

On wide-angle photo- and electroproduction of pions to twist-3 accuracy

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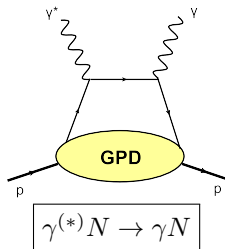
Outline

- 1 Handbag factorization
- 2 WAMP at twist-3
- 3 Numerical results
 - Photoproduction
 - Electroproduction
 - Spin effects
- 4 Summary

Handbag factorization

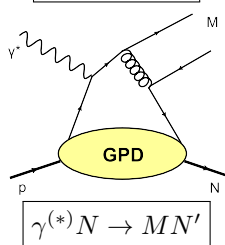
DEEPLY VIRTUAL

WIDE ANGLE



DVCS (Compton scattering)

WACS



DVMP (meson production)

WAMP

Handbag factorization

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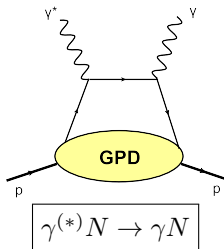
$$Q^2 \gg, -t \ll$$

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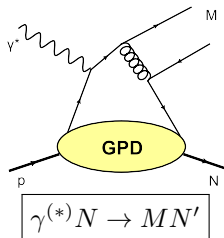
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WAMP



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$$q + k_j = q' + k'_j$$

$$Q^2 = -q^2, s = (q + p)^2, t = (p - p')^2, u \rightarrow \text{parent process}$$

$$Q^2, \hat{s}, \hat{u}, \hat{t} \rightarrow \text{active parton}$$

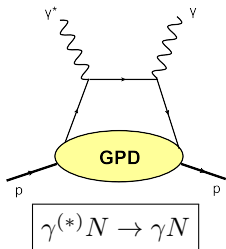
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[Collins, Freund '99]



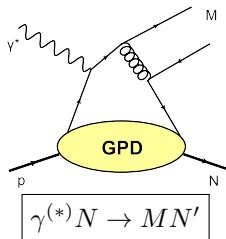
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 $\mathcal{H} \otimes GPD$

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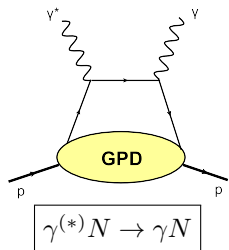
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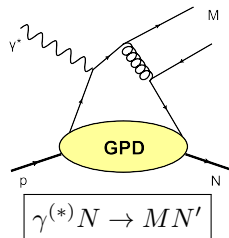
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[Radyushkin '98]

[Diehl, Feldman, Kroll, Jakob '98]

WAMP

[Huang, Kroll '00]

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 $\mathcal{H}(1/x \otimes GPD(\xi = 0))$

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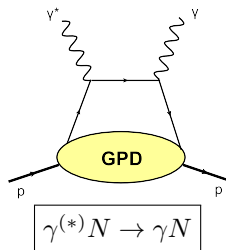
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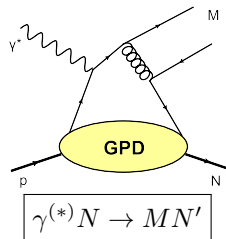
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 - leading twist-2 theoretical predictions (γ_L^*) bellow the experimental data which indicate the importance of γ_T^*
 - ⇒ twist-3 calculations with transversity (chiral-odd) GPDs ($H_T...$)
[Goloskokov, Kroll '10] (2-body, i.e, WW approximation), [Goldstein, Hernandez, Liuti '13]

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 [Goloskokov, Kroll '10] (2-body, i.e, WW approximation), [Goldstein, Hernandez, Liuti '13]
- $WA\pi P$:
 - twist-2 results [Huang, Kroll '00] well bellow the experimental data for photoproduction ($Q^2 = 0$)
 - twist-3 2-body contribution to pion photoproduction in WW approximation vanishes [Huang, Jakob, Kroll, P-K '03]
 - twist-3 (2- and 3-body) prediction to π_0 photoproduction calculated [Kroll, P-K '18] and fitted to CLAS data [CLAS '17]
 - [Kroll, P-K. '21, arXiv:2107.04544]: twist-3 prediction for $P = \pi^\pm, \pi^0$ photo- and electroproduction analyzed ($Q^2 < -t$); extension to other PS mesons and well as DVMP is straightforward

