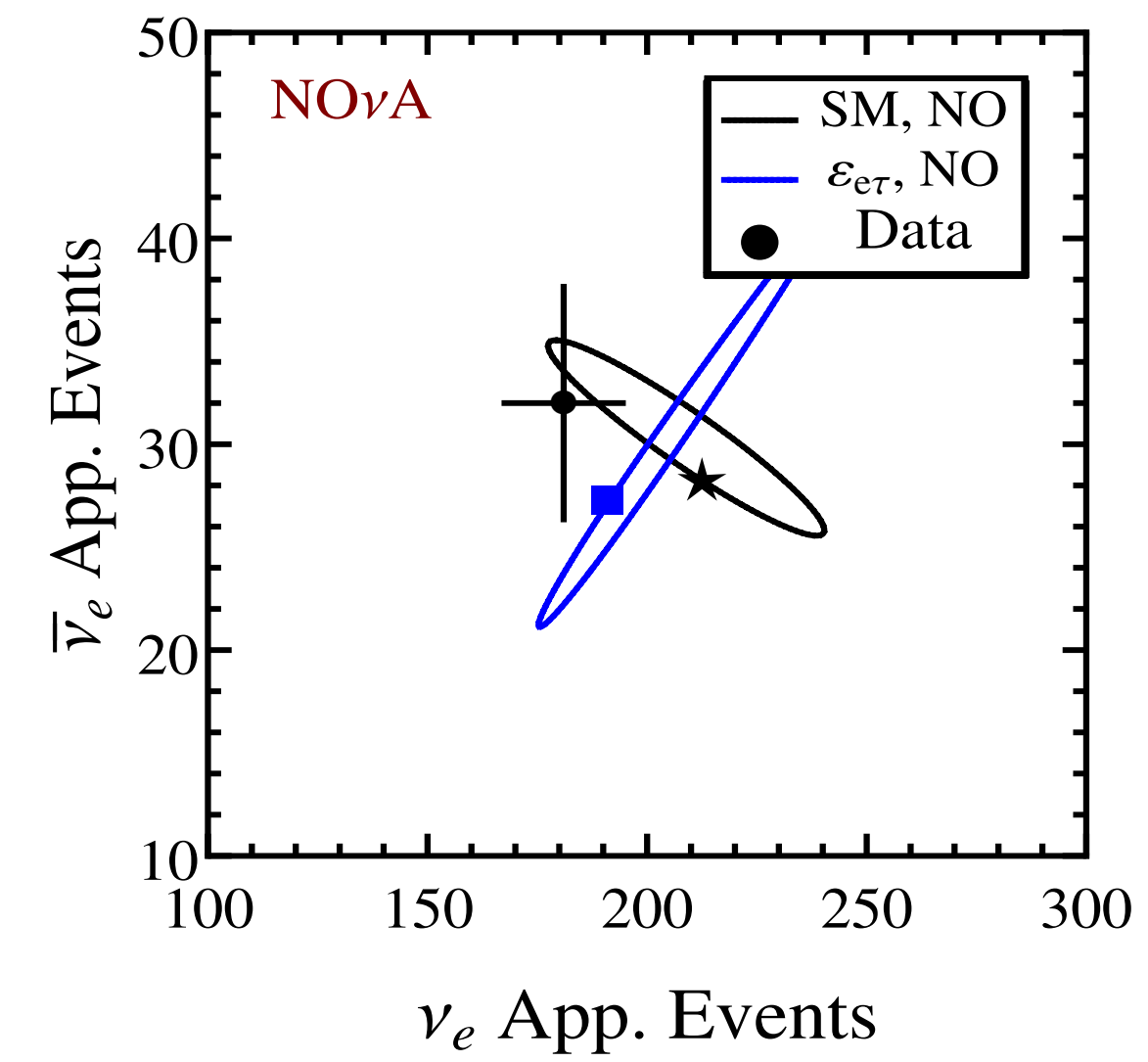
