

Photo- and hadron-production of mesons

Łukasz Bibrzycki
on behalf of the JPAC collaboration

Pedagogical University of Krakow

19th International Conference on Hadron Spectroscopy and
Structure, Ciudad de México
26 July - 1 August 2021



Topics to be covered

I will focus on two topics recently studied by the JPAC collaboration:

- 1 High energy $\pi^- p \rightarrow \pi^- \eta^{(\prime)} p$ production
- 2 Photoproduction of resonances in the $\pi^+ \pi^-$ system

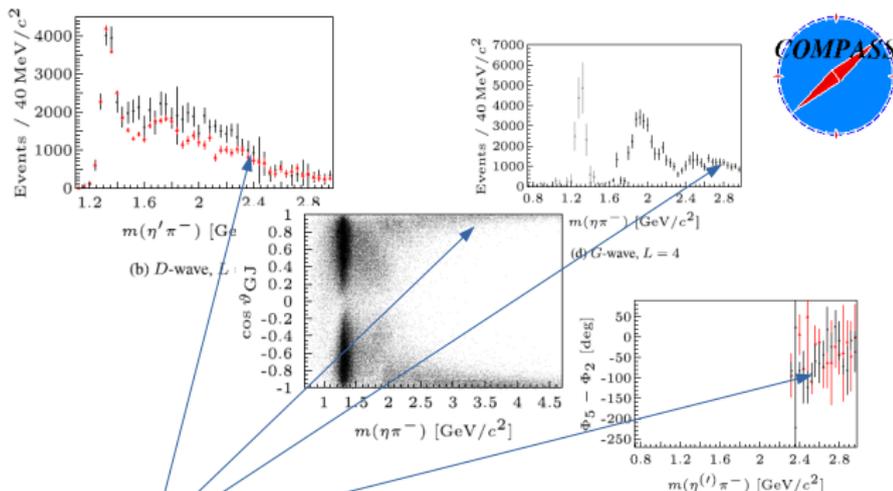


Motivation of the $\pi^- \eta^{(\prime)}$ channel study

- $\pi^- \eta^{(\prime)}$ pairs constitute a golden channel for the searches of hybrid exotics (odd partial waves are exotic)
- COMPASS experiment at CERN ([Adolph et al. PLB 740, 2015](#)) observed a strong forward-backward asymmetry in the $\pi^- \eta^{(\prime)}$ channels (stronger in the $\pi \eta'$ channel)
- the asymmetry is due to odd-even partial wave interference
- the strongest odd wave is the P -wave, which in the resonance region can be attributed to the π_1 hybrid
- relation between the high and low invariant mass region can be described in terms of Finite Energy Sum Rules (special kind of dispersion relations)



Experimental motivation



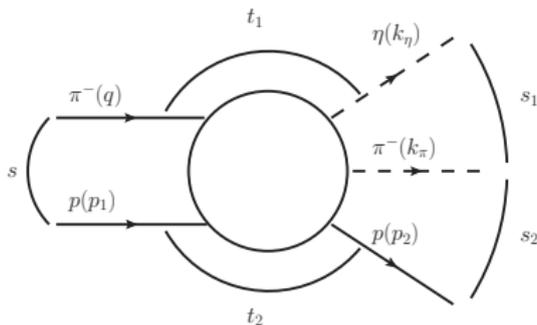
Objectives:

- Describe the $\pi^- \eta^{(\prime)}$ production above the resonance region.
- Identify dominant Regge exchanges and amplitude strengths.



Kinematics

- The $2 \rightarrow 3$ reaction (upolarized) is determined by 5 kinematical variables
- In Regge analysis it is customary to choose 5 Lorentz invariants, eg:
 $s = (q + p_1)^2$, $t_1 = (q - k_\eta)^2$, $t_2 = (p_1 - p_2)^2$, $s_1 = (k_\eta + k_\pi)^2$,
 $s_2 = (k_\pi + p_2)^2$.



- COMPASS analysis was performed in the Gottfried-Jackson frame, with θ and ϕ defining the direction of outgoing $\eta^{(\prime)}$
- In this frame $\cos \theta$ is related to t_1 and ϕ is related to s_2 (the other variables being s , s_1 and t_2).



