



Next generation nuclear PDFs and their relevance to hadron structure

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**XUNTA
DE GALICIA**

What the nuclear PDFs are?

Based on the collinear factorization of QCD:

$$d\sigma^{AB \rightarrow k+X} \stackrel{Q \gg \Lambda_{\text{QCD}}}{=} \sum_{i,j,X'} f_i^A(Q^2) \otimes d\hat{\sigma}^{ij \rightarrow k+X'}(Q^2) \otimes f_j^B(Q^2) + \mathcal{O}(1/Q^2)$$

The coefficient functions $d\hat{\sigma}^{ij \rightarrow k+X'}$ are calculable from perturbative QCD...

PDFs are *universal*, process independent, and obey the DGLAP equations

$$Q^2 \frac{\partial f_i^A}{\partial Q^2} = \sum_j P_{ij} \otimes f_j^A$$

How do we get the $f_i^{p/A}$?

- **Physical models:** too numerous to describe here – ‘Everybody’s Model is Cool’
- **Extract from lattice:** problematic due to the PDF definition on the light cone
- **Fit to data:** parametrize the x - and A -dependence – **the global analysis approach**

... but the parton distribution functions f_i^A, f_j^B contain long-range physics and cannot be obtained by perturbative means

For a nucleus A , one can decompose

$$f_i^A(x, Q^2) = \overset{\text{bound-proton PDF}}{Z f_i^{p/A}(x, Q^2)} + \overset{\text{bound-neutron PDF}}{(A-Z) f_i^{n/A}(x, Q^2)},$$

and assume $f_i^{p/A} \overset{\text{isospin}}{\longleftrightarrow} f_j^{n/A}$

Nuclear modification factors

Nuclear PDFs (nPDFs) often described in terms of

$$f_i^{p/A}(x, Q^2) = R_i^{p/A}(x, Q^2) f_i^p(x, Q^2)$$

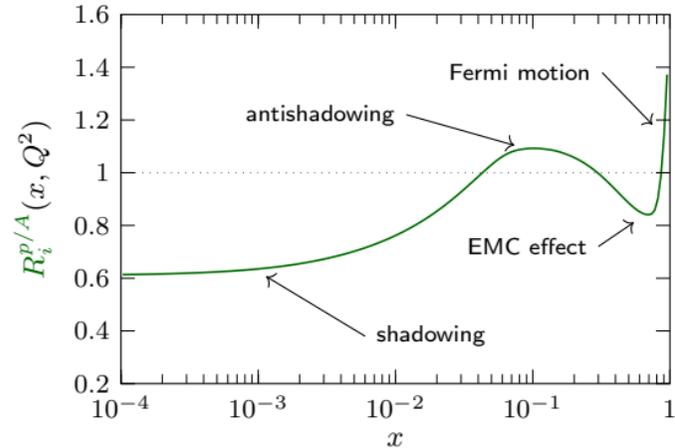
bound-proton PDF nuclear modification free-proton PDF

where $R_i^{p/A}$ exhibits the typical shape of

- Fermi motion at $x > 0.7$
- EMC (European Muon Collaboration) effect at $0.3 < x < 0.7$
- Antishadowing at $0.03 < x < 0.3$
- Shadowing at $x < 0.03$

where x is the fraction of nucleon momentum carried by the parton

These effects were originally discovered in deep-inelastic scattering (DIS) experiments, but have since been verified also in other perturbative processes (nPDF universality)

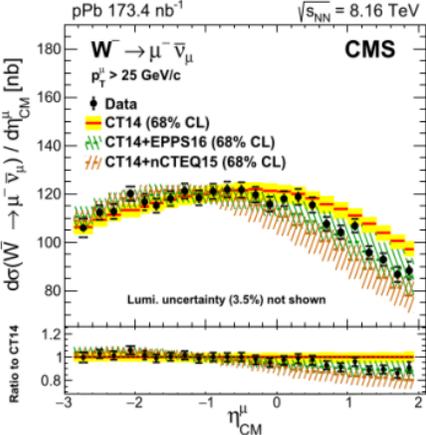
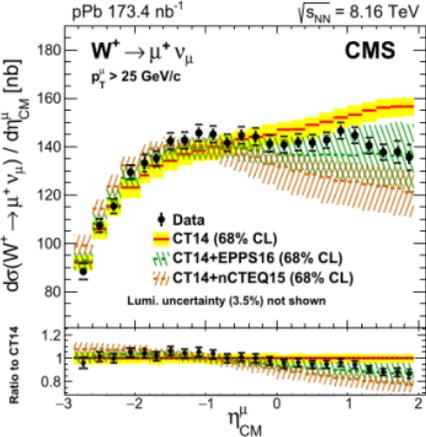


Latest and next generation NLO nPDF global fits

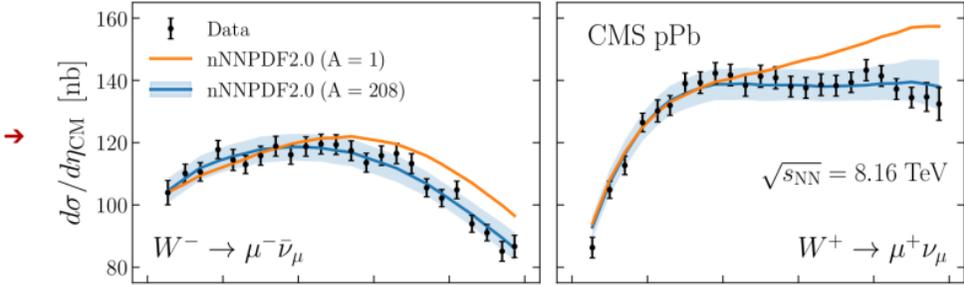
	EPS16	nNNPDF2.0	nCTEQ15WZ	nCTEQ15HIX	EPS21 <i>prelim.</i>
IA NC DIS	✓	✓	✓	✓	✓
+ JLab NC DIS				✓	✓ <i>new!</i>
ν A CC DIS	✓	✓			✓
pA DY	✓		✓	✓	✓
π A DY	✓				✓
RHIC dAu/pp π^0	✓		✓		✓
LHC pPb dijet R_{FB}	✓				
→ dijet R_{pPb}					✓ <i>new!</i>
LHC pPb D^0					✓ <i>new!</i>
LHC pPb W,Z Run 1	✓	✓	✓		✓
+ Run 2 pPb W		✓	✓		✓ <i>new!</i>
Q cut in DIS	1.3 GeV	1.87 GeV	2 GeV	1.3 GeV	1.3 GeV
Data points	1811	1467	828	1564	2023 <i>prelim.</i>
Free parameters	20	256	19	19	24 <i>prelim.</i>
Error analysis	Hessian	Monte Carlo	Hessian	Hessian	Hessian
Error tolerance $\Delta\chi^2$	52	N/A	35	35	35 <i>prelim.</i>
Free-proton PDFs	CT14	NNPDF3.1	~CTEQ6M	~CTEQ6M	CT18A <i>prelim.</i>
HQ treatment	S-ACOT	FONLL	S-ACOT	S-ACOT	S-ACOT
Indep. flavours	6	6	5	4	6
Reference	EPJC 77, 163	JHEP 09, 183	EPJC 80, 968	PRD 103, 114015	TBA

W bosons in pPb at 8.16 TeV

[CMS, Phys.Lett.B 800 (2020) 135048]



[Abdul Khalek, Ethier, Rojo & van Weelden, JHEP 09 (2020) 183]



Potential probes of the flavour separation (and strangeness):

- $u\bar{d} (u\bar{s}, c\bar{s}) \rightarrow W^+$
- $d\bar{u} (s\bar{u}, s\bar{c}) \rightarrow W^-$

Remember: small- x , high- Q^2 quarks and gluons correlated by DGLAP evolution → constraints for gluons

Increased statistics for W bosons in the 8.16 TeV data set

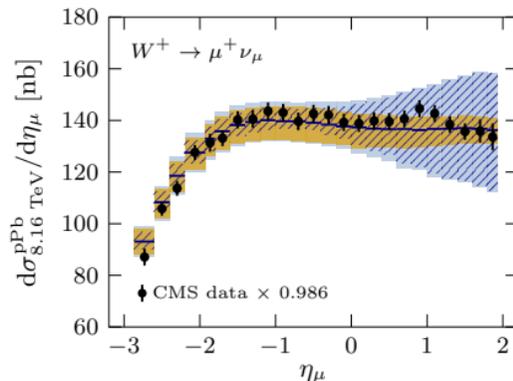
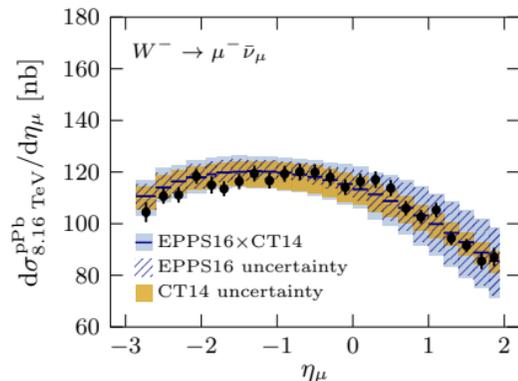
→ Included in nNNPDF2.0 and nCTEQ15WZ

Need to mitigate free-proton PDF uncertainty

Absolute cross sections carry large proton-PDF uncertainty!

Difficult to disentangle nuclear modifications from the proton d.o.f.s

We could use the data as:



- **Absolute cross sections**

- susceptible to the proton-PDF uncertainties, should be accounted in the fit

- **Self-normalized cross sections**

- cancel overall-normalization uncertainty, some proton-PDF uncertainties bound to remain

- **Forward-to-backward ratios**

- more direct cancellation of the proton-PDF uncertainties, lose some data points

- **Nuclear modification ratios (with 8.0 TeV pp)**

- expect good cancellation of the proton-PDF uncertainties, additional experimental uncertainties from the proton-proton measurement

as in nNNPDF2.0, nCTEQ15WZ

as in EPPS16

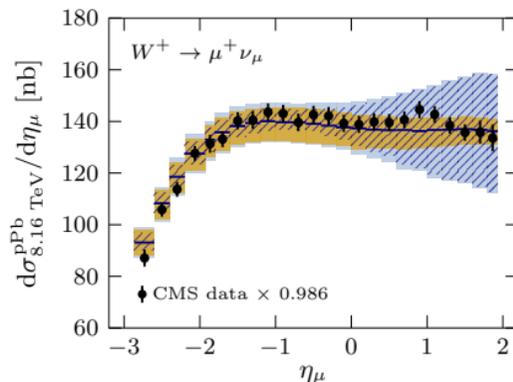
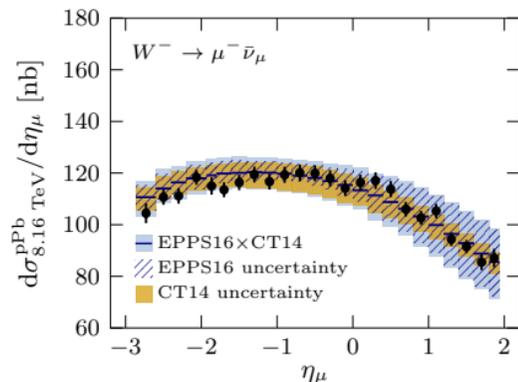
the current plan for EPPS21