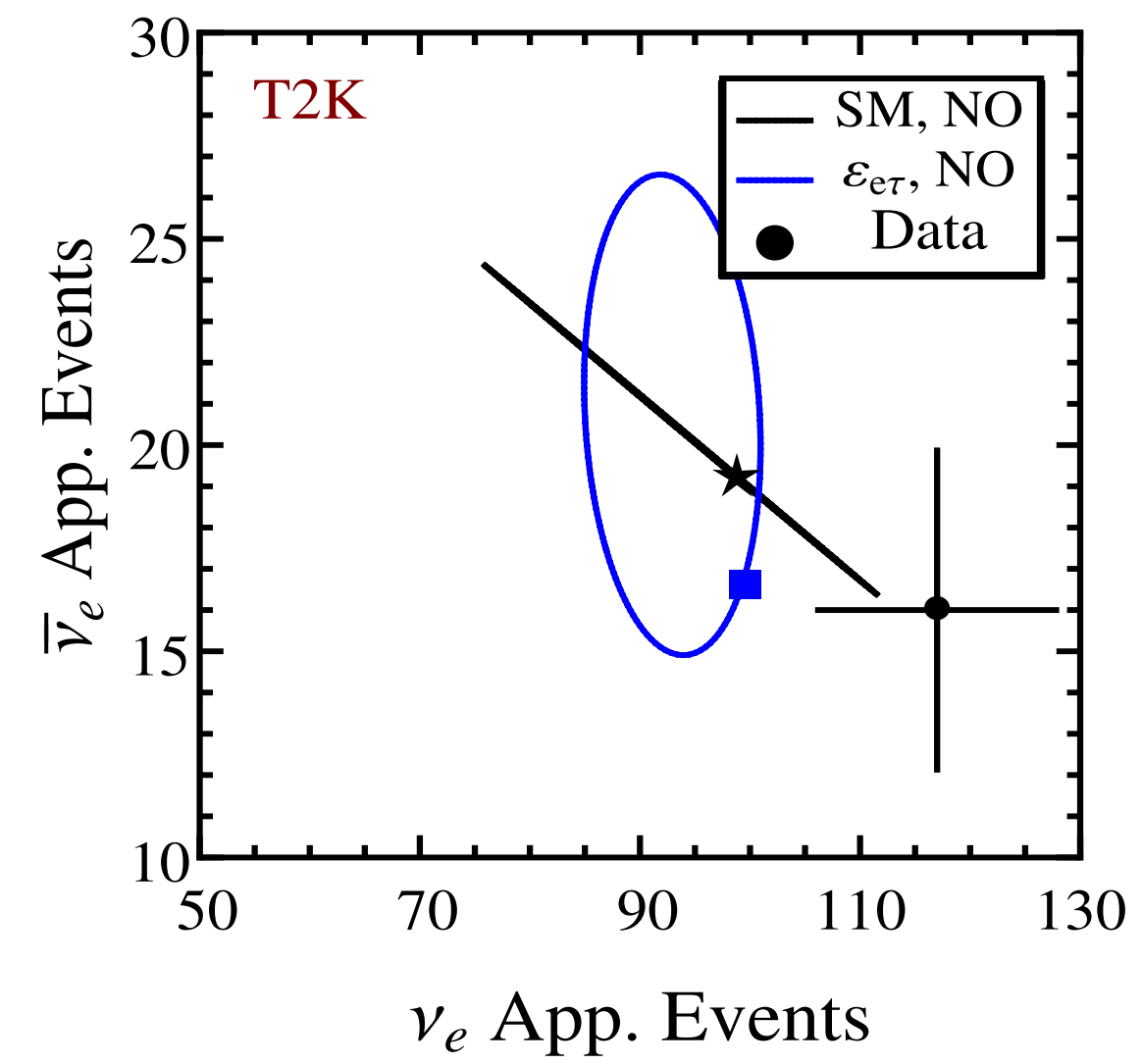
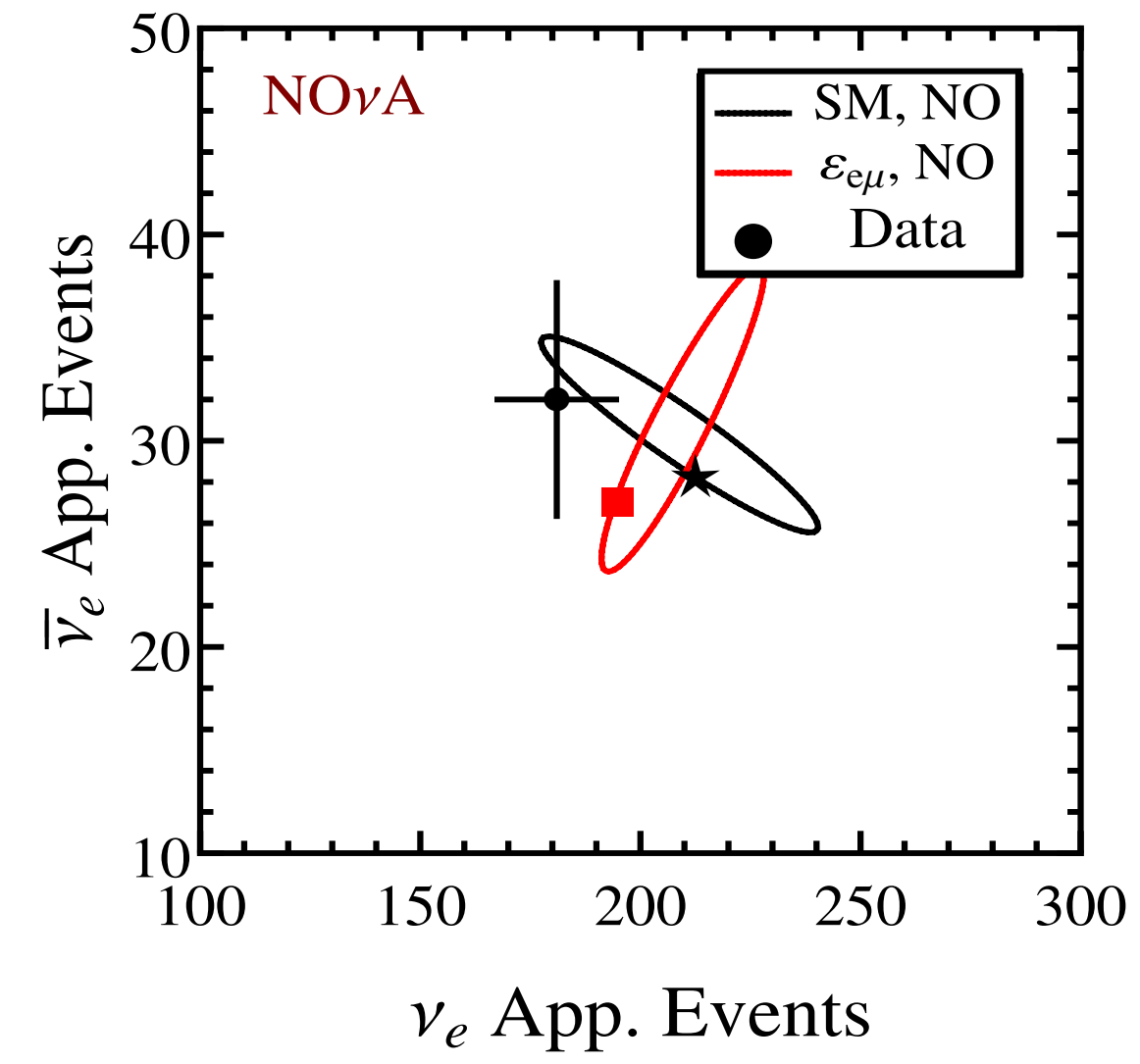