Helicity amplitudes \mathcal{M} for WAMP

$$\begin{aligned} \mathcal{M}_{0+, \mu+}^P &= \frac{e_0}{2} \sum_{\lambda} \left[\mathcal{H}_{0\lambda, \mu\lambda}^P \left(R_V^P(t) + 2\lambda R_A^P(t) \right) \right. \\ &\quad \left. - 2\lambda \frac{\sqrt{-t}}{2m} \mathcal{H}_{0-\lambda, \mu\lambda}^P \bar{S}_T^P(t) \right] \\ \mathcal{M}_{0-, \mu+}^P &= \frac{e_0}{2} \sum_{\lambda} \left[\frac{\sqrt{-t}}{2m} \mathcal{H}_{0\lambda, \mu\lambda}^P R_T^P(t) \right. \\ &\quad \left. - 2\lambda \frac{t}{2m^2} \mathcal{H}_{0-\lambda, \mu\lambda}^P S_S^P(t) \right] + e_0 \mathcal{H}_{0-, \mu+}^P S_T^P(t) \end{aligned}$$

μ photon helicity, $\lambda \dots$ quark helicities, $P = (\pi^{\pm}, \pi^0)$,

form factors: $R_V^a(t) = \int \frac{dx}{x} H^a(x, \xi = 0, t)$

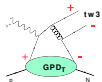
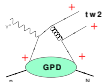
$$R_V^{\pm} = R_V^u - R_V^d, \quad R_V^0 = \frac{1}{\sqrt{2}} (e_u R_V^u - e_d R_V^d)$$

$\mathcal{H}_{0\lambda, \mu\lambda}^P \dots$ non-flip subprocess amplitudes (twist-2)

$$R_V \rightarrow H, \quad R_A \rightarrow \tilde{H}, \quad R_T \rightarrow \tilde{E}$$

$\mathcal{H}_{0-\lambda, \mu\lambda}^P \dots$ flip subprocess amplitudes (twist-3)

$$S_T \rightarrow H_T, \quad \bar{S}_T \rightarrow \bar{E}_T, \quad S_S \rightarrow \tilde{H}_T \quad (\text{transversity GPDs})$$



Helicity amplitudes \mathcal{M} for WAMP

μ photon helicity, $\lambda \dots$ quark helicities, $P = (\pi^\pm, \pi^0)$,

Transverse photon polarization ($\mu = \pm 1$)

$$\begin{aligned} \mathcal{M}_{0^+, \mu^+}^P &= \frac{e_0}{2} \sum_{\lambda} \left[\mathcal{H}_{0\lambda, \mu\lambda}^P \left(R_V^P(t) + 2\lambda R_A^P(t) \right) \rightarrow \text{twist-2} \right. \\ &\quad \left. - 2\lambda \frac{\sqrt{-t}}{2m} \mathcal{H}_{0-\lambda, \mu\lambda}^P \bar{S}_T^P(t) \right] \rightarrow \text{twist-3} \\ \mathcal{M}_{0^-, \mu^+}^P &= \frac{e_0}{2} \sum_{\lambda} \left[\frac{\sqrt{-t}}{2m} \mathcal{H}_{0\lambda, \mu\lambda}^P R_T^P(t) \rightarrow \text{twist-2} \right. \\ &\quad \left. - 2\lambda \frac{t}{2m^2} \mathcal{H}_{0-\lambda, \mu\lambda}^P S_S^P(t) \right] + e_0 \mathcal{H}_{0^-, \mu^+}^P S_T^P(t) \rightarrow \text{twist-3} \end{aligned}$$

