# Three flavor Excluded-volume model for Quarkyonic matter

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Hadrons in hot and nuclear environment including hypernuclei-3





### Outline

- Motivation
- Quarkyonic Matter
  - Excluded Volume Model
- Final Remarks

QCD under extreme conditions (temperature and finite density) plays an important role in understanding the transitions that took place in the early universe.





Observation and analysis of GW170817: Important clues to understand cold and dense matter.

 The structure of a neutron star (NS) is determined by the Tolman-Oppenheimer-Volkoff Equation (TOV).



Description of Equation of State (EoS) of dense QCD matter:

- Around saturation density: Nuclear experiments.
- Very high density limit: Asymptotic freedom allows perturbative calculation.



TOV and EoS can give some insight about the transition quark-nucleon matter.



EoS should be hard enough to support  $2M_{\odot}$ and soft enough to satisfy  $R_{14} \leq 13.5$  km.

This is also reflected in sound velocity, that should increase rapidly and can be greater then its conformal value  $c_s^2 \ge 1/3$ .

Any suggestions?



F. J. Fattoyev et. al, PRL 120, 172702 (2018)

Phase of dense matter, argued from large Nc approximation and model computations.



Gluon loop  $\rightarrow g^2 N_c T^2 \sim T^{2}$ →Dynamics not affected by quarks;

→Debye screening at large distances.

#### Quark loop

→~  $\mu_0^2 g^2$  ⇒ Supressed by  $1/N_c$  at large  $N_c$ . +High density limit:  $\mu_0 \gg \Lambda_{\text{OCD}}$ , so quarks are important when  $\mu_O \sim N_c^{1/2} \Lambda_{\text{OCD.}}$ •Debye screen mass  $m_D \simeq g \mu_O$ 



### • For $k_F^B < \Lambda_{\rm QCD}$ : Quarks confined in nucleons.

Nuclear  $\longrightarrow$  Quarkyonic (at few times  $\rho_0$ ) Nucleons Quarks

- For  $k_F^B < \Lambda_{\rm QCD}$ : Quarks confined in nucleons.
  - For  $\Lambda_{\rm QCD} \leq k_F^B \leq N_c \Lambda_{\rm QCD}$ : Quarks starts to take low phase space, and a shell-like structure is formed.

Nuclear > Quarkyonic

(at few times  $\rho_0$ )

Quarks

• For  $k_F^B < \Lambda_{\rm QCD}$ : Quarks confined in nucleons.

• For  $\Lambda_{\rm QCD} \leq k_F^B \leq N_c \Lambda_{\rm QCD}$ : Quarks starts to take low phase space, and a shell-like structure is formed.

• For  $k_F^B \simeq N_c^{3/2} \Lambda_{\rm QCD}$ : Confinement disappears.

Total baryon density has smooth behavior and chemical potential for confined states enhance suddenly, then pressure suddenly increases. *This is not an usual phase transition!* 

Nucleons with hard-core volume  $v_0 = \frac{4}{3}\pi r_0^3$ , where  $r_0$  is the hard-core radius. Hard-core density:  $n_0 = 1/v_0$ 

In a system with baryon density  $n_N$  and volume V, the excluded volume (not occupied by baryon cores) is:  $V_{ex} = V\left(1 - \frac{n_N}{n_0}\right)$ 

$$n_{ex} = \frac{n_N}{1 - n_N/n_0} = 2N_f \int^{k_F} \frac{d^3k}{(2\pi)^3} \qquad \qquad \mu_N = \frac{\partial\varepsilon}{\partial n_F}$$

$$\varepsilon = 2N_f \left(1 - \frac{n_N}{n_0}\right) \int^{k_F} \frac{d^3k}{(2\pi)^3} \sqrt{k^2 + M^2} \qquad \qquad P = -\varepsilon + \mu_F$$

$$n_{ex} = \frac{n_N}{1 - n_N/n_0} = \frac{N_f}{\pi^2} \int_{k_F}^{k_F + \Delta} dk \ k^2$$

$$\varepsilon = \frac{N_f}{\pi^2} \left( 1 - \frac{n_N}{n_0} \right) \int_{k_F}^{k_F + \Delta} dk \ k^2 \sqrt{k^2 + M^2} + \varepsilon_Q$$
Free gas of
quarks
$$\begin{cases} n_Q = \frac{N_f}{\pi^2} \int_0^{k_Q} dk \ k^2 = \frac{N_f}{3\pi^2} k_Q^3 \\ \varepsilon_Q = \frac{N_c N_f}{2} \int_0^{k_Q} dk \ k^2 \sqrt{k^2 + m^2} \end{cases}$$