Model vs. experimental data

- The COMPASS experiment operated with a fixed beam momentum of 191 GeV and t_2 was integrated in the region $t_2 \in [-1.0, -0.1] \text{ GeV}^2$.
- The invariant mass ($m = \sqrt{s_1}$) and angular dependent intensity was parametrized as:

$$I(m, \Omega)_{COMPASS} = \sum_{\epsilon=\pm 1} \left| \sum_{L,M} f_{LM}^{\epsilon}(m) \Psi_{LM}^{\epsilon}(\Omega) \right|^2,$$

where ϵ is the reflectivity (\approx naturality in high energy limit), kept $\epsilon=+1$ and

$$\Psi_{LM}^{\epsilon=+1}(\theta, \phi) = \sqrt{2} Y_{LM}(\theta, 0) \sin(M\phi)$$

$$f_{LM}^{\epsilon=+1}(m) = \sqrt{I_{LM}} e^{i\phi_{LM}}$$

where the I_{LM} and ϕ_{LM} are the COMPASS experimental partial wave intensities and phaseshifts (determined relative to ϕ_{21}).



Fitting experimental data at large invariant masses

- The easiest approach: fit the model partial waves to experimental ones

But:

- COMPASS analysis was based on partial wave expansion truncated at $L = 6$ and $M = 1$, even though it converges slowly for the $\pi\eta^{(\prime)}$ invariant masses above the resonance region,
- The intensity was normalized to the number of events in the mass bin.

Therefore:

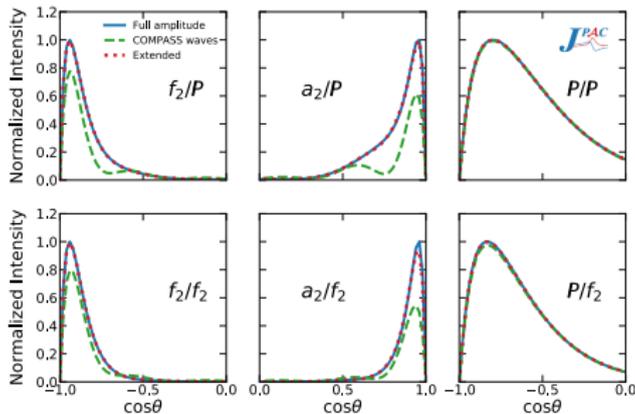
- The angular distribution constructed from the truncated partial wave expansion represents total yield.



Fitting experimental data at large invariant masses

On the model side

- Model intensities for full amplitudes and partial wave amplitudes truncated at $L = 6$ differ considerably.



Recipe:

- Fit the mass and angular dependent intensity.



Fitting experimental data at large invariant masses

- Practically we fit the extended log likelihood ([Barlow, Nucl.Instr.Meth. A 297, 1990](#))

$$\mathcal{L}_{\text{ext}} = \sum_{m_i} \int d\Omega [I_{JPAC}(m_i, \Omega) - I_{COMPASS}(m_i, \Omega) \log I_{JPAC}(m_i, \Omega)]$$

with model intensity defined as:

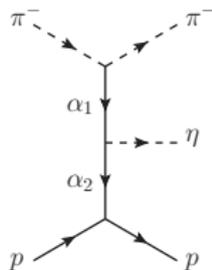
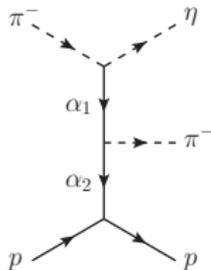
$$I_{JPAC}(m, z = \cos \theta, \phi) = q |T|^2 = q \left| \sum_{i=1}^6 a_i T^i(m_{\pi\eta}, z, \phi) \right|^2$$

where $q = \lambda^{1/2}(m^2, m_\pi^2, m_\eta^2)/m$.



Double Regge exchange model

- Leading natural exchanges



Type I - fast η

Type II - fast π

Type of diagram	α_1	α_2
I (fast η)	α_{a_2}	α_P
	α_{a_2}	α_{f_2}
II (fast π)	α_{f_2}	α_P
	α_{f_2}	α_{f_2}
	α_P	α_P
	α_P	α_{f_2}

- Individual diagram strengths depend on the 6 coupling triples:

$G_{a_2\pi\eta} G_{a_2\pi} P G_P N N$, $G_{a_2\pi\eta} G_{a_2\pi f_2} G_{f_2} N N$, $G_{f_2\pi\pi} G_{f_2\eta} P G_P N N$,
 $G_{f_2\pi\pi} G_{f_2\eta f_2} G_{f_2} N N$, $G_P \pi \pi G_\eta P P G_P N N$, $G_P \pi \pi G_{f_2\eta} P G_{f_2} N N$, wherein
 at least one coupling is unknown.

- Therefore we treat diagram strengths as parameters to be fitted.



General form of the amplitude

- Double reggeon exchange (we follow Shimada *et al.* NPB 142, 1978)

$$T = -K\Gamma(1 - \alpha_1)\Gamma(1 - \alpha_2)$$

$$\left[(\alpha' s)^{\alpha_1 - 1} (\alpha' s_2)^{\alpha_2 - \alpha_1} \xi_1 \xi_{21} \hat{V}_1 + (\alpha' s)^{\alpha_2 - 1} (\alpha' s_1)^{\alpha_1 - \alpha_2} \xi_2 \xi_{12} \hat{V}_2 \right]$$

where ξ_i and ξ_{ij} signature factors, \hat{V}_1

$$\hat{V}_1(\alpha_1, \alpha_2, \eta) = \frac{\Gamma(\alpha_1 - \alpha_2)}{\Gamma(1 - \alpha_2)} {}_1F_1(1 - \alpha_1, 1 - \alpha_1 + \alpha_2, -\kappa)$$

$$\hat{V}_2 = \hat{V}_1(\alpha_1 \leftrightarrow \alpha_2) \quad \text{with} \quad \kappa^{-1} \equiv s/(\alpha' s_1 s_2)$$

and $K = -4\sqrt{s_1}|q||k_\eta||p_2| \sin \theta_2 \sin \theta \sin \phi$

- Both α_1 and α_2 are of 2^{++} type so only positive signature and naturality.
- Regge trajectories:

$$\alpha_{f_2}(t) = 0.47 + 0.89t \quad \alpha_{a_2}(t) = 0.53 + 0.90t \quad \alpha_P(t) = 1.08 + 0.25t$$

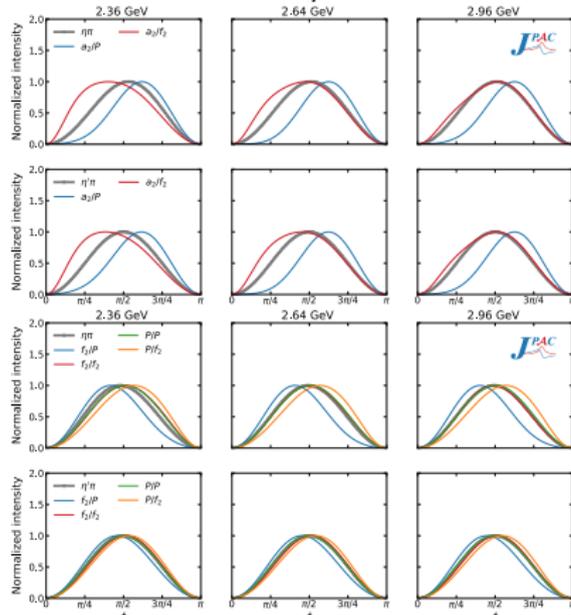
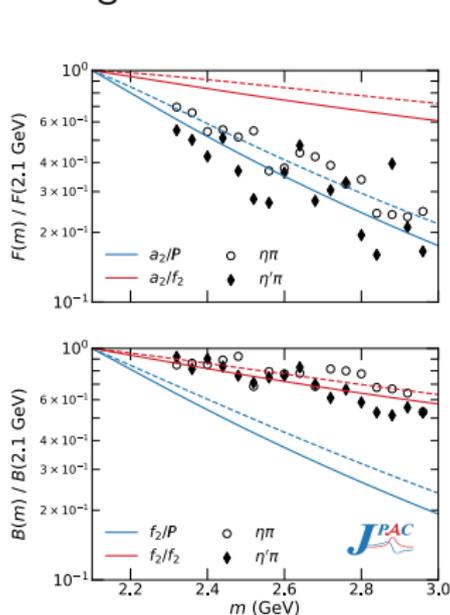


Fit results



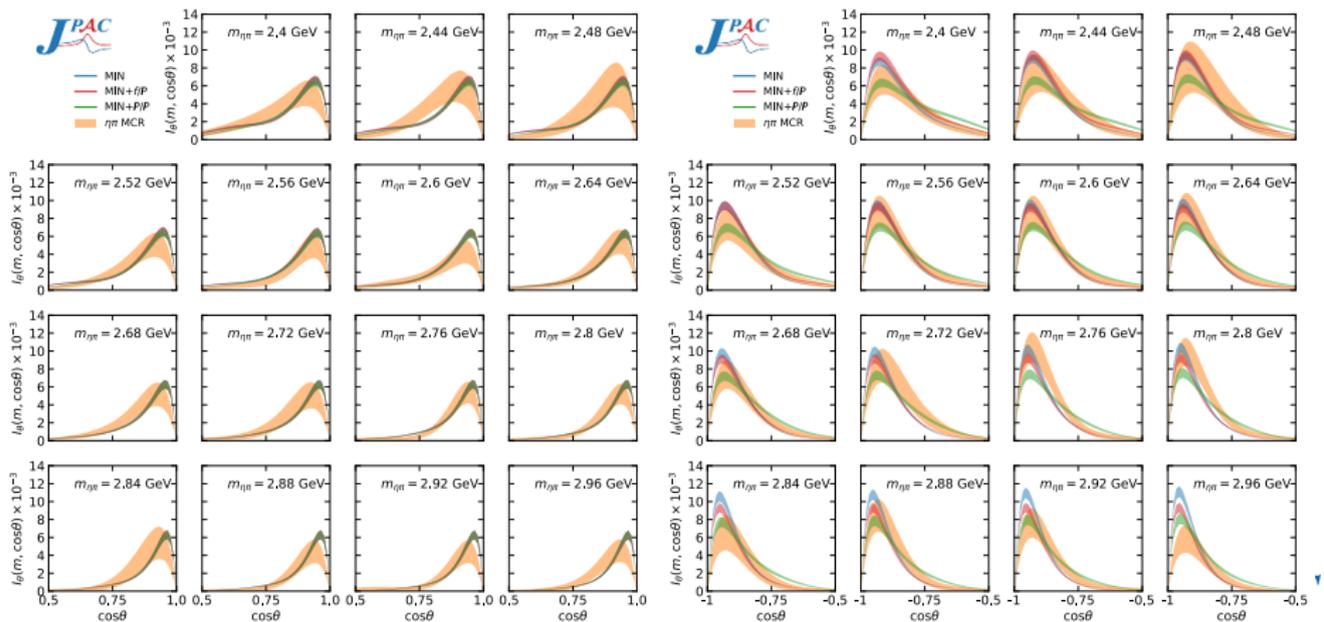
Minimal set of amplitudes

Fitting the full set of 6 amplitudes is statistically inconclusive.

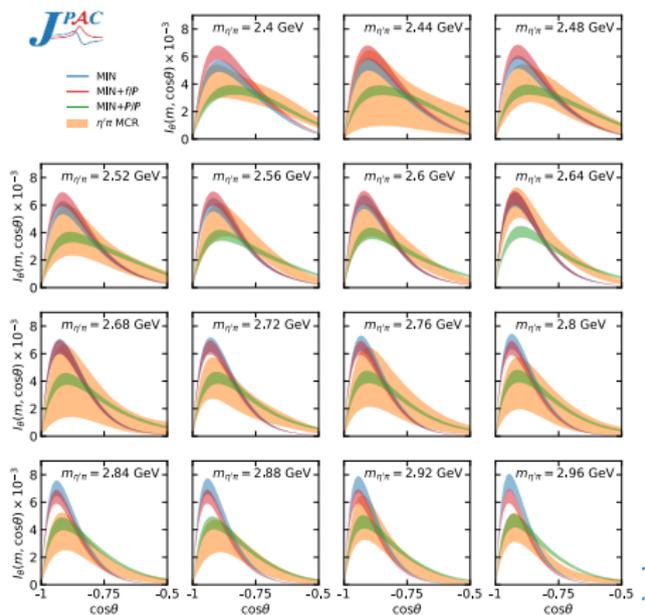
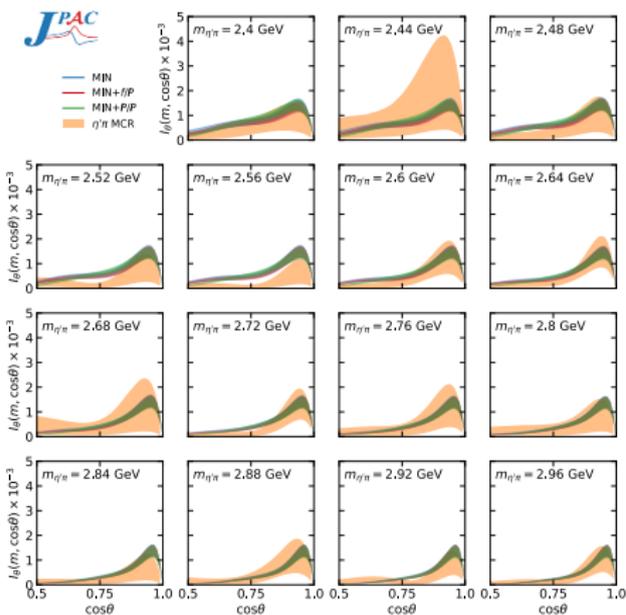


From the analysis of the forward and backward mass and ϕ distributions we infer that the minimal set of amplitudes should include a_2/P , a_2/f_2 and f_2/f_2 .

Forward and backward peaks for $\pi\eta$

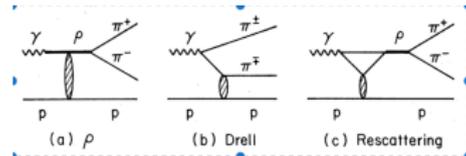
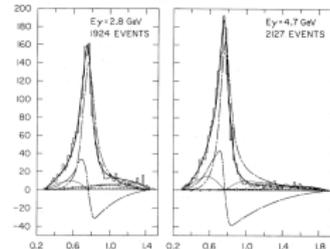
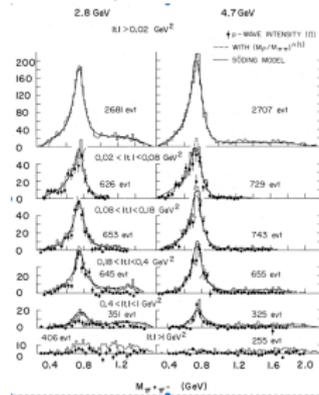
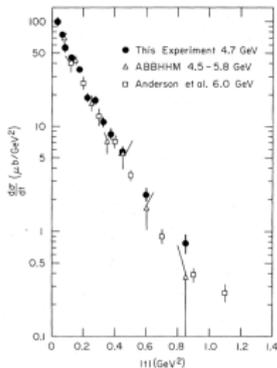