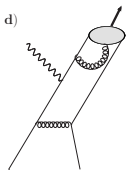
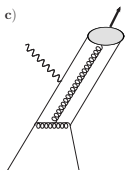
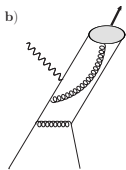
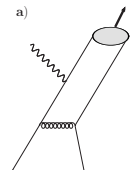
Longitudinal photon polarization

$$\begin{aligned} \mathcal{M}_{0^+, 0^+}^P &= e_0 \mathcal{H}_{0^+, 0^+}^P R_A^P(t) \rightarrow \text{twist-2} \\ \mathcal{M}_{0^-, 0^+}^P &= e_0 \mathcal{H}_{0^-, 0^+}^P S_T^P(t) \rightarrow \text{twist-3} \end{aligned}$$

Subprocess amplitudes \mathcal{H}

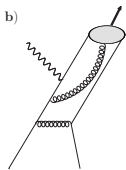
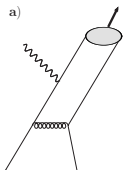
$q\bar{q} \rightarrow \pi$ projector (a) [Beneke, Feldmann '00]
 $(\tau q' + k_{\perp}) + (\bar{\tau} q' - k_{\perp}) = q'$

$$\mathcal{P}_2^P \sim f_{\pi} \left\{ \begin{aligned} & \gamma_5 q' \phi_{\pi}(\tau, \mu_F) \\ & + \mu_{\pi}(\mu_F) \left[\gamma_5 \phi_{\pi P}(\tau, \mu_F) \right. \\ & - \frac{i}{6} \gamma_5 \sigma_{\mu\nu} \frac{q'^{\mu} n^{\nu}}{q' \cdot n} \phi'_{\pi\sigma}(\tau, \mu_F) \\ & \left. + \frac{i}{6} \gamma_5 \sigma_{\mu\nu} q'^{\mu} \phi_{\pi\sigma}(\tau, \mu_F) \frac{\partial}{\partial k_{\perp\nu}} \right] \end{aligned} \right\}_{k_{\perp} \rightarrow 0}$$



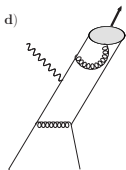
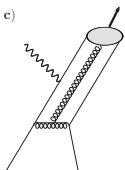
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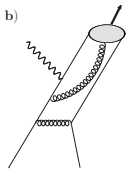
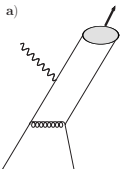
$q\bar{q}g \rightarrow \pi$ projector (b, c) [Kroll, P-K '18]
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$$\mathcal{P}_3^P \sim f_{3\pi}(\mu_F) \frac{i}{g} \gamma_5 \sigma_{\mu\nu} q'^\mu g_{\perp}^{\nu\rho} \frac{\phi_{3\pi}(\tau_a, \tau_b, \tau_g, \mu_F)}{\tau_g}$$

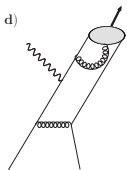
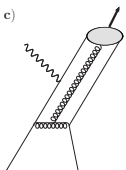
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$$\mu_\pi = m_\pi^2 / (m_u + m_d) \cong 2 \text{ GeV}$$

distribution amplitudes (DAs):

twist-2: ϕ_π

2-body twist-3 $\phi_{\pi p}, \phi_{\pi\sigma}$ 3-body twist-3 $\phi_{3\pi}$

→ connected by equations of motion (EOMs)

DAs and EOMs

$$\tau \phi_{\pi p}(\tau) + \frac{\tau}{6} \phi'_{\pi\sigma}(\tau) - \frac{1}{3} \phi_{\pi\sigma}(\tau) = \phi_{\pi 2}^{EOM}(\bar{\tau})$$

$$\bar{\tau} \phi_{\pi p}(\tau) - \frac{\bar{\tau}}{6} \phi'_{\pi\sigma}(\tau) - \frac{1}{3} \phi_{\pi\sigma}(\tau) = \phi_{\pi 2}^{EOM}(\tau)$$

$$\phi_{\pi 2}^{EOM}(\tau) = 2 \frac{f_{3\pi}}{f_{\pi} \mu_{\pi}} \int_0^{\bar{\tau}} \frac{d\tau_g}{\tau_g} \phi_{3\pi}(\tau, \bar{\tau} - \tau_g, \tau_g)$$