 $\varepsilon_Q = \frac{1+c^{2+j}}{\pi^2} \int_0^{\infty}$ 

$$k_Q = k_F / N_c \qquad m = M / N_c$$



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Modification in the low density Fermi distribution in a way that does not affect its behavior for large Fermi momenta:

contribution

$$1 \to \frac{\sqrt{k_Q^2 + \Lambda^2}}{k_Q}$$

$$n_Q = \frac{N_f}{3\pi^2} \left[ \left( k_Q^2 + \Lambda^2 \right)^{3/2} - \Lambda^3 \right]$$

$$\varepsilon_Q = \frac{N_c N_f}{\pi^2} \int_0^{k_Q} dk \ k \sqrt{k^2 + \Lambda^2} \sqrt{k^2 + m^2}$$





Good agreement with sound velocity obtained from an equation of state extracted from neutron stars properties.

- Hard core repulsion: Scale can be measured by the effective size of the baryon.
- Protons + Neutrons + Hyperons in an excluded volume for the shell

 $n_N = n_p + n_n + n_\Lambda;$   $n_{\tilde{N}} = n_p + n_n + (1 + \alpha)n_\Lambda$ 

 For neutron stars phenomenology: β-equilibrium and charge neutrality must be imposed.

$$\varepsilon_{\rm qy.} = 2\left(1 - \frac{\tilde{n}_b}{n_0}\right) \sum_{i}^{\{n,p,\Lambda\}} \int_{k_F^{b_i}}^{[k_F + \Delta]_{b_i}} \frac{d^3k}{(2\pi)^3} \sqrt{k^2 + m_{b_i}^2} \\ + \frac{N_c}{\pi^2} \sum_{j}^{\{u,d,s\}} \int_{0}^{k_F^{Q_j}} dk \mathcal{M}_j(k^2) \sqrt{k^2 + m_{Q_j}^2} + \frac{(3\pi^2)^{\frac{4}{3}}}{4\pi^2} n_e^{\frac{4}{3}}$$

Lower boundary of baryon shell:

$$k_F^n = k_{\text{conf}}^u + 2k_{\text{conf}}^d$$
$$k_F^p = 2k_{\text{conf}}^u + k_{\text{conf}}^d$$
$$k_F^\Lambda = k_{\text{conf}}^u + k_{\text{conf}}^d + k_{\text{conf}}^s$$

#### Quark Density.

$$n_{\tilde{Q}_i} \equiv \frac{1}{\pi^2} \int_0^{k_F^{Q_i}} dk \mathcal{M}_i(k^2) = \frac{1}{\pi^2} \int_0^{k_F^{Q_i}} dk (k^2 + \Lambda_{Q_i}^2)$$

For the minimum of energy density:  $dn_B = dn_n + dn_Q = 0$ which results in  $\mu_n = N_c \mu_{\tilde{d}} - \mu_e$ 

Electromagnetic charge neutrality

 $n_e = n_p + 2n_{\tilde{u}} - n_{\tilde{d}} - n_{\tilde{s}}$ 

Beta equilibrium conditions

 $\mu_{\tilde{d}} = \mu_{\tilde{u}} + 3\mu_e$ Existence of  $\Lambda$  hyperon  $\mu_{\Lambda} = \mu_n$ Existence of s quark

п

 $\mu_{ ilde{s}} = \mu_{ ilde{d}}$ 





→ Correction of low density regime EoS: use of a rich neutron matter EoS in the range  $n_B < n_M$ .

$$E/A = \sqrt{(p_F^n)^2 + M_n^2} - M_n + \tilde{a} \left(\frac{n_n}{\rho_0}\right) + \tilde{b} \left(\frac{n_n}{\rho_0}\right)^2$$
$$\tilde{a} = -28.3 \text{ MeV} \quad \text{and} \quad \tilde{b} = 10.7 \text{ MeV}$$



D. Duarte, K.S. Jeong, S.HO arXiv:2007.08098

### **Final Remarks**

- Analysis of GW data have been providing very important insights about the properties of dense QCD matter.
- We extend the excluded volume model of isospin symmetric two-flavor dense Quarkyonic matter including strange baryons and quarks and address its implications for neutron stars.
- The extension to finite temperature is also an interesting problem, since future experiments in the NICA/FAIR facilities may provide more insights about the QCD phase diagram in the regime of high density and intermediate temperatures.

# THANKS FOR WATCHING: