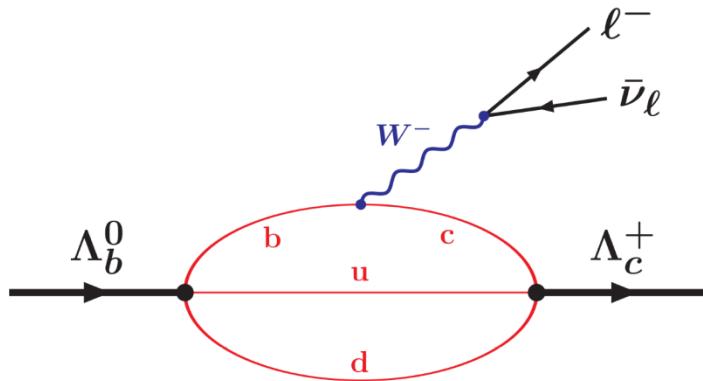


# Branching ratio of $\Lambda_b \rightarrow \Lambda_c^- e^- \bar{\nu}_e$ decay



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# Introduction

Citation: P.A. Zyla *et al.* (Particle Data Group), Prog. Theor. Exp. Phys. 2020, 083C01

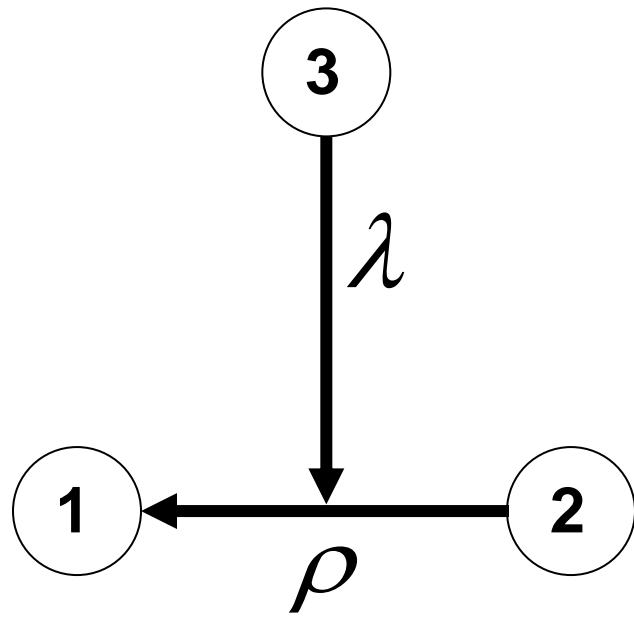
$\Lambda_c(2595)^+ \pi^-$ ,		$(3.4 \pm 1.5) \times 10^{-4}$
$\Lambda_c(2595)^+ \rightarrow \Lambda_c^+ \pi^+ \pi^-$		
$\Lambda_c(2625)^+ \pi^-$ ,		$(3.3 \pm 1.3) \times 10^{-4}$
$\Lambda_c(2625)^+ \rightarrow \Lambda_c^+ \pi^+ \pi^-$		
$\Sigma_c(2455)^0 \pi^+ \pi^-$ , $\Sigma_c^0 \rightarrow \Lambda_c^+ \pi^-$		$(5.7 \pm 2.2) \times 10^{-4}$
$\Sigma_c(2455)^{++} \pi^- \pi^-$ , $\Sigma_c^{++} \rightarrow \Lambda_c^+ \pi^+$		$(3.2 \pm 1.6) \times 10^{-4}$
$\Lambda_c^+ p \bar{p} \pi^-$		$(2.65 \pm 0.29) \times 10^{-4}$
$\Sigma_c(2455)^0 p \bar{p}$ , $\Sigma_c^0 \rightarrow \Lambda_c^+ \pi^-$		$(2.4 \pm 0.5) \times 10^{-5}$
$\Sigma_c(2520)^0 p \bar{p}$ , $\Sigma_c(2520)^0 \rightarrow \Lambda_c^+ \pi^-$		$(3.2 \pm 0.7) \times 10^{-5}$
$\Lambda_c^+ \ell^- \bar{\nu}_\ell$ anything	[v]	$(10.9 \pm 2.2) \%$
$\Lambda_c^+ \ell^- \bar{\nu}_\ell$		$(6.2 \begin{array}{l} +1.4 \\ -1.3 \end{array}) \%$
$\Lambda_c^+ \pi^+ \pi^- \ell^- \bar{\nu}_\ell$		$(5.6 \pm 3.1) \%$
$\Lambda_c(2595)^+ \ell^- \bar{\nu}_\ell$		$(7.9 \begin{array}{l} +4.0 \\ -3.5 \end{array}) \times 10^{-3}$
$\Lambda_c(2625)^+ \ell^- \bar{\nu}_\ell$		$(1.3 \begin{array}{l} +0.6 \\ -0.5 \end{array}) \%$
$p h^-$	[x]	$< 2.3 \times 10^{-5}$
$p \pi^-$		$(4.5 \pm 0.8) \times 10^{-6}$
$p K^-$		$(5.4 \pm 1.0) \times 10^{-6}$