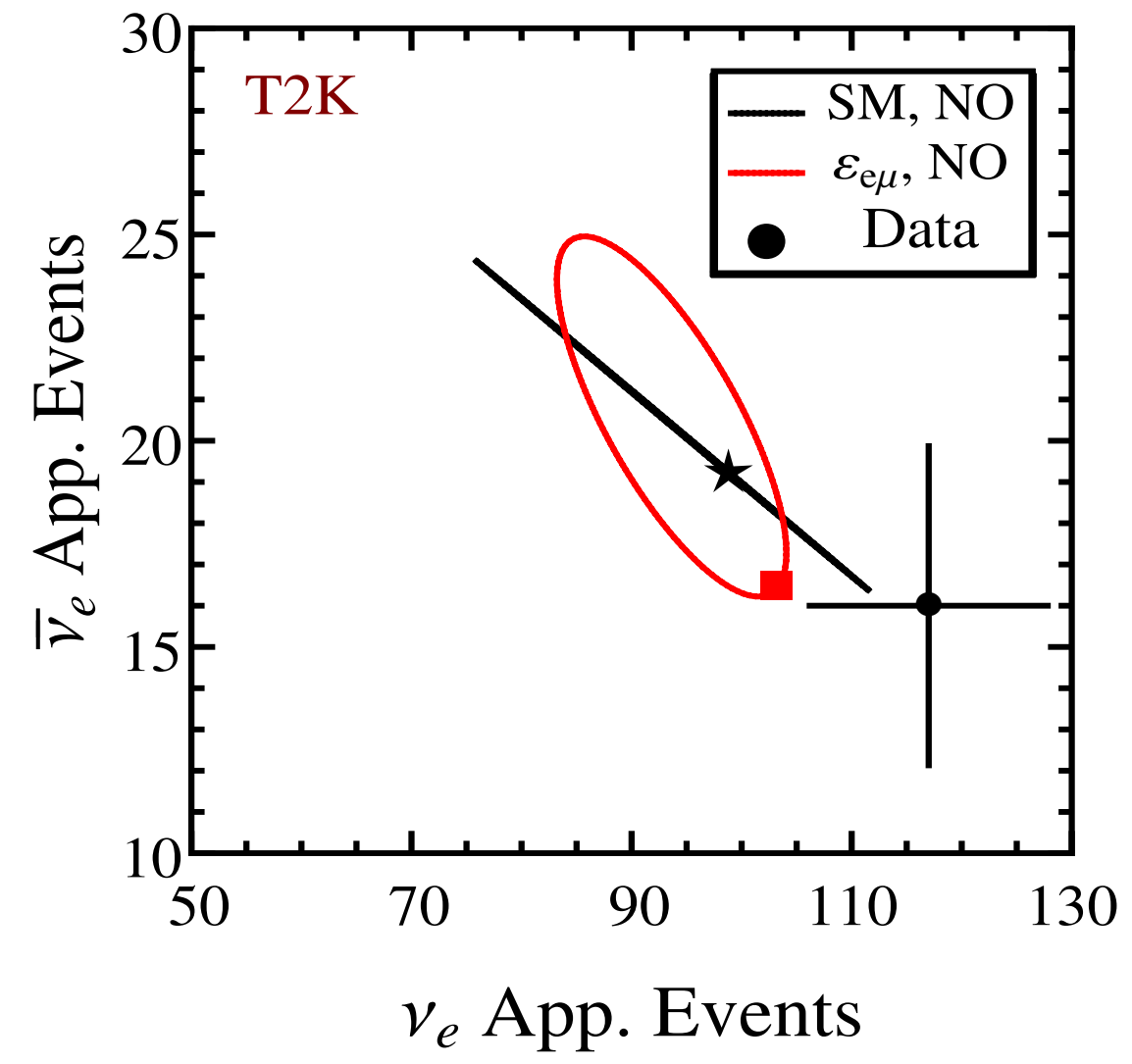
NuFit6.0, Esteban et la,
arXiv: 2410.05380