- EOMs and symmetry properties $\phi_{\pi^*}(\bar{\tau}) = \phi_{\pi^*}(\tau)$
 $\phi_{3\pi}(\tau_a, \tau_b, \tau_g) = \phi_{\pi}(\tau_b, \tau_a, \tau_g) \Rightarrow$ the subprocess amplitudes in terms of two twist-3 DAs, 2- and 3-body contributions combined
- combined EOMs \rightarrow first order differential equation \Rightarrow from known form of $\phi_{3\pi}$ [Braun, Filyanov '90] one determines $\phi_{\pi p}$ (and $\phi_{\pi\sigma}$)

Note: $q\bar{q}g$ projector and EOMs were derived using light-cone gauge for constituent gluon

Subprocess amplitudes: twist-2

Transverse photon polarization ($\mu = \pm 1$) T

$$\mathcal{H}_{0\lambda, \mu\lambda}^{P, tw2} \sim f_\pi C_F \alpha_s(\mu_R) \frac{\sqrt{-\hat{t}}}{\hat{s} + Q^2} \int_0^1 d\tau \phi_\pi(\tau) \left[(2\lambda\mu + 1) \left(\frac{(\hat{s}\tau + Q^2)(\hat{s} + Q^2) - \hat{u}Q^2\bar{\tau}}{\hat{s}\bar{\tau}(Q^2\bar{\tau} - \hat{t}\tau)} e_a \right. \right. \\ \left. \left. + \frac{(\hat{s}\tau - Q^2)(\hat{s} + Q^2) - \hat{u}Q^2\bar{\tau}}{\hat{u}\tau(Q^2\tau - \hat{t}\bar{\tau})} e_b \right) + (2\lambda\mu - 1) \left(\frac{\hat{u} e_a}{(Q^2\bar{\tau} - \hat{t}\tau)} + \frac{\hat{s}\bar{\tau} e_b}{\tau(Q^2\tau - \hat{t}\bar{\tau})} \right) \right]$$

Longitudinal photon polarization L

$$\mathcal{H}_{0\lambda, 0\lambda}^{P, tw2} \sim f_\pi C_F \alpha_s(\mu_R) \lambda \frac{Q\sqrt{-\hat{u}\hat{s}}}{\hat{s} + Q^2} \int_0^1 d\tau \phi_\pi(\tau) \left(\frac{\hat{u} e_a}{\hat{s}(Q^2\bar{\tau} - \hat{t}\tau)} - \frac{(\hat{t} + \tau\hat{u}) e_b}{\tau\hat{u}(Q^2\tau - \hat{t}\bar{\tau})} \right)$$

Subprocess amplitudes: twist-2

Transverse photon polarization ($\mu = \pm 1$) **T**

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→ photoproduction ($Q \rightarrow 0$): $\mathcal{H}_L^{P, tw2} \Big|_{Q \rightarrow 0} = 0$

$$\mathcal{H}_T^{P, tw2} \Big|_{Q \rightarrow 0} \sim f_\pi C_F \alpha_s(\mu_R) \frac{1}{\sqrt{-\hat{t}}} \int_0^1 \frac{d\tau}{\tau} \phi_\pi(\tau) \left((1 + 2\lambda\mu) \hat{s} - (1 - 2\lambda\mu) \hat{u} \right) \left(\frac{e_a}{\hat{s}} + \frac{e_b}{\hat{u}} \right)$$

Subprocess amplitudes: twist-2

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Longitudinal photon polarization **L**

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→ DVMP ($\hat{t} \rightarrow 0$): $\mathcal{H}_T^{P,tw2} \Big|_{\hat{t} \rightarrow 0} = 0$

$$\mathcal{H}_L^{P,tw2} \Big|_{\hat{t} \rightarrow 0} : \quad \hat{s} = -\frac{\xi - x}{2\xi} Q^2, \quad \hat{u} = -\frac{\xi + x}{2\xi} Q^2 \quad \Rightarrow \text{well known LO result for DVMP}$$

