

EL SABOR DE LA FÍSICA

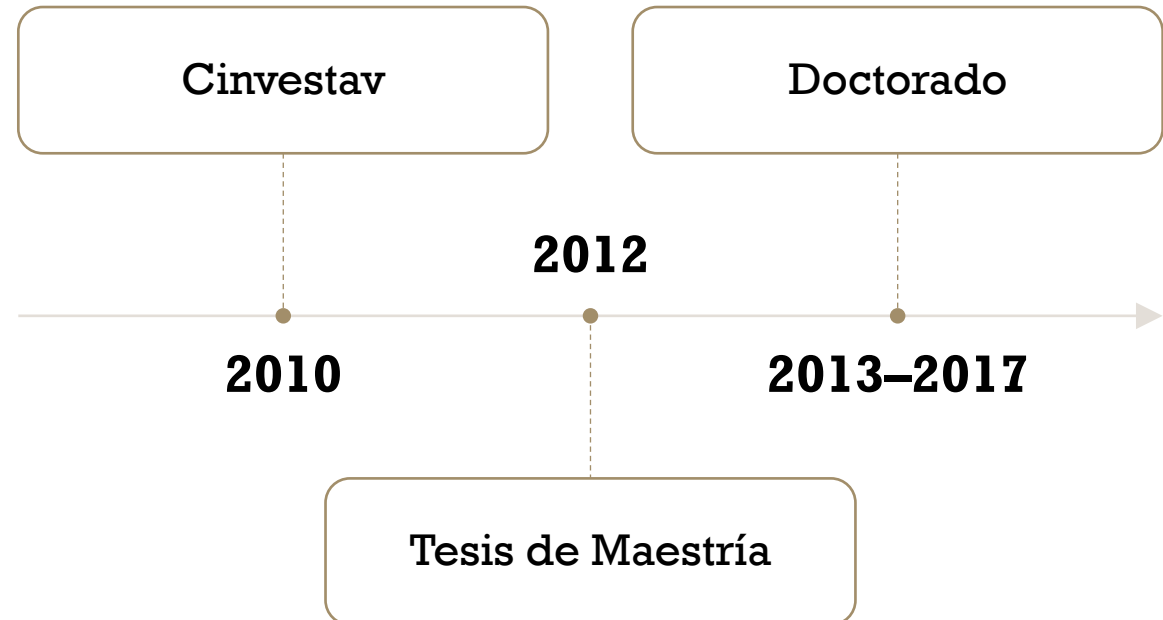
Taller en celebración del 60 aniversario de

Gabriel López Castro

Sergio Tostado
Universidad Santiago de Cali

**“MEZCLAS DE
SABOR”**

INICIOS



MATRIZ DE MEZCLA DE LOS QUARKS

Corriente cargada:

$$\frac{-g}{\sqrt{2}}(\bar{u}_L, \bar{c}_L, \bar{t}_L)\gamma^\mu W_\mu^+ V_{\text{CKM}} \begin{pmatrix} d_L \\ s_L \\ b_L \end{pmatrix} + \text{h.c.} \quad \longrightarrow \quad V_{\text{CKM}} \equiv V_L^u V_L^{d\dagger} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

$$V_{\text{CKM}} = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix}$$

- Unitaria

$$V_{\text{CKM}} V_{\text{CKM}}^\dagger = \mathbb{1}$$

- Violación CP

$$V_{\text{CKM}} \neq V_{\text{CKM}}^*$$

- Patrón jerárquico

$$s_{13} \ll s_{23} \ll s_{12} \ll 1$$

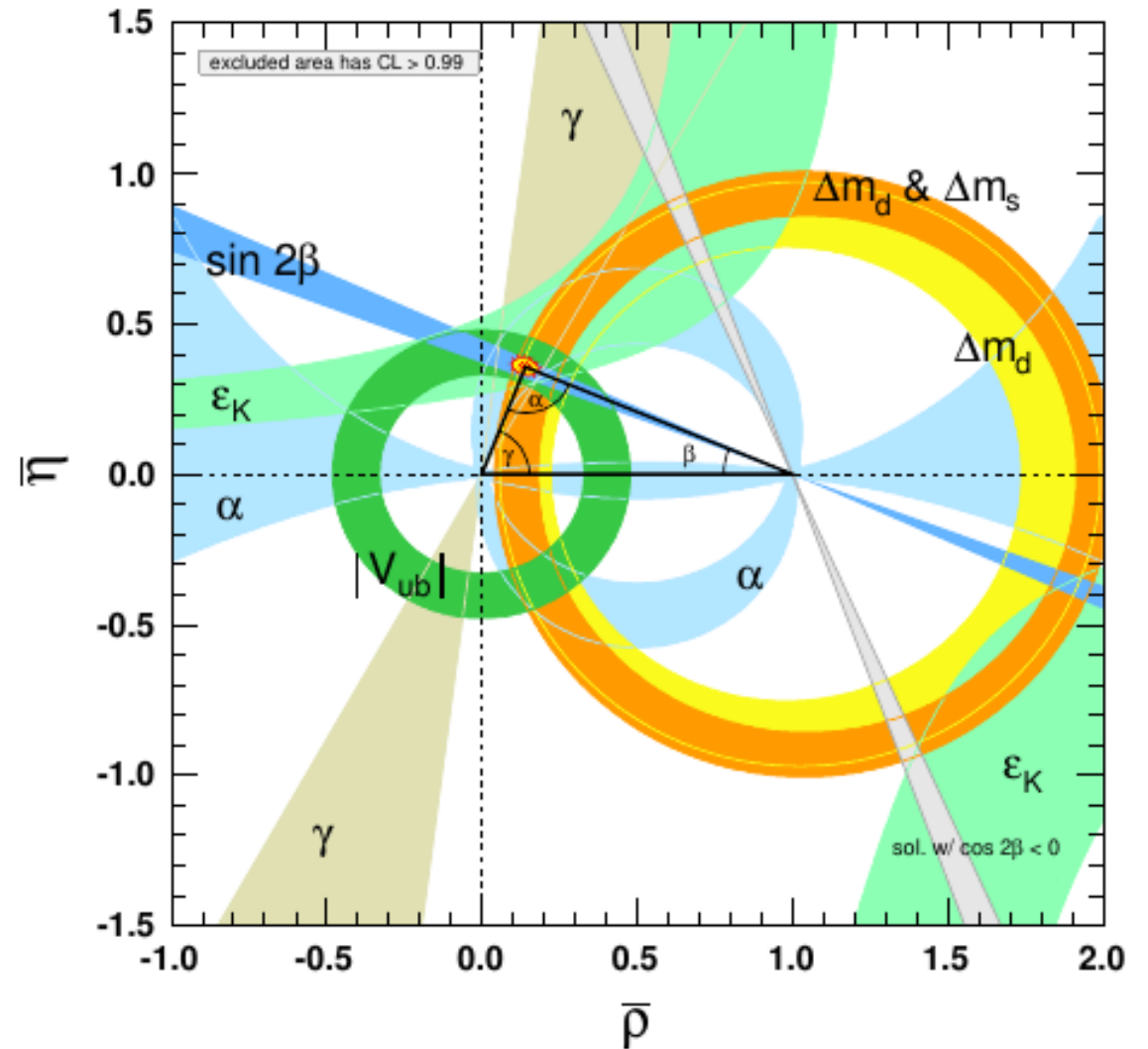
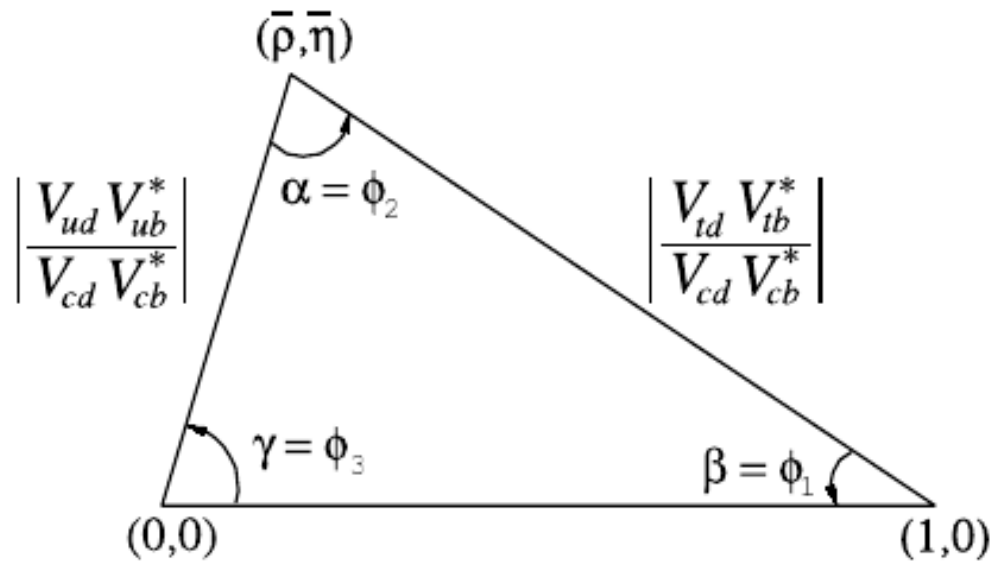


