



19th International Conference on Hadron Spectroscopy and Structure

LHCb results in charmed baryons

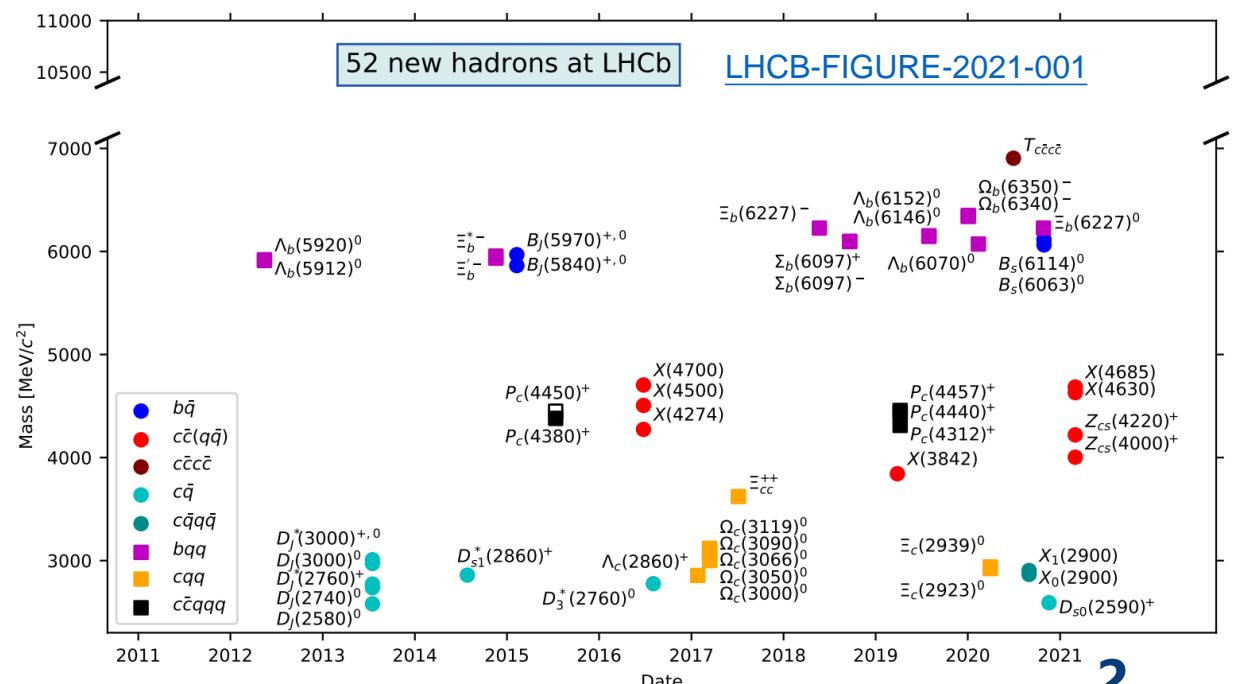
Zhihao Xu

(on behalf of the LHCb collaboration)

Introduction

- LHCb collected the **largest samples** of reconstructed charmed hadrons during LHC Run 1 and Run 2.
 - Providing the **most precise measurements** of properties and production of known charmed baryons.
 - Recent result:
 - **Excited charmed baryons**
 - $\Omega_c^{**0}, \Xi_c^{**0}$
 - **Double charmed baryons**
 - $\Xi_{cc}^+, \Omega_{cc}^+$
 - **Properties**
 - Lifetime
 - Branching fraction

The figure is a scatter plot showing the mass distribution of 52 new hadron species discovered by LHCb. The y-axis represents the mass in MeV/c², ranging from 3000 to 11000. The x-axis represents the mass in MeV/c², ranging from 3000 to 11000. Data points are color-coded according to their quark composition: b-anti-q (blue), c-anti-c(q-anti-q) (red), c-anti-c-anti-c (dark red), c-anti-q (cyan), c-anti-q-anti-q (teal), b-anti-q-anti-q (magenta), and c-anti-q-anti-q-anti-q (orange). The plot includes several labeled resonance peaks: $\Lambda_b(5920)^0$, $\Lambda_b(5912)^0$, Ξ_b^{*-} , Ξ_b' , $B_J(5970)^{+,0}$, $B_J(5840)^{+,0}$, $P_c(4450)^+$, $P_c(4380)^+$, $X(4700)$, $X(4500)$, $X(4274)$, Ξ_{cc}^{++} , $D_s^*(3000)^{+,0}$, $D_s(3000)^0$, $D_s^*(2860)^+$, $D_s(2760)^{+,0}$, $\Lambda_c(2860)^+$, $\Omega_c(3119)^0$, $\Omega_c(3090)^0$, $\Omega_c(3066)^0$, $\Omega_c(3050)^0$, $\Sigma_b(6097)^+$, $\Sigma_b(6097)^-$, $\Xi_b(6227)^-$, $\Lambda_b(6152)^+$, $\Lambda_b(6146)^-$, and $\Xi_c(3221)^-$. A blue box in the upper right corner contains the text "52 new hadrons at LHCb". Below the plot, the text "LHCb-FIGURE" is visible.



LHCb experiment

$$\sigma_{\text{IP}} = 20 \mu\text{m}$$

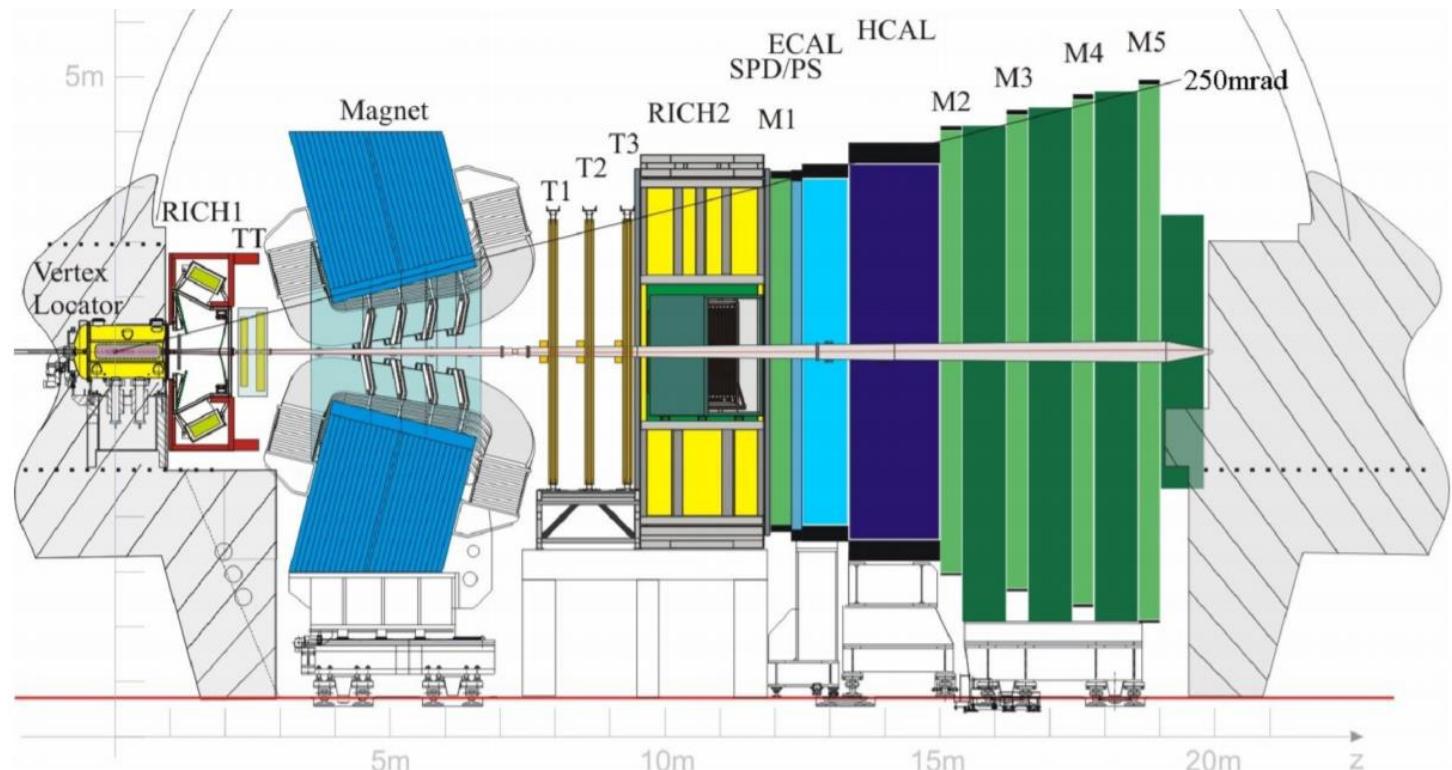
$$\sigma_{\tau} = 45 \text{ fs}$$

$$\sigma_p/p \sim 0.5\% - 1\%$$

$$\sigma_E/E = \frac{10\%}{\sqrt{E}} \pm 1\%$$

$$\epsilon(K \rightarrow K) \sim 95\%$$

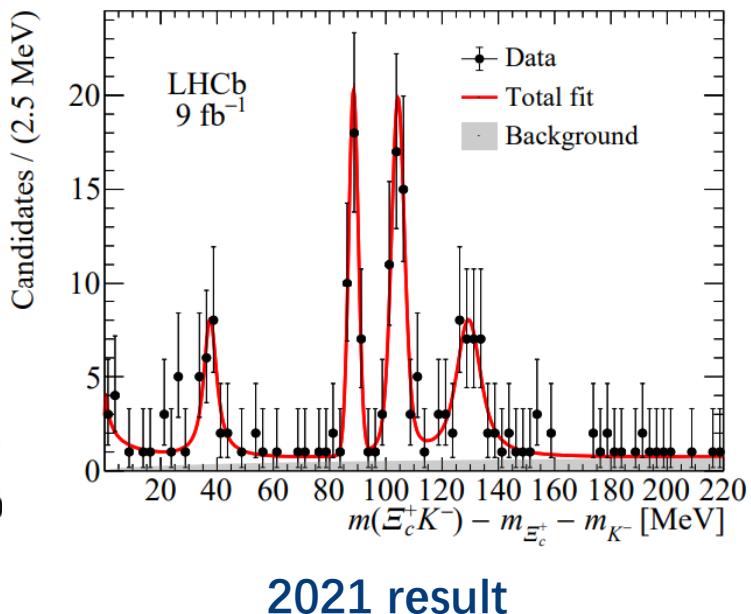
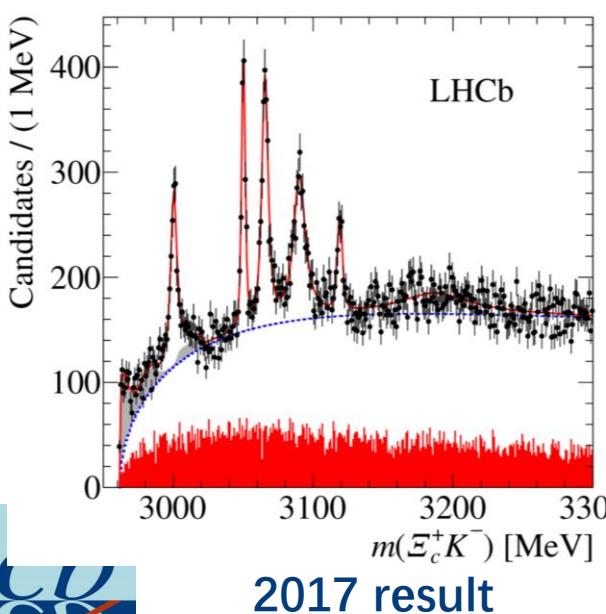
$$\text{Mis-ID } \epsilon(\pi \rightarrow K) \sim 5\%$$



- LHCb designed for study charmed and bottom hadron.
- Excellent vertex, tracking and PID performance.

Excited Ω_c^0

- In 2017, LHCb observed five new excited Ω_c^0 in $m(\Xi_c^+ K^-)$.
[PHYS. REV. LETT. 118 \(2017\) 182001](#)
- In 2021, LHCb observed 4 of them from $\Omega_b^- \rightarrow \Omega_c^0 \pi^-$.
[ARXIV:2107.03419.](#)
FIND MORE DETAILS IN SARA ELIZABETH MITCHELL'S TALK.

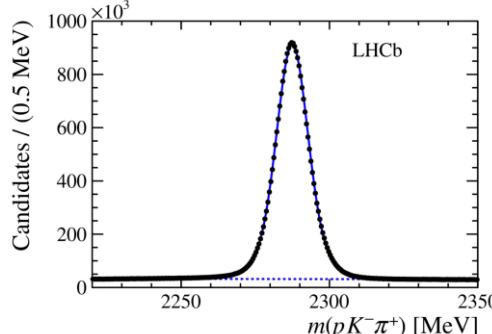
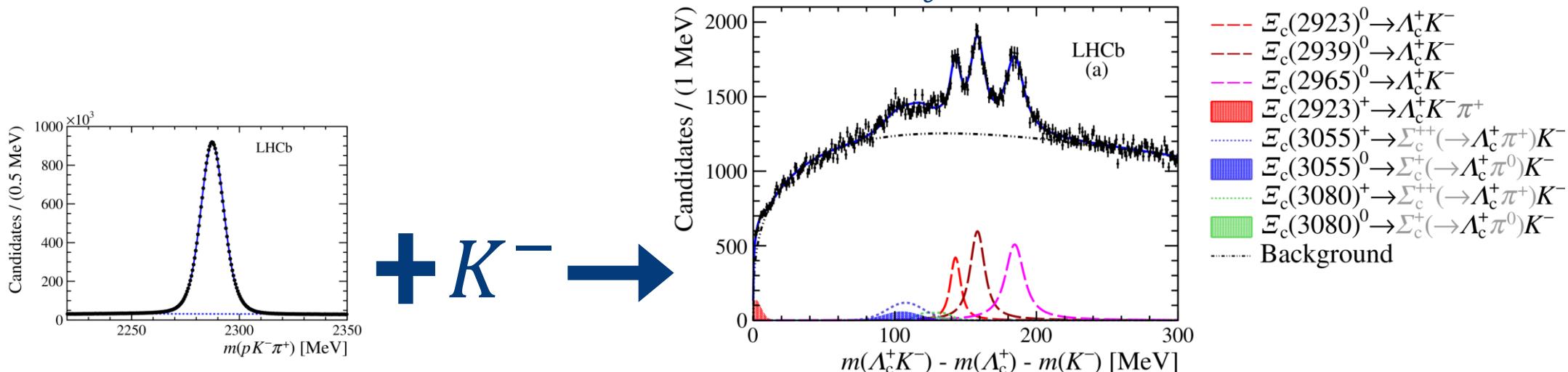


State	Observable	Measurement	
		Stat.	Sys.
Ω_b^-	m \mathcal{R}	$6044.3 \pm 1.2 \pm 1.1^{+0.19}_{-0.22}$ MeV $1.35 \pm 0.11 \pm 0.05$	
Threshold structure	Significance		4.3σ
$\Omega_c(3000)^0$	ΔM m Γ \mathcal{P}	$37.6 \pm 0.9 \pm 0.9$ MeV $2999.2 \pm 0.9 \pm 0.9^{+0.19}_{-0.22}$ MeV $4.8 \pm 2.1 \pm 2.5$ MeV $0.11 \pm 0.02 \pm 0.04$	6.2σ
	J rejection	0.5σ ($J = 1/2$), 0.8σ ($J = 3/2$), 0.4σ ($J = 5/2$)	
$\Omega_c(3050)^0$	ΔM m Γ \mathcal{P}	$88.5 \pm 0.3 \pm 0.2$ MeV $3050.1 \pm 0.3 \pm 0.2^{+0.19}_{-0.22}$ MeV < 1.6 MeV, 95% CL $0.15 \pm 0.02 \pm 0.02$	9.9σ
	J rejection	2.2σ ($J = 1/2$), 0.1σ ($J = 3/2$), 1.2σ ($J = 5/2$)	
$\Omega_c(3065)^0$	ΔM m Γ \mathcal{P}	$104.3 \pm 0.4 \pm 0.4$ MeV $3065.9 \pm 0.4 \pm 0.4^{+0.19}_{-0.22}$ MeV $1.7 \pm 1.0 \pm 0.5$ MeV $0.23 \pm 0.02 \pm 0.02$	11.9σ
	J rejection	3.6σ ($J = 1/2$), 0.6σ ($J = 3/2$), 1.2σ ($J = 5/2$)	
$\Omega_c(3090)^0$	ΔM m Γ \mathcal{P}	$129.4 \pm 1.1 \pm 1.0$ MeV $3091.0 \pm 1.1 \pm 1.0^{+0.19}_{-0.22}$ MeV $7.4 \pm 3.1 \pm 2.8$ MeV $0.19 \pm 0.02 \pm 0.04$	7.8σ
	J rejection	0.3σ ($J = 1/2$), 0.8σ ($J = 3/2$), 0.5σ ($J = 5/2$)	
$\Omega_c(3120)^0$	\mathcal{P}	< 0.03 , 95% CL	

$$\Xi_c^{**0} \rightarrow \Lambda_c^+ K^-$$

PHYS. REV. LETT. 124 (2020) 222001

- Three excited Ξ_c^0 were observed in $m(\Lambda_c^+ K^-)$.
- Using LHCb 2016-2018 data, at 13 TeV and 5.4 fb^{-1} .
- Multivariate method was used in the selection of Λ_c^+ .



$+ K^- \rightarrow$

Resonance	Peak of ΔM [MeV]	Mass [MeV]			Γ [MeV]
		Stat.	Sys.	input	
$\Xi_c(2923)^0$	$142.91 \pm 0.25 \pm 0.20$	$2923.04 \pm 0.25 \pm 0.20 \pm 0.14$			$7.1 \pm 0.8 \pm 1.8$
$\Xi_c(2939)^0$	$158.45 \pm 0.21 \pm 0.17$	$2938.55 \pm 0.21 \pm 0.17 \pm 0.14$			$10.2 \pm 0.8 \pm 1.1$
$\Xi_c(2965)^0$	$184.75 \pm 0.26 \pm 0.14$	$2964.88 \pm 0.26 \pm 0.14 \pm 0.14$			$14.1 \pm 0.9 \pm 1.3$

$$\Xi_c^{**0} \rightarrow \Lambda_c^+ K^-$$

PHYS. REV. LETT. 124 (2020) 222001

- Gell-Mann-Okubo formula for charmed baryons:

$$m(\Omega_c^{**}) - m(\Xi_c^{**}) = m(\Xi_c^{**}) - m(\Sigma_c^{**})$$

- After this analysis, we have:

$$\begin{aligned} & m(\Omega_c^0(3050)) - m(\Xi_c^0(2923)) \\ & \approx m(\Xi_c^0(2923)) - m(\Sigma_c^0(2800)) \approx 125 \text{ MeV} \\ & m(\Omega_c^0(3065)) - m(\Xi_c^0(2939)) \approx 125 \text{ MeV} \\ & m(\Omega_c^0(3090)) - m(\Xi_c^0(2965)) \approx 125 \text{ MeV} \end{aligned}$$

