

# Neutrinos and Dark Matter

Carlos A. Vaquera-Araujo

CONACYT - DCI Universidad de Guanajuato - DCPIHEP

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# Outline

- 1 BSM physics and Neutrino Mass
- 2 New Ideas on Neutrino Masses and DM candidates
- 3 Conclusions

# BSM physics and Neutrino Mass

# Neutrinos in the SM

In the SM neutrinos are **massless**

- Minimal field content: No right-handed neutrinos (SM Singlets)
- Only renormalizable interactions
- Accidental Lepton number  $L$  conservation.

## Neutrino solar problem

- Deficit of solar neutrinos reaching the earth (only detected approx. 1/3 of the expected)
- Solution: Neutrinos **Oscillate**
- $\Rightarrow$  Neutrinos are **Massive**

## Neutrino Oscillations

### Two Inequivalent bases: Mass vs Flavor

$$\nu_\ell = U_{\ell j} \nu_j, \quad \ell = e, \mu, \tau, \quad j = 1, 2, 3, \dots$$

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13} e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13} e^{i\delta} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & e^{i\frac{\phi_2}{2}} & 0 \\ 0 & 0 & e^{i\frac{\phi_3}{2}} \end{pmatrix}$$

with  $c_{ij} \equiv \cos \theta_{ij}$  and  $s_{ij} \equiv \sin \theta_{ij}$ .

$$P(\nu_\alpha \rightarrow \nu_\beta) = \delta_{\alpha\beta} - 4 \sum_{i>j} \text{Re}(U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*) \sin^2\left(\Delta m_{ij}^2 \frac{L}{4E}\right) + 2 \sum_{i>j} \text{Im}(U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*) \sin\left(\Delta m_{ij}^2 \frac{L}{2E}\right)$$

where  $\Delta m_{ij}^2 = m_i^2 - m_j^2$ .

## Current Status: De Salas et al. 2006.11237 [hep-ph]

parameter	best fit $\pm 1\sigma$	$2\sigma$ range	$3\sigma$ range
$\Delta m_{21}^2 [10^{-5} \text{eV}^2]$	$7.50^{+0.22}_{-0.20}$	7.12–7.93	6.94–8.14
$ \Delta m_{31}^2  [10^{-3} \text{eV}^2]$ (NO)	$2.55^{+0.02}_{-0.03}$	2.49–2.60	2.47–2.63
$ \Delta m_{31}^2  [10^{-3} \text{eV}^2]$ (IO)	$2.45^{+0.02}_{-0.03}$	2.39–2.50	2.37–2.53
$\sin^2 \theta_{12}/10^{-1}$	$3.18 \pm 0.16$	2.86–3.52	2.71–3.69
$\theta_{12}/^\circ$	$34.3 \pm 1.0$	32.3–36.4	31.4–37.4
$\sin^2 \theta_{23}/10^{-1}$ (NO)	$5.74 \pm 0.14$	5.41–5.99	4.34–6.10
$\theta_{23}/^\circ$ (NO)	$49.26 \pm 0.79$	47.37–50.71	41.20–51.33
$\sin^2 \theta_{23}/10^{-1}$ (IO)	$5.78^{+0.10}_{-0.17}$	5.41–5.98	4.33–6.08
$\theta_{23}/^\circ$ (IO)	$49.46^{+0.60}_{-0.97}$	47.35–50.67	41.16–51.25
$\sin^2 \theta_{13}/10^{-2}$ (NO)	$2.200^{+0.069}_{-0.062}$	2.069–2.337	2.000–2.405
$\theta_{13}/^\circ$ (NO)	$8.53^{+0.13}_{-0.12}$	8.27–8.79	8.13–8.92
$\sin^2 \theta_{13}/10^{-2}$ (IO)	$2.225^{+0.064}_{-0.070}$	2.086–2.356	2.018–2.424
$\theta_{13}/^\circ$ (IO)	$8.58^{+0.12}_{-0.14}$	8.30–8.83	8.17–8.96
$\delta/\pi$ (NO)	$1.08^{+0.13}_{-0.12}$	0.84–1.42	0.71–1.99
$\delta/^\circ$ (NO)	$194^{+24}_{-22}$	152–255	128–359
$\delta/\pi$ (IO)	$1.58^{+0.15}_{-0.16}$	1.26–1.85	1.11–1.96
$\delta/^\circ$ (IO)	$284^{+26}_{-28}$	226–332	200–353

Two possible scenarios:

- Normal Ordering:  $m_1 < m_2 < m_3$
- Inverted Ordering:  $m_3 < m_1 < m_2$

Two possible choices for the neutrino nature:

- Dirac:  $m\bar{\nu}_L\nu_R + \text{h.c.}$
- Majorana:  $\frac{m}{2}\bar{\nu}_L\nu_L^c + \text{h.c.}$



# Neutrino Mass Generation Mechanisms

## Neutrinos in the SM

Field	$SU(3)_c$	$SU(2)_L$	$U(1)_Y$
$Q_{iL}$	<b>3</b>	<b>2</b>	1/6
$u_{iR}$	<b>3</b>	<b>1</b>	2/3
$d_{iR}$	<b>3</b>	<b>1</b>	-1/3
$L_{iL}$	<b>1</b>	<b>2</b>	-1/2
$e_{iR}$	<b>1</b>	<b>1</b>	-1
$H$	<b>1</b>	<b>2</b>	1/2

$$Q_{iL} = \begin{pmatrix} u \\ d \end{pmatrix}_{iL}, \quad L_{iL} = \begin{pmatrix} \nu \\ e \end{pmatrix}_{iL}, \quad H = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix}, \quad i = 1, 2, 3.$$

$D = 5$  Weinberg Operator

$$\mathcal{L} \supset -\frac{y^\nu}{\Lambda} (\bar{L}_L \tilde{H}) (\tilde{H}^T L_L^c) + \text{h.c.} \rightarrow -\frac{m_\nu}{2} \bar{\nu}_L \nu_L^c + \text{h.c.}$$

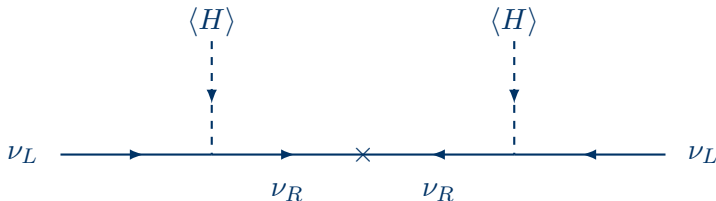


- Simplest option and unique for  $D = 5$
- No new fields needed beyond the SM content
- Majorana neutrino
- Effective theory: Non renormalizable

Seesaw (type I) Minkowski, Gell-Mann, Ramond, Slansky, Yanagida, Mohapatra, Senjanovic, Schechter, Valle

