EIC impact on (un)polarized collinear PDFs

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EIC impact on unpolarized PDFs

on polarized PDFs

- Double longitudinal asymmetry ALL
- Parity violating DIS asymmetry AuL



EIC predictions: unpolarized PDFs

Current knowledge of unpolarized collinear PDFs has been driven by:

- inclusive neutral current (NC) and
- charged current DIS cross sections
- $p\bar{p}$ collisions at the Tevatron
- *pp* collisions at LHC

Range: x down to 10^{-5} and Q^2 up to 10^4 GeV². Complementary in accessing the small-x and large-x longitudinal hadron structure.

EIC: overlapping kinematic range between HERA and the fixed-target experiments, instantaneous luminosity 3 orders larger

Better constraint on existing measurements: ALL New observables available: AUL

Simulated statistical and systematic uncertainties for eP NC DIS at $\sqrt{s} = 140.7 \text{ GeV}$

18x275 e-p N.C. Uncertainties



PDFs at EIC: unpolarized reduced σ

To assess the impact of EIC data on the unpolarized PDF we study the reduced cross section for different configurations

Different scenarios

DIS Neutral Current

DIS Charged Current

with electron and positron beam

 $\sigma_r = \frac{d\sigma^c}{dx dQ^2} \frac{x_q}{2\pi\alpha^2 [1 + 1]}$

For the neutral current

$$\begin{bmatrix} F_2^{\gamma}, F_2^{\gamma Z}, F_2^{Z} \end{bmatrix} = x \sum_{q} \begin{bmatrix} e_q^2, 2e_q g_V^q, g_V^{q2} + g_A^{q2} \end{bmatrix} (q + \bar{q})$$
$$\begin{bmatrix} F_3^{\gamma}, F_3^{\gamma Z}, F_3^{Z} \end{bmatrix} = \sum_{q} \begin{bmatrix} 0, 2e_q g_A^q, 2g_V^q g_A^q \end{bmatrix} (q - \bar{q})$$

for neutron: $d \leftrightarrow u$

$$\frac{xQ^4}{(1-y)^2]} = F_2^c(x,Q^2) - \frac{y^2}{1+(1-y^2)}F_L^c(x,Q^2)$$

For the charged current

$$F_2^{W-} = 2x(u + \bar{d} + \bar{s} + c...)$$

$$F_3^{W^-} = 2(u - \bar{d} - \bar{s} + c...)$$

For W+ : $d \leftrightarrow u, s \leftrightarrow c$

JAM Monte Carlo resampling methodology



PDF parametrization at input scale:

$$f(x) = Nx^{\alpha}(1-x)^{\beta}(1+\gamma\sqrt{x}) + \eta x$$

Determine set of parameters through Bayesian posterior resampling

likelihood function

$$e^{-\frac{\chi^2}{2}}$$

Multi-step procedure: repeated including additional datasets at each step



unpolarized EIC pseudodata

For spin-averaged PDFs



Compare the uncertainties of these two last steps

EIC impact: unpol. PDFs uncertainties

Comparison of relative uncertainties for unpolarized PDFs xf(x) for multiple flavors, before and after the inclusion of EIC data for electron beam



EIC predictions: unpol. PDFs comparison

Comparison of relative uncertainties for unpolarized PDFs xf(x) for multiple flavors,



EIC predictions: impact on Δg uncertainties

A precise determination of the helicity gluon distribution function **Δ***g* is one of the golden measurements of nucleon spin structure at the EIC

Proton Spin Puzzle: Open problem since EMC experiment

In particular for **gluons**

 $S_g(Q^2)$ $\Delta f(x,Q^2) \equiv .$

with f+(f-) denoting the number density of partons with the same (opposite) helicity as the nucleons

EIC White Paper [1212.1701]

$$\frac{1}{2} = S_q + L_q + S_g + L_g$$

$$= \int_0^1 \Delta_g(x, Q^2) dx$$
$$f^+(x, Q^2) - f^-(x, Q^2)$$







Impact on polarized PDFs



impact of future EIC data on quark and gluon helicity distributions in the proton

DOUBLE LONGITUDINAL SPIN ASYMMETR
$$A_{LL} = \frac{\sigma^{\uparrow \uparrow} - \sigma^{\downarrow \uparrow}}{\sigma^{\downarrow \uparrow} + \sigma^{\uparrow \uparrow}}$$

longitudinally polarized e⁻ off longit. polarized hadrons

PARITY VIOLATING ASYMMETRY

$$A_{\rm UL} = \frac{\sigma^{\Uparrow} - \sigma^{\Downarrow}}{\sigma^{\Uparrow} + \sigma^{\Downarrow}}$$

unpolarized leptons off Longitudinally polarized hadrons



EIC impact on helicity PDFs

- EIC will cover a wider range of (x,Q²)
- How much this will improve our determination of Δg ?