Roughly, 1σ uncertainties of $\sin^2 \theta_{ij}$ ($ij = 12, 23, 23$) is $\sim 3 - 4 \%$

$$\Delta m_{21}^2 \text{ is } \sim 3 \% \qquad |\Delta m_{31}^2| \simeq |\Delta m_{32}^2| \text{ is } \sim 1\% \qquad \delta_{\text{CP}} \text{ is } \sim 30\text{-}40^\circ$$

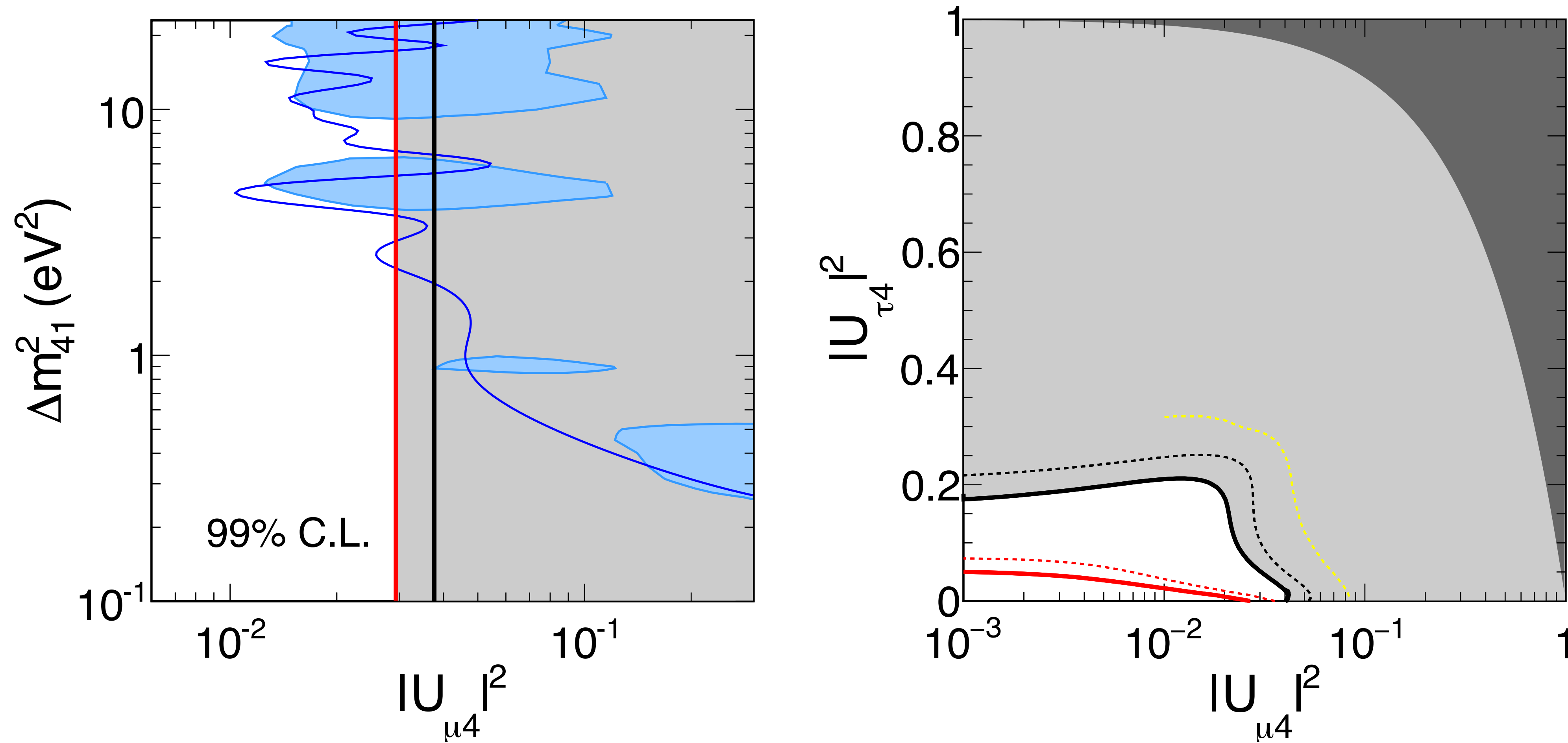
Neutrino Physics is in a Precision Era !

