

Study of one-particle spectra at high- p_T at LHC energies

Perturbative and non-perturbative
particle production mechanisms
at LHC energies

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28 September 2010, Mexico City*

1. Motivation

***Jet and hadron production in
proton-proton
and
proton-antiproton collisions***

***--- from RHIC to LHC energies ---
[Exp. data & theory (pQCD)]***

Hard physics: pion production in pp collision at high- p_T

Perturbative QCD calculations in NLO for $p+p \rightarrow \pi + X$ process with finite k_T

NLO : M. Aversa et al. NPB327,105; P. Chiappetta et al. NPB412,3; P. Aurenche et al. NPB399,34; ...)

+ intrinsic k_T : G. Papp, P. Levai, G.G. Barnaföldi, G. Fai, hep-ph/0212249, EPJC33(2004)609

$$E_\pi \frac{d\sigma^{pp}}{d^3 p_\pi} = \frac{1}{S} \sum_{abc} \int_{vW/z_c}^{1-(1-v)/z_c} \frac{dv}{v(1-v)} \int_{vW/vz_c}^1 \frac{dw}{w} \int^1 dz_c$$

$$\int d^2 k_{Ta} \int d^2 k_{Tb} f_{a/p}(x_a, k_{Ta}, Q^2) f_{b/p}(x_b, k_{Tb}, Q^2)$$

$$\left[\frac{d\sigma^{BORN}}{dv} \delta(1-w) + \frac{\alpha_s(Q_R)}{\pi} K_{ab,c}(s, v, w, Q, Q_R, Q_F) \right] \frac{D_c^\pi(z_c)}{\pi z_c^2}$$

An approximation for the unintegrated parton distribution functions (PDFs) :

$$f_{a/p}(x_a, k_{Ta}, Q^2) = f_{a/p}(x_a, Q^2) g(k_{Ta})$$

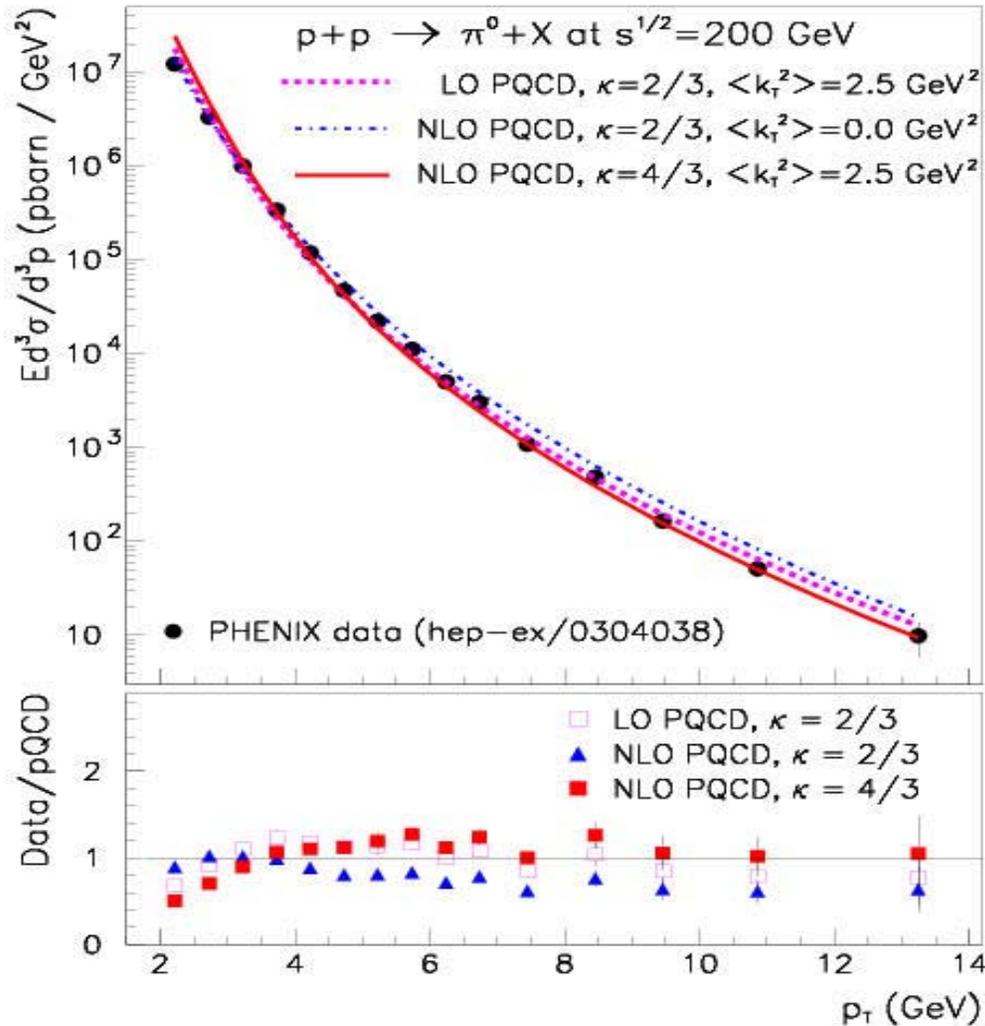
Where we use gaussian

$$g(k_{Ta}) = \frac{1}{\pi \langle k_T^2 \rangle} e^{-k_T^2 / \langle k_T^2 \rangle}$$

The width of the gaussian distribution for intrinsic- k_T

Hard physics: pion production in pp collision at high- p_T

Perturbative QCD calculations in LO and NLO for pp --- including intrinsic- k_T



LO:

$$Q = \kappa p_T / z_c, \quad Q_F = \kappa p_T$$

NLO:

$$Q = Q_R = \kappa p_T / z_c, \quad Q_F = \kappa p_T$$

**All descriptions are approx.
good enough at $2 \text{ GeV} < p_T < 5 \text{ GeV}$.**

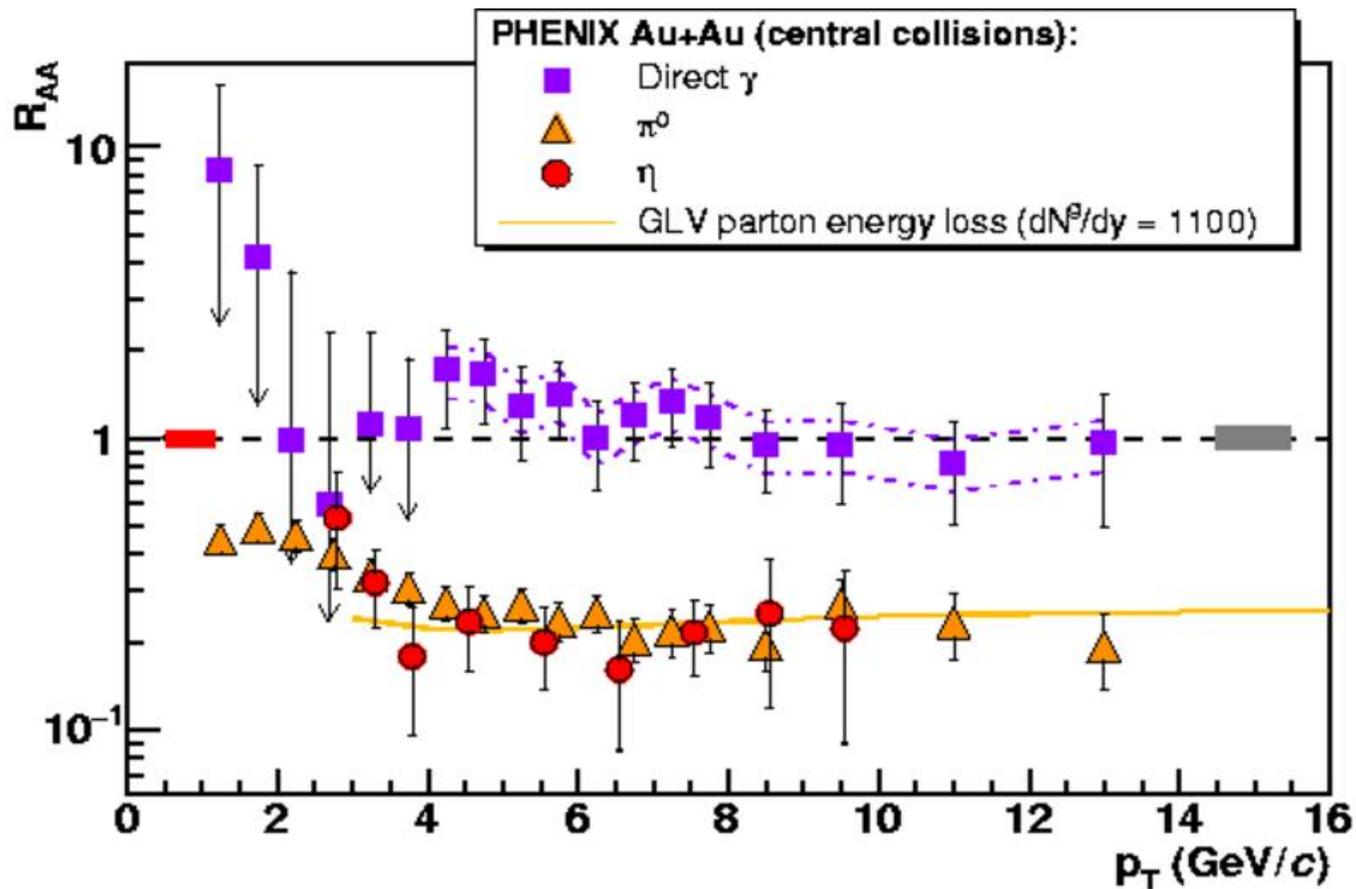
Which κ should be used ? ←

**Y. Zhang, G. Fai, G. Papp,
G.G. Barnaföldi, P.L.:
PRC 65 (2002) 034903.**

Hard physics: pion production in AuAu collision at high- p_T

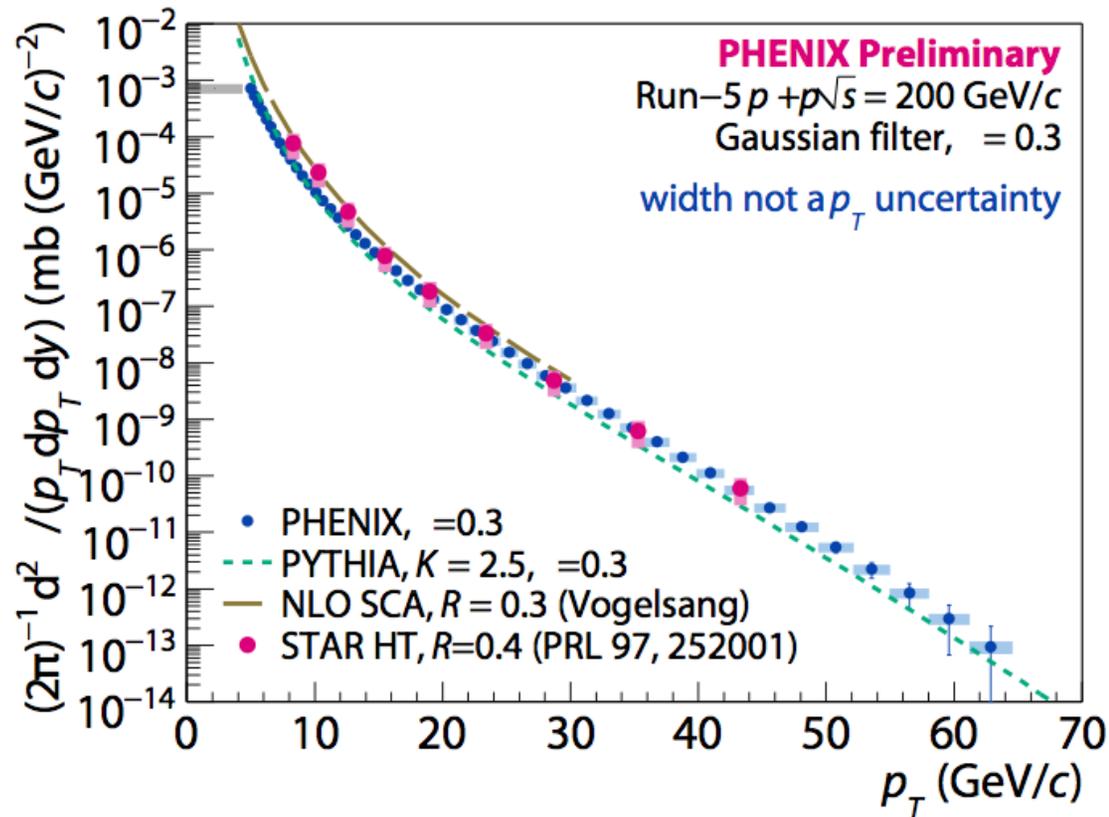
Jet energy loss \rightarrow Jet-tomography, corona-graphy, ...

wQGP vs. sQGP, heavy quark energy loss, AdS/CFT, ...



nucl-ex/0601037

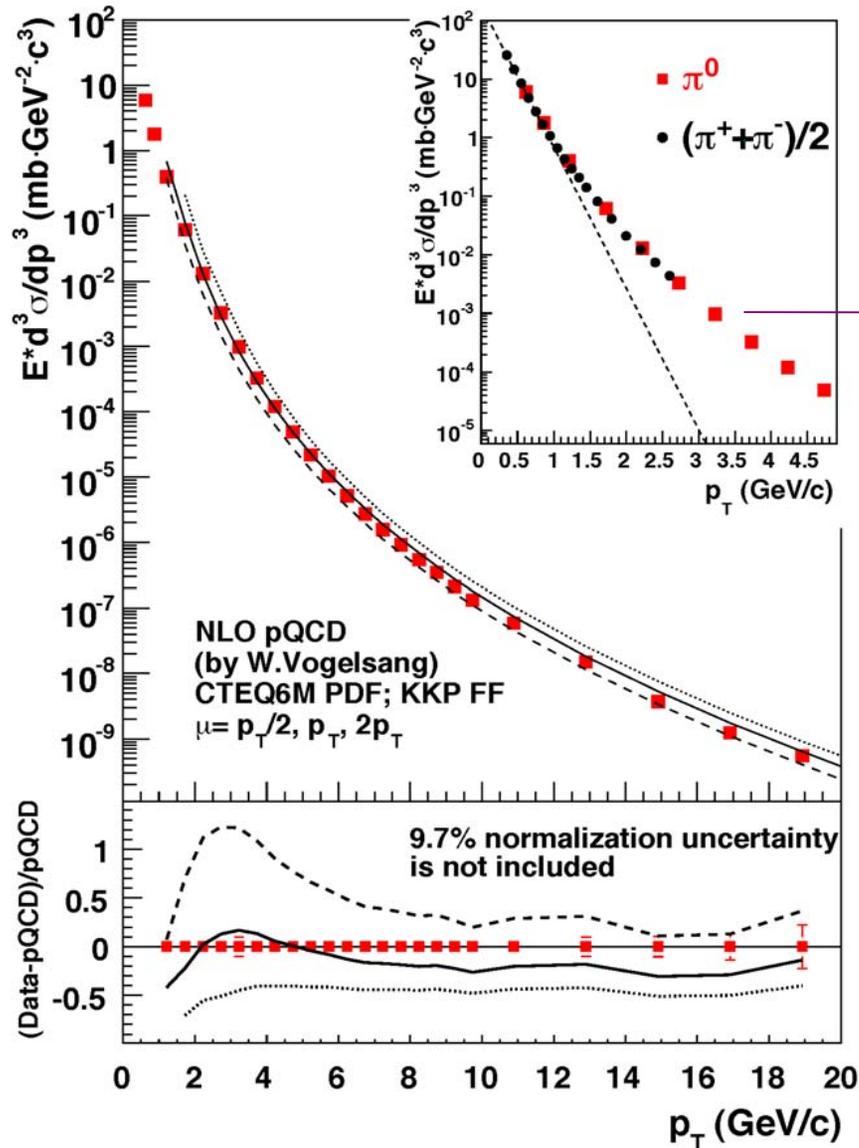
Jet production in pp collisions in the high- p_T region at RHIC:



PHENIX and STAR results (2010, Prag) at 200 GeV

NLO pQCD and PYTHIA seems to reproduce the exp. data very well (on this log scale)

Hadron production in pp collisions in the high- p_T region at RHIC:

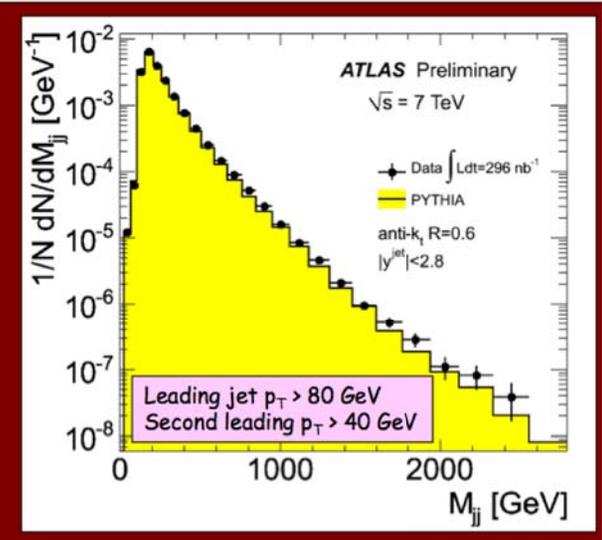
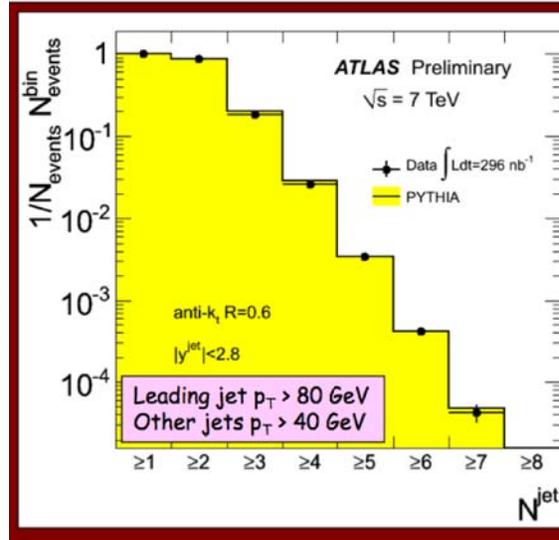
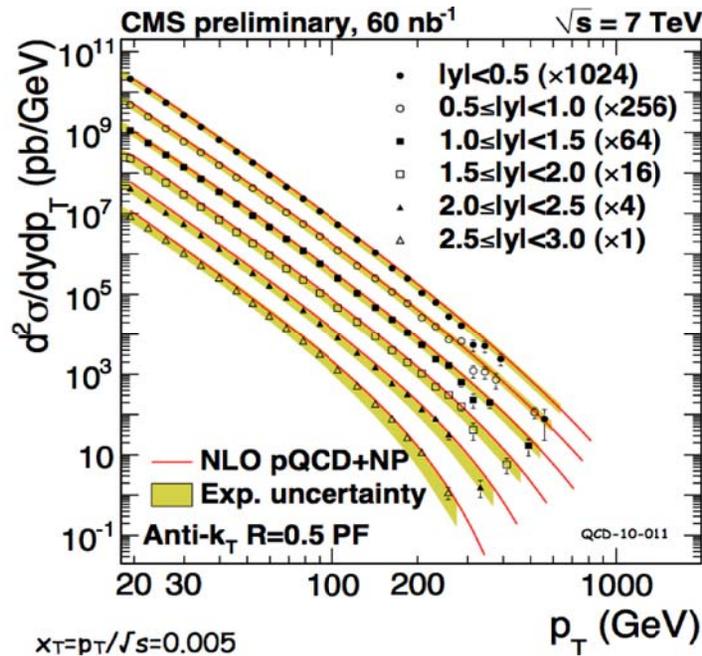


PHENIX results (2006)
 $p+p \rightarrow \pi^0$ at 200 GeV

***NLO pQCD seems to reproduce
the exp. data very well***

(Main 'propaganda' slide.)

Jet production in pp collisions in the high- p_T region at LHC:



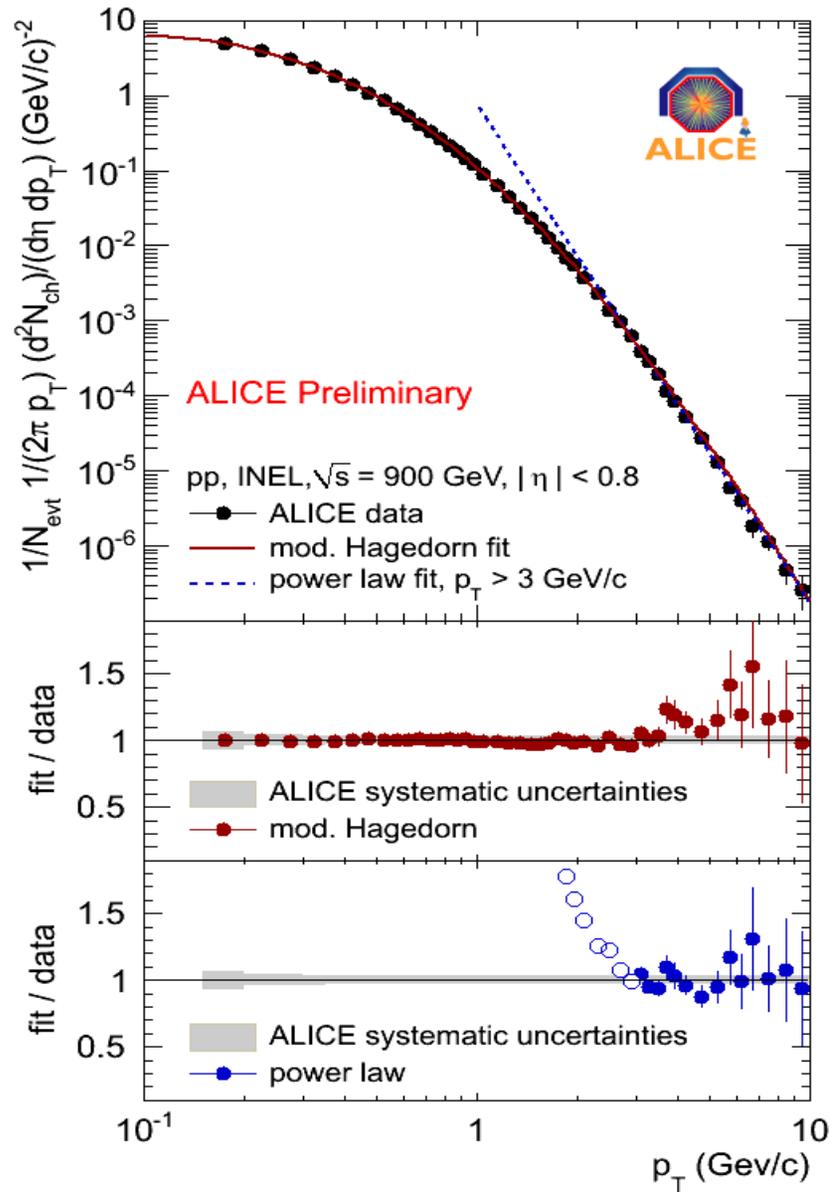
CMS result at 7 TeV

ATLAS results at 7 TeV

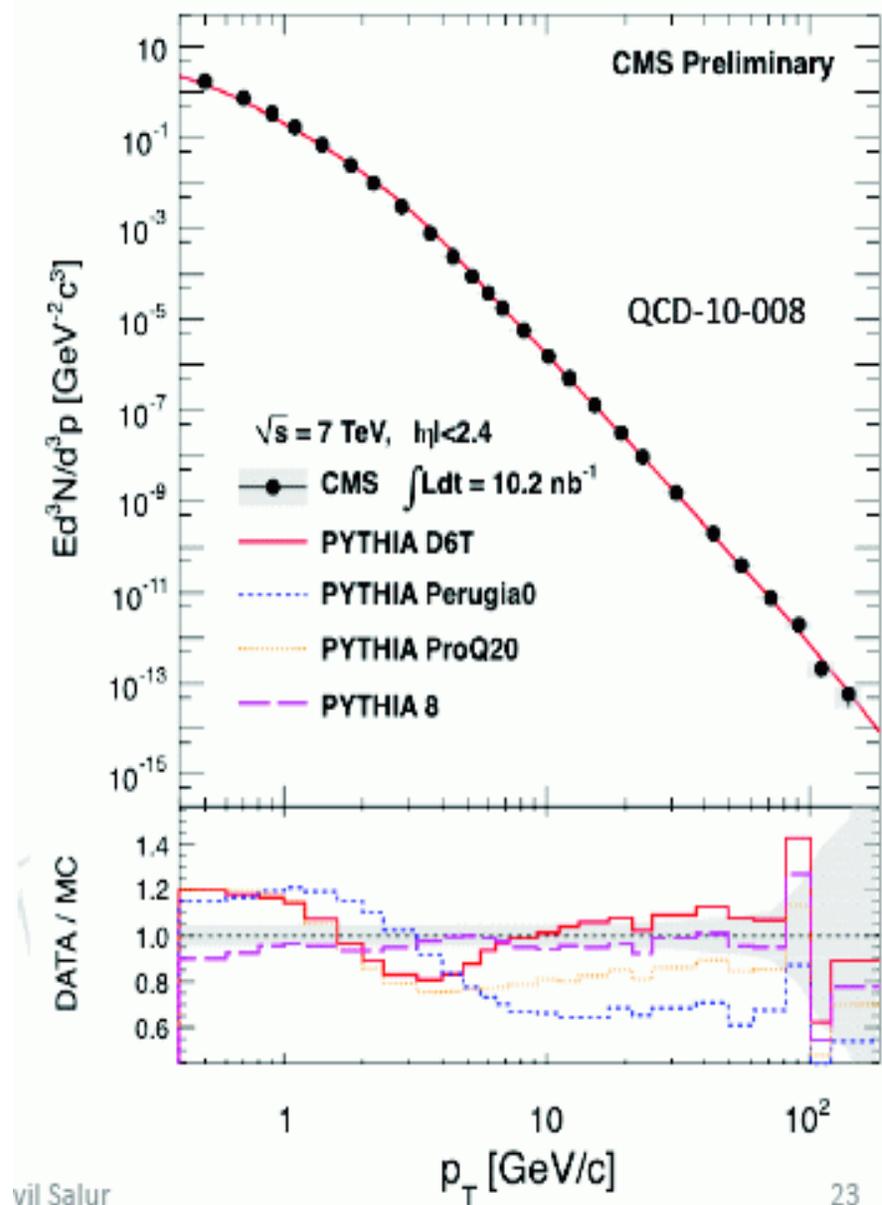
***NLO pQCD (+NP) seems to reproduce the exp. data
 (First 100 nb⁻¹)***

Prag WS 2010

Charged hadron production in pp collisions in the high- p_T region :



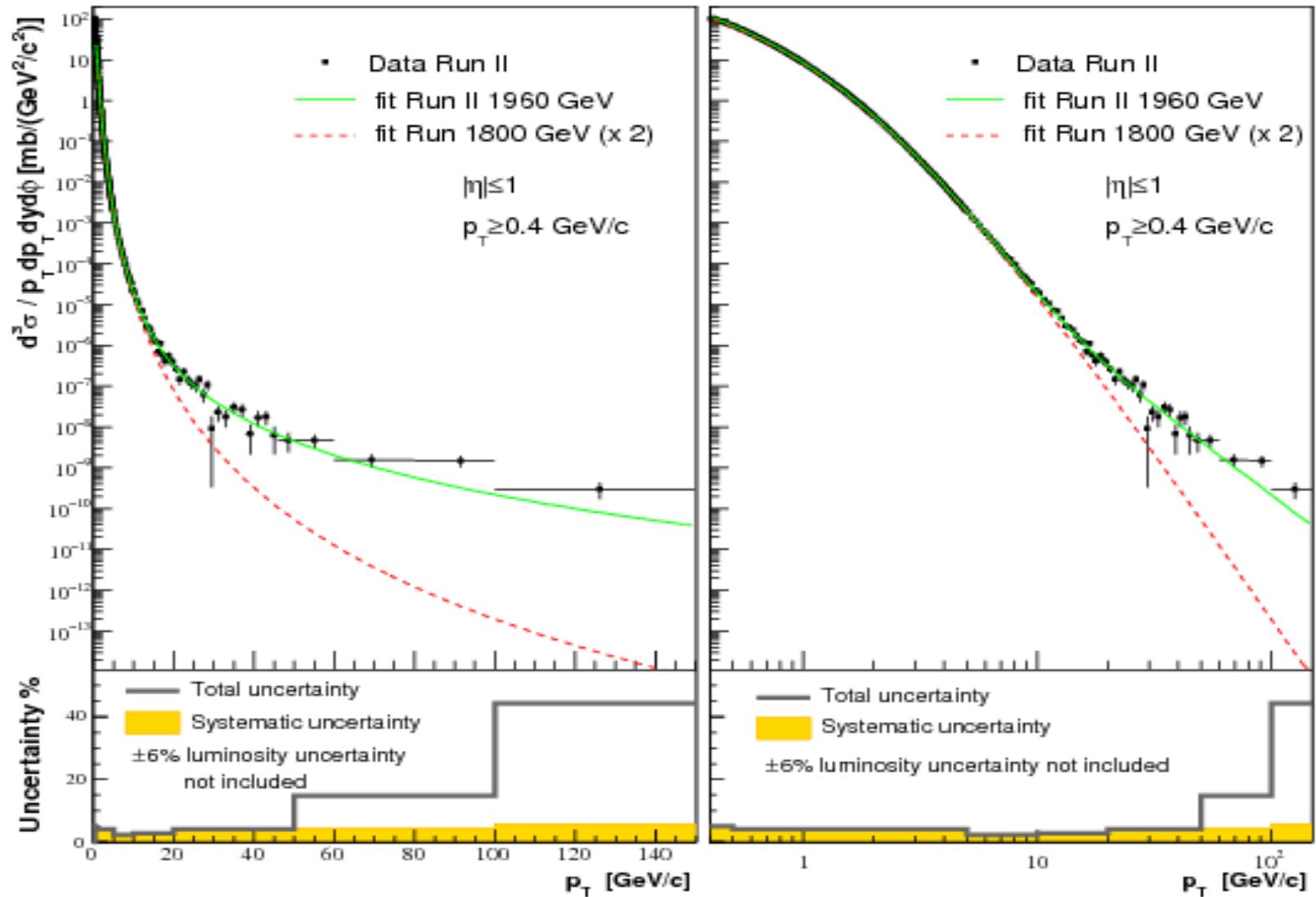
LHC ALICE (Prag'10)



LHC CMS (Prag'10)

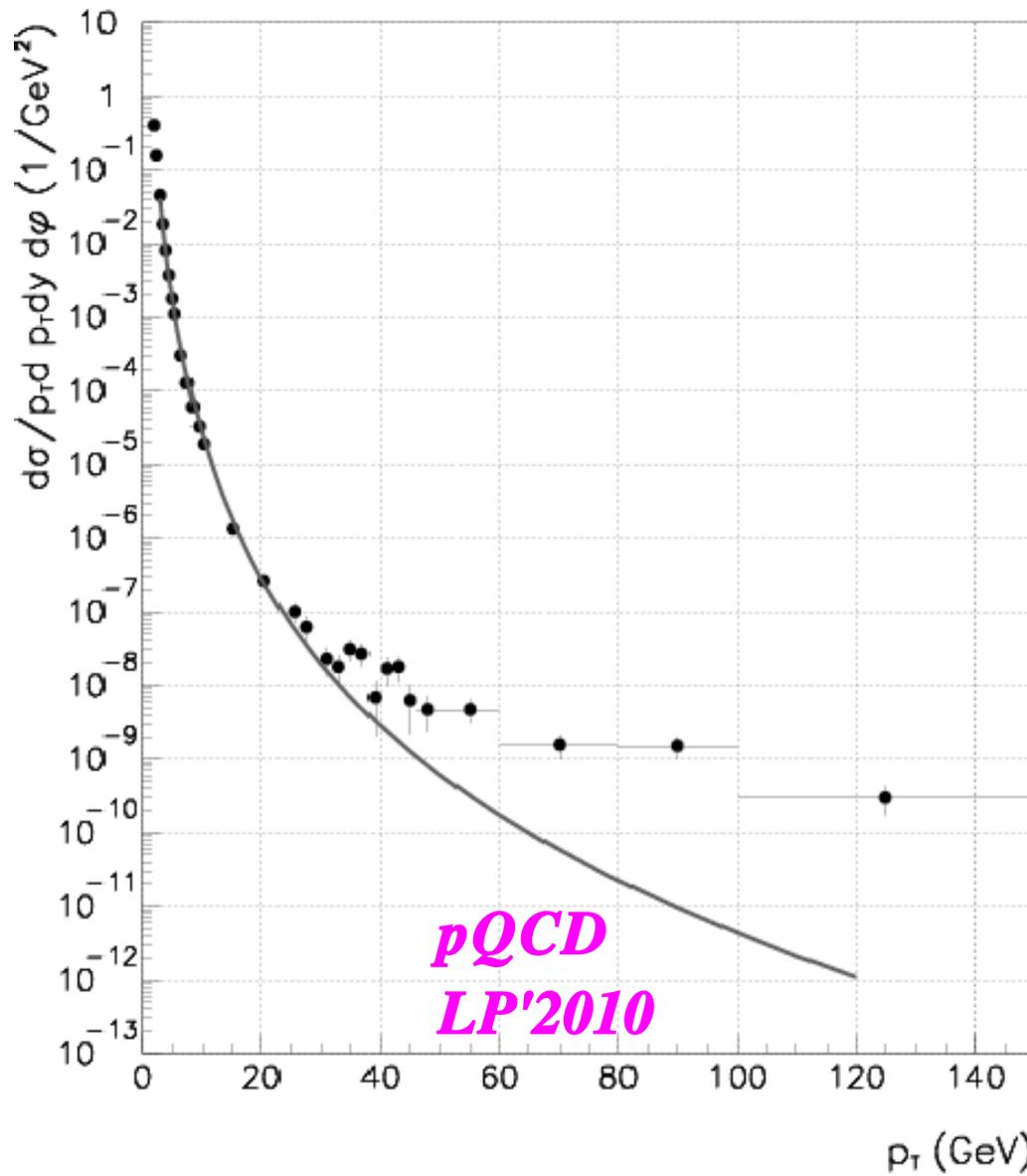
BOMB SHELL (!):

Charged hadron production in pp collisions at TEVATRON:



New data from TEVATRON CDF experiment: PRD 79 (2009) 112005.

