



Measurements of the CKM angle γ at LHCb

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On behalf of the **LHCb** collaboration

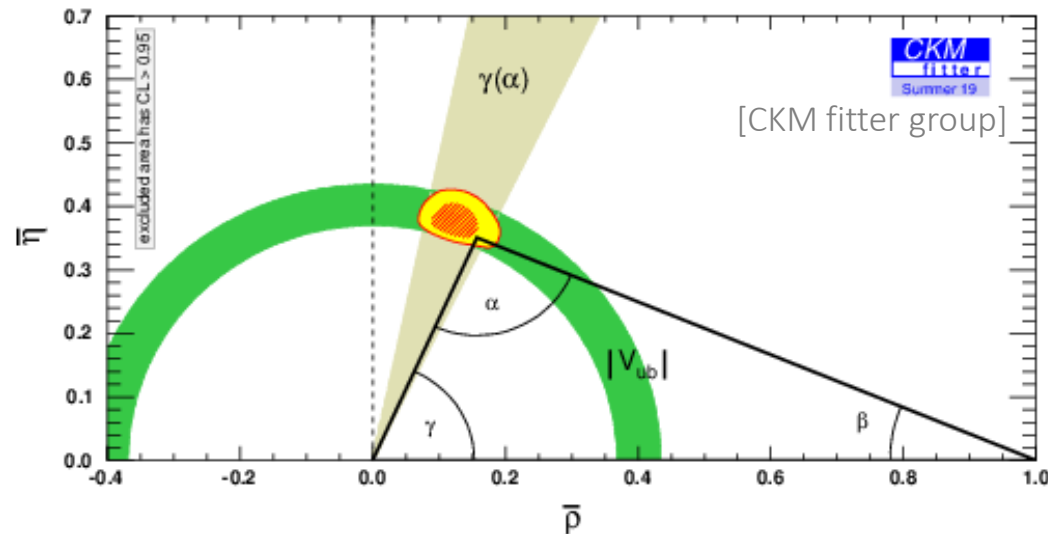
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Introduction

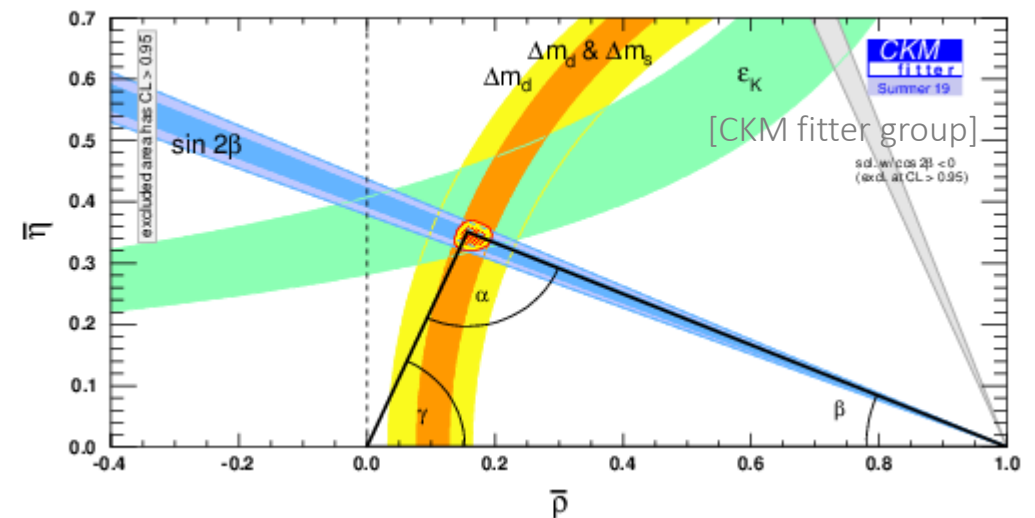
The angle γ is one of the angles of the CKM unitarity triangle:

$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 1 - \frac{1}{2}\lambda^2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{1}{2}\lambda^2 & A\lambda^2 \\ A\lambda^3(1 - \bar{\rho} - i\bar{\eta}) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4)$$

Tree only measurements



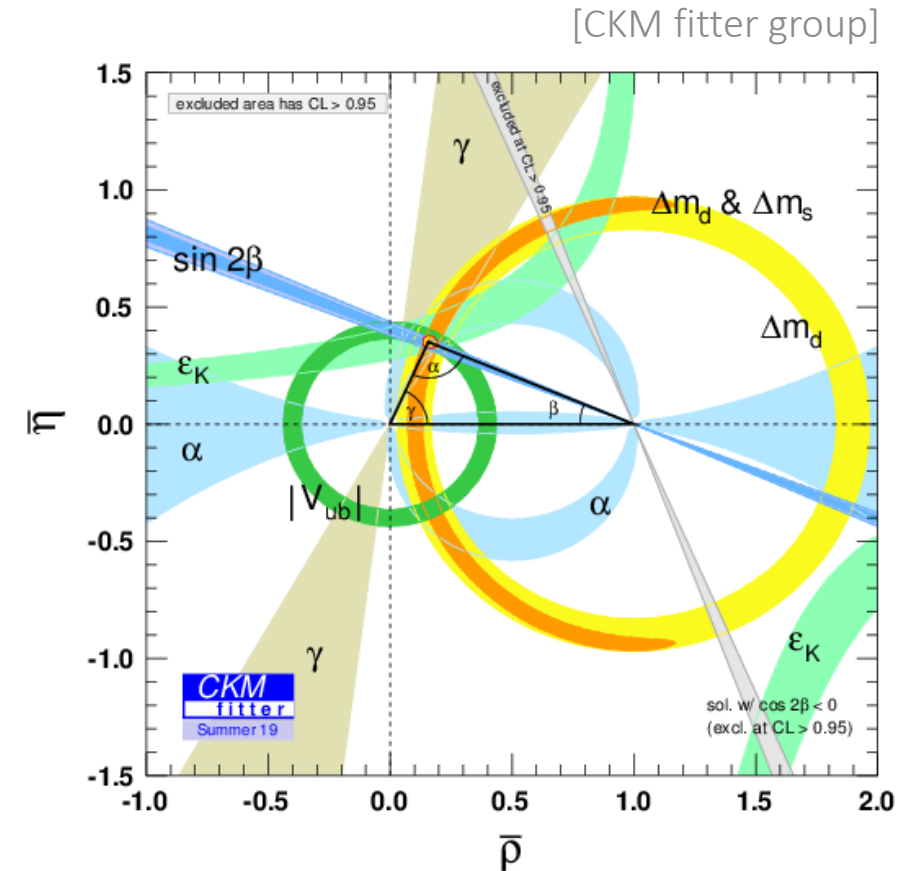
Loop only measurements



Introduction

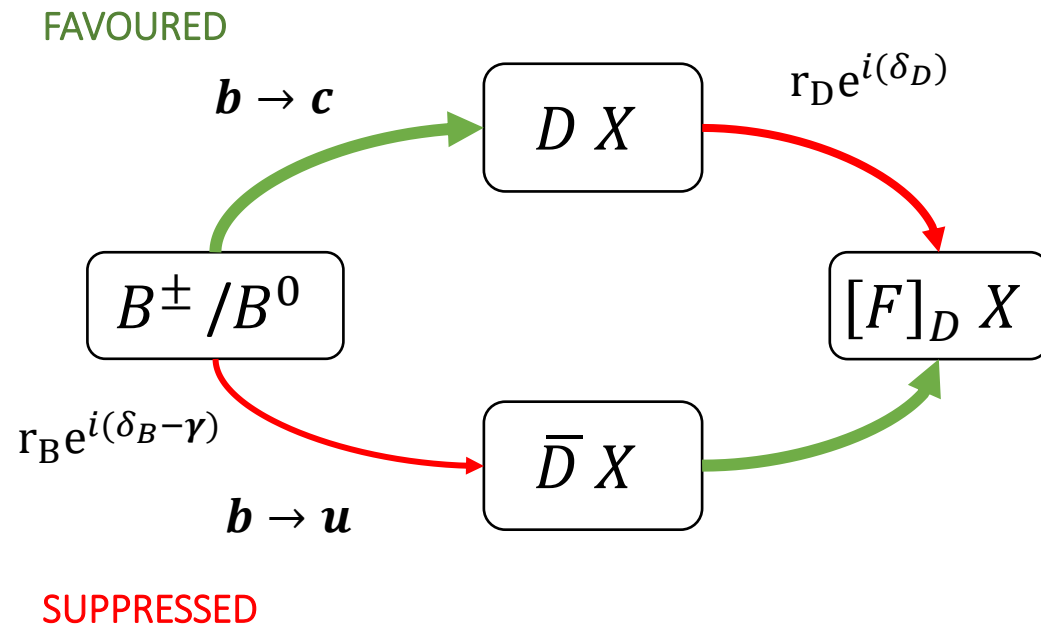
The angle γ is one of the angles of the CKM unitarity triangle:

- It is studied in the heavy flavour physics experiments like LHCb, BELL, KEKB and BaBar.
- It is a Charge-Parity Violation (CPV) parameter.
- It can be measured from tree-level processes only and it is a standard candle measurement in the SM.
- Very small theoretical uncertainties associated with tree-level measurements: $\delta\gamma/\gamma = O(10^{-7})$. [JHEP 01 051]
- Discrepancy between tree-level and loop measurements can be used in probing the New Physics effects beyond the Standard Model.



$B \rightarrow DK$ decays

The CKM angle γ can be measured in processes where the interference between favoured quark transition $b \rightarrow c$ and suppressed $b \rightarrow u$ occurs.



	Method	X	$[F]_D$
B^0/B^\pm	ADS (mixed state)	K, π	$[K\pi, K\pi\pi\pi]$
B^0/B^\pm	GLW (CP eigenstate)	K, π	$[KK, \pi\pi, \pi\pi\pi\pi]$
B^0/B^\pm	GLS	K, π	$[hh]$
B^0	BPGGSZ	K^{*0}	$[K_S^0 hh]$
B^0/B_S^0	Time-Dependent	$K, K^{*\pm}, K^{*0}$	$[hhh, hh]$

$$r_B = \frac{A(B \rightarrow \bar{D}K)}{A(B \rightarrow DK)}$$

$$r_D = \frac{A(D \rightarrow FX)}{A(\bar{D} \rightarrow FX)}$$

$B \rightarrow DK$ decays

Several methods of measurements of the angle γ : GLW, ADS, Dalitz plots and time-dependent.

GLW

[PL B253 1991 483]

$$A_{CP} = \frac{\Gamma(\bar{B}^0 \rightarrow D_{CP} \bar{K}^{*0}) - \Gamma(B^0 \rightarrow D_{CP} K^{*0})}{\Gamma(\bar{B}^0 \rightarrow D_{CP} \bar{K}^{*0}) + \Gamma(B^0 \rightarrow D_{CP} K^{*0})}$$

$$A_{CP} = \frac{2\kappa r_B^{DK^{*0}} \sin(\delta_B^{DK^{*0}}) \sin(\gamma)}{1 + r_B^2 \pm 2r_B \cos(\delta_B) \cos(\gamma)} \propto R_{CP}$$

$KK/\pi\pi$

BPGGSZ

[PRD 68 054018]

$$N_i^\pm = h_\pm [F_i + (x_\pm^2 + y_\pm^2) F_{-i} + 2\sqrt{F_i F_{-i}} (x_\pm c_i + y_\pm s_i)]$$

$$x_\pm = r_B \cos(\delta_B \pm \gamma)$$

$$y_\pm = r_B \sin(\delta_B \pm \gamma)$$

ADS

[PRL 78 1997 3257]

$$A_{CP} = \frac{\Gamma(\bar{B}^0 \rightarrow D_{K^+\pi^-}^0 \bar{K}^{*0}) - \Gamma(B^0 \rightarrow D_{K^-\pi^+}^0 K^{*0})}{\Gamma(\bar{B}^0 \rightarrow D_{K^+\pi^-}^0 \bar{K}^{*0}) + \Gamma(B^0 \rightarrow D_{K^-\pi^+}^0 K^{*0})} \propto R_{CP}$$

$$A_{CP} = \frac{2\kappa r_B^{DK^{*0}} r_D^{K^*0} \sin(\delta_B^{K^*0} + \delta_D^{K\pi}) \sin(\gamma)}{(r_B^{DK^{*0}})^2 + (r_D^{K\pi})^2 + 2\kappa r_B^{DK^{*0}} r_D^{K^*0} \cos(\delta_B^{DK^{*0}} + \delta_D^{K\pi}) \cos(\gamma)} \propto R_{CP}$$

Time-Dependent

$$\frac{d\Gamma(x, t)}{e^{-\Gamma_s t} dt d\phi_4}$$

$$\propto (|A_f^c(x)|^2 + r^2 |A_f^u(x)|^2) \cosh\left(\frac{\Delta\Gamma_s t}{2}\right)$$

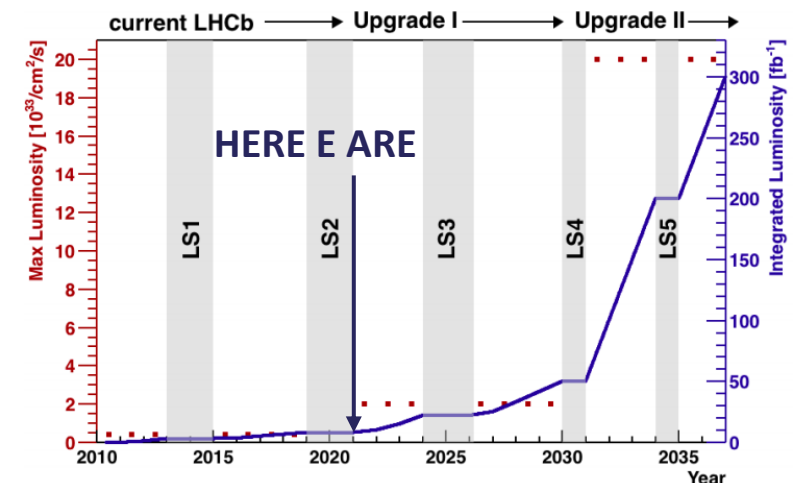
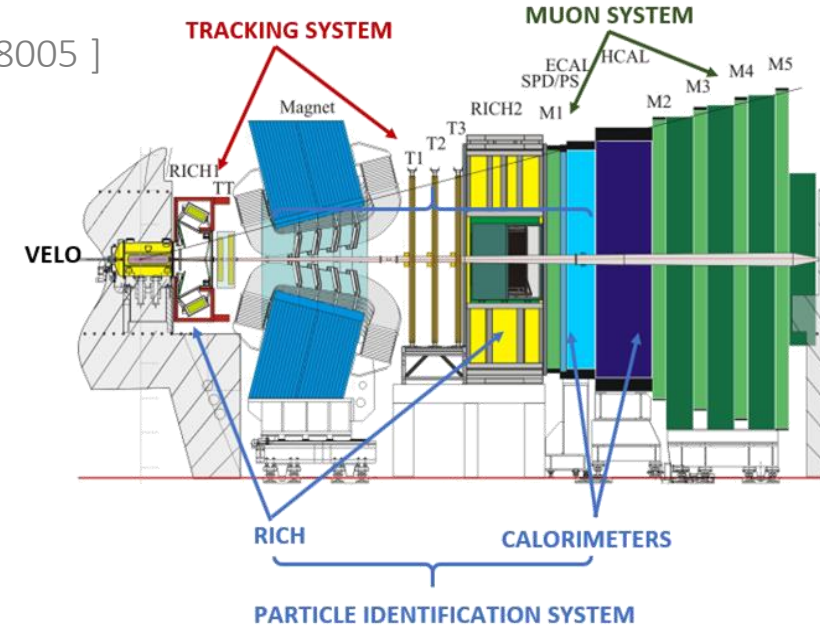
$$- 2\text{Re}(A_f^c(x)^* r^2 A_f^u(x) e^{i\delta - i\gamma - 2\beta_s}) \sinh\left(\frac{\Delta\Gamma_s t}{2}\right) + \dots$$

LHCb detector

LHCb spectrometer, which is designed to study heavy flavor physics of B mesons and C mesons:

- Covering the pseudorapidity range ($2 < \eta < 5$).
- Identification : $\epsilon_{h-h} \sim 90\%$ $\epsilon_{\mu} \sim 97\%$
- IP resolution : $\sigma_{IP} = 20 \mu\text{m}$
- Momentum resolution: $\Delta p/p = 0.5 - 0.8 \%$
- Mass resolution : $\sigma(m_{B \rightarrow hh}) \approx 22 \text{ MeV}$
- Time resolution 45– 55 fs

[JINST 3 S08005]



Outline

Several **new** and updated results from 2020 and 2021:

[LHCb-CONF-2020-003]

- $B^0 \rightarrow DK^{*0}$: the **new** D decay mode:
 $D \rightarrow K^- \pi^- \pi^+ \pi^-$ analysis over Run 1 + 2015 and 2016 data samples
- $B_s^0 \rightarrow D^{\mp} K^{\pm} \pi^{\pm} \pi^{\mp}$: the time-dependent and model – independent analysis of using the full Run 1 & 2 data samples.
- $B^+ \rightarrow Dh^+, D \rightarrow K_s^0 h^+ h^-$: the Run 1 & 2 analysis independent of the modelling of the D-decay amplitude.
- $B^+ \rightarrow D^{(*)} h^{\pm}$: the Run 1 & 2 simultaneous measurement of B^+ decay to D^{*0} and D^0

B decay	D decay	Method	Ref.	Dataset	Status since Ref. [3]
$B^+ \rightarrow Dh^+$	$D \rightarrow h^+ h^-$	GLW/ADS	[16]	Run 1+2	Updated
$B^+ \rightarrow Dh^+$	$D \rightarrow h^+ \pi^- \pi^+ \pi^-$	GLW/ADS	[24]	Run 1	As before
$B^+ \rightarrow Dh^+$	$D \rightarrow h^+ h^- \pi^0$	GLW/ADS	[25]	Run 1	As before
$B^+ \rightarrow Dh^+$	$D \rightarrow K_s^0 h^+ h^-$	BPGGSZ	[17]	Run 1+2	Updated
$B^+ \rightarrow Dh^+$	$D \rightarrow K_s^0 K^{\pm} \pi^{\mp}$	GLS	[20]	Run 1+2	Updated
$B^+ \rightarrow D^* h^+$	$D \rightarrow h^+ h^-$	GLW/ADS	[16]	Run 1+2	Updated
$B^+ \rightarrow DK^{*+}$	$D \rightarrow h^+ h^-$	GLW/ADS	[26]	Run 1+2(*)	As before
$B^+ \rightarrow DK^{*+}$	$D \rightarrow h^+ \pi^- \pi^+ \pi^-$	GLW/ADS	[26]	Run 1+2(*)	As before
$B^+ \rightarrow DK^+ \pi^+ \pi^-$	$D \rightarrow h^+ h^-$	GLW/ADS	[27]	Run 1	As before
$B^0 \rightarrow DK^{*0}$	$D \rightarrow h^+ h^-$	GLW/ADS	[21]	Run 1+2(*)	Updated
$B^0 \rightarrow DK^{*0}$	$D \rightarrow h^+ \pi^- \pi^+ \pi^-$	GLW/ADS	[21]	Run 1+2(*)	New
$B^0 \rightarrow DK^+ \pi^-$	$D \rightarrow h^+ h^-$	GLW-Dalitz	[22]	Run 1	Superseded
$B^0 \rightarrow DK^{*0}$	$D \rightarrow K_s^0 \pi^+ \pi^-$	BPGGSZ	[28]	Run 1	As before
$B^0 \rightarrow D^{\mp} \pi^{\pm}$	$D^{\pm} \rightarrow K^{\mp} \pi^{\pm} \pi^{\pm}$	TD	[29]	Run 1	As before
$B_s^0 \rightarrow D_s^{\mp} K^{\pm}$	$D_s^{\pm} \rightarrow h^{\pm} h^{\mp} \pi^{\pm}$	TD	[30]	Run 1	As before
$B_s^0 \rightarrow D_s^{\mp} K^{\pm} \pi^{\pm} \pi^{\mp}$	$D_s^{\pm} \rightarrow h^{\pm} h^{\mp} \pi^{\pm}$	TD	[23]	Run 1+2	New

$B^0 \rightarrow DK^{*0}$

Updated result from 2014 over Run 1 and Run 2 data sample of 4.8 fb^{-1}

➤ Two-body (GLW):

$$D^0 \rightarrow K^\pm K^\mp,$$

$$D^0 \rightarrow K^\pm \pi^\mp,$$

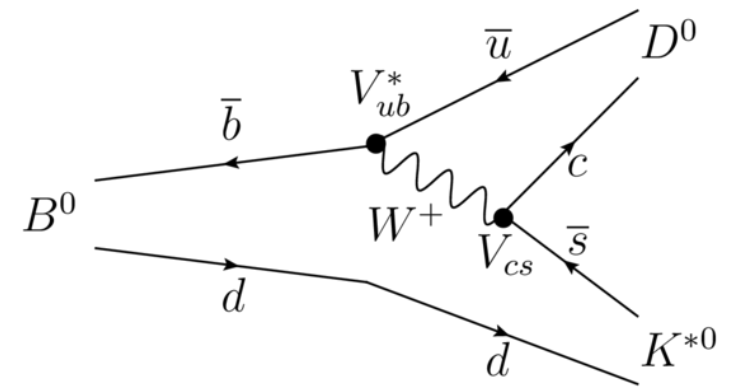
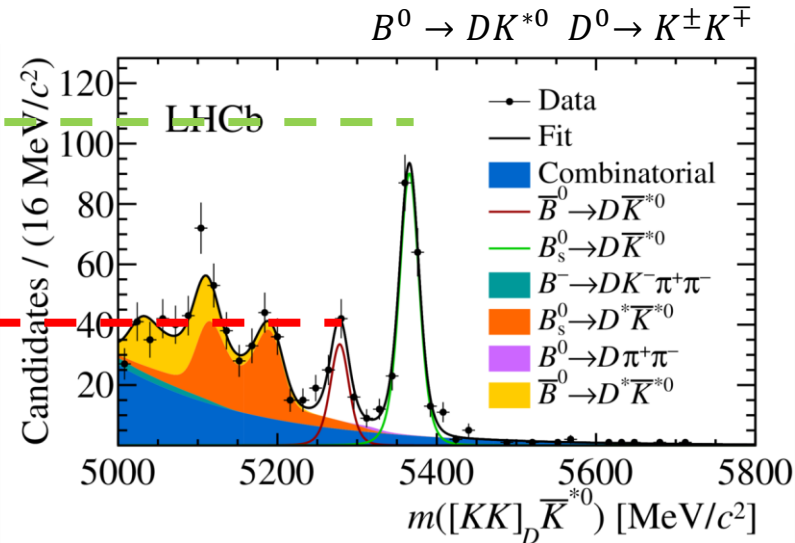
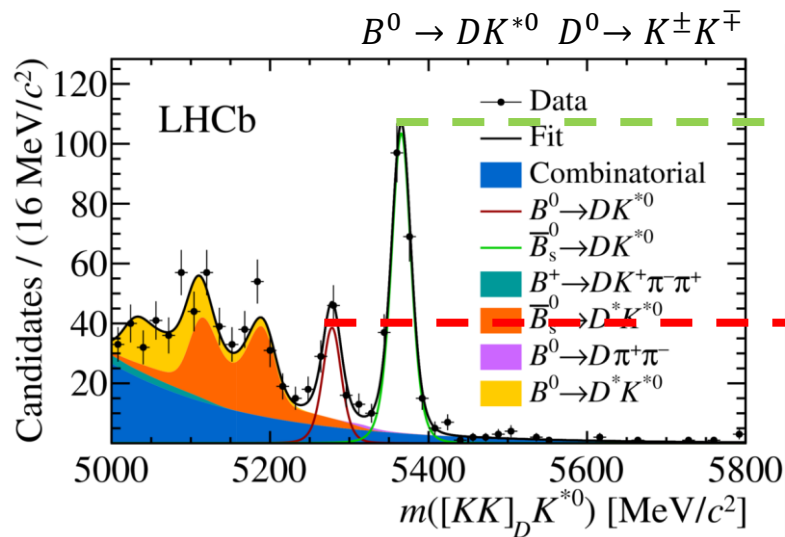
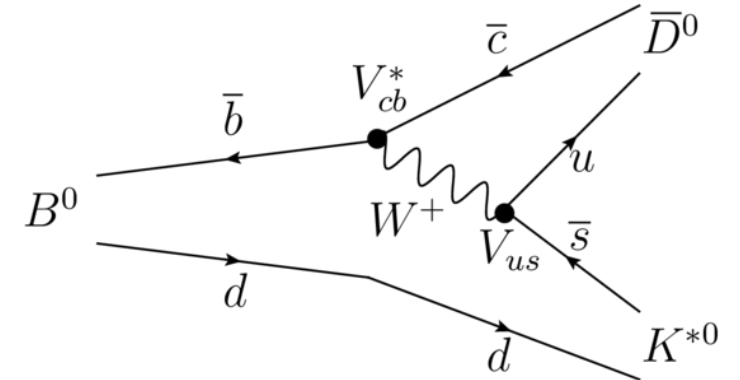
$$D^0 \rightarrow \pi^\pm \pi^\mp$$

➤ Four-body (quasi-GLW):

NEW!

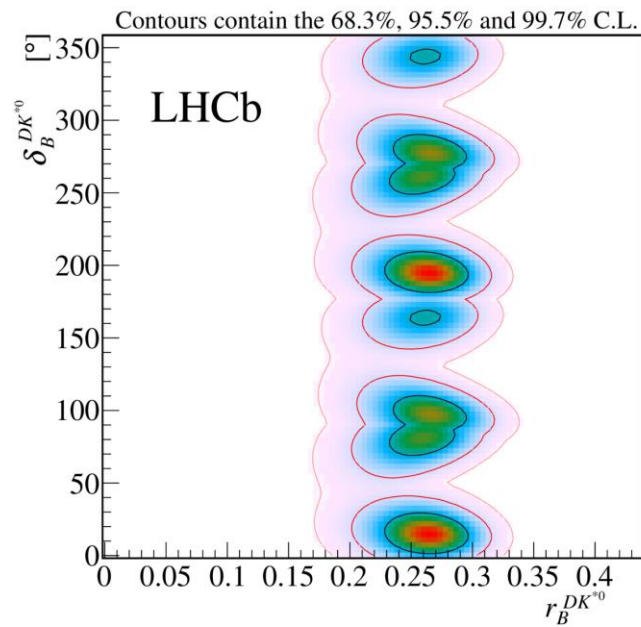
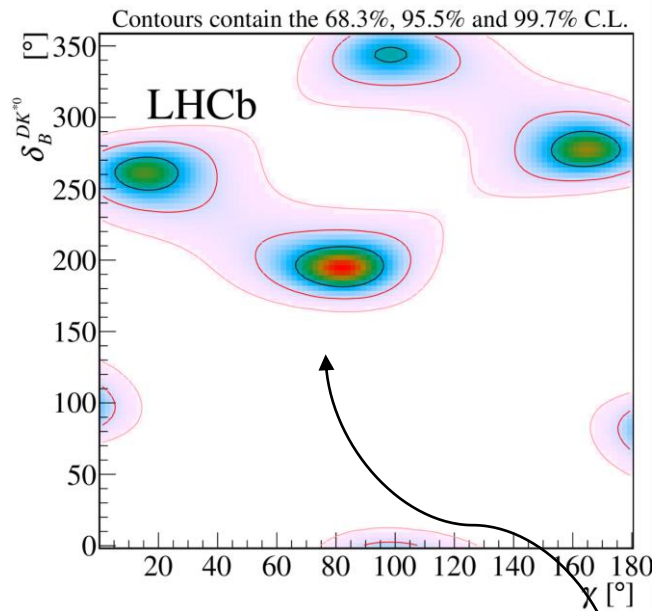
$$D^0 \rightarrow K^\pm \pi^\mp \pi^+ \pi^-,$$

$$D^0 \rightarrow \pi^\pm \pi^\mp \pi^+ \pi^-$$



$B^0 \rightarrow DK^{*0}$

The 2D scans of $\delta_B^{DK^{*0}}$ vs. γ and $\delta_B^{DK^{*0}}$ versus $r_B^{DK^{*0}}$



$\Delta\chi^2 = 2.30, 6.18$ and 11.8 contours \longleftrightarrow 68.6%, 95.5% and 99.7% C.L

Excellent constrains on the γ angle value!

Measurement of CP parameters:

$$\begin{aligned} \mathcal{A}_{\text{ADS}}^{\pi K} &= 0.19 \pm 0.19 \pm 0.01, \\ \mathcal{R}_{\text{ADS}}^{\pi K} &= 0.080 \pm 0.015 \pm 0.002, \\ \mathcal{A}_{\text{ADS}}^{\pi K \pi \pi} &= -0.01 \pm 0.24 \pm 0.01, \\ \mathcal{R}_{\text{ADS}}^{\pi K \pi \pi} &= 0.073 \pm 0.018 \pm 0.002. \end{aligned}$$

GLW

$$A_{CP} = \frac{2\kappa r_B^{DK^{*0}} \sin(\delta_B^{DK^{*0}}) \sin(\gamma)}{1 + r_B^2 \pm 2r_B \cos(\delta_B) \cos(\gamma)}$$

ADS

$$A_{CP} = \frac{2\kappa r_B^{DK^{*0}} r_D^{K^{*0}} \sin(\delta_B^{K^{*0}} + \delta_D^{K\pi}) \sin(\gamma)}{(r_B^{DK^{*0}})^2 + (r_D^{K\pi})^2 + 2\kappa r_B^{DK^{*0}} r_D^{K^{*0}} \cos(\delta_B^{DK^{*0}} + \delta_D^{K\pi}) \cos(\gamma)}$$

$$B_S^0 \rightarrow D_S^- h^+ \pi^+ \pi^-$$

Measurement of the angle γ in $B_S^0 \rightarrow D_S^- h^+ \pi^+ \pi^-$ decay:

(Full Run 1 & 2: 9 fb^{-1} data sample)

A time-dependent amplitude analysis:

the time-dependent amplitude fit using signal PDF through full-spectrum decay rate.

$$\langle f | B_S^0 \rangle = A^c(x) \quad \langle f | \overline{B_S^0} \rangle = r e^{i(\delta-\gamma)} A^u(x)$$

$$C_f, A_f^{\Delta\Gamma}, A_{\bar{f}}^{\Delta\Gamma}, S_f, S_{\bar{f}}$$

$$A^u(x) = \sum_i a_i^u A_i(x)$$

$$A^c(x) = \sum_i a_i^c A_i(x)$$

$$\frac{d\Gamma(x,t)}{e^{-\Gamma_s t} dt d\phi_4}$$

$$\propto (|A_f^c(x)|^2 + r^2 |A_f^u(x)|^2) \cosh\left(\frac{\Delta\Gamma_s t}{2}\right) + qf (|A_f^c(x)|^2 r^2 |A_f^u(x)|^2) \cos(\Delta m_s t)$$

$$- 2\text{Re}(A_f^c(x)^* r A_f^u(x) e^{i\delta - if(\gamma - 2\beta_s)}) \sinh\left(\frac{\Delta\Gamma_s t}{2}\right) - 2qf \text{Im}(A_f^c(x)^* r A_f^u(x) e^{i\delta - if(\gamma - 2\beta_s)}) \sin(\Delta m_s t)$$

$$S_f = f \frac{2r\kappa \sin(\delta - f(\gamma - 2\beta_s))}{1 + r^2}$$

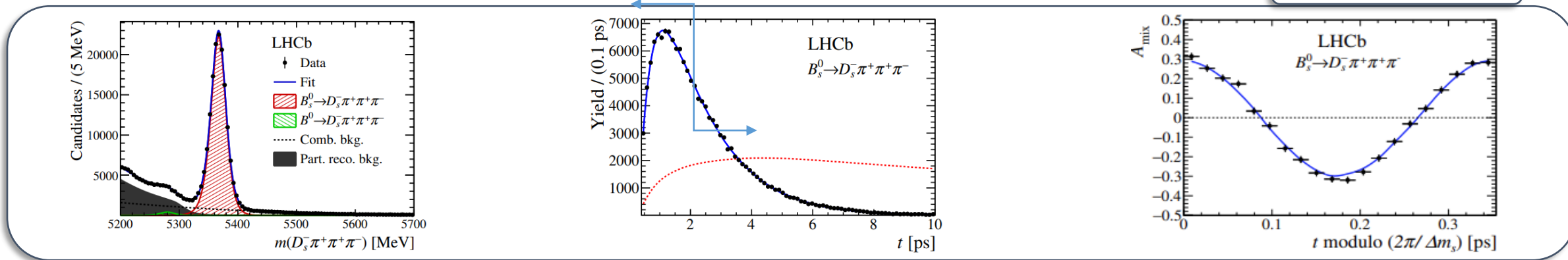
C_f

D_f

S_f

$B_S^0 \rightarrow D_S^- h^+ \pi^+ \pi^-$

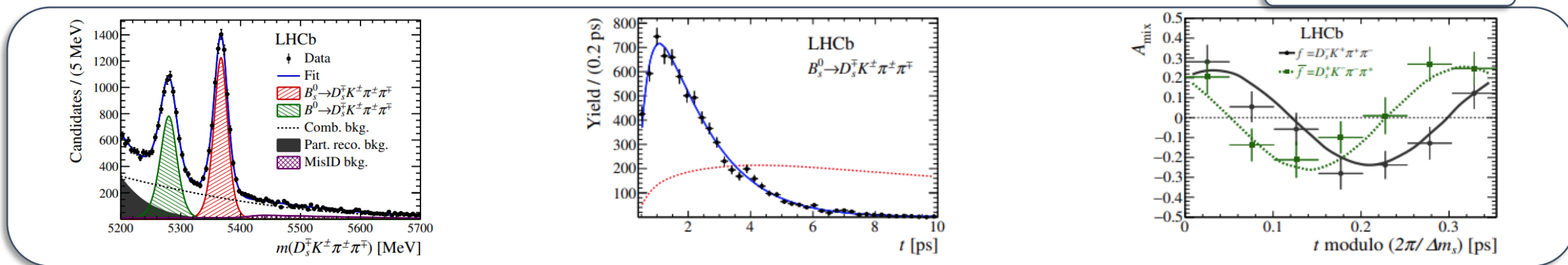
$B_S^0 \rightarrow D_S^- K^+ \pi^+ \pi^-$



Decay-time

The mixing asymmetry folded into one oscillation period along with the fit projections

$B_S^0 \rightarrow D_S^- \pi^+ \pi^+ \pi^-$

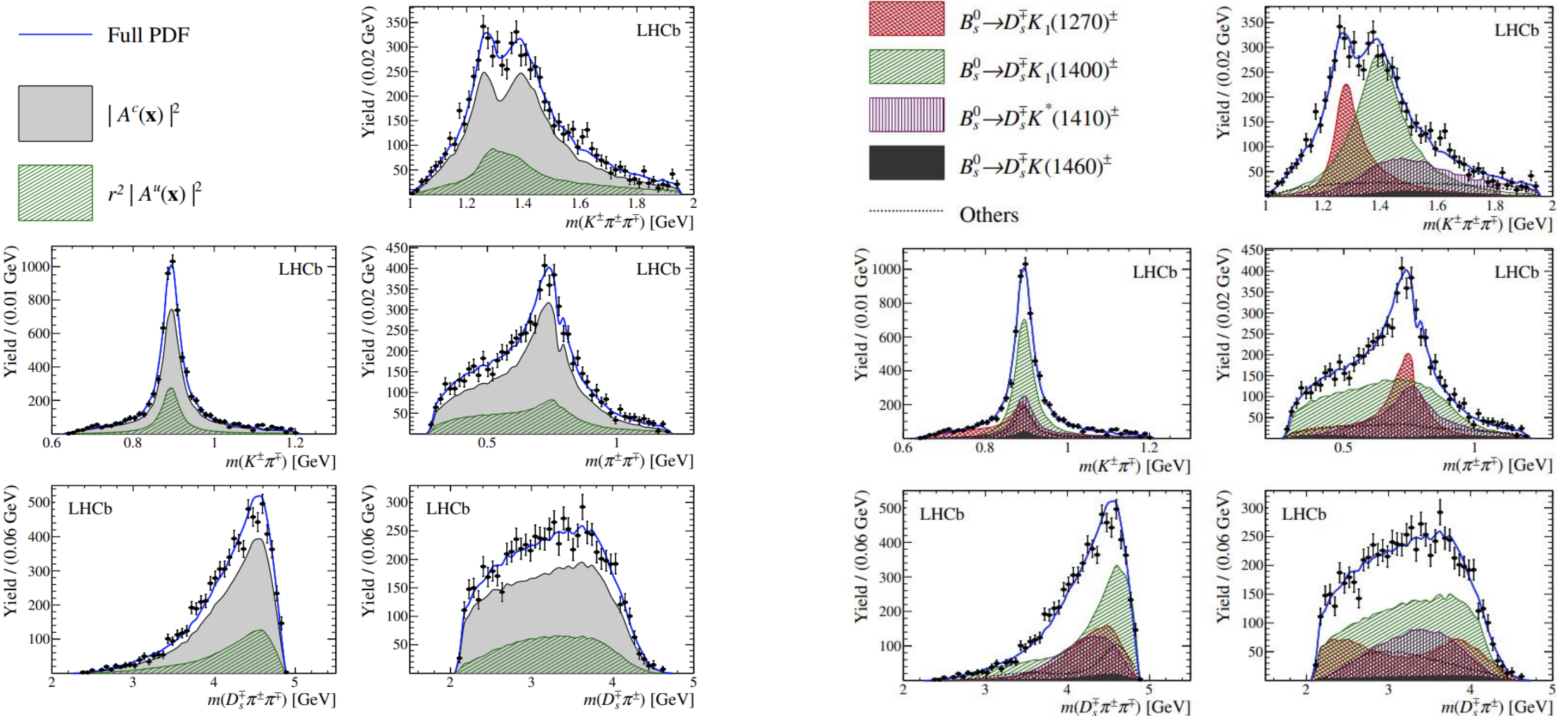


$\Delta m_s = (17.757 \pm 0.007(stat) \pm 0.008(syst))ps^{-1}$ - the most precise measurement of Δm_s !

$$B_S^0 \rightarrow D_S^- h^+ \pi^+ \pi^-$$

Contributions from $b \rightarrow c$ and $b \rightarrow u$ decay amplitudes

Incoherent contributions from intermediate-state components.



$$B_S^0 \rightarrow D_S^- h^+ \pi^+ \pi^-$$

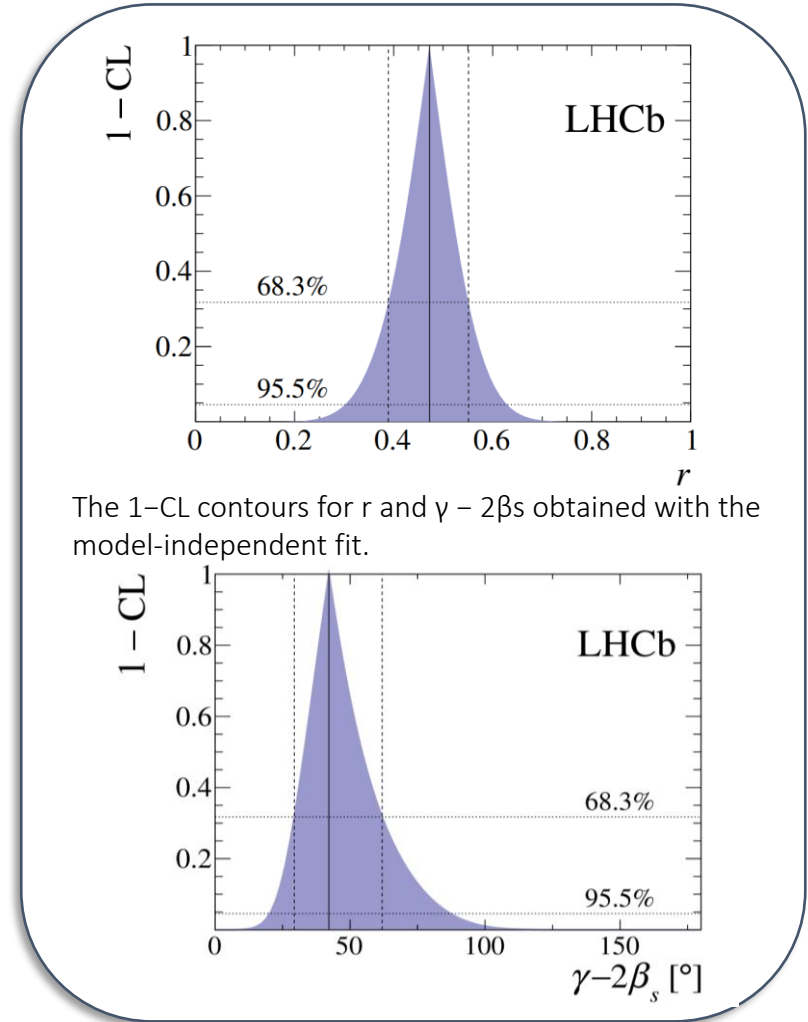
A model-independent analysis:

A time-dependent amplitude analysis:

Decay channel	F_i^c [%]	F_i^u [%]
$B_S^0 \rightarrow D_S^- (K_1(1270)^\pm \rightarrow K^*(892)^0 \pi^\pm)$	$13.0 \pm 2.4 \pm 2.7 \pm 3.4$	$4.1 \pm 2.2 \pm 2.9 \pm 2.6$
$B_S^0 \rightarrow D_S^- (K_1(1270)^\pm \rightarrow K^\pm \rho(770)^0)$	$16.0 \pm 1.4 \pm 1.8 \pm 2.1$	$5.1 \pm 2.2 \pm 3.5 \pm 2.0$
$B_S^0 \rightarrow D_S^- (K_1(1270)^\pm \rightarrow K_0^*(1430)^0 \pi^\pm)$	$3.4 \pm 0.5 \pm 1.0 \pm 0.4$	$1.1 \pm 0.5 \pm 0.6 \pm 0.5$
$B_S^0 \rightarrow D_S^- (K_1(1400)^\pm \rightarrow K^*(892)^0 \pi^\pm)$	$63.9 \pm 5.1 \pm 7.4 \pm 13.5$	$19.3 \pm 5.2 \pm 8.3 \pm 7.8$
$B_S^0 \rightarrow D_S^- (K^*(1410)^\pm \rightarrow K^*(892)^0 \pi^\pm)$	$12.8 \pm 0.8 \pm 1.5 \pm 3.2$	$12.6 \pm 2.0 \pm 2.6 \pm 4.1$
$B_S^0 \rightarrow D_S^- (K^*(1410)^\pm \rightarrow K^\pm \rho(770)^0)$	$5.6 \pm 0.4 \pm 0.6 \pm 0.7$	$5.6 \pm 1.0 \pm 1.2 \pm 1.8$
$B_S^0 \rightarrow D_S^- (K(1460)^\pm \rightarrow K^*(892)^0 \pi^\pm)$		$11.9 \pm 2.5 \pm 2.9 \pm 3.1$
$B_S^0 \rightarrow (D_S^\mp \pi^\pm)_P K^*(892)^0$	$10.2 \pm 1.6 \pm 1.8 \pm 4.5$	$28.4 \pm 5.6 \pm 6.4 \pm 15.3$
$B_S^0 \rightarrow (D_S^\mp K^\pm)_P \rho(770)^0$	$0.9 \pm 0.4 \pm 0.5 \pm 1.0$	
Sum	$125.7 \pm 6.4 \pm 6.9 \pm 19.9$	$88.1 \pm 7.0 \pm 10.0 \pm 20.9$

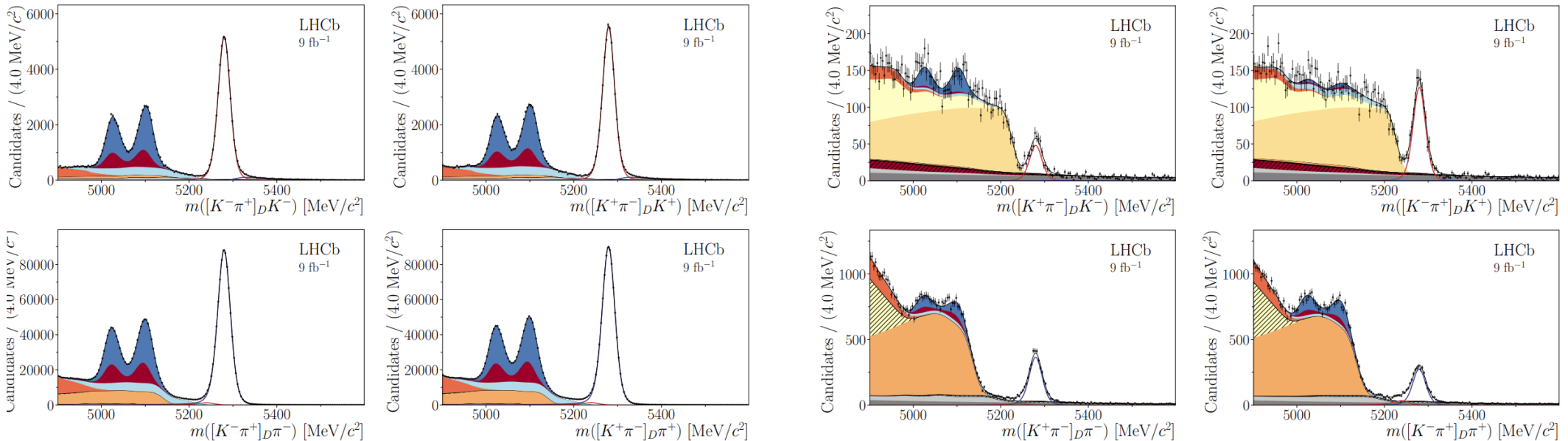
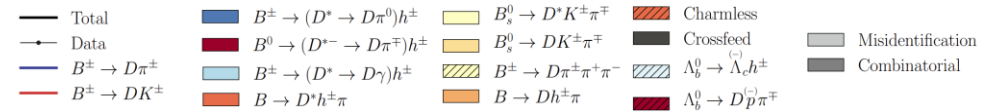
Fit parameter	Value
C_f	$0.631 \pm 0.096 \pm 0.032$
$A_f^{\Delta\Gamma}$	$-0.334 \pm 0.232 \pm 0.097$
$A_{\bar{f}}^{\Delta\Gamma}$	$-0.695 \pm 0.215 \pm 0.081$
S_f	$-0.424 \pm 0.135 \pm 0.033$
$S_{\bar{f}}$	$-0.463 \pm 0.134 \pm 0.031$

Parameter	Model-independent	Model-dependent
r	$0.47^{+0.08}_{-0.08} {}^{+0.02}_{-0.03}$	$0.56 \pm 0.05 \pm 0.04 \pm 0.07$
κ	$0.88^{+0.12}_{-0.19} {}^{+0.04}_{-0.07}$	$0.72 \pm 0.04 \pm 0.06 \pm 0.04$
δ [°]	$-6^{+10}_{-12} {}^{+2}_{-4}$	$-14 \pm 10 \pm 4 \pm 5$
$\gamma - 2\beta_s$ [°]	$42^{+19}_{-13} {}^{+6}_{-2}$	$42 \pm 10 \pm 4 \pm 5$



$B^+ \rightarrow D^{(*)} h^+$

- The Run 1 and Run 2 data sample of 8.7 fb^{-1}
- Simultaneous D^0 and D^{*0} analysis with $D^{(*)}$ decay to $D\pi^0$ and $D\gamma$ and $D \rightarrow K^\pm \pi^\mp, D \rightarrow K^\pm K^\mp, D \rightarrow \pi^\pm \pi^\mp$
- Measurement of partially reconstructed $B^+ \rightarrow D^{(*)} K^+$ and $B^+ \rightarrow D^{(*)} \pi^+$ with $D \rightarrow K^\pm \pi^\mp$.
- First observation of $B^+ \rightarrow (D\pi^0)_{D^*} \pi^+$ decay.



$B^+ \rightarrow D^{(*)} h^+$

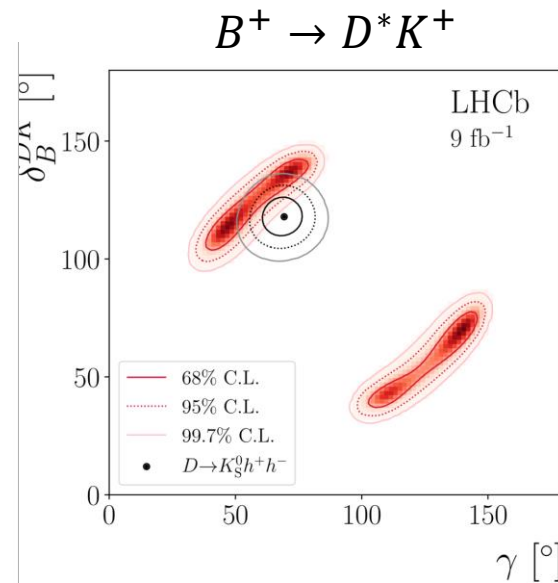
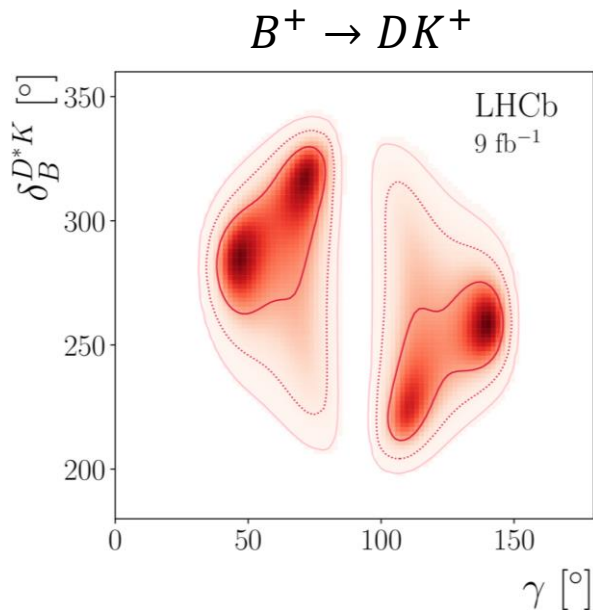
➤ Measurement of CP parameters provide powerful constraints on the angle γ for other LHCb measurements:

$$A_K^{CP} = 0.136 \pm 0.009 \pm 0.001,$$

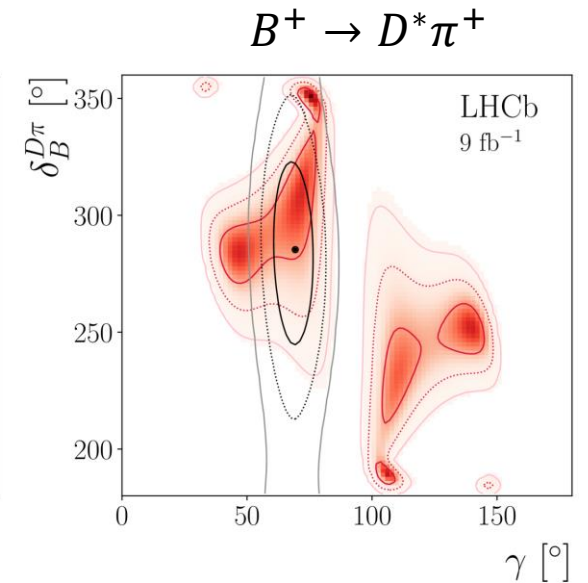
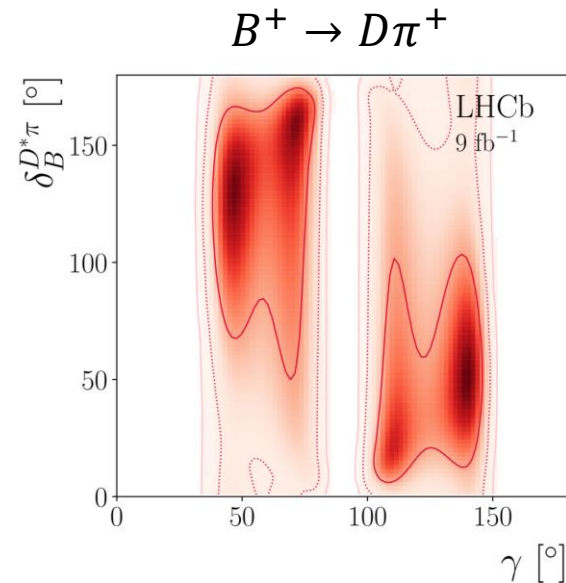
$$A_\pi^{CP} = -0.008 \pm 0.002 \pm 0.002,$$

$$A_K^{K\pi} = -0.011 \pm 0.003 \pm 0.002,$$

$$R^{CP} = 0.950 \pm 0.009 \pm 0.010,$$



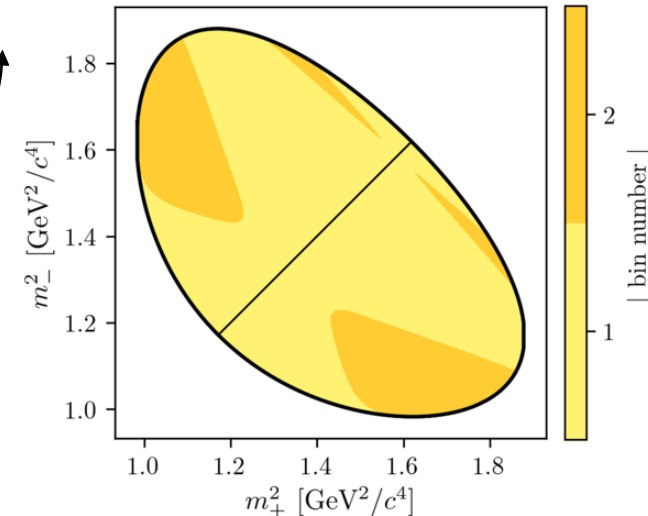
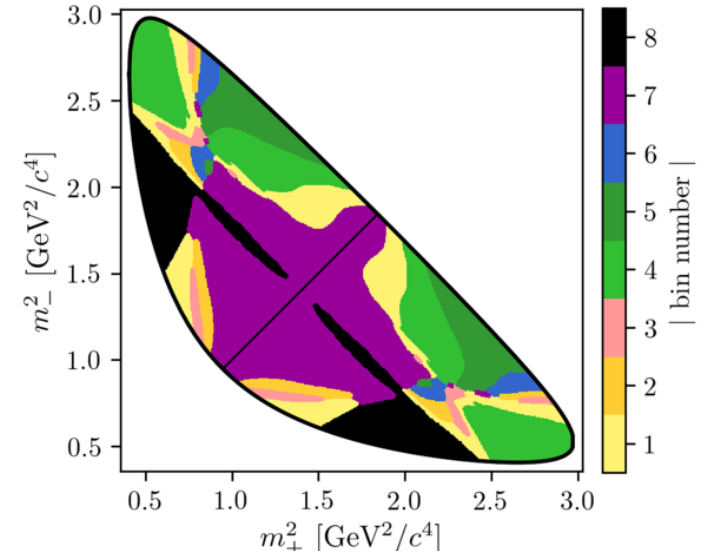
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$B^+ \rightarrow Dh^+, D \rightarrow K_S^0 h^+ h^-$

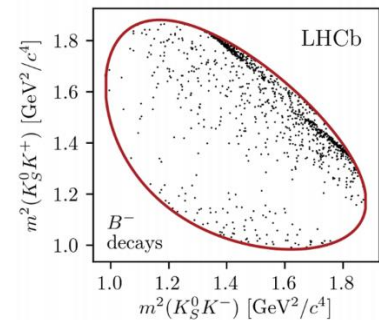
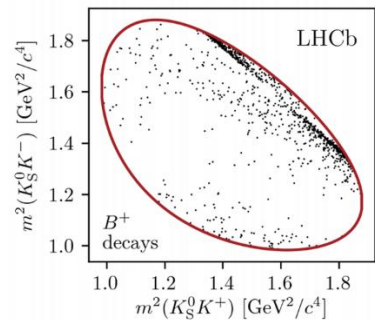
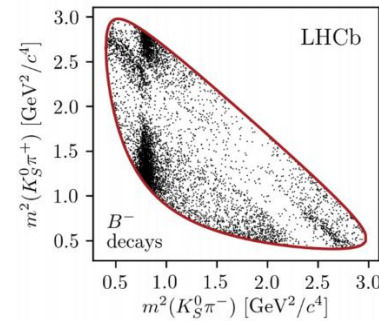
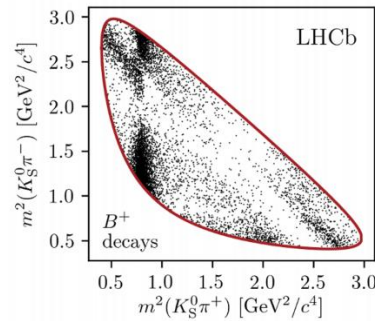
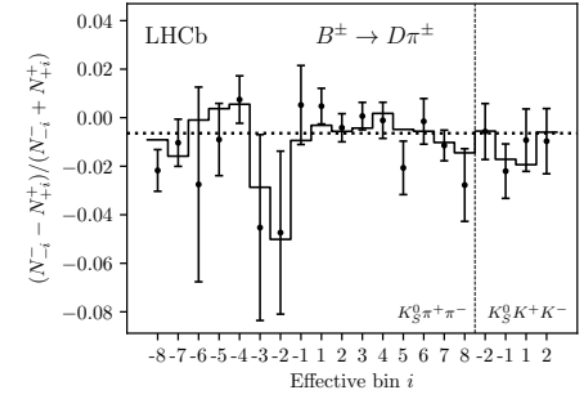
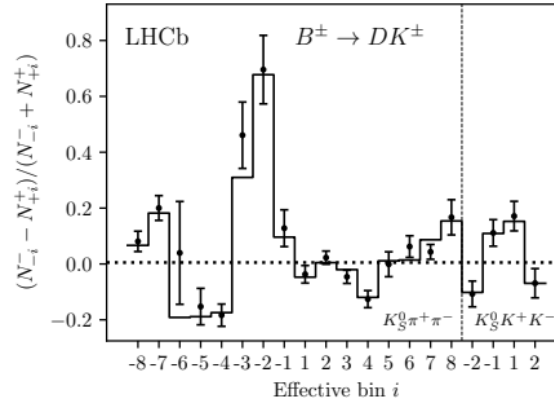
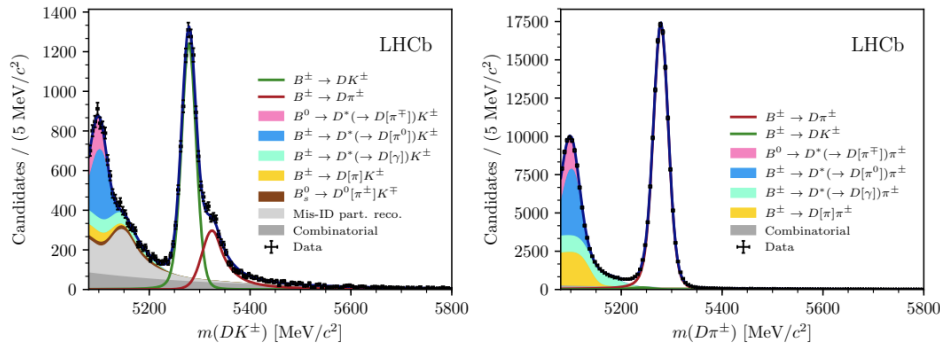
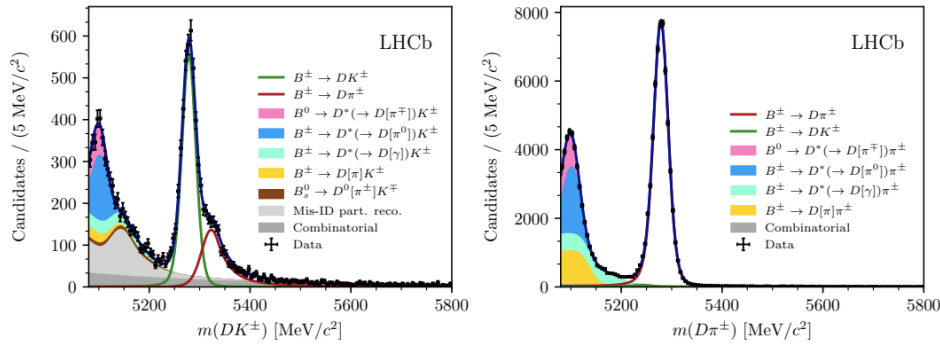
- The Run 1 and Run 2 data sample of $9 fb^{-1}$
- Type of 3 body D decay analysis at LHCb:
 - Model independent – method takes inputs from CLEO / BESIII experiments (smaller uncertainties and smaller sensitivity to the angle γ)
 - Model dependent – method performs an amplitude analysis of D decay (bigger uncertainties and better sensitivity of the angle γ)
- Simultaneous measurements of: $\gamma, r_B^{DK}, \delta_B^{DK}, r_B^{D\pi}, \delta_B^{D\pi}$
- Dalitz plot analysis: measurement of the yield in each bin of the Dalitz plot.

[PR D82 112006] [PR D102 052008]
- Strong phase input: c_i, s_i measured by CLEO and BESIII



Optimal binning schemes for $D \rightarrow K_S^0 K^+ K^-$ decays and $D \rightarrow K_S^0 \pi^+ \pi^-$ decays.

$B^+ \rightarrow Dh^+, D \rightarrow K_S^0 h^+ h^-$



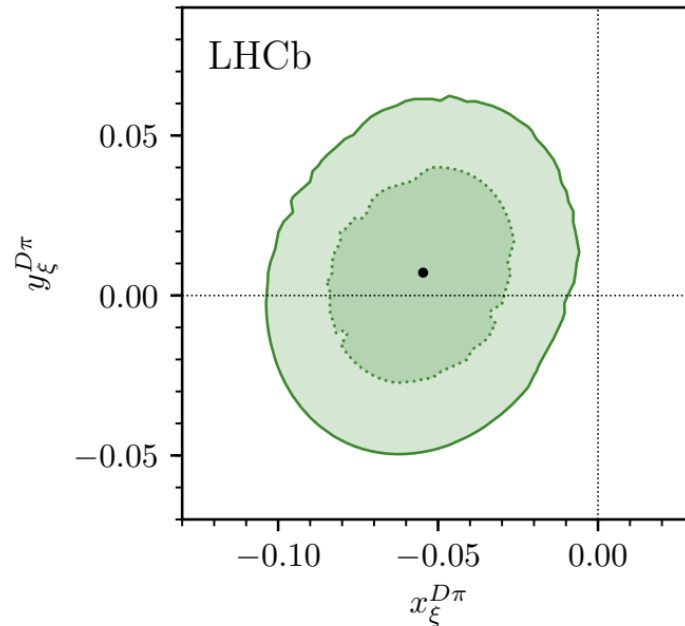
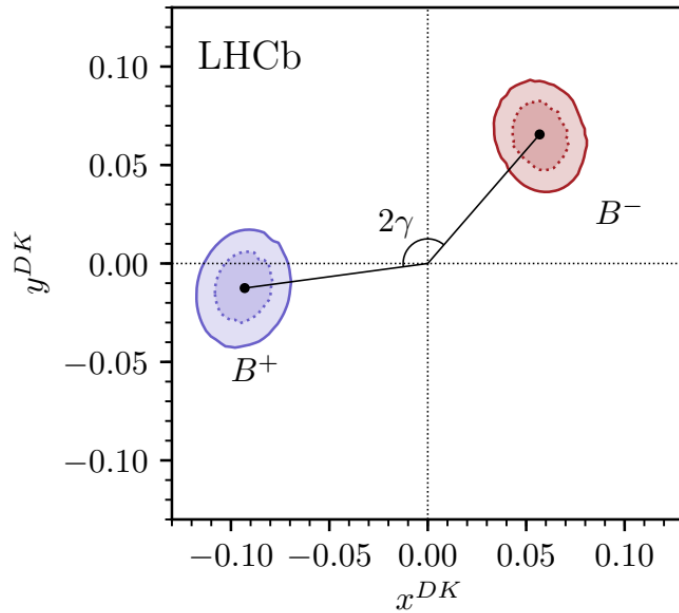
Selection of candidates and mass fit for each decay mode

Dalitz plot analysis

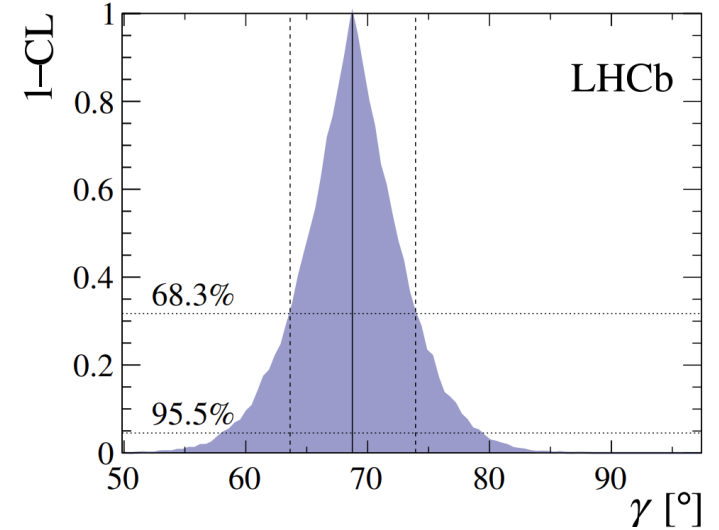
Measurement of the bin-by-bin asymmetries

$B^+ \rightarrow Dh^+, D \rightarrow K_S^0 h^+ h^-$

➤ Fit results for CPV observables:



The 1-CL contours for angle γ



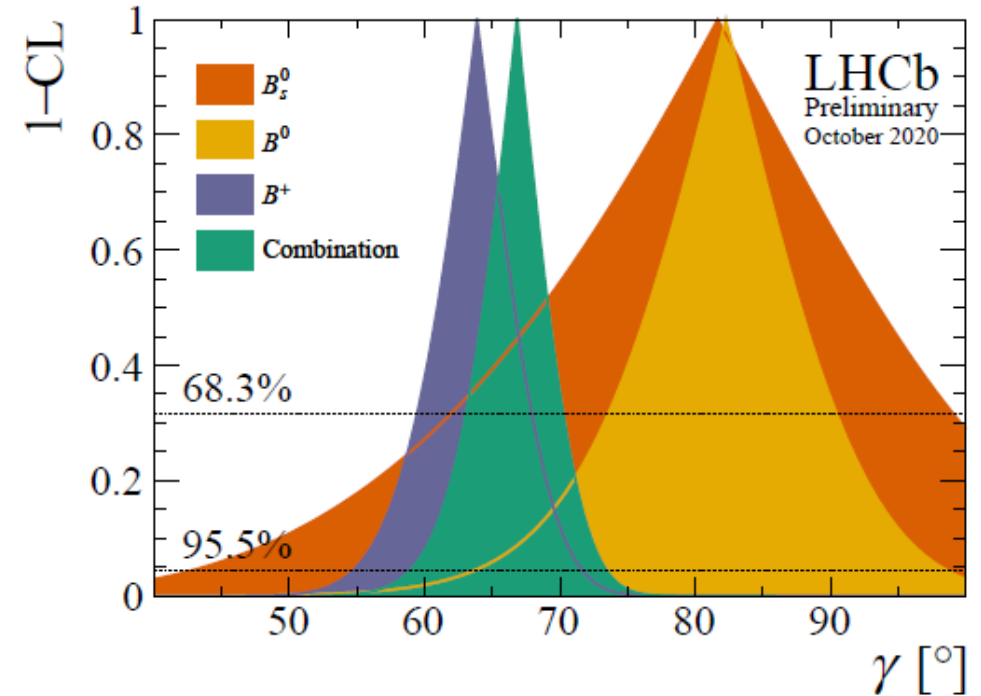
$$\begin{aligned} \gamma &= (68.7^{+5.2}_{-5.1})^\circ, \\ r_B^{DK^\pm} &= 0.0904^{+0.0077}_{-0.0075}, \\ \delta_B^{DK^\pm} &= (118.3^{+5.5}_{-5.6})^\circ, \\ r_B^{D\pi^\pm} &= 0.0050 \pm 0.0017, \\ \delta_B^{D\pi^\pm} &= (291^{+24}_{-26})^\circ. \end{aligned}$$

➤ The most precise single measurement of angle γ

γ combination by LHCb collaboration

[LHCb-CONF-2020-003]

- LHCb provides several CKM angle γ measurements using different:
 - B meson type (B^+ , B^0 , B_s^0)
 - Decay mode ($B^0 \rightarrow DK^{*0}$)
 - Measurement method (GLW, ADS, ...)
- LHCb combination is in excellent agreement with the indirect determinations of $\gamma = 65_{-2.7}^{+0.9}^\circ$ (CKM group) and $\gamma = 65.8 \pm 2.2^\circ$ (UT collaboration)



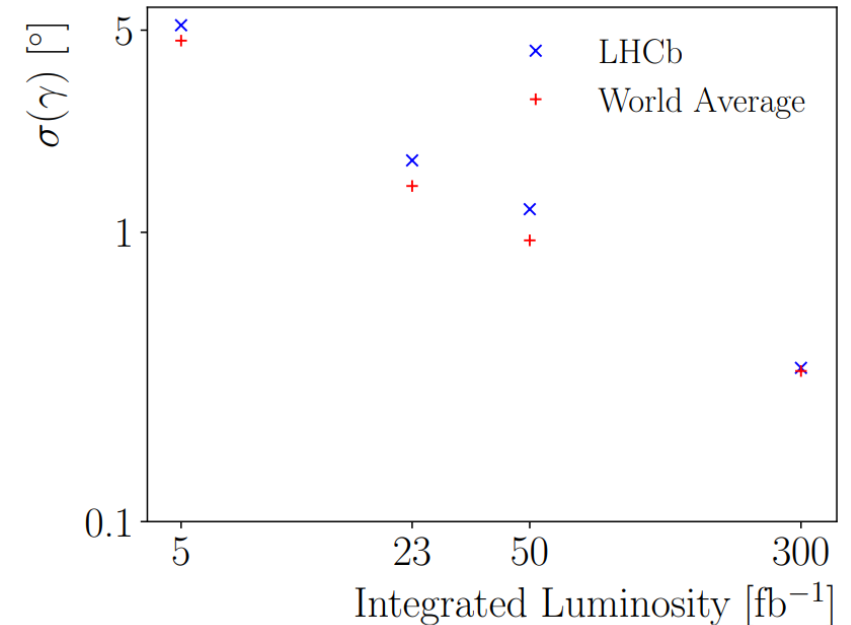
LHCb measurements :

$$\gamma = 67 \pm 4^\circ \text{ at } 68.3\% \text{ C.L.}$$

$$\gamma = 67_{-8}^{+7}^\circ \text{ at } 95.5\% \text{ C.L.}$$

Summary

- Many **new** and updated results of analysis over Run 1 & 2 data.
- Exploration of decays through resonance states and multi-body final states using a different methods and variety of beauty meson decays.
- Excellent results of studies of beauty to open charm processes which is good prospects for the **Run 3 & 4** measurements.

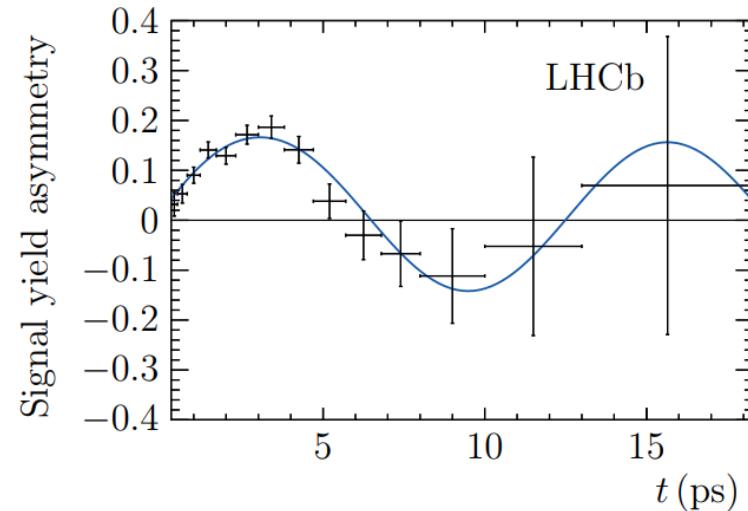
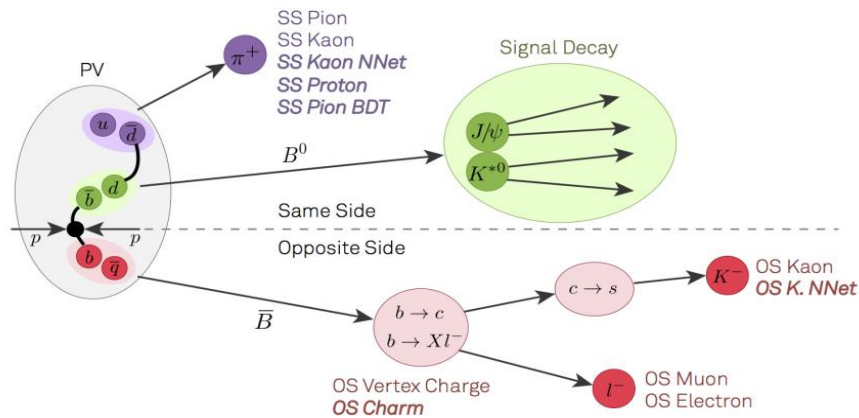


*Thank you for
attention.*

Backup

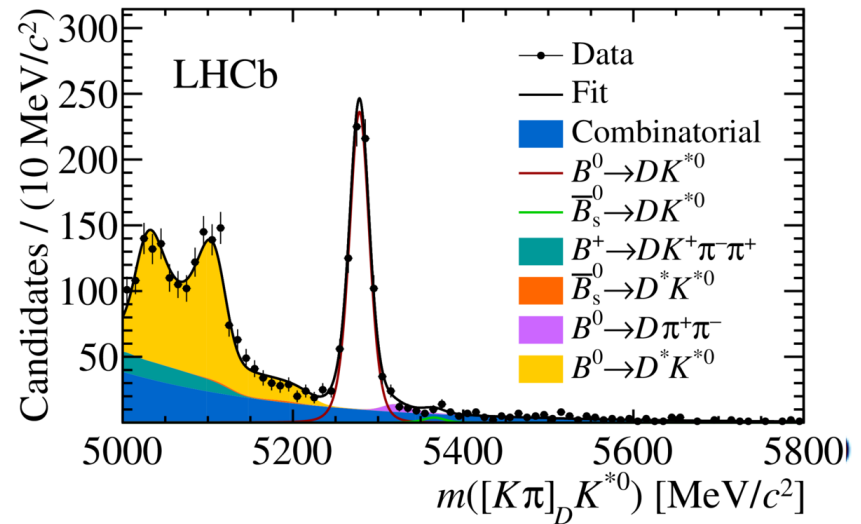
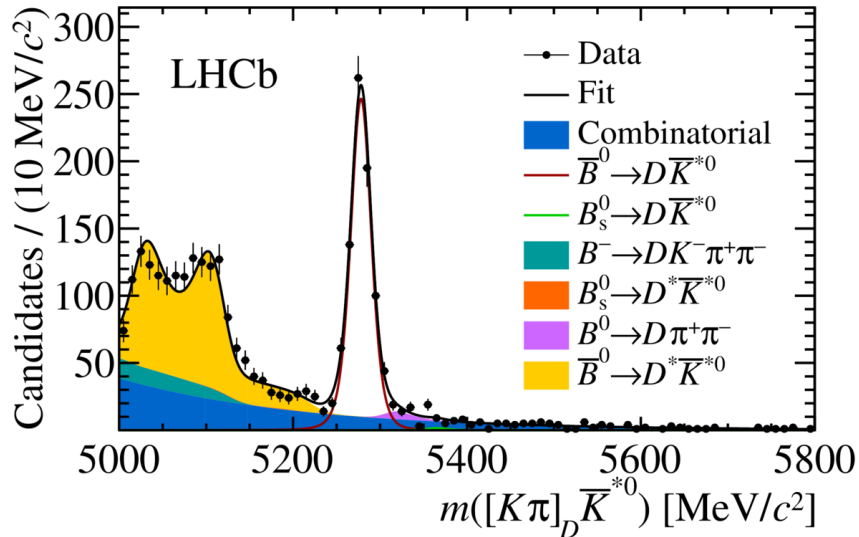
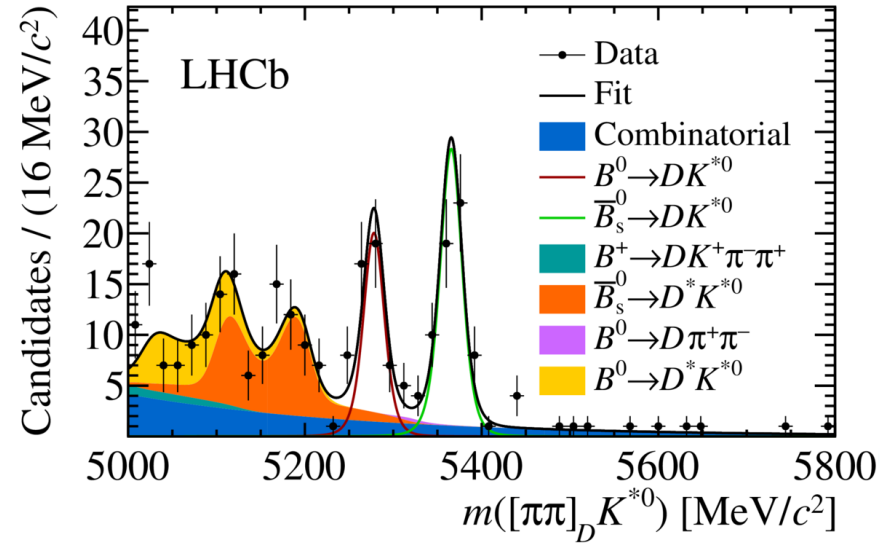
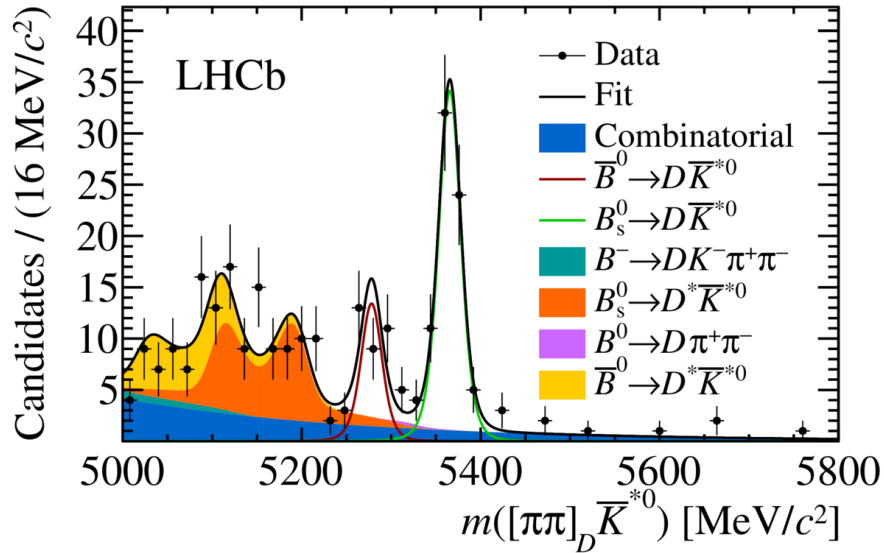
Backup: Flavour Tagging

- Flavor tagging algorithms tag the candidate as B or \bar{B} (tag decision) with some efficiency and mistag probability

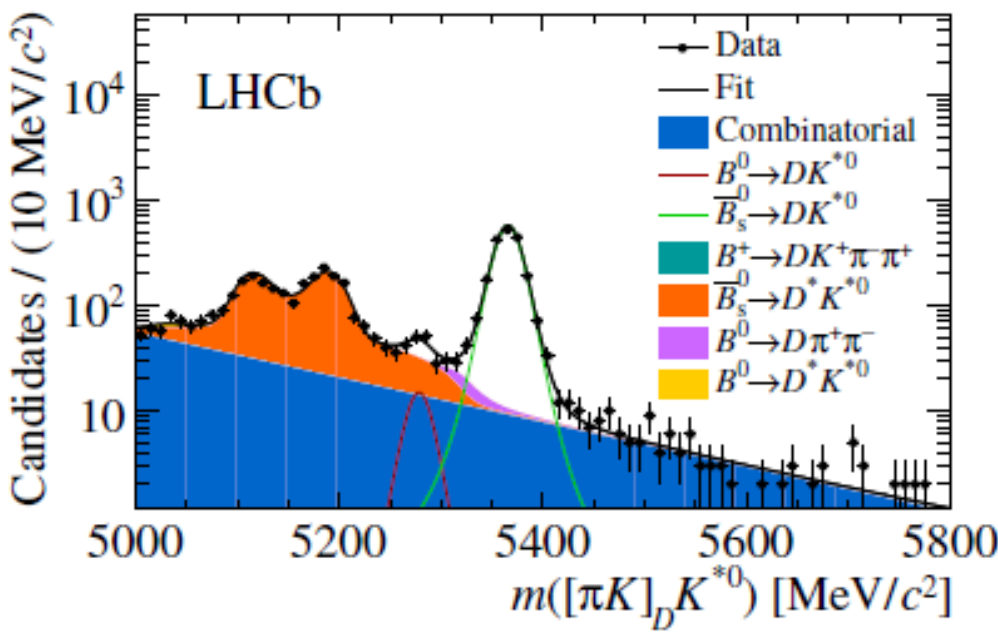
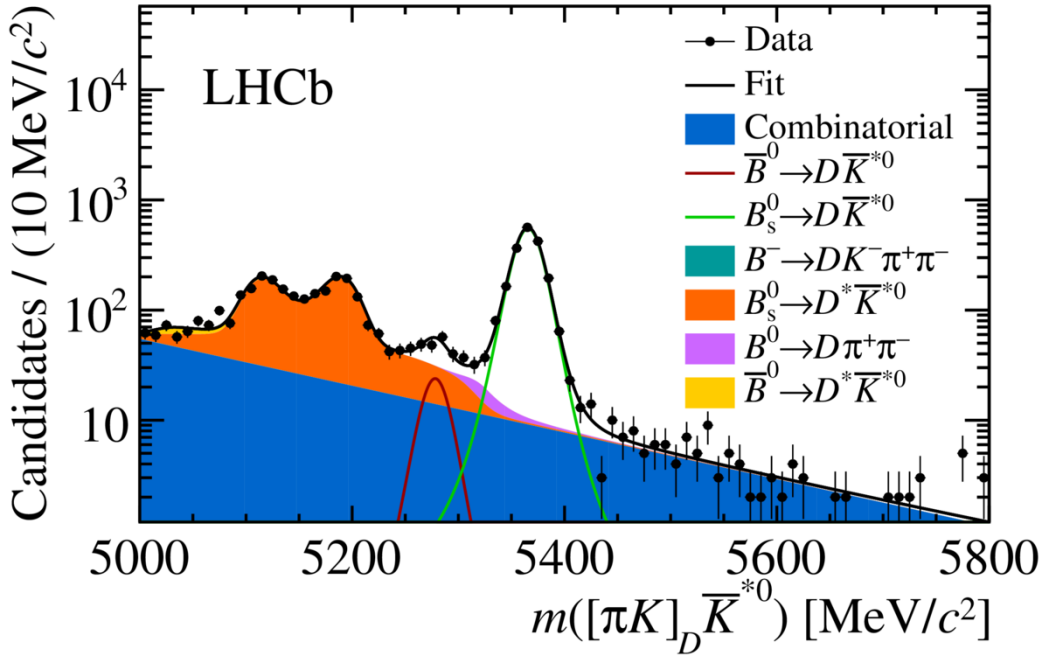


- Same Side (SS): correlation between flavor of the B meson and charge of the particle (pion, kaon, proton) produced close to the b -hadron in the PV.
- Opposite Side (OS): Correlation between flavor of the B meson and charged of charm meson and lepton or charge of tracks from Secondary Vertex.
- Calibrate tagging algorithm response using modes with known flavor (self-tagged, $B^+ \rightarrow J/\Psi K^+$, $B^+ \rightarrow D^0 \pi^+$).

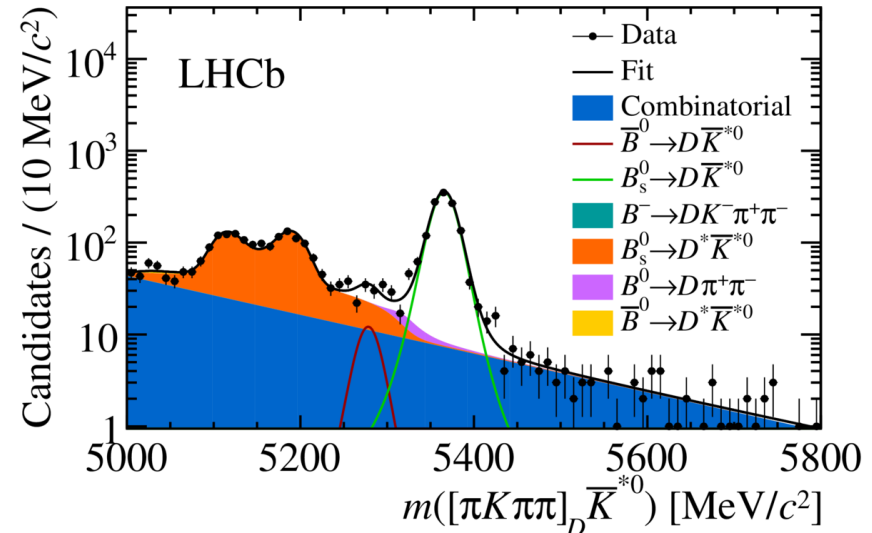
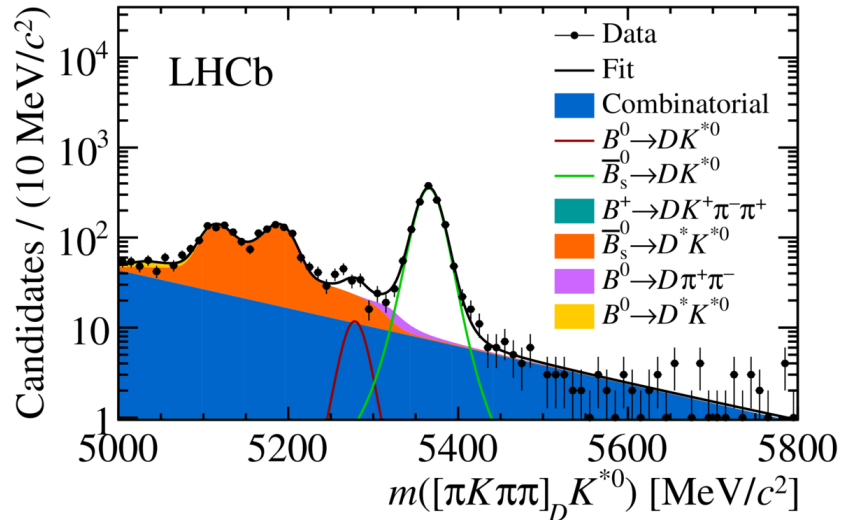
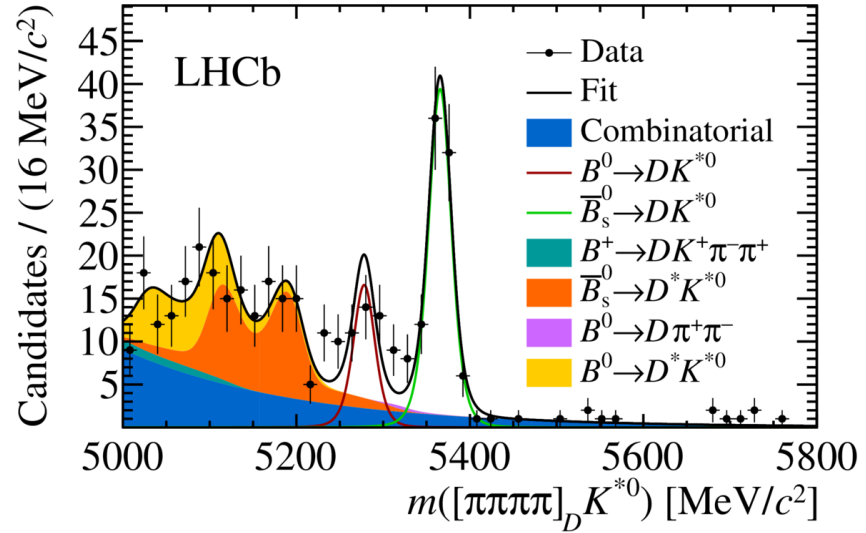
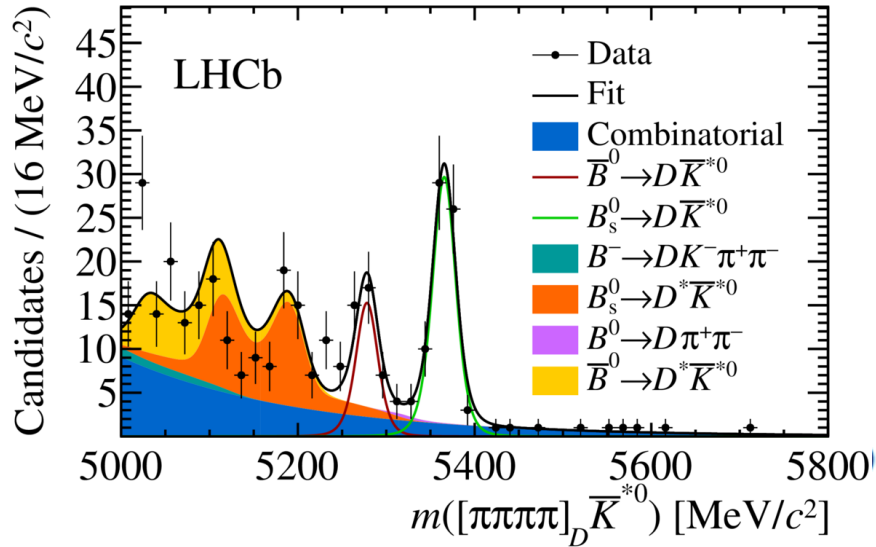
Backup: $B^0 \rightarrow DK^{*0}$



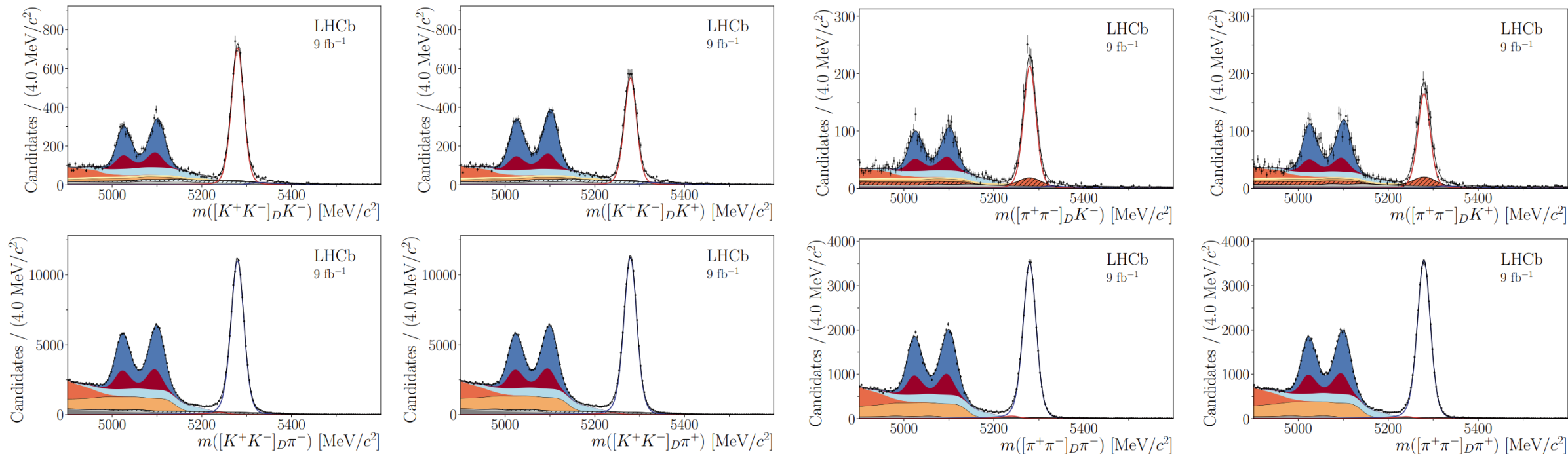
Backup: $B^0 \rightarrow DK^{*0}$



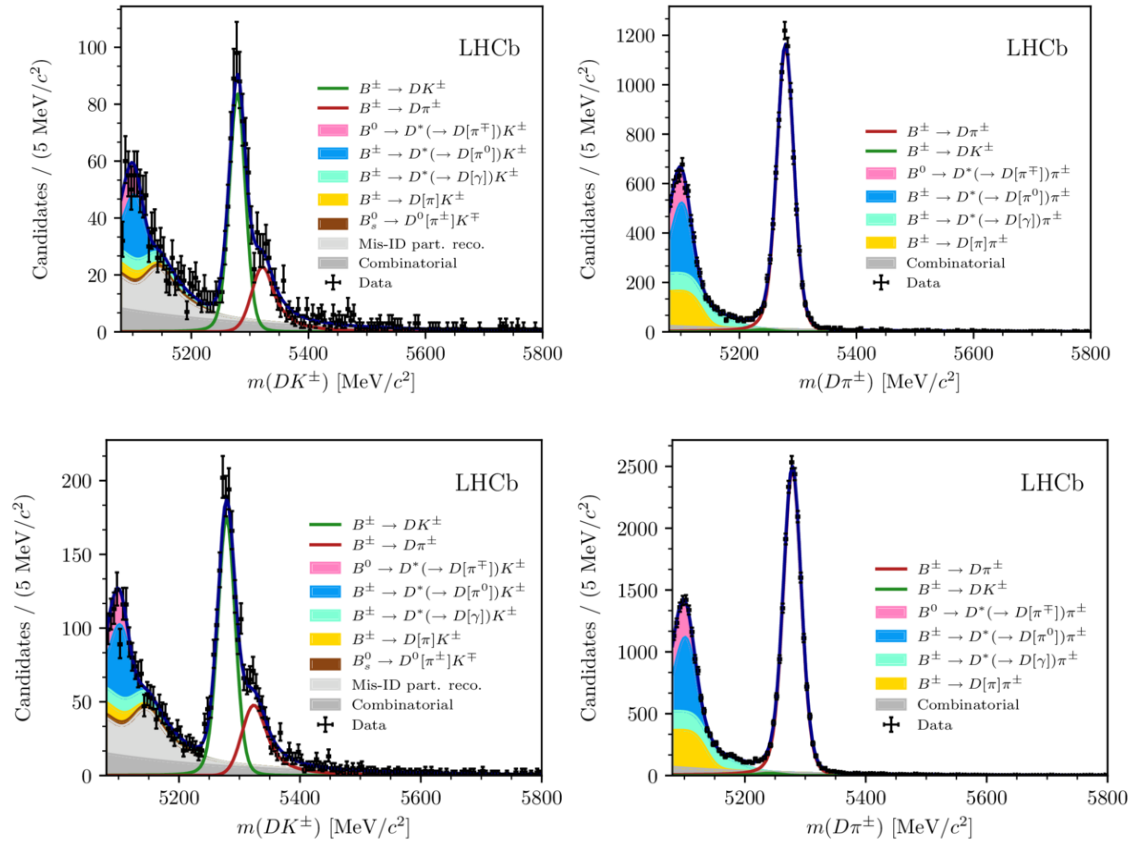
Backup: $B^0 \rightarrow DK^{*0}$



$B^+ \rightarrow D^{(*)} h^+$



$B^+ \rightarrow Dh^+, D \rightarrow K_S^0 h^+ h^-$



$$c_i \equiv \frac{\int_i dm_-^2 dm_+^2 |A_D(m_-^2, m_+^2)| |A_D(m_+^2, m_-^2)| \cos [\delta_D(m_-^2, m_+^2) - \delta_D(m_+^2, m_-^2)]}{\sqrt{\int_i dm_-^2 dm_+^2 |A_D(m_-^2, m_+^2)|^2 \int_i dm_-^2 dm_+^2 |A_D(m_+^2, m_-^2)|^2}}$$