

# Hypernuclei based on chiral interactions



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19th International Conference on Hadron Spectroscopy and Structure  
in memoriam Simon Eidelman (HADRON 2021), Mexico City

- Motivation
- Chiral YN interactions and estimates of 3BF contributions
- SRG evolution of (hyper-)nuclear interactions
- Impact of an increased  $E_{\Lambda}({}^3_{\Lambda}H)$  on hypernuclear binding
- Light  $S = -2$  hypernuclei
- Determination of CSB contact interactions and  $\Lambda n$  scattering length
- Conclusions & Outlook

in collaboration with Johann Haidenbauer, **Hoai Le**, Ulf Meißner

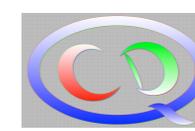
J. Haidenbauer et al. [arXiv:2107.01134 [nucl-th]].

H. Le et al., Eur. Phys. J. A 57 (2021), 217 [arXiv:2103.08395 [nucl-th]].

H. Le et al., Eur. Phys. J. A 56 (2020) 301 [arXiv:2008.11565 [nucl-th]].

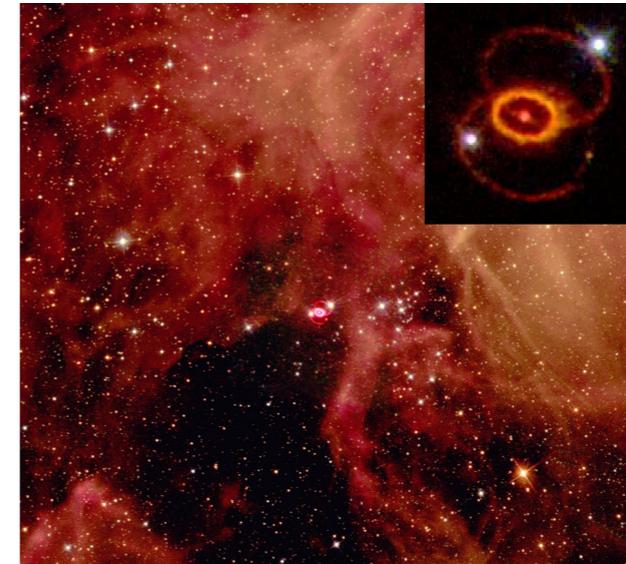
H. Le et al., Phys. Lett. B 801 (2020), 135189 [arXiv:1909.02882 [nucl-th]].

# Hypernuclear interactions

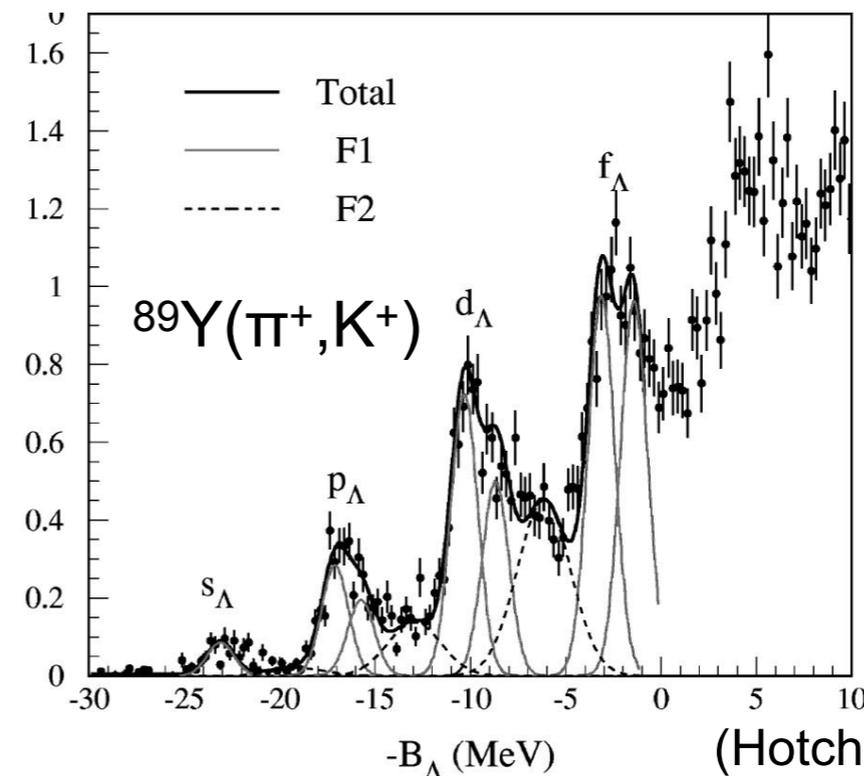
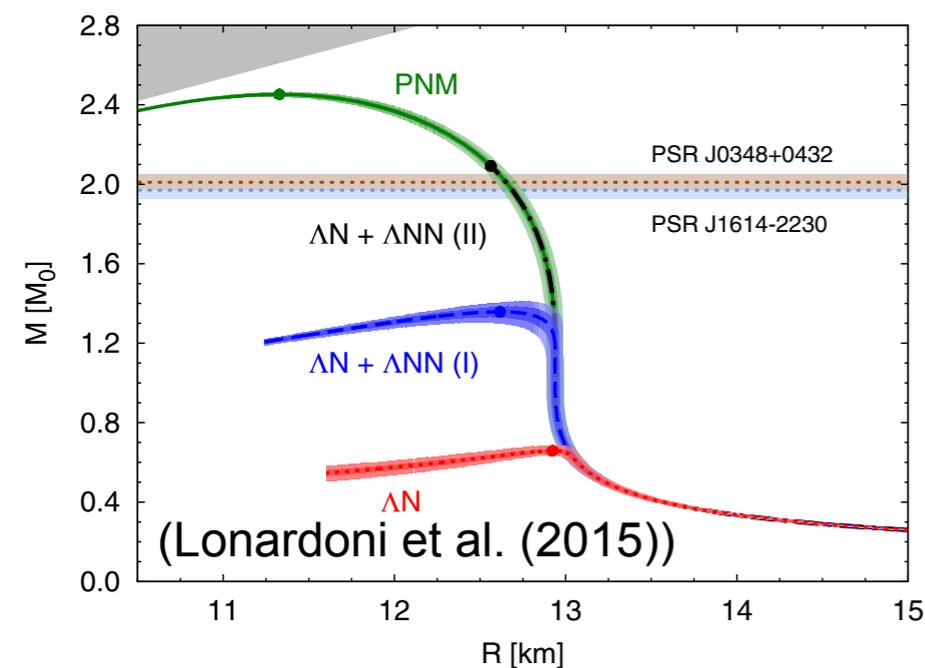
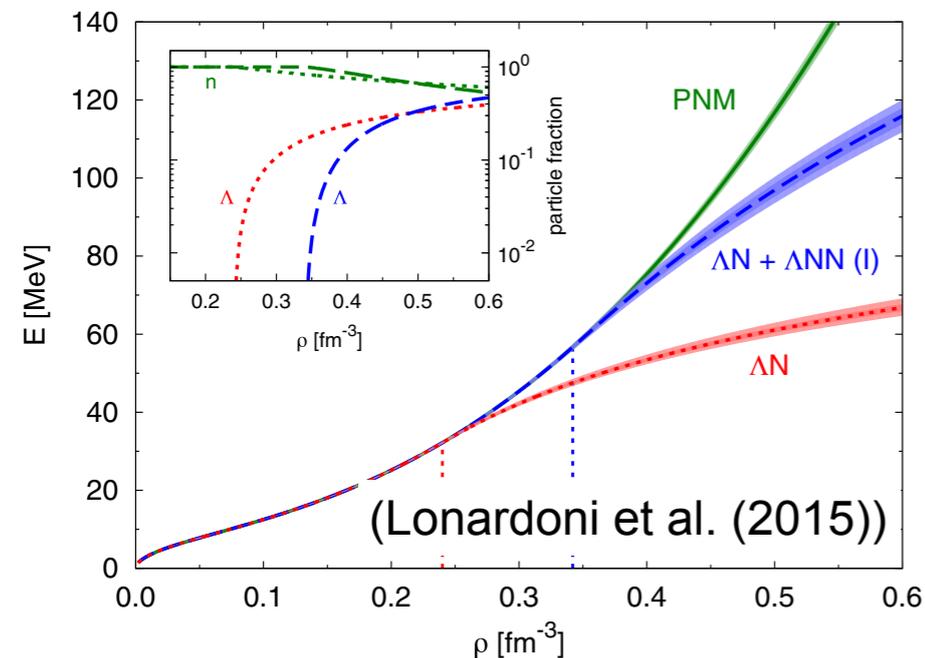


## Why is understanding hypernuclear interactions interesting?

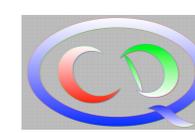
- „phenomenologically“
  - *hyperon contribution to the EOS, neutron stars, supernovae*
  - *$\Lambda$  as probe to nuclear structure*



(SN1987a, Wikipedia)



# Hypernuclear interactions

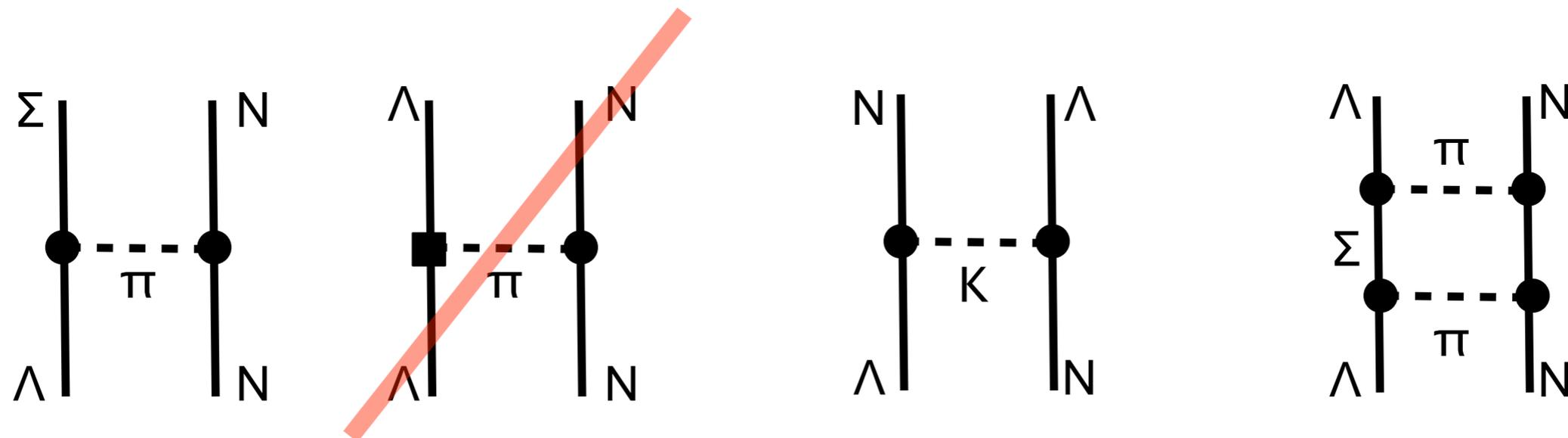


## Why is understanding hypernuclear interactions interesting?

- Hypernuclear interactions have interesting properties

### For example

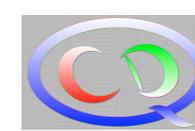
- *Particle conversion process is sometimes long-range part of the interaction*
- *experimental access to explicit chiral symmetry breaking*



suppressed by  
isospin symmetry (CSB!)

$$m_K \approx 500 \text{ MeV}$$

# Chiral NN & YN & YY interactions



	BB force	3B force	4B force	
<b>LO</b>		—	—	<b>5 (+1) NN/YN (YY)</b> short range parameters
<b>NLO</b>		—	—	<b>23(+5) NN/YN (YY)</b> short range parameters
<b>N<sup>2</sup>LO</b>			—	

(adapted from Epelbaum, 2008)

additional constraints required (e.g. for YN only 35 data, but 23 parameters at NLO)  
data too scarce to uniquely determine the short range LECs!

