

# Description of the Hyperon global polarization in Heavy-Ion Collisions at HADES, NICA and RHIC energies from the Core-Corona Model

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XIX Mexican School of Particles and Fields



# Outline

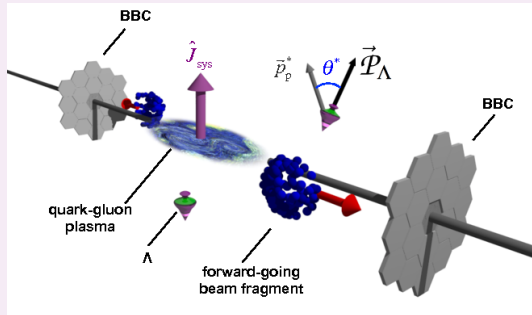


- 1 Motivation
- 2 Core Corona Model
- 3 Excitation Function for the Global  $\Lambda$  and  $\bar{\Lambda}$  Polarization
- 4 Summary

Section 1

# Motivation

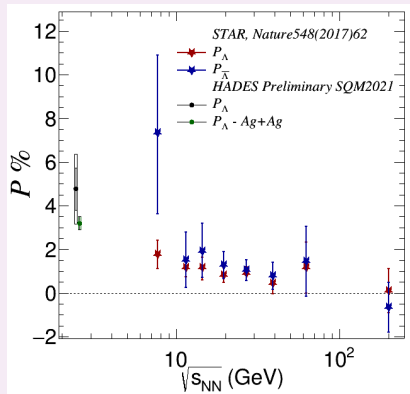
# Motivation: Why we are interested in measure Hyperon Global Polarization?



The fluid at midrapidity has a whirling substructure oriented (on average in the direction of the total angular momentum,  $J$ ). [Nature 548,62-65(2017)]

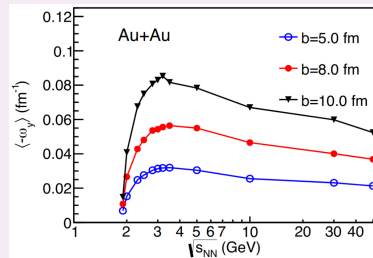
- The  $\Lambda$  and  $\bar{\Lambda}$  polarization are linked to the properties of the medium produced in relativistic heavy-ion collisions
- For semicentral collisions, Angular momentum can be quantified in terms of the thermal vorticity
- The global polarization can be measured using the self-analysing  $\Lambda/\bar{\Lambda}$  decays.

# Global Polarization as a function of energy



Energy range  $\sqrt{s_{NN}} = \{2, 11\}$  GeV can be covered by ongoing/future experiments

STAR BES-II + FXT: 3-19 GeV  
 HADES: 2-3 GeV  
 NICA: 4-11 GeV  $\rightarrow$  MPD



Energy dependence of kinematic vorticity predicted by a transport model (UrQMD) <sup>□</sup>

<sup>□</sup>X.-G. Deng et al., PRC101.064908(2020)

Section 2

## **Core Corona Model**



# Core Corona Model: Two-component source

In heavy-ion collisions,  $\Lambda$  and  $\bar{\Lambda}$  come from different density regions

- **Core:** Via QGP processes like

$$q\bar{q} \rightarrow s\bar{s} \text{ and } gg \rightarrow s\bar{s}$$

- **Corona:** Via  $n + n$  reactions by recombination-like processes

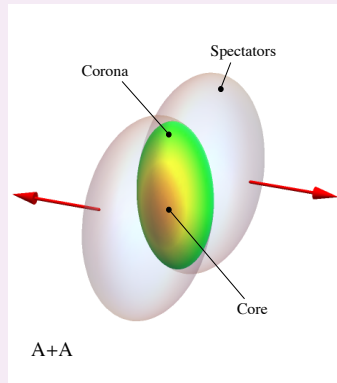
The number of  $\Lambda$ s can be written

$$N_{\Lambda} = N_{\Lambda_{QGP}} + N_{\Lambda_{REC}}$$

The polarization

$$\mathcal{P} = \frac{N^{\uparrow} - N^{\downarrow}}{N^{\uparrow} + N^{\downarrow}}$$

can be rewritten in terms of the number of  $\Lambda$ s (or  $\bar{\Lambda}$ s) produced in the different density regions