$$\begin{aligned}
U &= \begin{bmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{bmatrix} \begin{bmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{bmatrix} \begin{bmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{bmatrix} \\
&= \begin{bmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{bmatrix}
\end{aligned}$$



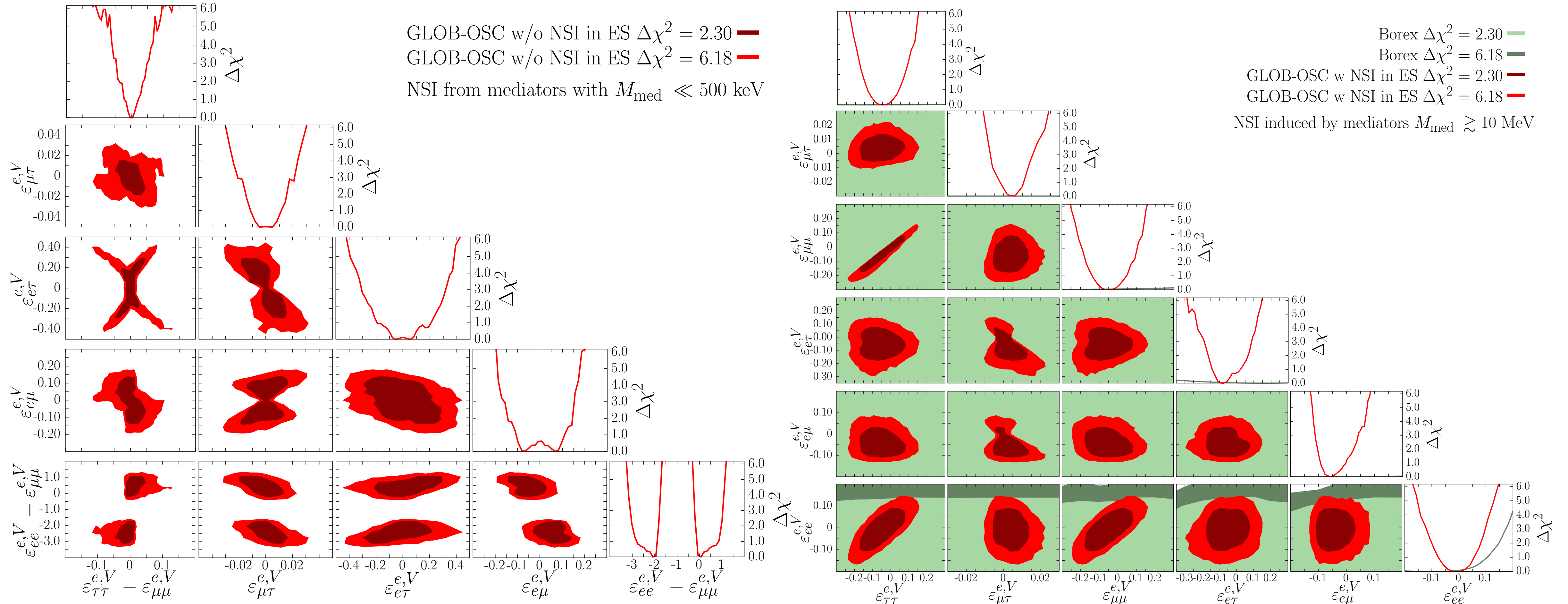
S. S. Chatterjee and A. Palazzo, arXiv:2409.10599 [hep-ph]

Test of Sterile Neutrino by Hyper-K



Abe et al (HK Collab.), Design Report [arXiv:1805.04163v2 [hep-ex]]

Current Bounds on NSI with electrons (by Global Analysis)



Coloma et al, JHEP08, 032 (2023) [arXiv:2305.07698 [hep-ph]]

Current Bounds on NSI with electrons (by Global Analysis)

	Allowed ranges at 90% CL (marginalized)			
	Vector ($X = V$)		Axial-vector ($X = A$)	
	Borexino	GLOB-OSC w NSI in ES	Borexino	GLOB-OSC w NSI in ES
$\varepsilon_{ee}^{e,X}$	$[-1.1, +0.17]$	$[-0.13, +0.10]$	$[-0.38, +0.24]$	$[-0.13, +0.11]$
$\varepsilon_{\mu\mu}^{e,X}$	$[-2.4, +1.5]$	$[-0.20, +0.10]$	$[-1.5, +2.4]$	$[-0.70, +1.2]$
$\varepsilon_{\tau\tau}^{e,X}$	$[-2.8, +2.1]$	$[-0.17, +0.093]$	$[-1.8, +2.8]$	$[-0.53, +1.0]$
$\varepsilon_{e\mu}^{e,X}$	$[-0.83, +0.84]$	$[-0.097, +0.011]$	$[-0.79, +0.76]$	$[-0.41, +0.40]$
$\varepsilon_{e\tau}^{e,X}$	$[-0.90, +0.85]$	$[-0.18, +0.080]$	$[-0.81, +0.78]$	$[-0.36, +0.36]$
$\varepsilon_{\mu\tau}^{e,X}$	$[-2.1, +2.1]$	$[-0.0063, +0.016]$	$[-1.9, +1.9]$	$[-0.79, +0.81]$

Coloma et al, JHEP08, 032 (2023) [arXiv:2305.07698 [hep-ph]]

Current Bounds on NSI with quarks (by Global Analysis)