➔ **Two** realization for the YN interaction at NLO: NLO13 & NLO19  
with different assumptions on the LECs

(J. Haidenbauer et al., 2013 & 2019)

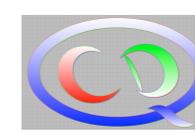
**YY interaction at NLO**

(J. Haidenbauer et al., 2016 & 2019)

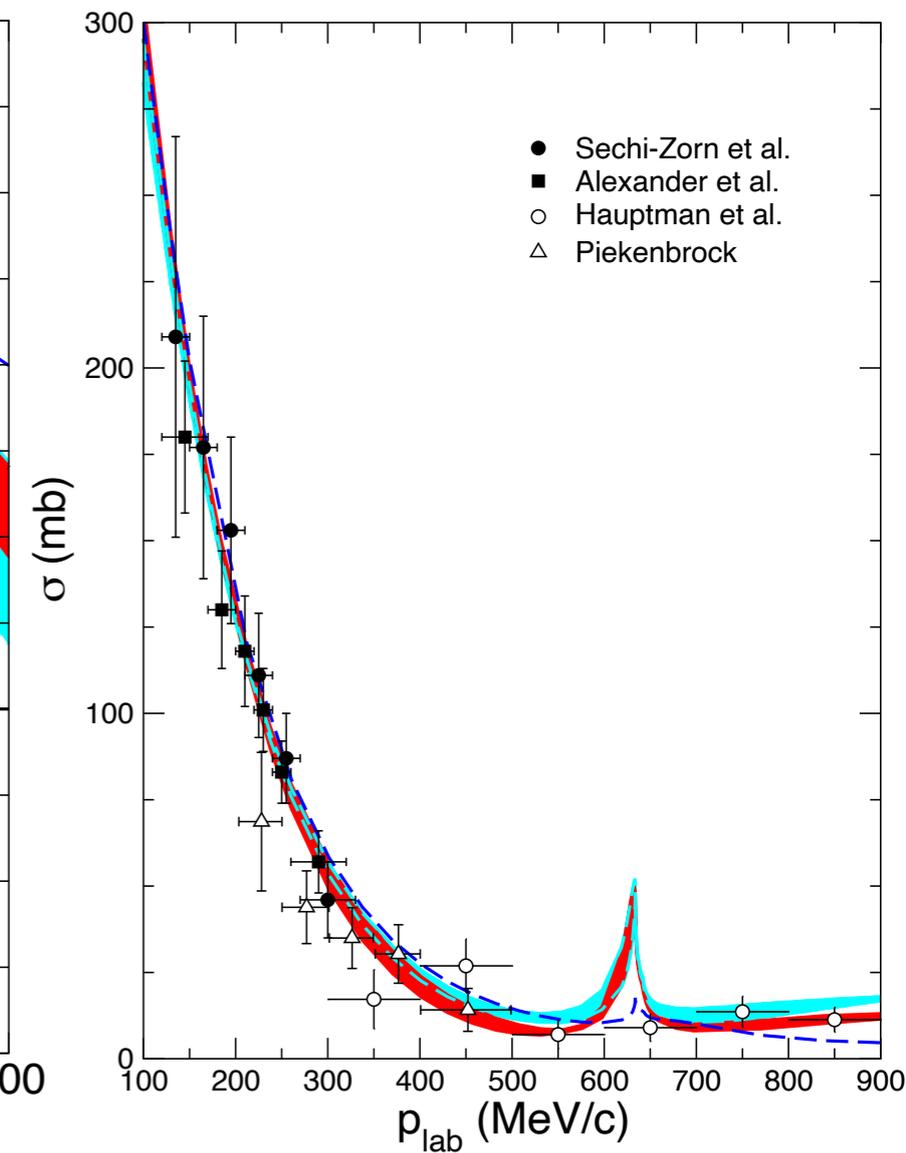
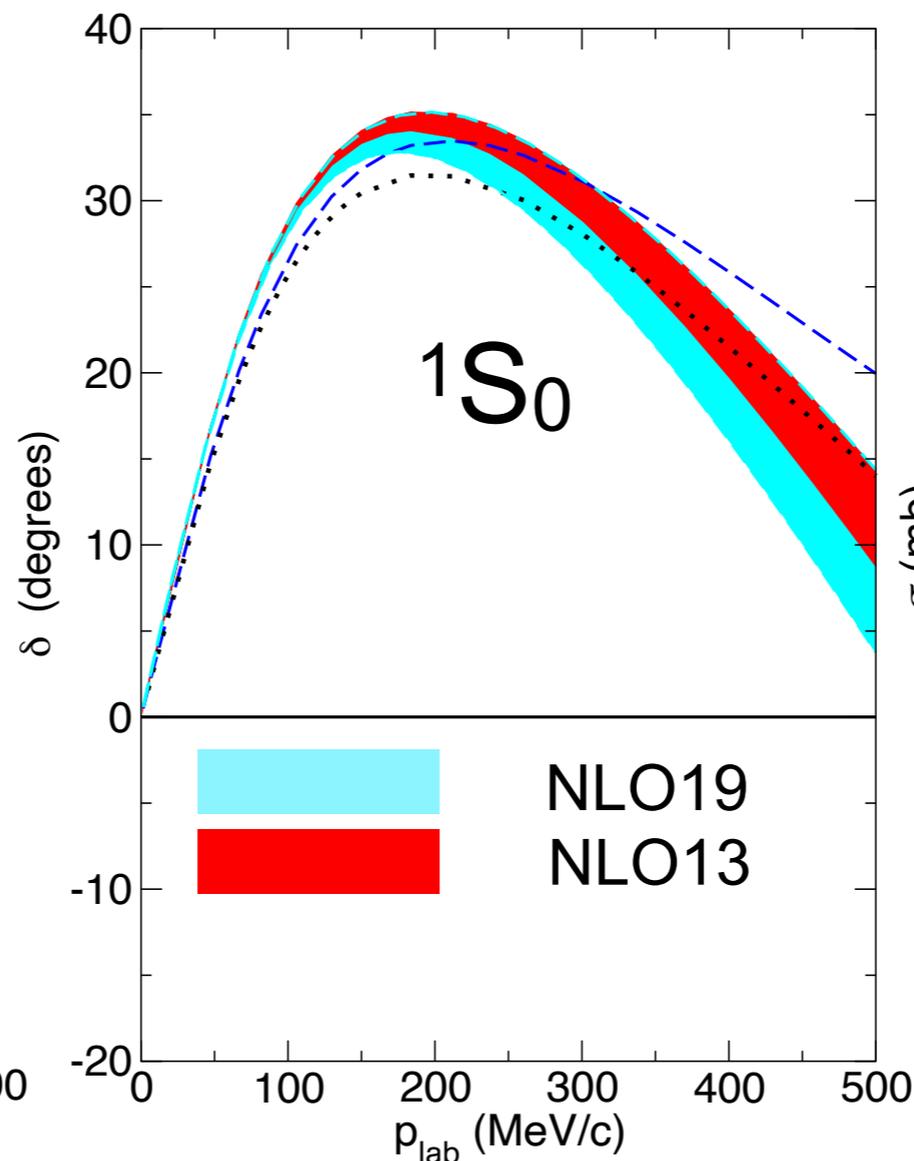
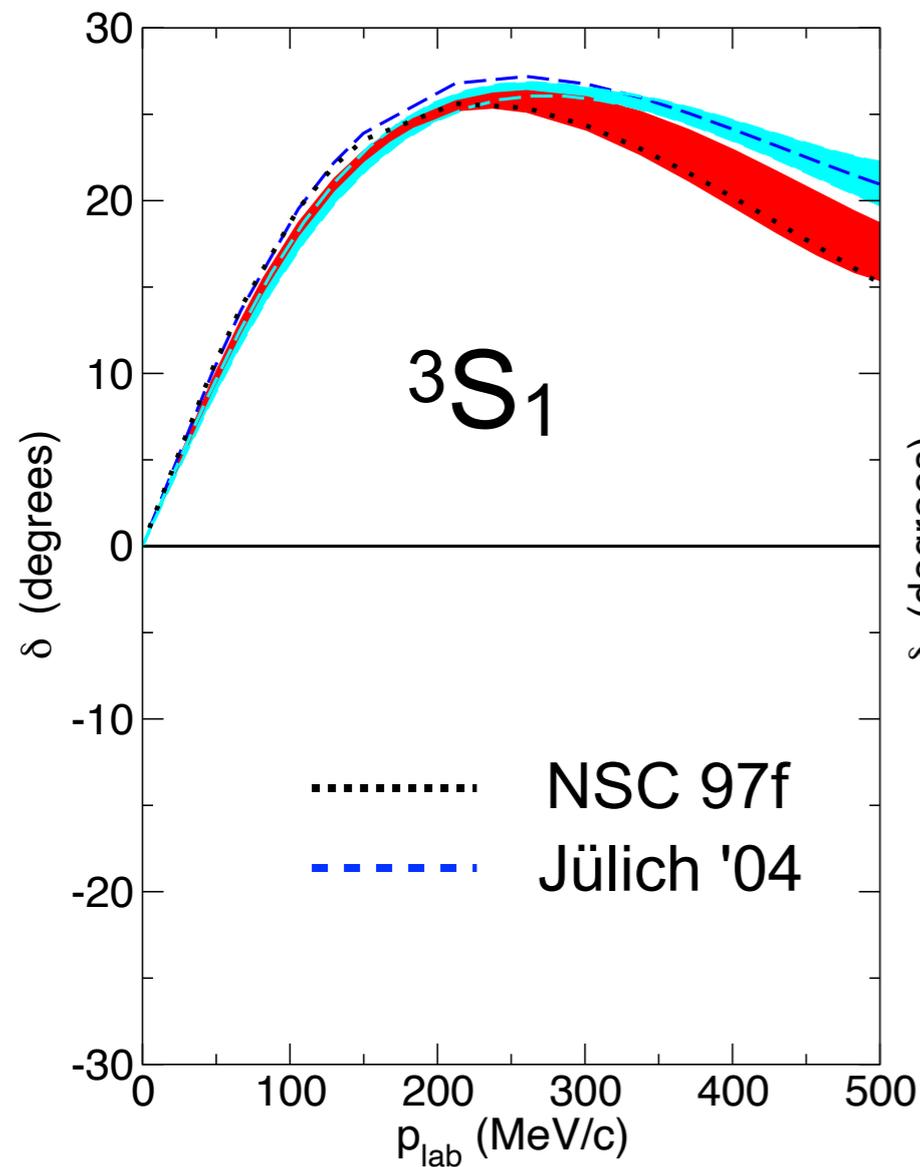
Chiral interactions include symmetries of QCD & retain flexibility to adjust to data

Regulator required — cutoff is also used to estimate uncertainty

# NLO13 / NLO19 - tool to estimate 3BF

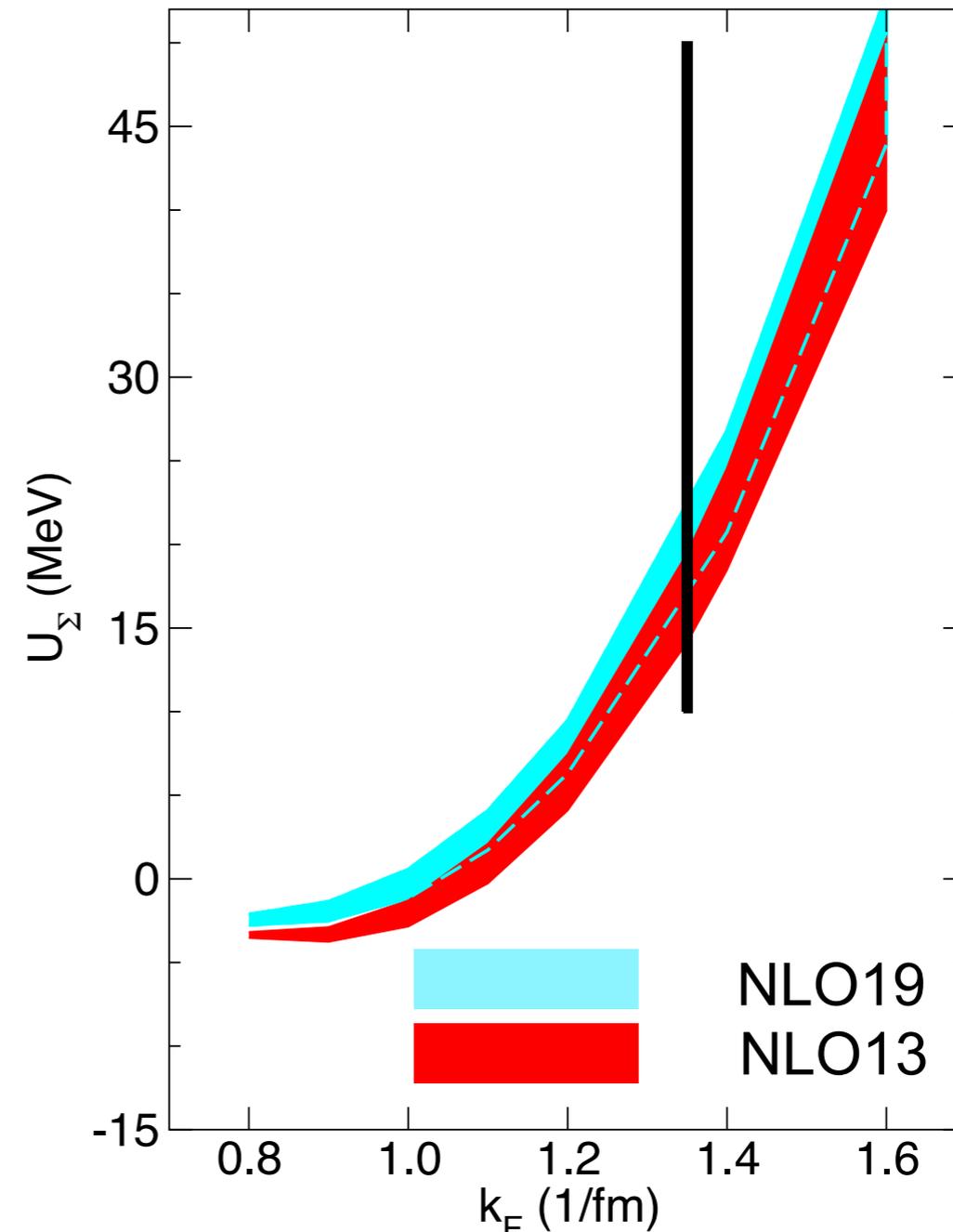
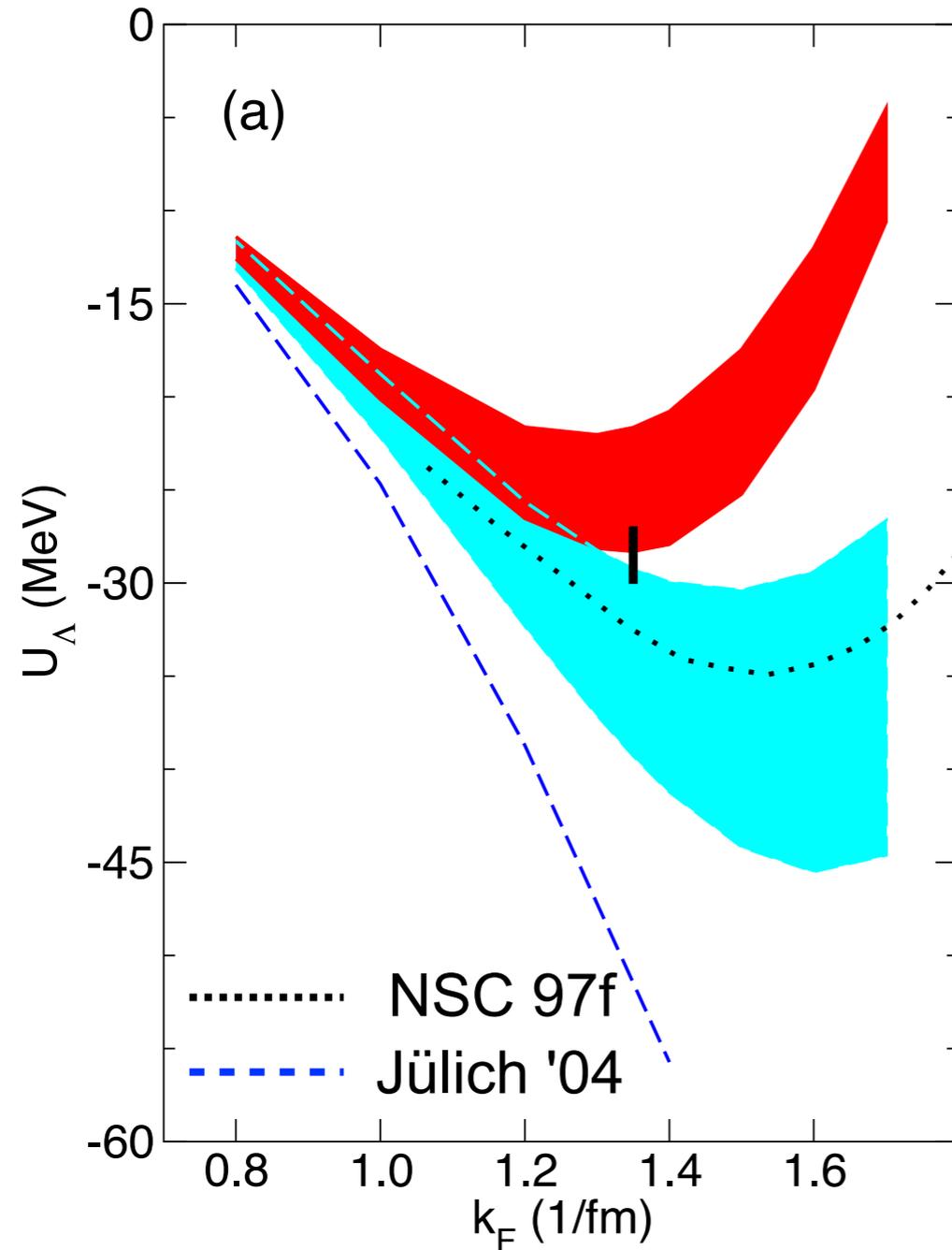
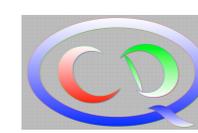


