



Dirac neutrino masses and  
axion + WIMP dark matter  
from Peccei Quinn symmetry

XXXIV RADPyC - SMF  
2020

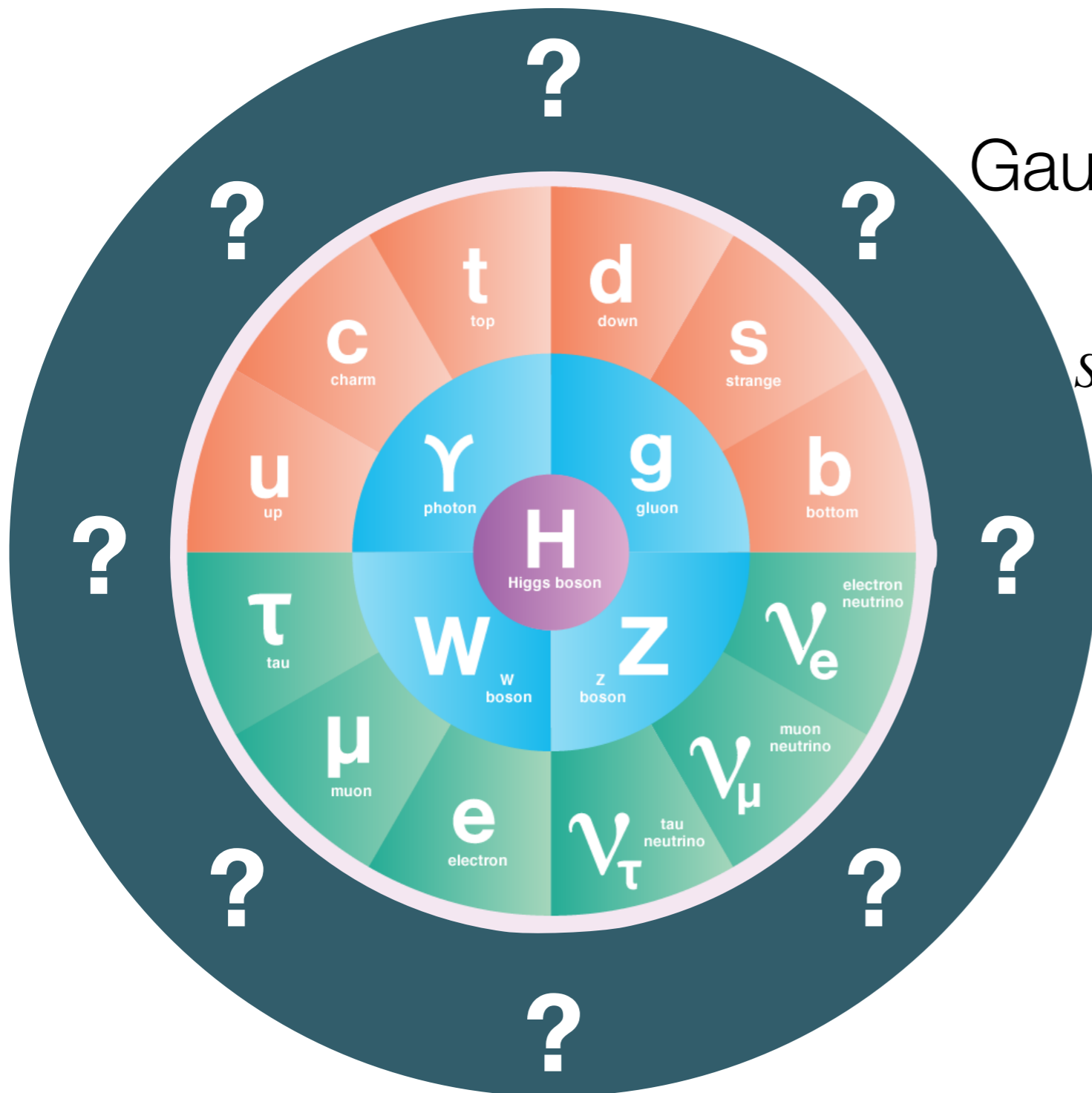
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## Outline

- Motivation (Neutrino masses, DM, strong CP problem)
- PQ solution to CP problem
- Models for neutrino masses
- PQ models for neutrino masses and WIMP DM

# Standard Model



Gauge group + Pattern of SSB

$$SU(3)_c \times SU(2)_L \times U(1)_Y \rightarrow SU(3)_c \times U(1)_Q$$

Yukawa couplings for fermion masses

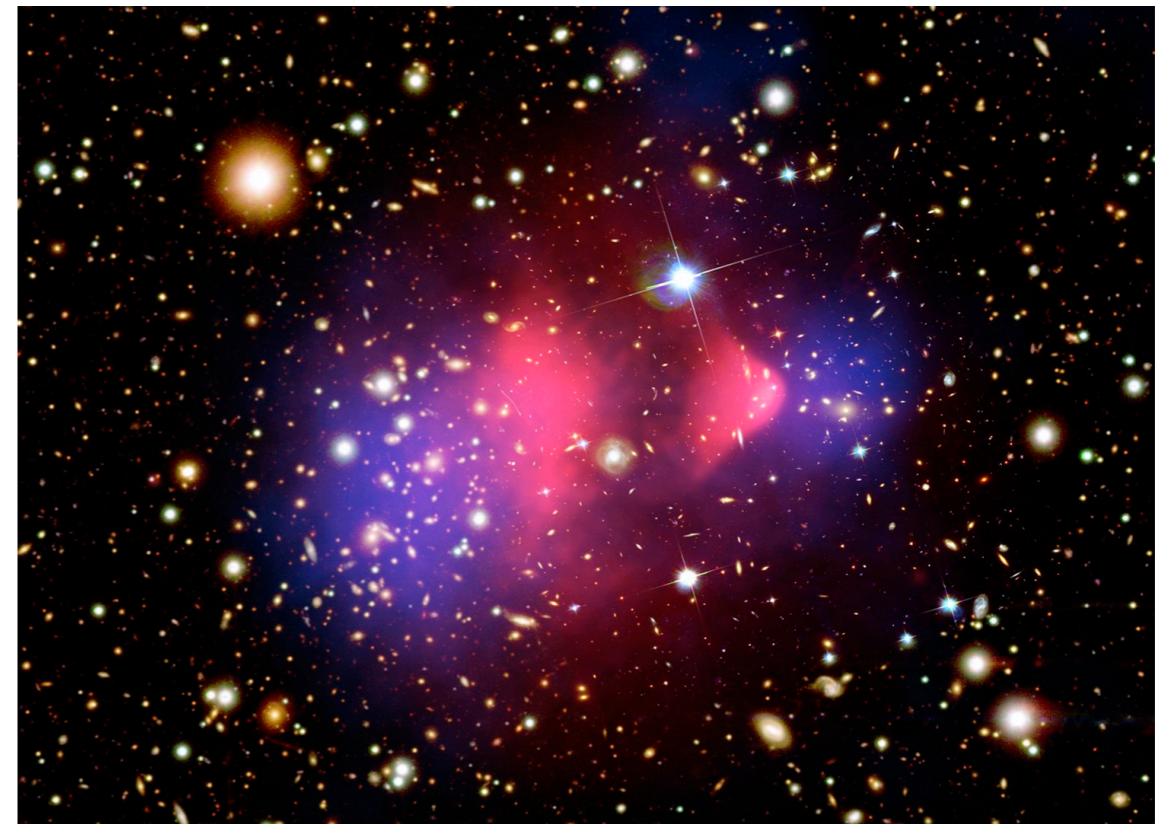
## Standard Model

### Dark Matter

Neutral non-baryonic  
component of matter

~25% of matter-energy of the  
Universe today

- WIMPs ?
- Axion & ALPs ?
- MACHOs ?
- ...