SM +  $\nu_{iR}$ : two new mass terms

$$\mathcal{L} \supset -y^\nu \bar{L}_L \tilde{H} \nu_R - \frac{M}{2} \bar{\nu}_R \nu_R^c + \text{h.c.} \rightarrow -\frac{1}{2} (\bar{\nu}_L \quad \bar{\nu}_R^c) \begin{pmatrix} 0 & m \\ m^T & M \end{pmatrix} \begin{pmatrix} \nu_L^c \\ \nu_R \end{pmatrix} + \text{h.c.}$$



- Majorana Neutrinos
- If  $M \gg m$ , naturally light active neutrinos:  $m_{\text{light}} \sim -mM^{-1}m^T$ , and heavy mostly right-handed states  $m_{\text{heavy}} \sim M$

## Scotogenic model (Ma, 0601225[hep-ph])

Two BSM ingredients:

- Inert scalar isodoublet  $\eta \sim (\mathbf{1}, \mathbf{2}, 1/2)$
- Singlet fermions  $S_{iR} \sim (\mathbf{1}, \mathbf{1}, 0)$

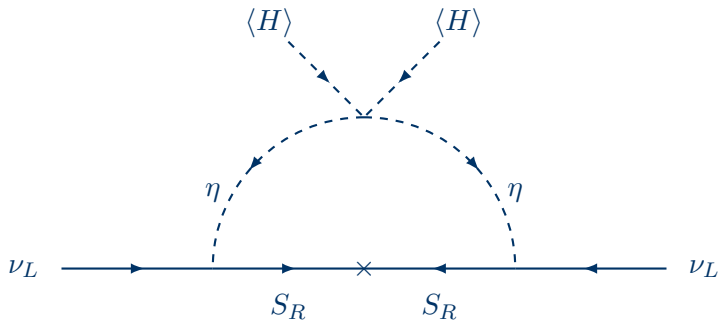
Extra global symmetry  $\mathbb{Z}_2$ :  $\eta \rightarrow -\eta$ ,  $S_R \rightarrow -S_R$ .

Relevant terms

$$\mathcal{L} \supset -h\bar{L}_L\tilde{\eta}S_R - \frac{M}{2}\bar{S}_R S_R^c + \text{h.c.} \quad V(H, \eta) \supset \frac{\lambda_5}{2}(H^\dagger\eta)^2 + \text{h.c.}$$

- No tree level neutrino mass term

## Radiative mechanism



$$m_{ij}^{\text{light}} = \sum_k \frac{h_{ik} h_{jk} m_{S_k}}{32\pi^2} \left[ \frac{m_R^2}{m_R^2 - m_{S_k}^2} \log \left( \frac{m_R^2}{m_{S_k}^2} \right) - \frac{m_I^2}{m_I^2 - m_{S_k}^2} \log \left( \frac{m_I^2}{m_{S_k}^2} \right) \right].$$

## Scotogenic model features

- Majorana neutrinos
- Naturally small masses through loop suppression
- Low scale mediators
- **WIMP Dark Matter candidate**: lightest electrically neutral  $\mathbb{Z}_2$ -odd state
- Ad hoc stabilizing global symmetry  $\mathbb{Z}_2$ .

## New Ideas on Neutrino Masses and DM candidates

- $B - L$  Scotogenic Dirac Neutrinos
- $3 - 3 - 1 - 1$  Models
- Extra-dimensional Models



# $B - L$ Scotogenic Dirac Neutrinos

- J. Leite, [América Morales](#), J.W.F. Valle, CAV-A 2003.02950 [hep-ph]
- Extended Gauge Symmetry  $SU(3)_c \times SU(2)_W \times U(1)_Y \times U(1)_{B-L}$
  - Unbroken  $B - L$  symmetry stabilizing DM
  - Dirac Neutrinos
  - Massive  $Z'$  by Stueckelberg mechanism

Fields	$SU(3)_C$	$SU(2)_L$	$U(1)_Y$	$U(1)_{B-L}$	$\mathbb{Z}_2$
$\nu_{iR}$	1	1	0	-1	-
$S_{iL}$	1	1	0	$2n$	+
$S_{iR}$	1	1	0	$2n$	+
$\eta$	1	2	1/2	$2n+1$	+
$\sigma$	1	1	0	$2n+1$	-

- $n(\neq 0) \in \mathbb{Z}$
- $U(1)_{B-L}$  promoted to gauge symmetry through the inclusion of three left-handed neutrinos with  $B - L = -1$
- Auxiliary discrete  $\mathbb{Z}_2$  that forbids tree level Dirac masses is softly broken by the trilinear term in the scalar potential  $\frac{\mu_3}{\sqrt{2}}(\eta^\dagger H \sigma + h.c.)$ .

## Stueckelberg Mechanism

$$\mathcal{L}_{\text{kin}}^{\text{St}} = -\frac{1}{4}Z'^{\mu\nu}Z'_{\mu\nu} + \frac{1}{2}(M_{Z'}Z'^{\mu} - \partial^{\mu}A)^2,$$

is invariant under the  $U(1)_{B-L}$  gauge transformations

$$\begin{aligned}Z'^{\mu} &\rightarrow Z'^{\mu} + \partial^{\mu}\Lambda, \\ A &\rightarrow A + M_{Z'}\Lambda,\end{aligned}$$

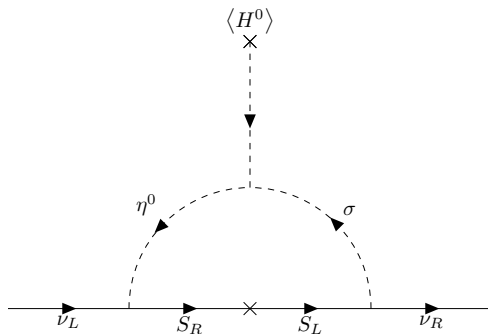
where  $A$  is a scalar Stueckelberg compensator and  $Z'^{\mu\nu} = \partial^{\mu}Z'^{\nu} - \partial^{\nu}Z'^{\mu}$ . Upon gauge-fixing

$$\mathcal{L}_{\text{fg}}^{\text{St}} = -\frac{1}{2\xi}(\partial_{\mu}Z'^{\mu} + M_{Z'}\xi A)^2,$$

the  $Z'$  boson acquires mass  $M_{Z'}$  and the compensator  $A$  decouples:

$$\mathcal{L}_{\text{kin}}^{\text{St}} + \mathcal{L}_{\text{fg}}^{\text{St}} = -\frac{1}{4}Z'^{\mu\nu}Z'_{\mu\nu} + \frac{1}{2}M_{Z'}^2Z'^{\mu}Z'_{\mu} - \frac{1}{2\xi}(\partial_{\mu}Z'^{\mu})^2 + \frac{1}{2}\partial^{\mu}A\partial_{\mu}A - \frac{1}{2}M_{Z'}^2\xi A^2.$$