- Regularization required
  - Dependence on cutoff **indicates** uncertainty
- NLO13 and NLO19 interactions largely phase shift equivalent
  - differences indicate size of three-baryon interactions



(Haidenbauer et al., 2019)

# 3BF contribution in nuclear matter ?

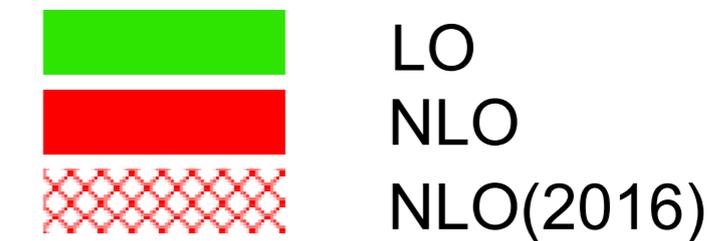
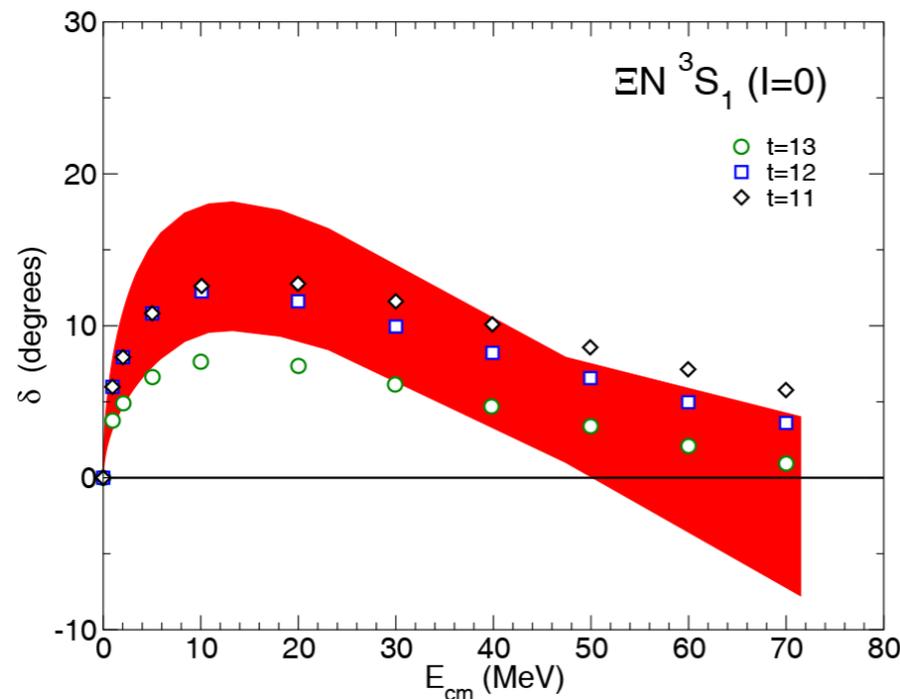
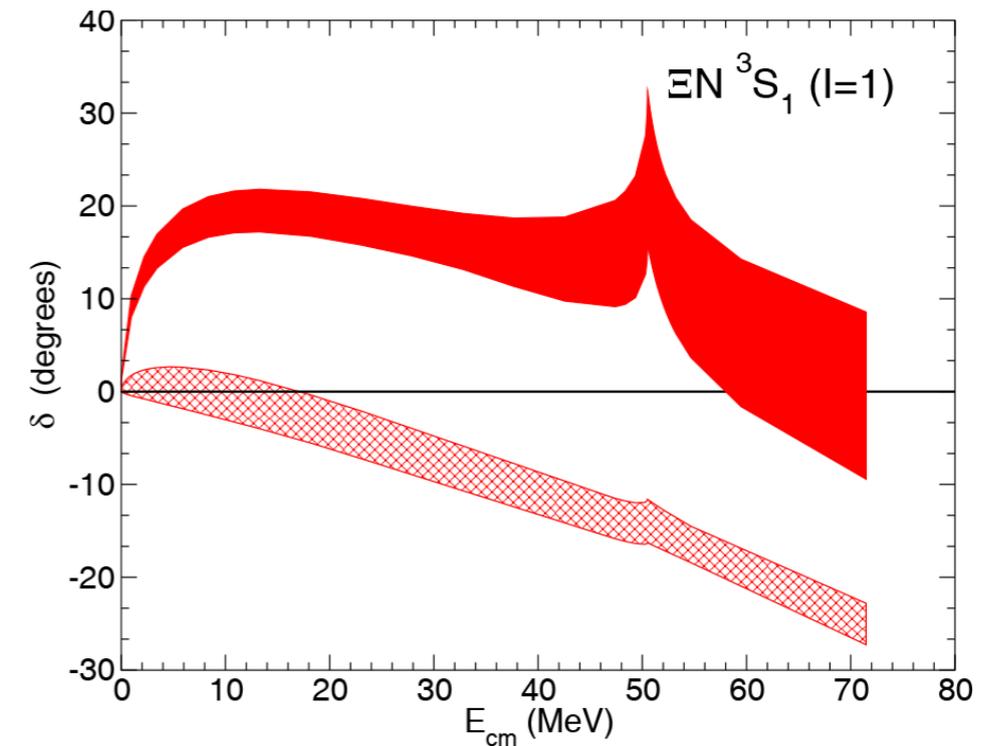
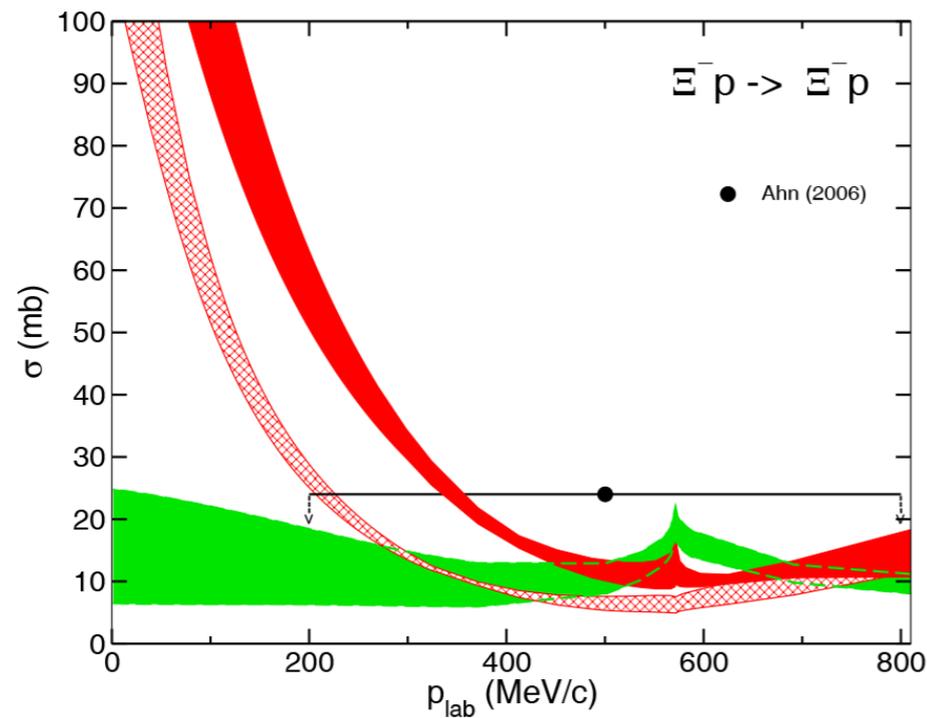
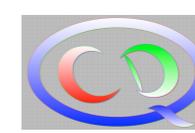


(Haidenbauer et al., 2019)



Indication that 3BF contribution is significant at saturation density  
Probably less important for light hypernuclei

# YY interaction



(Haidenbauer et al., 2019)



adjusted to data & LQCD (HAL QCD)

updated version consistent with  $\Xi$ -nuclei (only change in  $\Xi N \ ^3S_1$ )

**Similarity renormalization group** is by now a **standard tool** to obtain soft effective interactions for various many-body approaches (NCSM, coupled-cluster, MBPT, ...)