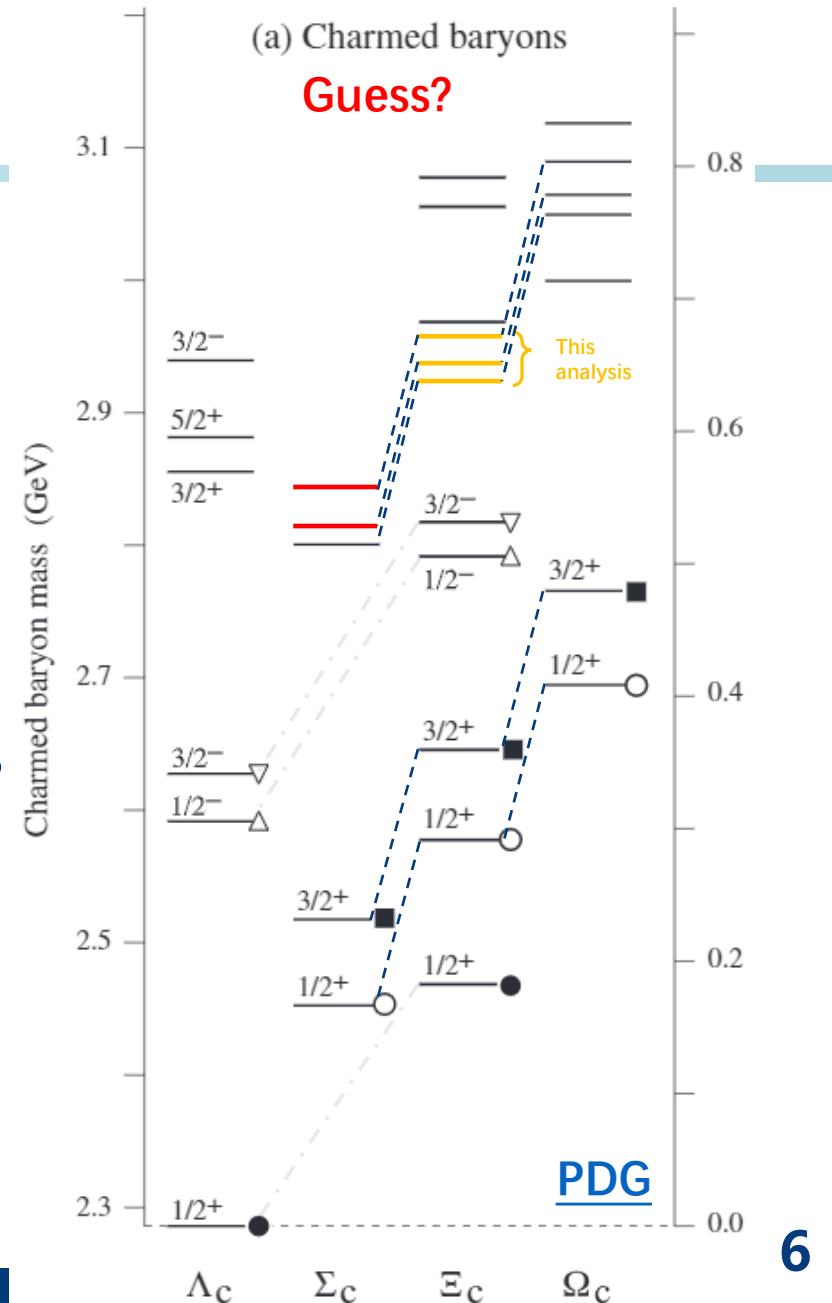
- They should belong to the same flavour multiplets?

If so, their quantum number should be the same.

Spin-parities test should be done to confirm that.

- More topic...

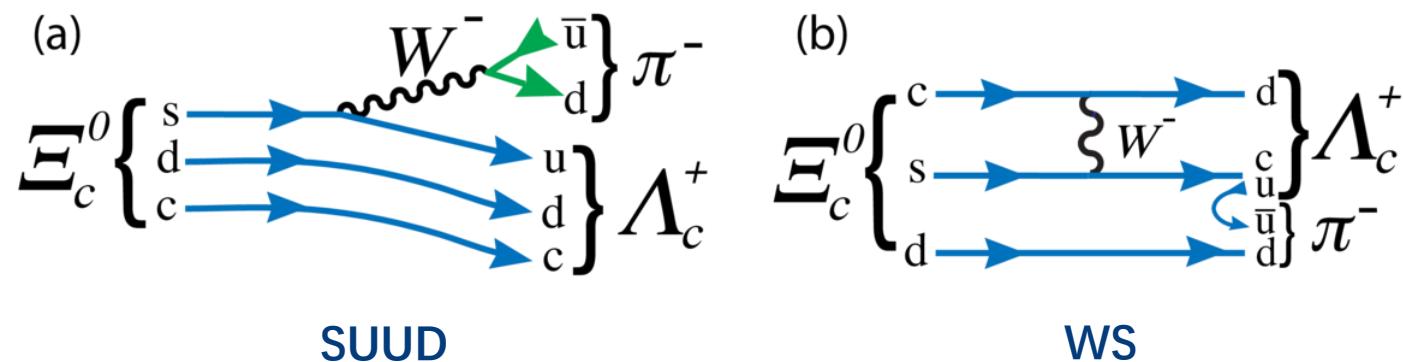
- Dominant decay ($\Xi_c^+ \pi^-$, $\Xi_c'^+ \pi^-$).
- Inner structure (molecular states?).



$\mathcal{B}(\Xi_c^0 \rightarrow \Lambda_c^+ \pi^-)$

PHYS. REV. D102 (2020) 071101(R)

- Usually, Ξ_c^0 decay into the charmless final states by the $c \rightarrow s$ transition. It also can decay in to $\Lambda_c^+ \pi^-$ by $cs \rightarrow dc$ weak scattering.
- For this decay, there are two amplitudes (SUUD and WS), and their interference can be positive or negative.



$$\mathcal{B}(\Xi_c^0 \rightarrow \Lambda_c^+ \pi^-)$$

PHYS. REV. D102 (2020) 071101(R)

- Firstly measured the $\mathcal{B}(\Xi_c^0 \rightarrow \Lambda_c^+ \pi^-)$ in 2017-2018 LHCb data.
 - This branching fraction was determined by two observables:

$$\mathcal{R}_1 \equiv \frac{N(\Xi_c^0)}{N(\Lambda_c^+)} = \frac{f_{\Xi_c^0}}{f_{\Lambda_c^+}} \mathcal{B}(\Xi_c^0 \rightarrow \Lambda_c^+ \pi^-)$$

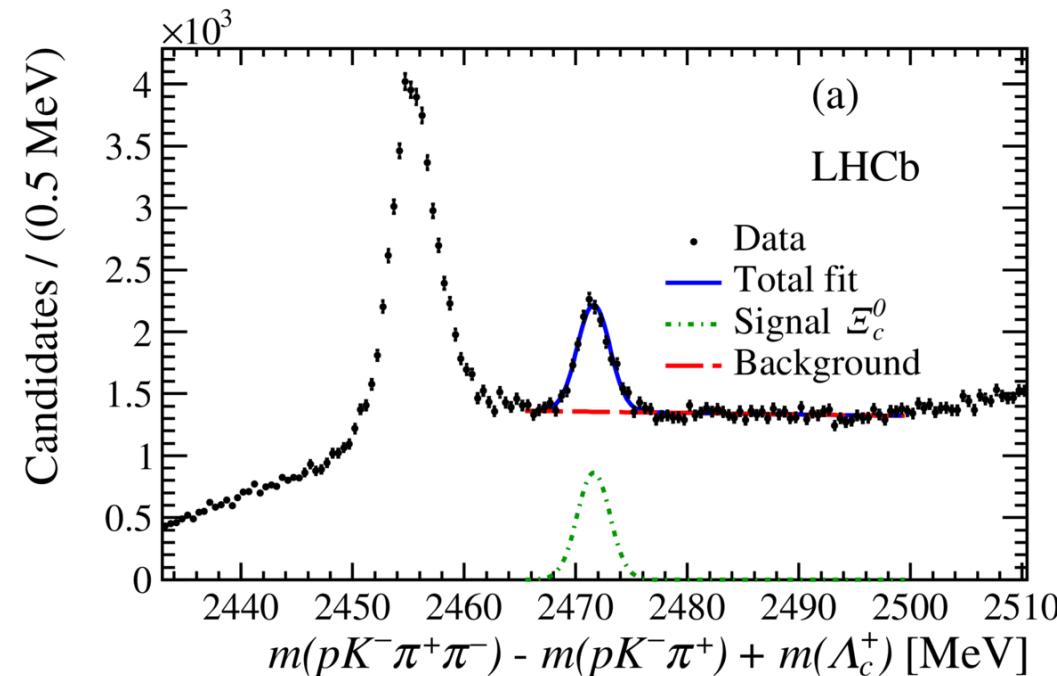
And

[derivation]

$$\mathcal{R}_2 \equiv \frac{N(\Xi_c^0)}{N(\Xi_c^+)} = \frac{f_{\Xi_c^0}}{f_{\Xi_c^+}} \cdot \frac{\mathcal{B}(\Lambda_c^+ \rightarrow p K^- \pi^+)}{\mathcal{B}(\Xi_c^+ \rightarrow p K^- \pi^+)} \cdot \mathcal{B}(\Xi_c^0 \rightarrow \Lambda_c^+ \pi^-)$$

- The result of these observables:
 $\mathcal{R}_1 = (0.095 \pm 0.003 \pm 0.012)\%$
 $\mathcal{R}_2 = (5.70 \pm 0.19 \pm 0.07)\%$
 - Then the branching fraction can be calculate:

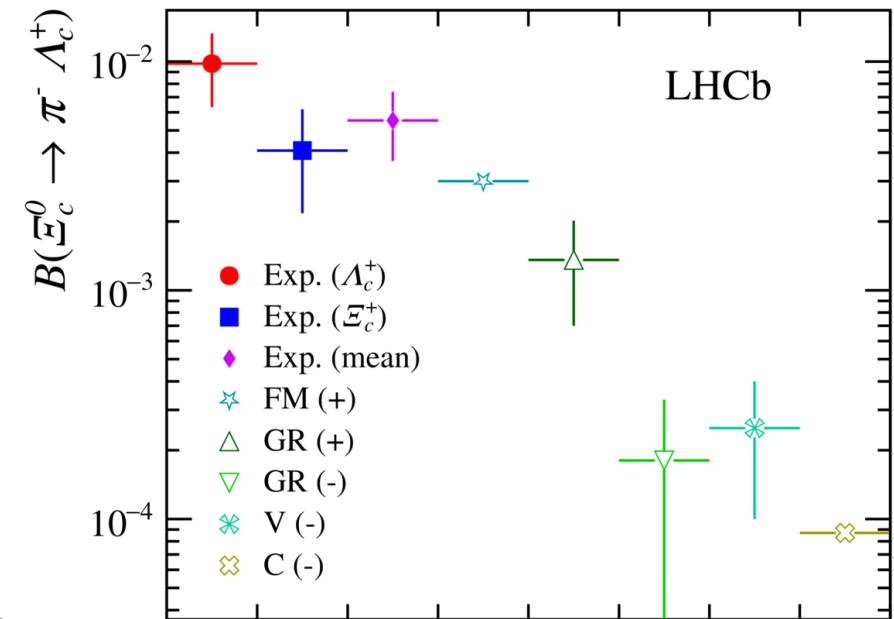
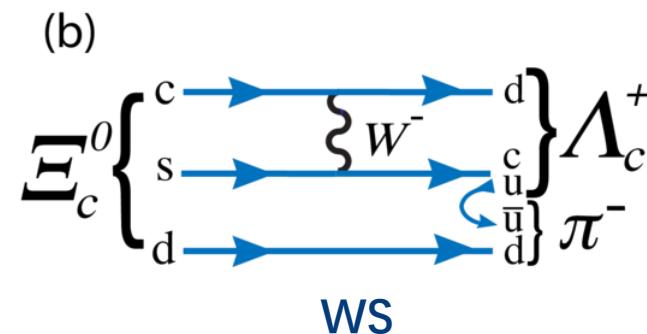
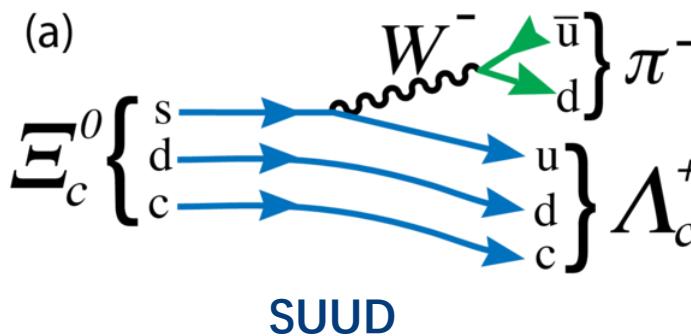
$$\mathcal{B}(\Xi_c^0 \rightarrow \Lambda_c^+ \pi^-) = (0.55 \pm 0.02 \pm 0.18)\%$$