Charged hadron production in pp collisions at TEVATRON :



**Charged hadrons
at 2 TeV
p+antip**

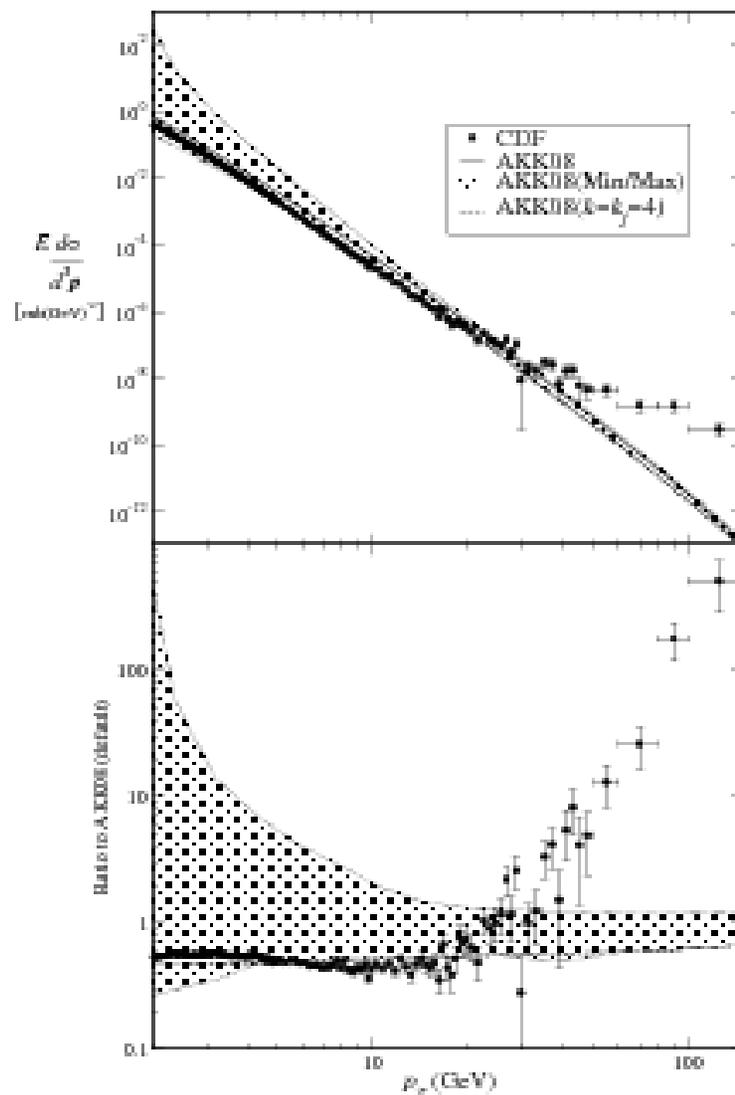
**Data vs.
LO pQCD calc.**

**2 TeV \leftrightarrow 30 GeV
 $x_T = 0.015$
| $\bar{\eta}$**

7 TeV \leftrightarrow 100 GeV

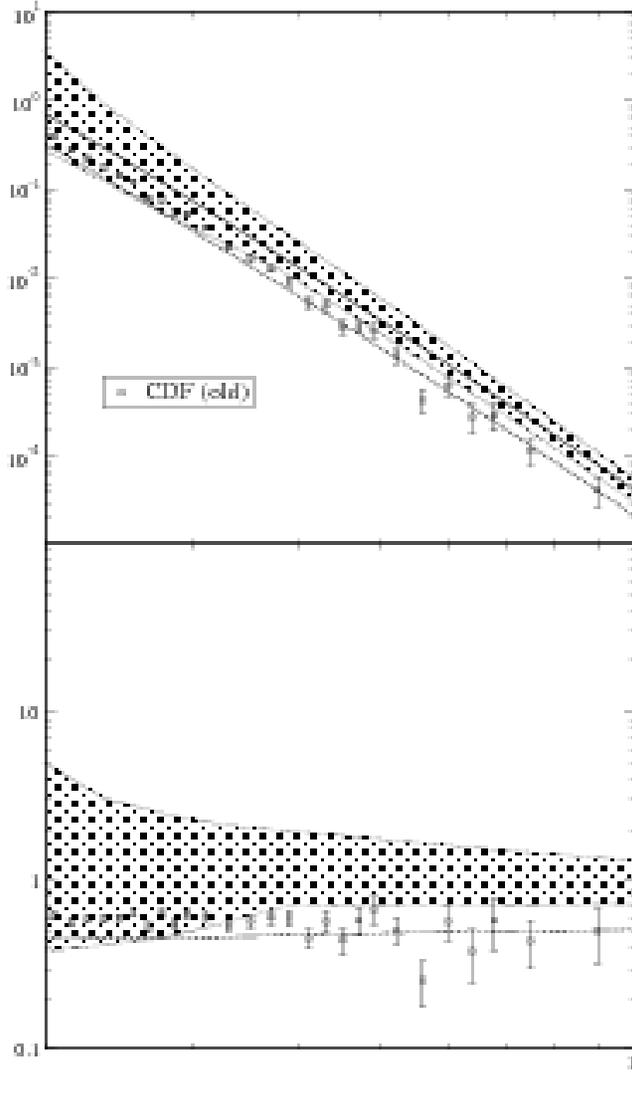
New data from TEVATRON CDF : PRD 79 (2009) 112005.

Charged hadron production in pp collisions at TEVATRON :



New data

PRD 79 (2009) 112005.



Old data

PRL 60 (1988) 1819

***NLO PQCD
calculation
(investigation)
from AKK:***

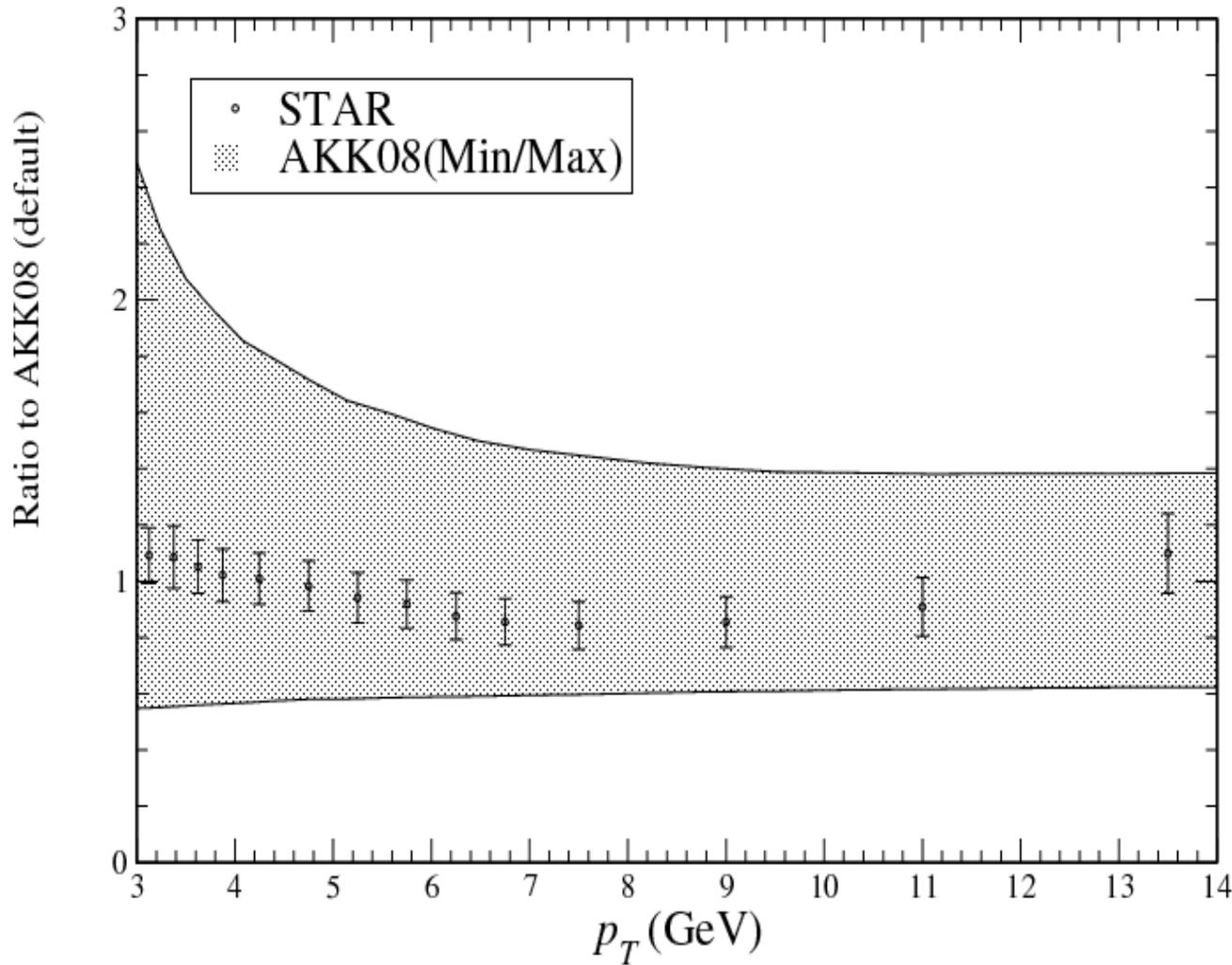
***MWST'08 PDF
AKK'08 FF***

Latest parametr.

Theory - AKK

PRL 104 (2010) 242001

Charged hadron production in pp collisions at RHIC (200 GeV) :



*NLO PQCD
calculation
(investigation)
from AKK:*

*MWST'08 PDF
AKK'08 FF*

Latest parametr.

New STAR data

Y. Xu, EPJ C62 (2009) 187

Theory - AKK

PRL 104 (2010) 242001

Long time valid conclusion:

(NLO) pQCD can reproduce

jet and hadron production at high- p_T

in proton+proton (antiproton) collisions

at RHIC, TEVATRON and LHC energies

New CDF data at TEVATRON!

If they valid (let us assume this), then possible answers:

--- a production mechanism is missing;

--- a channel is missing;

--- NLO is not enough, but NNLO, NNNLO, ...

--- multiparton collisions (UE) --> G.G. Barnaföldi

--- multi-jet production (3/4/...) --> S. Pochybova talk

--- something is wrong with the PDF fits;

--- something is wrong with the FF fits (at high- p_T);

--- ... (???)

***2. Jet and hadron production mechanisms
in heavy ion collisions***

***--- from RHIC to LHC energies ---
[Theory]***

And what about proton-proton collisions ?

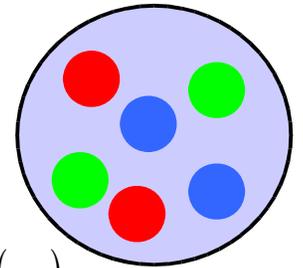
Particle production mechanisms in high energy HI collisions:

I. Dilute parton gas limit as initial condition + parton cascade:

PDF(p,n) + pQCD + Glauber + [Shad; Multisc; Quench; Fluct; ...]

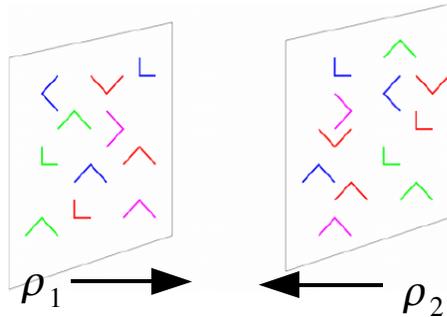
$$E_\pi \frac{d\sigma^{pp}}{d^3 p_\pi} = \int dx_1 \int dx_2 \int dz_c f_{a/p}(x_a, Q^2) f_{b/p}(x_b, Q^2) \frac{d\sigma}{d\hat{t}} \frac{D_c^\pi(z_c)}{\pi z_c^2}$$

$$E_\pi \frac{d\sigma^{AB}}{d^3 p_\pi} = \int d^2 b d^2 r t_A(\vec{r}) t_B(|\vec{b}-\vec{r}|) E_\pi \frac{d\sigma^{pp}}{d^3 p_\pi} \otimes S(\dots) \otimes M(\dots) \otimes Q(\dots) \otimes F(\dots)$$



Dilute gas

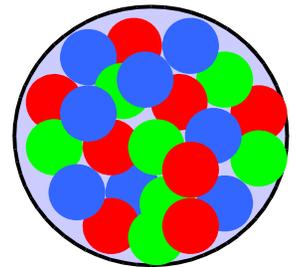
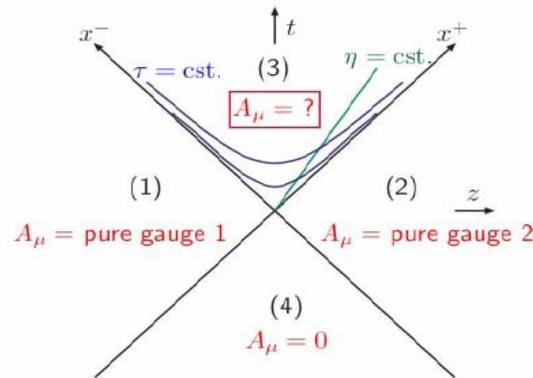
II. Dense gluon matter limit as initial condition + hydro:



CGC initial condition:

$$J^\mu = \delta^{\mu+} \delta(x^-) \rho_1(\mathbf{x}_T) + \delta^{\mu-} \delta(x^+) \rho_2(\mathbf{x}_T)$$

where $-D_i \alpha_{(m)}^i = \rho_{(m)}(\mathbf{x}_\perp)$. **and** α_1, α_2 **gluon fields of nuclei**

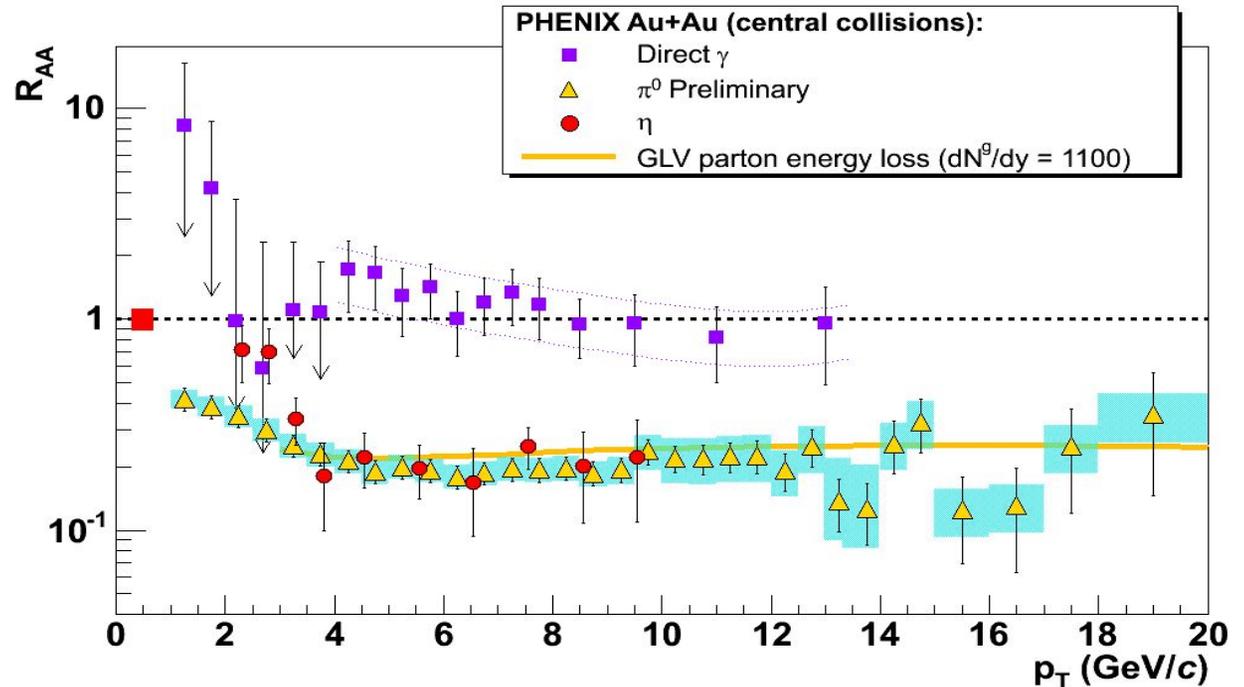


CGC: high density gluons

Successful applications of I and II:

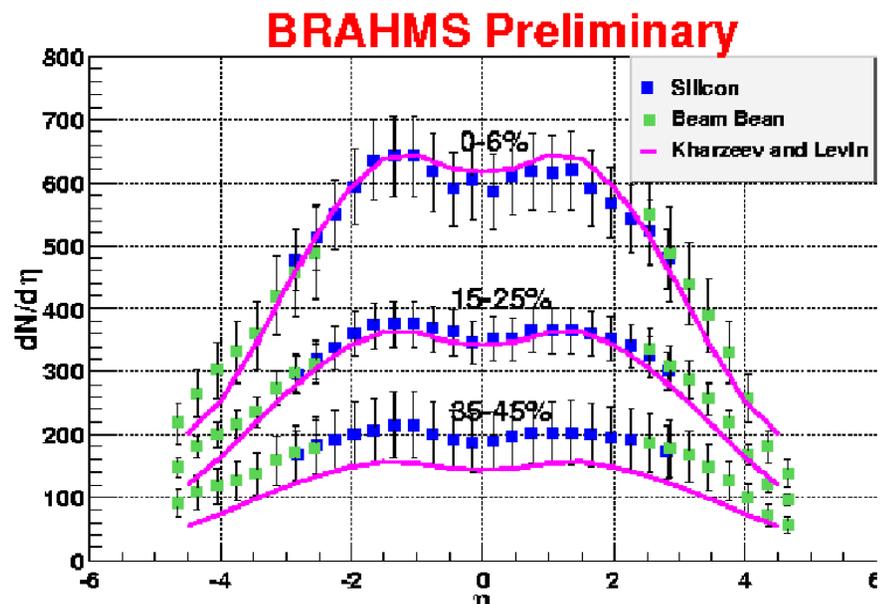
I. pQCD model:

- hard probes
- high- p_T physics
- jets
- h-h correlations
- ...



II. CGC model:

- soft physics
- multiplicities
- centrality dependence
- E_T production
- rapidity distributions
- ...



Problems:

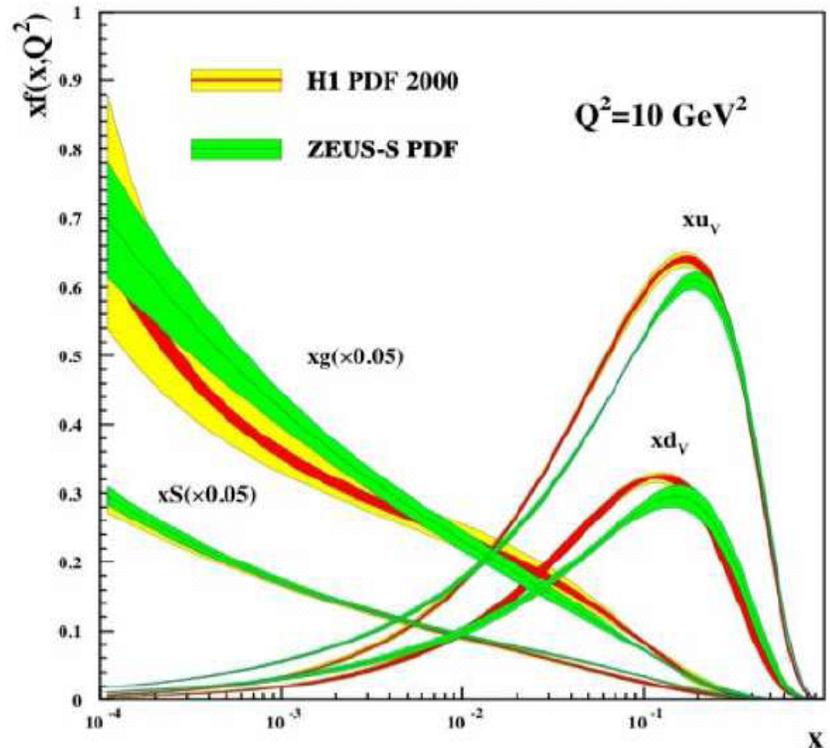
I. pQCD model (Feynman graphs):

- LO, NLO, ... ?*
- factorization (k_T)*
- resummations*
- soft physics*
- heavy quark quenching*
- ...*

II. CGC model (asymptotic):

- hard probes*
- jet physics*
- correlations*
- ...*

Connection between I and II:



Large-x: valence partons

random color charge, $\rho^a(x)$

Small-x: radiation field,

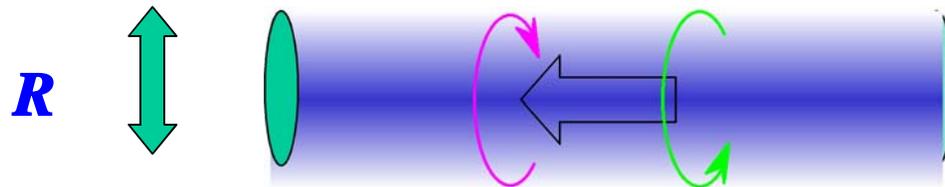
created by $\rho^a(x)$

A further model for particle production:

III. Non-perturbative, non-asymptotic color transport:

“confined flux tube formation and breaking”

- phenomenological approximations are known (string, rope)**
- phenomenology is applied successfully in string-based codes**
- FRITIOF, PYTHIA, HIJING are using strings**
- URQMD, HIJING-BB is using ropes (melted strings)**
- good agreement with data at different energies**
- ...**



- formal QCD-based equations are known (Heinz, Mrowczynski)**
- YM-field evolution in 3+1 dim, collision (Poschl, Müller)**
- lattice-QCD calculations have been started (Krasnitz, Lappi)**
- ...**

A further model for particle production:

III. Non-perturbative, non-asymptotic color transport: **“pair-creation in strong fields”**

--- strong (Abelian) static E field: Schwinger mechanism
probability of pair-creation:

$$P(p_T) d^2 p_T = -\frac{eE}{4\pi^3} \ln\left(1 - \exp\left[-\pi \frac{m^2 + p_T^2}{eE}\right]\right) d^2 p_T$$

integrated probability at mass m:

$$P_m = \frac{(eE)^2}{4\pi^3} \sum_{n=1}^{\infty} \frac{1}{n^2} \exp\left[-\pi \frac{nm^2}{eE}\right]$$

ratio of production rates (e.g. strange to light)

$$\gamma_s = \frac{P(s\bar{s})}{P(q\bar{q})} = \exp\left[-\pi \frac{m_s^2 - m_q^2}{eE}\right] \quad eE = 0.9 \text{ GeV/fm}$$

--- strong time dependent SU(N) color fields:

Kinetic Equation for the color Wigner function

A.V. Prozokevich, S.A. Smolyansky, S.V. Ilyin, hep-ph/0301169.

Kinetic equation for fermion pair production:

Wigner function: $W(k_1, k_2, k_3)$

Color decomposition: $W = W^s + W^a t^a$, where $a=1, 2, \dots, N_c^2 - 1$

Spinor decomposition: $W^{s;a} = a^{s;a} + b_\mu^{s;a} \gamma^\mu + c_{\mu\nu}^{s;a} \sigma^{\mu\nu} + d_\mu^{s;a} \gamma^\mu \gamma^5 + i e^{s;a} \gamma^5$

Color vector field (longit.): $A_\mu^a = (0, -\vec{A}) = (0, 0, 0, A_3^a)$

Kinetic equation for Wigner function:

$$\begin{aligned} \partial_t W + \frac{g}{8} \frac{\partial}{\partial k_i} \left(4 \{W, F_{0,i}\} + 2 \{F_{i\nu}, [W, \gamma^0 \gamma^\nu]\} - [F_{i\nu}, \{W, \gamma^0 \gamma^\nu\}] \right) = \\ = i k_i \{ \gamma^0 \gamma^i, W \} - i m [\gamma^0, W] + i g [A_i, [\gamma^0 \gamma^i, W]]. \end{aligned}$$

*for details see V.V. Skokov, PL: PRD71 (2005) 094010 for U(1)
PRD78 (2008) 054004 for SU(2)
in preparation for SU(3)*

Distribution function for fermions with mass m :

$$f_f(\vec{k}, t) = \frac{m a^s(\vec{k}, t) + \vec{k} \vec{b}^s(\vec{k}, t)}{\omega(\vec{k})} + \frac{1}{2}$$

Time dependent external field, $E(t)$ and neglected mass, $m=0$:

A, Pulse field (dotted):

$$E_{pulse}(t) = E_0 [1 - \tanh^2(t/\delta)]$$

B, Constant field (dashed):

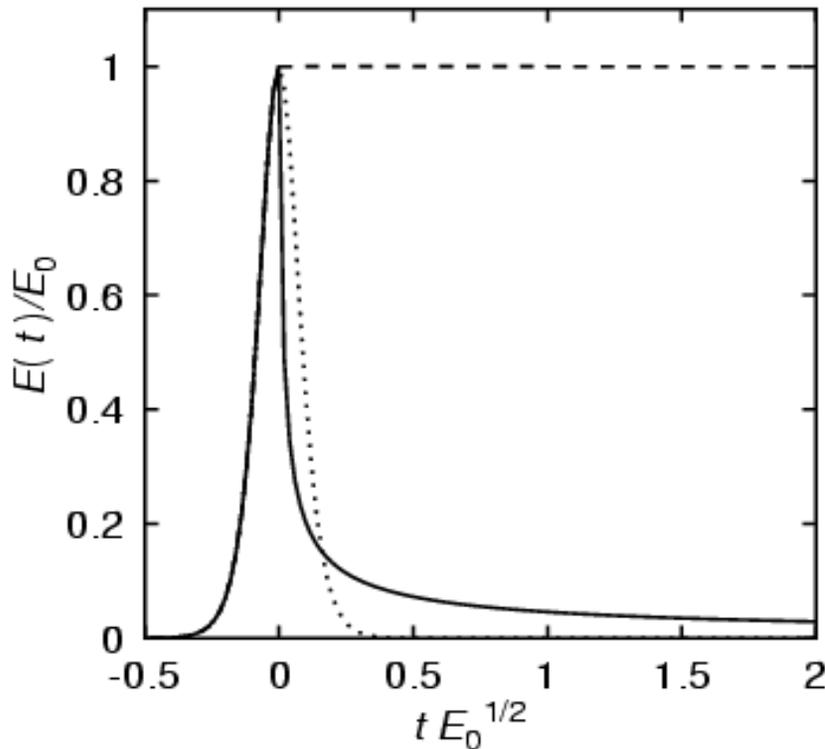
$$E_{const}(t) = E_{pulse}(t) \quad \text{at } t < 0$$

$$E_{const}(t) = E_0 \quad \text{at } t > 0$$

C, Scaled field (solid):

$$E_{scaled}(t) = E_{pulse}(t) \quad \text{at } t < 0$$

$$E_{scaled}(t) = \frac{E_0}{(1 + t/t_0)^\kappa} \quad \text{at } t > 0$$



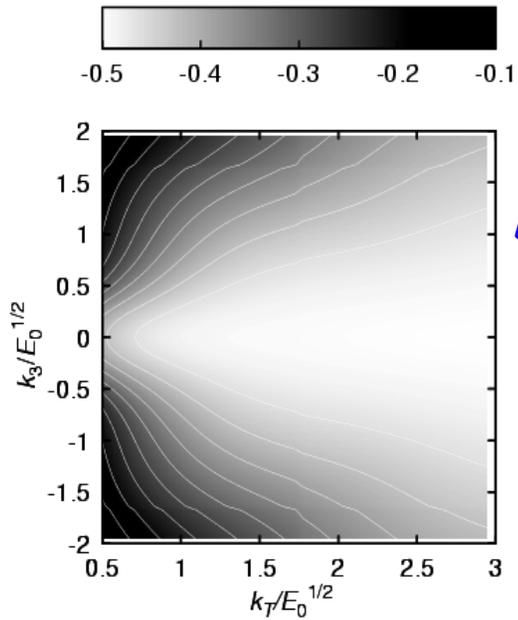
$$\delta = 0.1 / E_0^{1/2} \quad \text{at RHIC energy}$$

$$\kappa = 2/3 \quad \text{for scaled Bjorken expans.}$$

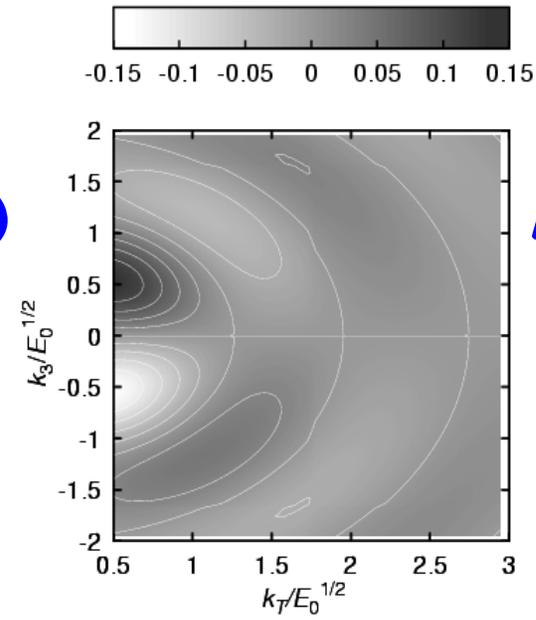
$$\text{with } t_0 = 0.01 / E_0^{1/2}$$

Numerical results (b^i) for the Bjorken expansion at $t=2/\sqrt{E_0}$ in $SU(2)$:

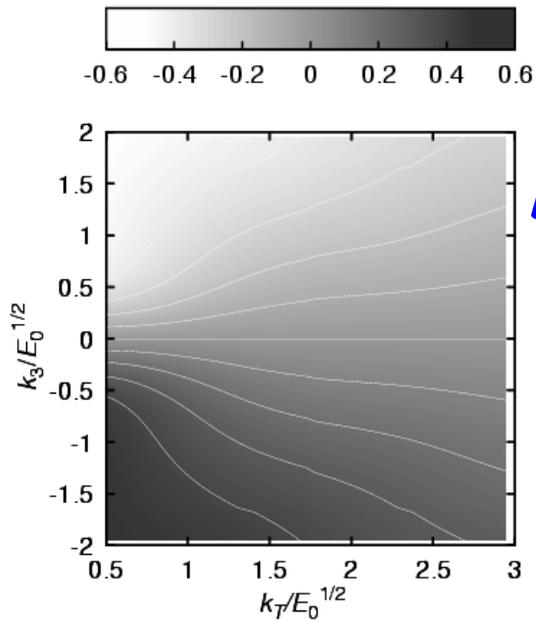
$m = 0$



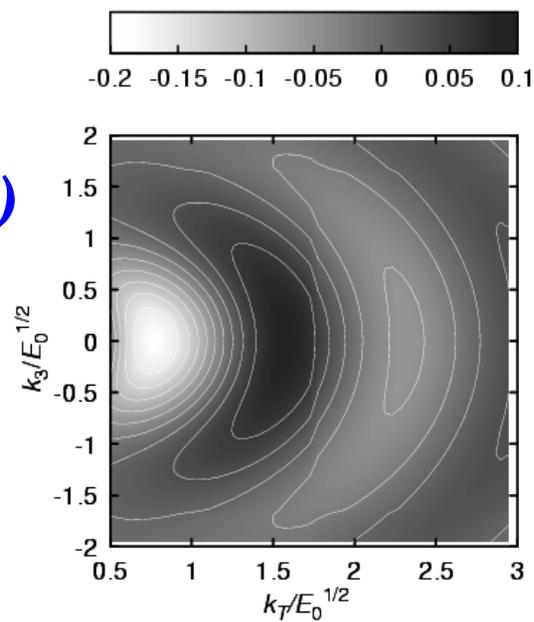
$b^s_T(k_T, k_3)$



$b^a_T(k_T, k_3)$

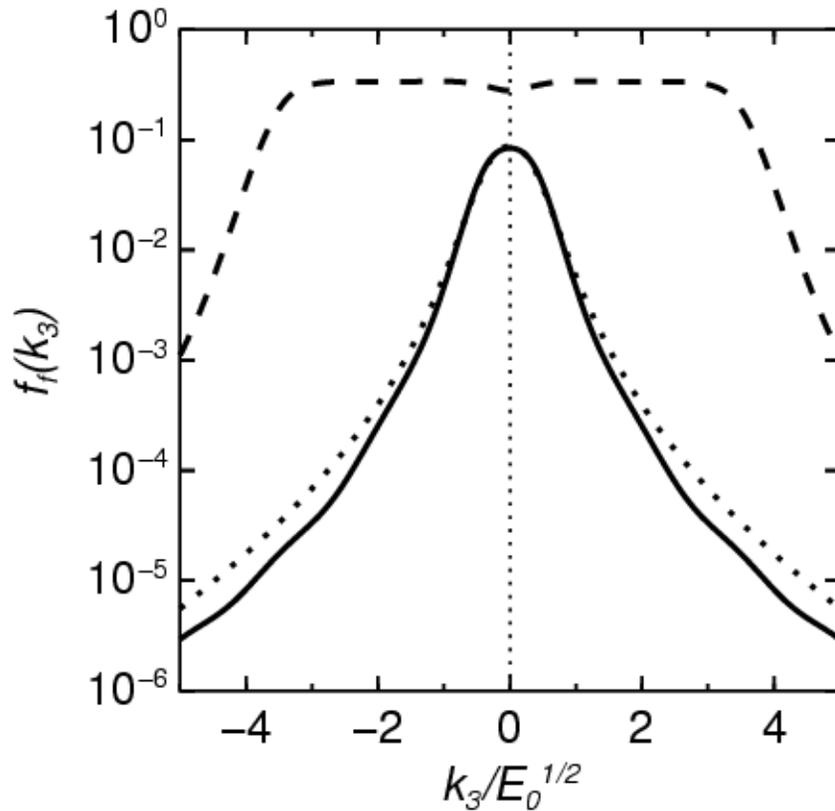


$b^s_3(k_T, k_3)$

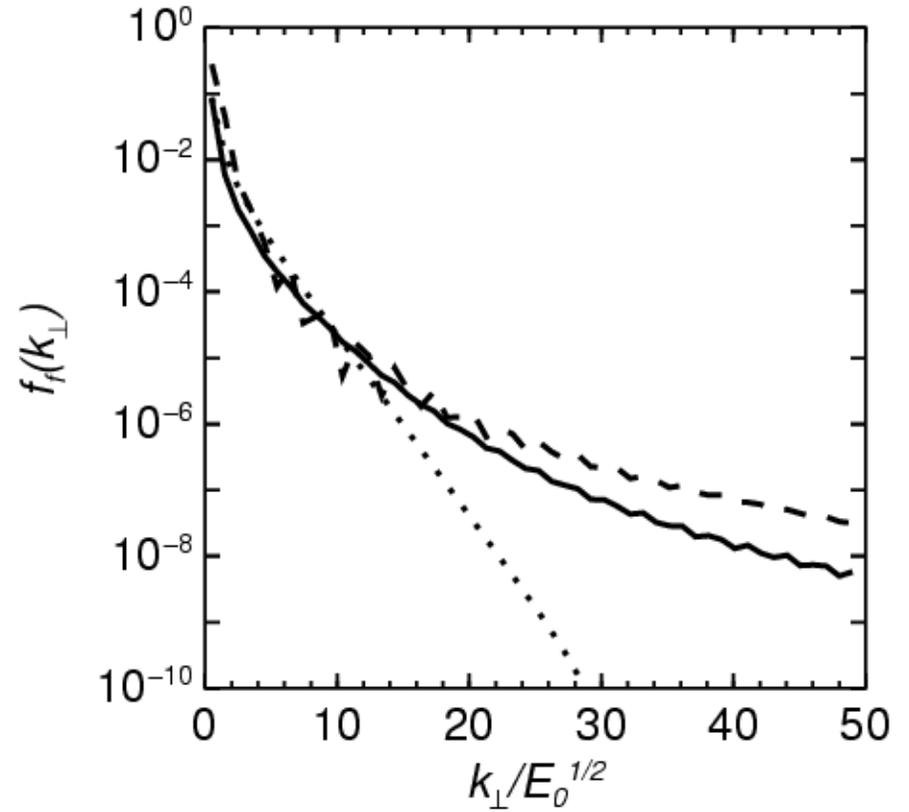


$b^a_3(k_T, k_3)$

Numerical results for fermion distributions at $t=2/\sqrt{E_0}$ in $SU(2)$:



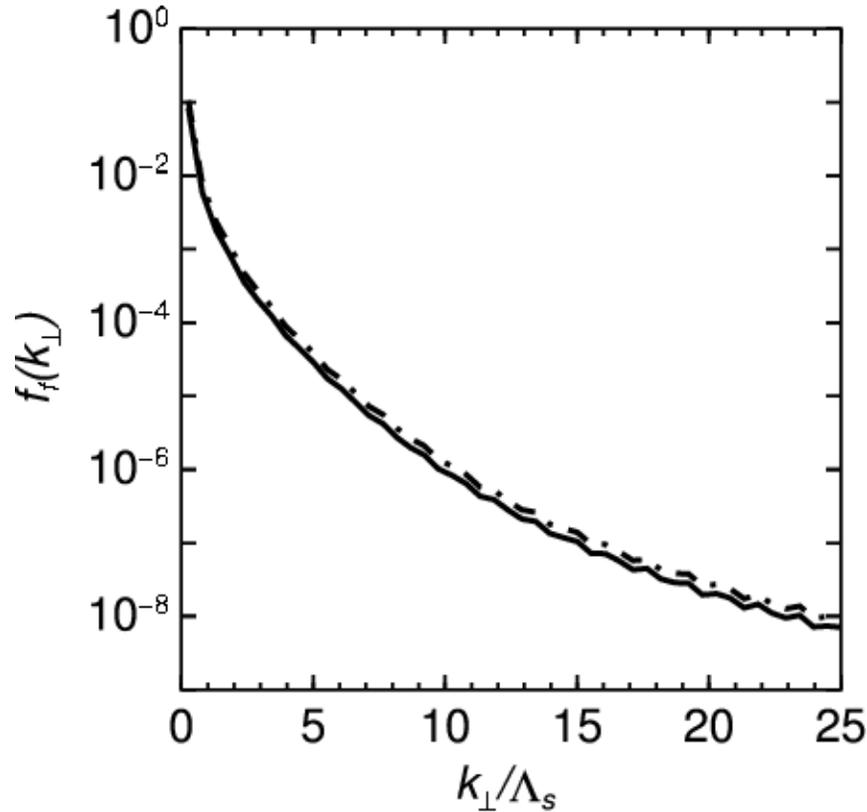
$f_f(k_3)$: longitudinal mom. distr.
 $k_T/\sqrt{E_0} = 0.5$



$f_f(k_T)$: transv. mom. distr.
 $k_3 = 0$

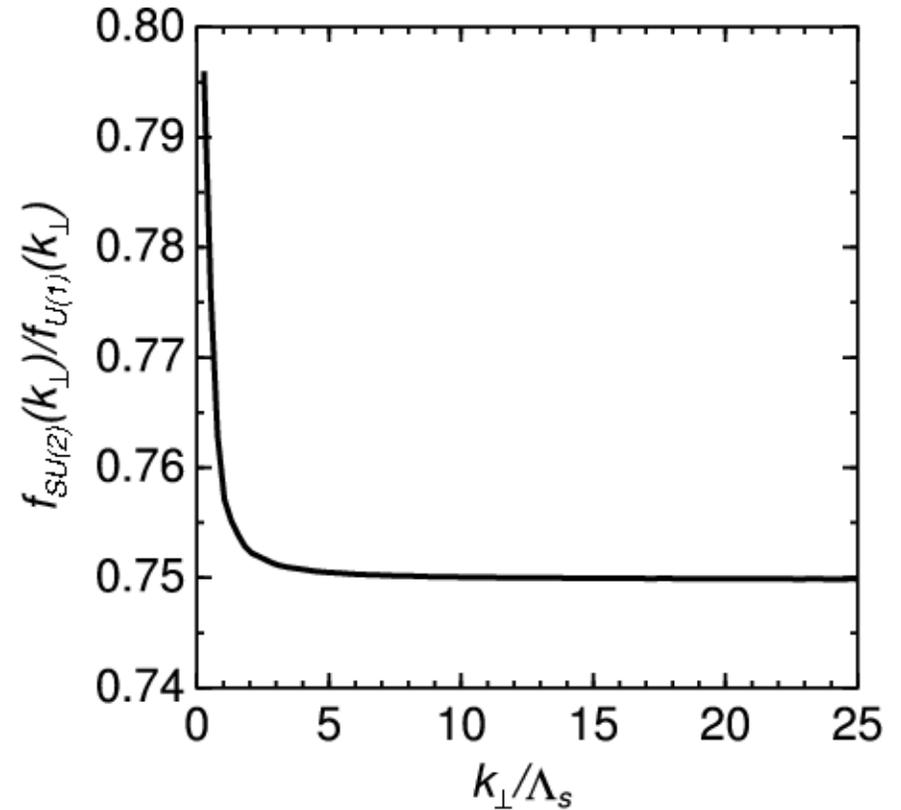
- \Rightarrow exponential (pulse)
- \Rightarrow polinomial (scaled)

Transverse momentum distr: scaling between U(1) and SU(2) at high-pT



$f_f(k_T)$: transv. mom. distr.

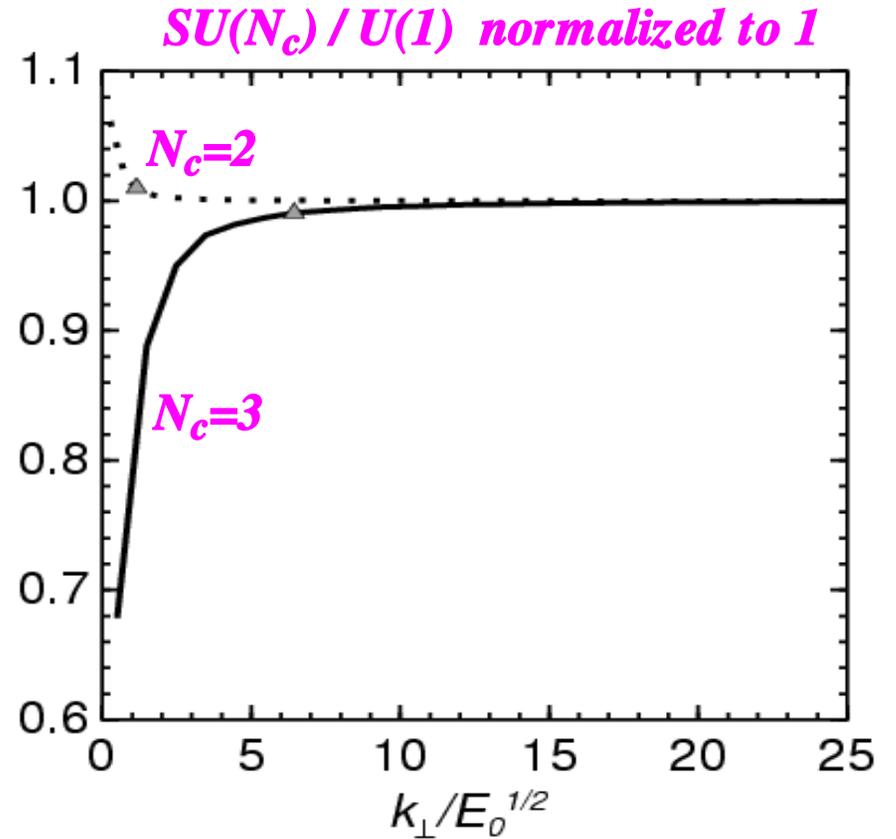
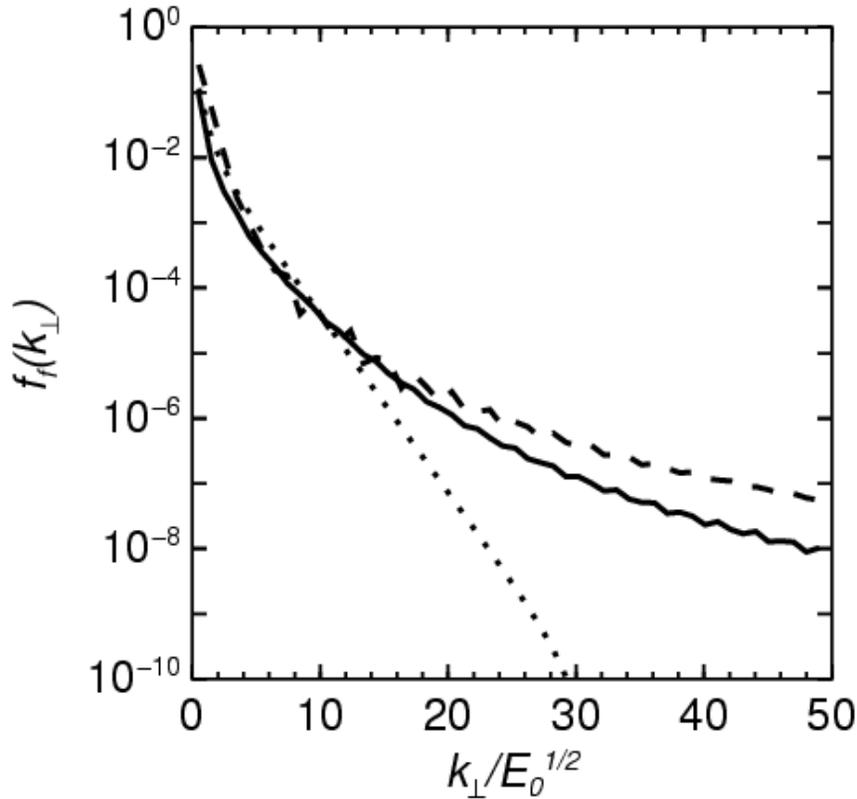
at $k_T/\sqrt{E_0} = 0.5$
in U(1) and SU(2)
[Bjorken scaled]



ratio: SU(2) / U(1)

$\Rightarrow 3/4$ at $k_T/\Lambda_s > 3$
(scaling in the Kinetic Eq.)

Transverse momentum distr: scaling in SU(3) at high-pT (m=0)



$f_T(k_T)$: transv. mom. distr.

in SU(3)

3 cases of $E(t)$

[similar to SU(2)]

Ratios (scaled time evol.):

$SU(2)/U(1) \Rightarrow 3/4$

$SU(3)/U(1) \Rightarrow 4/3$

(scaling in the Kinetic Eq.)

Conclusions - I:

- 1. Particle production mechanisms are not fully explored in non-Abelian cases, especially in case of strong fields.*
- 2. The overlap of colliding heavy ions (protons ?!) determine the space-time structure of the early phase, which can be substituted by a pulse-like strong field.*
- 3. Short pulses: the time evolution of the pulse determines the shape of the transverse momentum spectra.*
- 4. Thus: non-perturbative production could be suppressed at intermediate p_T and could become dominant at high- p_T (beyond pQCD).*
- 5. Could we validate the formation of a strong field in pp ?*

Q: Do we have another way to check the overlap of pQCD and NPQCD yields ?

***A: Quark-pair production in strong SU(N) fields
--- quark mass dependence ---***

***3. Mass-dependence of non-perturbative
particle production***

P. L. , V.V. Skokov:

--- J. Phys. G36 (2009) 064068.

--- arXiv: 0909.2323 [hep-th]

accepted in PRD (2010)

Mass dependent fermion production in SU(2):

Quark-pair production depends on the mass:

$$m(\text{light}) = 8 \text{ MeV}$$

$$m(\text{strange}) = 150 \text{ MeV}$$

$$m(\text{charm}) = 1200 \text{ MeV}$$

$$m(\text{bottom}) = 4200 \text{ MeV}$$

Usually 'm' mass behaves as a scale (see electron mass in QED).

But, what about zero mass limit?

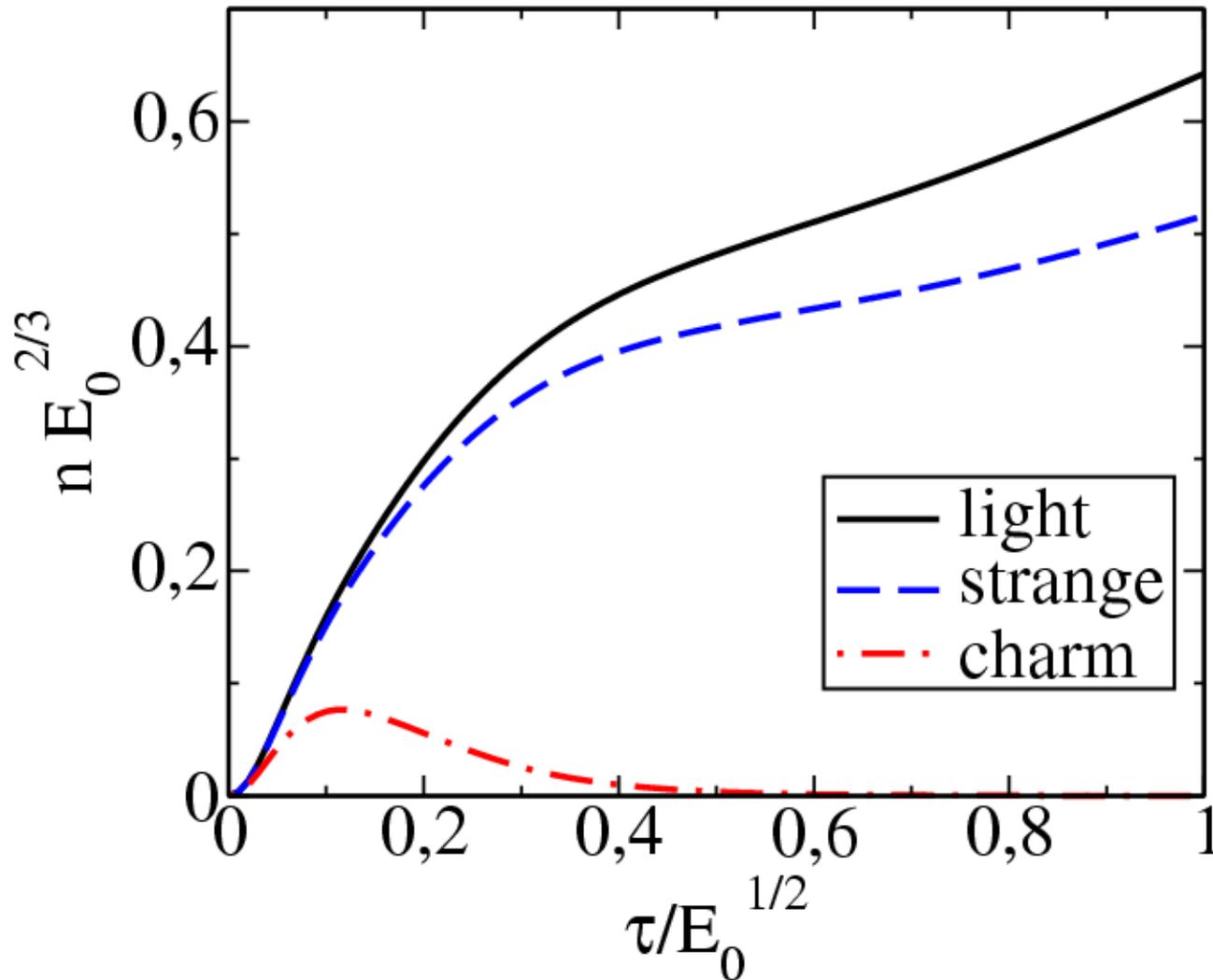
What is the scale in that case?