## Standard Model

### Strong CP problem

No observed effect of CP violating  $\theta$  term of QCD

$$\mathcal{L} \supset \frac{\alpha_s}{8\pi} G\tilde{G}\theta_{SM}$$

leads to

$$d_n \sim 3 \times 10^{-16} \theta_{SM} \text{ e cm}$$

PQ symmetry?

$$\theta_{SM} \leq 10^{-10}$$

## Standard Model

### Neutrino masses?

KATRIN:  $m_\nu \leq 1.1 \text{ eV}$

Cosmology:  $\sum m_\nu \leq 0.12 \text{ eV}$

Why is  $\frac{m_\nu}{EWBS} \leq 10^{-11}$  ?

### Dirac or Majorana?

KamLAND-Zen  $\langle m_{\beta\beta} \rangle \leq 0.061 - 0.165 \text{ eV}$

Is lepton number conserved?

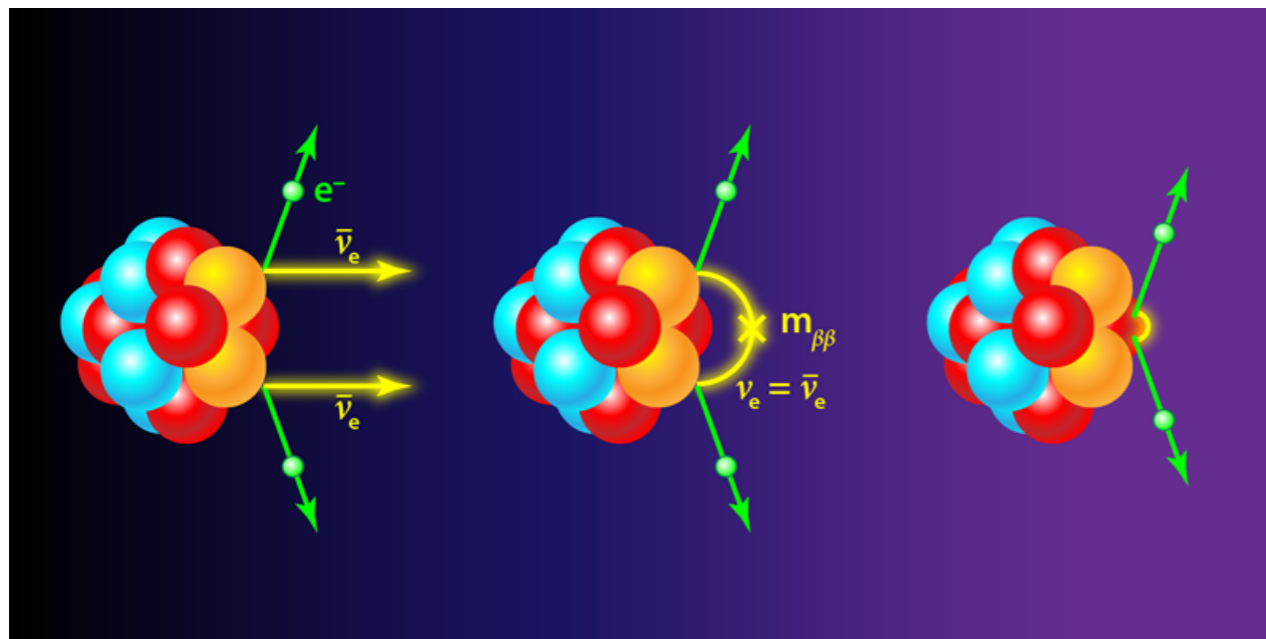
## Majorana v. Dirac masses

Lepton Number Violating terms:

$$m\nu^c\nu$$

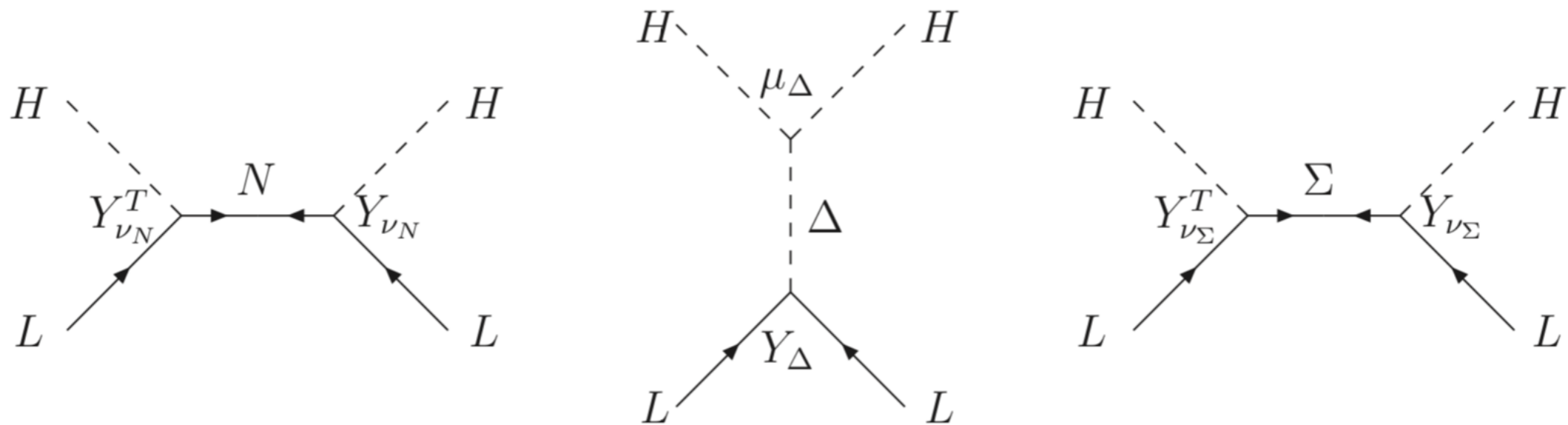
lead to processes

$$\Delta L = 2$$



## Majorana v. Dirac masses

SM symmetries allow Weinberg d=5 op:  $L^c \tilde{H} \tilde{H} L$

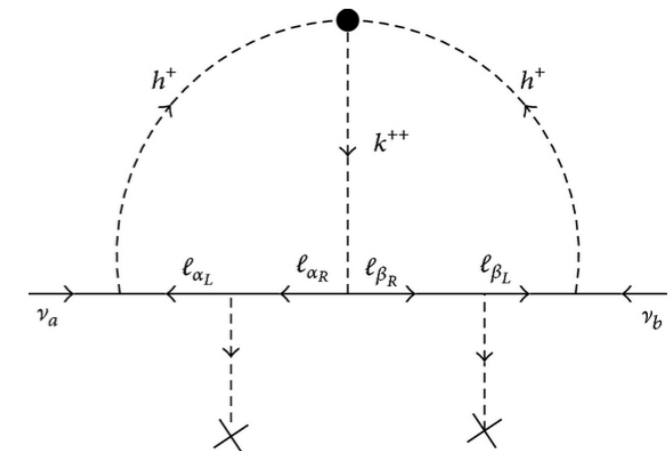
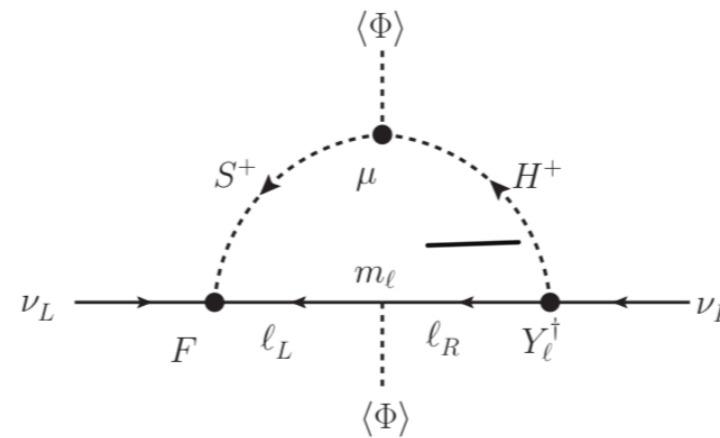
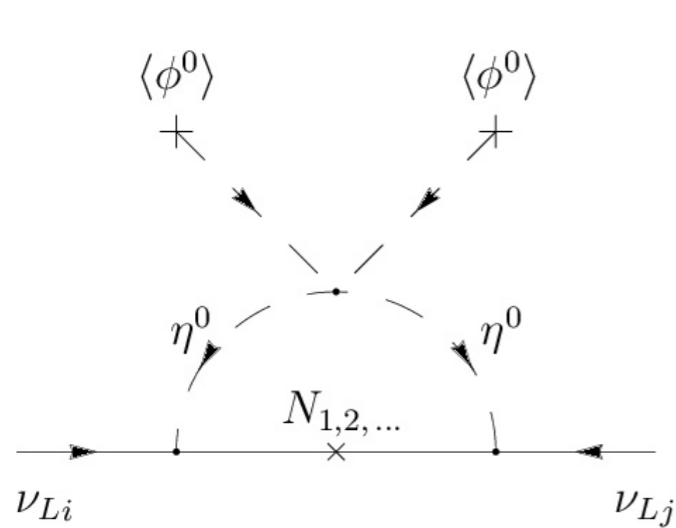