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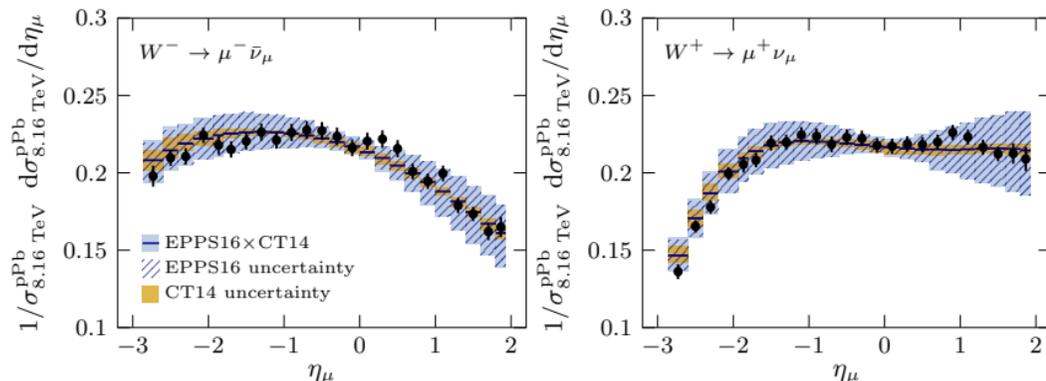
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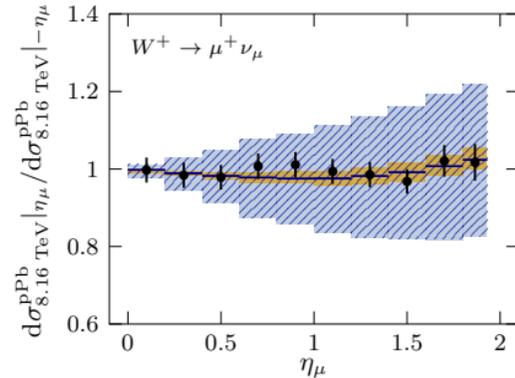
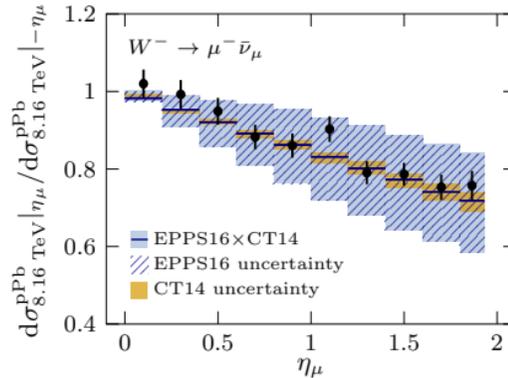
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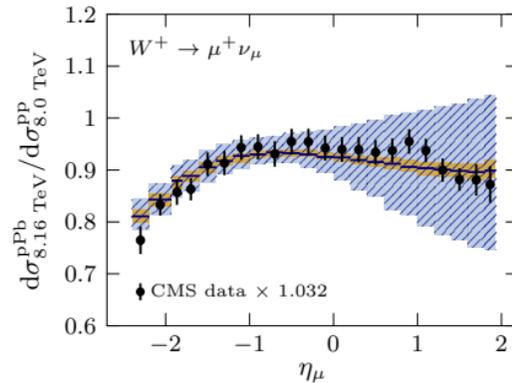
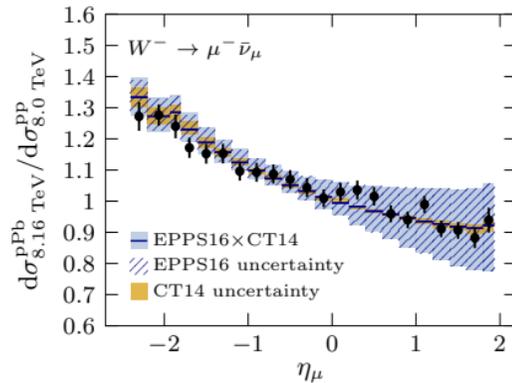
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the current plan for EPPS21

How to propagate proton-PDF uncertainties into nPDF fit?

Use a theoretical covariance matrix method

see [Abdul Khalek *et al.*, *Eur.Phys.J.* C79 (2019) 931]

$$\chi^2 = (D - f_N T)^T (C + S^{CT14})^{-1} (D - f_N T) + \left(\frac{f_N - 1}{\sigma_N} \right)^2,$$

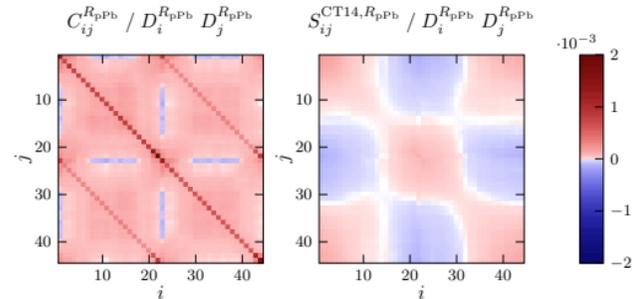
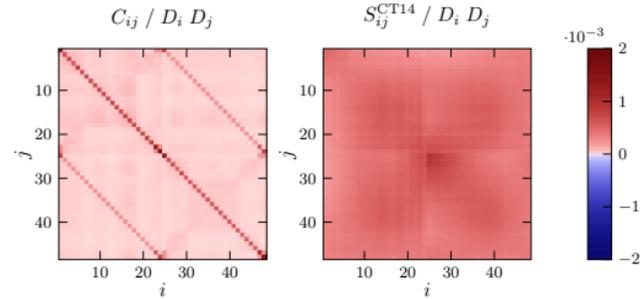
where the CT14 covariances are calculated with

$$S_{ij}^{CT14} = \sum_k \frac{y_i [S_{CT14,k}^+] - y_i [S_{CT14,k}^-]}{2 \times \underbrace{1.645}_{90\% \rightarrow 68\% \text{ conf. level}}} \frac{y_j [S_{CT14,k}^+] - y_j [S_{CT14,k}^-]}{2 \times 1.645}$$

We can also propagate the covariances into those of other observables via

$$C^{new} = J C J^T,$$

where J is the Jacobian of the transformation



Note: It is the strong *positive* correlations which make the uncertainty reduction with ratios possible!

Reweighting results

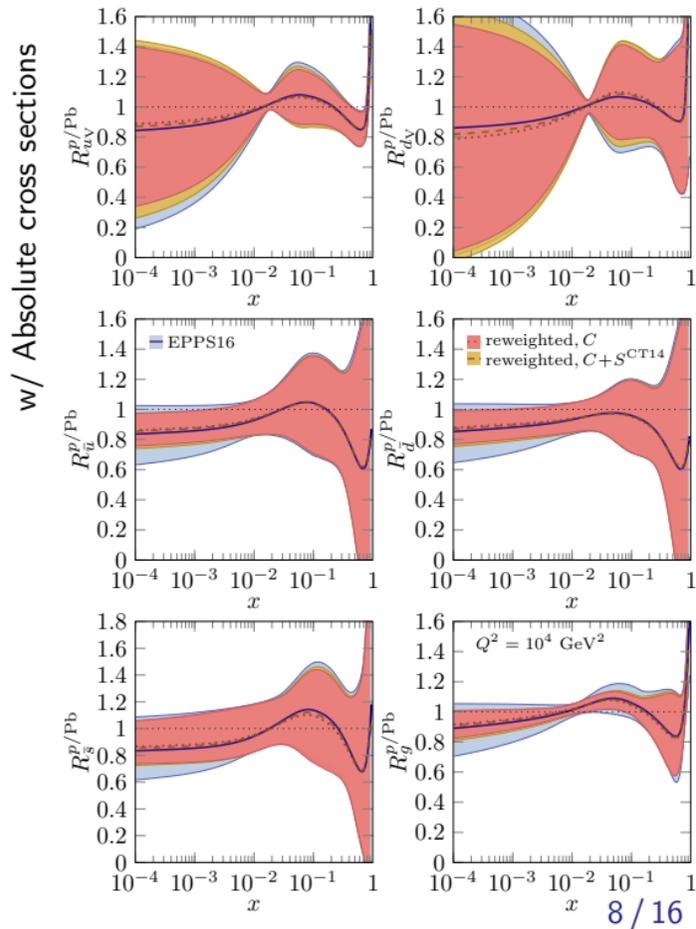
Study the impact on nuclear PDFs with the Hessian reweighting method

see [Paukkunen & Zurita, JHEP 12 (2014) 100]

Largest impact at the parametrization scale on gluons (probed through $g \rightarrow q\bar{q}$ splittings)

Proton-PDF uncertainties appear to be important only for the valence flavour separation

- can be reduced by using the ratio observables
- may still become relevant with the increased data precision at LHC Run 3
- possible consequences for the attempts to constrain EMC-effect models



