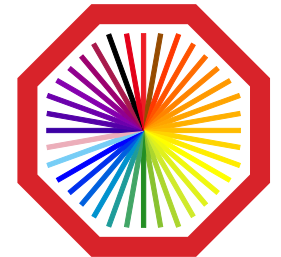




The Ohio State University



ALICE

**Studying the $a_0(980)$ tetraquark candidate
using $K^0_s K^\pm$ interactions
in the LHC ALICE Collaboration**

Thomas Humanic (Ohio State University)
for the ALICE Collaboration

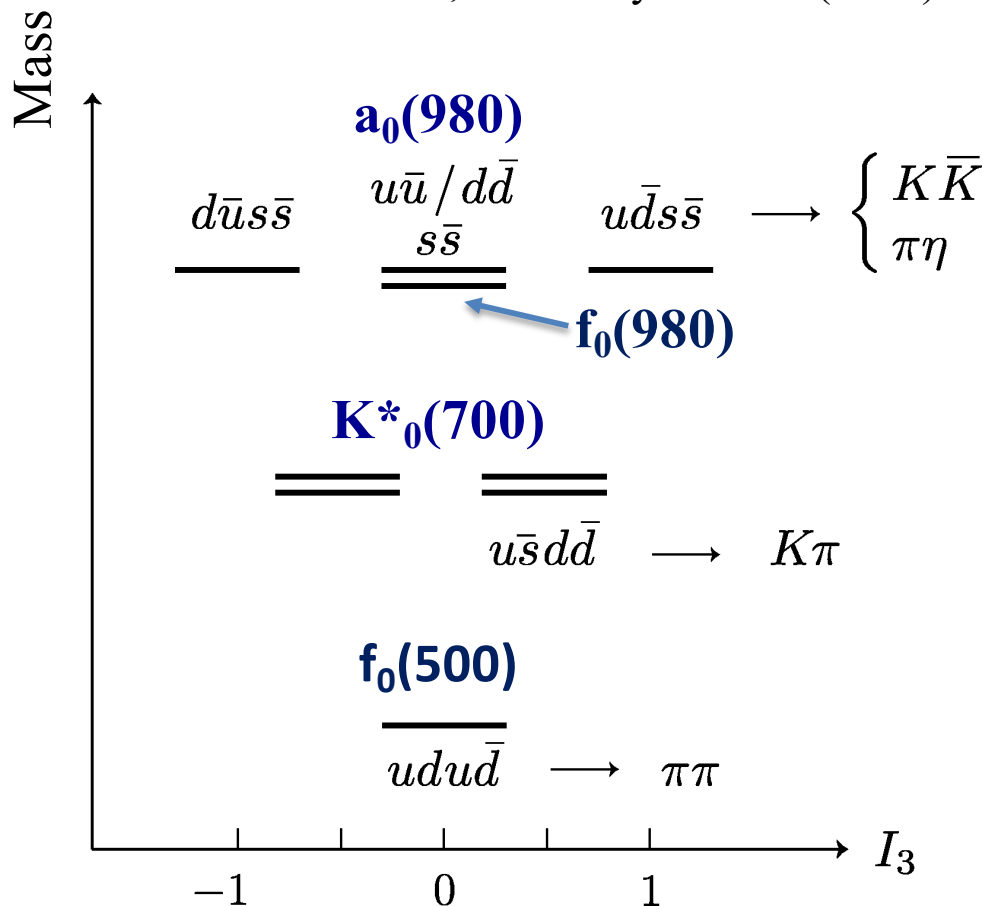
HADRON 2021

July 26 , 2021

Predicted low-lying tetraquark nonet with candidate mesons

Tetraquark nonet

Alford and Jaffe, Nucl. Phys. B 578 (2000)



Low-lying tetraquark states have been predicted for > 40 years.

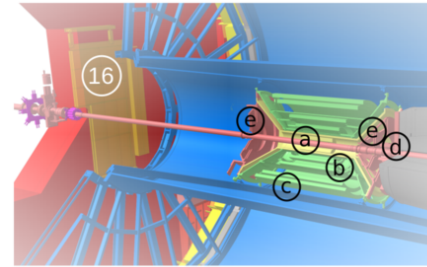
Candidate mesons with the expected masses, isospins and decay channels have been found:

e.g. $a_0(980)$, $f_0(980)$, $K^*_0(700)$, $f_0(500)$..