Subprocess amplitudes: twist-3

General structure:

$$\begin{aligned}\mathcal{H}^{P,tw3} &= \mathcal{H}^{P,tw3,q\bar{q}} + \mathcal{H}^{P,tw3,q\bar{q}g} \\ &= \left(\mathcal{H}^{P,\phi_{\pi p}} + \mathcal{H}^{P,\phi_{\pi^2}^{EOM}} \right) + \underbrace{\left(\mathcal{H}^{P,q\bar{q}g,C_F} + \mathcal{H}^{P,q\bar{q}g,C_G} \right)} \\ &= \mathcal{H}^{P,\phi_{\pi p}} + \mathcal{H}^{P,\phi_{3\pi},C_F} + \mathcal{H}^{P,\phi_{3\pi},C_G}\end{aligned}$$

- 2-body twist-3 $\sim C_F$; 3-body C_F and C_G proportional parts
- C_G part is separately gauge invariant
- the sum of 2- and 3-body C_F parts is gauge invariant (QED and QCD)
- no end-point singularities for finite \hat{t}

Subprocess amplitudes: twist-3 at $Q \ll$ or $\hat{t} \ll$

General structure:

$$\begin{aligned}
 \mathcal{H}^{P,tw3} &= \mathcal{H}^{P,tw3,q\bar{q}} + \mathcal{H}^{P,tw3,q\bar{q}g} \\
 &= \left(\mathcal{H}^{P,\phi\pi p} + \mathcal{H}^{P,\phi_{\pi 2}^{EOM}} \right) + \underbrace{\left(\mathcal{H}^{P,q\bar{q}g,C_F} + \mathcal{H}^{P,q\bar{q}g,C_G} \right)} \\
 &= \mathcal{H}^{P,\phi\pi p} + \mathcal{H}^{P,\phi_{3\pi},C_F} + \mathcal{H}^{P,\phi_{3\pi},C_G}
 \end{aligned}$$

- $\mathcal{H}_L^{P,tw3} \sim Q\sqrt{-t}$ vanishes both for $Q \rightarrow 0$ and $\hat{t} \rightarrow 0$
- photoproduction ($Q \rightarrow 0$): $\mathcal{H}^{P,\phi\pi p} = 0$ [Kroll, P-K '18], $\mathcal{H}_T^{P,tw3}$ proportional to $(2\lambda - \mu)$
- DVMP ($\hat{t} \rightarrow 0$): $\mathcal{H}^{P,\phi_{\pi 2}^{EOM}} = 0$, end-point singularities in $\mathcal{H}^{P,\phi\pi p}$ [Goloskokov, Kroll '10], $\mathcal{H}_T^{P,tw3}$ proportional to $(2\lambda + \mu)$

Pion distribution amplitudes

Twist-2 DA: $\phi_\pi(\tau, \mu_F) = 6\tau\bar{\tau} [1 + a_2(\mu_F) C_2^{3/2}(2\tau - 1)]$

Twist-3 DAs:

$$\begin{aligned}\phi_{3\pi}(\tau_a, \tau_b, \tau_g, \mu_F) &= 360\tau_a\tau_b\tau_g^2 \left[1 + \omega_{1,0}(\mu_F) \frac{1}{2}(7\tau_g - 3) \right. \\ &+ \omega_{2,0}(\mu_F) (2 - 4\tau_a\tau_b - 8\tau_g + 8\tau_g^2) \\ &+ \left. \omega_{1,1}(\mu_F) (3\tau_a\tau_b - 2\tau_g + 3\tau_g^2) \right] \text{ [Braun, Filyanov '90]}\end{aligned}$$

using EOMs [Kroll, P-K '18]:

$$\begin{aligned}\phi_{\pi p}(\tau, \mu_F) &= 1 + \frac{1}{7} \frac{f_{3\pi}(\mu_F)}{f_\pi \mu_\pi(\mu_F)} \left(7\omega_{1,0}(\mu_F) - 2\omega_{2,0}(\mu_F) - \omega_{1,1}(\mu_F) \right) \\ &\times \left(10 C_2^{1/2}(2\tau - 1) - 3 C_4^{1/2}(2\tau - 1) \right), \quad \phi_{\pi\sigma}(\tau) = \dots\end{aligned}$$

Parameters:

- $a_2(\mu_0) = 0.1364 \pm 0.0213$ at $\mu_0 = 2$ GeV [Braun et al '15] (lattice)
- $\omega_{10}(\mu_0) = -2.55$, $\omega_{11}(\mu_0) = 0.0$ and $f_{3\pi}(\mu_0) = 0.004$ GeV². [Ball '99]
- $\omega_{20}(\mu_0) = 8.0$ [Kroll, P-K '18] fit to π^0 photoproduction data [CLAS '17]

Evolution of the decay constants and DA parameters taken into account.

Choice of scales: $\mu_R^2 = \mu_F^2 = \hat{t}\hat{u}/\hat{s}$

Form factors and GPDs

$R_i \dots 1/x$ moment of $\xi = 0$ GPD (K_i)

- $R_V(\leftarrow H), R_T(\leftarrow E)$ from nucleon form factor analysis [Diehl, Kroll '13]
- $R_A(\leftarrow \tilde{H})$ form factor analysis and WACS KLL asymmetry [Kroll '17]
- $S_T(\leftarrow H_T), \bar{S}_T(\leftarrow \bar{E}_T)$ low $-t$ from DVMP analysis [Goloskokov, Kroll '11]
- $S_S(\leftarrow \tilde{H}_T) \cong \bar{S}_T/2$ ($\bar{E}_T = 2\tilde{H}_T + E_T$)

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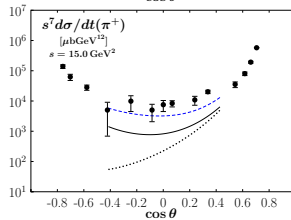
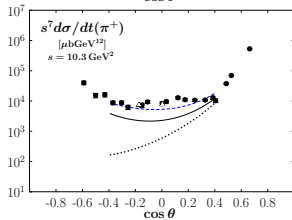
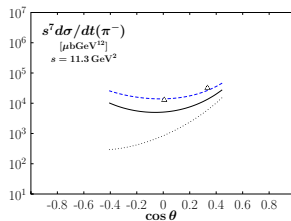
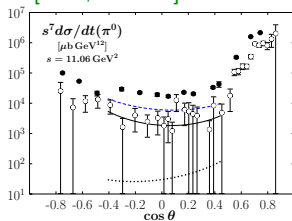
GPD parameterization [Diehl, Feldmann, Jakob, Kroll '04, Diehl, Kroll '13]

$$K_i^a = k_i^a(x) \exp[t f_i^a(x)], f_i^a(x) = (B_i^a - \alpha_i^a \ln x)(1-x)^3 + A_i^a x(1-x)^2$$

- strong $x - t$ correlation
- power behaviour for large $(-t)$
- choice for transversity GPDs $A = 0.5 \text{ GeV}^{-2}$

Photoproduction

[Kroll, P-K '21]



theoretical predictions with parameters from [Kroll, P-K '18] (fit of π^0 twist-3 prediction to [CLAS '17] data)

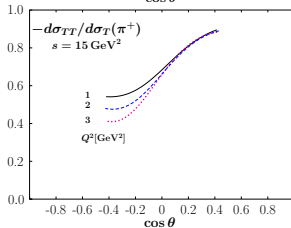
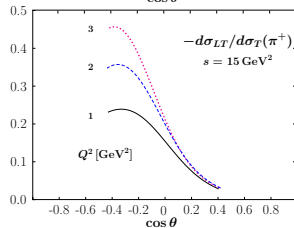
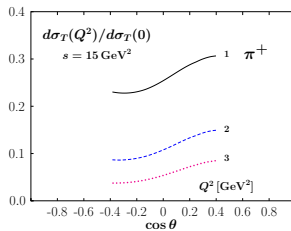
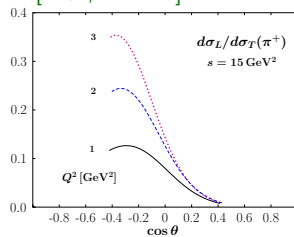
solid curves: complete twist-3
dotted curves: twist-2
dashed curves: $\omega_{20} = 10.3$
 $\mu_R = \mu_F = 1 \text{ GeV}$

exp data:
full circles [SLAC '76]
open circles [CLAS '17]
triangles [JLab, Hall A '05]