Idea: perform a unitary transformation of the NN (and YN interaction) using a cleverly defined "generator"

$$\frac{dH_s}{ds} = \left[ \underbrace{[T, H(s)]}_{\equiv \eta(s)}, H(s) \right] \quad H(s) = T + V(s)$$

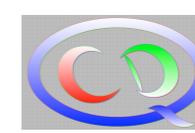
this choice of generator drives  $V(s)$  into a diagonal form in momentum space

- $V(s)$  will be phase equivalent to original interaction
- short range  $V(s)$  will change towards softer interactions
- 3BF, 4BF, ... can in principle be generated but are omitted here
- $\lambda = \left( \frac{4\mu_{BN}^2}{s} \right)^{1/4}$  is a measure of the width of the interaction in momentum space

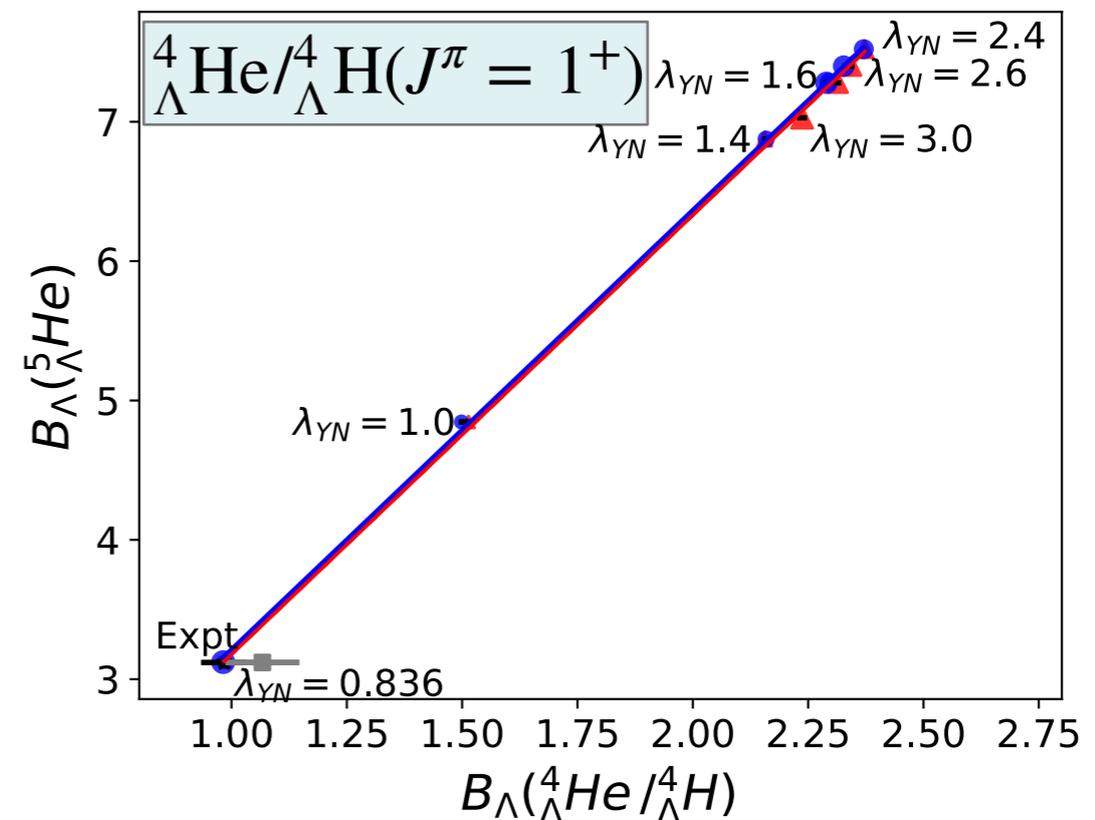
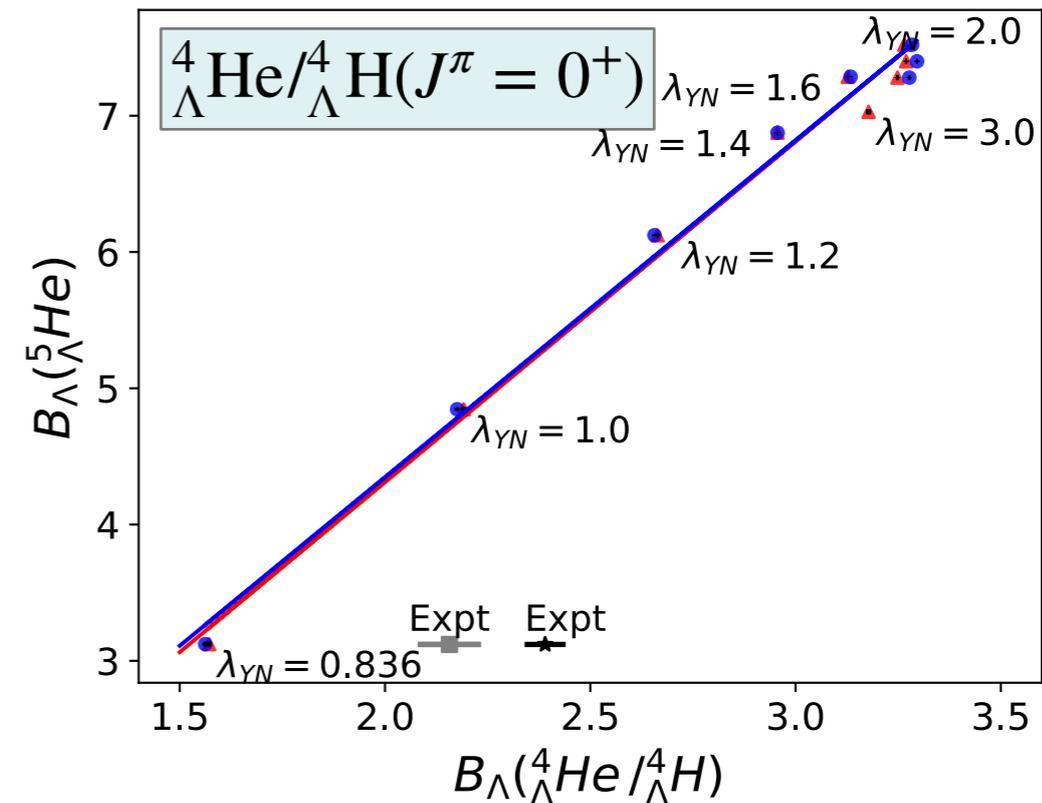
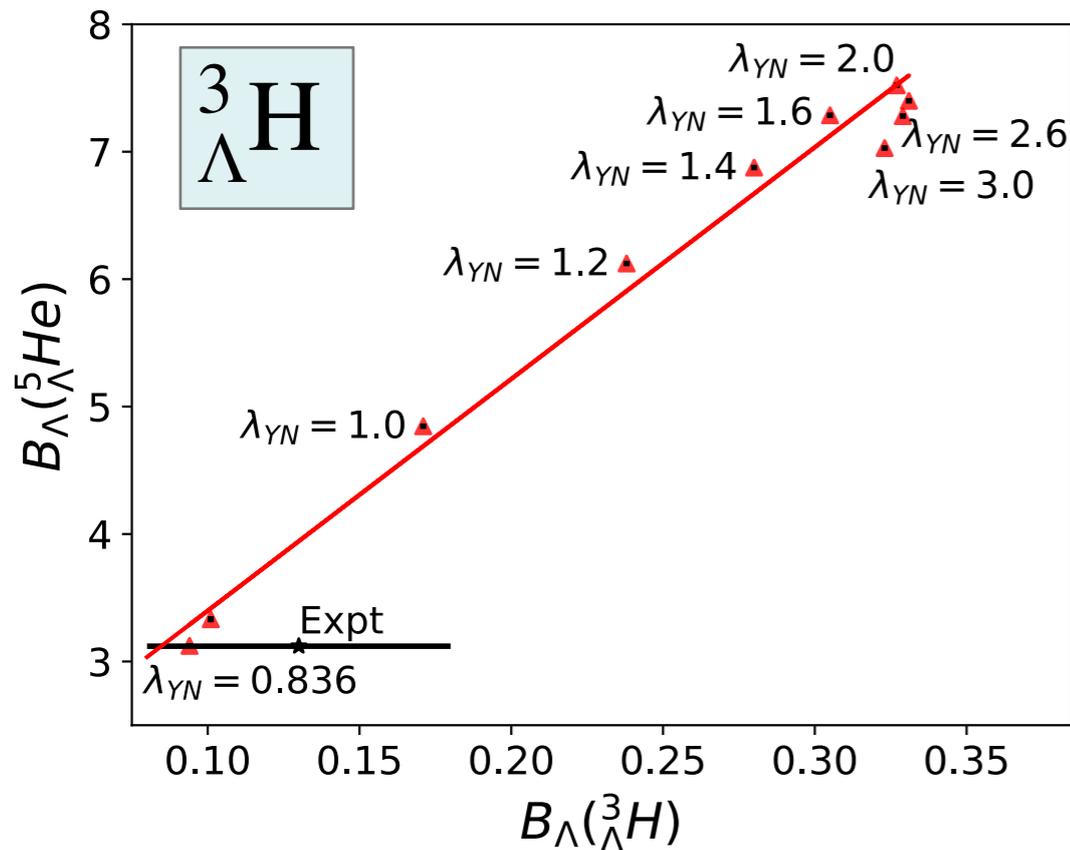
(Bogner et al., 2007)

**Unfortunately:  $\Lambda$ NN SRG induced-3BFs are large, probably much larger than chiral ones!** (see also Wirth et al. (2016))

# Correlation of separation energies

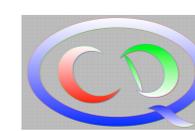


Separation energies of s-shell hypernuclei are strongly correlated (to  ${}^5_{\Lambda}\text{He}$ )

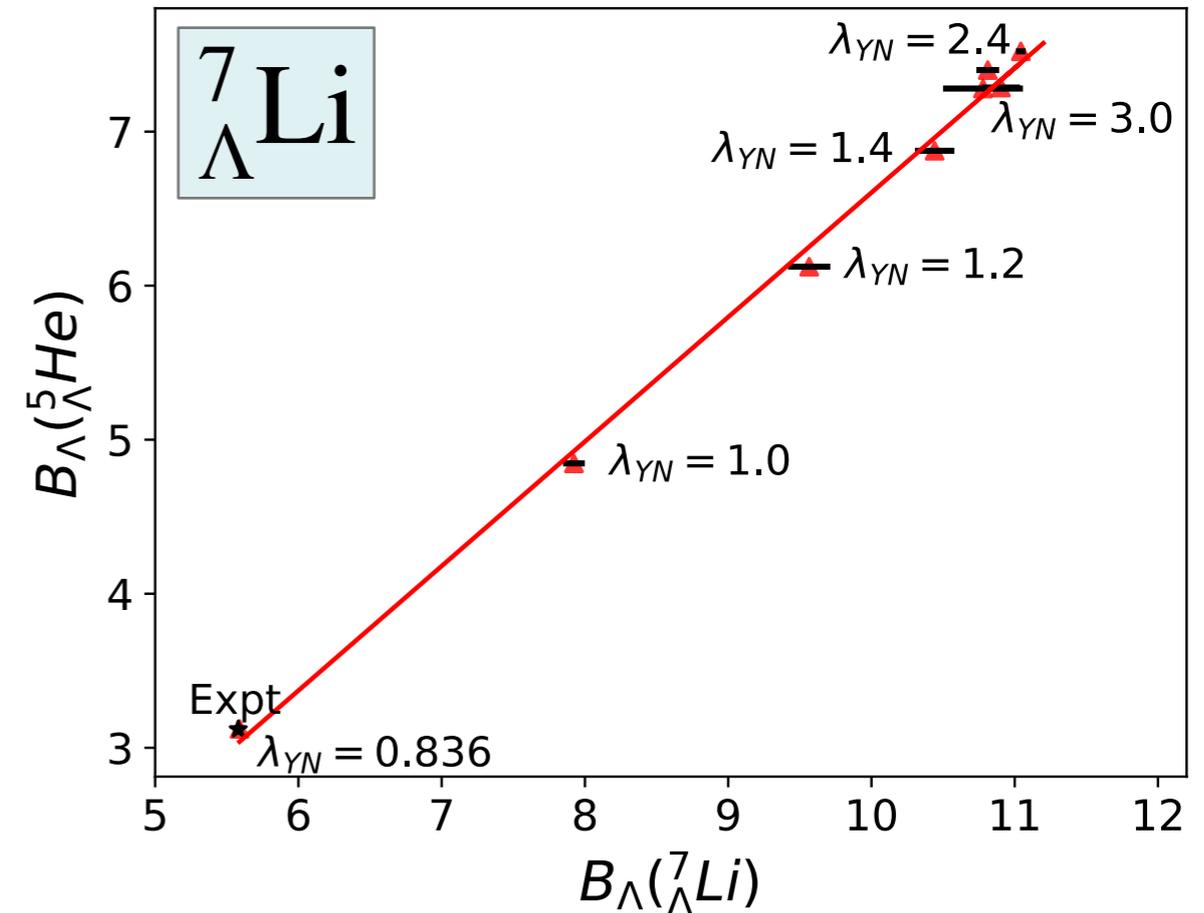
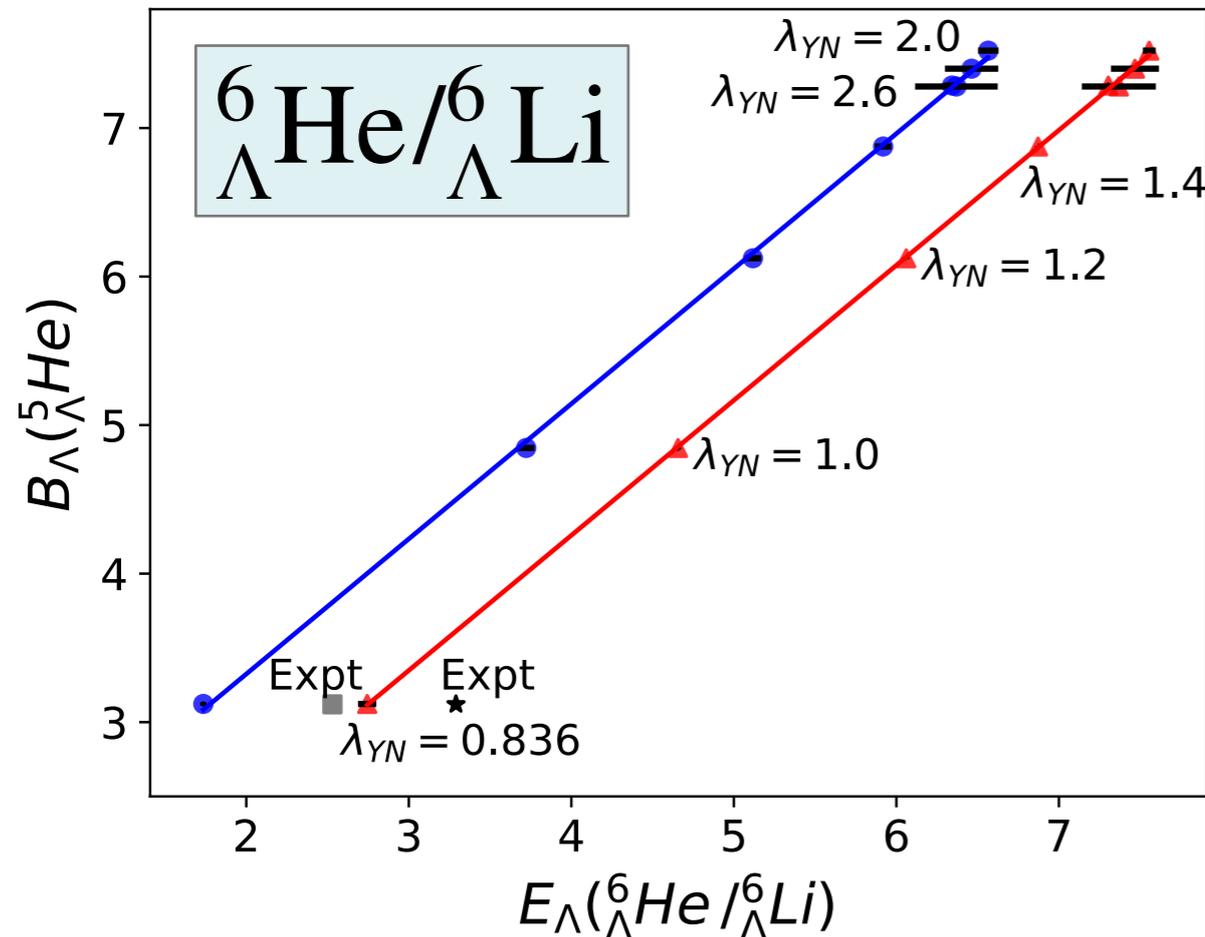