*Since we have non-zero fermion production,
then some scale must exist.*

The characteristic time of the changes in $E(t)$??

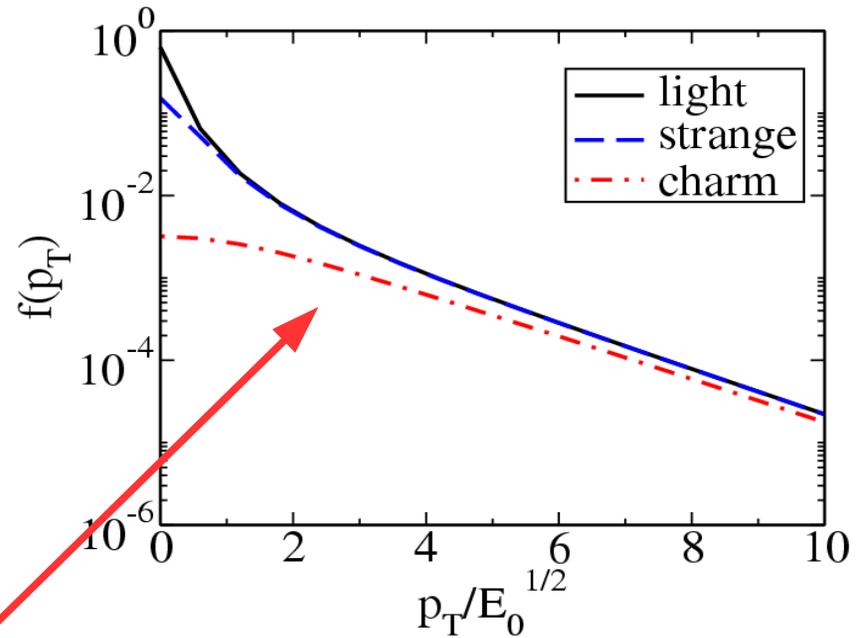
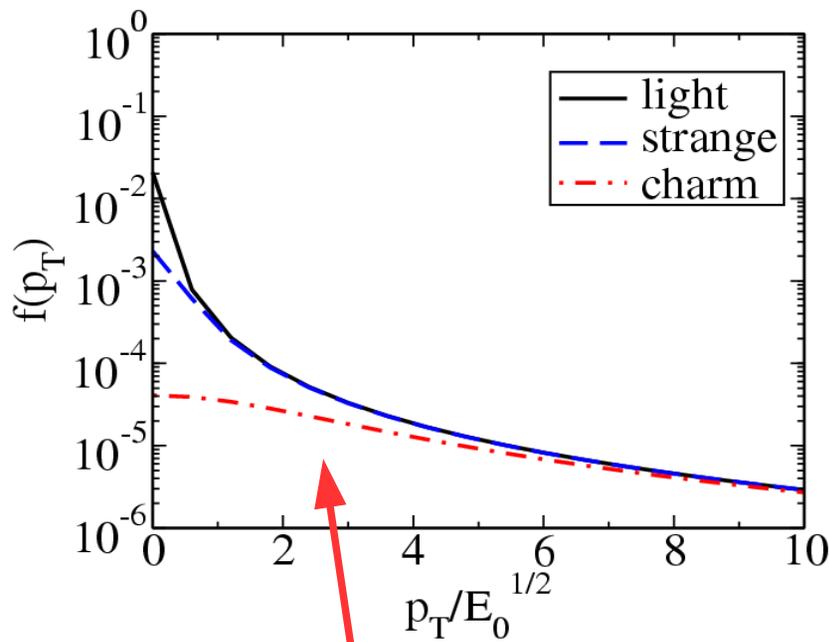
$$\tau \Rightarrow \delta$$

Mass dependent fermion production in SU(2) [pulse-like time dep.]



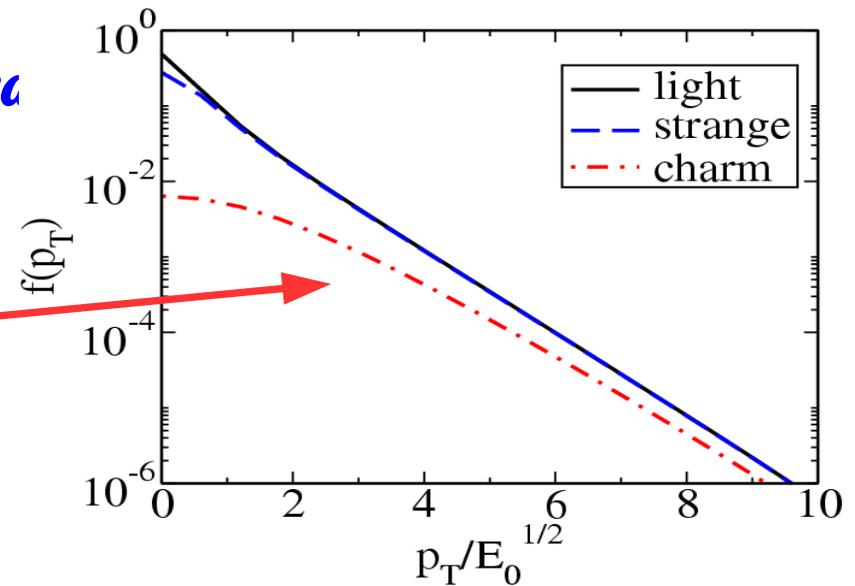
Fermion number (n) depends on the characteristic time of the pulse width: $\tau = \delta$ in the pulse scenario

Mass dependent fermion production in SU(2) [pulse-like time dep.]

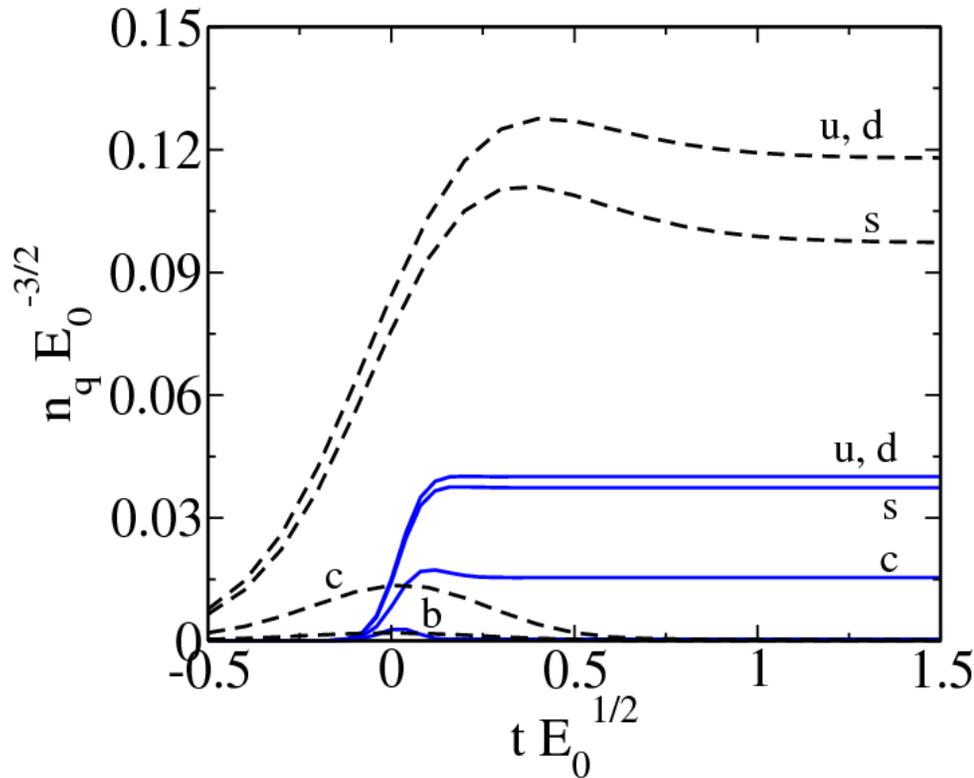


**Transverse momentum spectra
at different pulse width:**

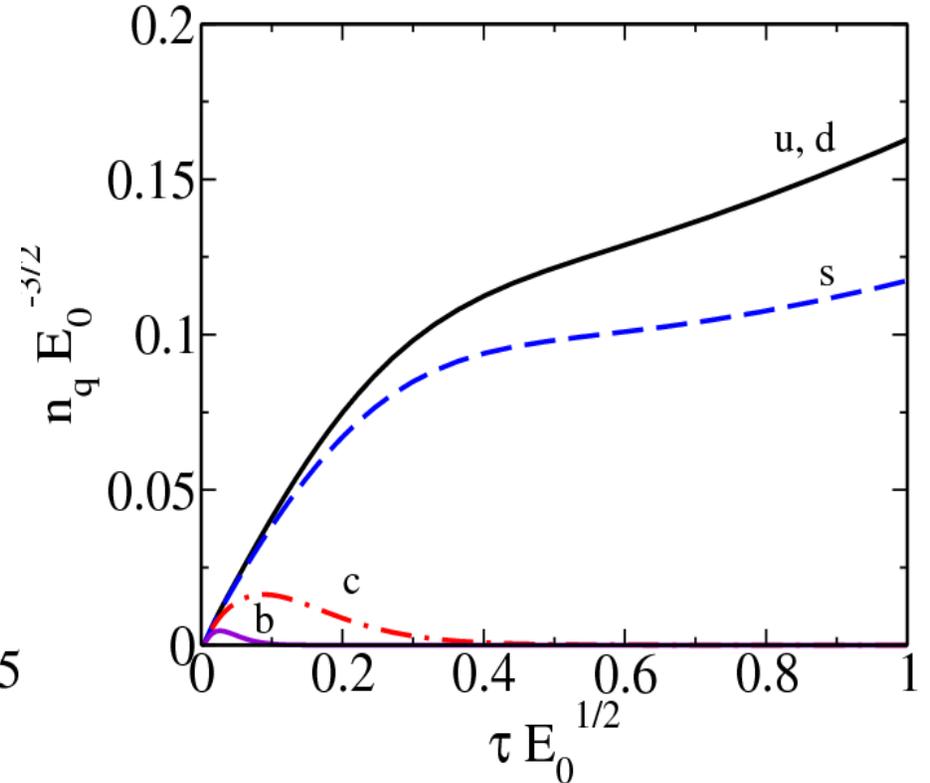
$\tau\sqrt{E_0} = 0.01; 0.1; 0.2$



Mass dependent fermion production in SU(2) [pulse-like time dep.]



t: time in the CM frame



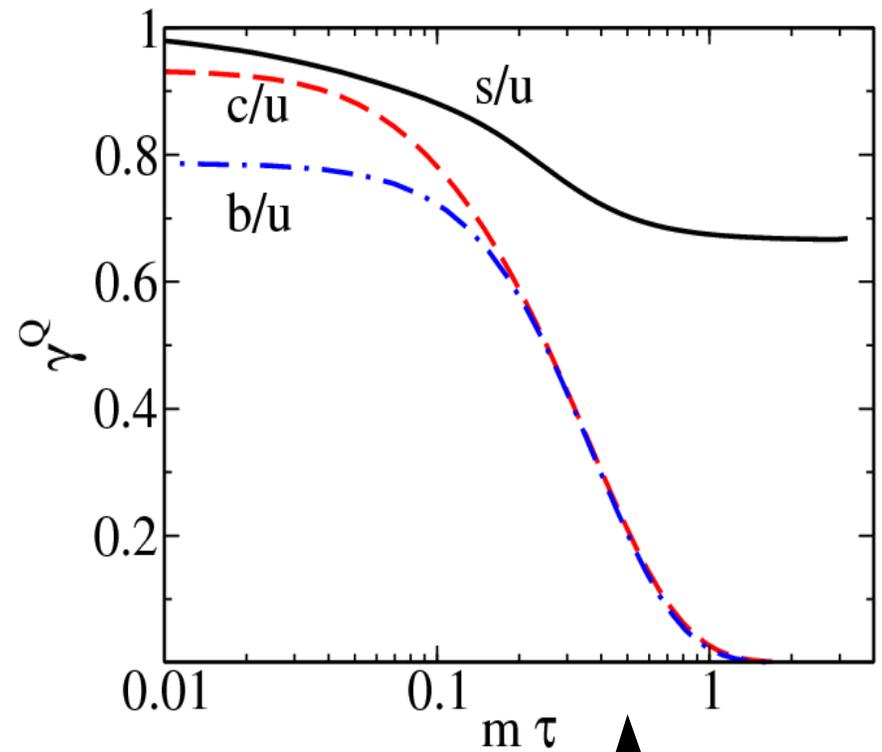
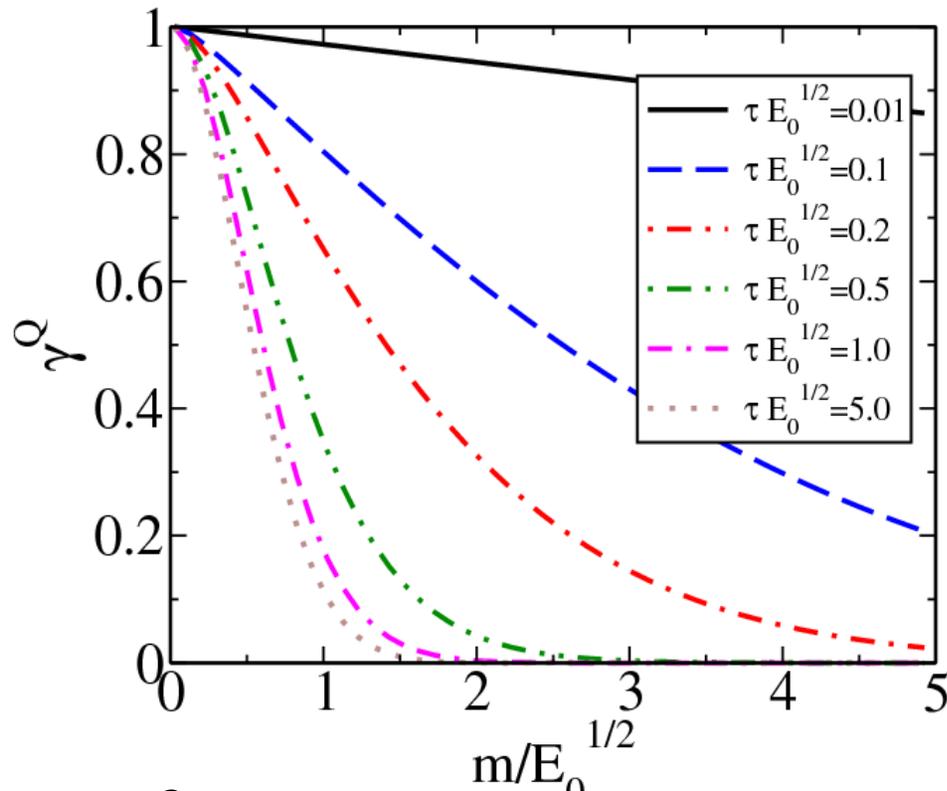
τ: pulse width ($t \rightarrow \infty$)

Full line: $\tau \sqrt{E_0} = 0.1$ ($\tau = 0.05 \text{ fm}$)

Dashed line: $\tau \sqrt{E_0} = 0.5$ ($\tau = 0.25 \text{ fm}$)

$E_0 = 0.68 \text{ GeV/fm}$, $g=2$ $\rightarrow \rightarrow \rightarrow$ $g \cdot E_0 \propto \kappa = 1.17 \text{ GeV/fm}$

Mass dependent fermion production in SU(2) [pulse-like time dep.]



$$\gamma^Q = \lim_{t \rightarrow \infty} n_Q(t) / n_u(t)$$

flavour suppression factor

$m\tau$ scaling !!!!