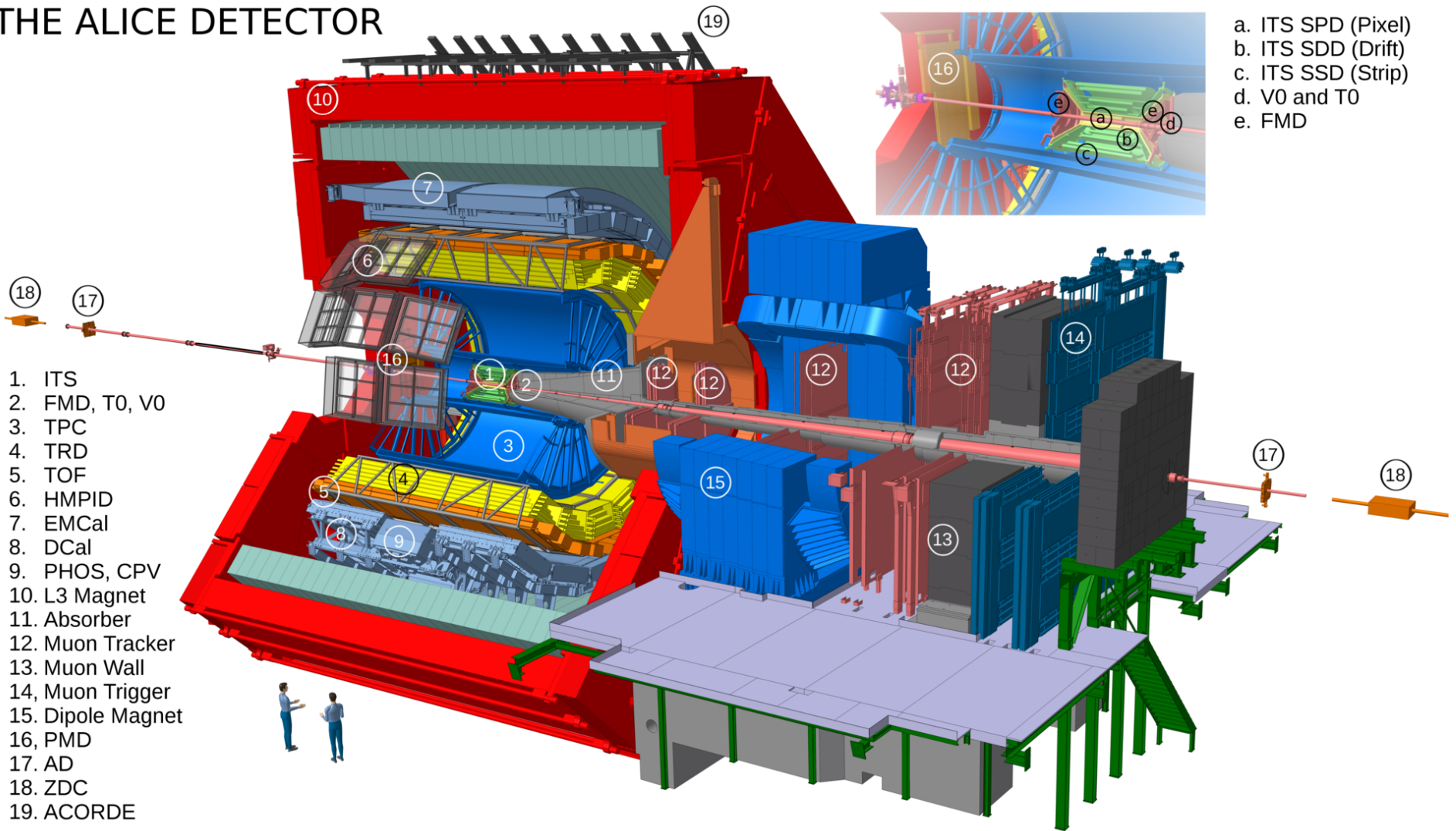
\rightarrow But, it is still controversial whether or not these mesons are four-quark states (e.g. see “Non-qq-bar Mesons” in 2021 Review of Particle Physics)