- YN interaction: **NLO 600 (2015)**
- no CSB in YN and masses added here (yet)
- strong overbinding for  $\lambda \gtrsim 1.0 \text{ fm}^{-1}$
- but  $A=3$  and  $A=5$  consistently predicted for  $\lambda \approx 0.836 \text{ fm}^{-1}$

# p-shell hypernuclei

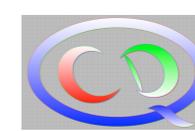


Separation energies of p-shell hypernuclei are also correlated (to  ${}^5_{\Lambda}\text{He}$ )



- YN interaction: **NLO19(600)**
- ${}^7_{\Lambda}\text{Li}$  astonishingly well reproduced at "magic"  $\lambda \approx 0.836 \text{ fm}^{-1}$
- $A=6$  in our calculations not particle stable
- NCSM works for narrow resonances
- Coulomb contribution in  $A = 6$  ( ${}^4\text{He}$  is used as baseline)

# Increased binding of ${}^3_{\Lambda}\text{H}$



- ${}^3_{\Lambda}\text{H}$  is used to determine relative strength of  ${}^3\text{S}_1/{}^1\text{S}_0$  interactions  
or relative size of  $a_3^{\Lambda N}$  and  $a_1^{\Lambda N}$
- Jurič et al. (1973!)  
new: Adam et al. (2019)

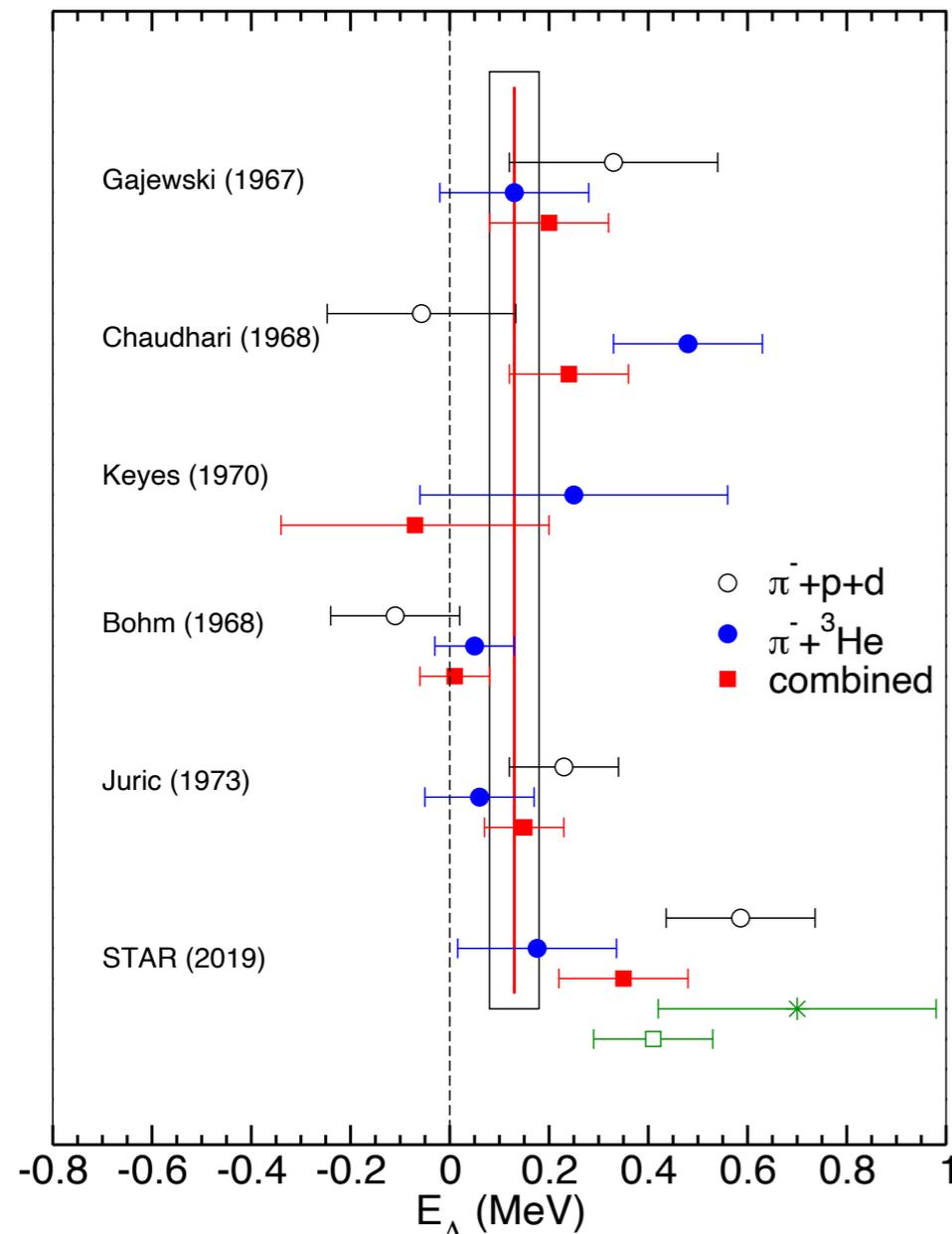
$$E_{\Lambda}({}^3_{\Lambda}\text{H}) = (130 \pm 50) \text{ keV}$$

$$E_{\Lambda}({}^3_{\Lambda}\text{H}) = (410 \pm 120) \text{ keV}$$

- separation energies of light hypernuclei have often been obtained many years ago from emulsion data
- systematic uncertainties?
- different experiments contradict each other

What would be the impact on hypernuclear binding in general if  ${}^3_{\Lambda}\text{H}$  the binding increases?

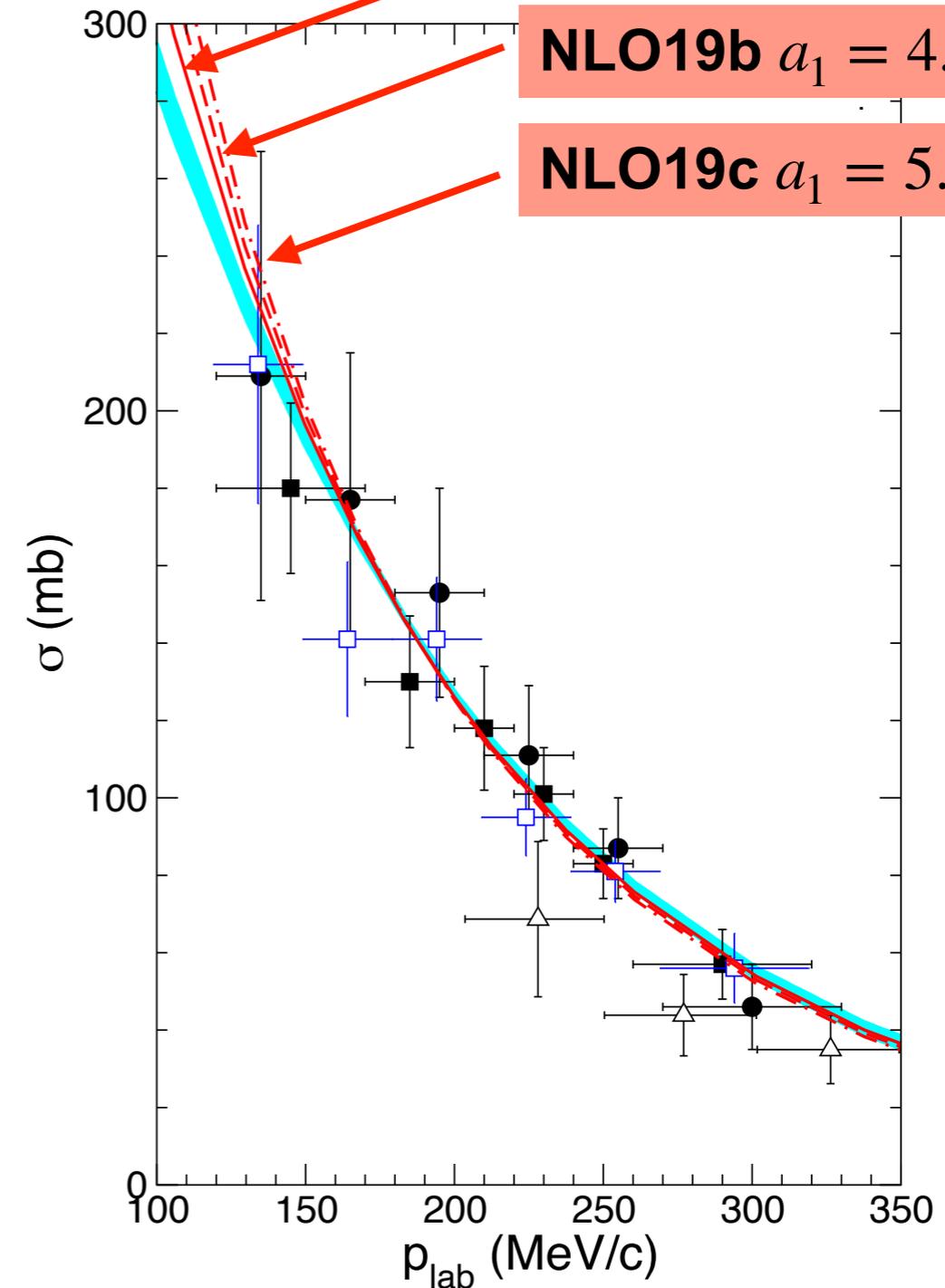
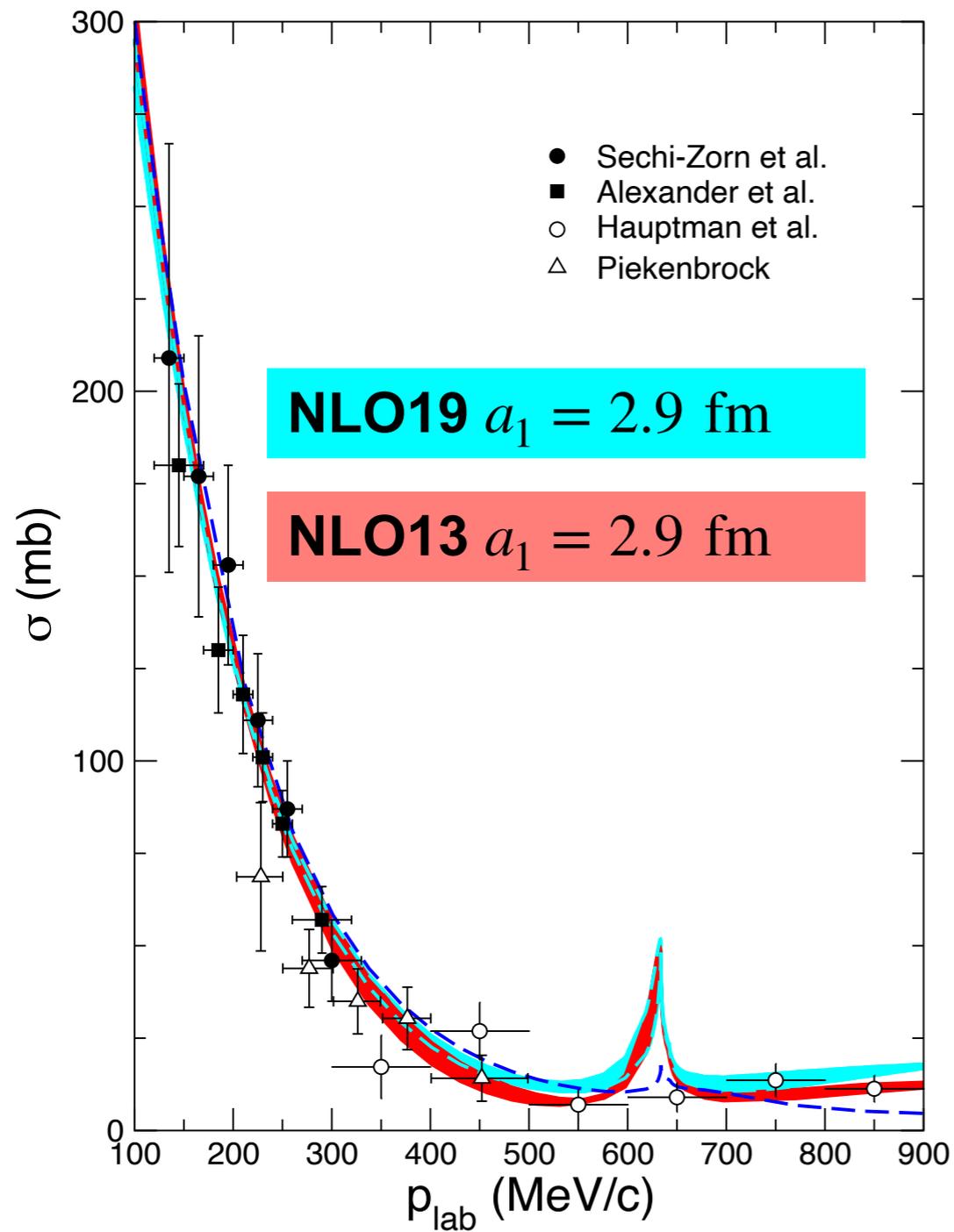
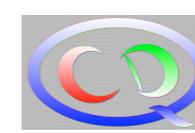
Equivalent to: What happens if  $a_1^{\Lambda N}$  increases?