	Allowed ranges at 90% CL (marginalized)			Allowed ranges at 90% CL (marginalized)
	GLOB-OSC			GLOB-OSC+CE ν NS
	LMA	LMA \oplus LMA-D		LMA = LMA \oplus LMA-D
$\varepsilon_{ee}^{u,V} - \varepsilon_{\mu\mu}^{u,V}$	$[-0.063, +0.36]$	$[-1.1, -0.79] \oplus [-0.063, +0.36]$	$\varepsilon_{ee}^{u,V}$	$[-0.038, +0.034] \oplus [+0.34, +0.42]$
$\varepsilon_{\tau\tau}^{u,V} - \varepsilon_{\mu\mu}^{u,V}$	$[-0.0053, +0.017]$	$[-0.021, +0.018]$	$\varepsilon_{\mu\mu}^{u,V}$	$[-0.046, +0.031] \oplus [+0.35, +0.42]$
$\varepsilon_{e\mu}^{u,V}$	$[-0.057, +0.013]$	$[-0.057, +0.061]$	$\varepsilon_{\tau\tau}^{u,V}$	$[-0.046, +0.033] \oplus [+0.35, +0.42]$
$\varepsilon_{e\tau}^{u,V}$	$[-0.076, +0.11]$	$[-0.12, +0.11]$	$\varepsilon_{e\mu}^{u,V}$	$[-0.044, +0.0049]$
$\varepsilon_{\mu\tau}^{u,V}$	$[-0.0077, +0.0042]$	$[-0.0077, +0.0083]$	$\varepsilon_{e\tau}^{d,V}$	$[-0.079, +0.11]$
$\varepsilon_{ee}^{d,V} - \varepsilon_{\mu\mu}^{d,V}$	$[-0.069, +0.38]$	$[-1.3, -0.91] \oplus [-0.072, +0.38]$	$\varepsilon_{\mu\mu}^{d,V}$	$[-0.040, +0.038] \oplus [+0.31, +0.39]$
$\varepsilon_{\tau\tau}^{d,V} - \varepsilon_{\mu\mu}^{d,V}$	$[-0.0058, +0.018]$	$[-0.029, +0.019]$	$\varepsilon_{\tau\tau}^{d,V}$	$[-0.041, +0.043] \oplus [+0.31, +0.39]$
$\varepsilon_{e\mu}^{d,V}$	$[-0.058, +0.014]$	$[-0.058, +0.098]$	$\varepsilon_{e\mu}^{d,V}$	$[-0.054, +0.0045]$
$\varepsilon_{e\tau}^{d,V}$	$[-0.079, +0.11]$	$[-0.16, +0.11]$	$\varepsilon_{e\tau}^{d,V}$	$[-0.051, +0.11]$
$\varepsilon_{\mu\tau}^{d,V}$	$[-0.0087, +0.0051]$	$[-0.0087, +0.015]$	$\varepsilon_{\mu\tau}^{d,V}$	$[-0.0075, +0.0046]$

Coloma et al, JHEP08, 032 (2023) [arXiv:2305.07698 [hep-ph]]

How to parametrize the Non-Unitary mixing matrix?

How many free parameters (for oscillation) we have for U if Unitarity is not assumed?

$$18 - 3 - 2 = 13 \text{ free parameters}$$

3 phase can be removed by redefinition of charged lepton fields

2 Majorana phases by relaxing normalisation (3) and closure (6) conditions

$$\text{or } 4 + 9 = 13 \text{ free parameters}$$

Non-Unitarity U can be parametrised, e.g., as,

$$U = \begin{bmatrix} |U_{e1}| & |U_{e2}|e^{i\phi_{e2}} & |U_{e3}|e^{i\phi_{e3}} \\ |U_{\mu1}| & |U_{\mu2}| & |U_{\mu3}| \\ |U_{\tau1}| & |U_{\tau2}|e^{i\phi_{\tau2}} & |U_{\tau3}|e^{i\phi_{\tau3}} \end{bmatrix}$$

Phenomenological “equivalence” between NSI and Non-unitarity

production and detection NSI can be mapped NU effect as

$$\varepsilon_{\beta\alpha}^{s*} = \varepsilon_{\alpha\beta}^d = \alpha_{ij} \quad (\alpha, \beta = e, \mu, \tau \rightarrow i, j = 1, 2, 3)$$

propagation NSI can be mapped NU effect as

$$\begin{aligned} \varepsilon_{ee} &= -(1 - \alpha_{11}), & \varepsilon_{\mu\mu} &= -(1 - \alpha_{22}), & \varepsilon_{\tau\tau} &= -(1 - \alpha_{33}), \\ \varepsilon_{e\mu} &= \alpha_{21}^*/2, & \varepsilon_{e\tau} &= \alpha_{31}^*/2, & \varepsilon_{\mu\tau} &= \alpha_{32}^*/2 \end{aligned}$$

Blennow et al, JHEP04, 153(2017) [arXiv:1609.08637 [hep-ph]]