$\mathcal{B}(\Xi_c^0 \rightarrow \Lambda_c^+ \pi^-)$

PHYS. REV. D102 (2020) 071101(R)

- Interference between SUUD and WS can be obtained from this measurement.
- This result is in agreement with the positive assuming.



Lifetimes of charmed baryons

- The expected lifetime of single charmed baryons hierarchy should be:

$$\tau_{\Xi_c^+} > \tau_{\Lambda_c^+} > \tau_{\Xi_c^0} > \tau_{\Omega_c^0}$$

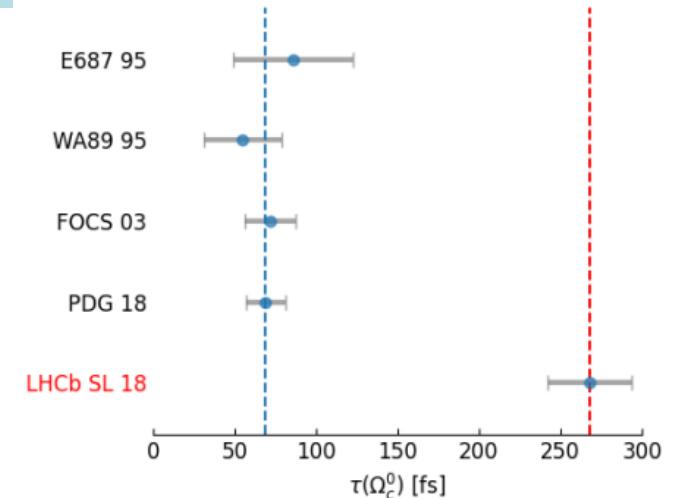
[Frontiers of Physics 10.6 \(2015\): 101406.](#)

[International Journal of Modern Physics A 30.10 \(2015\): 1543005.](#)

Or

$$\tau_{\Xi_c^+} > \tau_{\Omega_c^0} > \tau_{\Lambda_c^+} > \tau_{\Xi_c^0}$$

[JHEP 11\(2018\)014](#)



- Measurement results before 2018:

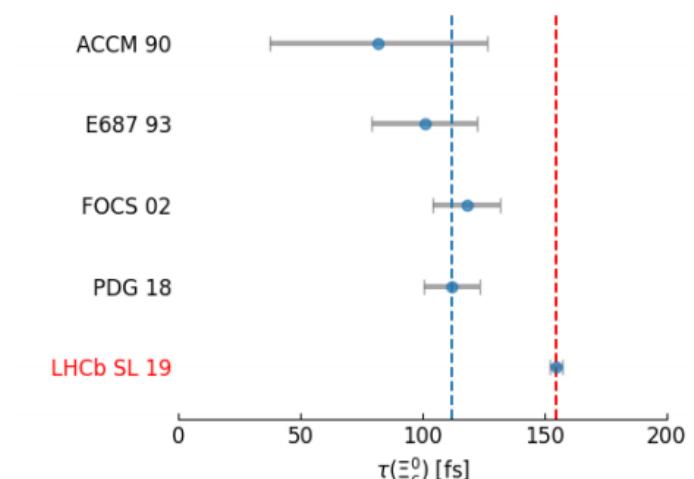
$$\tau_{\Xi_c^+} > \tau_{\Lambda_c^+} > \tau_{\Xi_c^0} > \tau_{\Omega_c^0}$$

- LHCb Run-1 result with signals from semi-leptonic beauty-hadron decays:

$$\tau_{\Xi_c^+} > \tau_{\Omega_c^0} > \tau_{\Lambda_c^+} > \tau_{\Xi_c^0}$$

[PHYS. REV. LETT. 121 \(2018\) 092003](#)

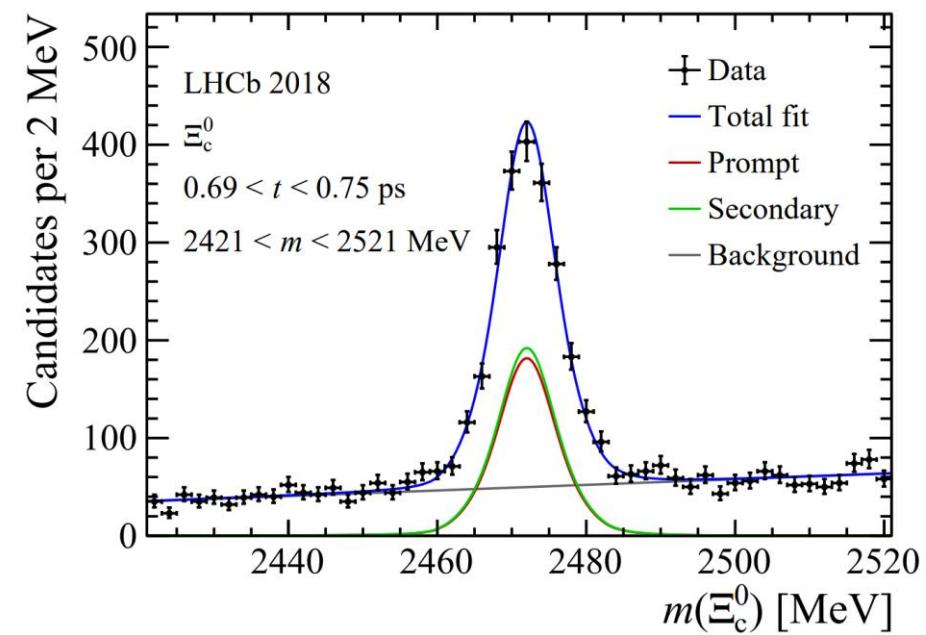
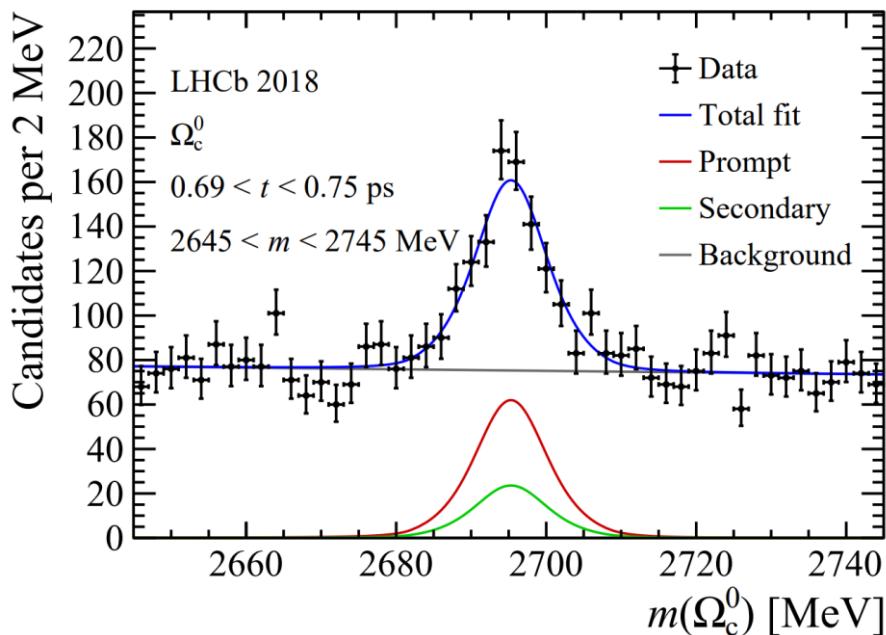
[PHYS. REV. D100 \(2019\) 032001](#)



Lifetimes of Ω_c^0 and Ξ_c^0

PAPER-2021-021 (IN PREPARATION)

- The lifetimes of Ω_c^0 and Ξ_c^0 baryons is measured in 2016-2018 data.
- Both Ω_c^0 and Ξ_c^0 were reconstructed in the $pK^-K^-\pi^+$ final states.

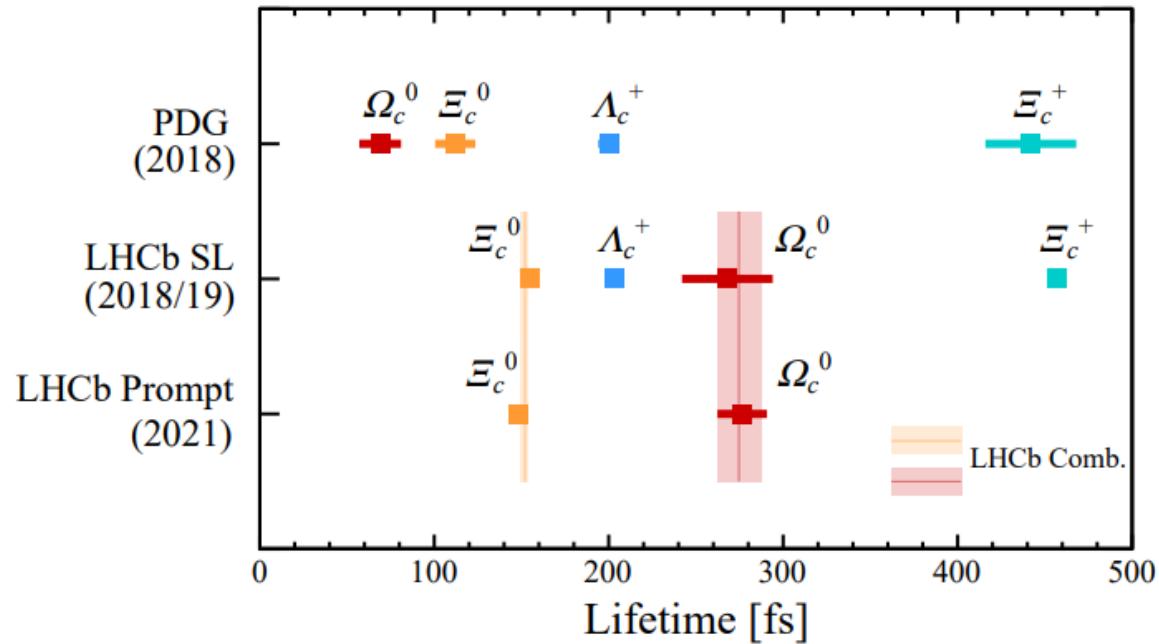
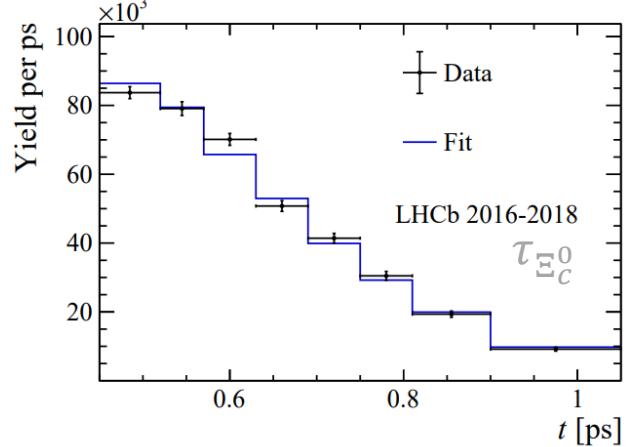
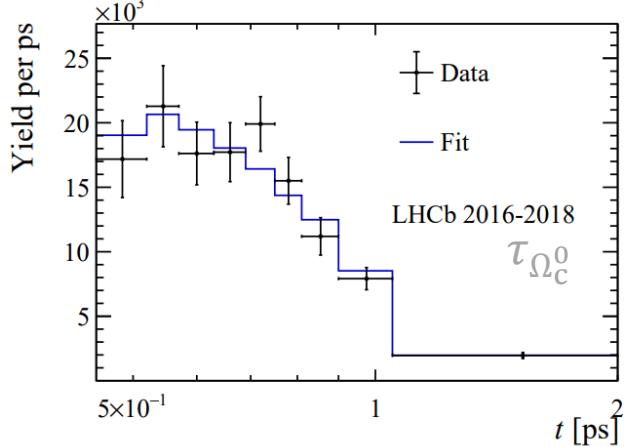


Prompt: candidates from pp interaction point.
Secondary: candidates from b -hadron decay.

New

Lifetimes of Ω_c^0 and Ξ_c^0

PAPER-2021-021 (IN PREPARATION)



- Results from this analysis:

$$\begin{aligned}\tau_{\Omega_c^0} &= (276.5 \pm 13.4 \pm 4.3 \pm 0.7) \text{ fs} \\ \tau_{\Xi_c^0} &= (148.0 \pm 2.3 \pm 2.2 \pm 0.2) \text{ fs}\end{aligned}$$

- Combine with previous results:

[PHYS. REV. LETT. 121 \(2018\) 092003](#)
[PHYS. REV. D100 \(2019\) 032001](#)

$$\begin{aligned}\tau_{\Omega_c^0} &= (274.6 \pm 12.4) \text{ fs} \\ \tau_{\Xi_c^0} &= (152.0 \pm 2.0) \text{ fs}\end{aligned}$$

Doubly charmed baryons

- Doubly charmed baryons were predicted by $SU(4)$ multiplet. Ξ_{cc}^{++} (ucc), Ξ_{cc}^+ (dcc), Ω_{cc}^+ (scc).

- A lot of Ξ_{cc}^{++} study done by LHCb:

- Mass

$$m(\Xi_{cc}^{++}) = 3621.55 \pm 0.23 \pm 0.30 \text{ MeV}/c^2$$

[JHEP 02 \(2020\) 049](#)

- Lifetime

$$\tau(\Xi_{cc}^{++}) = 0.256^{+0.024}_{-0.022} \pm 0.014 \text{ ps}$$

[PRL 121 \(2018\) 052002](#)

- Production

$$\frac{\sigma(\Xi_{cc}^{++}) \times \mathcal{B}(\Xi_{cc}^{++} \rightarrow \Lambda_c^+ K^- \pi^+ \pi^+)}{\sigma(\Lambda_c^+)}$$

$$= 2.22 \pm 0.27 \pm 0.29$$

[CPC44 \(2020\) 022001](#)

- Branching fraction

$$\Xi_{cc}^{++} \rightarrow \Xi_c^+ \pi^+$$

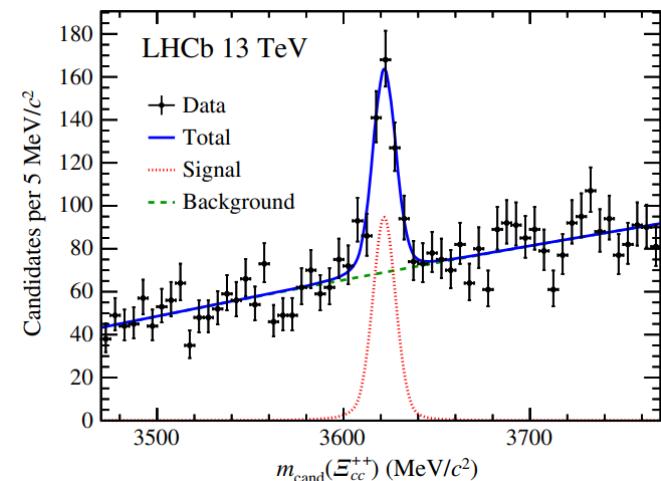
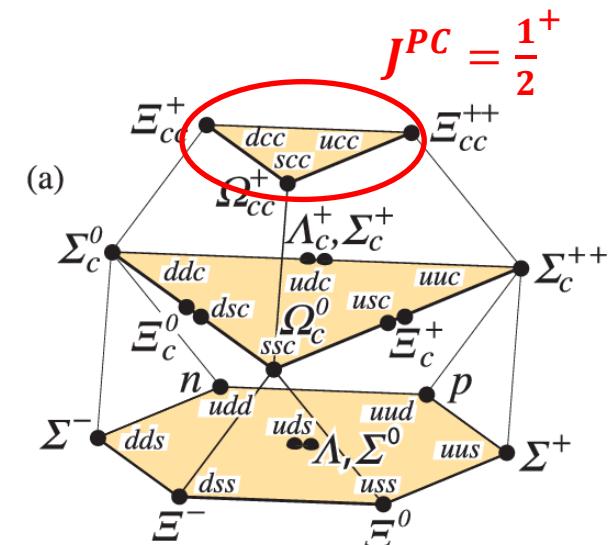
$$\frac{\mathcal{B}(\Xi_{cc}^{++} \rightarrow \Xi_c^+ \pi^+) \times \mathcal{B}(\Xi_c^+ \rightarrow p K^- \pi^+)}{\mathcal{B}(\Xi_{cc}^{++} \rightarrow \Lambda_c^+ K^- \pi^+ \pi^+) \times \mathcal{B}(\Lambda_c^+ \rightarrow p K^- \pi^+)} = 0.035 \pm 0.009 \pm 0.003$$

[PRL 121 \(2018\) 162002](#)

$$\Xi_{cc}^{++} \rightarrow D^+ p K^- \pi^+$$

$$\frac{\mathcal{B}(\Xi_{cc}^{++} \rightarrow D^+ p K^- \pi^+)}{\mathcal{B}(\Xi_{cc}^{++} \rightarrow \Lambda_c^+ K^- \pi^+ \pi^+)} < 1.7$$

[JHEP 10 \(2019\) 124](#)



First observation in $m(\Lambda_c^+ K^- \pi^+ \pi^+)$
[PRL 119 \(2017\) 112001](#)