(Le et al., 2020)

# Increasing $a_1^{\Lambda N}$ ....

$\Lambda p \rightarrow \Lambda p$



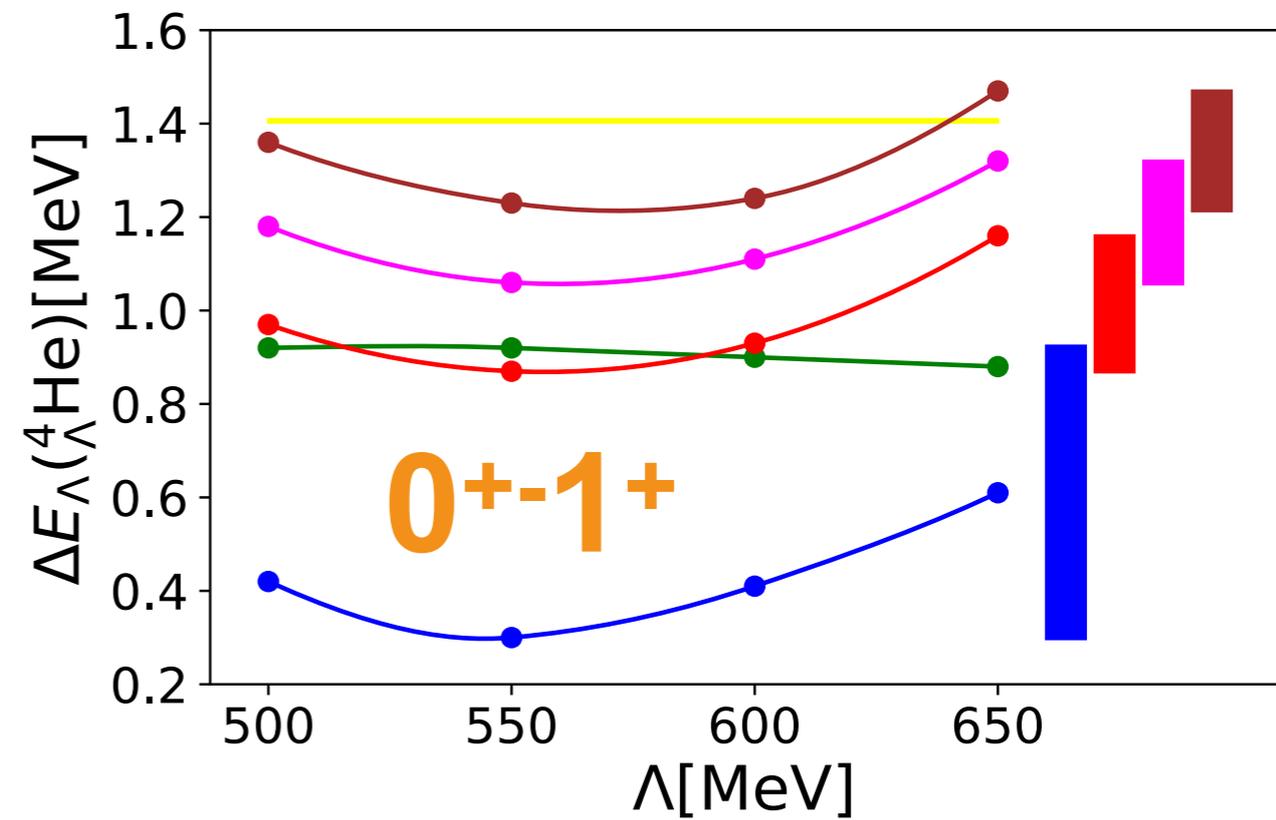
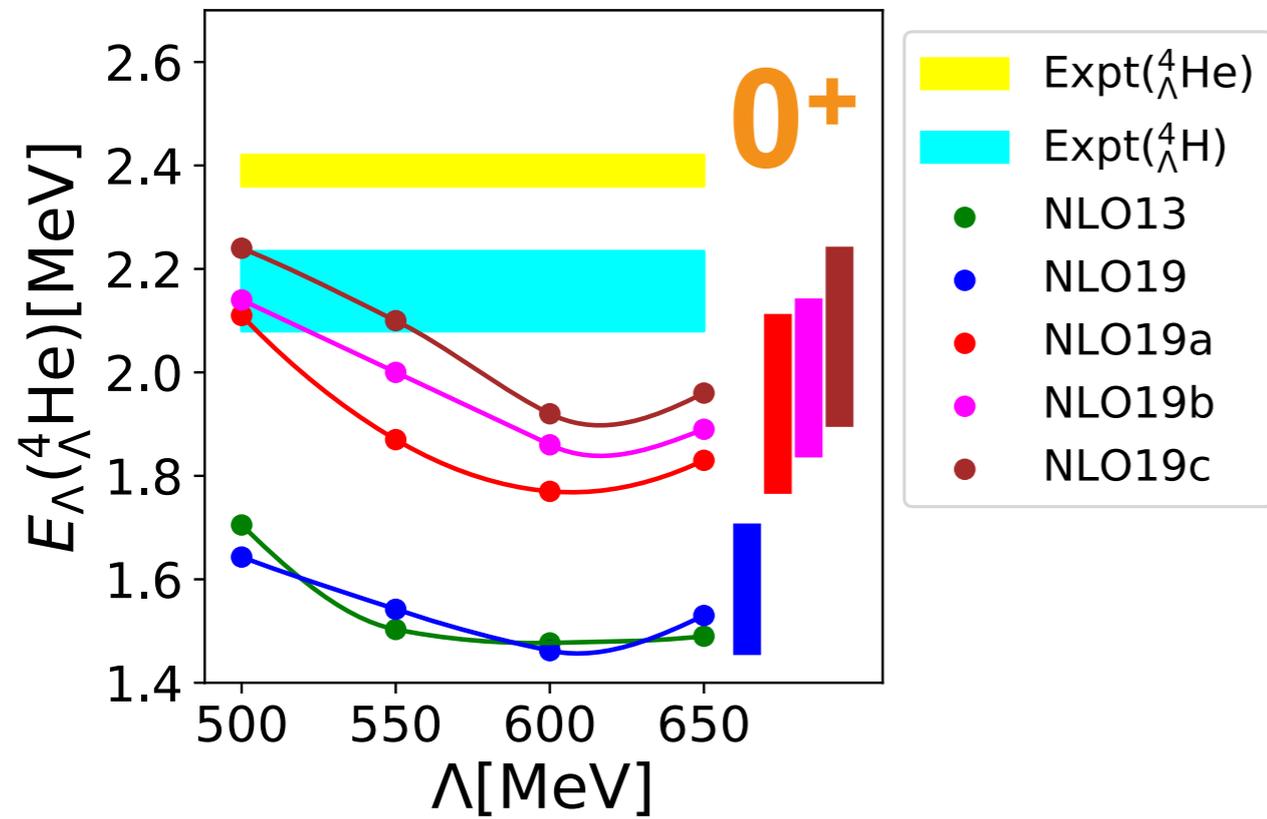
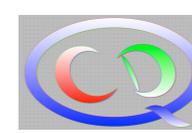
**NLO19a**  $a_1 = 4.0$  fm

**NLO19b**  $a_1 = 4.5$  fm

**NLO19c**  $a_1 = 5.0$  fm

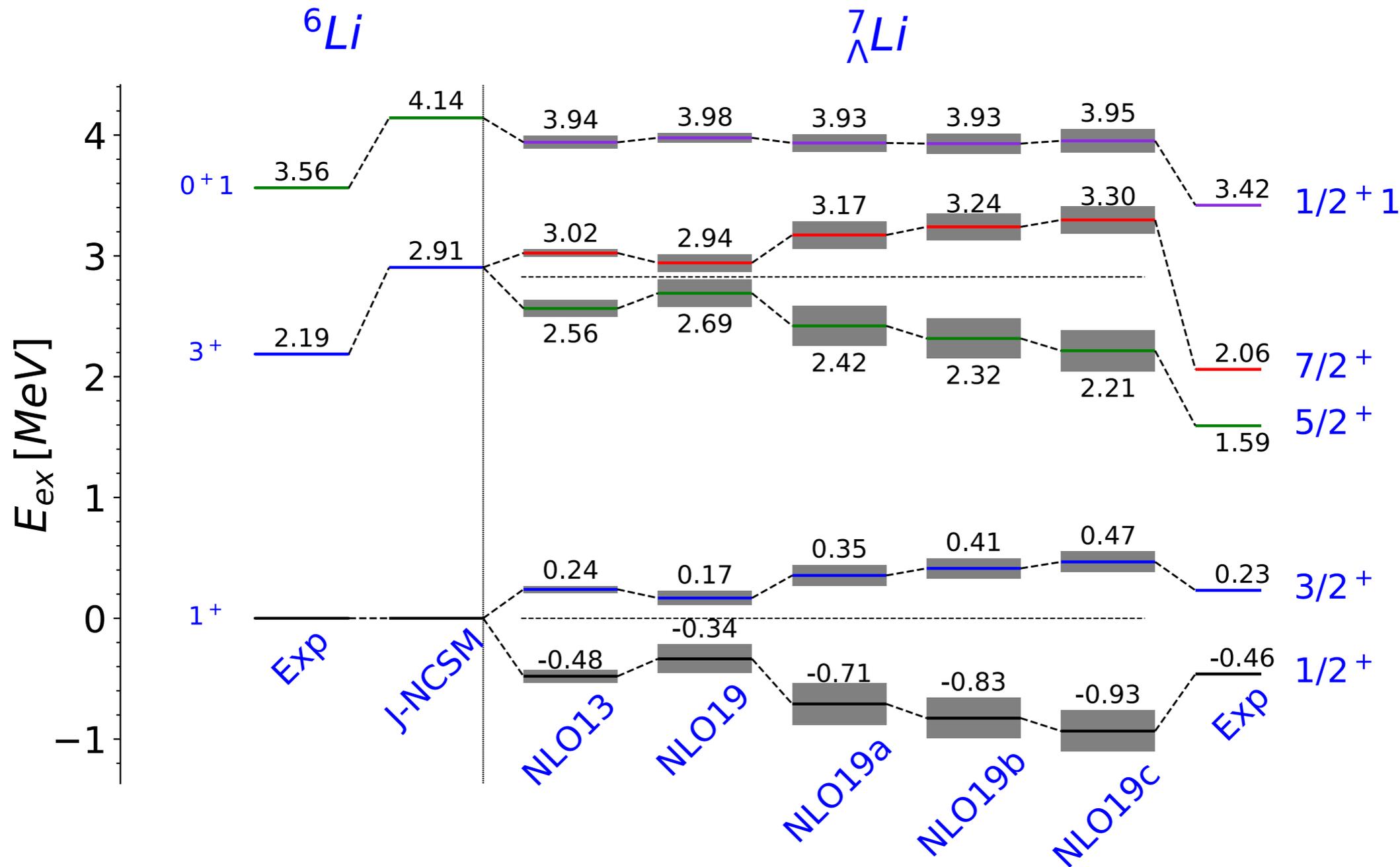
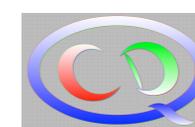
... can be done without changing the nice description of available YN data ✓

Increasing  $a_1^{\Lambda N}$  ....



... improves the description of  $^4_{\Lambda}\text{He}$  ✓

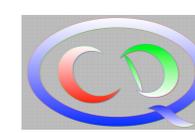
Increasing  $a_1^{\Lambda N}$  ....