- twist-2 prediction well beyond the data [Huang, Kroll '00]
- scaling: s^{-7} (s^{-8}) twist-2 (twist-3) \rightarrow effective s^{-9} \rightarrow too strong

Electroproduction

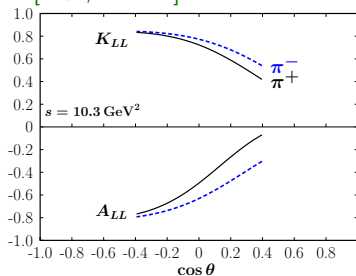
[Kroll, P-K '21]



- both for σ_L and σ_{LT} no twist-2 and twist-3 interference
 \Rightarrow information on S_T (H_T)
- information on S_S (H_T) from σ_{TT} (suppressed for DVMP)

Spin effects - photoproduction

[Kroll, P-K '21]



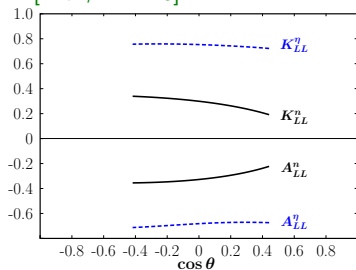
$A_{LL}(K_{LL})$... correlation of the helicities of the photon and incoming (outgoing) nucleon

$$A_{LL}^{P,tw2} = K_{LL}^{P,tw2}$$

$$A_{LL}^{P,tw3} = -K_{LL}^{P,tw3}$$

→ characteristic signature for dominance of twist-3 (like $\sigma_T \gg \sigma_L$ in DVMP)

[Kroll, P-K '18]



$A_{LL}(K_{LL})$ for π^0 photoproduction on neutron and η photoproduction

Conclusions, questions, outlook...

- handbag factorization applied to wide-angle photo- and electroproduction of pions → WAMP
- in contrast to WACS, but like DVMP, the leading twist-2 analysis (helicity non-flip GPDs) for wide-angle photoproduction fails by order of magnitude
- twist-3 prediction for WAMP obtained, both 2 and 3-body contributions included
- π^0 photoproduction was fitted to the data
- interesting helicity correlations show that twist-3 dominates
- different combinations of form factors along with available data should allow to extract the form factors and to learn about large $-t$ behaviour of transversity GPDs important for parton tomography
- extension to other pseudoscalar mesons straightforward

Conclusions, questions, outlook...

- handbag factorization applied to wide-angle photo- and electroproduction of pions → WAMP
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Thank you!

Subprocess amplitudes: twist-3 at $Q \rightarrow 0, t \rightarrow 0$

photoproduction

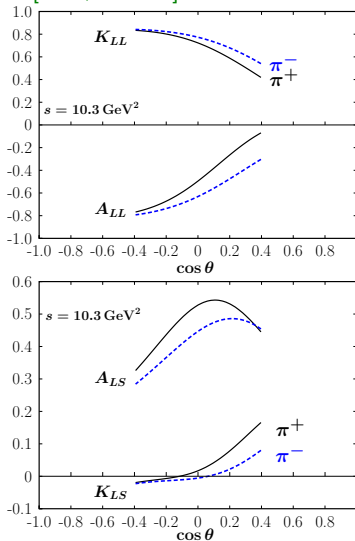
$$\begin{aligned} \mathcal{H}_{0-\lambda, \mu\lambda}^{P, tw3} |_{Q^2 \rightarrow 0} &\sim (2\lambda - \mu) f_{3\pi} \alpha_S(\mu_R) \sqrt{-\hat{s}\hat{u}} \int_0^1 d\tau \int_0^{\bar{\tau}} \frac{d\tau_g}{\tau_g} \phi_{3\pi}(\tau, \bar{\tau} - \tau_g, \tau_g) \\ &\times \left[C_F \left(\frac{1}{\bar{\tau}^2} - \frac{1}{\bar{\tau}(\bar{\tau} - \tau_g)} \right) \left(\frac{e_a}{\hat{s}^2} + \frac{e_b}{\hat{u}^2} \right) + \right. \\ &\quad \left. - C_G \frac{2}{\tau\tau_g} \frac{\hat{t}}{\hat{s}\hat{u}} \left(\frac{e_a}{\hat{s}} + \frac{e_b}{\hat{u}} \right) \right] \end{aligned}$$