## Neutrino masses



$$(m_\nu)_{ij} = \frac{\sin(2\theta)}{32\pi^2} \sum_k y_{ik}^\nu h_{kj} m_{S_k} \left[ \frac{m_{\varphi_1}^2}{m_{\varphi_1}^2 - m_{S_k}^2} \ln \frac{m_{\varphi_1}^2}{m_{S_k}^2} - \frac{m_{\varphi_2}^2}{m_{\varphi_2}^2 - m_{S_k}^2} \ln \frac{m_{\varphi_2}^2}{m_{S_k}^2} \right].$$

## 3 – 3 – 1 – 1 Models

S.K. Kang, O. Popov, R. Srivastava, J.W.F. Valle, CAV-A 1902.05966  
[hep-ph]

- Extended Gauge Symmetry  $SU(3)_c \times SU(3)_W \times U(1)_X \times U(1)_N$
- First scotogenic model in this framework
- Majorana neutrinos
- DM stabilized by Matter Parity in a non-supersymmetric context

## 3 – 3 – 1 Models

Gauge symmetry

$$SU(3)_c \otimes SU(3)_W \otimes U(1)_X$$

One additional diagonal generator

$$T_8 = \frac{\lambda_8}{2} = \frac{1}{2\sqrt{3}} \text{diag}(1, 1, -2)$$

⇒ Different models based on Hypercharge embedding

$$Y = \beta T_8 + X$$

Basic Fields (arbitrary  $\beta$ )

$$\psi_{aL} \equiv \begin{pmatrix} \nu_{aL} \\ \ell_{aL} \\ k_{aL} \end{pmatrix} \sim \mathbf{3}, \quad Q_{3L} \equiv \begin{pmatrix} u_{3L} \\ d_{3L} \\ j_{3L} \end{pmatrix} \sim \mathbf{3}, \quad Q_{\alpha L} \equiv \begin{pmatrix} d_{\alpha L} \\ -u_{\alpha L} \\ j_{\alpha L} \end{pmatrix} \sim \bar{\mathbf{3}},$$

$$\nu_{aR}, \ell_{aR}, k_{aR}, u_{aR}, d_{aR}, j_{aR} \sim \mathbf{1}, \quad a = 1, 2, 3, \quad \alpha = 1, 2.$$

- Left handed leptons go into triplets of  $SU(3)_L$
- Two families of left-handed quarks go into anti-triplets
- To cancel gauge anomalies, the third family of left handed quarks transform as a triplet.
- One can exchange triplets for anti-triplets and viceversa to obtain an almost equivalent model.

## Original SVS (Singer-Valle-Schechter) model

Field	331 rep	Components	Lepton number ?
$\psi_{aL}$	$(\mathbf{1}, \mathbf{3}, -\frac{1}{3})$	$((\nu_{aL}, \ell_{aL}), \nu_{aR}^c)^T$	$(1, 1, -1)^T$
$\ell_{aR}$	$(\mathbf{1}, \mathbf{1}, -1)$	$\ell_{aR}$	1
$Q_{\alpha L}$	$(\mathbf{3}, \bar{\mathbf{3}}, 0)$	$((d_{\alpha}, -u_{\alpha}), D_{\alpha})^T$	$(0, 0, 2)^T$
$Q_{3L}$	$(\mathbf{3}, \mathbf{3}, \frac{1}{3})$	$((t_L, b_L), U_{3L})^T$	$(0, 0, -2)^T$
$u_{aR}, U_{3R}$	$(\mathbf{3}, \mathbf{1}, \frac{2}{3})$	$u_{aR}, U_{3R}$	0
$d_{aR}, D_{\alpha R}$	$(\mathbf{3}, \mathbf{1}, -\frac{1}{3})$	$d_{aR}, D_{\alpha R}$	0
$\phi_1$	$(\mathbf{1}, \mathbf{3}, \frac{2}{3})$	$((\phi_1^+, \phi_1^0), \tilde{\phi}_1^+)^T$	$(0, 0, -2)^T$
$\phi_{i=2,3}$	$(\mathbf{1}, \mathbf{3}, -\frac{1}{3})$	$((\phi_i^0, \phi_i^-), \tilde{\phi}_i^0)^T$	$(0, 0, -2)^T$



## VEV alignment

$$\langle \phi_1 \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ u \\ 0 \end{pmatrix}, \quad \langle \phi_2 \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} u' \\ 0 \\ 0 \end{pmatrix}, \quad \langle \phi_3 \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ 0 \\ w \end{pmatrix}$$

## SSB pattern

- $w \gg u, u'$ :

$$\begin{aligned} &SU(3)_c \otimes SU(3)_L \otimes U(1)_X \\ &\quad \downarrow w \\ &SU(3)_c \otimes SU(2)_L \otimes U(1)_Y \\ &\quad \downarrow u, u' \\ &SU(3)_c \otimes U(1)_Q \end{aligned}$$

- This minimal SVS model is not viable, as it cannot accommodate the current neutrino oscillation data (Fonseca, Hirsch, 2017).
- Here  $L$  is a combination of  $T_8$  and a global  $U(1)$  symmetry generated by  $\mathcal{L}$  (Tully, Joshi 2001):

$$L = \frac{2}{\sqrt{3}}T_8 + \mathcal{L}, \quad (\text{SVS}).$$

Is it this symmetry consistent?

There is a class of models based on 3-3-1 where Lepton number is consistently defined: Those with gauged  $\mathcal{L}$  (Dong,Tham,Huong, 2013), known as 3-3-1-1 models.

## Scotogenic 3311 (Kang, Popov, Srivastava, Valle, V-A, 2019)

Field	$SU(3)_c$	$SU(3)_L$	$U(1)_X$	$U(1)_N$	$M_P = (-1)^{3(B-L)+2s}$
$q_{iL}$	<b>3</b>	$\bar{\mathbf{3}}$	<b>0</b>	<b>0</b>	$(++-)^T$
$q_{3L}$	<b>3</b>	<b>3</b>	1/3	2/3	$(++-)^T$
$u_{aR}$	<b>3</b>	<b>1</b>	2/3	1/3	+
$d_{aR}$	<b>3</b>	<b>1</b>	-1/3	1/3	+
$U_{3R}$	<b>3</b>	<b>1</b>	2/3	4/3	-
$D_{iR}$	<b>3</b>	<b>1</b>	-1/3	-2/3	-
$l_{aL}$	<b>1</b>	<b>3</b>	-1/3	-2/3	$(++-)^T$
$e_{aR}$	<b>1</b>	<b>1</b>	-1	-1	+
$\nu_{iR}$	<b>1</b>	<b>1</b>	0	-4	-
$\nu_{3R}$	<b>1</b>	<b>1</b>	0	5	+
$F_{aL,R}$	<b>1</b>	<b>3</b>	-1/3	-1/3	$(--+)$