Blue line: $\tau\sqrt{E_0} = 0.1$ ($\tau = 0.05$ fm)

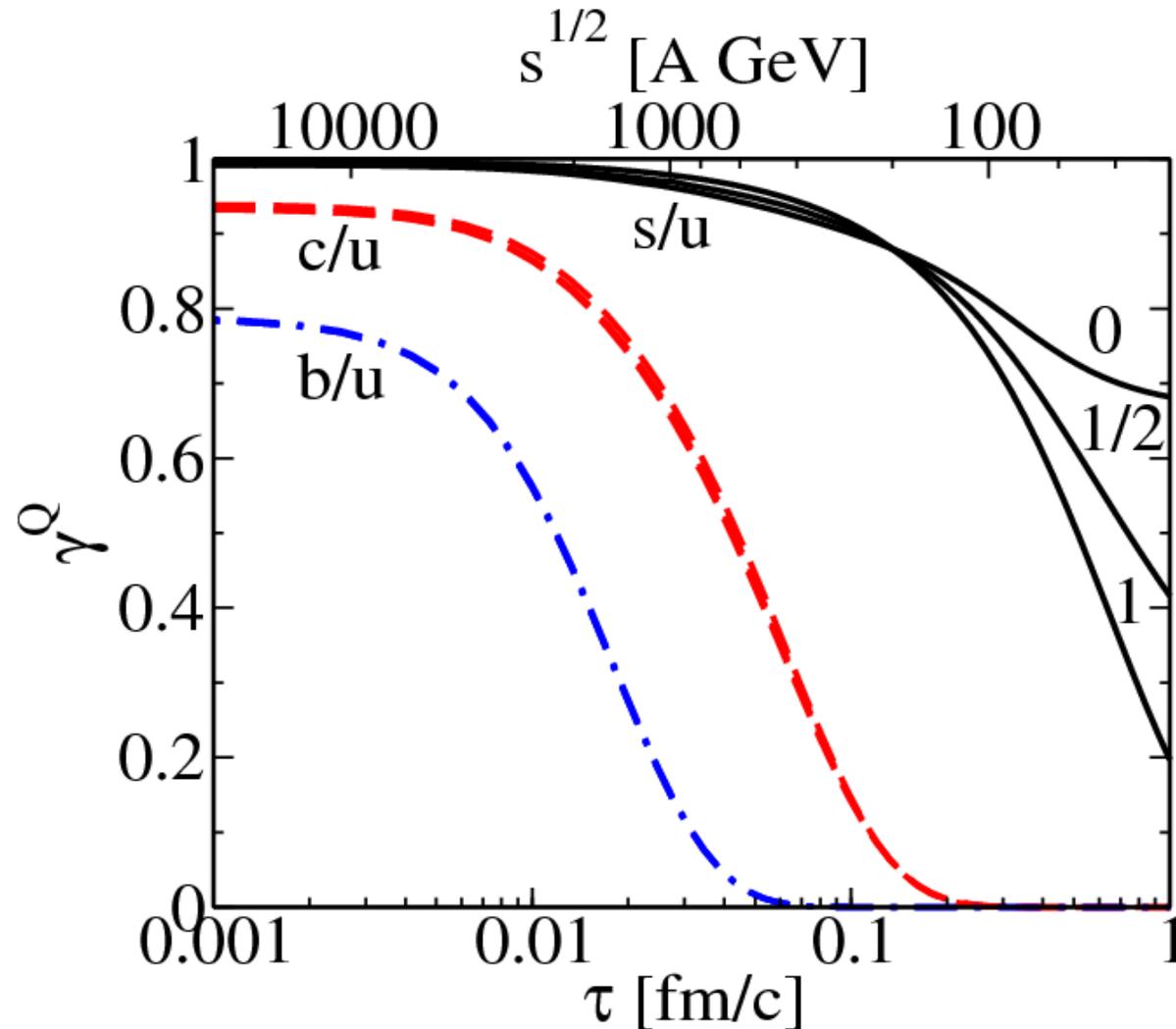
At large τ heavy quarks are suppressed.

Enhanced heavy fermion production at small τ

$$\tau_{\text{eff}} = \delta + m^{-1}$$

$$[m_{\text{eff}} \Rightarrow \delta^{-1}]$$

Mass dependent fermion production in SU(2) [pulse-like time dep.]



***Collisional energy dependence of the quark flavour suppression
 + $E_0(t) = E_0 (\tau_0 / \tau)^\beta$ where $\beta : 0, 1/2, 1$***

Mass dependent fermion production in SU(2)

Numerical values for suppression factors :

	<i>Schwinger</i>	<i>130 AGeV</i>	<i>200 AGeV</i>	<i>1 ATeV</i>	<i>2 ATeV</i>	<i>5.5 ATeV</i>
<i>s</i>	0.74	0.84	0.88	0.96	0.98	0.99
<i>c</i>	3 10⁻⁹	9 10⁻³	0.06	0.66	0.82	0.91
<i>b</i>	≈ 0	≈ 0	10⁻⁶	0.15	0.45	0.72

Effective string constants and massive fermion suppression in SU(2)

Schwinger formula for static field and static string:

$$\frac{dN}{dt d^3 x} = \frac{\kappa^2}{4\pi^3} \exp(-\pi m^2 / \kappa)$$

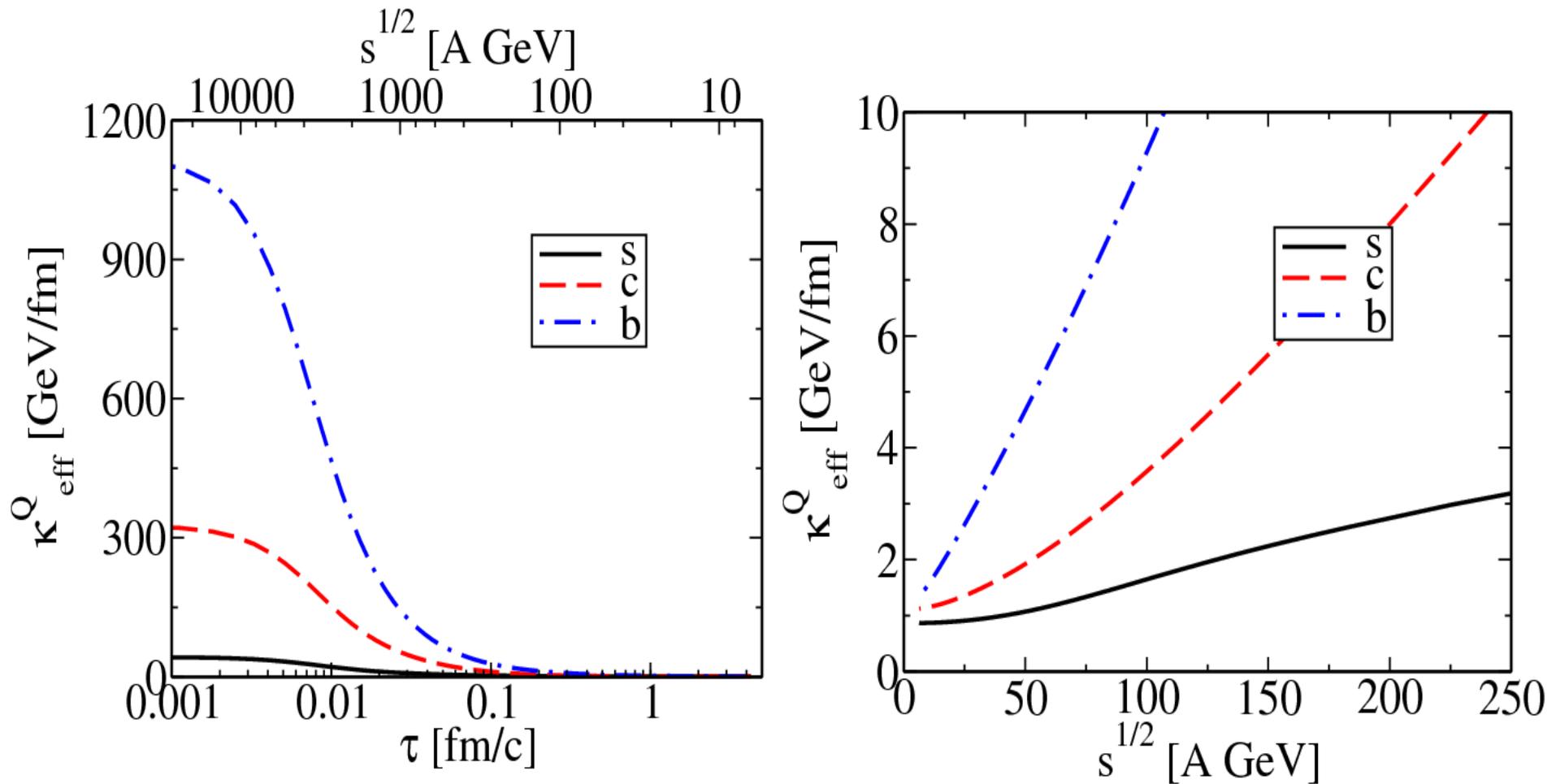
Suppression factor:

$$\gamma^Q = \exp(-\pi (m_Q^2 - m_q^2) / \kappa)$$

**Results of our dynamical calculation can be fit by
an effective string tension, κ_{eff} :**

$$\gamma_{\infty}^Q(\kappa_{eff}^Q) = \gamma^{(Q)}(\tau)$$

Effective string constants and massive fermion suppression in SU(2)



***Pulse width and collisional energy dependence
of the flavour dependent effective string constant
---- too much difference (and what about for light quarks)***

Effective string constants and massive fermion suppression in SU(2)

Solution:

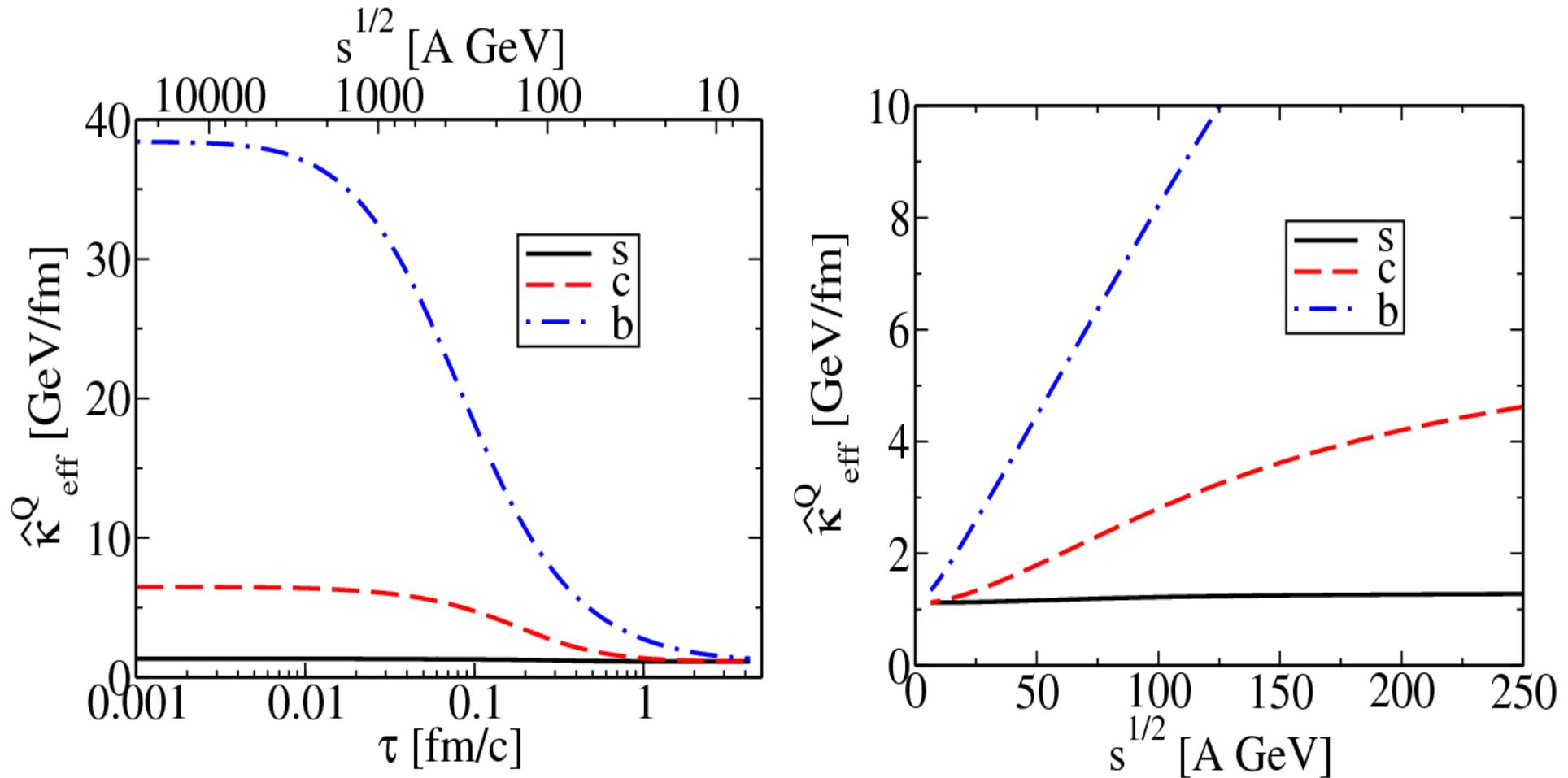
Let us keep a fixed string constant for the light quarks

$$\hat{K}_{eff}^u = 1.17 \text{ GeV} / \text{fm}$$

and fix flavour specific effective string constant for the heavier quarks (strange, charm, bottom):

$$\hat{\gamma}_{\infty}^Q = \left(\frac{\hat{K}_{eff}^Q}{\hat{K}_{eff}^u} \right)^2 \exp \left(-\pi \frac{m_Q^2}{\hat{K}_{eff}^Q} + \pi \frac{m_u^2}{\hat{K}_{eff}^u} \right) = \gamma^Q(\tau)$$

Effective string constants and massive fermion suppression in SU(2)



***Pulse width and collisional energy dependence
of the flavour specific effective string constants***

--> strange string constant is nice, for heavy Q we get large values

Effective string constants and massive fermion suppression in SU(2)

*Numerical values for flavour specific effective string constants
in GeV/fm:*

	<i>130 AGeV</i>	<i>200 AGeV</i>	<i>1 ATeV</i>	<i>2 ATeV</i>	<i>5.5 ATeV</i>
<i>u,d</i>	<i>1.17</i>	<i>1.17</i>	<i>1.17</i>	<i>1.17</i>	<i>1.17</i>
<i>s</i>	<i>1.24</i>	<i>1.26</i>	<i>1.32</i>	<i>1.33</i>	<i>1.34</i>
<i>c</i>	<i>3.32</i>	<i>4.2</i>	<i>6.1</i>	<i>6.3</i>	<i>6.5</i>
<i>b</i>	<i>10.3</i>	<i>14.7</i>	<i>32</i>	<i>36</i>	<i>38</i>

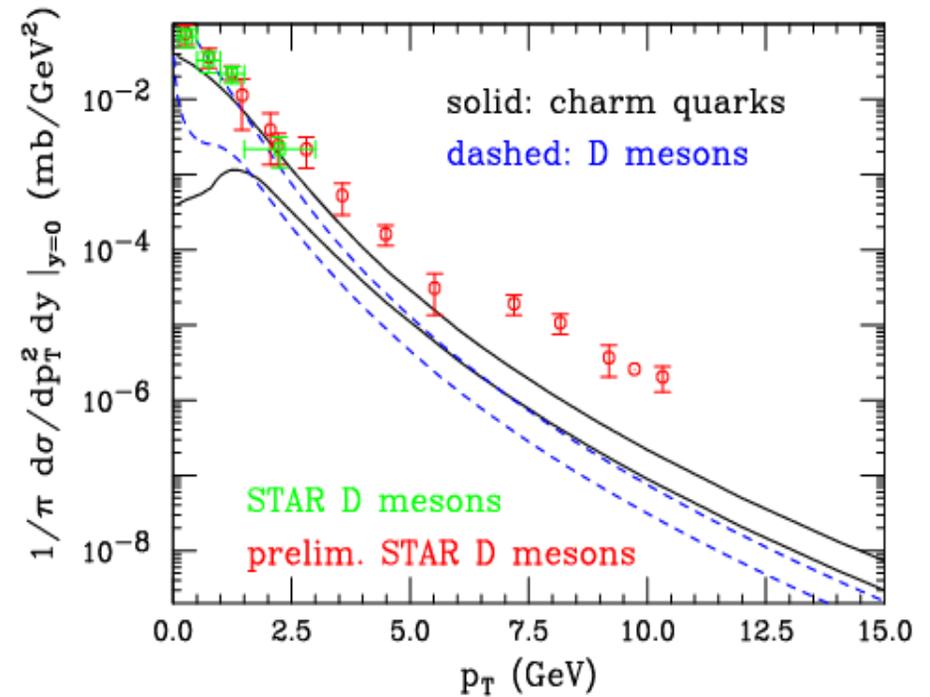
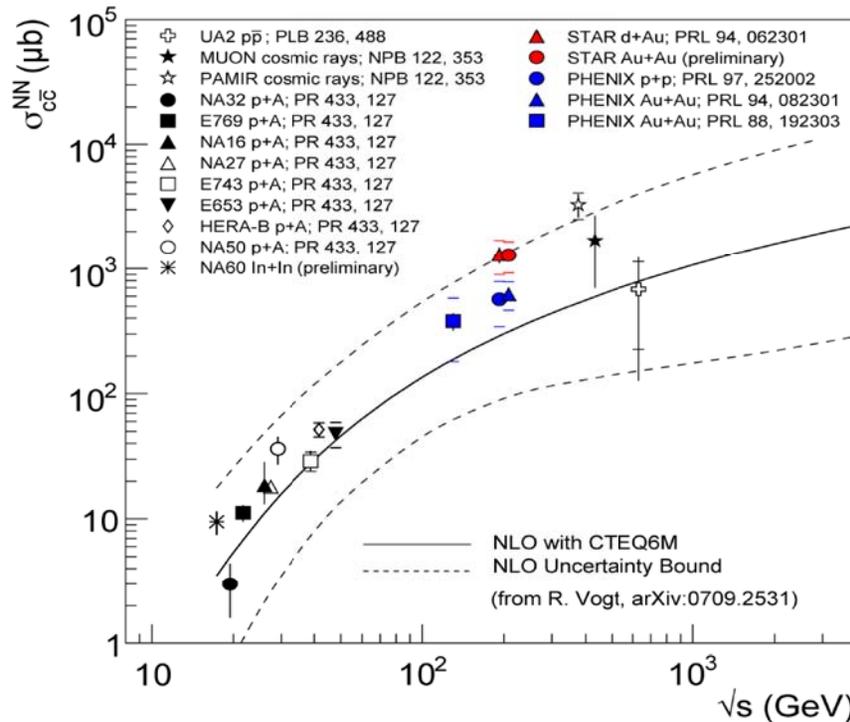
Saturation at higher LHC energies !!!!