Reweighting results

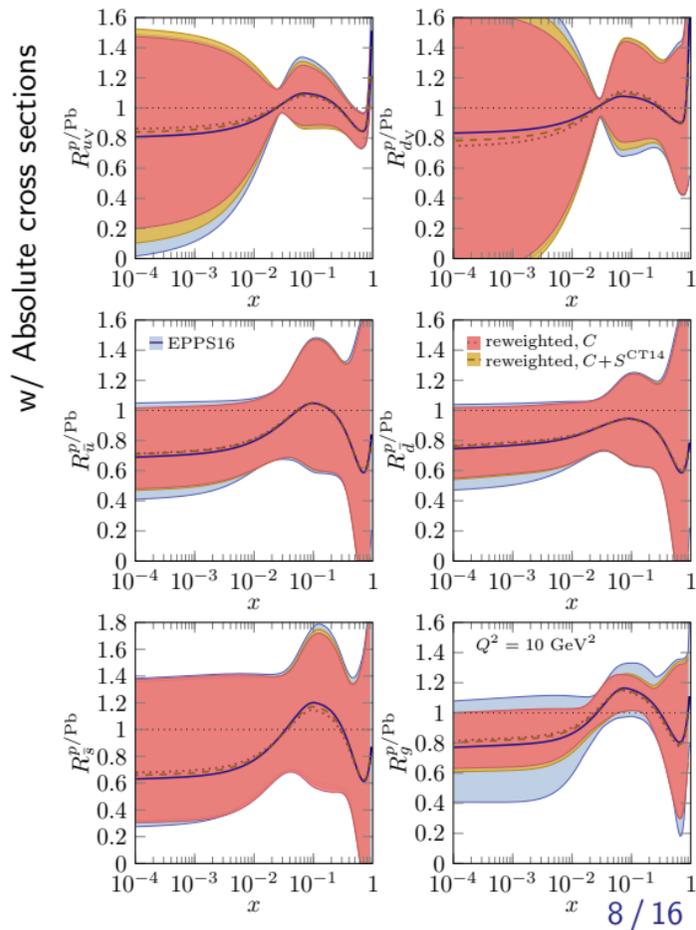
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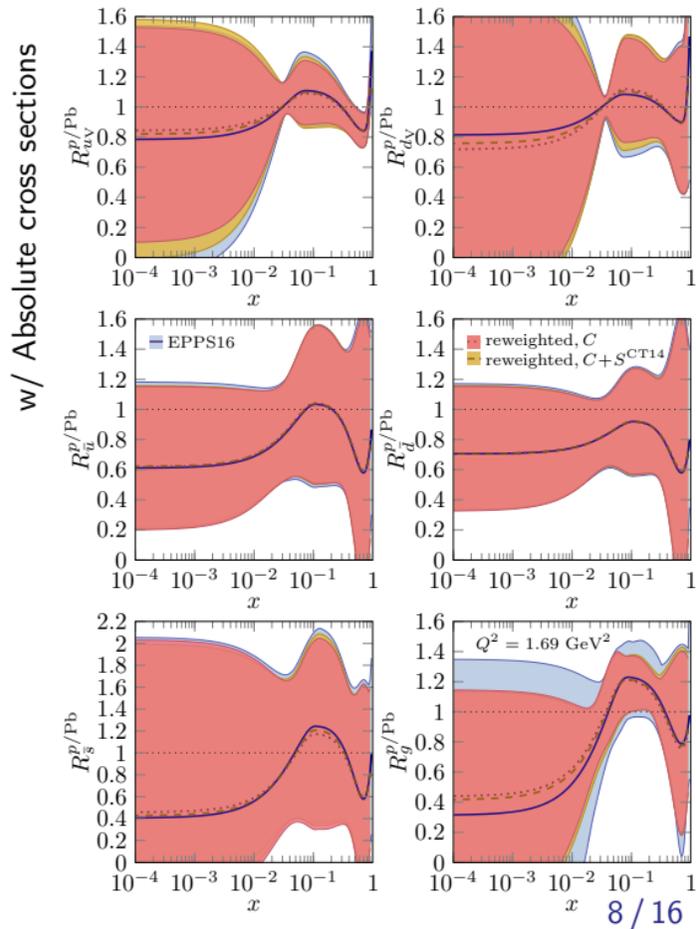
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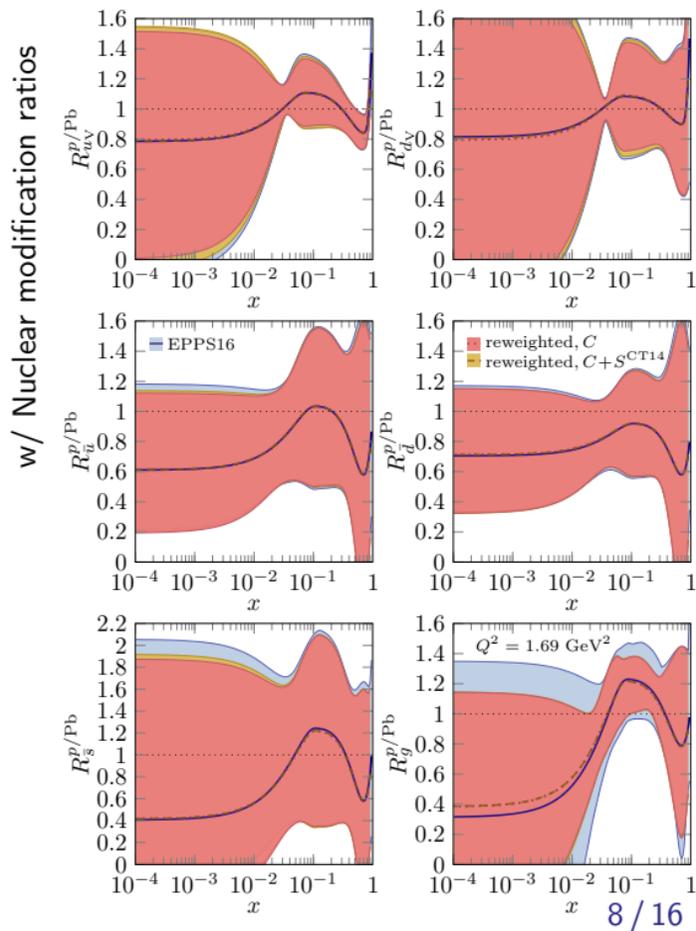
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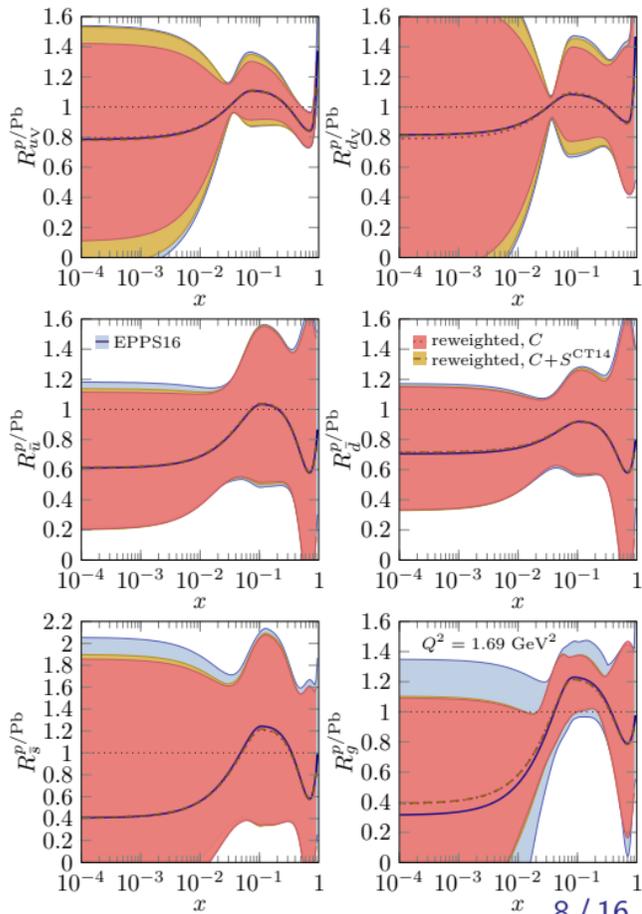
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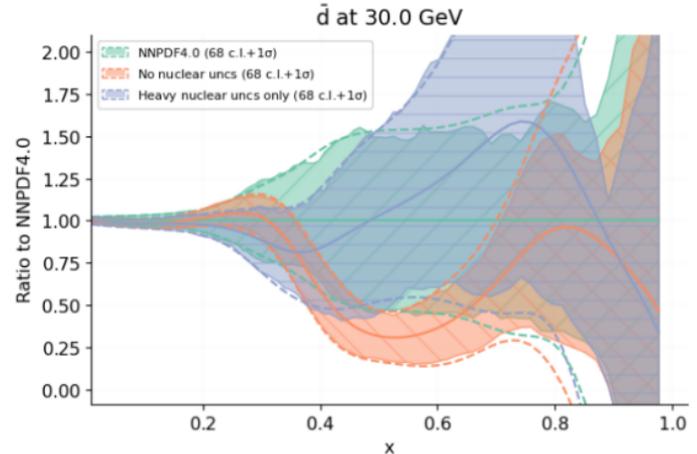
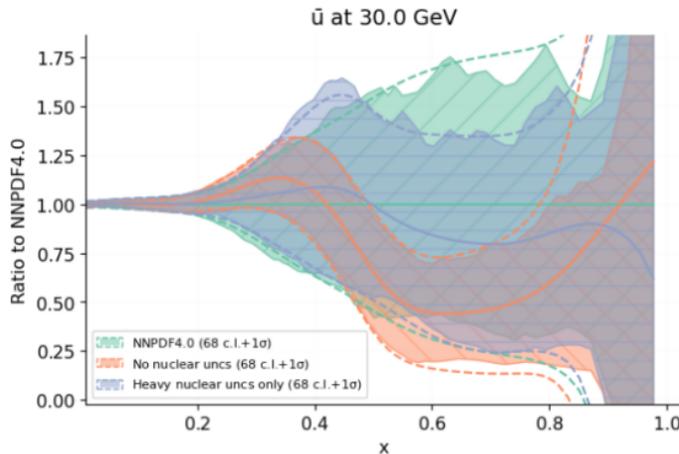
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w/ Mock data with reduced stat. uncertainties



Detour: Nuclear uncertainties in proton-PDF analyses

[Pearson, Ball & Nocera, arXiv:2106.12349, see also Eur.Phys.J.C 79 (2019) 282]



Also proton-PDF analyses rely on heavy nuclear data (fixed-target DIS and DY)

→ Large- x flavour separation depends on (assumed/fitted) nuclear corrections and uncertainties

■ Might find a need for a proton+nPDF master analysis, or an iterative procedure

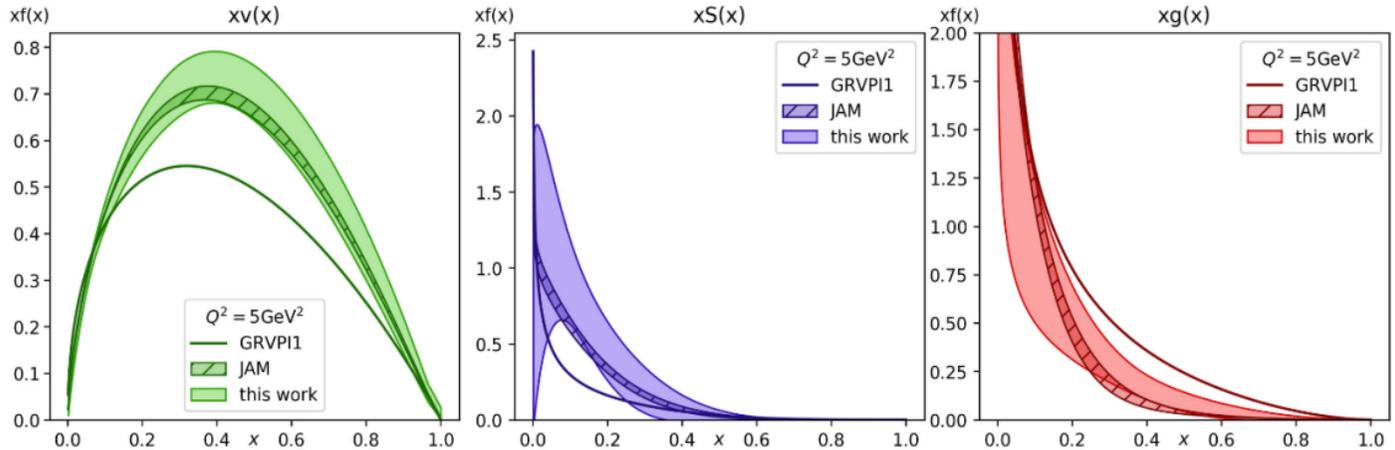
see [Ball, Nocera & Pearson, Eur.Phys.J.C 81 (2021) 37]

■ New data from non-heavy targets and understanding deuterium corrections extremely important

see plenary talks by Paul E. Reimer and Timothy Hobbs

Detour: Nuclear uncertainties in pion-PDF analyses

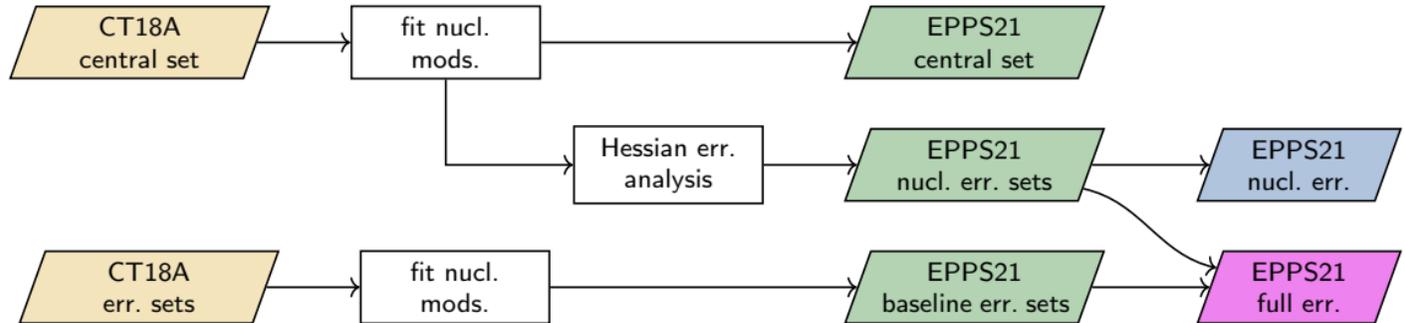
[Notikov *et al.*, *Phys.Rev.D* 102 (2020) 014040]



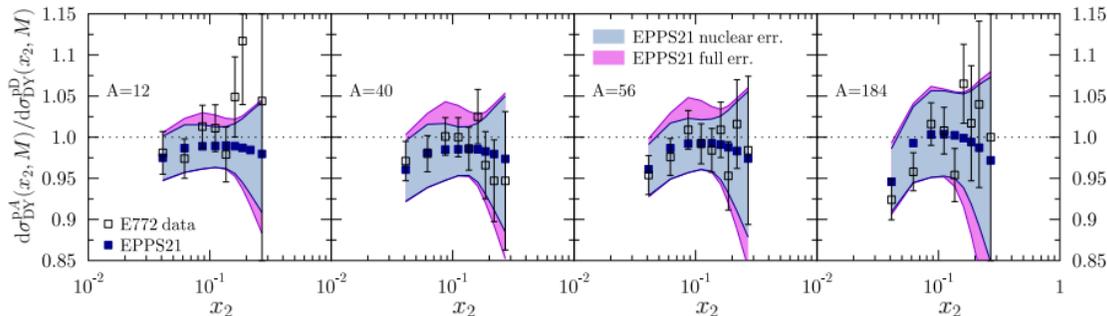
PDFs of charged pions are obtained from pion-nucleus DY and direct photon data

- Much larger errors when nuclear uncertainties are accounted for
... but note that different data are used in the fits
- Pion-PDF uncertainties become correlated with the nuclear ones
- ! Need for a way to consistently propagate the cross-correlated uncertainties to observables

We study baseline-PDF sensitivity by fitting nuclear modifications separately for each CT18A error set



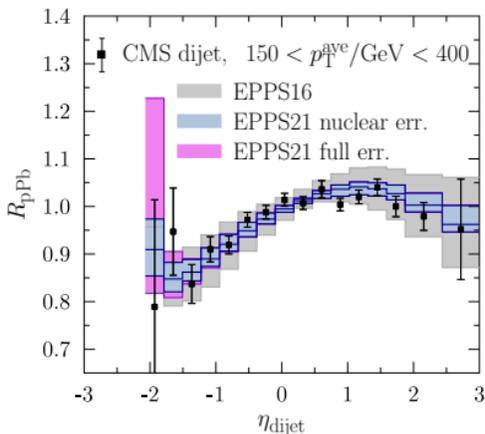
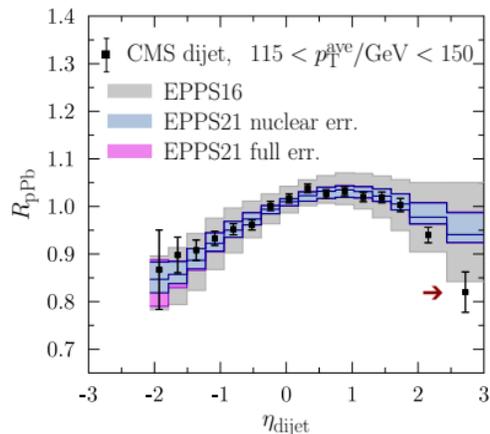
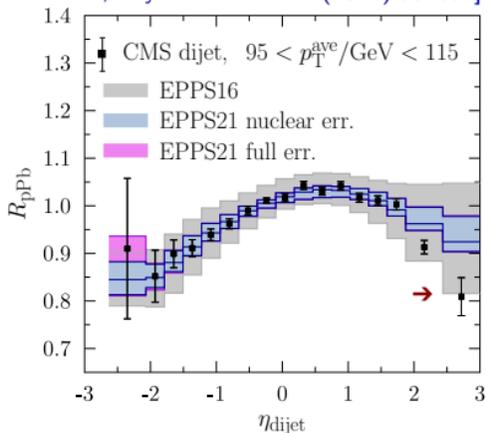
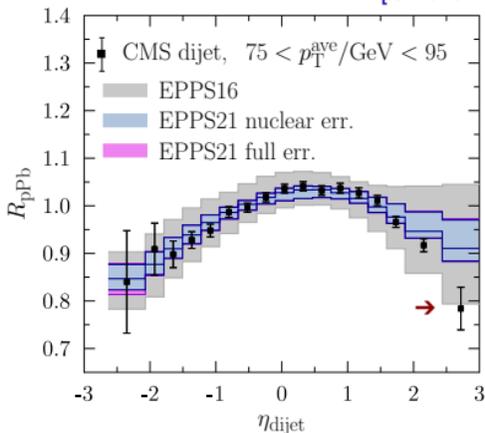
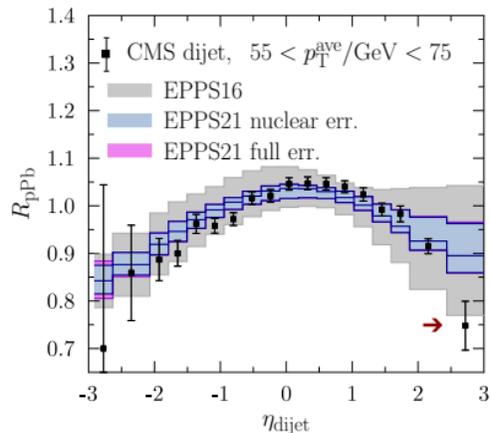
Baseline error mostly subdominant in the observables we fit, but shows up e.g. in the fixed-target DY



Dijets at 5.02 TeV *new!*

preliminary results,
Ref: [Eskola, PP, Paukkunen & Salgado, arXiv:2106.13661]

data from: [CMS Collaboration, Phys.Rev.Lett. 121 (2018) 062002]



Results in line with
the reweighting study

[Eskola, PP & Paukkunen,
Eur.Phys.J.C 79 (2019) 511]

Still finding it difficult to fit
the forwardmost data points

→ currently excluded
from the fit

D^0 s at 5.02 TeV – backward *new!*

Excellent fit!

Results in line with the reweighting study

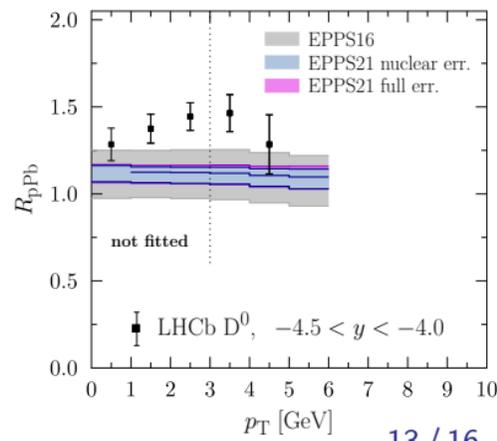
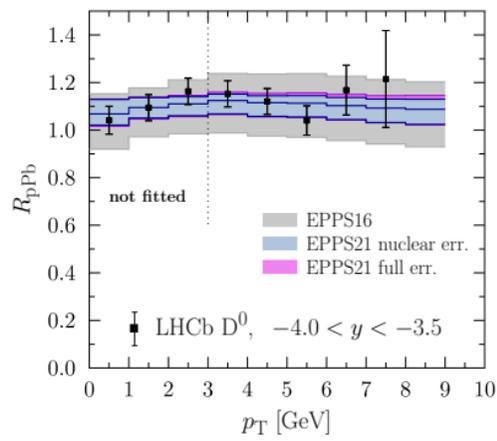
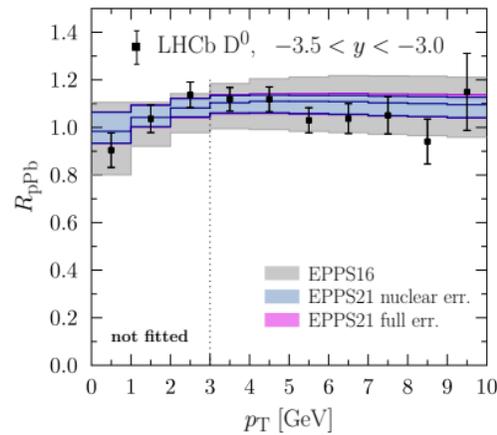
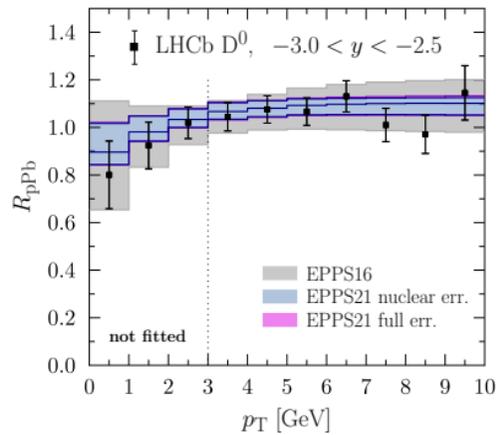
[Eskola, Helenius, PP & Paukkunen, JHEP 05 (2020) 037]

Using the NLO pQCD S-ACOT- m_T GM-VFNS

[Helenius & Paukkunen, JHEP 05 (2018) 196]

Using a $p_T > 3$ GeV cut to reduce theoretical uncertainties

data from: [LHCb Collaboration, JHEP 10 (2017) 090]



D^0 s at 5.02 TeV – forward *new!*

Ref: [Eskola, PP, Paukkunen & Salgado, arXiv:2106.13661] preliminary results,

Excellent fit!

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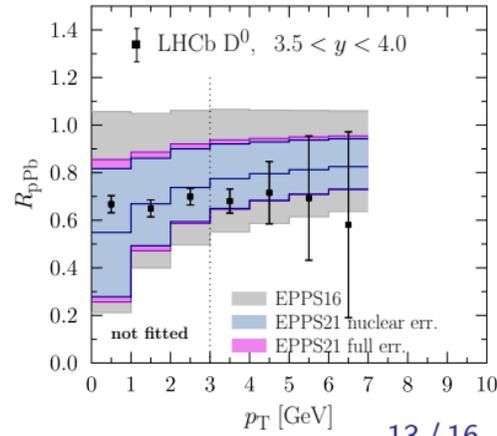
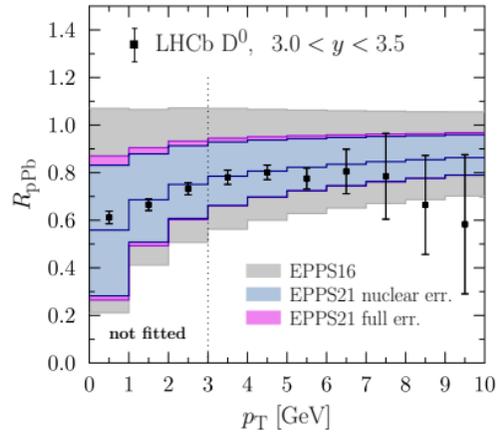
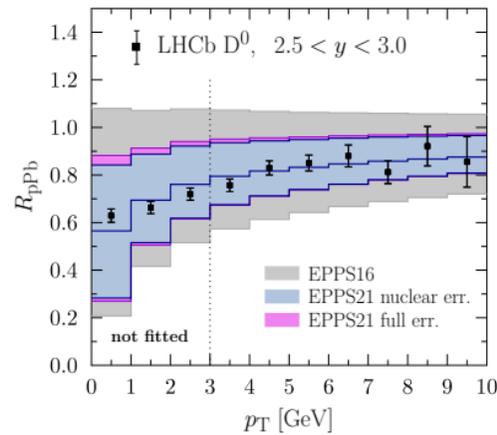
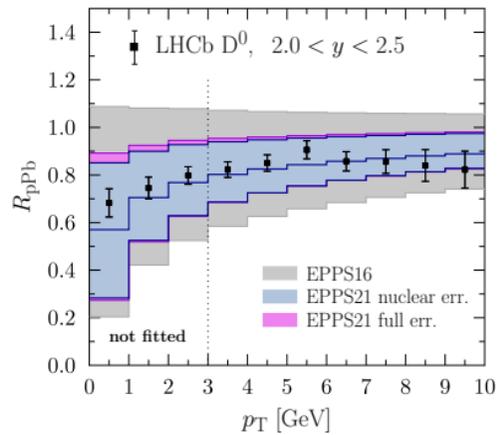
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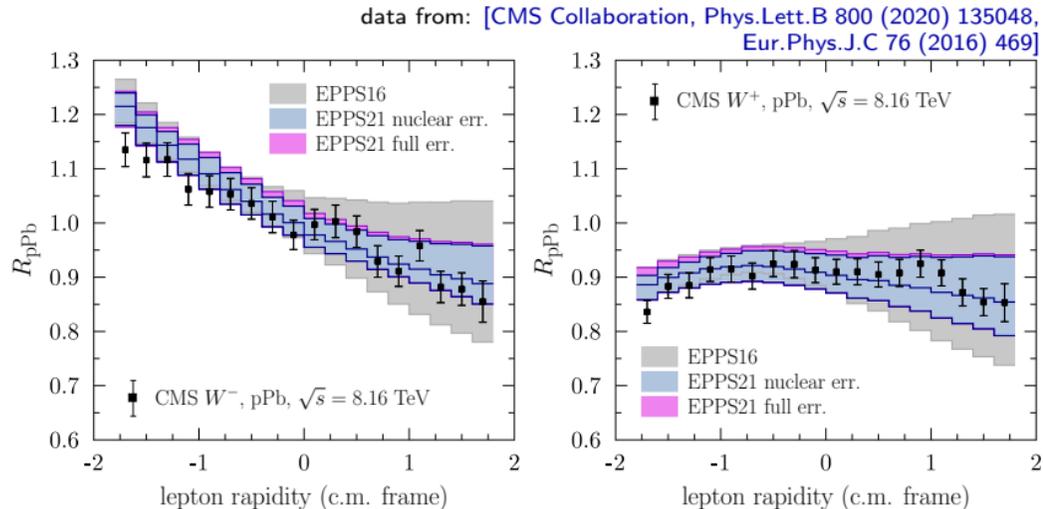


Excellent fit!

Using the mixed-energy nuclear modification ratio

$$R_{pPb} = \frac{d\sigma_{8.16 \text{ TeV}}^{pPb}/d\eta_\mu}{d\sigma_{8.0 \text{ TeV}}^{pp}/d\eta_\mu}$$

to cancel the free-proton PDF uncertainty



Fully consistent with the dijets and D^0 s

- Important check on the nPDF universality & factorization

These data do not appear to give additional flavour-separation constraints on top of those we had already in EPPS16

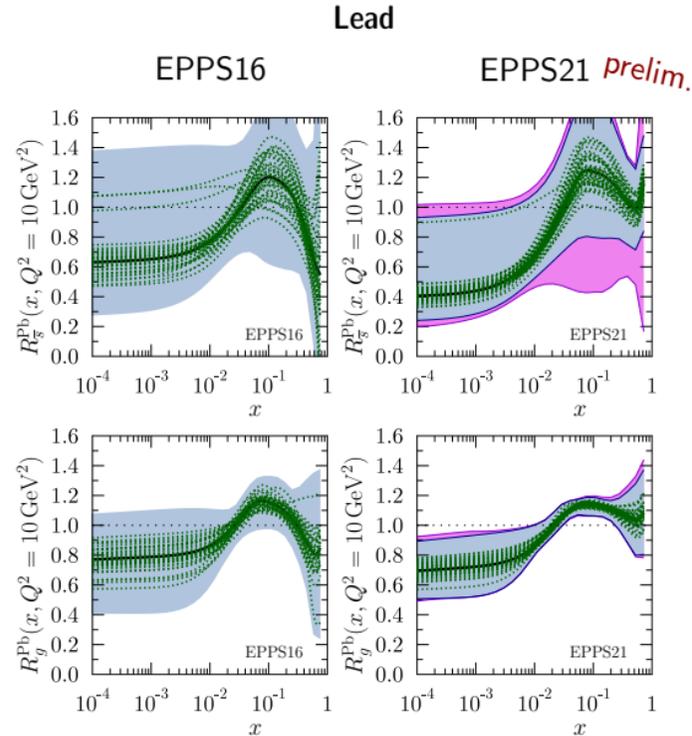
- Looking forward to increased precision at LHC Run 3

Flavour separation (esp. strangeness) remains a difficult beast to tame

- Not enough data to put stringent constraints on a flavour by flavour basis
- Some sensitivity to proton-PDF uncertainties

Significant reduction in the gluon uncertainties!

- Driven by dijet and D^0 data, but consistent with W s
- Strong evidence for mid- x antishadowing and small- x shadowing



Summary

Next generation nuclear PDFs will include a large set of data from the LHC pPb collisions

- A new EPPS nPDF fit on its way...
- New constraints on gluon modifications in lead → strong evidence for (anti)shadowing!
- Flavour separation uncertainties still remain large

With increasing precision the free-proton PDF uncertainties become more important

- Can use data as suitable ratios to reduce the uncertainty and decorrelate nuclear-modification and free-proton d.o.f.s
- Residual free-proton PDF uncertainty can still be relevant e.g. for the flavour separation

Nuclear data also used in proton and pion PDF analyses

- Nuclear uncertainties can be large and are taken into account in some analyses but not all
- For accurate predictions it would be needed to provide the correlations to the general user

Backup

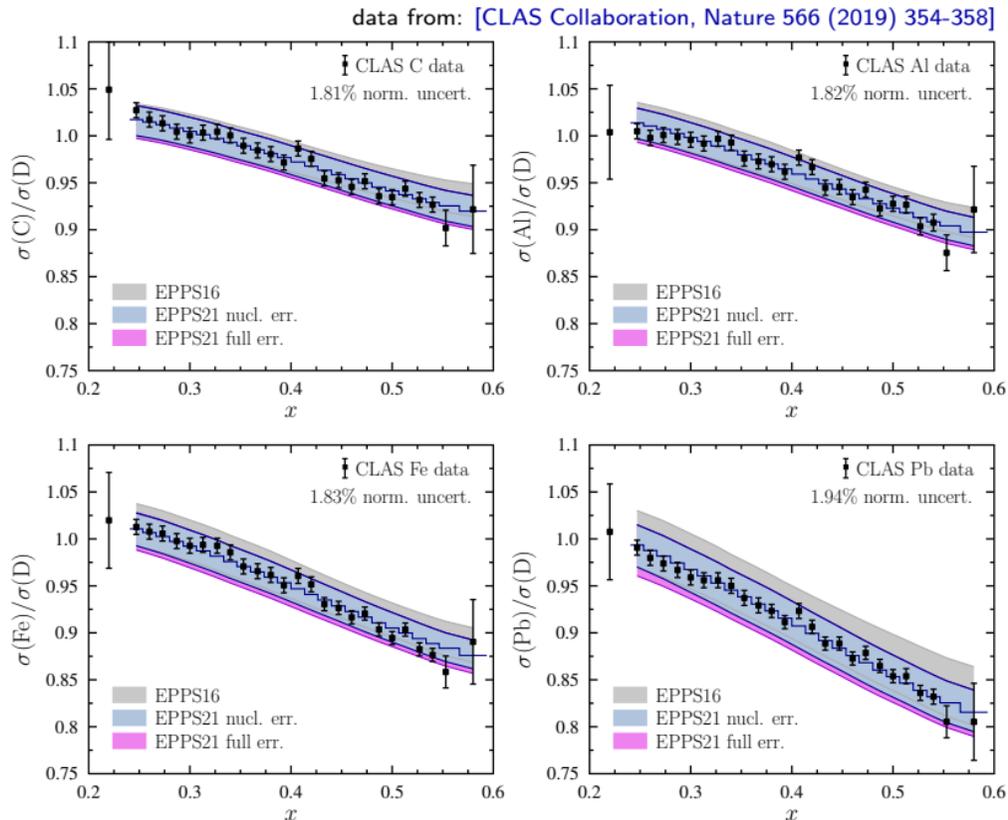
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the reweighting study

[Paukkunen & Zurita,
Eur.Phys.J.C 80 (2020) 381]

We take into account
the leading target-mass
corrections

No sign of isospin-dependence
in the bound-proton
nuclear modifications $R_i^{p/A}$



Fit results – valence

preliminary results,
Ref: [Eskola, PP, Paukkunen & Salgado, arXiv:2106.13661]

Bound-proton modifications *Prelim.*

Carbon

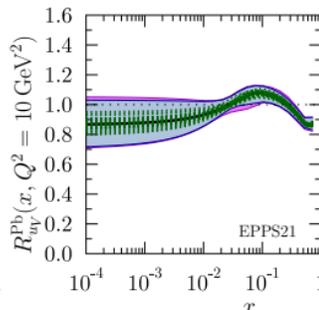
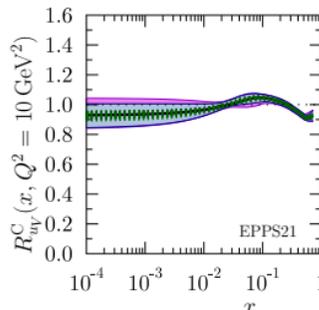
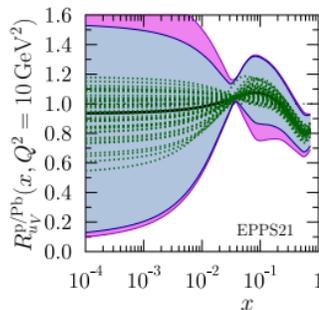
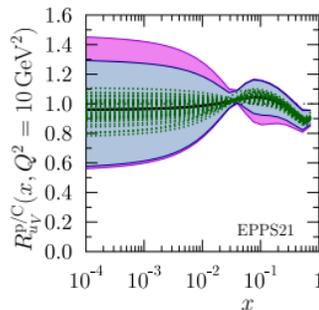
Lead

Full-nucleus modifications *Prelim.*

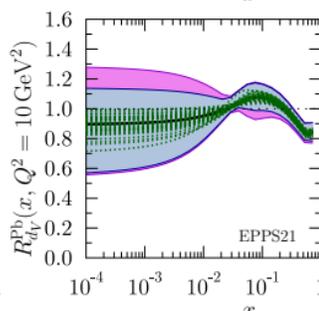
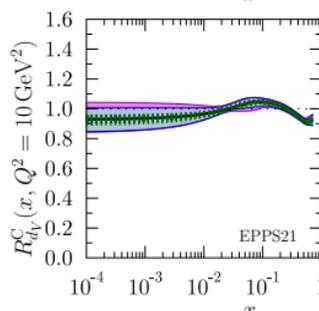
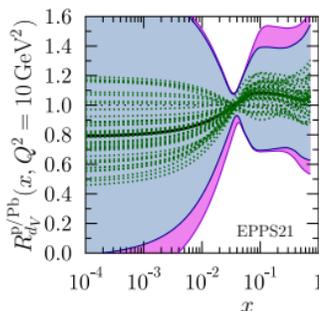
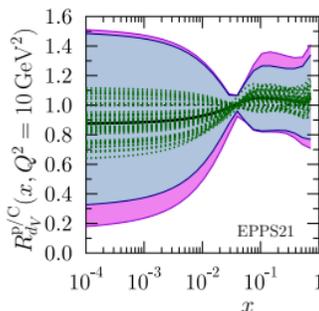
Carbon

Lead

u_V



d_V



$$R_i^{p/A} = \frac{f_i^{p/A}}{f_i^p}$$

$$R_i^A = \frac{Z f_i^{p/A} + N f_i^{n/A}}{Z f_i^p + N f_i^n}$$

Bound-proton modifications *Prelim.*

Carbon

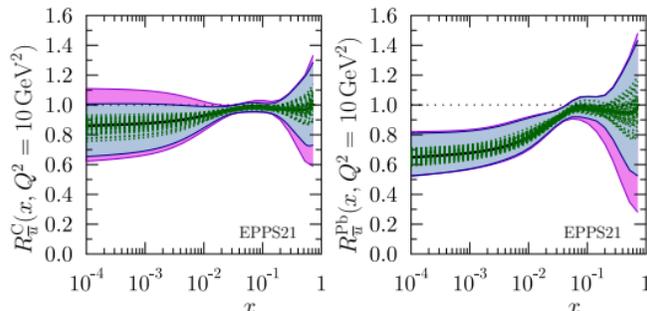
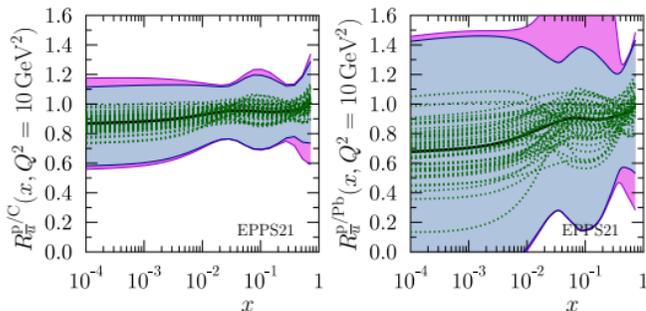
Lead

Full-nucleus modifications *Prelim.*

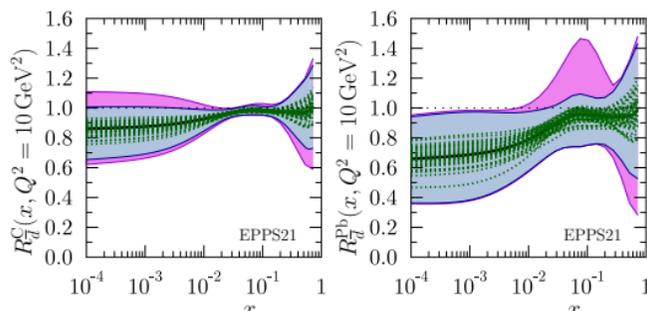
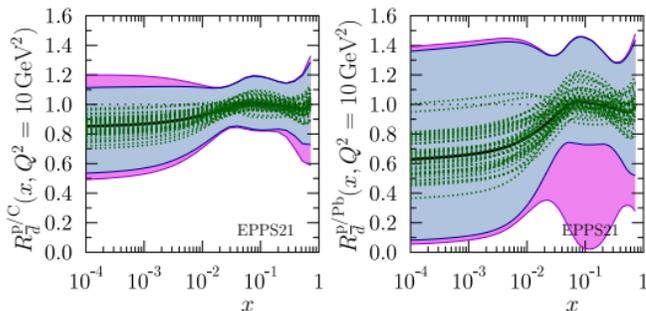
Carbon

Lead

\bar{u}



\bar{d}



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Fit results – strange and glue

Bound-proton modifications *Prelim.*

Carbon

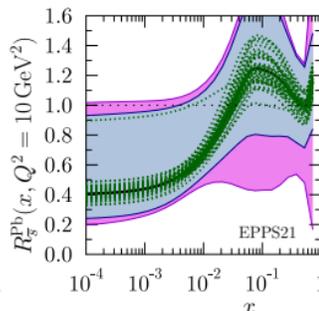
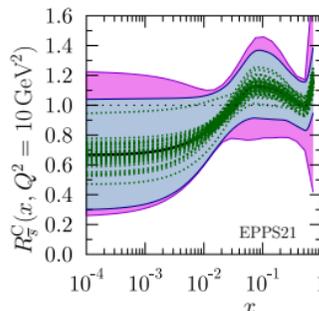
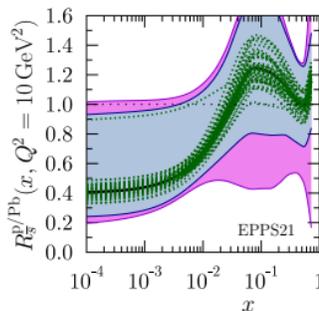
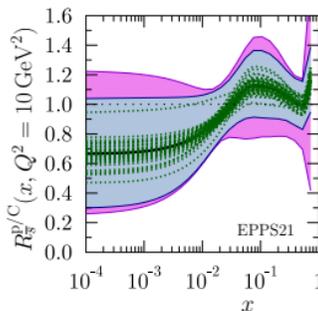
Lead

Full-nucleus modifications *Prelim.*

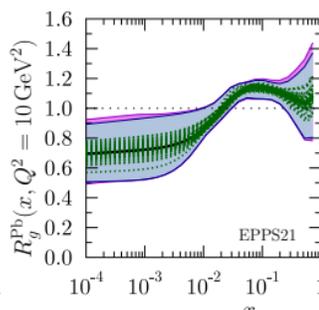
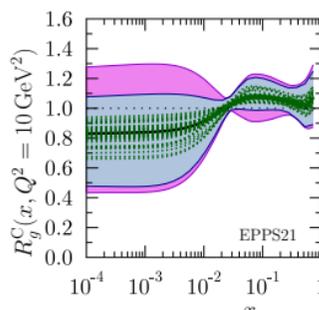
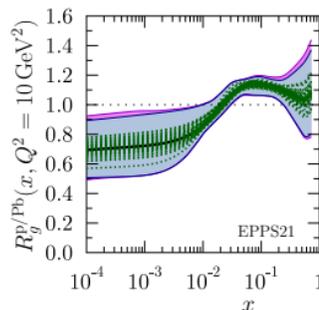
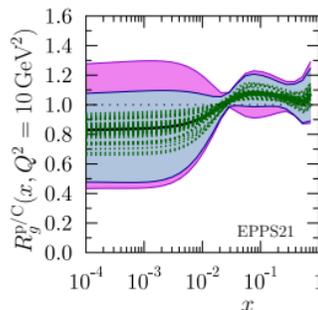
Carbon

Lead

\bar{s}



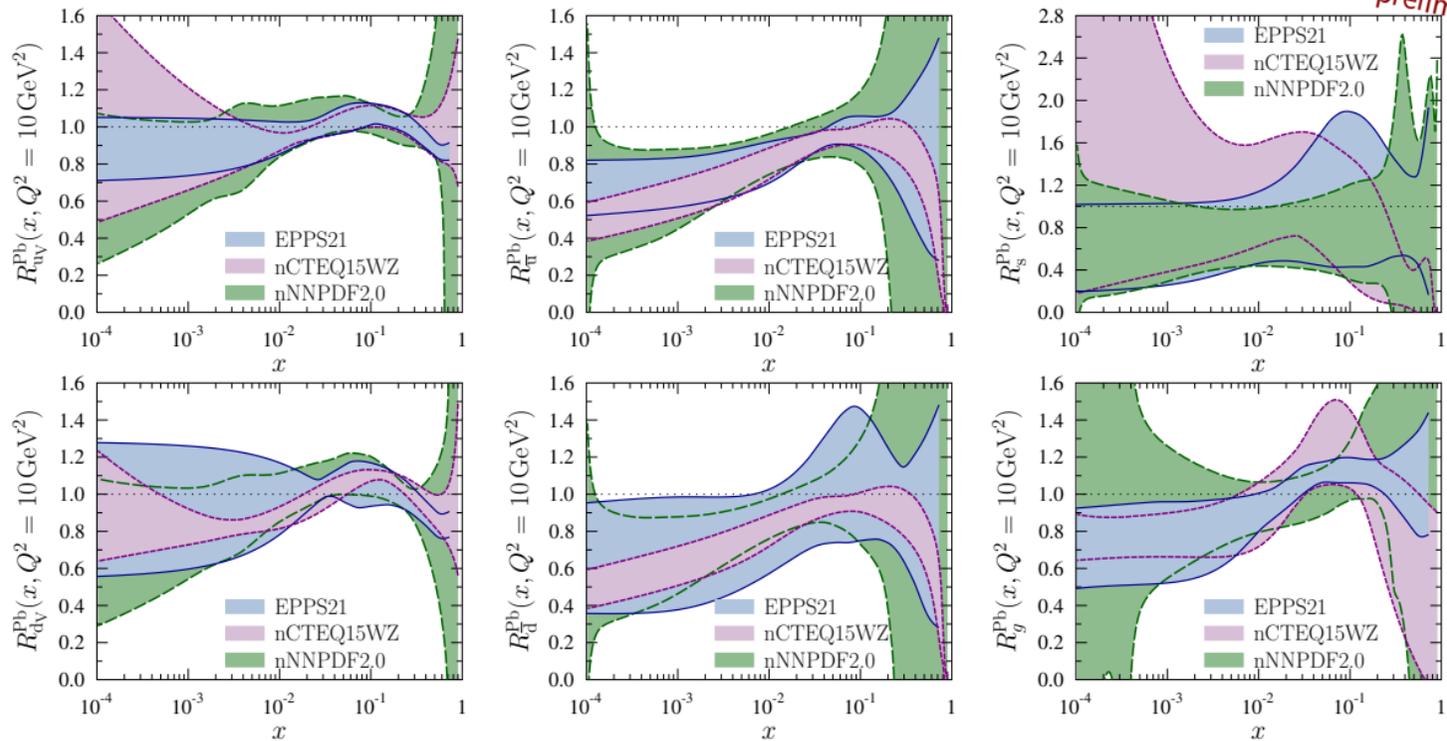
g



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Prelim.

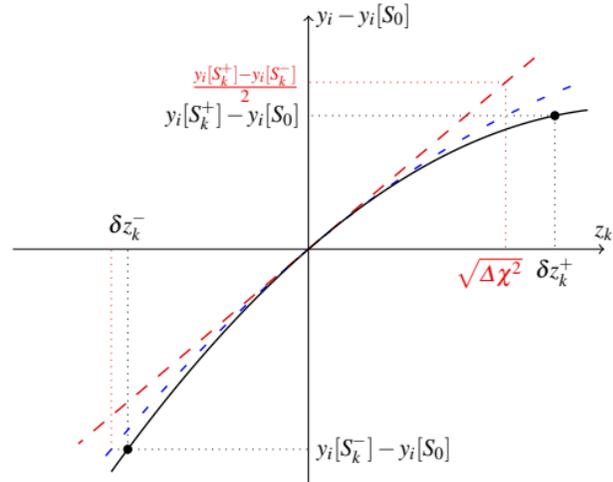
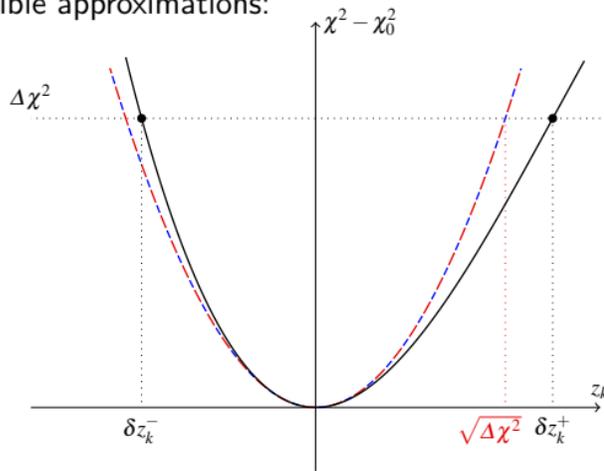


- All three consistent within uncertainties, but significant differences in the uncertainty estimates
- Best constrained gluons in the (prelim.) EPPS21 fit!

The Hessian reweighting is a method to study the impact of a new set of data on the PDFs without performing a full global fit

$$\chi_{\text{new}}^2(\mathbf{z}) = \chi_{\text{old}}^2(\mathbf{z}) + \sum_{ij} (y_i(\mathbf{z}) - y_i^{\text{data}}) C_{ij}^{-1} (y_j(\mathbf{z}) - y_j^{\text{data}})$$

Possible approximations:



quadratic-linear: $\chi_{\text{old}}^2 \approx \chi_0^2 + \sum_k z_k^2$,

quadratic-quadratic: $\chi_{\text{old}}^2 \approx \chi_0^2 + \sum_k z_k^2$,

cubic-quadratic: $\chi_{\text{old}}^2 \approx \chi_0^2 + \sum_k (a_k z_k^2 + b_k z_k^3)$,

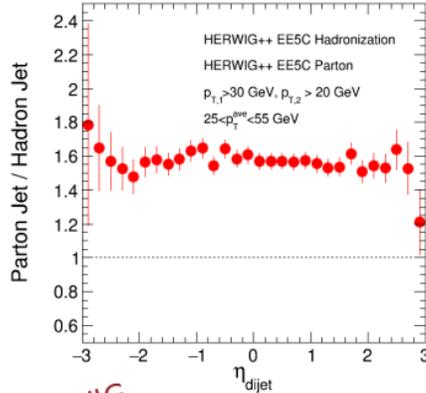
$y_i \approx y_i[S_0] + \sum_k d_{ik} z_k$

$y_i \approx y_i[S_0] + \sum_k (d_{ik} z_k + e_{ik} z_k^2)$

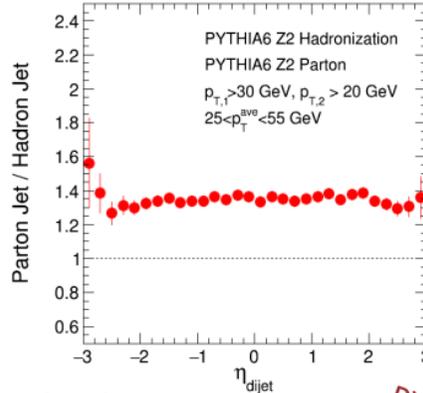
$y_i \approx y_i[S_0] + \sum_k (d_{ik} z_k + e_{ik} z_k^2)$

HERWIG

Cross-section ratios



PYTHIA



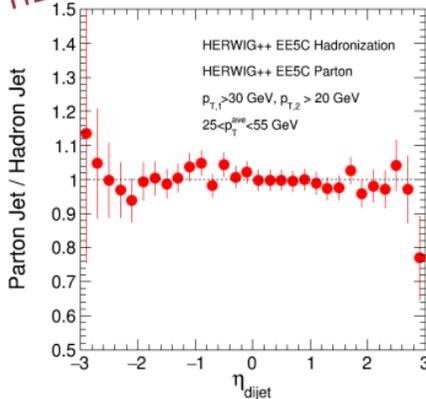
Hadronization uncertainty

Parton jets have higher cross section for $R = 0.3$ jets with same kinematic selections compared to hadron jets

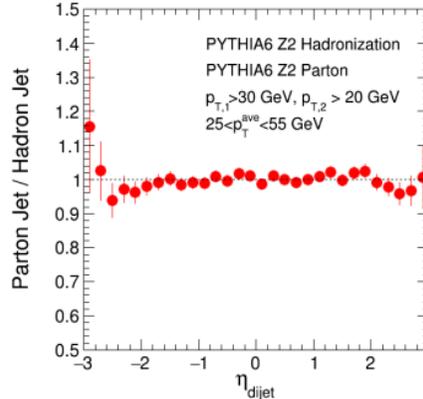
Parton jets are harder fragmenting

HERWIG

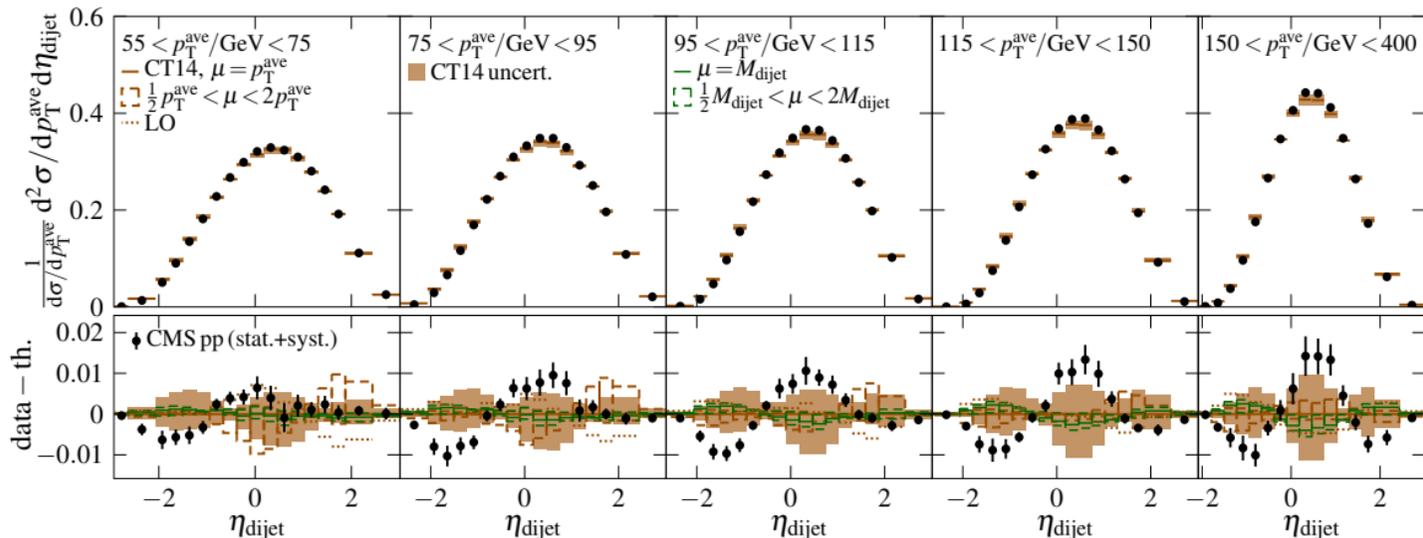
Area normalized ratios



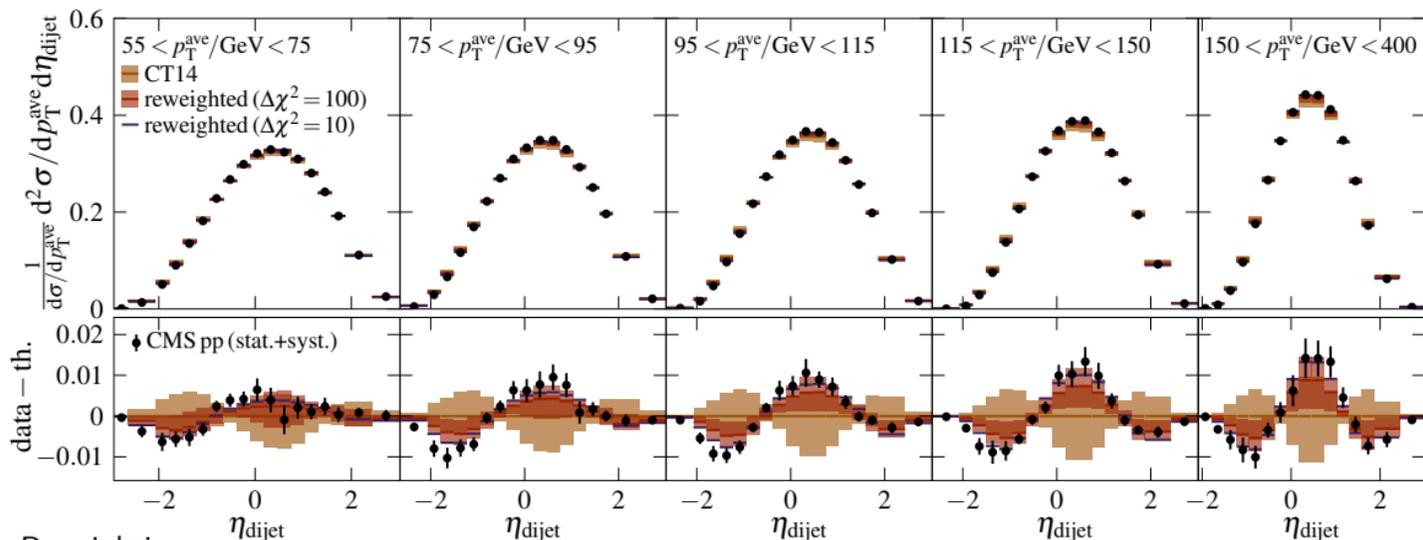
PYTHIA



After self normalization effect of hadronization is negligible



- Predicted NLO distributions somewhat wider than the measured spectra
- High- p_T^{ave} midrapidity robust against scale variations and LO-to-NLO effects
 - can expect NNLO corrections to be small in this region
 - observed discrepancy seems to be a PDF related issue
- Refitting might be needed to improve agreement with data
 - study the impact with the reweighting method

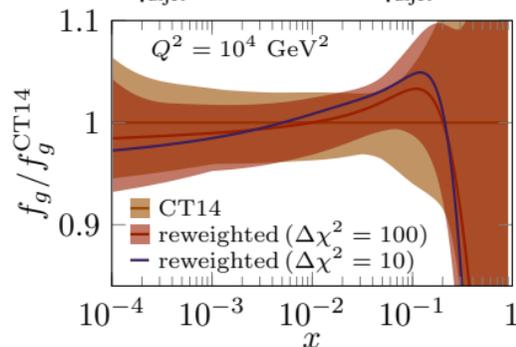


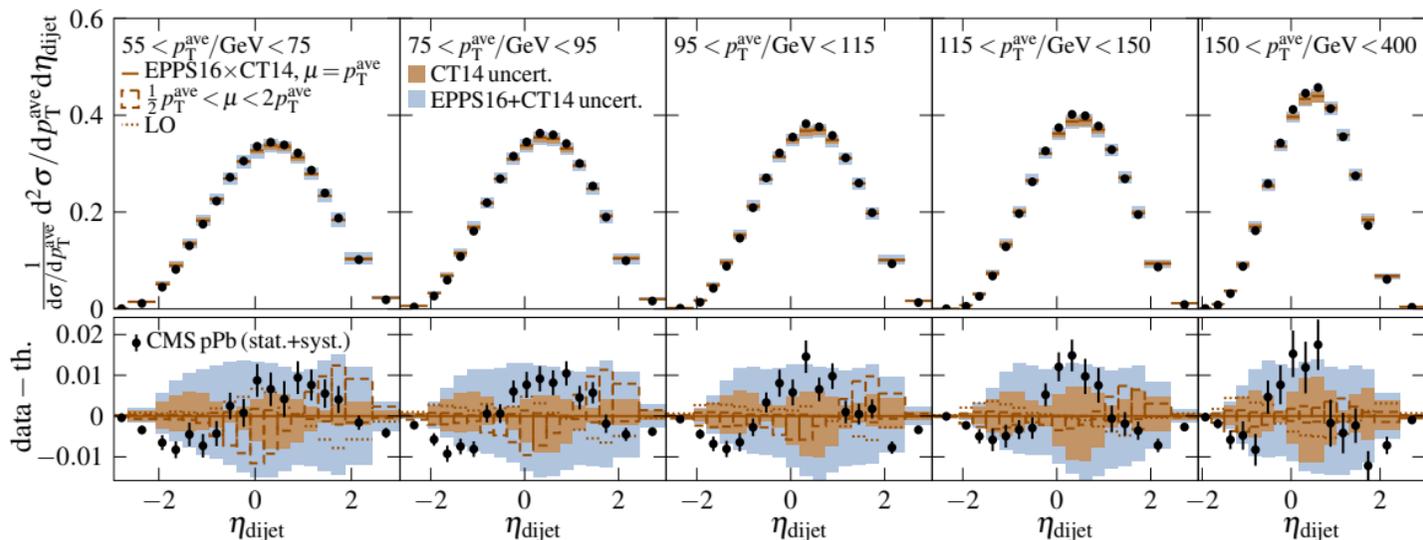
Rewighting:

- improves midrapidity description
- is not able to fully reproduce data at large rapidities even when applied with additional weight ($\Delta\chi^2 = 10$) (high- x parametrization issue? NNLO? data systematics?)

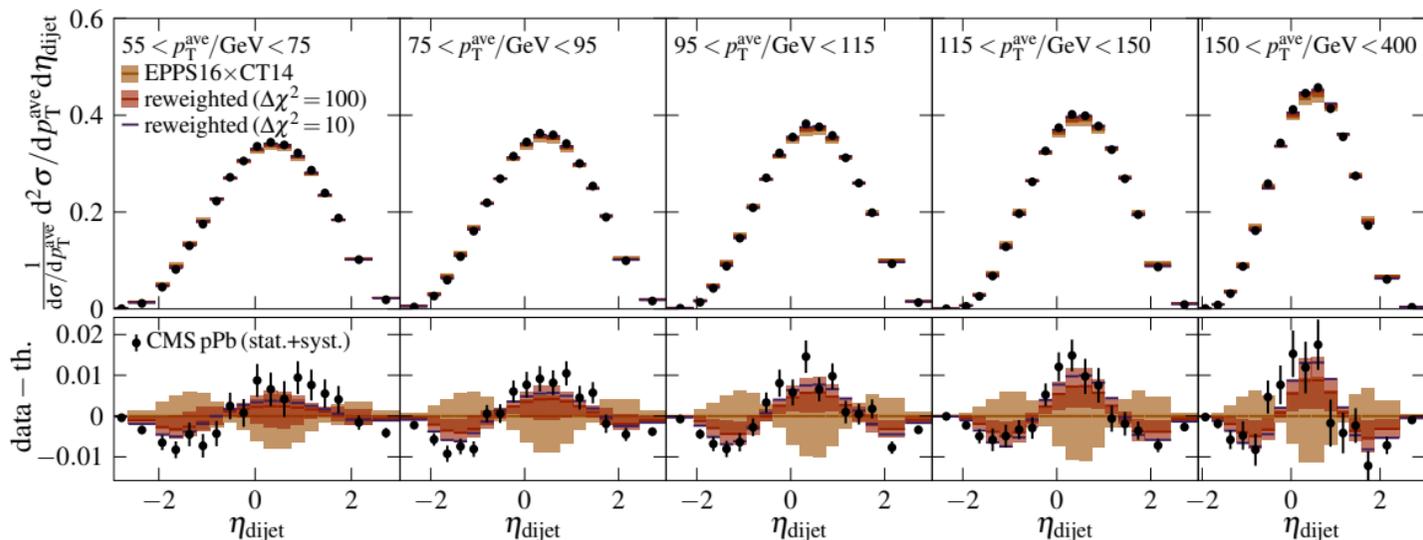
Significant gluon modifications needed especially at large x

- also valence quarks get modified





- pPb data deviates from NLO calculations *almost the same way* as the pp data
 - had we not seen the same deviations in pp, we might have interpreted this as a fault in our nuclear PDFs
- Compared to pp case we have additional suppression in data compared to theory at forward rapidities
 - implication of deeper gluon shadowing



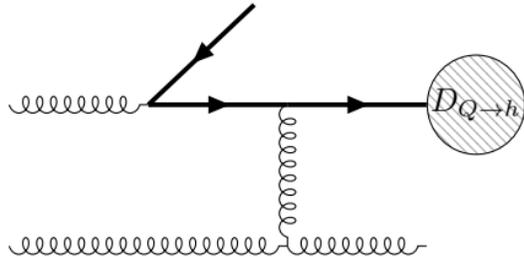
- Modifications needed in CT14 to describe pp data have large impact on pPb predictions
 - it is imperative to understand the pp baseline before making far-reaching conclusions from pPb data
 - Using these data directly in nuclear PDF analysis with CT14 proton PDFs would lead to
 - ▶ overestimating nuclear effects
 - ▶ large scale-choice bias
- Consider nuclear modification factor instead

Heavy-flavour production mass schemes

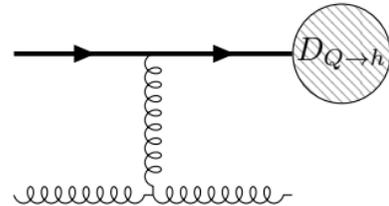
FFNS

In *fixed flavour number scheme*, valid at small p_T , heavy quarks are produced only at the matrix element level

Contains $\log(p_T/m)$ and m/p_T terms



- subtraction term +



ZM-VFNS

In *zero-mass variable flavour number scheme*, valid at large p_T , heavy quarks are treated as massless particles produced also in ISR/FSR

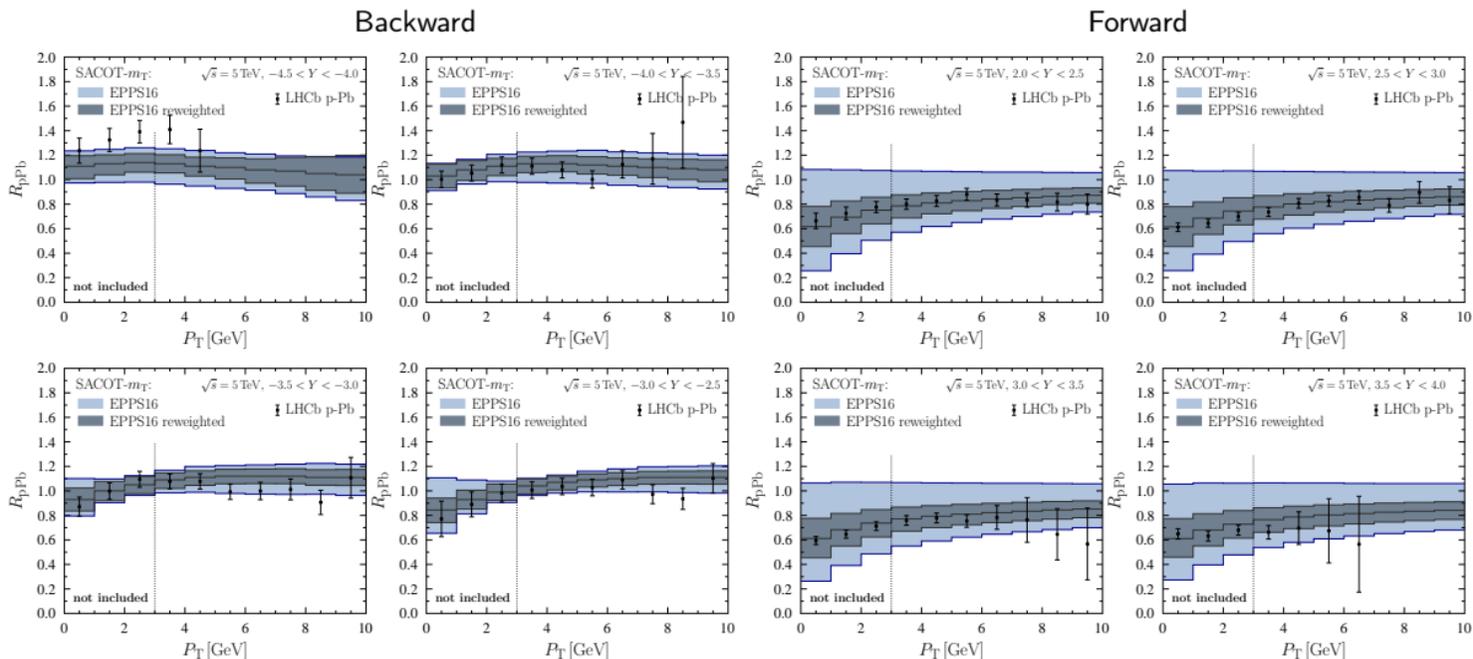
Resums $\log(p_T/m)$ but ignores m/p_T terms

GM-VFNS

A *general-mass variable flavour number scheme* combines the two by supplementing subtraction terms to prevent double counting of the resummed splittings, valid at all p_T

Resums $\log(p_T/m)$ and includes m/p_T terms in the FFNS matrix elements

Important: includes also **gluon-to-HF fragmentation** – large contribution to the cross section!

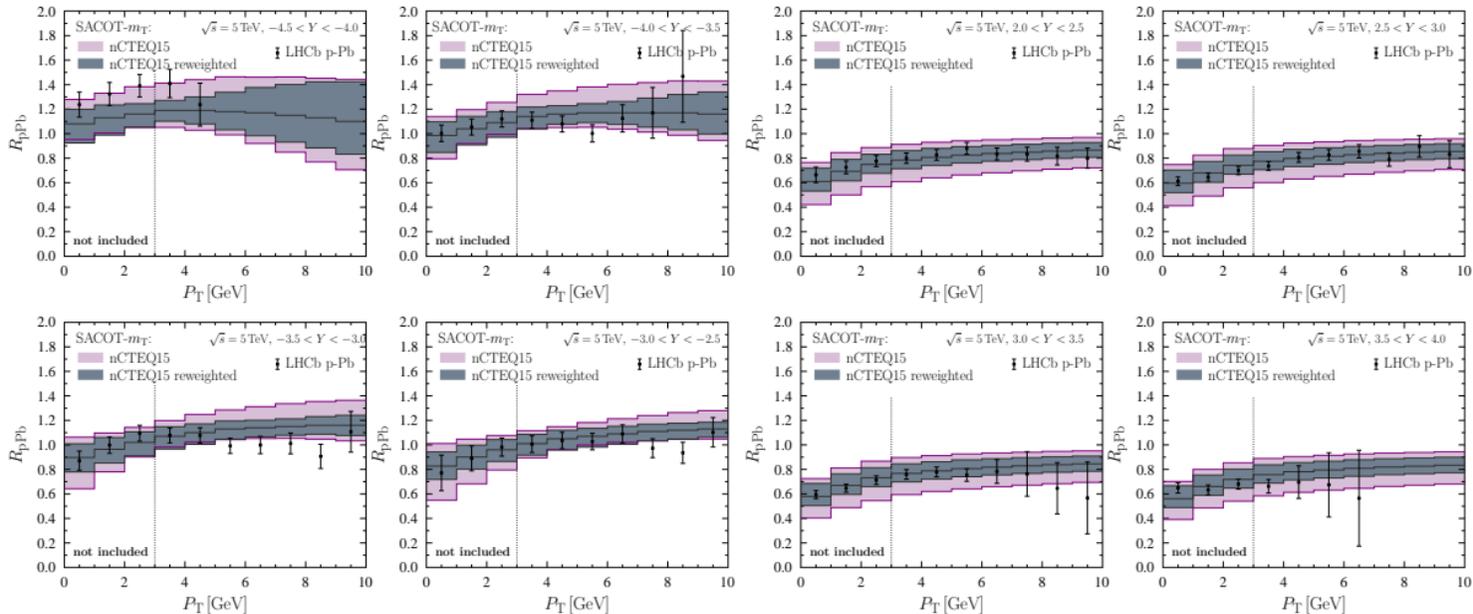


- Data well reproduced with the reweighted results
- Significant reduction in EPPS16 uncertainties especially in forward bins
- Good agreement with data below cut – no physics beyond collinear factorization needed

nCTEQ15 reweighted LHCb D-meson R_{pPb} [Eskola, Helenius, PP & Paukkunen, JHEP 05 (2020) 037]

Backward

Forward



- Uncertainties smaller to begin with in the forward direction (less flexible small- x parametrization) while larger in backward – almost identical results
- Data well reproduced