Forward and backward peaks for $\pi\eta'$



Motivation for the $\pi^+ \pi^-$ photoproduction study

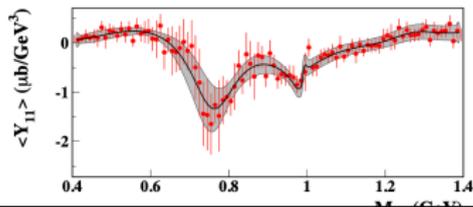
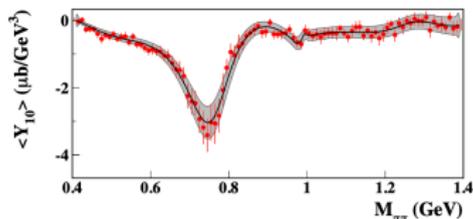
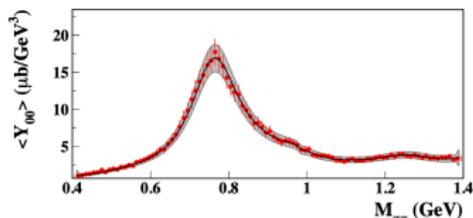
- Basic interpretation of the $\gamma p \rightarrow \pi^+ \pi^- p$ reaction was formulated in classical SLAC papers (Ballam et al, 197-)



- Diffractive peak in the $d\sigma/dt$ distribution,
- Line shape distorted due to interference with Drell background,
- These properties are grasped by Söding model (assumed diffractive πp scattering)

Motivation for the $\pi^+ \pi^-$ photoproduction study

- Decade ago the topic was revisited by the CLAS collaboration (Battaglieri et al. PRD 80, 2009)



New results:

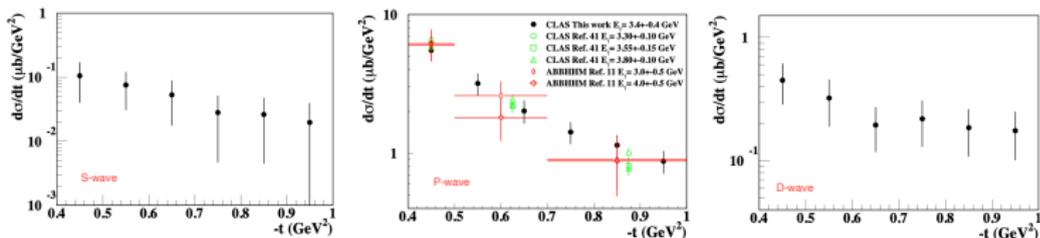
- Comprehensive analysis of the angular distribution with moments
- First observation of the $f_0(980)$ in the photoproduction



Motivation for the $\pi^+ \pi^-$ photoproduction study

Is there anything left to study ? It is !

- Assumption of diffractive πp scattering (Deck (1964), Söding (1966), Pumplin(1970)) is usually not valid,
- No uniform description of partial waves



-varying slopes suggest different production mechanisms.

- Coupled channel effects may be strong particularly in the S - and D -waves.
- Description of polarisation effects still in early stage (see [Mathieu, Pilloni et al. PRD 102, 2020](#)).



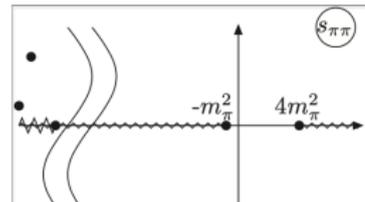
Unitarity compatible form of the $\gamma p \rightarrow \pi^+ \pi^- p$ amplitude

- Aitchinson and Bowler, J. Phys. G., 3, 1978 had shown that the general form of the unitarity compatible photoproduction amplitude reads:

$$M = M_{diffuse} e^{i\delta_{\pi\pi}} \cos \delta_{\pi\pi} + M_{compact} e^{i\delta_{\pi\pi}} \sin \delta_{\pi\pi}$$

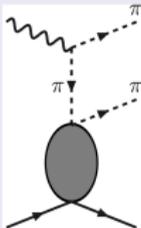
- $M_{diffuse}$ and $M_{compact}$ denote the production amplitudes where pion pair is produced from the compact or diffuse (asymptotically stretched) source
- In hadron physics a practical infinitely long interaction is achieved with exchanging the particle of smallest mass, which is pion.
- One pion exchange brings us to the Deck model.
- Short range interaction can be modelled by flat energy dependence so we put $M_{compact} = A + Bs_{\pi\pi}$.

t-channel exchange propagator	Fourier transform of the propagator
$1/(t - m^2)$	$\sim \frac{e^{-mr}}{r}$