Field	$SU(3)_c$	$SU(3)_L$	$U(1)_X$	$U(1)_N$	$M_P = (-1)^{3(B-L)+2s}$
$\eta$	<b>1</b>	<b>3</b>	$-1/3$	$1/3$	$(++-)^T$
$\rho$	<b>1</b>	<b>3</b>	$2/3$	$1/3$	$(++-)^T$
$\chi$	<b>1</b>	<b>3</b>	$-1/3$	$-2/3$	$(--+)^T$
$\phi$	<b>1</b>	<b>1</b>	0	2	+
$S$	<b>1</b>	<b>1</b>	0	$2/3$	+
$\sigma$	<b>1</b>	<b>1</b>	0	$1/3$	-
$\Omega$	<b>1</b>	<b>6</b>	$2/3$	$2/3$	$\begin{pmatrix} + & + & - \\ + & + & - \\ - & - & + \end{pmatrix}$

## Yukawa Interactions

$$\mathcal{L}^{\text{Yuk}} \supset \bar{l}_{aL}^i Y_e^{ab} e_{bR} \rho_i + \bar{F}_{aR}^i Y_1^{ab} l_{ibL} \sigma + \bar{F}_{aL} m_F^{ab} F_{bR} \\ + F_{iaL,R} Y_{2L,R}^{ab} F_{jbL,R} \Omega^{ij} + \text{h.c.},$$

## VEV alignment

$$\langle \eta \rangle = \frac{1}{\sqrt{2}} (v_1, 0, 0)^T, \quad \langle \rho \rangle = \frac{1}{\sqrt{2}} (0, v_2, 0)^T, \quad \langle \chi \rangle = (0, 0, w)^T, \quad \langle \phi \rangle = \frac{1}{\sqrt{2}} \Lambda,$$

$$\langle S \rangle = v_s, \quad \langle \sigma \rangle = 0, \quad \langle \Omega \rangle = \begin{pmatrix} w_1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & w_2 \end{pmatrix}.$$

## Spontaneous symmetry breaking pattern

$$SU(3)_C \times SU(3)_L \times U(1)_X \times U(1)_N$$

$$\downarrow w, \Lambda, w_2, v_s$$

$$SU(3)_C \times SU(2)_L \times U(1)_Y \times M_P$$

$$\downarrow v_1, v_2, w_1$$

$$SU(3)_C \times U(1)_Q \times M_P.$$

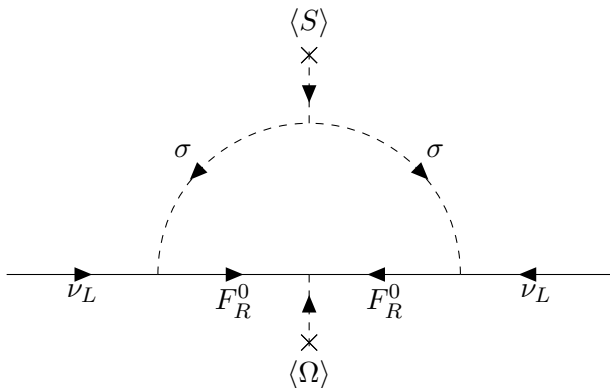
- $\phi \sim (1, 1, 0, 2)$  breaks spontaneously  $B - L$  by two units.
- After SSB a remnant discrete symmetry is preserved

$$M_P = (-1)^{3(B-L)+2s}$$

Matter-parity without invoking supersymmetry!

## Neutrino mass relevant terms

$$\mathcal{L}_{m\nu} = \overline{F}_{aR}^i Y_1^{ab} l_{ibL} \sigma + F_{iaR} Y_{2R}^{ab} F_{jbR} \Omega^{ij} + \mu_2 \sigma^2 S^* + \text{h.c.}$$



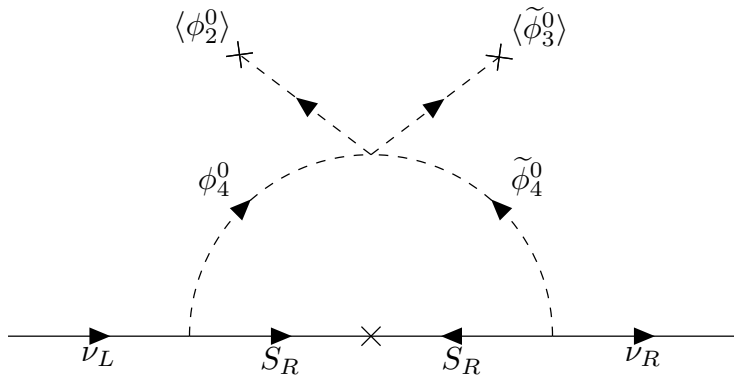
J. Leite, [América Morales](#), J.W.F. Valle, CAV-A 2005.03600 [hep-ph]

- $3 - 3 - 1 - 1$  version of our previous  $B - L$  extension
- Gauge  $B - L$  preserved after EWSB stabilizes WIMP DM
- Dirac Neutrinos
- Rich DM phenomenology.