TRIÁNGULOS UNITARIOS

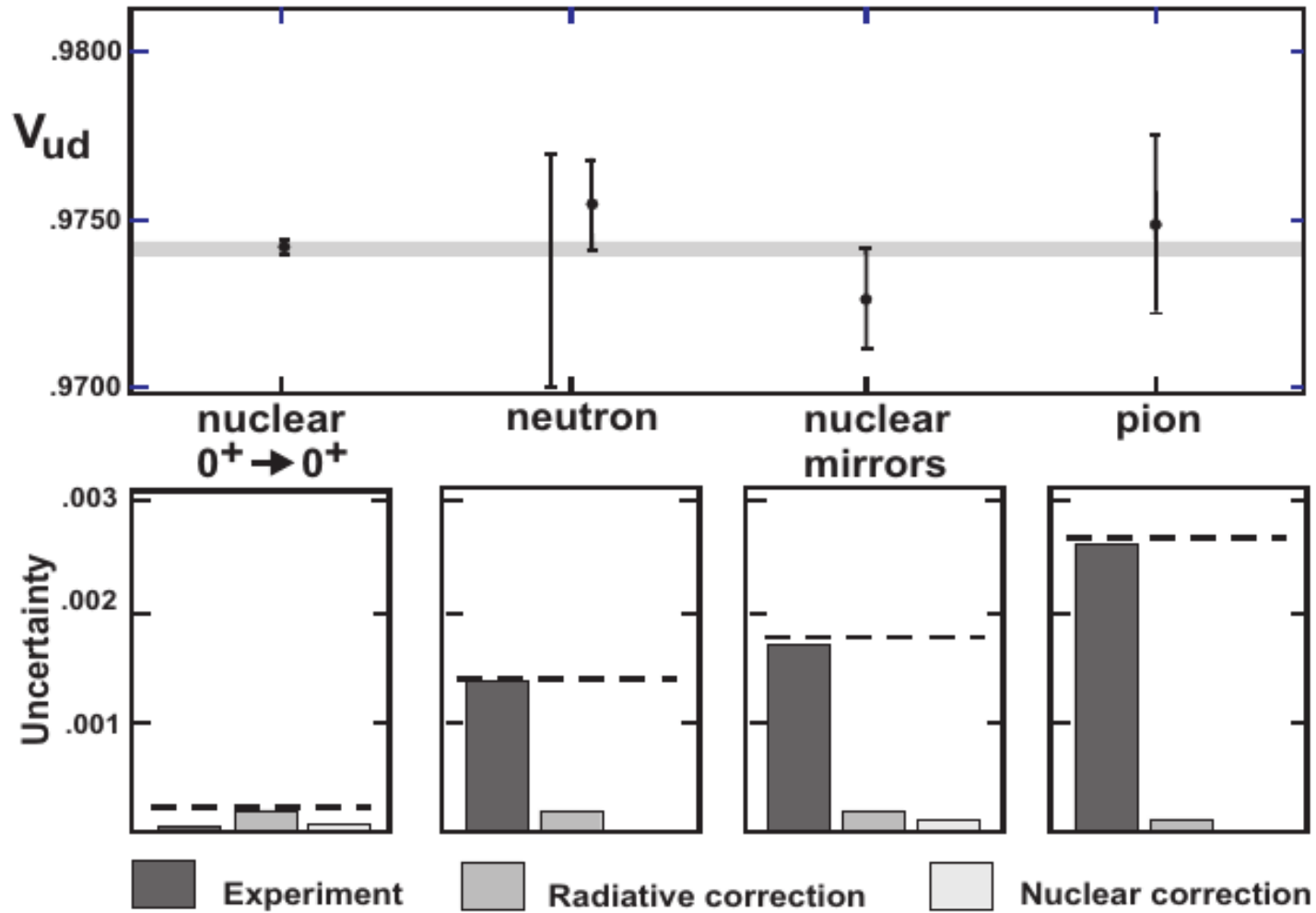
$$V_{ud} V_{ub}^* + V_{cd} V_{cb}^* + V_{td} V_{tb}^* = 0$$

$$\frac{V_{ud} V_{ub}^*}{V_{cd} V_{cb}^*} + 1 + \frac{V_{td} V_{tb}^*}{V_{cd} V_{cb}^*} = 0,$$

$$-(\bar{\rho} + i\bar{\eta}) + 1 - (1 - \bar{\rho}) + i\bar{\eta} = 0$$



CORRECCIONES RADIATIVAS



Hardy and Towner, CIPANP 2018 (arXiv: 1807.01146)