\rightarrow Study the $a_0(980)$ with $K^0_s K^\pm$ femtoscopy in pp and Pb-Pb collisions in the LHC ALICE Collaboration

THE ALICE DETECTOR



- a. ITS SPD (Pixel)
- b. ITS SDD (Drift)
- c. ITS SDD (Strip)
- d. V0 and T0
- e. FMD



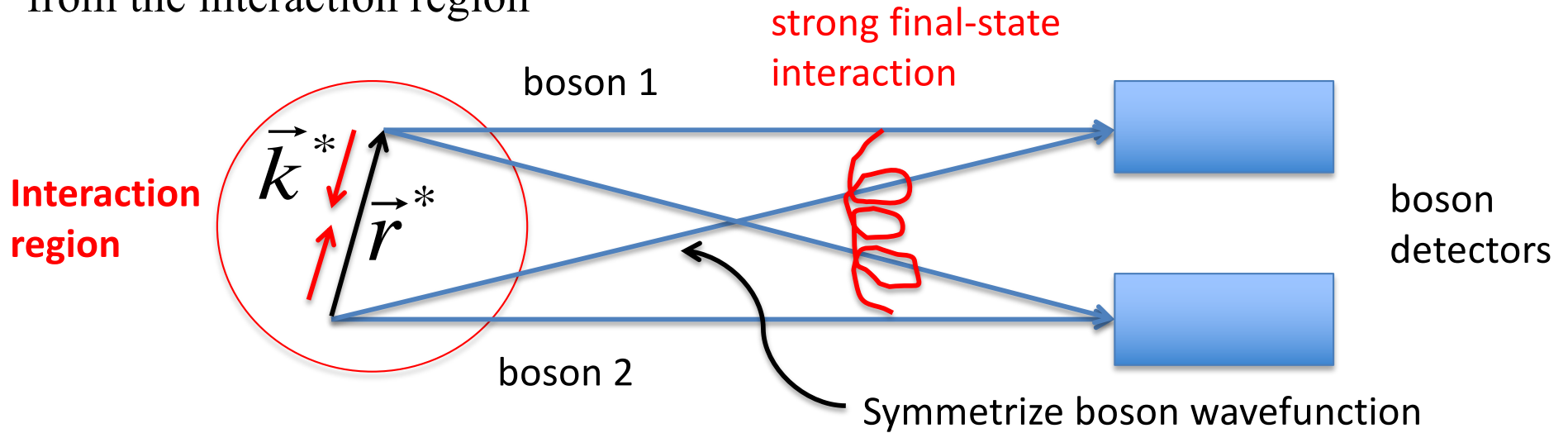
1. ITS
2. FMD, T0, V0
3. TPC
4. TRD
5. TOF
6. HMPID
7. EMCal
8. DCal
9. PHOS, CPV
10. L3 Magnet
11. Absorber
12. Muon Tracker
13. Muon Wall
14. Muon Trigger
15. Dipole Magnet
16. PMD
17. AD
18. ZDC
19. ACORDE

Data sets used in this analysis: → $\sqrt{s_{NN}} = 2.76 \text{ TeV Pb - Pb collisions, 0-10\% central}$
 $\sqrt{s} = 7 \text{ TeV pp collisions, minimum bias}$

Femtoscscopy with quantum statistics and strong final-state interactions

R. Lednicky and V.L. Lyuboshits, (Sov. J. Nucl. Phys. 35 (1982))

Consider the correlations of two **identical bosons**, e.g. $K^0_s K^0_s$, emitted from the interaction region