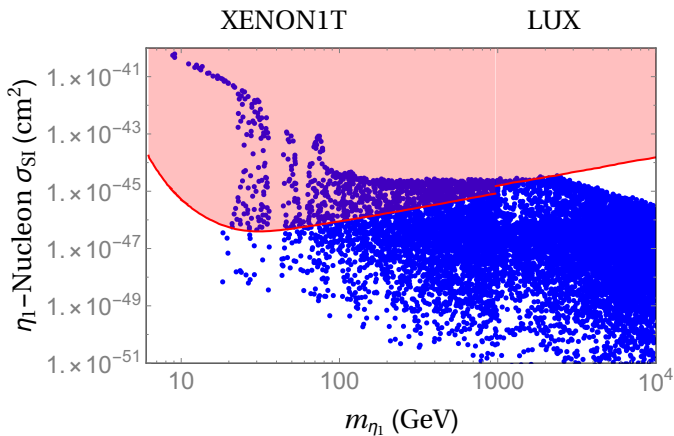


Field	3-3-1-1 rep	Components	$B - L$	$U(1)_{PQ}$
$Q_{\alpha L}$	$(\mathbf{3}, \mathbf{3}, 0, -\frac{1}{3})$	$((u_{\alpha L}, d_{\alpha L}), D_{\alpha L})^T$	$(\frac{1}{3}, \frac{1}{3}, -\frac{5}{3})^T$	1
$Q_{3L}$	$(\mathbf{3}, \mathbf{3}^*, \frac{1}{3}, 1)$	$((b_L, -t_L), U_{3L})^T$	$(\frac{1}{3}, \frac{1}{3}, \frac{7}{3})^T$	1
$u_{aR}$	$(\mathbf{3}, \mathbf{1}, \frac{2}{3}, \frac{1}{3})$	$u_{aR}$	$\frac{1}{3}$	4
$U_{3R}$	$(\mathbf{3}, \mathbf{1}, \frac{2}{3}, \frac{7}{3})$	$U_{3R}$	$\frac{7}{3}$	4
$d_{aR}$	$(\mathbf{3}, \mathbf{1}, -\frac{1}{3}, \frac{1}{3})$	$d_{aR}$	$\frac{1}{3}$	-2
$D_{\alpha R}$	$(\mathbf{3}, \mathbf{1}, -\frac{1}{3}, -\frac{5}{3})$	$D_{\alpha R}$	$-\frac{5}{3}$	-2
$\psi_{aL}$	$(\mathbf{1}, \mathbf{3}^*, -\frac{1}{3}, -\frac{1}{3})$	$((e_{aL}, -\nu_{aL}), \nu_{aR}^c)^T$	$(-1, -1, +1)^T$	-3
$e_{aR}$	$(\mathbf{1}, \mathbf{1}, -1, -1)$	$e_{aR}$	-1	-6
$S_{aR}$	$(\mathbf{1}, \mathbf{1}, 0, 0)$	$S_{aR}$	0	0
$\Phi_1$	$(\mathbf{1}, \mathbf{3}^*, \frac{2}{3}, \frac{2}{3})$	$((\phi_1^0, -\phi_1^+), \tilde{\phi}_1^+)^T$	$(0, 0, 2)^T$	3
$\Phi_2$	$(\mathbf{1}, \mathbf{3}^*, -\frac{1}{3}, \frac{2}{3})$	$((\phi_2^-, -\phi_2^0), \tilde{\phi}_2^0)^T$	$(0, 0, 2)^T$	-3
$\Phi_3$	$(\mathbf{1}, \mathbf{3}^*, -\frac{1}{3}, -\frac{4}{3})$	$((\phi_3^-, -\phi_3^0), \tilde{\phi}_3^0)^T$	$(-2, -2, 0)^T$	-3
$\Phi_4$	$(\mathbf{1}, \mathbf{3}^*, -\frac{1}{3}, -\frac{1}{3})$	$((\phi_4^-, -\phi_4^0), \tilde{\phi}_4^0)^T$	$(-1, -1, 1)^T$	-3

## Neutrino Mass



## Wimp Dark matter

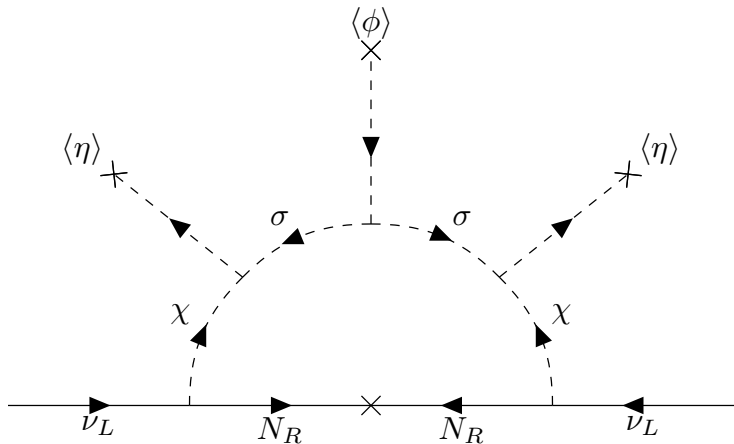


A.E. Cárcamo Hernández, J.W.F. Valle, CAV-A 2006.06009 [hep-ph]

- Minimal  $3 - 3 - 1 - 1$  scotogenic model
- Majorana Neutrinos
- DM stabilized by Matter Parity

Field	SU(3) <sub>c</sub>	SU(3) <sub>L</sub>	U(1) <sub>X</sub>	U(1) <sub>N</sub>	Q	$M_P = (-1)^{3(B-L)+2s}$
$q_{iL}$	<b>3</b>	$\bar{\mathbf{3}}$	<b>0</b>	<b>0</b>	$(-\frac{1}{3}, \frac{2}{3}, -\frac{1}{3})^T$	$(++-)^T$
$q_{3L}$	<b>3</b>	<b>3</b>	$\frac{1}{3}$	$\frac{2}{3}$	$(\frac{2}{3}, -\frac{1}{3}, \frac{2}{3})^T$	$(++-)^T$
$u_{aR}$	<b>3</b>	<b>1</b>	$\frac{2}{3}$	$-\frac{1}{3}$	$\frac{1}{3}$	+
$d_{aR}$	<b>3</b>	<b>1</b>	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	+
$U_{3R}$	<b>3</b>	<b>1</b>	$\frac{2}{3}$	$\frac{4}{3}$	$\frac{2}{3}$	-
$D_{iR}$	<b>3</b>	<b>1</b>	$-\frac{1}{3}$	$-\frac{2}{3}$	$-\frac{1}{3}$	-
$l_{aL}$	<b>1</b>	<b>3</b>	$-\frac{1}{3}$	$-\frac{2}{3}$	$(0, -1, 0)^T$	$(++-)^T$
$e_{aR}$	<b>1</b>	<b>1</b>	-1	-1	-1	+
$\nu_{iR}$	<b>1</b>	<b>1</b>	<b>0</b>	-4	<b>0</b>	-
$\nu_{3R}$	<b>1</b>	<b>1</b>	<b>0</b>	5	<b>0</b>	+
$N_{aR}$	<b>1</b>	<b>1</b>	<b>0</b>	<b>0</b>	<b>0</b>	-
$\eta$	<b>1</b>	<b>3</b>	$-\frac{1}{3}$	$\frac{1}{3}$	$(0, -1, 0)^T$	$(++-)^T$
$\rho$	<b>1</b>	<b>3</b>	$\frac{2}{3}$	$\frac{1}{3}$	$(1, 0, 1)^T$	$(++-)^T$
$\chi$	<b>1</b>	<b>3</b>	$-\frac{1}{3}$	$-\frac{2}{3}$	$(0, -1, 0)^T$	$(--)^T$
$\phi$	<b>1</b>	<b>1</b>	<b>0</b>	<b>2</b>	<b>0</b>	+
$\sigma$	<b>1</b>	<b>1</b>	<b>0</b>	<b>1</b>	<b>0</b>	-

## Neutrino Mass



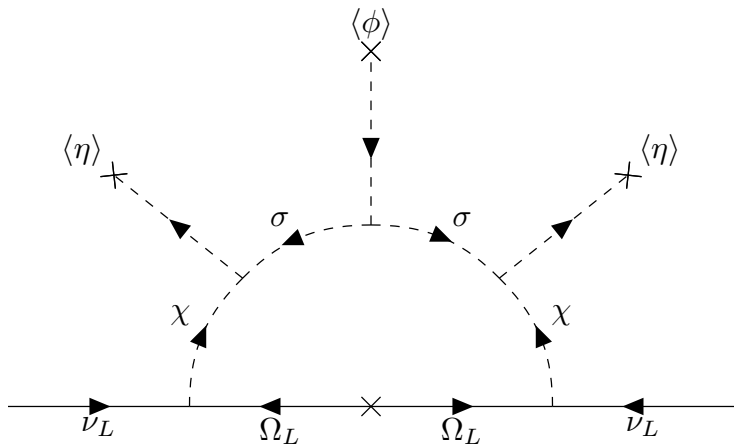
A.E. Cárcamo Hernández, C. Hati, S. Kovalenko, J.W.F. Valle, CAV-A  
2109.05029 [hep-ph]