Neutrón

$$\frac{1}{\tau_n} = \frac{G_\mu^2 |V_{ud}|^2}{2\pi^3} m_e^5 (1 + 3g_A^2) (1 + RC) f$$

Czarnercki, Marciano and Sirlin *PRD* 100 (2019) 7, 073008

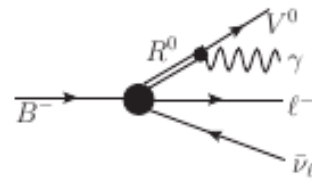
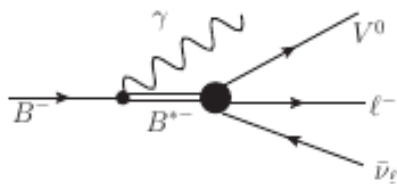
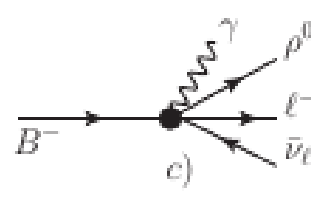
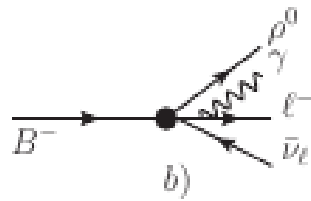
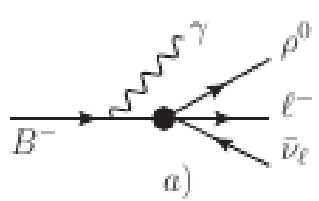
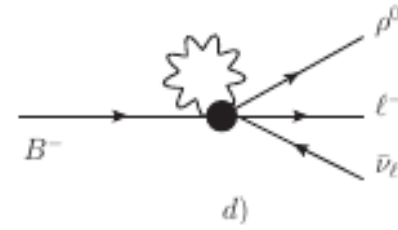
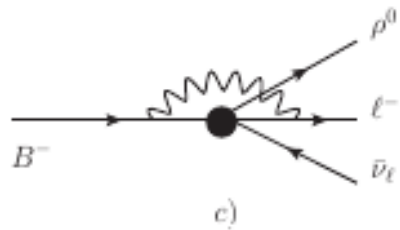
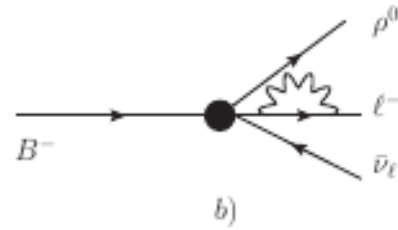
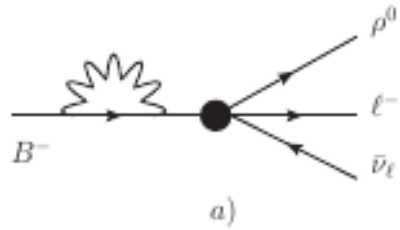
- Incertidumbres: factores de forma y del tiempo de vida
- Resultados más precisos para el neutrón
→ Factorizar adecuadamente las RC (~1%)

ST, Tesis de Maestría, Cinvestav 2011.



CORRECCIONES RADIATIVAS:

V_{ub}, V_{cb}



$$B^- \rightarrow (\rho^0, \omega) \ell^- \bar{\nu}_\ell$$

$$\delta_T^1(\ell) = \begin{cases} (1.62 \pm 0.10 \pm 0.04)\%, & \text{for } \ell = \mu \\ (1.63 \pm 0.11 \pm 0.04)\%, & \text{for } \ell = e \end{cases}$$

$$B^- \rightarrow D^{*0} \ell^- \bar{\nu}$$

$$\delta_T^1(\ell) = \begin{cases} (1.53 \pm 0.06 \pm 0.04)\%, & \text{for } \ell = \mu \\ (1.53 \pm 0.08 \pm 0.04)\%, & \text{for } \ell = e \end{cases}$$

hasta 10% en Dalitz Plot

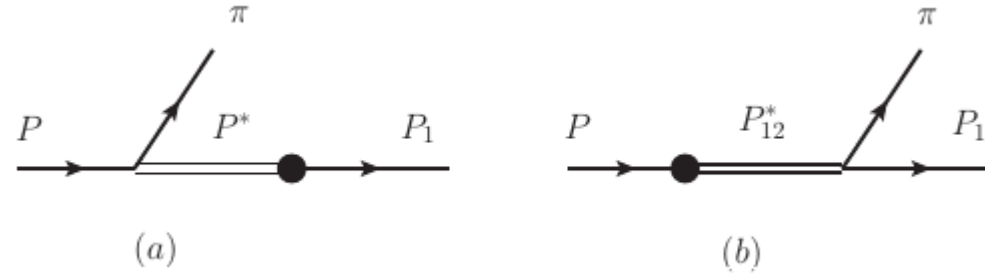
➤ **Importante para extracción precisa de FFs**

G. López-Castro and ST, EPJC 76, 495 (2016)



OTRAS CORRECCIONES

$$P \rightarrow P_2 P^* \rightarrow P_1 P_2 \ell \nu_\ell$$



$$|V_{ub}| = \sqrt{\frac{B(B \rightarrow (\pi\pi)_\rho \ell \nu_\ell)}{\tau_B \cdot \Delta\zeta \cdot (1 + \delta_{P^*}) B(\rho \rightarrow \pi\pi)}}$$

Neutro (cargado)

$$\delta_{B^*} = 1.7 (6.4)\%$$



$$= 1.9(8.2)\%$$

$$|V_{ub}| = (3.73 \pm 0.30) \times 10^{-3}$$

$$|V_{cd}|_{\rho+D^*} = 0.224 \pm 0.011$$

$$|V_{cb}| \quad \text{Sin cambios}$$

**Incertidumbre
dominada por los
factores de forma**



PANORAMA ACTUAL

$$V_{\text{CKM}} = \begin{pmatrix} 0.97401 \pm 0.00011 & 0.22650 \pm 0.00048 & 0.00361^{+0.00011}_{-0.00009} \\ 0.22636 \pm 0.00048 & 0.97320 \pm 0.00011 & 0.04053^{+0.00083}_{-0.00061} \\ 0.00854^{+0.00023}_{-0.00016} & 0.03978^{+0.00082}_{-0.00060} & 0.999172^{+0.000024}_{-0.000035} \end{pmatrix}$$

$$\begin{aligned} \lambda &= 0.22650 \pm 0.00048, & A &= 0.790^{+0.017}_{-0.012}, \\ \bar{\rho} &= 0.141^{+0.016}_{-0.017}, & \bar{\eta} &= 0.357 \pm 0.011. \end{aligned}$$

$$V_{\text{CKM}} = \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4)$$



MEZCLA DE NEUTRINOS

La corriente cargada:

$$-\mathcal{L}_{CC} = \frac{g}{\sqrt{2}} (\bar{e} \ \bar{\mu} \ \bar{\tau})_L \gamma^\mu U \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix} W_\mu^- + h.c.$$

- $U_\nu^\dagger M_\nu U_\nu^* = \text{Diag}(m_1, m_2, m_3) \equiv M_\nu^{diag}$
- U_ℓ esta asociada con la diagonalización M_ℓ .



$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = U \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix} \quad \begin{matrix} m_1 \\ m_2 \\ m_3 \end{matrix}$$

$$U_{PMNS} = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta_{CP}} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta_{CP}} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta_{CP}} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta_{CP}} & -c_{12}s_{23} - c_{23}s_{12}s_{13}e^{i\delta_{CP}} & c_{23}c_{13} \end{pmatrix} P_\nu.$$

$$c_{ij} \equiv \cos \theta_{ij}, s_{ij} \equiv \sin \theta_{ij}$$

Fases de Majorana

$$P_\nu = \text{Diag}(e^{-i\frac{\beta_1}{2}}, e^{-i\frac{\beta_2}{2}}, 1).$$



SIMETRIA MU-TAU

Primeros Experimentos

→ $U_{PMNS} |_{\theta_{13}=0, \theta_{23}=45^\circ}$

$$U = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix}$$

$$U = U^{\mu-\tau} = \begin{pmatrix} c_{12} & s_{12} & 0 \\ \frac{-s_{12}}{\sqrt{2}} & \frac{c_{12}}{\sqrt{2}} & \frac{-1}{\sqrt{2}} \\ \frac{-s_{12}}{\sqrt{2}} & \frac{c_{12}}{\sqrt{2}} & \frac{1}{\sqrt{2}} \end{pmatrix}, \quad |U_{\mu i}| = |U_{\tau i}|$$

Dado que: $M_\nu = U M_\nu^{diag} U^T$.

$$M_\nu^{\mu-\tau} = \begin{pmatrix} m_1 c_{12}^2 + m_2 s_{12}^2 & (m_2 - m_1) \frac{s_{212}}{\sqrt{8}} & (m_2 - m_1) \frac{s_{212}}{\sqrt{8}} \\ (m_2 - m_1) \frac{s_{212}}{\sqrt{8}} & \frac{1}{2} (m_1 s_{12}^2 + m_2 c_{12}^2 + m_3) & \frac{1}{2} (m_1 s_{12}^2 + m_2 c_{12}^2 - m_3) \\ (m_2 - m_1) \frac{s_{212}}{\sqrt{8}} & \frac{1}{2} (m_1 s_{12}^2 + m_2 c_{12}^2 - m_3) & \frac{1}{2} (m_1 s_{12}^2 + m_2 c_{12}^2 + m_3) \end{pmatrix}$$

$M_\nu^{\mu-\tau}$ invariante ante el intercambio de etiquetas $\nu_\mu \leftrightarrow \nu_\tau$.



DESVIACIONES AL PATRÓN TBM

Cuando $\sin^2 \theta_{12} = 1/3$

$$U_{TBM} = \begin{pmatrix} \sqrt{2/3} & \sqrt{1/3} & 0 \\ -\sqrt{1/6} & \sqrt{1/3} & -\sqrt{1/2} \\ -\sqrt{1/6} & \sqrt{1/3} & \sqrt{1/2} \end{pmatrix}$$

Se puede de generar en algunas extensiones del ME.

S.T. Petcov, Nucl. Phys. B 892 (2015) 400.
P.P. Novichkov, et.al., PLB 793 (2019) 247.

Se han explorado algunas correcciones de la forma

$$U_{PMNS} = U_{TBM} U_{Corr}$$

Ucorr Real:

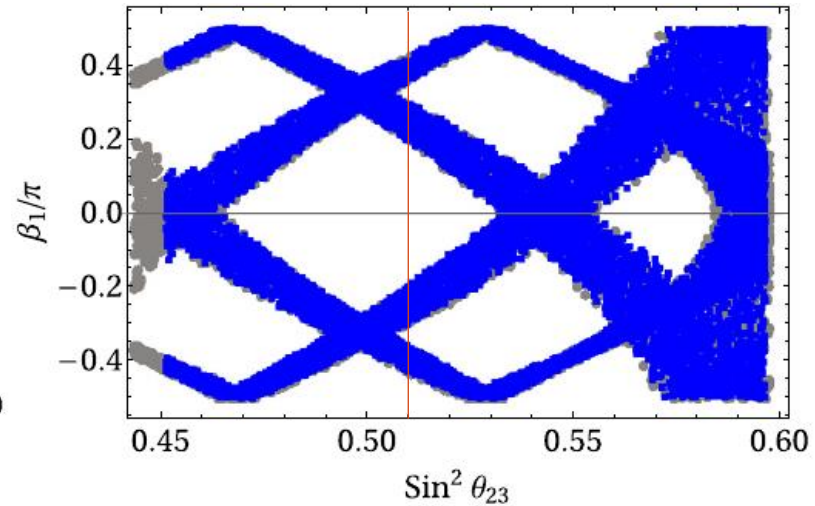
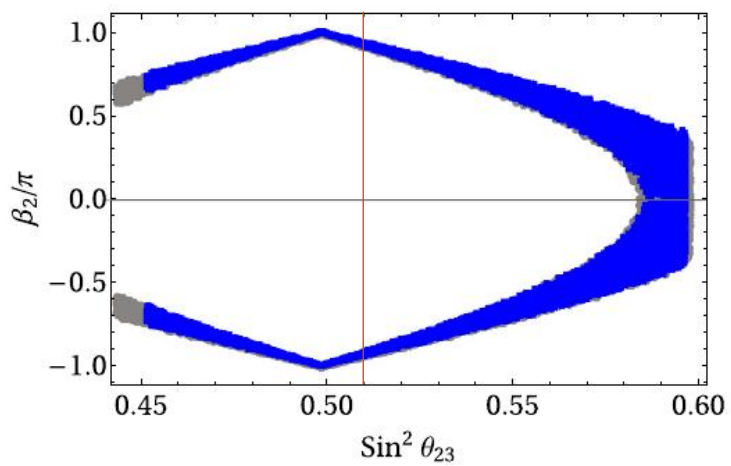
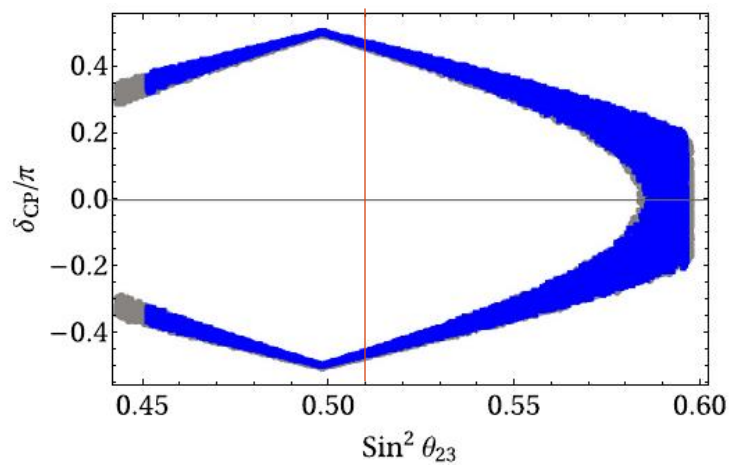
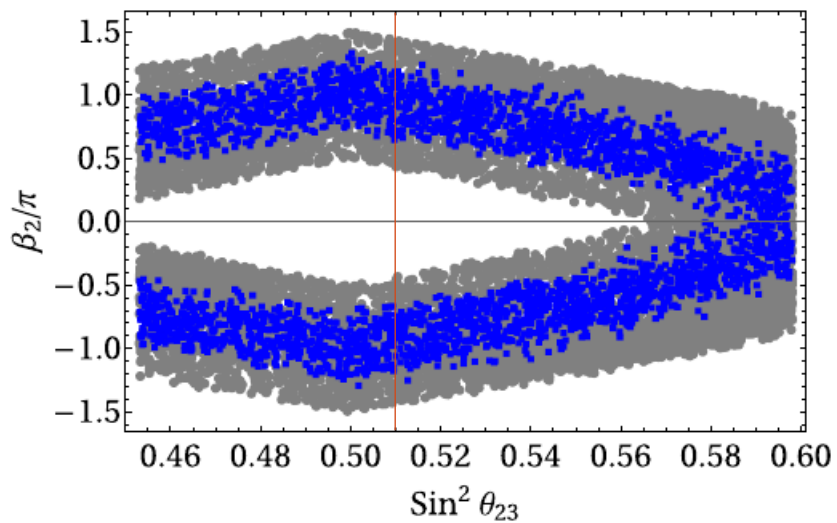
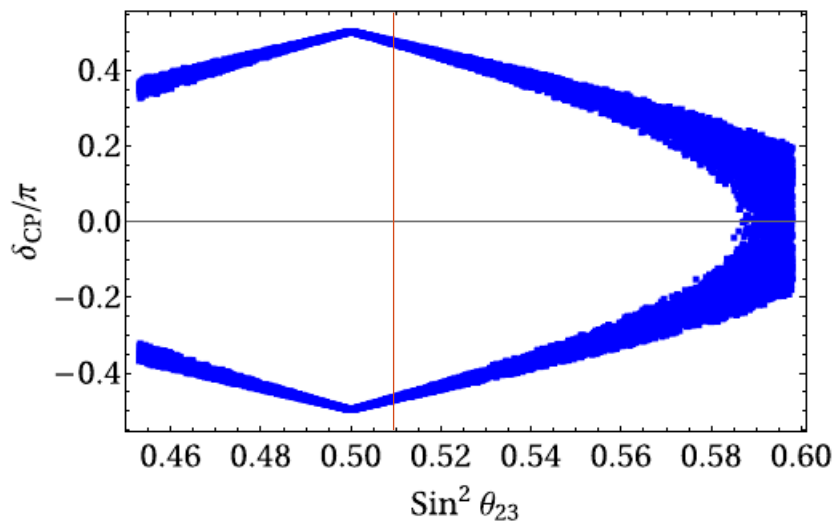
S.K. Garg, S. Gupta, J. High Energy Phys. 10 (2013) 128.
Y. Shimizu, M. Tanimoto, K. Yamamoto, Mod. Phys. Lett. A 30 (2015) 1550002.

Ucorr Compleja (fases CP Majorana)

D.C. Rivera-Agudelo, A. Pérez-Lorenzana, ST, PLB 794, 89(2019).
D.C. Rivera-Agudelo, ST, NPB 965, 115359 (2021).



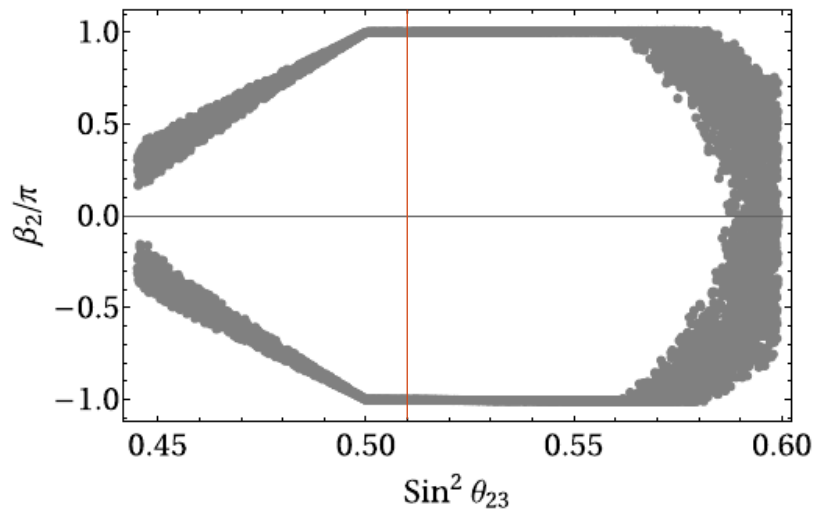
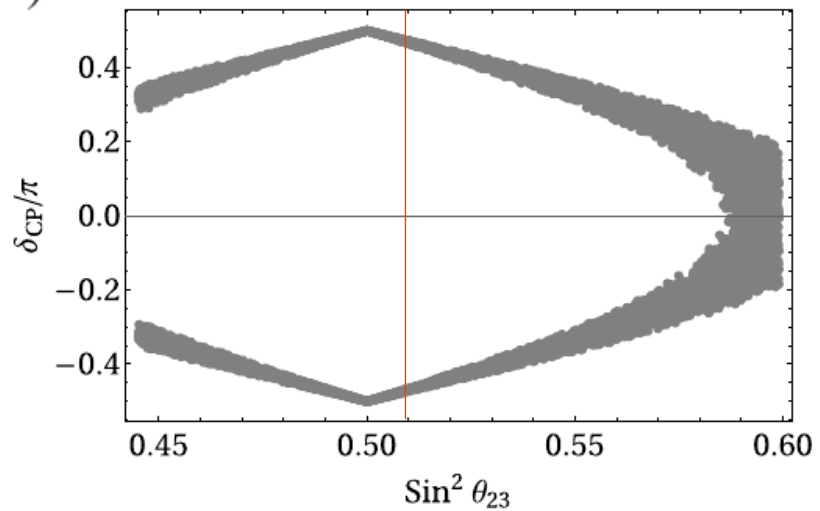
$$U_{12}(\phi, \sigma)U_{13}(\phi', \sigma')$$