If \vec{r}^* and \vec{k}^* are the relative distance between the bosons and the momentum of each boson in the pair reference frame, then the non-symmetrized wavefunction describing the elastic interaction between the bosons is

$$\Psi_{-\vec{k}^*}(\vec{r}^*) = \underbrace{e^{-i\vec{k}^* \cdot \vec{r}^*}}_{\text{plane wave}} + \underbrace{f(\vec{k}^*)}_{\text{S-wave scattering amplitude}} \frac{e^{i\vec{k}^* \cdot \vec{r}^*}}{r^*}$$

s-wave FSI term

Assume the boson source density in the pair reference frame is a Gaussian with radius parameter, R ,

$$S(r^*) \sim \exp\left(-\frac{r^{*2}}{4R^2}\right)$$

The two-boson correlation function is calculated by integrating over the symmetrized wavefunction weighted by the boson source density,

$$C(k^*) = \int d^3\vec{r}^* S(r^*) \left| \Psi_{-\vec{k}^*}^S(\vec{r}^*) \right|^2$$

$$= 1 + \lambda e^{-4k^{*2}R^2} + \lambda\alpha \left[\left| \frac{f(k^*)}{R} \right|^2 + \frac{4\Re f(k^*)}{\sqrt{\pi}R} F_1(2Rk^*) - \frac{2\Im f(k^*)}{R} F_2(2Rk^*) \right]_{+\Delta C}$$

quantum statistics term
Final-state interaction term

$$\text{where } F_1(z) = \int_0^z dx \frac{e^{x^2-z^2}}{z} \quad F_2(z) = \frac{1-e^{-z^2}}{z}$$

The parameter λ is an empirical parameter that measures the correlation strength $\rightarrow \lambda = 1$ in the ideal case, and $\alpha = 0.5$ for $K_s^0 K_s^0$ correlations.

Scattering amplitude
for $K^0_s K^0_s$

$$f(k^*) = \frac{f_0(k^*) + f_1(k^*)}{2}$$

where,

$$f_I(k^*) = \frac{\gamma_I}{m_I^2 - s - i(\gamma_I k^* + \gamma'_I k'_I)}$$

$I = 0$ refers to the isospin-0 $f_0(980)$ resonance and $I = 1$ refers to the isospin-1 $a_0(980)$ resonance, and the γ_I are the couplings of the resonances to their decay channels.

$f_0(980)$ [1]	$I^G(J^{PC}) = 0^+(0^{++})$
Mass $m = 990 \pm 20$ MeV	
Full width $\Gamma = 10$ to 100 MeV	
$f_0(980)$ DECAY MODES	Fraction (Γ_i/Γ)
$\pi\pi$	dominant
$K\bar{K}$	seen
$\gamma\gamma$	seen
p (MeV/c)	
	476
	36
	495
$a_0(980)$ [1]	$I^G(J^{PC}) = 1^-(0^{++})$
Mass $m = 980 \pm 20$ MeV	
Full width $\Gamma = 50$ to 100 MeV	
$a_0(980)$ DECAY MODES	Fraction (Γ_i/Γ)
$\eta\pi$	dominant
$K\bar{K}$	seen
$\gamma\gamma$	seen
p (MeV/c)	
	319
	†
	490