- Scotogenic  $3 - 3 - 1 - 1$  with octets
- Majorana neutrinos
- DM stabilized by Matter Parity
- Gauge coupling unification

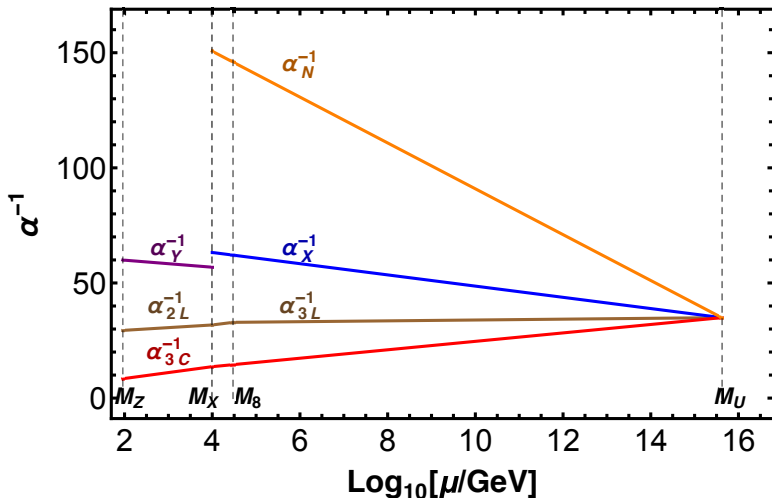
Field	SU(3) <sub>c</sub>	SU(3) <sub>L</sub>	U(1) <sub>X</sub>	U(1) <sub>N</sub>	Q	$M_P = (-1)^{3(B-L)+2s}$
$q_{iL}$	<b>3</b>	$\bar{\mathbf{3}}$	<b>0</b>	<b>0</b>	$(-\frac{1}{3}, \frac{2}{3}, -\frac{1}{3})^T$	$(+ + -)^T$
$q_{3L}$	<b>3</b>	<b>3</b>	<b>1</b>	<b>2</b>	$(\frac{2}{3}, -\frac{1}{3}, \frac{2}{3})^T$	$(+ + -)^T$
$u_{aR}$	<b>3</b>	<b>1</b>	$-\frac{1}{3}$	$-\frac{1}{3}$	$\frac{1}{3}$	+
$d_{aR}$	<b>3</b>	<b>1</b>	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	+
$U_{3R}$	<b>3</b>	<b>1</b>	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{1}{3}$	-
$D_{iR}$	<b>3</b>	<b>1</b>	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	-
$l_{aL}$	<b>1</b>	<b>3</b>	$-\frac{1}{3}$	$-\frac{1}{3}$	$(0, -1, 0)^T$	$(+ + -)^T$
$e_{aR}$	<b>1</b>	<b>1</b>	-1	-1	-1	+
$\nu_{iR}$	<b>1</b>	<b>1</b>	0	-4	0	-
$\nu_{3R}$	<b>1</b>	<b>1</b>	0	5	0	+
$\Omega_{aL}$	<b>1</b>	<b>8</b>	0	0	$\begin{pmatrix} 0 & 1 & 0 \\ -1 & 0 & -1 \\ 0 & 1 & 0 \end{pmatrix}$	$\begin{pmatrix} - & - & + \\ - & - & + \\ + & + & - \end{pmatrix}$
$\eta$	<b>1</b>	<b>3</b>	$-\frac{1}{3}$	$\frac{1}{3}$	$(0, -1, 0)^T$	$(+ + -)^T$
$\rho$	<b>1</b>	<b>3</b>	$\frac{1}{3}$	$-\frac{1}{3}$	$(1, 0, 1)^T$	$(+ + -)^T$
$\chi$	<b>1</b>	<b>3</b>	$-\frac{1}{3}$	$-\frac{1}{3}$	$(0, -1, 0)^T$	$(- - +)^T$
$\phi$	<b>1</b>	<b>1</b>	0	2	0	+
$\sigma$	<b>1</b>	<b>1</b>	0	1	0	-



## Neutrino Mass



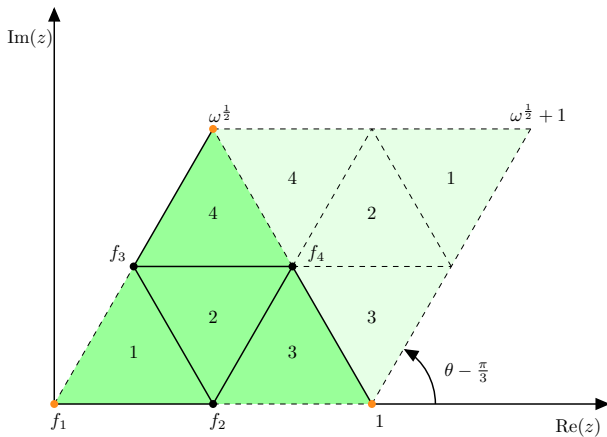
## Gauge Coupling Unification



# Extra-dimensional Models

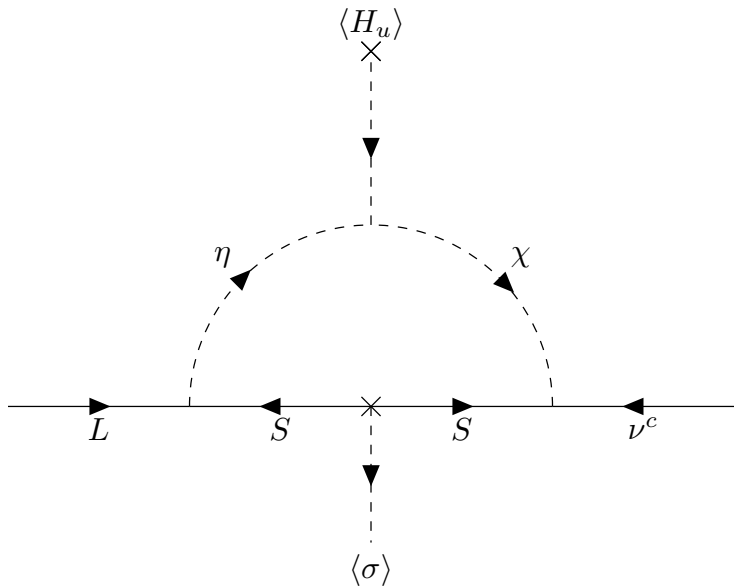
F. de Anda, I. Antoniadis, J.W.F. Valle, CAV-A 2007.10402 [hep-ph]

- Orbifolded  $6D$  model with remnant  $A_4$  flavor symmetry
- Dirac Neutrinos
- Realistic model for quark and lepton masses and mixings.