The semileptonic decay of heavy hadrons is a unique tool for determining the elements of the Cabibbo–Kobayashi–Maskawa (CKM) matrix.

The chosen semileptonic  $\Lambda_b \rightarrow \Lambda_c^- / \nu$  transition is one of the prominent decay channels out of the manifold available channels of the  $\Lambda b$  baryon reported by PDG.

The experimental group like DELPHI collaboration and LHCb collaboration reported their measurement on the slope parameter  $\rho^2$  of the Isgur-Wise function and the branching ratio of the semileptonic transition of  $\Lambda_b$  baryon.

# Framework: Hypercentral constituent quark model (HCQM)



*Jacobi Coordinates*

$$\rho = \frac{r_1 - r_2}{\sqrt{2}}$$
$$\lambda = \frac{r_1 + r_2 - 2r_3}{\sqrt{6}}$$

Hyperspherical Coordinates

$$x = \sqrt{\rho^2 + \lambda^2} \rightarrow \text{Hyperradius (Size)}$$

$$\xi = \arctan\left(\frac{\rho}{\lambda}\right) \rightarrow \text{Hyperangle (Form)}$$

# Framework: Hypercentral constituent quark model (HCQM)

Quark Wave Function Factorization

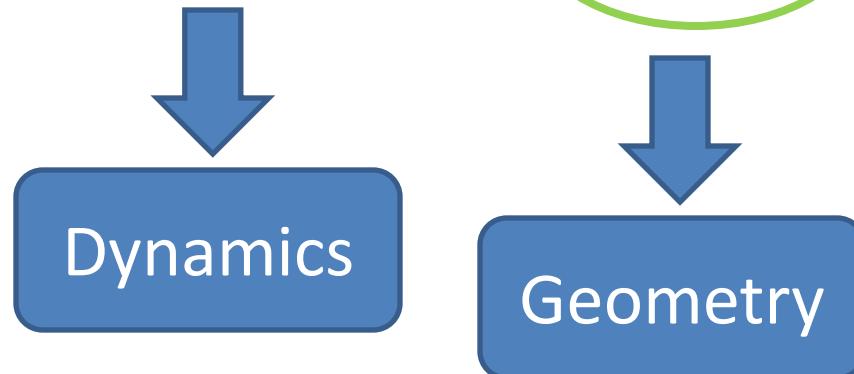
$$\psi(x, \xi, \Omega_\rho, \Omega_\lambda) = \boxed{\psi_{\nu\gamma}(x)}$$