From Particle Data Book for light
quark-antiquark mesons

$C(k^*)$ is measured experimentally as

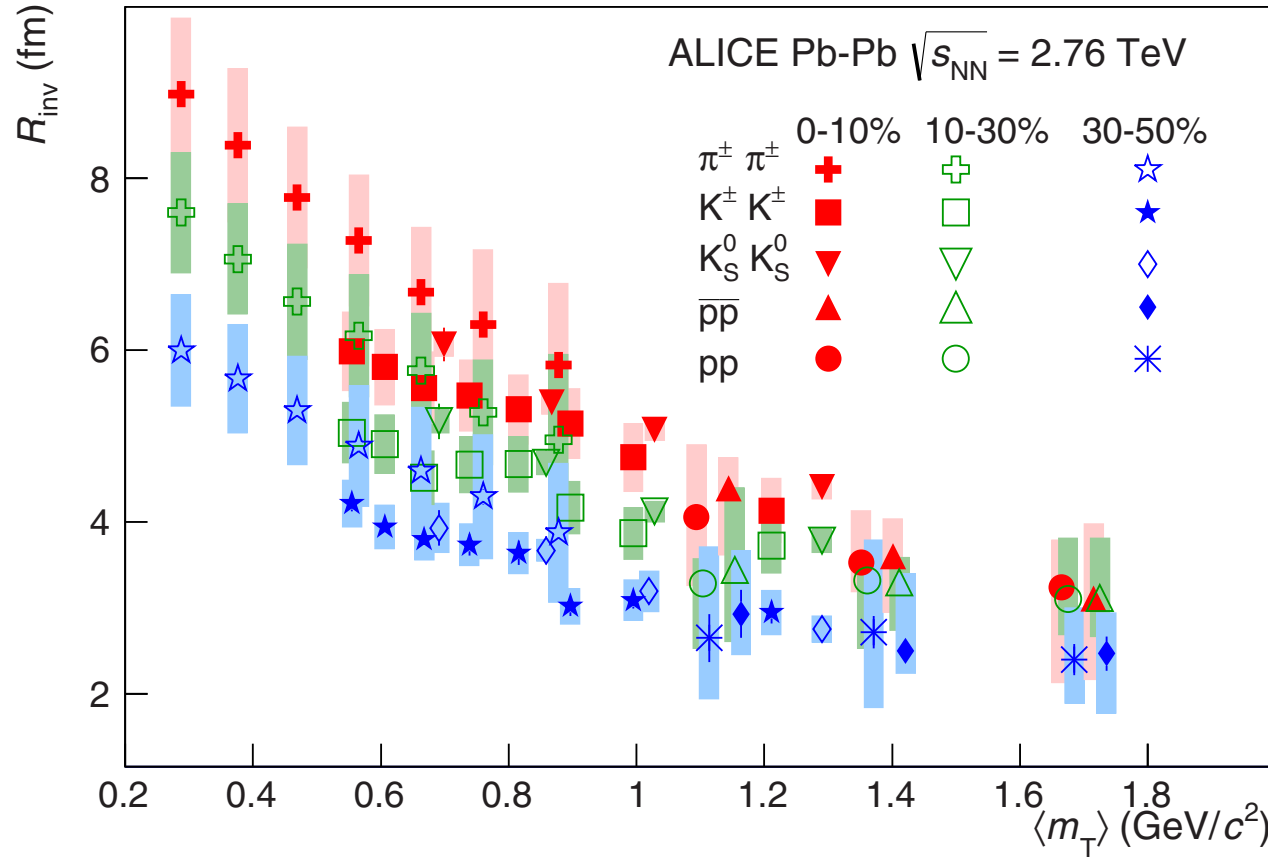
$$C(k^*) = \frac{A(k^*)}{B(k^*)}$$

Where $A(k^*)$ is the measured distribution of boson pairs from the same event, and $B(k^*)$ is the reference distribution of boson pairs from mixed events.

One extracts R and λ parameters from the data by fitting the Lednicky equation to this experimental $C(k^*)$

The LHC ALICE Experiment has published three femtoscopy papers using $K_S^0 K_S^0$ pairs to extract geometric information about the collision interaction region:

- 7 TeV pp $\rightarrow K_S^0 K_S^0$ Phys.Lett.B717 (2012)
- 2.76 TeV Pb-Pb $\rightarrow K_S^0 K_S^0, K^\pm K^\pm, \pi\pi, pp$ Phys.Rev.C92 (2015)
- 2.76 TeV Pb-Pb \rightarrow 3D $K_S^0 K_S^0, K^\pm K^\pm$ Phys.Rev.C96 (2017)



Phys.Rev.C92 (2015)

Radial flow effects and m_T scaling seen.

$$m_T = \sqrt{k_T^2 + m^2}$$

where

$$k_T = \frac{1}{2} |\vec{p}_{T1} + \vec{p}_{T2}|$$

$K_s^0 K^\pm$ femtoscopy

Pair-wise interactions present (or absent) for $K_s^0 K^\pm$ pairs

- non-identical pairs \rightarrow no quantum statistics
- K_s^0 is uncharged \rightarrow no Coulomb interaction
- $f_0(980)$ resonance is neutral \rightarrow no $f_0(980)$ strong interaction
- $a_0(980)$ resonance is isospin = 1 \rightarrow $a_0(980)$ strong interaction should be present for both $K_s^0 K^+$ and $K_s^0 K^-$ pairs

$\rightarrow K_s^0 K^\pm$ femtoscopy selects for the $a_0(980)^\pm$ as the FSI

Version of R. Lednicky equation used to extract (R, λ) for $K_S^0 K^\pm$

R. Lednicky and V.L. Lyuboshits, Sov. J. Nucl. Phys. 35 (1982)

$$C(k^*) = 1 + \frac{\lambda\alpha}{2} \left[\left| \frac{f(k^*)}{R} \right|^2 + \frac{4\Re f(k^*)}{\sqrt{\pi R}} F_1(2Rk^*) - \frac{2\Im f(k^*)}{R} F_2(2Rk^*) + \Delta C \right]$$