... does not distort the description of  ${}^7_{\Lambda}\text{Li}$  ✓

**In summary: an increase of the hypertriton binding energy is not excluded by binding energies of other light hypernuclei!**

# $S = -2$ hypernuclei — ${}_{\Lambda\Lambda}^6\text{He}$

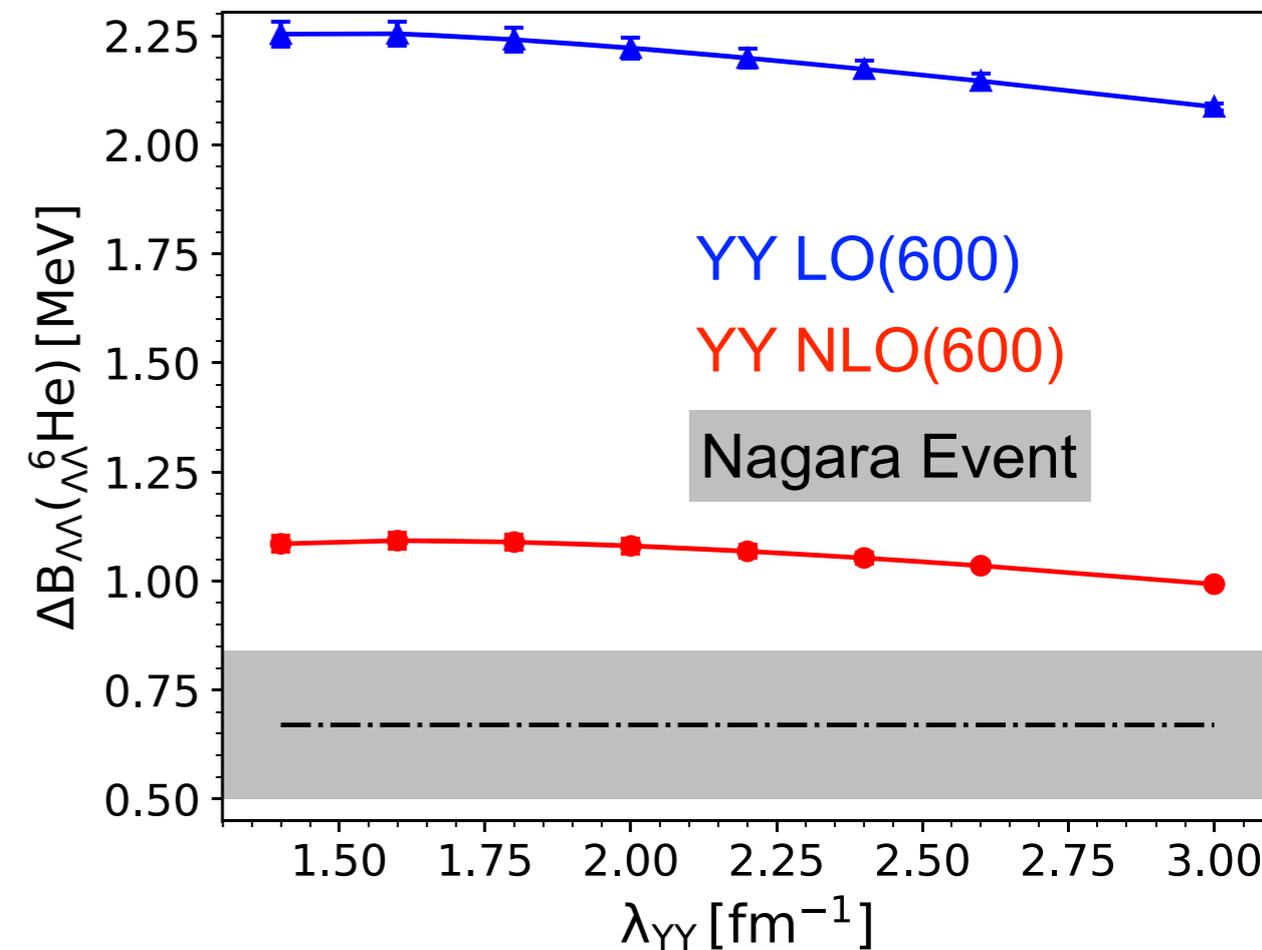


(Le et al., 2021)

- $\Lambda\Lambda$  excess binding energy

$$\begin{aligned}\Delta B_{\Lambda\Lambda} &= B_{\Lambda\Lambda} - 2B_{\Lambda} \\ &= 2E({}^A_{\Lambda}X) - E({}_{\Lambda\Lambda}^AX) - E({}^{A-2}X)\end{aligned}$$

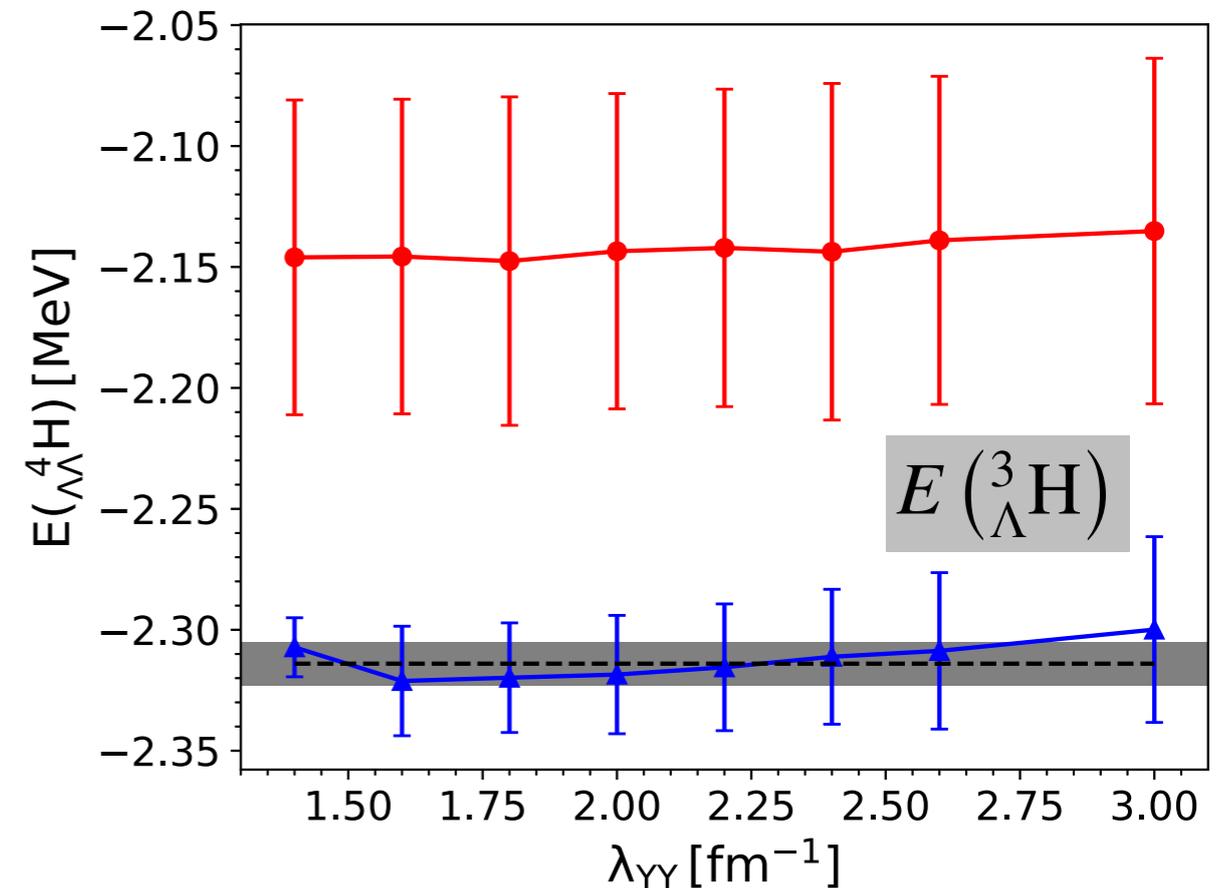
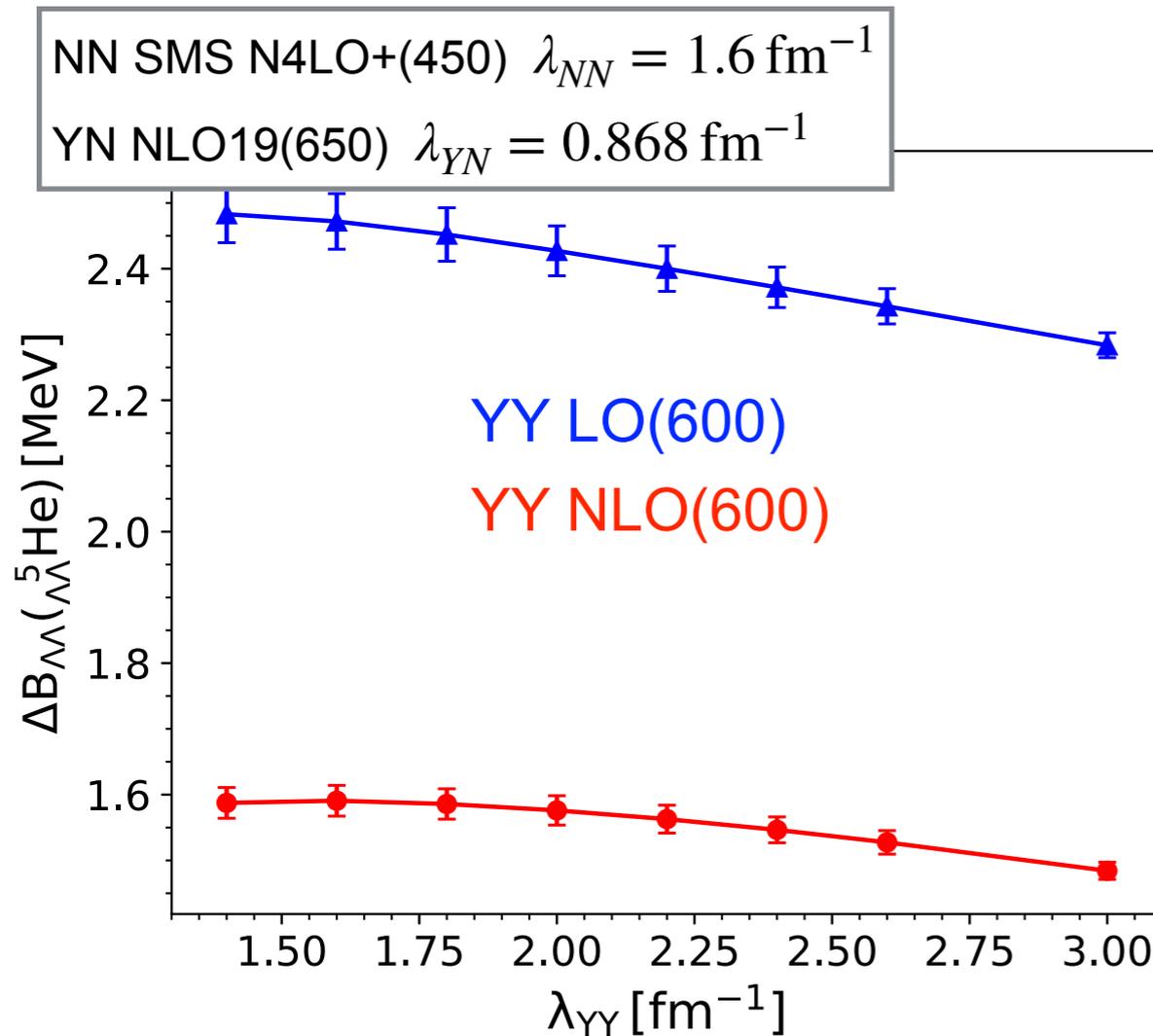
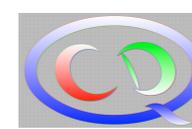
- NN, YN and YY interactions contribute
- use NN and YN that describe nuclei and single  $\Lambda$  hypernuclei
- small  $\lambda_{YY}$  dependence
- LO overbinds YY
- NLO predicts binding fairly well



NN SMS N4LO+(450)  $\lambda_{NN} = 1.6 \text{ fm}^{-1}$   
 YN NLO19(650)  $\lambda_{YN} = 0.868 \text{ fm}^{-1}$

**Can an  $S = -2$  bound state for  $A = 4,5$  be expected?**

# $S = -2$ hypernuclei — ${}_{\Lambda\Lambda}{}^5\text{He}$ & ${}_{\Lambda\Lambda}{}^4\text{H}$



- $A = 5$ :  $\Lambda\Lambda$  excess binding energy &  $A = 4$ : binding energy
- $A = 5$ : LO & NLO predicts bound state
- $A = 4$ : NLO unbound, LO at threshold to binding (see also Contessi et al., 2019)
- excess energy larger for  $A = 5$  than for  $A = 6$  (in contrast to Filikhin et al., 2002!)