 A_L Pseudodata for double-spin asymmetry

$$\begin{aligned} A_1 &= \frac{(g_1 - \gamma^2 g_2)}{F_1}, \qquad A_2 = \gamma \frac{(g_1 + g_2)}{F_1} \\ A_{LL} &= \frac{y (2 - y)}{y^2 + 2(1 - y)(1 + R)} \frac{g_1}{F_1} \\ g_1(x, Q^2) &= \frac{1}{2} \sum_q e_q^2 \left([\Delta C_{1q} \otimes \Delta q^+](x, Q^2) + [\Delta C_{1g} \otimes \Delta g](x, Q^2) \right) \end{aligned}$$
Flavor separation p, d, ³He

$$L_L = \frac{\sigma^{\uparrow\uparrow\uparrow} - \sigma^{\downarrow\uparrow\uparrow}}{\sigma^{\downarrow\uparrow\uparrow} + \sigma^{\uparrow\uparrow\uparrow}} = D\left(A_1 + \eta A_2\right)_{\uparrow\uparrow\uparrow}$$

$$A_2 = \gamma \frac{(g_1 + g_2)}{F_1}$$

Parity violating asymmetry

$$A_{\rm UL} = \frac{\sigma^{\uparrow} - \sigma^{\downarrow}}{\sigma^{\uparrow} + \sigma^{\downarrow}} \qquad \text{scattering of unpolarized legges} \\ = \frac{G_F x Q^2}{2\sqrt{2}\pi\alpha} \frac{g_A^e Y^- g_1^{\gamma Z} + g_V^e Y^+ g_5^{\gamma Z}}{xy^2 F_1 + (1 - y)F_2} \\ x, Q^2) = \sum_q e_q g_V^q \Big([\Delta C_{1q} \otimes \Delta q^+] (x, Q^2) + 2[\Delta C_{1g} \otimes \Delta g] (x, Q^2) \Big)$$

$$g_5^{\gamma Z}(x,Q^2) = \sum_q e_q g_A^q \left[\Delta C_{5q} \otimes \Delta q^-\right](x,Q^2)$$

 $g_1^{\gamma Z}$

otons hadrons

Independent linear combination of helicity PDFs together with g_1 allow cleaner flavor separation



Polarized pseudodata

Multistep Monte Carlo with Bayesian inference

For spin-averaged PDFs



For spin-dependent PDFs





Baseline PDFs for EIC pseudodata





6 scenarios

absolute statistical uncertainties for the asymmetries



Imposing or not SU(3) flavor symmetry

$$\int_{0}^{1} dx \left[\Delta u^{+}(x, Q^{2}) - \Delta d^{+}(x, Q^{2}) \right] = g_{A}$$
$$\int_{0}^{1} dx \left[\Delta u^{+}(x, Q^{2}) + \Delta d^{+}(x, Q^{2}) - 2\Delta s^{+}(x, Q^{2}) \right] = 0$$

 $= a_8$

EIC impact on g₁ uncertainties





Impact of projected e-p A_{LL} data on the proton g_1^p structure function

ElC impact on g1 uncertainties



Impact of projected e-p A_{LL} data on the neutron g_1^p structure function

EIC impact on truncated moments



$$\Delta \Sigma_{\text{trunc}} \left(Q^2 \right) = \sum_{q} \int_{10^{-4}}^{1} dx \left[\Delta q(x, Q^2) + \Delta \bar{q}(x, Q^2) \right]$$

$$\Delta G_{\text{trunc}}\left(Q^2\right) = \int_{10^{-4}}^{1} dx \,\Delta g(x, Q^2)$$



PDFs constraints from Aul pseudo data



Ratio of uncertainties on the PDFs as functions of x, including EIC data on the PVDIS asymmetry A_{PV} to those without EIC data



We performed a dedicated impact study of future EIC data on unpolarized cross section and polarization asymmetries, based on a global fit with a Monte Carlo approach

There is a significant impact in the unpolarized PDFs, mostly in the valence case

Study of polarized asymmetries can greatly improve the determination of helicity PDFs at low-x. ALL and APV acts in an almost complementary way on the quark singlet and gluon moment.

The EIC facility will provide unprecedented access to the flavor and spin structure of the nucleon in previously unexplored regions of kinematics at low x values