$\bar{K}^0 K^+$ or $K^0 K^-$

No quantum statistics
term or symmetrization

Since $|K_S^0\rangle = \frac{1}{\sqrt{2}} (|K^0\rangle + |\bar{K}^0\rangle)$ $\rightarrow \alpha = 1/2$, assuming no asymmetry

$$f(k^*) = \frac{\gamma_{a_0 \rightarrow K\bar{K}}}{m_{a_0}^2 - s - i\gamma_{a_0 \rightarrow K\bar{K}} k^* - i\gamma_{a_0 \rightarrow \pi\eta} k_{\pi\eta}}$$

Ref	m_{f_0}	$\gamma_{f_0 K\bar{K}}$	$\gamma_{f_0 \pi\pi}$	m_{a_0}	$\gamma_{a_0 K\bar{K}}$	$\gamma_{a_0 \pi\eta}$
[15, 16]	0.967	0.34	0.089	1.003	0.8365	0.4580

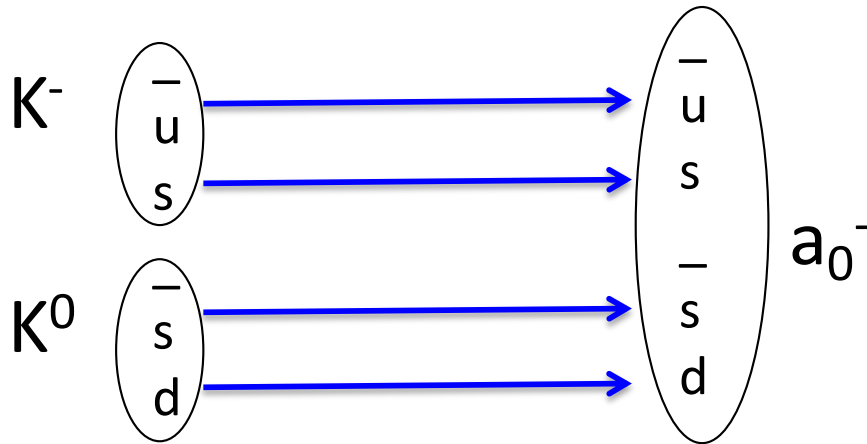
The f_0 and a_0 masses and coupling parameters used in the present analysis, all in GeV.

[15] N. N. Achasov and A. V. Kiselev, "The New analysis of the KLOE data on the $\phi \rightarrow \eta \pi^0 \gamma$ decay," *Phys. Rev. D* 68 (2003)

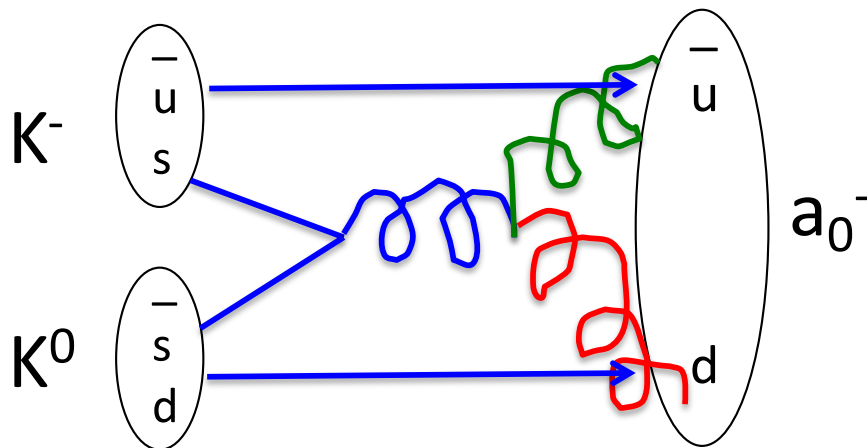
[16] ALICE Collaboration, K. Mikhaylov, "K+K- correlations in Pb-Pb collisions at $\sqrt{s_{NN}} = 2.76$ TeV by ALICE at the LHC," *Phys. Part. Nucl. (WPCF 2019, Dubna)* (2020)