3 ways to generate op. at tree level

$$m_\nu \sim \frac{v_{EW}^2}{\Lambda}$$

## Majorana v. Dirac masses

At loop level many completions are possible



Scotogenic

Zee

Zee-Babu



Additional symmetries forbid tree level masses



DM

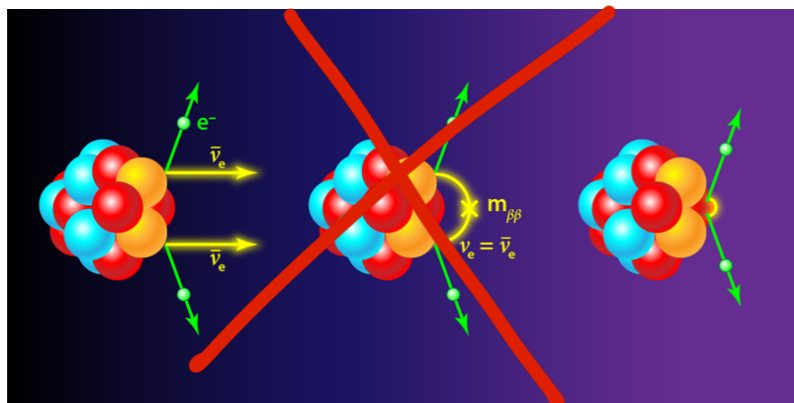
## Majorana v. Dirac masses

~~$$L^c \tilde{H} \hat{H} L$$~~

Forbidden by symmetry

$$L H \nu_R \checkmark$$

Lepton Number Conservation



Abelian or non-Abelian symmetries

(e.g. Aranda, Bonilla, Morisi, Peinado, Valle (2014) )

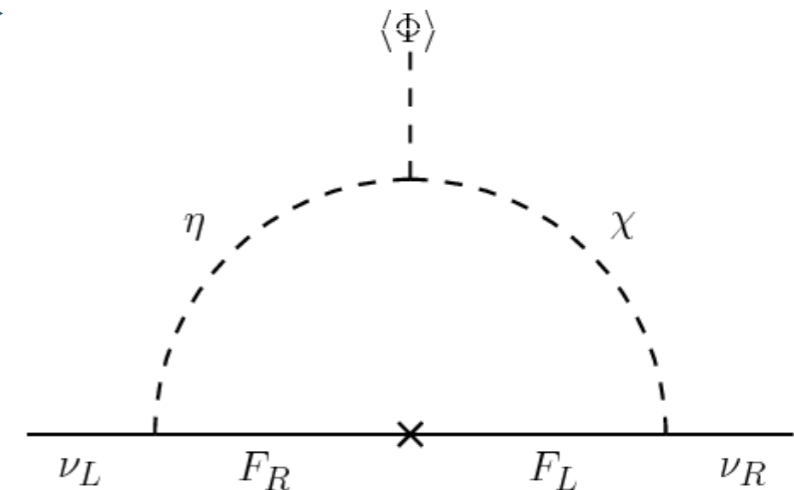
## Majorana v. Dirac masses

Smallness explained by  
loop suppression,  
higher order operators

$$\frac{\mathcal{C}}{\Lambda^n} LH\nu_R(\phi \dots)$$



$$LH\nu_R$$



Dirac d=4 Scotogenic

(or both...)

## Peccei-Quinn symmetry for $\nu$ masses

PQ symmetry -  $U(1)_{PQ}$  - absorbs  $\theta$  and solves strong CP

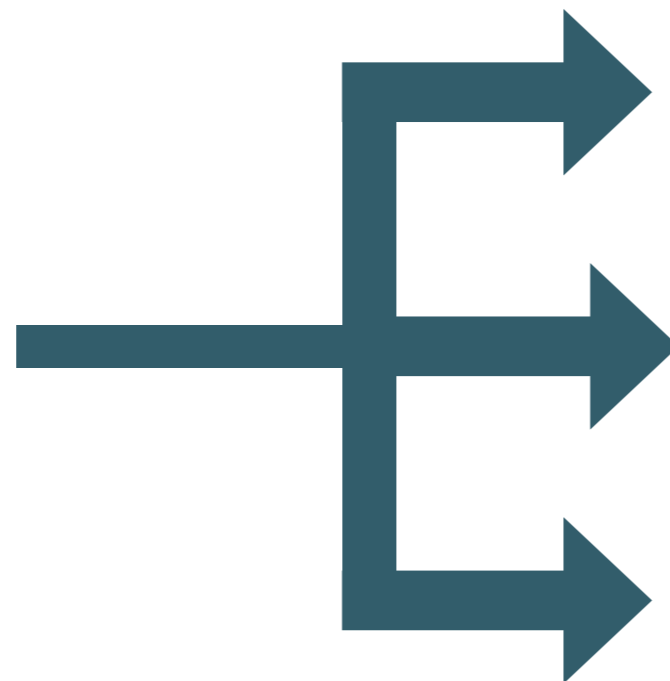


new pNGB is predicted - the axion



new energy scale - PQ breaking scale  $f_a$

$U(1)_{PQ}$



~~PQWW: Axion inside  $SU(2)_L$  doublet~~

$v_{EW} \ll v_{PQ}$

KSVZ: Heavy vector-like quarks

DFSZ: Axion couples to  $H_u, H_d$

## Peccei-Quinn symmetry for $\nu$ masses

DFSZ models:

$H_u$ ,  $H_d$  and a SM singlet  $\sigma$  charged under PQ

$$\mathcal{L} \supset \kappa H_u H_d \sigma \quad \text{or} \quad \mathcal{L} \supset \lambda H_u H_d \sigma^2$$

$H_u$ ,  $H_d$  give masses to fermions:

$$\mathcal{L} \supset Y \bar{Q} H_u u_r + Y \bar{Q} H_d d_r + Y \bar{L} H_d e_r$$



## Peccei-Quinn symmetry for $\nu$ masses

For  $\nu$  masses traditional mechanisms are possible:

**INVISIBLE AXIONS AND LIGHT NEUTRINOS —  
ARE THEY CONNECTED?**

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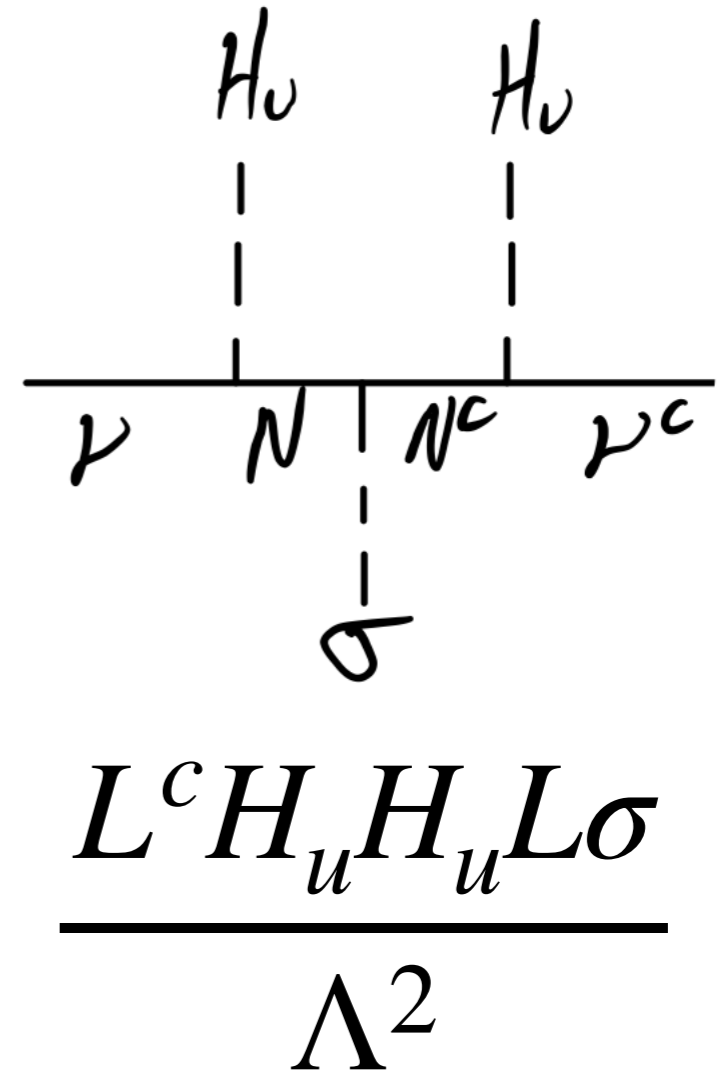
*Deutsches Elektronen-Synchrotron DESY, Hamburg, F. R. Germany*

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Received 14 November 1986



$$\frac{L^c H_u H_u L \sigma}{\Lambda^2}$$

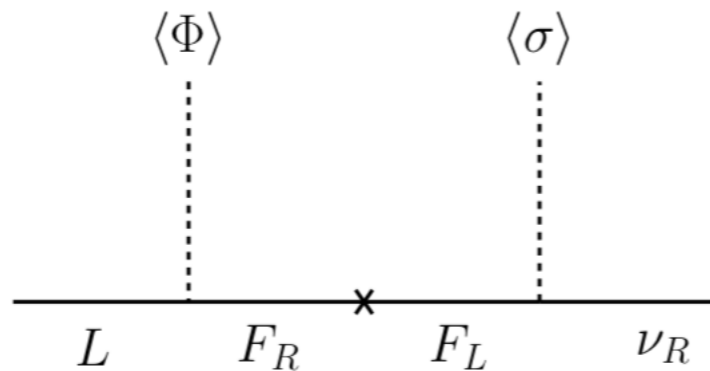
## Peccei-Quinn symmetry for $\nu$ masses

PQ charge assignment may forbid Majorana terms:

Fields/Symmetry	$Q_i$	$u_i^c$	$d_i^c$	$L_i$	$l_i^c$	$H_u$	$H_d$	$\sigma$
$SU(2)_L \times U(1)_Y$	(2,1/6)	(1,-2/3)	(1,1/3)	(2,-1/2)	(1,1)	(2,-1/2)	(2,1/2)	(0,0)
$U(1)_{PQ}$	1	1	1	1	1	2	2	4

$$\mathcal{L}_{dim\ 5} \sim \left\{ \begin{array}{ll} \frac{LL\tilde{H}_u\tilde{H}_u}{\Lambda_{UV}} & 1 + 1 + (-4) = -2 \\ \frac{LL\tilde{H}_u H_d}{\Lambda_{UV}} & 1 + 1 + (0) = +2 \\ \frac{LLH_d H_d}{\Lambda_{UV}} & 1 + 1 + (4) = +6 \end{array} \right. \quad \begin{array}{ll} \sigma^n & (4n); \quad (\sigma^*)^n \quad (-4n); \\ (H_u H_d)^n & (4n); \quad (H_u H_d)^{*n} \quad (-4n); \\ (H_u^\dagger H_u)^n & (0); \quad (H_d^\dagger H_d)^n \quad (0). \end{array}$$

Peinado, Reig, Srivastava, Valle (2019)



Exotic  $\nu_R$  charge :

$$\nu_R \sim -5$$

$$LH_u \nu_R \sigma \quad \checkmark$$

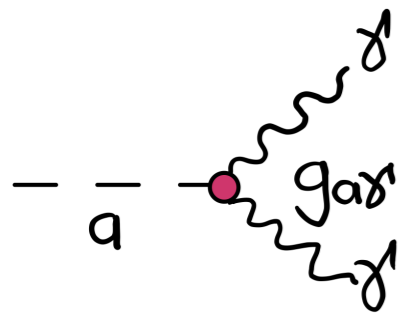
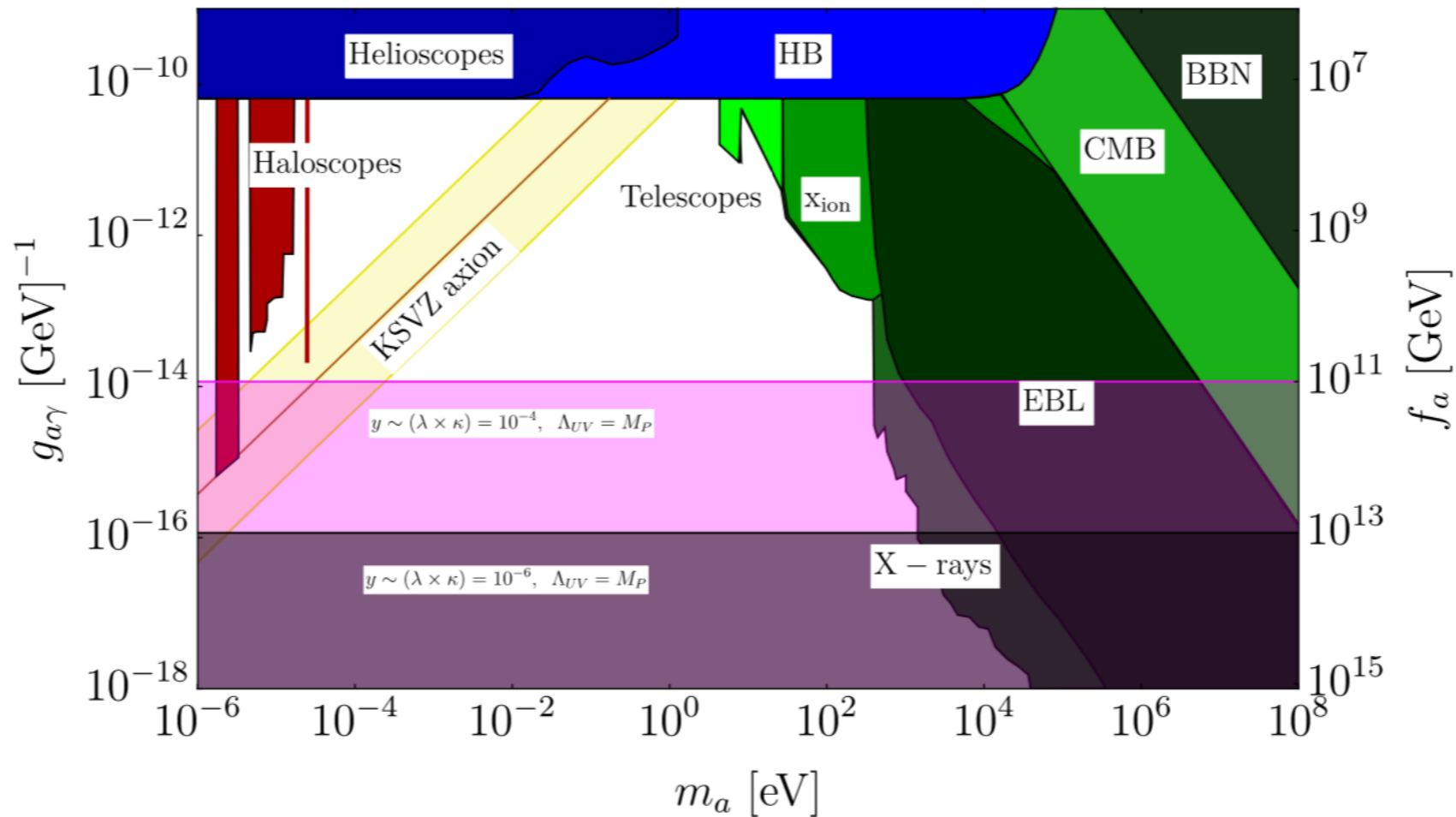
$$m_\nu \sim \frac{v_{EW} f_a}{\Lambda}$$

Peinado, Reig, Srivastava, Valle (2019)

$$m_\nu \sim \frac{v_{EW} f_a}{\Lambda}$$

$$\Lambda \sim M_{Pl}$$

$f_a$  bounded by above by  
neutrino mass bounds  
(KATRIN)



Relaxing the UV scale:

de la Vega, Nath, Peinado(2020)

arXiv: 2001.01846

Case I : Type-II Dirac Seesaw

Nucl. Phys. B 957 (2020)

Symmetry/Fields	$L_i$	$\nu_{Ri}$	$H_u$	$H_d$	$\sigma$	$\Phi_u$
$SU(2)_L \times U(1)_Y$	(2, -1/2)	(1, 1)	(2, -1/2)	(2, 1/2)	(0, 0)	(2, -1/2)
$U(1)_{PQ}$	1	-5	2	2	4	6

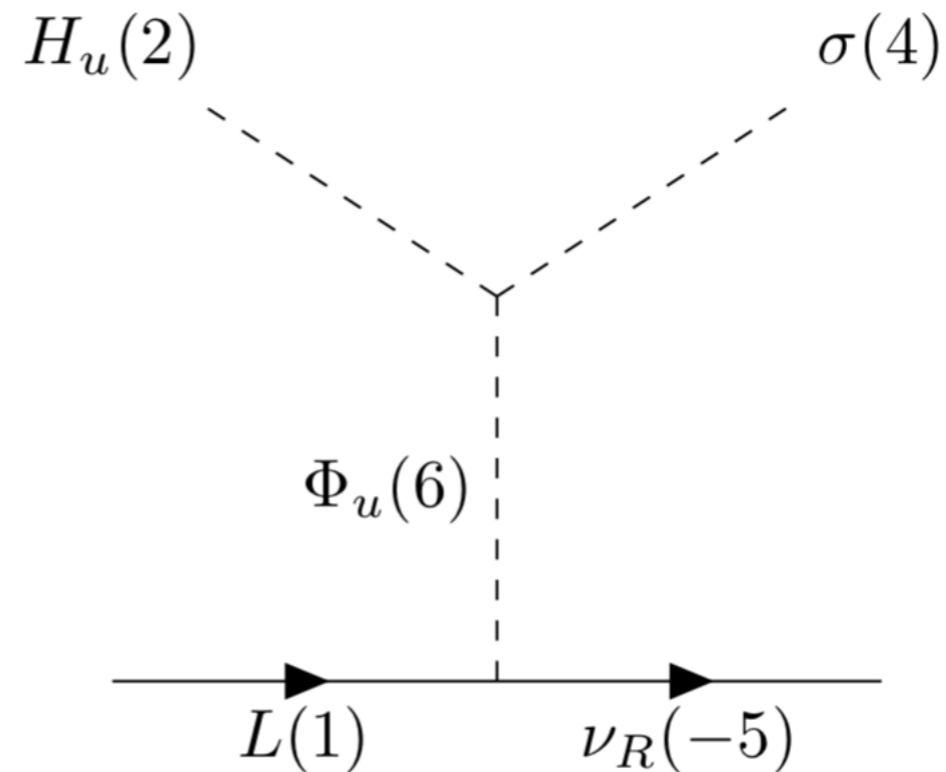
Operator	PQ charge					
$\mathcal{L}_{dim 5} \sim$	$\frac{LL\tilde{H}_u\tilde{H}_u}{\Lambda_{UV}}$	$1 + 1 + (-4) = -2$	$\sigma^n$	$(4n);$	$(\sigma^*)^n$	$(-4n);$
	$\frac{LL\tilde{H}_u H_d}{\Lambda_{UV}}$	$1 + 1 + (0) = +2$	$(H_u H_d)^n$	$(4n);$	$(H_u H_d)^{*n}$	$(-4n);$
	$\frac{LLH_d H_d}{\Lambda_{UV}}$	$1 + 1 + (4) = +6$	$(H_u^\dagger H_u)^n$	$(0);$	$(H_d^\dagger H_d)^n$	$(0);$
	$\frac{LL\tilde{\Phi}_u\tilde{\Phi}_u}{\Lambda_{UV}}$	$1 + 1 + (-12) = -10$	$(H_u^\dagger \Phi_u)^n$	$(4n);$	$(H_u^\dagger \Phi_u)^{*n}$	$(-4n);$
	$\frac{LL\tilde{H}_u\tilde{\Phi}_u}{\Lambda_{UV}}$	$1 + 1 + (-8) = -6$	$(H_d \Phi_u)^n$	$(8n);$	$(H_d \Phi_u)^{*n}$	$(-8n);$
	$\frac{LLH_d\tilde{\Phi}_u}{\Lambda_{UV}}$	$1 + 1 + (-4) = -2.$	$(\Phi_u^\dagger \Phi_u)^n$	$(0);$		

~~$L^c \tilde{H} \tilde{H} L$~~   
 ~~$L^c \tilde{H} \Phi L$~~   
 ~~$L^c \tilde{\Phi} \Phi L$~~

## Case I : Type-II Dirac Seesaw

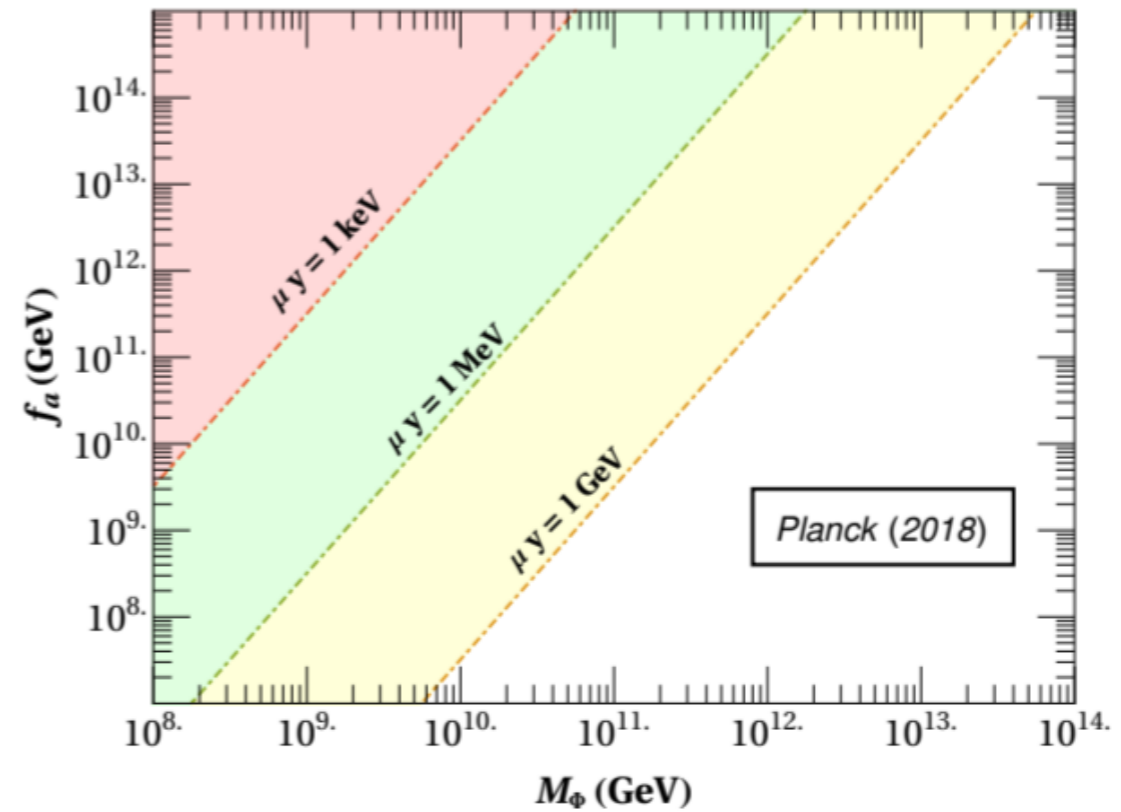
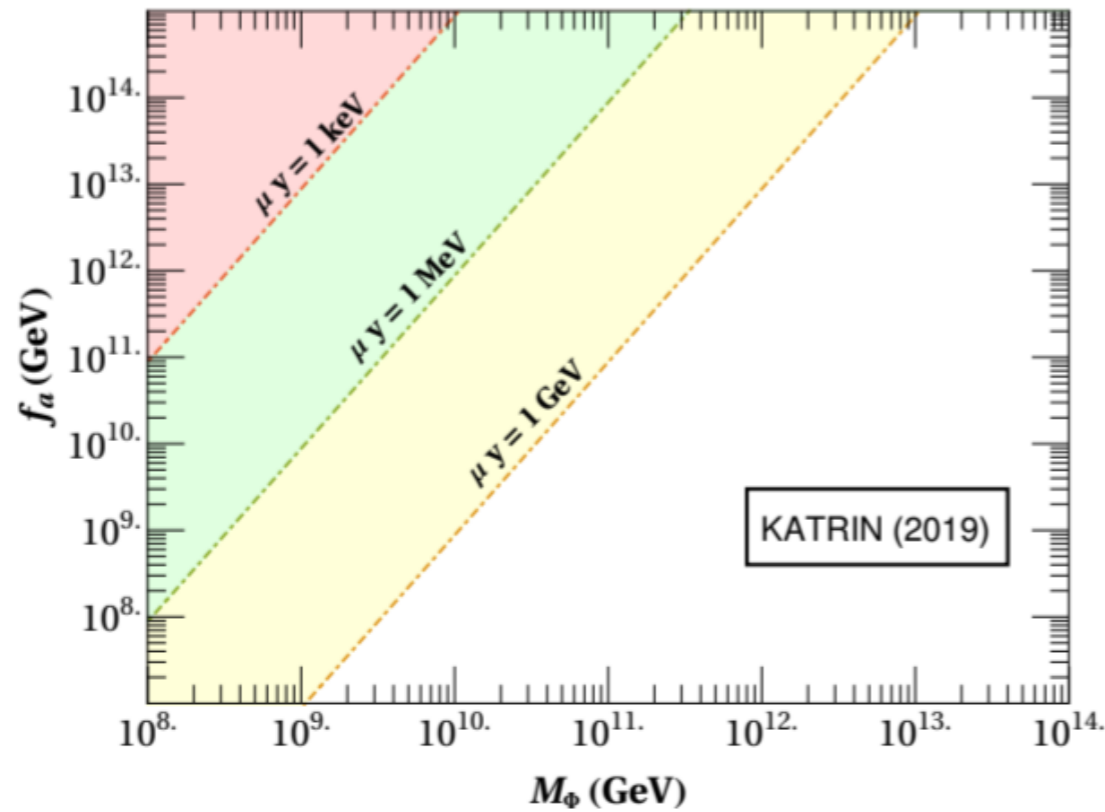
$$LH_u\nu_R\sigma \quad \checkmark$$

$$\mathcal{L}_Y \supset y_{ij}^\nu \bar{\nu}_{Li} \Phi_u \nu_{Rj} + \mu H_u \Phi_u^\dagger \sigma + h.c.$$



$$(m_\nu)_{ij} = y_{ij}^\nu \frac{\mu v_u f_a}{M_{\Phi_u}^2} \sim y_{ij}^\nu v_u \sin \theta$$

# Case I : Type-II Dirac Seesaw



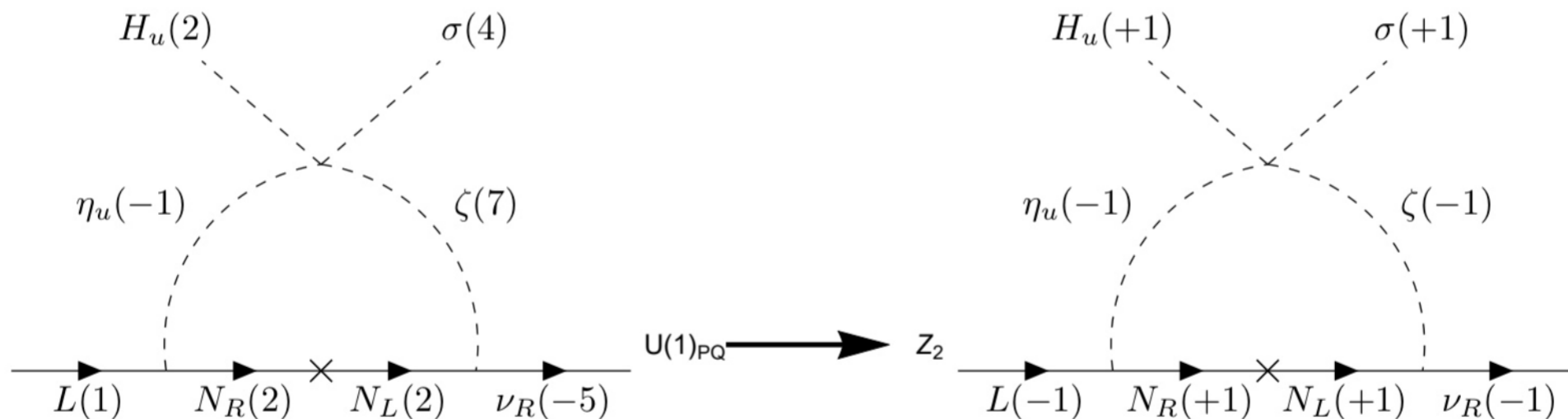
## Case II : Dirac Scotogenic-like loop

Symmetry/Fields	$L_i$	$\nu_{Ri}$	$H_u$	$H_d$	$N_R$	$N_L$	$\sigma$	$\eta_u$	$\zeta$
$SU(2)_L \times U(1)_Y$	(2, -1/2)	(1, 1)	(2, -1/2)	(2, 1/2)	(1, 0)	(1, 0)	(1, 0)	(2, -1/2)	(1, 0)
$U(1)_{PQ}$	1	-5	2	2	2	2	4	-1	7
$Z_2^{PQ}$	-1	-1	+1	+1	+1	+1	+1	-1	-1

$$\mathcal{L}_Y \supset y_{ij}^\nu \bar{L}_i \eta_u N_{Rj} + M_{jk} \bar{N}_{Rj} N_{Lk} + y_{ki}^{\nu'} \bar{N}_{Lk} \nu_{Ri} \zeta + h.c.$$

$$V \supset \lambda_1 H_u \eta_u^\dagger \zeta^* \sigma$$

$$\langle \eta_u \rangle = 0 = \langle \zeta \rangle$$



## Case II : Dirac Scotogenic-like loop

Scalar mixings

2 blocks:

$$(H_u, H_d, \sigma)$$

$$(\eta_u, \zeta)$$

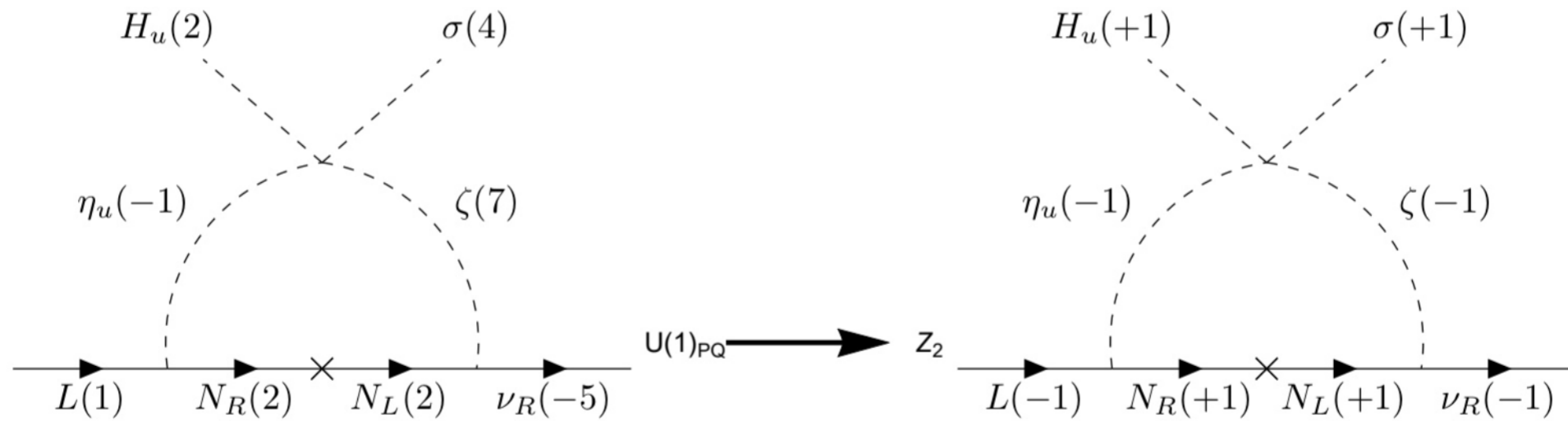
Spectrum:

$$(EW, PQ)$$

$$(1 \text{ TeV}, PQ)$$

$$\sin 2\theta_X \sim \frac{\lambda_1 v_u f_a}{m_{S_{X_2}}^2 - m_{S_{X_1}}^2}$$

## Case II : Dirac Scotogenic-like loop



$$m_{\nu}^{ij} = \frac{1}{64\pi^2} \sum_{X=R,I} \frac{\lambda_1 v_u f_a}{m_{S_{X_2}}^2 - m_{S_{X_1}}^2} \sum_k y^{ik} y'^{kj} m_{N_k} \left[ F\left(\frac{m_{S_{X_2}}^2}{m_{N_i}^2}\right) - F\left(\frac{m_{S_{X_1}}^2}{m_{N_i}^2}\right) \right]$$

$$F(x) = x \log(x) / (x - 1)$$

## Case II : Dirac Scotogenic-like loop

Light N

$$m_{\nu}^{ij} \sim 1\text{eV} \left( \frac{\lambda_1}{10^{-7}} \right) \left( \frac{v_u}{10^2\text{GeV}} \right) \left( \frac{f_a}{10^{12}\text{GeV}} \right) \left( \frac{y}{10^{-7}} \right) \left( \frac{y'}{0.82} \right) \left( \frac{m_{N_k}}{130\text{GeV}} \right) \left( \frac{(280\text{GeV})^2}{m_S^2} \right)$$

Light scalar

$$m_{\nu}^{ij} \sim \frac{\lambda_1 v_u f_a}{32\pi^2} \sum_k \frac{y^{ik} y'^{kj}}{m_{N_K}} \left[ \log \left( \frac{m_{N_k}^2}{m_S^2} \right) - 1 \right]$$

## Case II : Dirac Scotogenic-like loop

WIMP stability:

$Z_2$  + Lorentz

N must decay to an uneven number of fermions

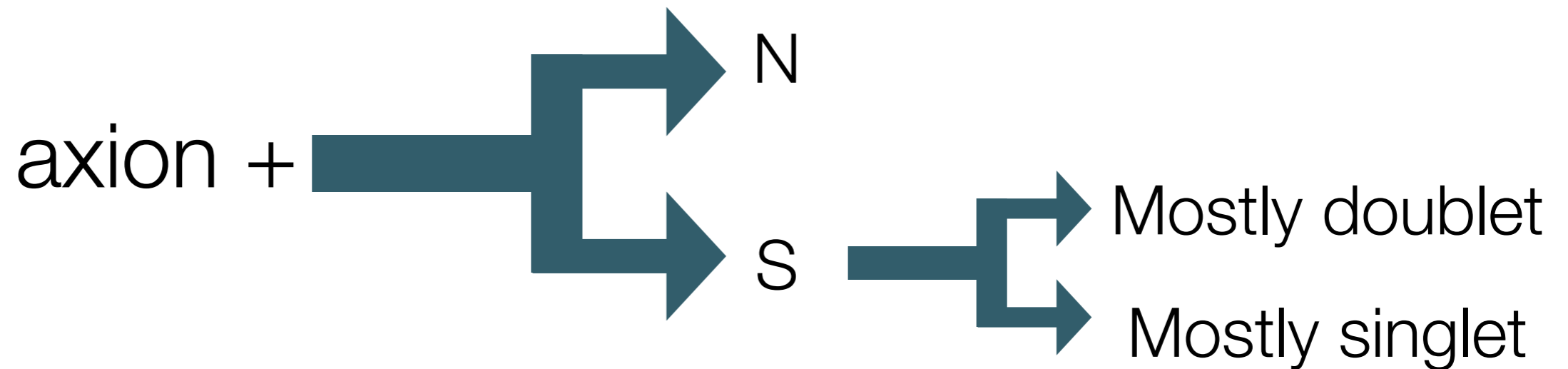
$(-1)^{2n-1} = -1$  , but N has even charge !

S must decay to an even number of fermions

$(-1)^{2n} = 1$  , but S has odd charge !

## Case II : Dirac Scotogenic-like loop

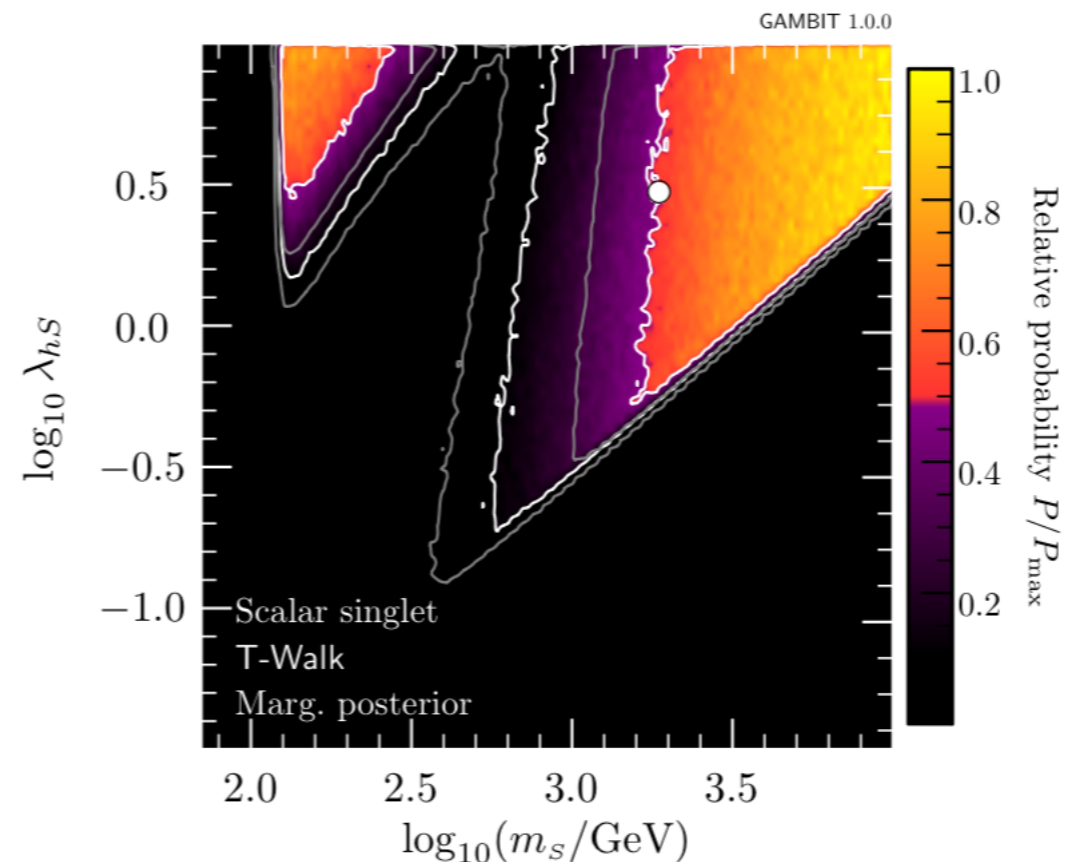
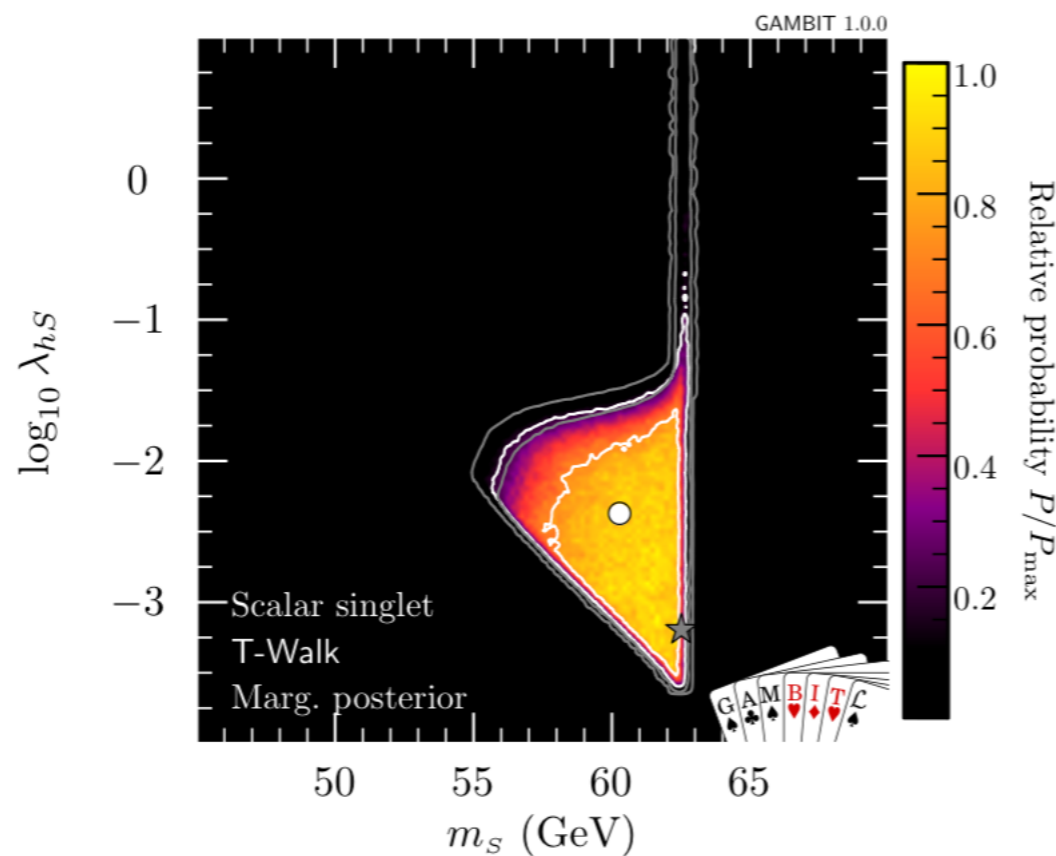
2 DM components: axion + lightest particle inside loop