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# Rewriting Polarization

$$\mathcal{P}^\Lambda = \frac{(N_{\Lambda QGP}^\uparrow + N_{\Lambda REC}^\uparrow) - (N_{\Lambda QGP}^\downarrow + N_{\Lambda REC}^\downarrow)}{(N_{\Lambda QGP}^\uparrow + N_{\Lambda REC}^\uparrow) + (N_{\Lambda QGP}^\downarrow + N_{\Lambda REC}^\downarrow)}$$

$$\mathcal{P}^{\bar{\Lambda}} = \frac{(N_{\bar{\Lambda} QGP}^\uparrow + N_{\bar{\Lambda} REC}^\uparrow) - (N_{\bar{\Lambda} QGP}^\downarrow + N_{\bar{\Lambda} REC}^\downarrow)}{(N_{\bar{\Lambda} QGP}^\uparrow + N_{\bar{\Lambda} REC}^\uparrow) + (N_{\bar{\Lambda} QGP}^\downarrow + N_{\bar{\Lambda} REC}^\downarrow)}$$

After some algebra, we get:

$$\mathcal{P}^\Lambda = \frac{\left( \mathcal{P}_{REC}^\Lambda + \frac{N_{\Lambda QGP}^\uparrow - N_{\Lambda QGP}^\downarrow}{N_{\Lambda REC}} \right)}{\left( 1 + \frac{N_{\Lambda QGP}}{N_{\Lambda REC}} \right)}$$

$$\mathcal{P}^{\bar{\Lambda}} = \frac{\left( \mathcal{P}_{REC}^{\bar{\Lambda}} + \frac{N_{\bar{\Lambda} QGP}^\uparrow - N_{\bar{\Lambda} QGP}^\downarrow}{N_{\bar{\Lambda} REC}} \right)}{\left( 1 + \frac{N_{\bar{\Lambda} QGP}}{N_{\bar{\Lambda} REC}} \right)}$$

Where the polarization along the angular momentum produced in the corona is:

$$\mathcal{P}_{REC}^\Lambda = \frac{N_{\Lambda REC}^\uparrow - N_{\Lambda REC}^\downarrow}{N_{\Lambda REC}^\uparrow + N_{\Lambda REC}^\downarrow}$$

$$\mathcal{P}_{REC}^{\bar{\Lambda}} = \frac{N_{\bar{\Lambda} REC}^\uparrow - N_{\bar{\Lambda} REC}^\downarrow}{N_{\bar{\Lambda} REC}^\uparrow + N_{\bar{\Lambda} REC}^\downarrow}$$



# Assumptions: Polarization of $\Lambda$ ( $\bar{\Lambda}$ ) from the Corona

$$\mathcal{P}^{\Lambda} = \frac{\left( \mathcal{P}_{REC}^{\Lambda} + \frac{N_{\Lambda QGP}^{\uparrow} - N_{\Lambda QGP}^{\downarrow}}{N_{\Lambda REC}} \right)}{\left( 1 + \frac{N_{\Lambda QGP}}{N_{\Lambda REC}} \right)}$$

$$\mathcal{P}^{\bar{\Lambda}} = \frac{\left( \mathcal{P}_{REC}^{\bar{\Lambda}} + \frac{N_{\bar{\Lambda} QGP}^{\uparrow} - N_{\bar{\Lambda} QGP}^{\downarrow}}{N_{\bar{\Lambda} REC}} \right)}{\left( 1 + \frac{N_{\bar{\Lambda} QGP}}{N_{\bar{\Lambda} REC}} \right)}$$

Where

$$\mathcal{P}_{REC}^{\Lambda} = \frac{N_{\Lambda REC}^{\uparrow} - N_{\Lambda REC}^{\downarrow}}{N_{\Lambda REC}^{\uparrow} + N_{\Lambda REC}^{\downarrow}}$$

$$\mathcal{P}_{REC}^{\bar{\Lambda}} = \frac{N_{\bar{\Lambda} REC}^{\uparrow} - N_{\bar{\Lambda} REC}^{\downarrow}}{N_{\bar{\Lambda} REC}^{\uparrow} + N_{\bar{\Lambda} REC}^{\downarrow}}$$

- Nucleon-Nucleon scattering not enough to align the spin in the direction of the angular momentum
- Polarization of  $\Lambda$  and  $\bar{\Lambda}$  averages to zero.

$$\mathcal{P}_{REC}^{\Lambda} = \mathcal{P}_{REC}^{\bar{\Lambda}} = 0$$

# Assumptions: Intrinsic Polarization

$$\mathcal{P}^{\Lambda} = \frac{\left( \mathcal{P}_{REC}^{\Lambda} + \frac{N_{\Lambda QGP}^{\uparrow} - N_{\Lambda QGP}^{\downarrow}}{N_{\Lambda REC}} \right)}{\left( 1 + \frac{N_{\Lambda QGP}}{N_{\Lambda REC}} \right)}$$

$$\mathcal{P}^{\bar{\Lambda}} = \frac{\left( \mathcal{P}_{REC}^{\bar{\Lambda}} + \frac{N_{\bar{\Lambda} QGP}^{\uparrow} - N_{\bar{\Lambda} QGP}^{\downarrow}}{N_{\bar{\Lambda} REC}} \right)}{\left( 1 + \frac{N_{\bar{\Lambda} QGP}}{N_{\bar{\Lambda} REC}} \right)}$$

We define  $\mathbf{z}$  and  $\bar{\mathbf{z}}$  which represent the  $\Lambda$  and  $\bar{\Lambda}$  intrinsic polarization respectively

$$N_{\Lambda QGP}^{\uparrow} - N_{\Lambda QGP}^{\downarrow} = \mathbf{z} N_{\Lambda QGP}$$

$$N_{\bar{\Lambda} QGP}^{\uparrow} - N_{\bar{\Lambda} QGP}^{\downarrow} = \bar{\mathbf{z}} N_{\bar{\Lambda} QGP}$$

# Assumptions: The ratio $N_{\Lambda_{QGP}}/N_{\Lambda_{REC}}$

$$\mathcal{P}^{\Lambda} = \frac{\left( \mathcal{P}_{REC}^{\Lambda} + \frac{N_{\Lambda_{QGP}}^{\uparrow} - N_{\Lambda_{QGP}}^{\downarrow}}{N_{\Lambda_{REC}}} \right)}{\left( 1 + \frac{N_{\Lambda_{QGP}}}{N_{\Lambda_{REC}}} \right)}$$

$$\mathcal{P}^{\bar{\Lambda}} = \frac{\left( \mathcal{P}_{REC}^{\bar{\Lambda}} + \frac{N_{\bar{\Lambda}_{QGP}}^{\uparrow} - N_{\bar{\Lambda}_{QGP}}^{\downarrow}}{N_{\bar{\Lambda}_{REC}}} \right)}{\left( 1 + \frac{N_{\bar{\Lambda}_{QGP}}}{N_{\bar{\Lambda}_{REC}}} \right)}$$

The number of  $\bar{\Lambda}$ s are proportional to an energy-dependent coefficient  $\mathbf{w}(\mathbf{w}')$  times the number of  $\Lambda$ s in the corona(core)

$$N_{\bar{\Lambda}_{REC}} = \mathbf{w} N_{\Lambda_{REC}}$$

$$N_{\bar{\Lambda}_{QGP}} = \mathbf{w}' N_{\Lambda_{QGP}}$$

# $\Lambda$ and $\bar{\Lambda}$ global polarization

With this assumptions

$$\mathcal{P}_{REC}^{\Lambda} = \mathcal{P}_{REC}^{\bar{\Lambda}} = 0$$

$$N_{\Lambda QGP}^{\uparrow} - N_{\Lambda QGP}^{\downarrow} = z N_{\Lambda QGP}$$

$$N_{\bar{\Lambda} QGP}^{\uparrow} - N_{\bar{\Lambda} QGP}^{\downarrow} = \bar{z} N_{\bar{\Lambda} QGP}$$

$$N_{\bar{\Lambda} REC} = w N_{\Lambda REC}$$

$$N_{\bar{\Lambda} QGP} = w' N_{\Lambda QGP}$$

Global polarization depends on the coefficients  $w, w', z, \bar{z}$  and the ratio  $\frac{N_{\Lambda QGP}}{N_{\Lambda REC}}$  that can be estimated from data or calculated

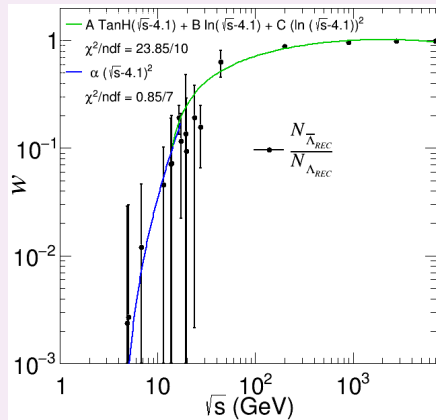
$$\mathcal{P}^{\Lambda} = \frac{z \frac{N_{\Lambda QGP}}{N_{\Lambda REC}}}{1 + \frac{N_{\Lambda QGP}}{N_{\Lambda REC}}}$$

$$\mathcal{P}^{\bar{\Lambda}} = \frac{\bar{z} \left(\frac{w'}{w}\right) \frac{N_{\Lambda QGP}}{N_{\Lambda REC}}}{1 + \left(\frac{w'}{w}\right) \frac{N_{\Lambda QGP}}{N_{\Lambda REC}}}$$

# The ratio $w = N_{\bar{\Lambda}_{REC}} / N_{\Lambda_{REC}}$

Model as  $p + p$  collisions

- Experimental data obtained from  $p + p$  collisions at different energies<sup>1</sup>
- $w$  is defined only for  $\sqrt{s} > 4.1\text{GeV}$ . The threshold energy for  $p + p \rightarrow p + p + \Lambda + \bar{\Lambda}$
- $w$  is smaller than 1 except for energies  $\sqrt{s} > 1\text{ TeV}$



<sup>1</sup>

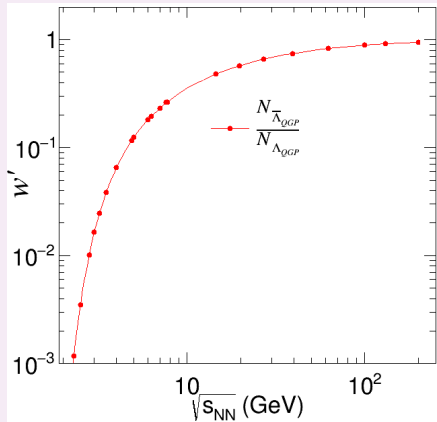
M. Gazdzicki and D. Rohrich, Z. Phys. C 71 (1996) 55; V. Blobel et al. Nucl. Phys. B 69(1974), 454–492; J. W. Chapman et al., Phys. Lett. 47B (1973) 465; D. Brick et al., Nucl. Phys. B 164 (1980) 1; C. Höhne, CERN-THESIS-2003-034; J. Baechler et al. [NA35 Collaboration], Nucl. Phys. A 525 (1991) 221C; G. Chariton et al., Phys. Rev. Lett. 30 (1973) 574; F. Lopinto et al., Phys. Rev. D 22 (1980) 573; H. Kichimi et al., Phys. Rev. D 20 (1979) 37; F. W. Busser et al., Phys. Lett. 61B (1976) 309; S. Erhan, et al., Phys. Lett. 85B(1979) 447; B. I. Abelev et al. [STAR Collaboration], Phys. Rev. C 75 (2007) 064901; E. Abbas et al. [ALICE Collaboration], Eur. Phys. J. C 73 (2013) 2496