$M^6 \rightarrow M^4 \times (T^2/\mathbb{Z}_2)$  orbifold compactification


Field	$SU(3)$	$SU(2)$	$U(1)$	$A_4$	$\mathbb{Z}_3$	$\mathbb{Z}_2$	Localization
$L$	$\mathbf{1}$	$\mathbf{2}$	$-1/2$	$\mathbf{3}$	$\omega^2$	1	Brane
$d^c$	$\bar{\mathbf{3}}$	$\mathbf{1}$	$1/3$	$\mathbf{3}$	$\omega$	1	Brane
$e^c$	$\mathbf{1}$	$\mathbf{1}$	1	$\mathbf{3}$	$\omega$	1	Brane
$Q$	$\mathbf{3}$	$\mathbf{2}$	$1/6$	$\mathbf{3}$	$\omega^2$	1	Brane
$u^c$	$\bar{\mathbf{3}}$	$\mathbf{1}$	$-2/3$	$\mathbf{3}$	$\omega^2$	1	Brane
$\nu_i^c$	$\mathbf{1}$	$\mathbf{1}$	0	$\mathbf{1}$	1	1	Bulk
$T^c$	$\bar{\mathbf{3}}$	$\mathbf{1}$	$-2/3$	$\mathbf{1}$	$\omega$	1	Brane
$T$	$\mathbf{3}$	$\mathbf{1}$	$2/3$	$\mathbf{1}$	$\omega^2$	1	Brane
$H_u$	$\mathbf{1}$	$\mathbf{2}$	$1/2$	$\mathbf{3}$	$\omega^2$	1	Brane
$H_d$	$\mathbf{1}$	$\mathbf{2}$	$-1/2$	$\mathbf{3}$	1	1	Brane
$\sigma$	$\mathbf{1}$	$\mathbf{1}$	0	$\mathbf{3}$	$\omega$	1	Brane
$S$	$\mathbf{1}$	$\mathbf{1}$	0	$\mathbf{3}$	$\omega$	-1	Brane
$\eta$	$\mathbf{1}$	$\mathbf{2}$	$-1/2$	$\mathbf{3}$	1	-1	Brane
$\chi$	$\mathbf{1}$	$\mathbf{1}$	0	$\mathbf{3}$	$\omega^2$	-1	Brane

## Neutrino Mass



## Prediction: Golden Relation

$$\frac{m_\tau}{\sqrt{m_\mu m_e}} \approx \frac{m_b}{\sqrt{m_s m_d}}.$$

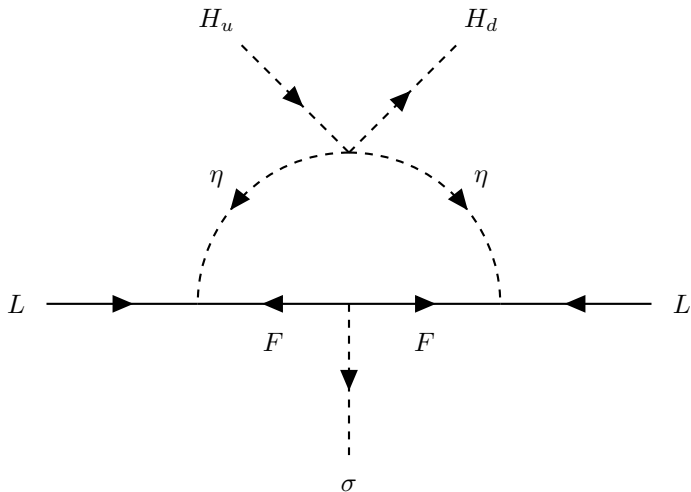
F. de Anda, O. Medina, J.W.F. Valle, CAV-A 2110.06810 [hep-ph]

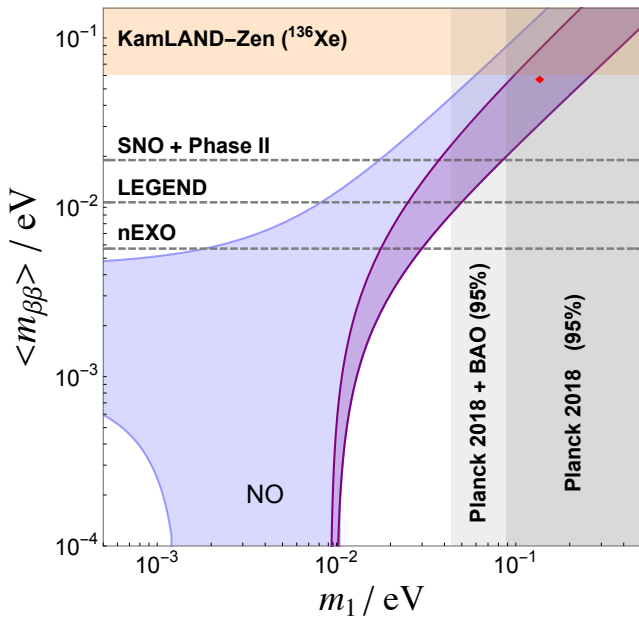
- Orbifolded  $6D$  model with remnant  $A_4$  flavor symmetry
- Majorana neutrinos
- Predictive model for quark and lepton masses and mixings  
 $\chi^2 = 1.96$  .

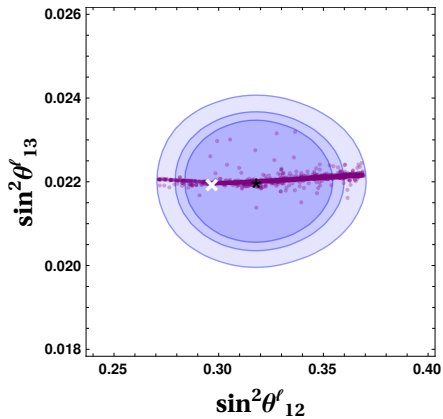
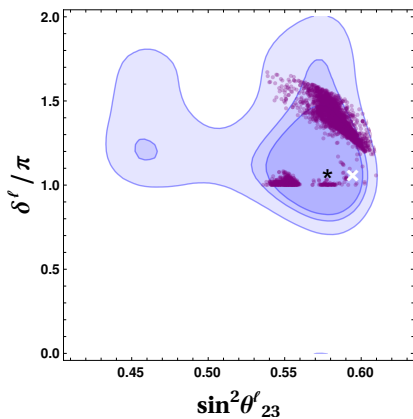