## Case II : Dirac Scotogenic-like loop

Scalar case:

Mostly singlet: Inert Singlet - like pheno



Case

N

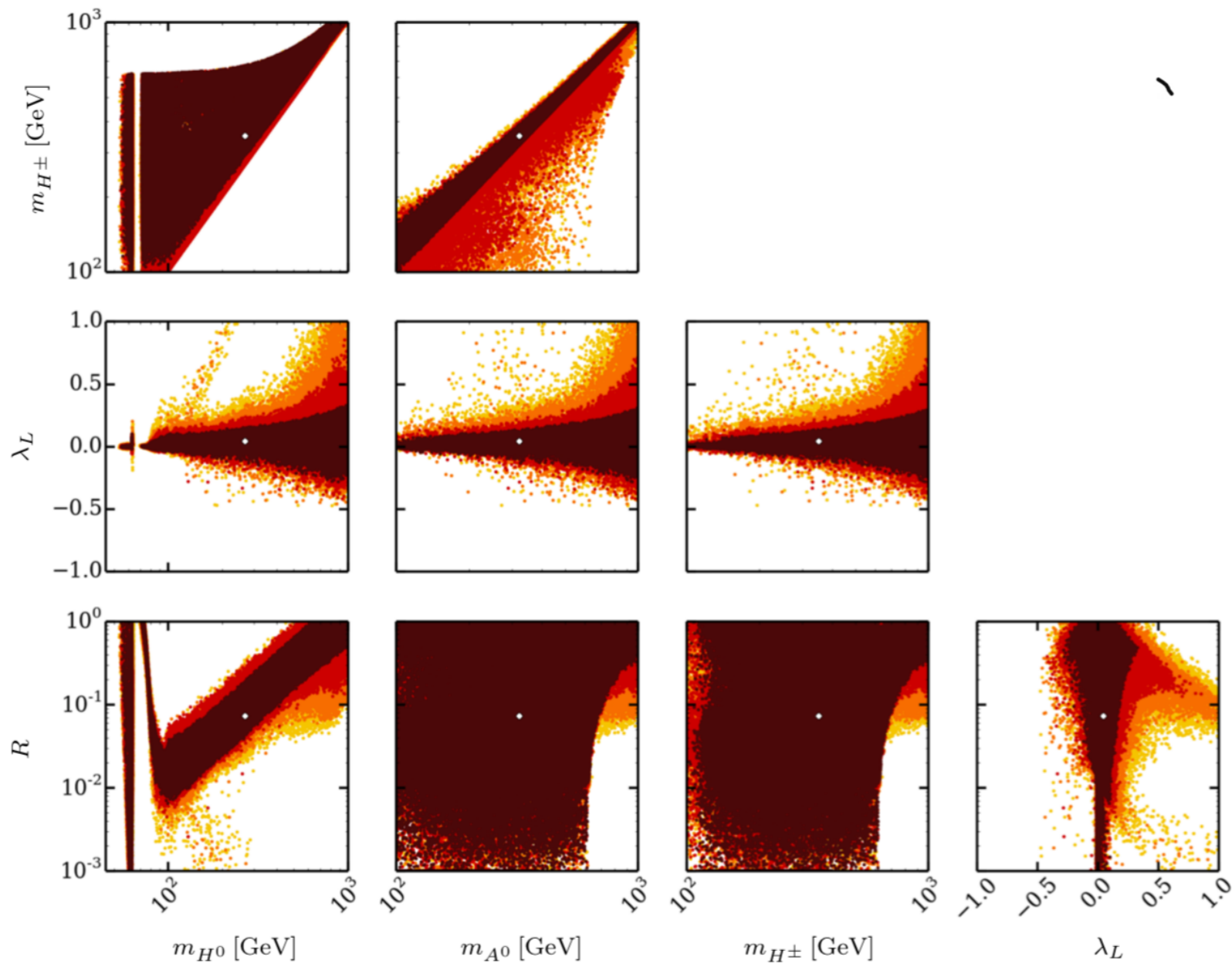


Figure 1: Global fit results for the IDM free parameters  $m_{H^0}$ ,  $m_{A^0}$ ,  $m_{H^\pm}$ ,  $\lambda_L$  and the DM fraction  $R$ . The brown, red, orange and yellow points lie within 1-, 2-, 3- and 4 $\sigma$  away from the best-fit point (denoted by a white dot), respectively. Here we take into account the log-likelihood contributions from all observables described in section 3, except the GCE spectrum and unconfirmed dwarfs.

## Case II : Dirac Scotogenic-like loop

Fermion case:

Relic density and LFV processes dictated by Yukawas



Large yukawas for  
efficient  
annihilation



Small yukawas to  
avoid saturation of  
LFV limits





## Case II : Dirac Scotogenic-like loop

Fermion case:

New coupling:  $N - \nu_R - \zeta$

NN-  $\nu_R \nu_R$  channel: saturation of  $N_{eff}$ ?

## Conclusions:

- PQ symmetry can provide a framework for neutrinos and DM
- PQ symmetry  $\rightarrow$  neutrino diracness?
- PQ symmetry  $\rightarrow$  multicomponent DM?
- Axion pheno  $\leftrightarrow$  Neutrino pheno  $\leftrightarrow$  DM pheno