$$Y_{\gamma, l_\rho, l_\lambda}$$

Where,

$\nu$  Hyperradial excitation

$\gamma$  Grandangular quantum number



The hyperspherical harmonics, satisfying the eigenvalue relation

$$L^2(\Omega)Y(\Omega) = \gamma(\gamma + 4) Y(\Omega)$$

# Framework: Hypercentral constituent quark model (HCQM)

$$\frac{P_x^2}{2m} = -\frac{\hbar^2}{2m}(\Delta_\rho + \Delta_\lambda) = -\frac{\hbar^2}{2m} \left( \frac{\partial^2}{\partial x^2} + \frac{5}{x} \frac{\partial}{\partial x} + \frac{L^2(\Omega)}{x^2} \right)$$

$$V(x) = \frac{\tau}{x} + \beta x + V_0$$

$$\left[ \frac{d^2}{dx^2} + \frac{5}{x} \frac{d}{dx} - \frac{\gamma(\gamma+4)}{x^2} \right] \psi_{\nu\gamma}(x) = -2m [E - V(x)] \psi_{\nu\gamma}(x)$$

$$\psi_{\nu\gamma} = \left[ \frac{(\nu-\gamma)!(2g)^6}{(2\nu+5)(\nu+\gamma+4)!} \right]^{\frac{1}{2}} (2gx)^\gamma \times e^{-gx} L_{\nu-\gamma}^{2\gamma+4}(2gx)$$

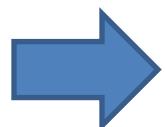
$$M_B = \sum m_i + \langle H \rangle$$

The wave function parameter g and hence the energy eigenvalue are obtained by applying virial theorem. The baryon masses are determined by the sum of the model quark masses, kinetic energy and potential energy.

$m_u$	$m_d$	$m_c$	$m_b$	$n_f$	$\alpha_s(\mu_0 = 1 \text{ GeV})$
0.330	0.350	1.55	4.95	4	0.6

# Isgur-Wise function for the Semileptonic transition of $\Lambda_b \rightarrow \Lambda_c e^- \bar{\nu}_e$

Approximation



$m_{b,c} \rightarrow \infty$

$$m_b, m_c \gg \Lambda_{QCD}$$

$$F_1(q^2) = G_1(q^2) = \xi(\omega), \quad F_2 = F_3 = G_2 = G_3 = 0$$

$$\xi(\omega) = 1 - \rho^2(\omega - 1) + c(\omega - 1)^2 + \dots \quad \rho^2 = -\frac{d\xi(\omega)}{d\omega}|_{\omega=1}$$

$$\omega = \frac{m_{\Lambda_b}^2 + m_{\Lambda_c}^2 - q^2}{2m_{\Lambda_b}m_{\Lambda_c}}$$

# Isgur-Wise function for the Semileptonic transition of $\Lambda_b \rightarrow \Lambda_c e^- \bar{\nu}_e$

Isgur-Wise function in HCQM

Phys. Rev. D 90, 074024 (2014)  
Eur. Phys. J. C 80:926 (2020)



$$\xi(\omega) = 16\pi^2 \int_0^\infty |\psi_{\nu\nu}(x)|^2 \cos(px) x^5 dx$$

$$\cos(px) = 1 - \frac{p^2 x^2}{2!} + \frac{p^4 x^4}{4!} + \dots \quad p^2 = 2m^2(\omega - 1)$$

# Slope and Curvature of the Isgur-Wise function

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- The slope and curvature of the Isgur-Wise function in HCQM can be derived as

$$\rho^2 = 16 \pi^2 m^2 \int_0^\infty |\psi_{v\gamma}(x)|^2 x^7 dx$$

$$c = \frac{8}{3} \pi^2 m^4 \int_0^\infty |\psi_{v\gamma}(x)|^2 x^9 dx$$

# Differential and Total Decay Width

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$$\frac{d\Gamma}{d\omega} = \frac{2}{3} m_{\Lambda_c}^4 m_{\Lambda_b} A \xi^2(\omega) \sqrt{\omega^2 - 1} \left[ 3\omega(\eta + \eta^{-1}) - 2 - 4\omega^2 \right]$$

To calculate the total decay width, we have integrated the above Equation over the solid angle as

$$\Gamma = \int_1^{\omega_{max}} \frac{d\Gamma}{d\omega} d\omega$$

where the upper bound of the integration  $\omega_{max}$  is the maximal recoil ( $q^2 = 0$ ) and it can be written as

$$\omega_{max} = \frac{m_{\Lambda_b}^2 + m_{\Lambda_c}^2}{2 m_{\Lambda_b} m_{\Lambda_c}}$$

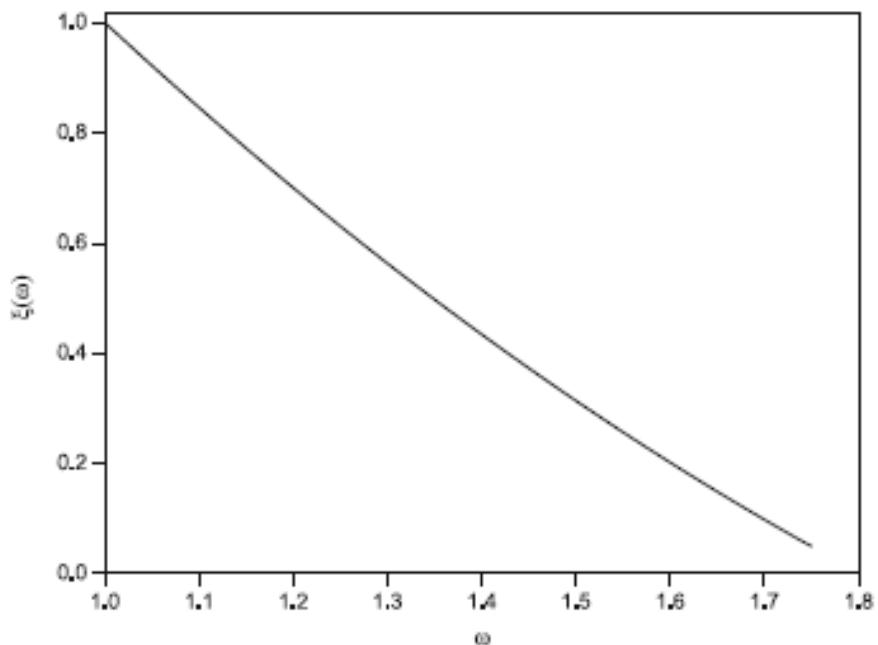
# Result

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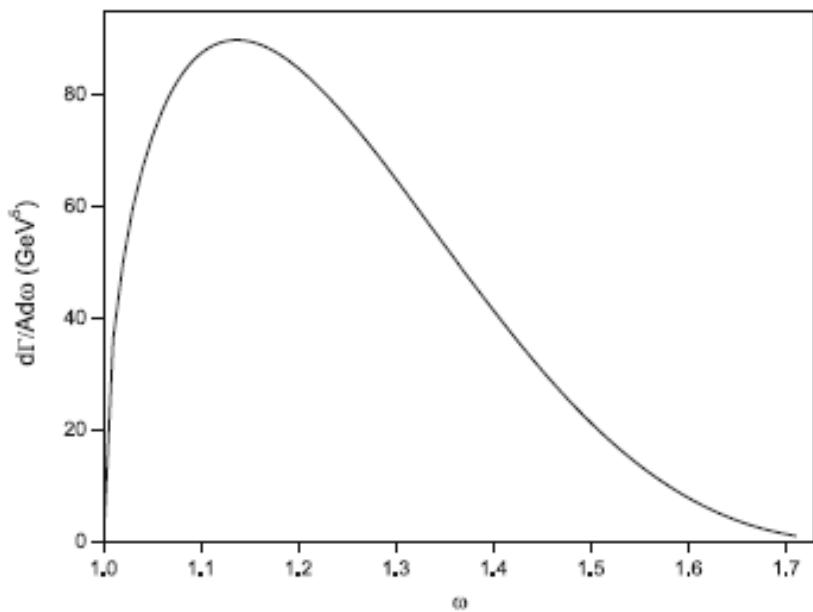
Slope ( $\rho^2$ )	Approach	
1.58	This work	
$1.63 \pm 0.07 \pm 0.08$	LHCb collaboration	PRD <b>96</b> , 112005 (2017)
1.51	Relativistic quark model	PRD <b>73</b> , 094002 (2006)
$1.35 \pm 0.13$	QCD sum rule	Phys. Lett. B <b>629</b> , 27 (2005)
$1.2^{+0.8}_{-1.1}$	Lattice QCD	Phys. Rev. D <b>57</b> , 6948 (1998)
1.61	Hyperspherical	Phys. Rev. D <b>90</b> 074024 (2014)
1.3	Large- $N_c$ limit	Nucl. Phys. B <b>396</b> , 38–52 (1993)
2.4	MIT bag model	Z. Phys. C <b>59</b> , 677 (1993)
1.4-1.6	Bethe–Salpeter equation	Phys. Rev. D <b>54</b> , 4629 (1996)
1.47	Light-front approach	Phys. Rev. D <b>77</b> 014020 (2008)
1.5	Spectator quark model	Z. Phys. C <b>51</b> 321 (1991)
$2.03 \pm 0.46^{+0.72}_{-1.00}$	DELPHI collaboration	Phys. Lett. B <b>585</b> , 63 (2004)

# Result

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**Fig. 1** The Isgur-Wise function ( $\xi(\omega)$ ) for the  $\Lambda_b \rightarrow \Lambda_c \ell \bar{\nu}$  semileptonic decay



**Fig. 2** The variation of differential decay rate for the  $\Lambda_b \rightarrow \Lambda_c \ell \bar{\nu}$  semileptonic decay

# RESULT

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Decay Width $\Gamma$ ( $10^{10}$ S $^{-1}$ )	References	Branching Ratio (%)	References
4.11	Present Work	6.04	Present Work
3.52	Phys. Rev. D <b>97</b> , 074007 (2018)	$6.04 \pm 1.70$	Phys. Rev. D <b>97</b> , 074007 (2018)
5.02	Phys. Rev. D <b>73</b> , 094002 (2006)	6. 9	Phys. Rev. D <b>73</b> , 094002 (2006)
4.42	Phys. Rev. D <b>94</b> , 073008 (2016)	6.48	Phys. Rev. D <b>94</b> , 073008 (2016)
4.86	Phys. Rev.D <b>91</b> , 074001 (2015)	6.9	Phys. Rev.D <b>91</b> , 074001 (2015)
5.39	Phys. Rev. D <b>56</b> , 348 (1997)	4.83	Phys. Rev. D <b>93</b> , 054003 (2016)
5.9	Phys. Rev. D <b>43</b> , 2939 (1991)	$6.2_{-1.3}^{+1.4}$	Phys. Rev.D <b>98</b> , 030001 (2018) Particle Data Group
4.92	Phys. Rev. D <b>90</b> , 074024 (2014)	$6.2_{-0.8}^{+1.1}$	(DELPHI Collaboration). Phys. Lett. B <b>585</b> , 63 (2004)

# RESULT AND CONCLUSIONS

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- The calculated value for the slope at zero recoil of the baryonic Isgur-Wise function is 1.58 which fairly agrees with other theoretical predictions.
- The predicted value for the slope of the Isgur-Wise function is in accordance with the experimental value  $1.63 \pm 0.07 \pm 0.08$ , recently reported by LHCb collaboration.
- By comparing the slope of the Isgur-Wise function at the zero recoil point for the heavy baryon and the heavy meson, we predict that the Isgur-Wise function for the baryons should be a much steeper function of  $\omega$  than the corresponding function for mesons.
- The HCQM gives plausible predictions for the Isgur-Wise function, decay width and the branching ratio corresponding to the  $\Lambda_b \rightarrow \Lambda_c e^- \bar{\nu}_e$  semileptonic decay

Thank You