Field	$SU(3)_C$	$SU(2)_L$	$U(1)_Y$	$\mathbb{Z}_4$	$A_4$	Location
$L$	<b>1</b>	<b>2</b>	-1	1	<b>3</b>	Brane
$d^c$	<b>3</b>	<b>1</b>	$2/3$	1	<b>3</b>	Brane
$e^c$	<b>1</b>	<b>1</b>	2	1	<b>3</b>	Brane
$Q$	<b>3</b>	<b>2</b>	$1/3$	1	<b>3</b>	Brane
$u_{1,2,3}^c$	<b>3</b>	<b>1</b>	$-4/3$	-1	$1'', 1', 1$	Bulk
$F$	<b>1</b>	<b>1</b>	0	$i$	<b>3</b>	Brane
$H_u$	<b>1</b>	<b>2</b>	1	-1	<b>3</b>	Brane
$H_d$	<b>1</b>	<b>2</b>	-1	1	<b>3</b>	Brane
$\eta$	<b>1</b>	<b>2</b>	1	$-i$	<b>1</b>	Brane
$\sigma$	<b>1</b>	<b>1</b>	0	-1	<b>3</b>	Bulk

## Neutrino Mass



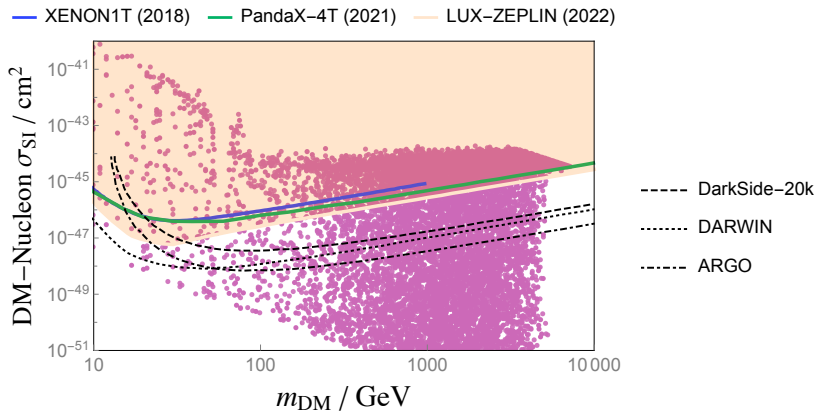


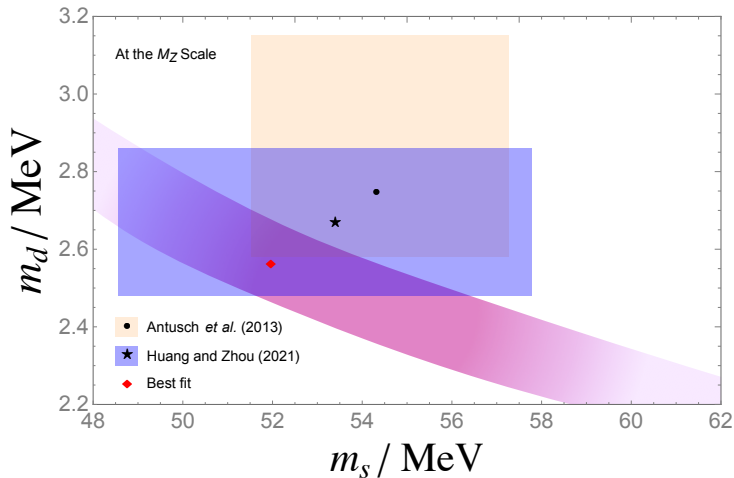


F. de Anda, O. Medina, J.W.F. Valle, CAV-A 2212.09174 [hep-ph]

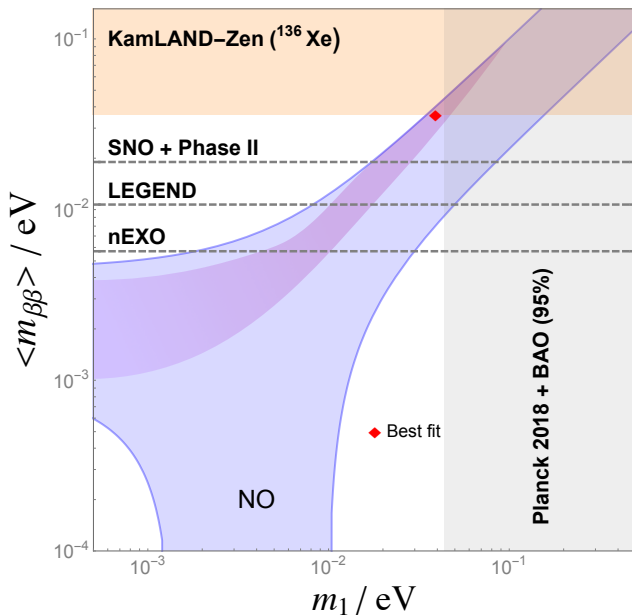
- Orbifolded  $6D$  model with remnant  $A_4$  flavor symmetry
- Majorana neutrinos with Low Scale See Saw
- WIMP Dark matter identified with first Kaluza-Klein excitation of scalar that drives family symmetry breaking and neutrino mass mechanism.
- Predictive model for quark and lepton masses and mixings  $\chi^2 = 1.05$  .

Field	$SU(3)_C$	$SU(2)_L$	$U(1)_Y$	$A_4$	$\mathbb{Z}_2$	$\mathbb{Z}_3$	Localization
$L$	<b>1</b>	<b>2</b>	$-1/2$	<b>3</b>	1	1	Brane
$d^c$	$\bar{\mathbf{3}}$	<b>1</b>	$1/3$	<b>3</b>	1	1	Brane
$e^c$	<b>1</b>	<b>1</b>	1	<b>3</b>	1	1	Brane
$Q$	<b>3</b>	<b>2</b>	$1/6$	<b>3</b>	1	1	Brane
$u_{1,2,3}^c$	$\bar{\mathbf{3}}$	<b>1</b>	$-2/3$	$\mathbf{1}'', \mathbf{1}', \mathbf{1}$	-1	1	Bulk
$\nu^c$	<b>1</b>	<b>1</b>	0	<b>3</b>	-1	$\omega$	Brane
$S$	<b>1</b>	<b>1</b>	0	<b>3</b>	-1	$\omega^2$	Brane
$H_u$	<b>1</b>	<b>2</b>	$1/2$	<b>3</b>	-1	1	Brane
$H_d$	<b>1</b>	<b>2</b>	$-1/2$	<b>3</b>	1	1	Brane
$H_\nu$	<b>1</b>	<b>2</b>	$1/2$	<b>3</b>	-1	$\omega^2$	Brane
$\sigma$	<b>1</b>	<b>1</b>	0	<b>3</b>	1	$\omega^2$	Bulk









# Conclusions

- Scotogenic scenarios for neutrino mass generation and WIMP DM emerge naturally in Gauge extensions of the SM and Extra-dimensional field theories, both for Majorana and Dirac Neutrinos
- DM Stability can be related to a robust Gauge symmetry or a discrete remnant symmetry after SSB.
- Wimp KKDM introduced by the neutrino mass generation mechanism in extra dimensions.

# Thanks