Deck model - brief recap

Deck amplitude (Pumplin 1970)

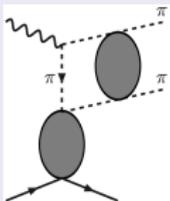


$$M_{\lambda_2 \lambda \lambda_1} = -e \left[\left(\frac{\epsilon_\lambda \cdot k_2}{q \cdot k_2} - \frac{\epsilon_\lambda \cdot (p_1 + p_2)}{q \cdot (p_1 + p_2)} \right) T_{\lambda_1 \lambda_2}^+ - \left(\frac{\epsilon_\lambda \cdot k_1}{q \cdot k_1} - \frac{\epsilon_\lambda \cdot (p_1 + p_2)}{q \cdot (p_1 + p_2)} \right) T_{\lambda_1 \lambda_2}^- \right]$$

Partial wave projection

$$\mathcal{M}_{\pi^+ \pi^-}^{lm}(\lambda_2 \lambda \lambda_1) = \frac{1}{\sqrt{4\pi}} \int d\Omega Y_{lm}^*(\Omega) M_{\lambda_2 \lambda \lambda_1},$$

Deck+FSI



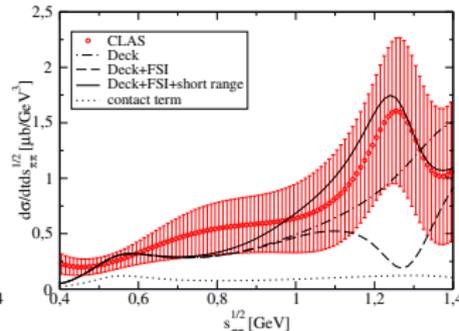
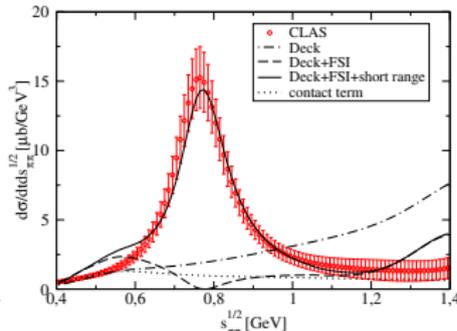
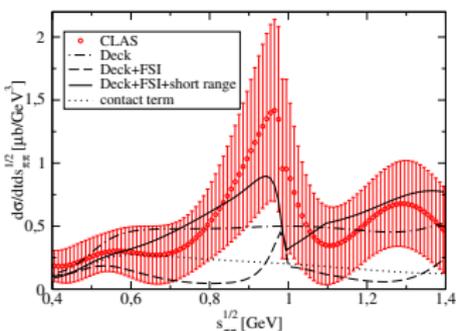
$$\mathcal{T}_{\pi^+ \pi^-}^{lm}(\lambda_2 \lambda \lambda_1) = (1 + i\rho t^l) \mathcal{M}_{\pi^+ \pi^-}^{lm}(\lambda_2 \lambda \lambda_1)$$

Deck model - brief recap

- To describe the πp interaction we use the SAID amplitudes (in ongoing analysis we use amplitudes from [Mathieu et al. PRD 92, 2015](#))
- We use the model of $\pi\pi$ FSI from [Bydžovský et al. PRD 94, 2016](#).
- The only parameters to be fitted are A and B coefficients in the linear approximation of the short range amplitude.
- Deck amplitude is essentially parameter free, thus enables precise determination of the short range contribution.

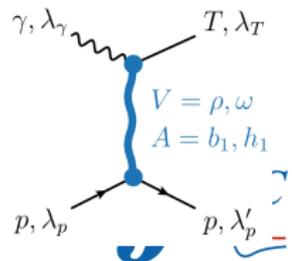


Model predictions vs. CLAS data



Work in progress:

- Better description of the short range component, eg. through Regge exchange [Mathieu et al. PRD 102, 2020](#)
- Prediction of polarized moments of angular distribution for CLAS12 and GlueX (talk by Nicholas Zachariou of CLAS12 earlier today).



Thank you for your attention