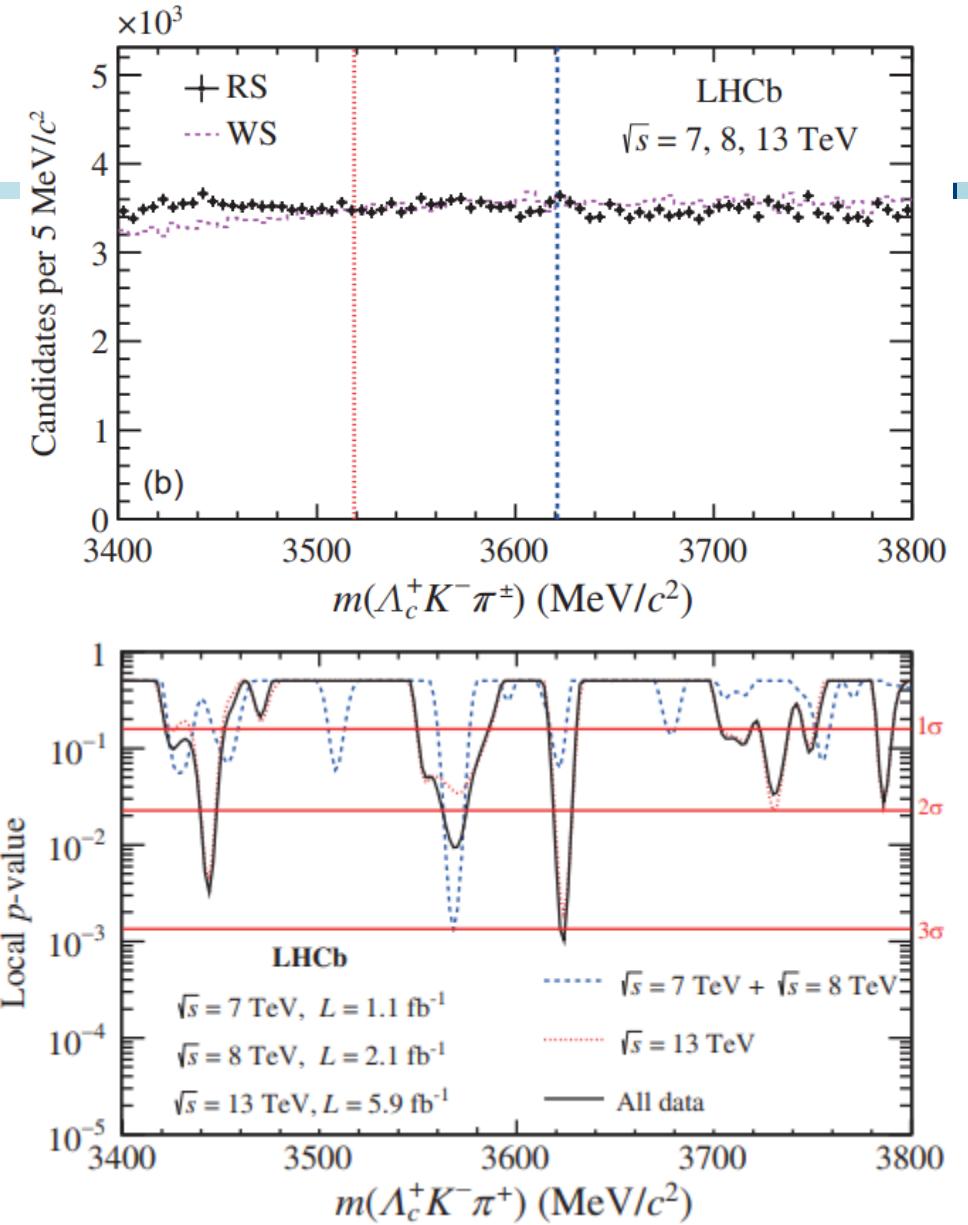
$$\Xi_{cc}^+ \rightarrow \Lambda_c^+ K^- \pi^+$$

SCPMA 63 (2020) 221062

- Search for Ξ_{cc}^+ in $\Lambda_c^+ K^- \pi^+$ final states.
- Using all LHCb data, 9 fb^{-1} .
- No significant signal was observed.
- Local (global) significance is 2.7σ (1.7σ)
- Upper limit of $\mathcal{R}(\Lambda_c^+/\Xi_{cc}^{++})$ were set at 95% CL.

$$\mathcal{R}(\Lambda_c^+) \equiv \frac{\sigma(\Xi_{cc}^+) \times \mathcal{B}(\Xi_{cc}^+ \rightarrow \Lambda_c^+ K^- \pi^+)}{\sigma(\Lambda_c^+)}$$

$$\mathcal{R}(\Xi_{cc}^{++}) \equiv \frac{\sigma(\Xi_{cc}^+) \times \mathcal{B}(\Xi_{cc}^+ \rightarrow \Lambda_c^+ K^- \pi^+)}{\sigma(\Xi_{cc}^{++}) \times \mathcal{B}(\Xi_{cc}^{++} \rightarrow \Lambda_c^+ K^- \pi^+ \pi^+)}$$

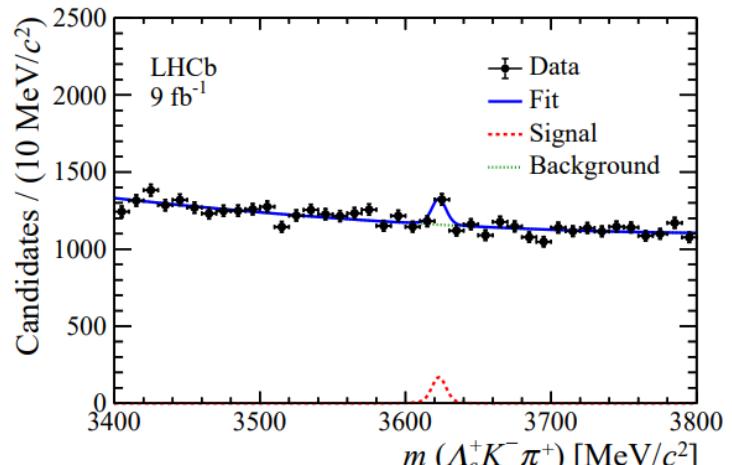
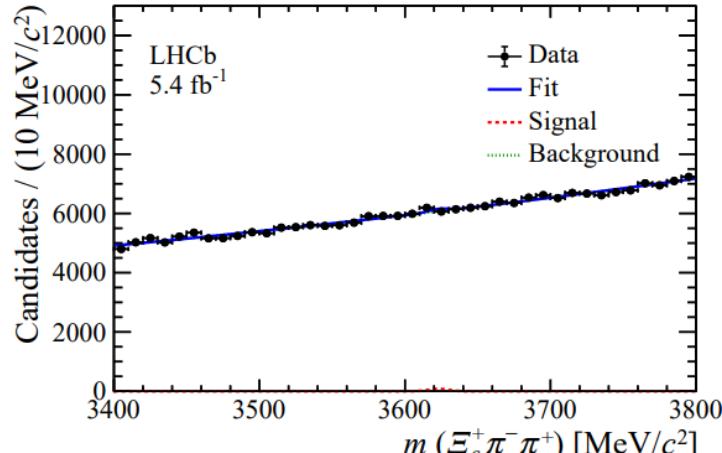
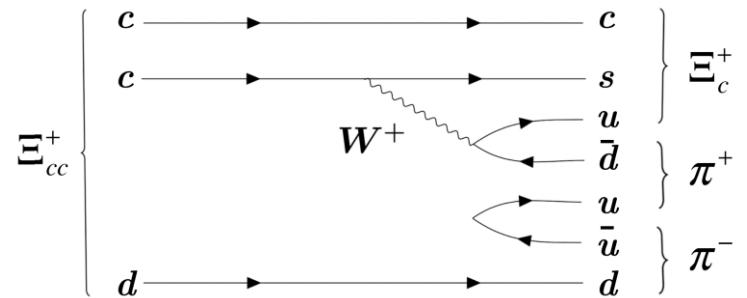


New

Search for Ξ_{cc}^+ in $\Xi_c^+\pi^-\pi^+$

PAPER-2021-019 (IN PREPARATION)

- Search for Ξ_{cc}^+ in $\Xi_c^+\pi^-\pi^+$ final states.
- Using LHCb 2016-2018 data, at 13 TeV and 5.4 fb^{-1} .
- No significant signal. Local significance is 2.3σ
- Combine with $\Xi_{cc}^+ \rightarrow \Lambda_c^+ K^- \pi^+$ result. [SCPMA 63 \(2020\) 221062](#)



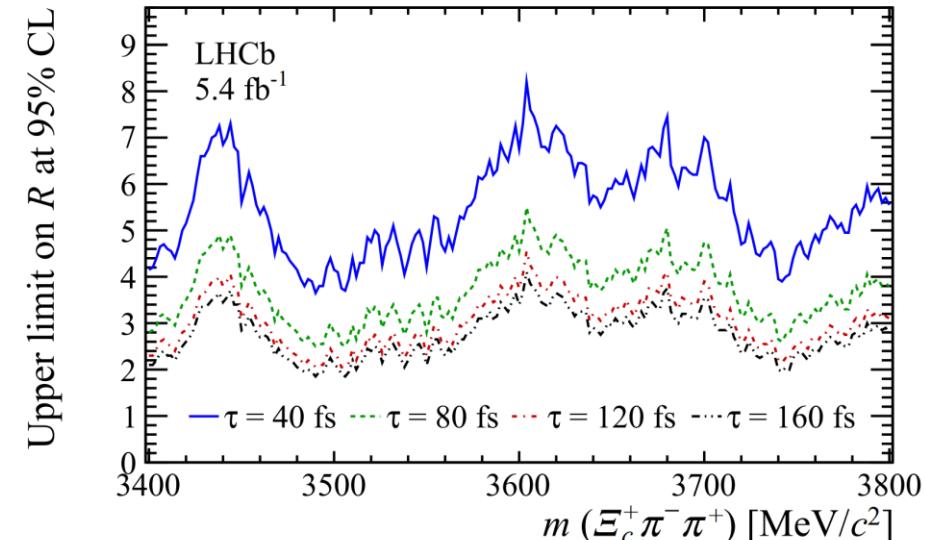
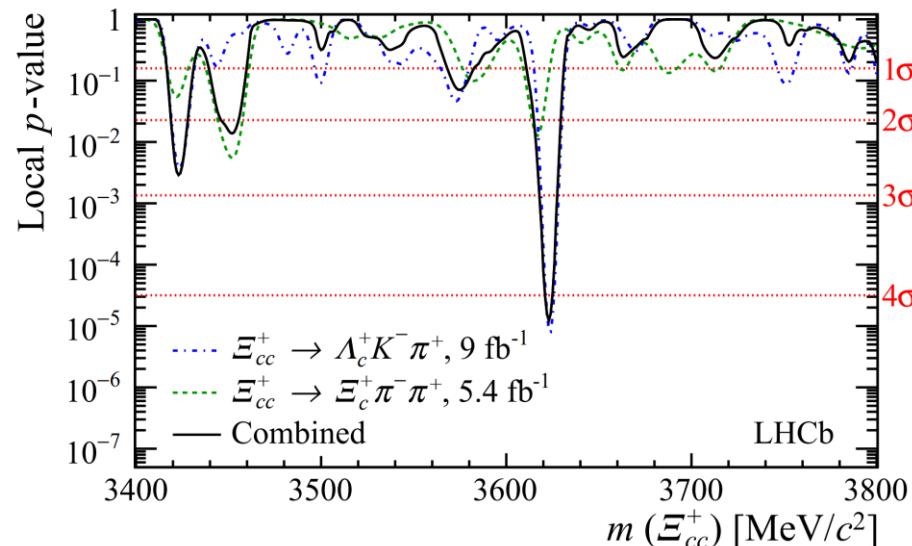
New

Search for Ξ_{cc}^+ in $\Xi_c^+\pi^-\pi^+$

PAPER-2021-019 (IN PREPARATION)

- Combined local (global) significance 4.0σ (2.9σ). Best fit found around 3623.0 MeV.
- Upper limit scan done in $3.4 - 3.8$ GeV on R for different lifetime hypotheses at 95% CL.

$$R = \frac{\sigma(\Xi_{cc}^+) \times \mathcal{B}(\Xi_{cc}^+ \rightarrow \Xi_c^+\pi^-\pi^+)}{\sigma(\Xi_{cc}^{++}) \times \mathcal{B}(\Xi_{cc}^{++} \rightarrow \Xi_c^+\pi^+)}$$

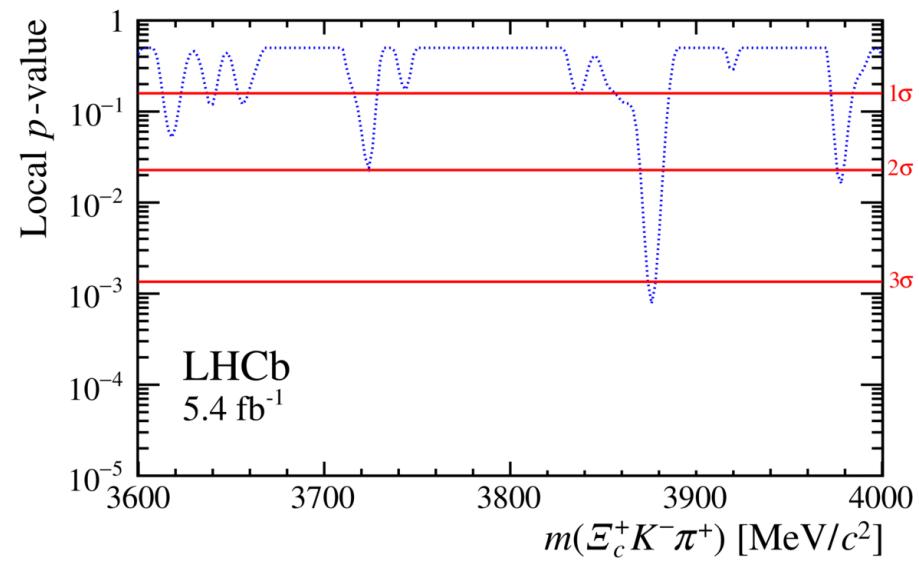
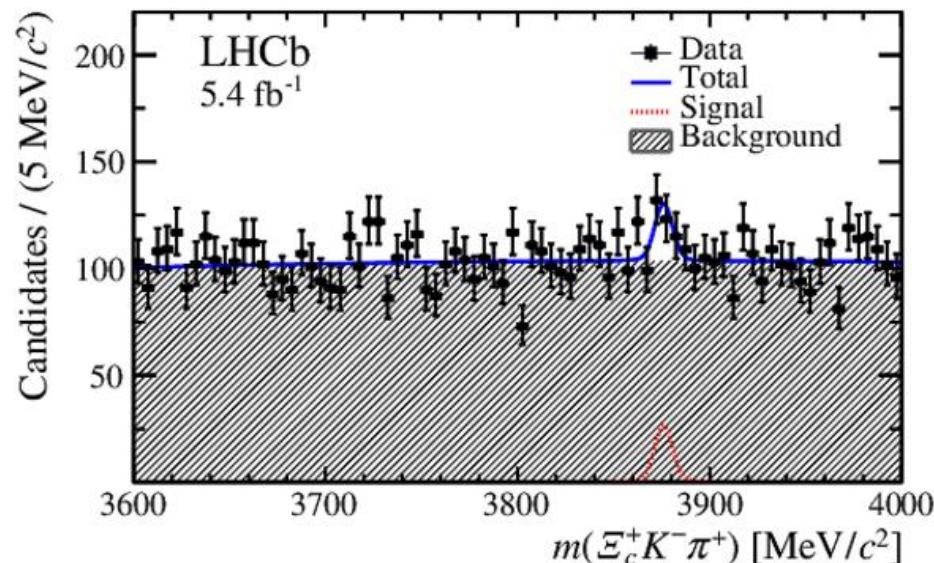
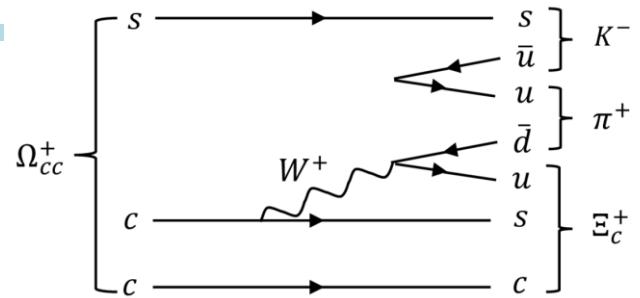


New

Search for Ω_{cc}^+ in $\Xi_c^+ K^- \pi^+$

[ARXIV:2105.06841](#)

- First searching for Ω_{cc}^+ in $\Xi_c^+ K^- \pi^+$ final states.
- Using LHCb 2016-2018 data, at 13 TeV and 5.4 fb^{-1} .
- 3.2σ (1.8σ) for local (global) significance, the largest local significance found around 3876.1 MeV.

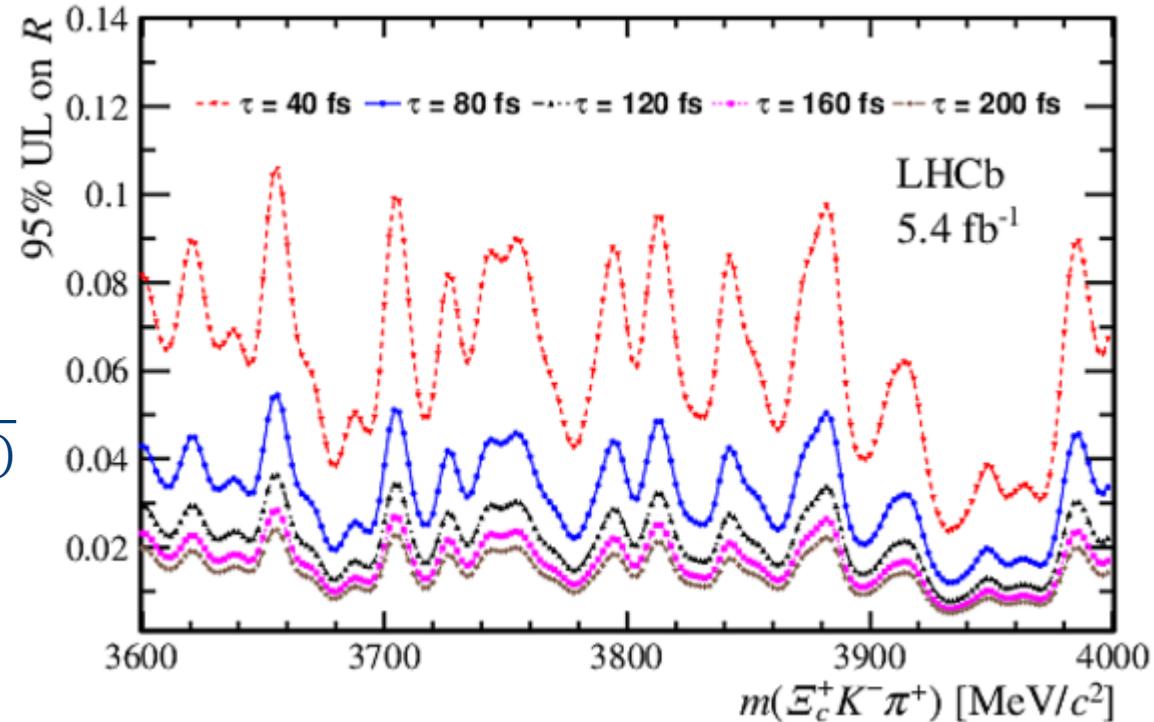


Search for Ω_{cc}^+ in $\Xi_c^+ K^- \pi^+$

[ARXIV:2105.06841](https://arxiv.org/abs/2105.06841)

- Global significance $< 3\sigma$
- Upper limit scan done in 3.6 – 4.0 GeV on R for different lifetime hypotheses at 95% CL.

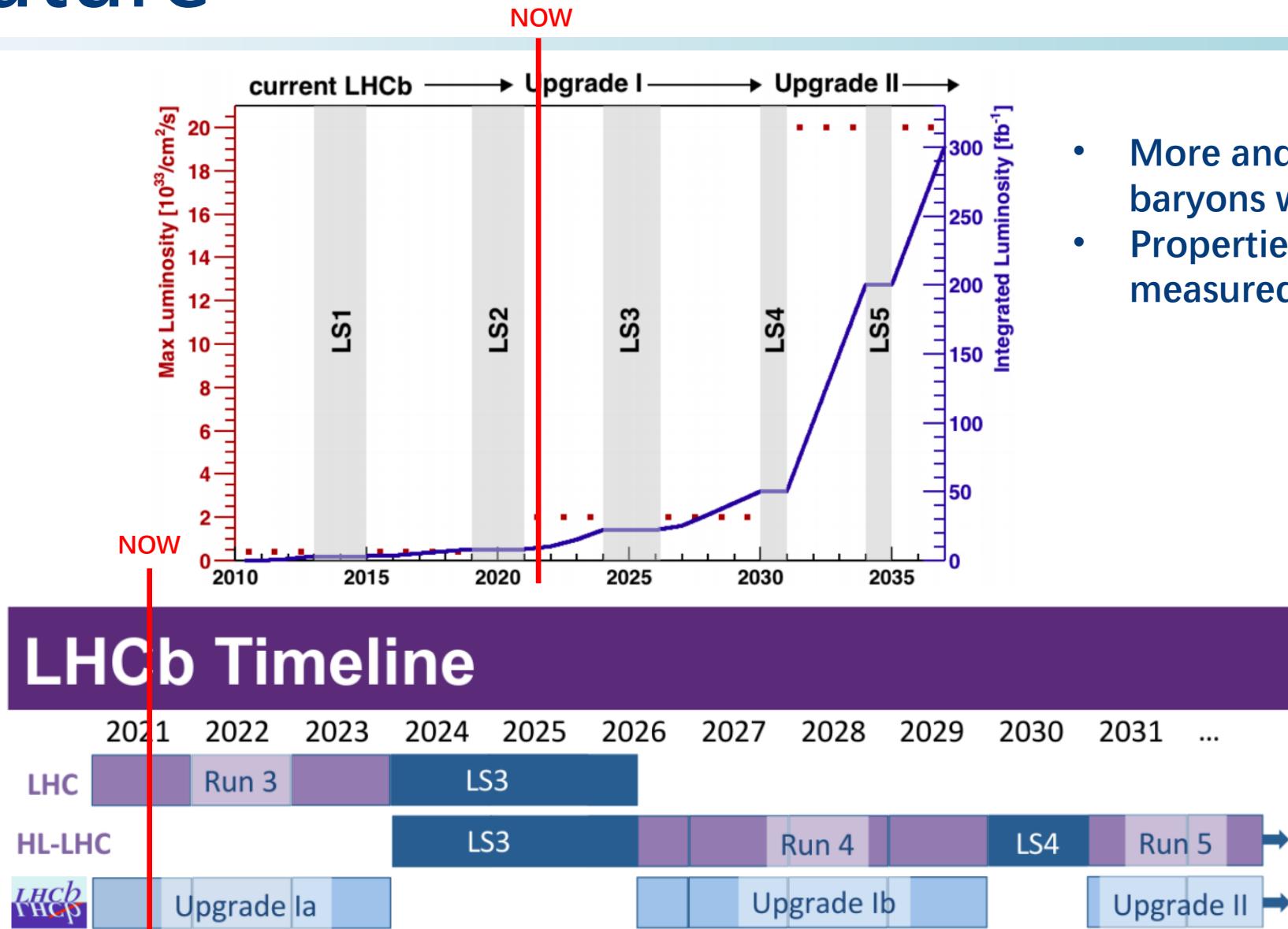
$$R = \frac{\sigma(\Omega_{cc}^+) \times \mathcal{B}(\Omega_{cc}^+ \rightarrow \Xi_c^+ K^- \pi^+) \times \mathcal{B}(\Xi_c^+ \rightarrow p K^- \pi^+)}{\sigma(\Xi_{cc}^{++}) \times \mathcal{B}(\Xi_{cc}^{++} \rightarrow \Lambda_c^+ K^- \pi^+ \pi^+) \times \mathcal{B}(\Lambda_c^+ \rightarrow p K^- \pi^+)}$$



Summary

- Charmed baryons
 - Observation of excited Ω_c^0 baryons
 - Observation of excited Ξ_c^0 baryons More states to be found...
 - First branching fraction measurement of the $\Xi_c^0 \rightarrow \Lambda_c^+ \pi^-$
 - Lifetime measurement of Ω_c^0 and Ξ_c^0 baryons More precise measurement to be done...
- Double charmed baryons
 - Search for the doubly charmed baryon Ω_{cc}^+
 - Search for the doubly charmed baryon Ξ_{cc}^+ More events to be accumulate...

Future



- More and more charmed baryons will be found.
- Properties will be measured more precisely.

Thanks!

Lifetime of Ω_c^0 and Ξ_c^0 New

PAPER-2021-021 (IN PREPARATION)

- The lifetimes of the Ω_c^0 and Ξ_c^0 baryons are determined from a binned χ^2 fit to the data collected in 2016–2018, which is constructed as:

$$\chi^2(\tau, \vec{C}) = \sum_{\text{year}} \sum_i \frac{\left(N_{i,\text{year}}^{\text{sig}} - C_{\text{year}} \times F_i(\tau) \times \frac{N_{i,\text{year}}^{\text{con}}}{M_{i,\text{year}}^{\text{con}}} \times M_{i,\text{year}}^{\text{sig}} \right)^2}{\sigma_{N_{i,\text{year}}^{\text{sig}}}^2 + C_{\text{year}}^2 \times F_i^2(\tau) \times \sigma_{\left(\frac{N_{i,\text{year}}^{\text{con}}}{M_{i,\text{year}}^{\text{con}}} \times M_{i,\text{year}}^{\text{sig}} \right)}^2},$$

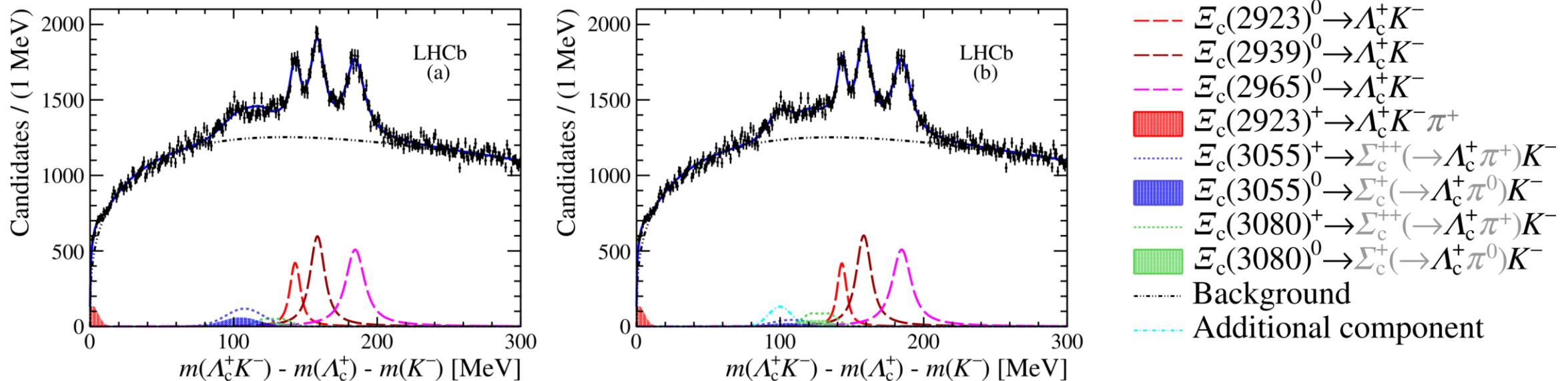
$$F_i(\tau) = \frac{\int_i \exp(-t/\tau) dt}{\int_i \exp(-t/\tau_{\text{sim}}) dt} / \frac{\int_i \exp(-t/\tau^{\text{con}}) dt}{\int_i \exp(-t/\tau_{\text{sim}}^{\text{con}}) dt}$$

where $N_{i,\text{year}}^{\text{sig}}$ ($N_{i,\text{year}}^{\text{con}}$) is the signal yield in data for the signal (control) mode in decay-time bin i and for each year, M is the effective yield predicted from simulation. $F_i(\tau)$ aim to account for the difference in lifetime between the data and the simulated samples and C is a normalisation factor for this term. σ is the uncertainty of the relevant quantity.

$$\Xi_c^{**0} \rightarrow \Lambda_c^+ K^-$$

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- Alternative fit with one additional components which need to be explain.



- More data are required to understanding this structure.

Derivation of \mathcal{R}_1

$$\mathcal{B}(\Xi_c^0 \rightarrow \pi^- \Lambda_c^+) = N(\Xi_c^0 \rightarrow \pi^- \Lambda_c^+)/N(\Xi_c^0)$$

$$N(\Xi_c^0) = \frac{f_{\Xi_c^0}}{f_{\Lambda_c^+}} \cdot N(\Lambda_c^+).$$

$$\frac{f_{\Xi_c^0}}{f_{\Lambda_c^+}} = \mathcal{C} \cdot \frac{f_{\Xi_b^-}}{f_{\Lambda_b^0}},$$

$$\mathcal{B}(\Xi_c^0 \rightarrow \pi^- \Lambda_c^+) = \underbrace{\frac{N(\Xi_c^0 \rightarrow \pi^- (\Lambda_c^+ \rightarrow pK^-\pi^+))}{N(\Lambda_c^+ \rightarrow pK^-\pi^+)}}_{\mathcal{R}_1:} \cdot \underbrace{\frac{1}{\mathcal{C}} \cdot \frac{f_{\Lambda_b^0}}{f_{\Xi_b^-}}}_{\text{Known}}.$$

Derivation of \mathcal{R}_2

$$\mathcal{B}(\Xi_c^0 \rightarrow \pi^- \Lambda_c^+) = N(\Xi_c^0 \rightarrow \pi^- \Lambda_c^+)/N(\Xi_c^0)$$

$$N(\Xi_c^0) = \frac{f_{\Xi_c^0}}{f_{\Xi_c^+}} \cdot N(\Xi_c^+)$$

$$\frac{f_{\Xi_c^0}}{f_{\Xi_c^+}} \approx 1$$

$$\mathcal{B}(\Xi_c^0 \rightarrow \pi^- \Lambda_c^+) = N(\Xi_c^0 \rightarrow \pi^- \Lambda_c^+)/N(\Xi_c^+).$$

$$\mathcal{B}(\Xi_c^0 \rightarrow \pi^- \Lambda_c^+) = \underbrace{\frac{N(\Xi_c^0 \rightarrow \pi^- (\Lambda_c^+ \rightarrow pK^-\pi^+))}{N(\Xi_c^+ \rightarrow pK^-\pi^+)}}_{\mathcal{R}_2:} \cdot \frac{\mathcal{B}(\Xi_c^+ \rightarrow pK^-\pi^+)}{\mathcal{B}(\Lambda_c^+ \rightarrow pK^-\pi^+)}.$$

$$\mathcal{B}(\Xi_c^+ \rightarrow pK^-\pi^+) = \underbrace{\frac{N(\Xi_c^+ \rightarrow pK^-\pi^+)}{N(\Lambda_c^+ \rightarrow pK^-\pi^+)}}_{\text{Can be measured}} \cdot \underbrace{\frac{1}{\mathcal{C}} \cdot \frac{f_{\Lambda_b^0}}{f_{\Xi_b^-}} \cdot \mathcal{B}(\Lambda_c^+ \rightarrow pK^-\pi^+)}_{\text{Known}},$$

$\mathcal{R}_2:$