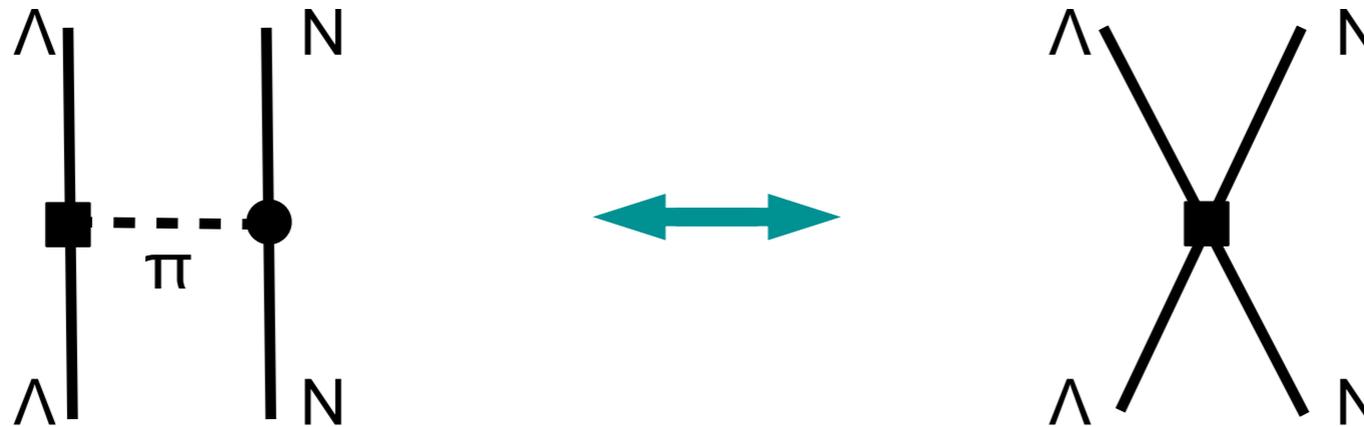
**$S = -2$  bound state for  $A = 5$  can be expected,**

**for  $A = 4$  less likely but not ruled out!**

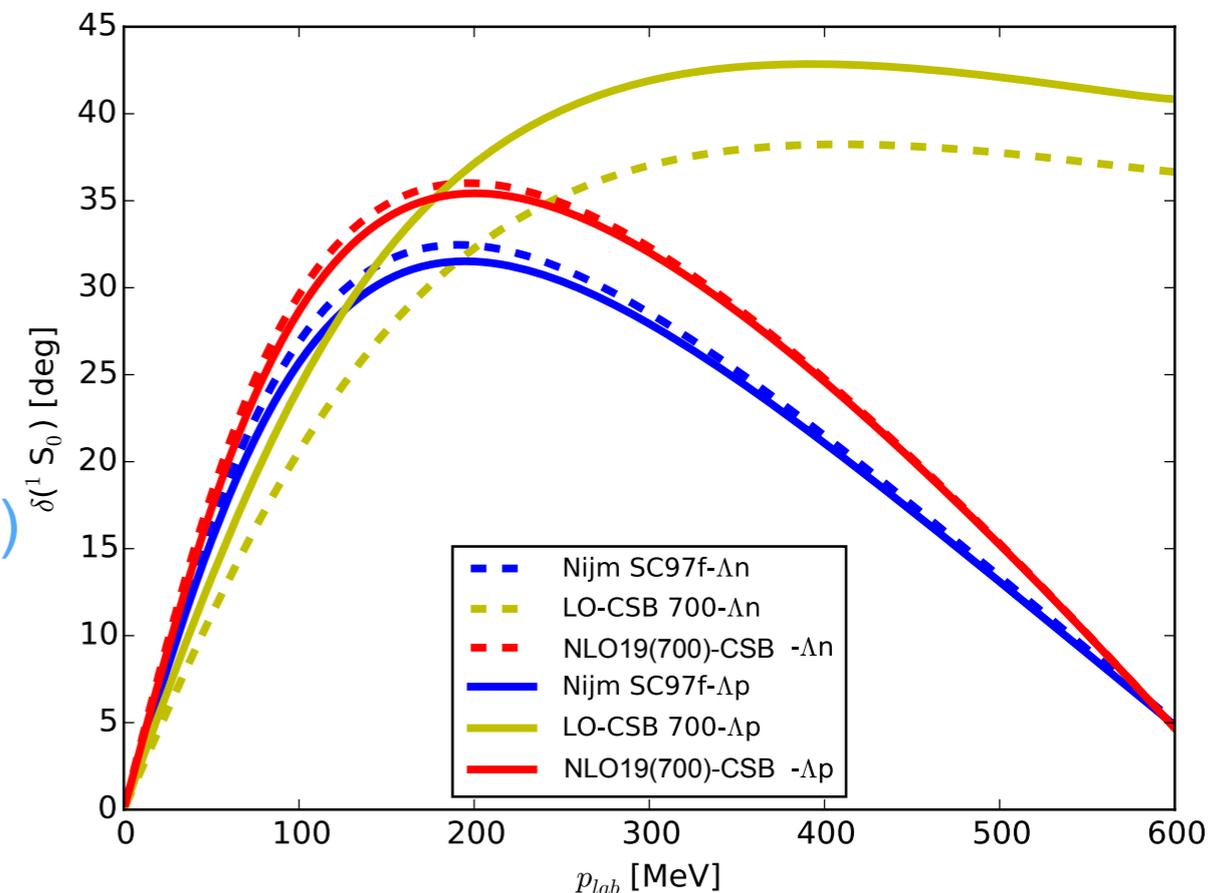
# Standard approach to CSB in YN

add  $\Lambda\Lambda\pi$  coupling using  $\Sigma^0$ - $\Lambda$  mixing and  $\pi^0$ - $\eta$  mixing

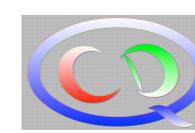
other short ranged mechanisms are usually neglected  $\longrightarrow$  **model dependence**



- CSB leads to new long-ranged contribution to the YN interaction
- possibly large CSB contributions
- CSB for LO larger than for SC97 and NLO
- seems to be supported by experiment (e.g. approximately 230 keV CSB in  $A=4$ )
- Gazda & Gal (2016) relate it to  $\Sigma N$ - $\Lambda N$  matrix elements to include long- and short range interactions



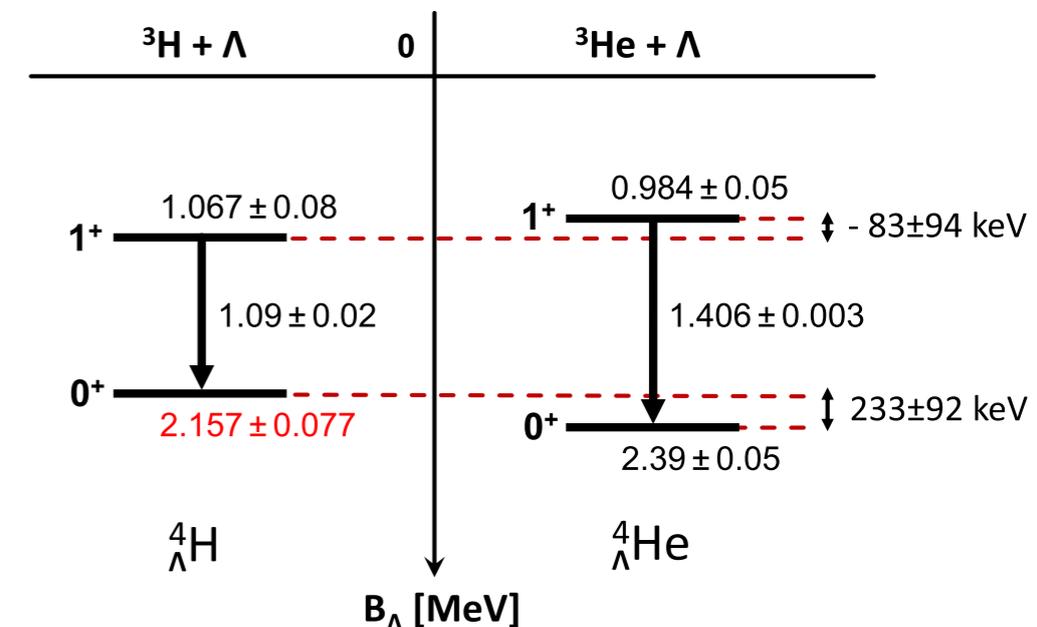
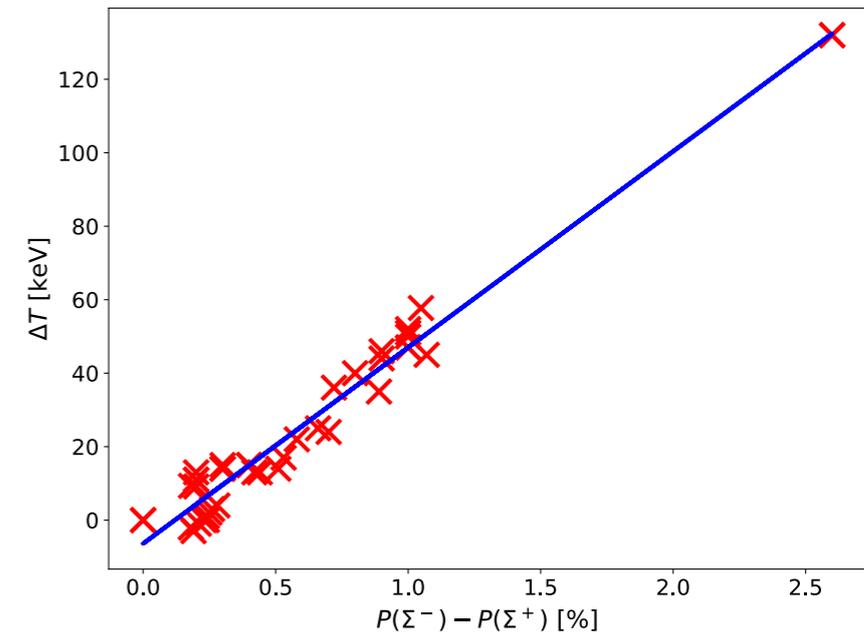
# CSB contributions in ${}^4_{\Lambda}\text{He}$



- perturbative calculations of CSB
- breakdown in kinetic energy, YN and NN interaction
- kinetic energy less important for chiral interactions

interaction	$\langle T \rangle_{\text{CSB}}$	$\langle V_{YN} \rangle_{\text{CSB}}$	$V_{NN}^{\text{CSB}}$	$\Delta E_{\Lambda}^{\text{pert}}$	$\Delta E_{\Lambda}$
NLO13(500)	44	200	16	261	265
NLO13(550)	46	191	20	257	261
NLO13(600)	44	187	20	252	256
NLO13(650)	38	189	18	245	249
NLO19(500)	14	224	5	243	249
NLO19(550)	14	226	7	247	252
NLO19(600)	22	204	12	238	243
NLO19(650)	26	207	12	245	250

interaction	$\langle T \rangle_{\text{CSB}}$	$\langle V_{YN} \rangle_{\text{CSB}}$	$V_{NN}^{\text{CSB}}$	$\Delta E_{\Lambda}^{\text{pert}}$	$\Delta E_{\Lambda}$
NLO13(500)	5	-90	15	-71	-66
NLO13(550)	5	-86	18	-63	-56
NLO13(600)	4	-83	19	-59	-53
NLO13(650)	3	-80	17	-59	-55
NLO19(500)	1	-84	3	-80	-75
NLO19(550)	2	-81	2	-77	-72
NLO19(600)	4	-82	6	-71	-67
NLO19(650)	4	-79	9	-66	-69

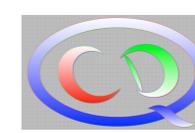


(Schulz et al., 2016; Yamamoto, 2015)

(Haidenbauer et al., 2021)

How model-dependent are predictions for the  $\Lambda n$  scattering length?

# Prediction for $\Lambda n$ scattering



- assuming the current experimental situation for  ${}^4_{\Lambda}\text{He}$  /  ${}^4_{\Lambda}\text{He}$
- **without CSB:**  $a_s^{\Lambda n} \approx 2.9 \text{ fm}$       **with CSB:**  $a_s^{\Lambda n} \approx 3.3 \text{ fm}$
- improved description of  $\Lambda p$  data
- almost independent of cutoff & NLO variant
- CSB of  $a_t^{\Lambda n}$  is smaller

	$a_s^{\Lambda p}$	$a_t^{\Lambda p}$	$a_s^{\Lambda n}$	$a_t^{\Lambda n}$	$\chi^2(\Lambda p)$	$\chi^2(\Sigma N)$	$\chi^2(\text{total})$
NLO13(500)	-2.604	-1.647	-3.267	-1.561	4.47	12.13	16.60
NLO13(550)	-2.586	-1.551	-3.291	-1.469	3.46	12.03	15.49
NLO13(600)	-2.588	-1.573	-3.291	-1.487	3.43	12.38	15.81
NLO13(650)	-2.592	-1.538	-3.271	-1.452	3.70	12.57	16.27
NLO19(500)	-2.649	-1.580	-3.202	-1.467	3.51	14.69	18.20
NLO19(550)	-2.640	-1.524	-3.205	-1.407	3.23	14.19	17.42
NLO19(600)	-2.632	-1.473	-3.227	-1.362	3.45	12.68	16.13
NLO19(650)	-2.620	-1.464	-3.225	-1.365	3.28	12.76	16.04

(Haidenbauer et al., 2021)

**An accurate prediction for the  $\Lambda n$  interaction is possible using hypernuclei!**

- **YN & YY interactions are interesting**
  - *EOS and hyperon puzzle*
  - *access to explicit chiral symmetry breaking*
- **YN & YY interactions not well understood**
  - *conversion processes often drive long range part of interaction*
  - *scarce YN, almost no YY data*
- **Hypernuclei provide important constraints**
  - *$^1S_0$   $\Lambda N$  scattering length &  $^3_{\Lambda}\text{H}$  & impact on other hypernuclei*
  - *$^1S_0$   $\Lambda\Lambda$  scattering length &  $^6_{\Lambda\Lambda}\text{He}$  & predictions for  $A=4,5$*
  - *CSB of  $\Lambda N$  scattering &  $^4_{\Lambda}\text{He}$  /  $^4_{\Lambda}\text{H}$*
- **J-NCSM**
  - *reliable predictions are possible for ranges of interactions for  $S = -1$  and  $-2$*
  - *need SRG induced 3BFs to validate choice of  $\lambda_{YN}$  (see also Wirth et al. (2016))*
  - *estimates of chiral 3BFs are needed (implementing Petschauer et al., (2016))*
  - *study sensitivity to p-wave interaction*
  - *study CSB of p-shell hypernuclei*