# The ratio $w' = N_{\bar{\Lambda}_{QGP}}/N_{\Lambda_{QGP}}$

- The coefficient  $w'$  is computed as the ratio of the equilibrium distributions of  $\bar{s}$  to  $s$ -quark for a given temperature and chemical potential  $\mu = \mu_B/3$

$$w' = \frac{e^{(m_s - \mu)/T} + 1}{e^{(m_s + \mu)/T} + 1}$$

$m_s$  the mass of the  $s$ -quark and  $\mu_B$  and  $T$  along the maximum chemical potential at freeze out.



# Production of $\Lambda$ in the core and the corona

## Number of $\Lambda$ s in the core

$$N_{\Lambda_{QGP}} = cN_{p_{QGP}}^2$$

in which

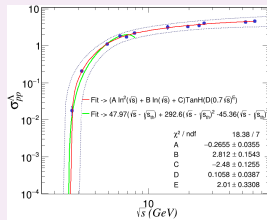
$$N_{p_{QGP}} = \int n_p(\mathbf{s}, \mathbf{b}) \theta[n_p(\mathbf{s}, \mathbf{b}) - n_c] d^2s$$

with  $n_c = 3.3 \text{ fm}^{-2}$ , the critical density required to form the QGP

## Number of $\Lambda$ s in the corona

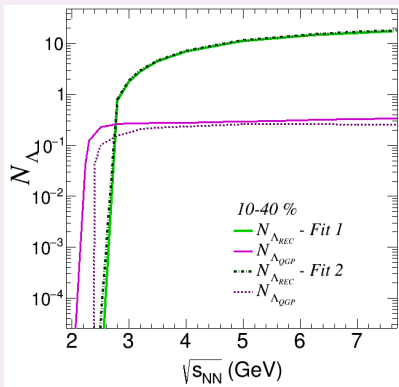
$$N_{\Lambda_{REC}} = \sigma_{NN}^{\Lambda} \int T_B(\mathbf{b}-\mathbf{s}) T_A(\mathbf{s}) \theta[n_c - n_p(\mathbf{s}, \mathbf{b})] d^2s$$

where  $\sigma_{NN}^{\Lambda}$  is obtained from experimental data

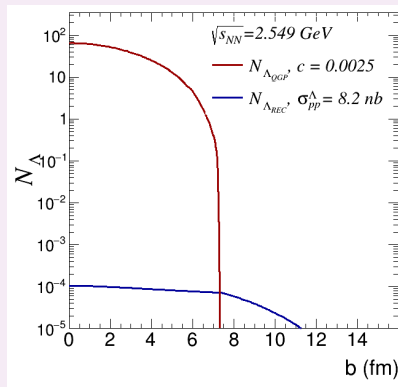


The density of participants  $n_p(\mathbf{s}, \mathbf{b}) = T_A(\mathbf{s})[1 - e^{-\sigma_{NN} T_B(\mathbf{s}-\mathbf{b})}] + T_B(\mathbf{s}-\mathbf{b})[1 - e^{-\sigma_{NN} T_A(\mathbf{s})}]$ ,  
 the thickness function  $T_A(z, \mathbf{s}) = \int_{-\infty}^{\infty} \rho_A(z, \mathbf{s}) dz$  and  
 the Woods-Saxon profile density  $\rho_A(\mathbf{s}) = \frac{\rho_0}{1 + e^{(r-R_A)/a}}$

# $\Lambda$ s in the Core and Corona



At low energies  $N_{\Lambda_{QGP}}$  depends on  $\sigma_{NN}$ , different parametrizations impact on the strenght of polarization



$\sigma_{NN}$  affects the ratio  $N_{\Lambda_{QGP}}/N_{\Lambda_{REC}}$  and the value of  $b$  at which the ratio is smaller than 1