Discussion: How large is the primary charm production ?

Do we have room for non-perturbative charm yield ?

**Charm pair production can be (must be ?) calculated in pQCD:
LO, NLO, NLL, FONLL, ...**

Results at RHIC energies



R. Vogt, EPJ ST 155 (2008) 213.

M. Cacciari, ..., PRL95,122001

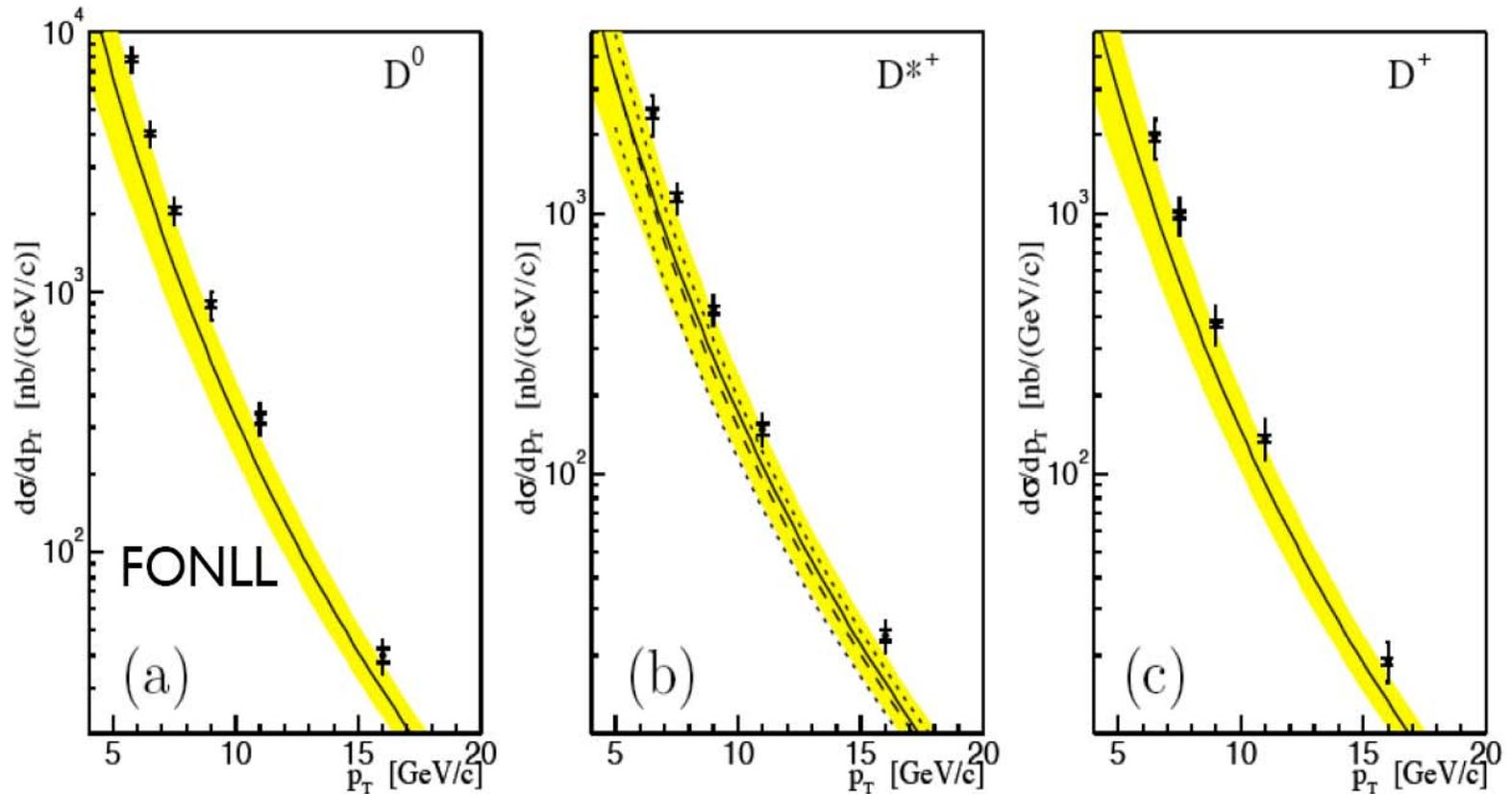
Data are at the upper limit of theory (or beyond) !?? (m_c = 1.2 GeV)

Discussion: How large is the primary charm production ?

Do we have room for non-perturbative charm yield ?

Charm production at FERMILAB energies ($pp\bar{p}$, $\sqrt{s} = 1.96$ TeV)

CDF Run II $c \rightarrow D$ data [PRL 91:241804,2003]

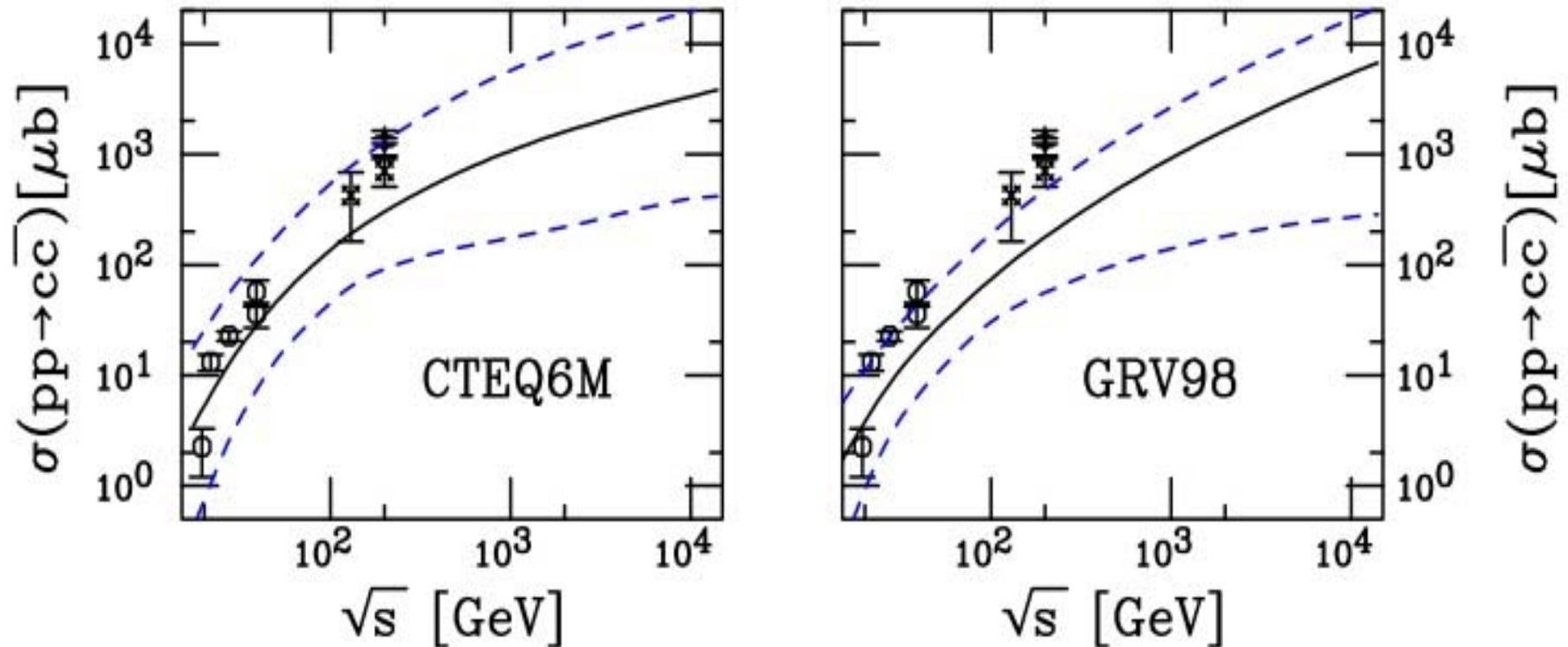


Data are at the upper limit of theory (or beyond) !?? (factor of 2 ?)

Discussion: How large is the primary charm production ?

Do we have room for non-perturbative charm yield ?

Charm production at LHC energies (pp , $\sqrt{s} = 2-14$ TeV)



R. Vogt, Private comm., 2009

Large uncertainties --> more data are needed to fix parameters

There is room for non-perturbative contributions (today).

Theoretical conclusions (today) on this section:

- 1. Particle production mechanisms are not fully explored in non-Abelian cases, especially in case of strong fields.***
- 2. If the overlap of colliding objects is very short (the time scale of the initial phase is also short), then***
 - transverse momentum spectra depend on overlap***
 - heavy quark production is not suppressed large mass.***
- 3. High- p_T spectra can carry message about the formation of a coherent strong field (even in pp collision)***
- 4. Heavy quark production can carry message about the time scale of the initial overlap at LHC energies.***

(strange quark mass is too close to light quark mass)
- 5. LHC data are extremely interesting,***

turning point is $\sim \sqrt{s} = 1-2 \text{ TeV}$ (and wait for LHC data)

Experimental side: Particle identification at high- p_T at LHC

1. LHC ALICE: TPC + TOF + ITS

Statistically up to 40-50 GeV/c

2. LHC ALICE upgrade: VHMPID (track-by-track)

Very High Momentum Particle Identification Detector

RICH modul + Trigger modul

Module-0: Installation in 2013 (hopefully)

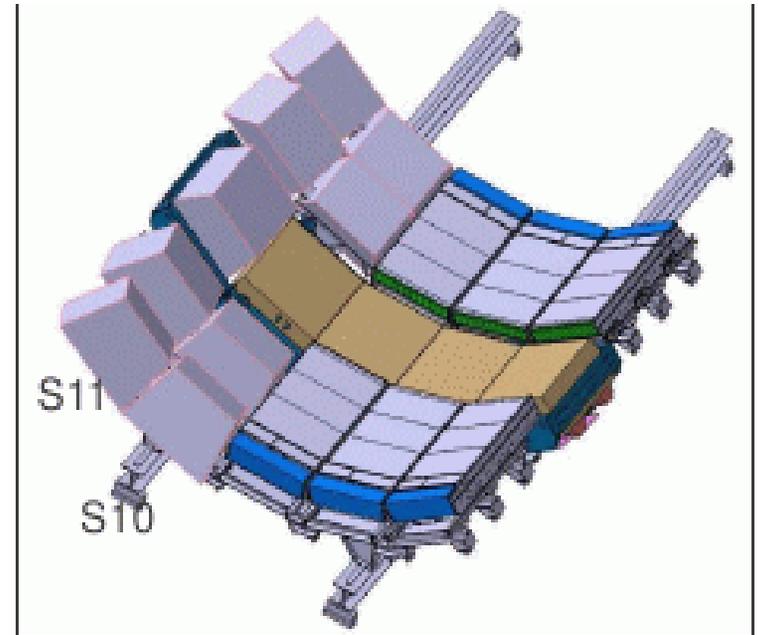
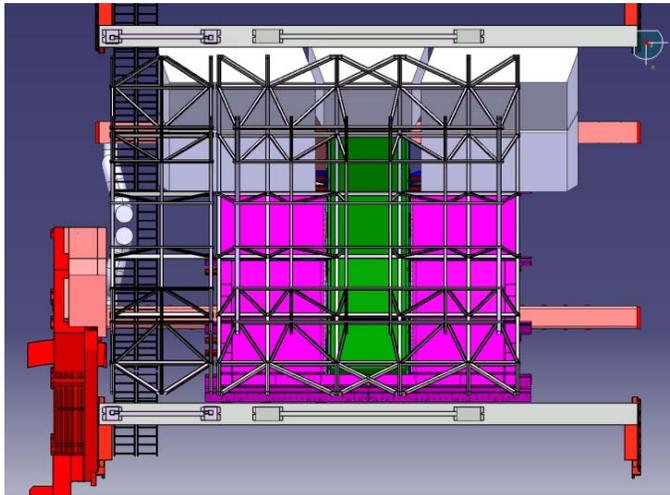
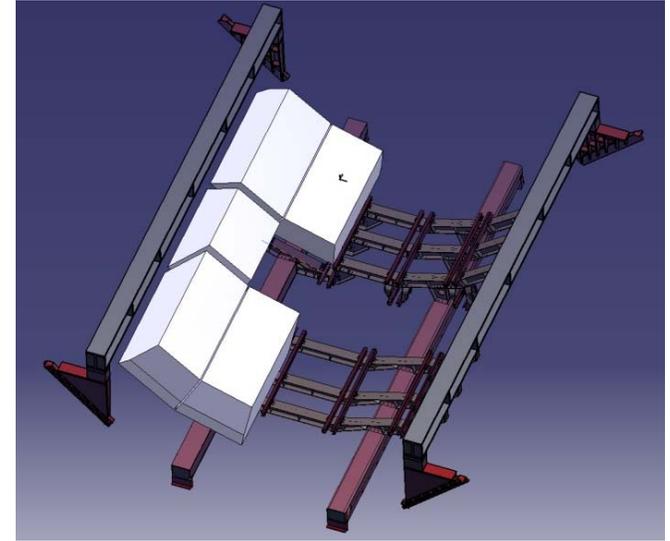
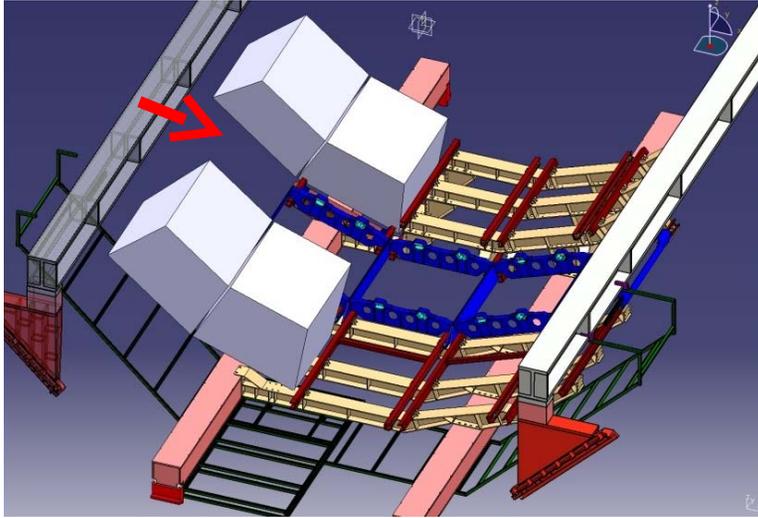
Modul-Xs: Installation in 2015

VHMPID mission: to identify charged hadrons

up-to 25 GeV (C_4F_{10})

or at even higher momenta (CH_4)

VHMPID layout evolution (2009-2010)



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