$$\sigma' = 0$$



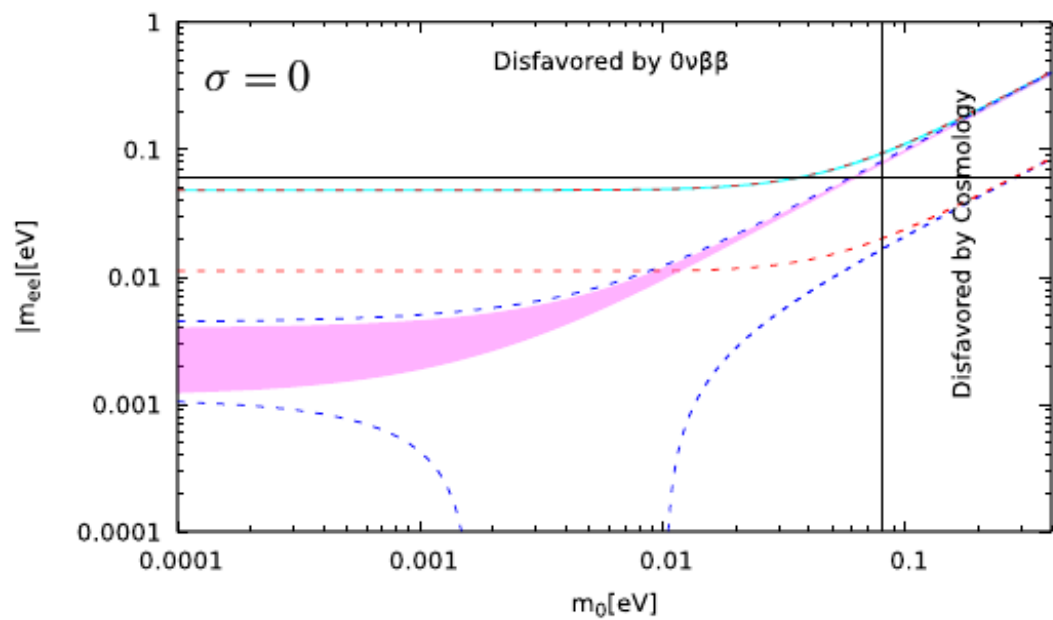
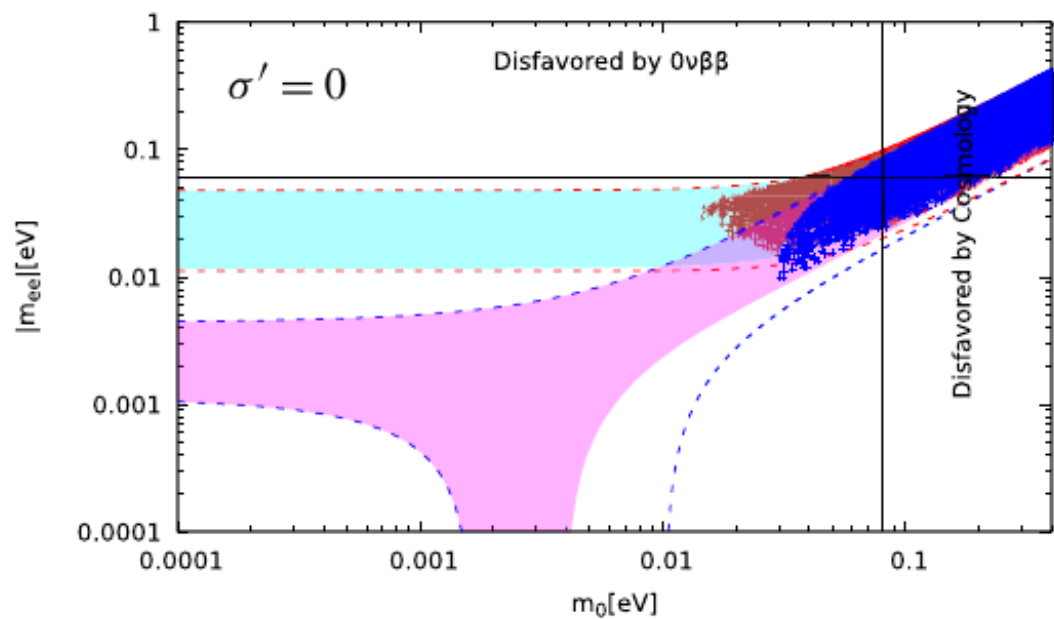
$$U_{12}(\phi, \sigma)U_{13}(\phi', \sigma')$$



$$\beta_1 = 0$$

$$0\nu\beta\beta$$

$$m_{ee} = \left| \sum_i m_i U_{ei}^2 \right|$$



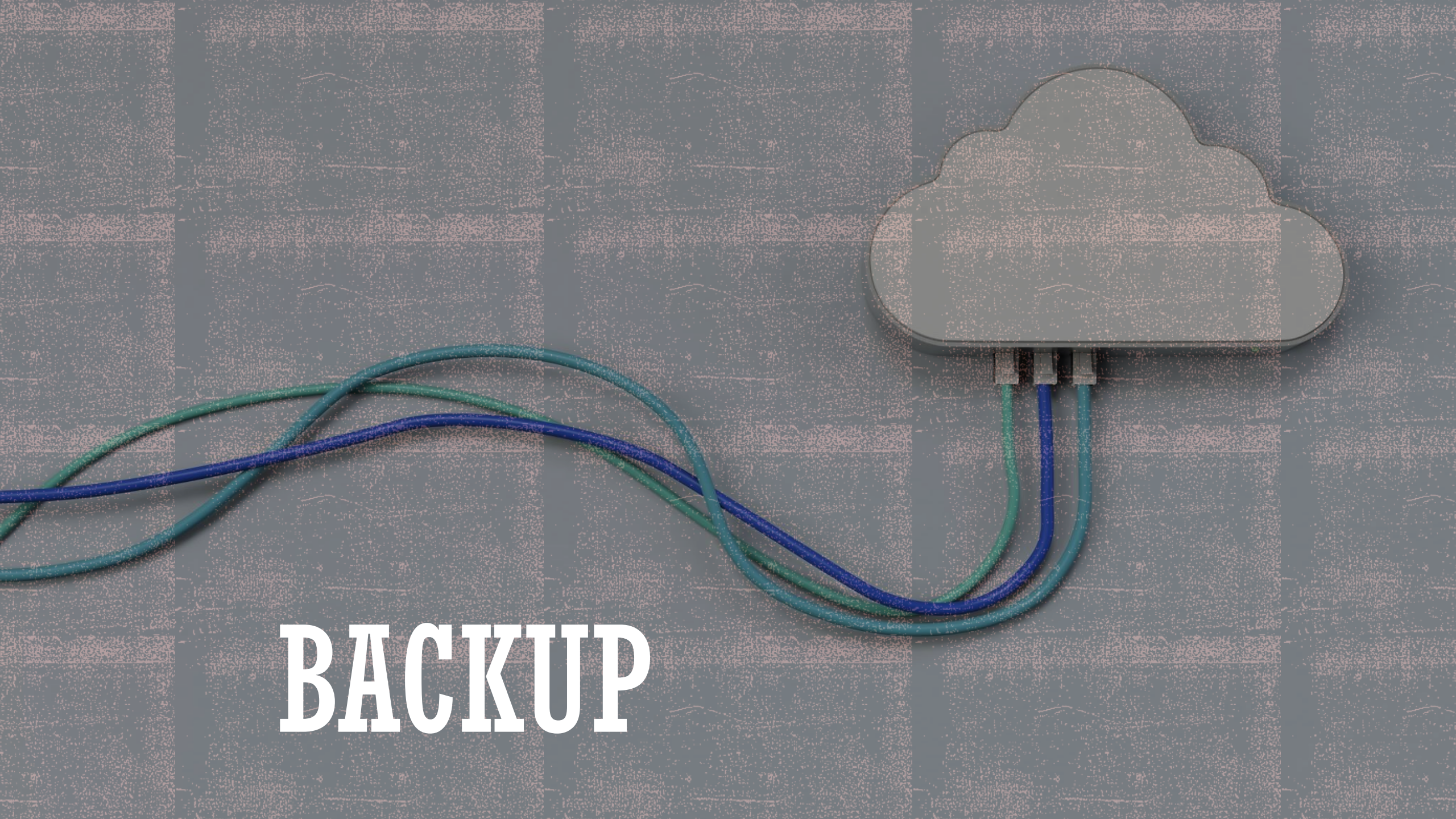
CONCLUSIONES Y PERSPECTIVAS

- Las pruebas de precisión en el sector de mezclas son indispensables en las búsquedas indirectas de nueva física.
- Los patrones de masas y mezclas de quarks y leptones se pueden relacionar en algunos modelos de sabor.
- Hay fuentes de violación CP adicionales en el sector de neutrinos.



GRACIAS





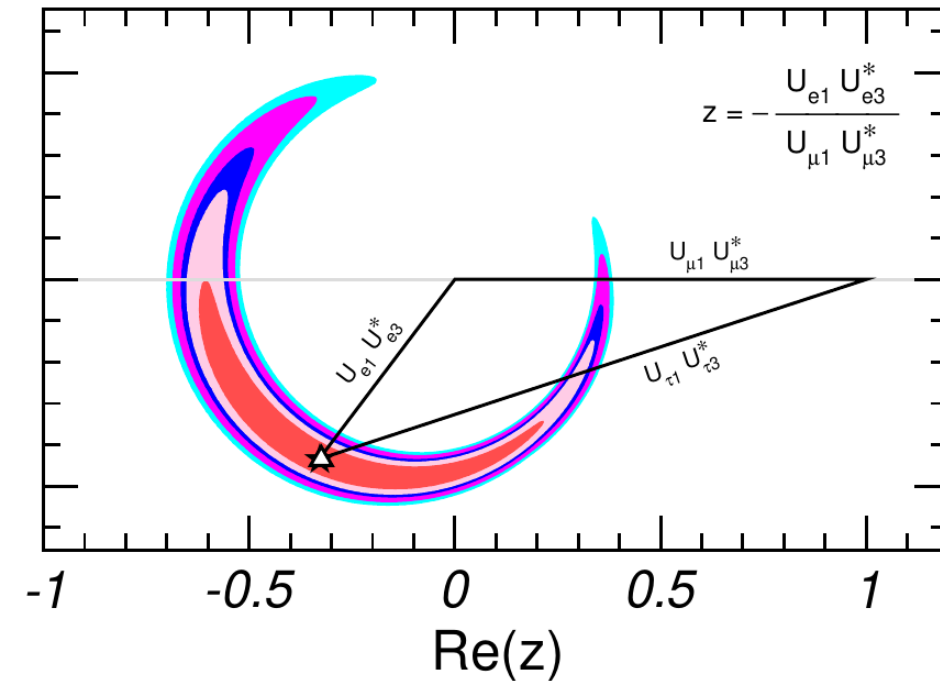
BACKUP

ESTATUS DE LOS NEUTRINOS

Param	Ref. [188] w SK-ATM		Best Fit Ordering	
	bfp $\pm 1\sigma$	3σ range		
$\frac{\sin^2 \theta_{12}}{10^{-1}}$	$3.10^{+0.13}_{-0.12}$	2.75 \rightarrow 3.50	$3.10^{+0.13}_{-0.12}$	2.75 \rightarrow 3.50
$\theta_{12}/^\circ$	$33.82^{+0.78}_{-0.76}$	31.61 \rightarrow 36.27	$33.82^{+0.78}_{-0.75}$	31.62 \rightarrow 36.27
$\frac{\sin^2 \theta_{23}}{10^{-1}}$	$5.63^{+0.18}_{-0.24}$	4.33 \rightarrow 6.09	$5.65^{+0.17}_{-0.22}$	4.36 \rightarrow 6.10
$\theta_{23}/^\circ$	$48.6^{+1.0}_{-1.4}$	41.1 \rightarrow 51.3	$48.8^{+1.0}_{-1.2}$	41.4 \rightarrow 51.3
$\frac{\sin^2 \theta_{13}}{10^{-2}}$	$2.237^{+0.066}_{-0.065}$	2.044 \rightarrow 2.435	$2.259^{+0.065}_{-0.065}$	2.064 \rightarrow 2.457
$\theta_{13}/^\circ$	$8.60^{+0.13}_{-0.13}$	8.22 \rightarrow 8.98	$8.64^{+0.12}_{-0.13}$	8.26 \rightarrow 9.02
$\delta_{CP}/^\circ$	221^{+39}_{-28}	144 \rightarrow 357	282^{+23}_{-25}	205 \rightarrow 348
$\frac{\Delta m_{21}^2}{10^{-5} \text{ eV}^2}$	$7.39^{+0.21}_{-0.20}$	6.79 \rightarrow 8.01	$7.39^{+0.21}_{-0.20}$	6.79 \rightarrow 8.01
$\frac{\Delta m_{32}^2}{10^{-3} \text{ eV}^2}$	$2.454^{+0.029}_{-0.031}$	2.362 \rightarrow 2.544	$-2.510^{+0.030}_{-0.031}$	$-2.601 \rightarrow -2.419$

NO

IO



I. Esteban *et al.*, JHEP **01**, 106 (2019), [arXiv:1811.05487].

I. Esteban *et al.*, "Nufit4.1 at nufit webpage," <http://www.nu-fit.org>.



RELACIÓN CON LOS PARÁMETROS DE MEZCLA

$$\sin^2 \theta_{12} = \frac{|U_{e2}|^2}{1 - |U_{e3}|^2}, \quad \sin^2 \theta_{23} = \frac{|U_{\mu 3}|^2}{1 - |U_{e3}|^2}, \quad \sin^2 \theta_{13} = |U_{e3}|^2$$

Invariantes de CP:

$$\begin{aligned} J_{CP} &= \text{Im} \left[U_{e1} U_{\mu 2} U_{e2}^* U_{\mu 1}^* \right] \\ &= (1 - s^2 \theta_{13}) \sqrt{s^2 \theta_{13} s^2 \theta_{12} s^2 \theta_{23} (1 - s^2 \theta_{12}) (1 - s^2 \theta_{23})} \sin \delta_{CP} \end{aligned}$$

$$I_1 = \text{Im} \left[U_{e2}^2 U_{e1}^{*2} \right] = -\cos^2 \theta_{12} \cos^4 \theta_{13} \sin^2 \theta_{12} \sin \beta_1 ,$$

$$I_2 = \text{Im} \left[U_{e3}^2 U_{e1}^{*2} \right] = -\cos^2 \theta_{12} \cos^2 \theta_{13} \sin^2 \theta_{13} \sin(\beta_2 + 2\delta_{CP})$$



Desviaciones en la matriz de masa

$$M_\nu = M_{\mu-\tau} + \delta M(\delta, \epsilon)$$

$$\hat{\delta} \equiv \frac{\delta}{m_{e\mu}} = \frac{\sum_i (U_{ei}U_{\tau i} - U_{ei}U_{\mu i})m_i}{\sum_i U_{ei}U_{\mu i}m_i},$$

$$\hat{\epsilon} \equiv \frac{\epsilon}{m_{\mu\mu}} = \frac{\sum_i (U_{\tau i}U_{\tau i} - U_{\mu i}U_{\mu i})m_i}{\sum_i U_{\mu i}U_{\mu i}m_i}.$$

Los parámetros de rompimiento dependen del ordenamiento de masas.

$$|m_2| = \sqrt{m_0^2 + \Delta m_{21}^2}, \quad |m_3| = \sqrt{m_0^2 + |\Delta m_{31}^2|} \quad \text{for NH,}$$

$$|m_1| = \sqrt{m_0^2 + |\Delta m_{31}^2|}, \quad |m_2| = \sqrt{m_0^2 + |\Delta m_{31}^2| + \Delta m_{21}^2} \quad \text{for IH}$$

Solar

$$\Delta m_{21}^2 = m_2^2 - m_1^2$$

Atmosférica

$$\Delta m_{31}^2 = m_3^2 - m_1^2$$



V_{us}

Decay Mode	$ V_{us} f_+(0)$
$K^\pm e3$	0.21714 ± 0.00091
$K^\pm \mu3$	0.21703 ± 0.00114
$K_L e3$	0.21617 ± 0.00047
$K_L \mu3$	0.21664 ± 0.00058
$K_S e3$	0.21530 ± 0.00122
$K_S \mu3$	0.21265 ± 0.00467
Average (including correlation effects [44])	0.21635 ± 0.00038

$$|V_{us}| = 0.2244(5)$$

$$|V_{ub}| = (4.13 \pm 0.12 \pm_{-0.14}^{+0.13} \pm 0.18) \times 10^{-3} \quad (\text{inclusive}),$$

$$|V_{ub}| = (3.70 \pm 0.10 \pm 0.12) \times 10^{-3} \quad (\text{exclusive}),$$

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 0.9985(6)(4)$$

$$|V_{cb}| = (42.2 \pm 0.8) \times 10^{-3} \quad (\text{inclusive})$$

$$|V_{cb}| = (39.4 \pm 0.8) \times 10^{-3} \quad (\text{exclusive}).$$



$P \rightarrow V$ and $P^* \rightarrow P_1$ Form Factors

$$F_i(q^2) = \frac{F_i(0)}{1 - q^2/m_i^2(J^P)}.$$

Transition	$A'_0(0)$	$A'_1(0)$	$A'_2(0)$	$V'(0)$	$m(0^-)$	$m(1^-)$	$m(1^+)$
$D^* \rightarrow K$ [139]	0.78	1.02	0.40	0.90	1.97	2.11	2.53
$D^* \rightarrow \pi$ [139]	0.75	1.08	0.37	0.76	1.87	2.01	2.42
$B^* \rightarrow \pi$ [170]	0.34	0.38	0.29	0.34	5.27	5.32	5.71
$B^* \rightarrow D$ [170]	0.63	0.66	0.56	0.70	6.30	6.34	6.73

Table 5.1. Form factors of the weak transition $P^* \rightarrow P_1$ at $q^2 = 0$ in the Wirbel-Stech-Bauer model [153, 154]. Values of pole masses are given in GeV units.

$B \rightarrow \rho$

Lattice

UKQCD Collaboration, L. Del Debbio, J. M. Flynn, L. Lellouch, and
 . Nieves, Phys. Lett. **B416** (1998) 392–401.

$D \rightarrow K^*$ and $D \rightarrow \rho$

Experiment

BESIII Collaboration, M. Ablikim *et al.*, Phys. Rev. **D94** (2016) 032001.