# Intrinsic Polarization

The intrinsic polarizations are given by:

$$z = 1 - e^{-\Delta\tau_{QGP}/\tau}$$

and

$$\bar{z} = 1 - e^{-\Delta\tau_{QGP}/\bar{\tau}}$$

in terms of the relaxation times  $\tau$  and  $\bar{\tau}$  and the QGP life-time  $\Delta\tau_{QGP}$

The relaxation time can be computed as the inverse of the interaction rate

$$\tau \equiv 1/\Gamma$$

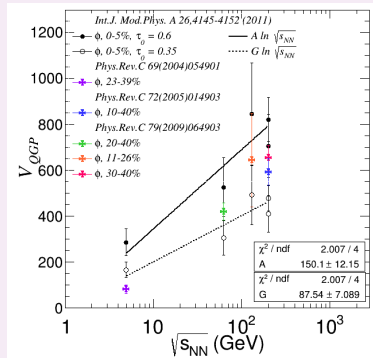
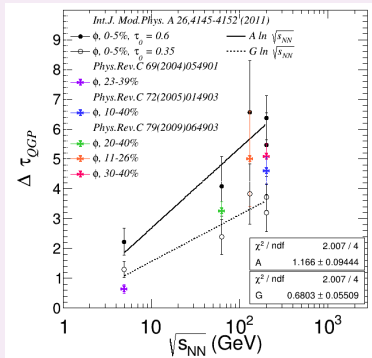
given by

$$\Gamma = V \int \frac{d^3p}{2\pi^3} \Gamma(p_0), \text{ with } V = \pi R^2 \Delta\tau_{QGP}$$

where  $V$  is the volume of the core region, related with the QGP life-time  $\Delta\tau_{QGP}$  in the scenario of a Bjorken expansion

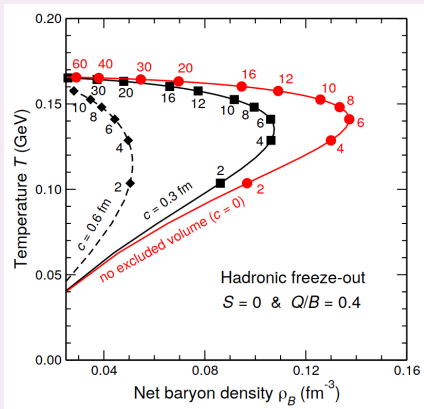
$$\Delta\tau_{QGP} = \tau_f - \tau_0 = \tau_0 \left[ \left( \frac{T_0}{T_f} \right)^3 - 1 \right]$$

# Volume and QGP life-time



$T_0$  is estimated from  $p_T$  of  $\phi$  mesons,  $\tau_0 = 0.35 - 0.60$  fm to incorporate the effect of collision centrality, and  $T_f$  is taken as the value along the maximum chemical potential curve at freeze-out

# $\mu_B$ and T at freeze out



Eur.Phys.J. 52 (2016) 218–219

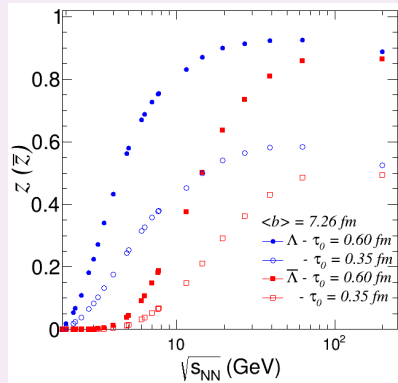
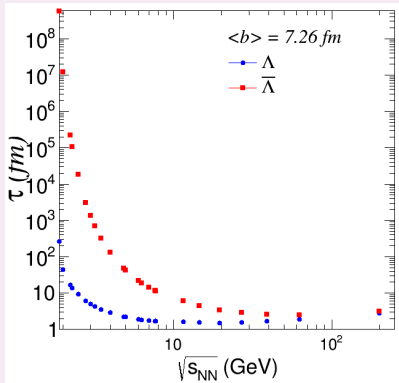
Maximum freeze-out baryon density in nuclear collisions

$$T(\mu_B) = 166 - 139\mu_B^2 - 53\mu_B^4$$

$$\mu_B(\sqrt{s_{NN}}) = \frac{1308}{1000 + 0.273\sqrt{s_{NN}}}$$

Phys.Rev.C 74 (2006) 047901

# Relaxation time and intrinsic polarization as a function of energy



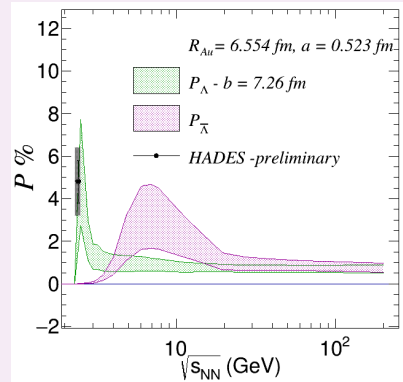
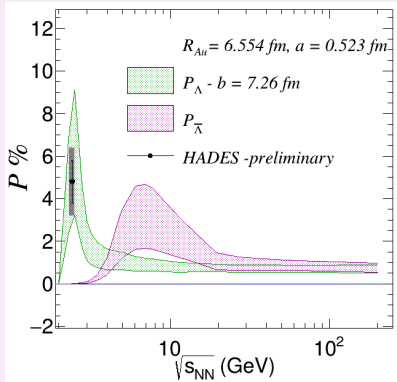
For energies below the  $\Lambda$  production threshold energy, the  $\tau$  and  $\bar{\tau}$  increase dramatically, as expected, since the interaction rate should vanish below these energies.

Section 3

# **Excitation Function for the Global $\Lambda$ and $\bar{\Lambda}$ Polarization**

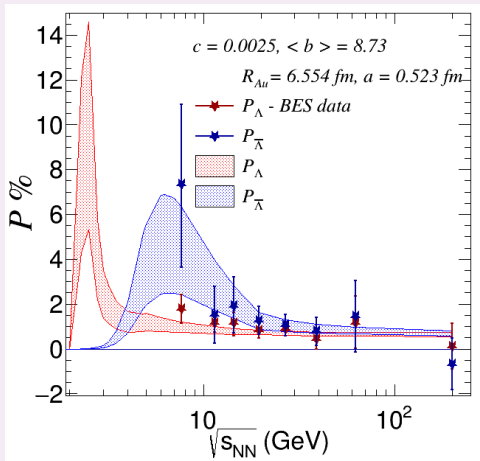
# $\Lambda$ and $\bar{\Lambda}$ polarization in Au+Au at HADES centrality

10 - 40 %



# $\Lambda$ and $\bar{\Lambda}$ polarization in Au+Au at BES centrality

20 - 50 %



- Similar trend to the case of the analysis with smaller centrality
- Magnitude of global polarization increases for larger centrality as a consequence of the angular velocity increase

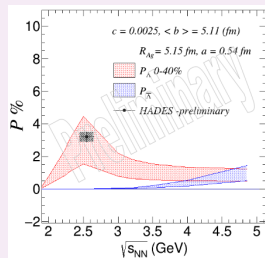
Section 4

## **Summary**



- The two component source model describes the main characteristic features of the  $\Lambda$  and  $\bar{\Lambda}$  polarization excitation functions in semi central relativistic heavy-ion collisions
- The change of the relative abundance of  $\Lambda$ s coming from the core versus those coming from the corona as a function of the collision energy has as a consequence that both polarization peak at collision energies  $\sqrt{s_{NN}} \lesssim 10$  GeV
- The relaxation time can be obtained from a field theoretical approach that links the alignment of the strange quark spin with the thermal vorticity, modeling the QGP volume and life-time using a simple scenario
- The model predicts a maximum for the  $\Lambda$  and  $\bar{\Lambda}$  polarizations which should be possible to be measured in the NICA and HADES energy range.

- Extend the analysis for Ag+Ag collisions to compare with HADES preliminary SQM2021
- Trend looks similar for 0 – 40% of centrality



Thank  
YOU