DVMP

$$\begin{aligned} \mathcal{H}_{0-\lambda, \mu\lambda}^{P, \phi_{\pi p}} |_{\hat{t} \rightarrow 0} &\sim (2\lambda + \mu) f_{\pi} \mu_{\pi} C_F \alpha_S(\mu_R) \sqrt{-\frac{\hat{u}}{\hat{s}}} \left[\frac{e_a}{\hat{s}} + \frac{\hat{s}}{\hat{u}} \frac{e_b}{\hat{u}} \right] \int_0^1 \frac{d\tau}{\bar{\tau}} \phi_{\pi p}(\tau) \\ \mathcal{H}_{0-\lambda, \mu\lambda}^{P, C_F, \phi_{3\pi}} |_{\hat{t} \rightarrow 0} &\sim -(2\lambda + \mu) f_{3\pi} C_F \alpha_S(\mu_R) \sqrt{-\frac{\hat{u}}{\hat{s}}} \left(\frac{e_a}{\hat{s}} + \frac{\hat{s}}{\hat{u}} \frac{e_b}{\hat{u}} \right) \\ &\times \int_0^1 \frac{d\tau}{\bar{\tau}^2} \int_0^{\bar{\tau}} \frac{d\tau_g}{\tau_g(\bar{\tau} - \tau_g)} \phi_{3\pi}(\tau, \bar{\tau} - \tau_g, \tau_g) \\ \mathcal{H}_{0-\lambda, \mu\lambda}^{P, qqq, C_G} |_{\hat{t} \rightarrow 0} &\sim (2\lambda + \mu) f_{3\pi} C_G \alpha_S(\mu_R) \frac{Q^2}{\sqrt{-\hat{s}\hat{u}}} \left(\frac{e_a}{\hat{s}} + \frac{e_b}{\hat{u}} \right) \\ &\times \int_0^1 \frac{d\tau}{\bar{\tau}} \int_0^{\bar{\tau}} \frac{d\tau_g}{\tau_g(\bar{\tau} - \tau_g)} \phi_{3\pi}(\tau, \bar{\tau} - \tau_g, \tau_g) \end{aligned}$$

Spin effects - photoproduction

[Kroll, P-K '21]



$A_{LL}(K_{LL})$... correlation of the helicities of the photon and incoming (outgoing) nucleon

$$A_{LL}^{P,tw2} = K_{LL}^{P,tw2}$$

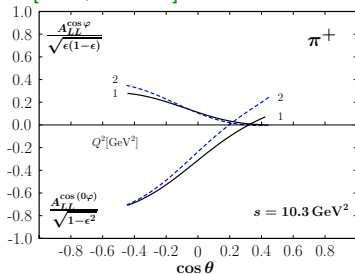
$$A_{LL}^{P,tw3} = -K_{LL}^{P,tw3}$$

→ characteristic signature for dominance of twist-3 (like $\sigma_T \gg \sigma_L$ in DVMP)

$A_{LS}(K_{LS})$... correlation of the helicities of the photon and sideways polarization of the incoming (outgoing) nucleon

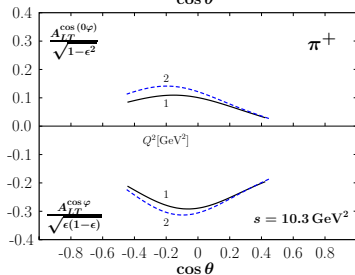
Spin effects - electroproduction

[Kroll, P-K '21]



$A_{LL}(K_{LL})$ have two modulations for electroproduction

(\rightarrow measured for DVMP [CLAS '15])



$A_{LT}(K_{LT})$... correlation between the lepton helicity and transversal target polarization