Two scenarios for FSI of $K^0 K^- \rightarrow a_0(980)^- \rightarrow \begin{cases} K^0 K^- \\ \eta \pi^- \end{cases}$

Tetraquark vs. Diquark



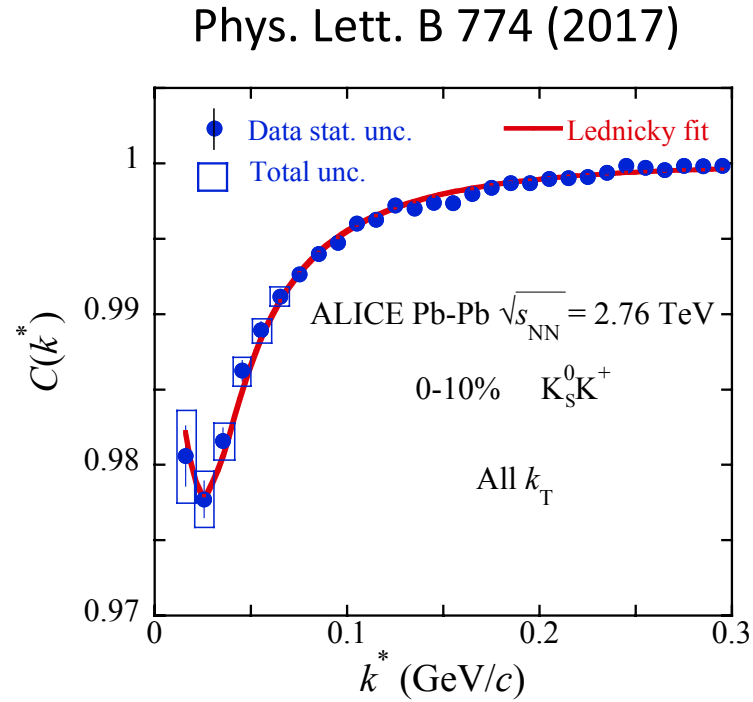
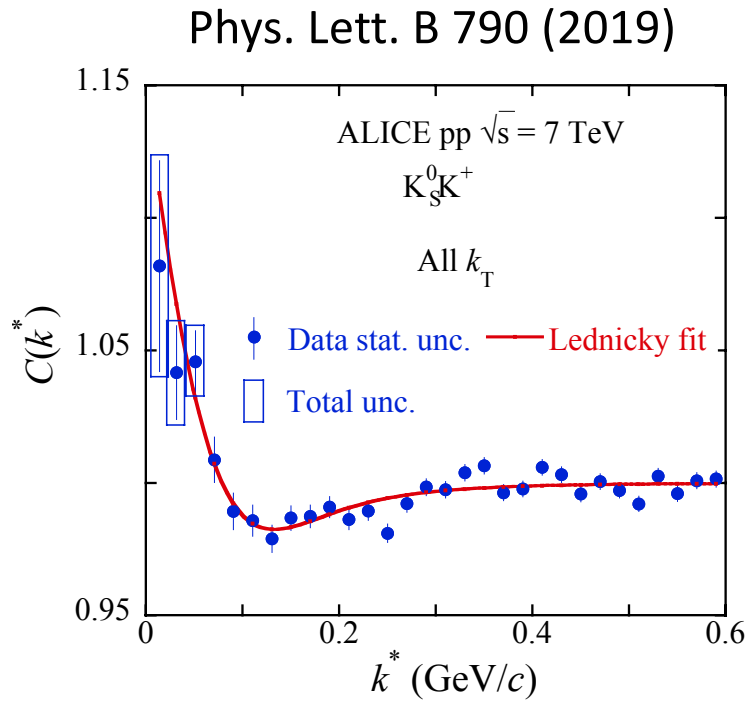
Tetraquark formation is a 1st-order process that proceeds through the direct transfer of existing quarks to the a_0^- from the collision of $K^0 K^-$



Diquark formation is a higher-order process requiring the annihilation of the strange quarks in the $K^0 K^-$ collision and transfer of energy via gluons to a_0^-

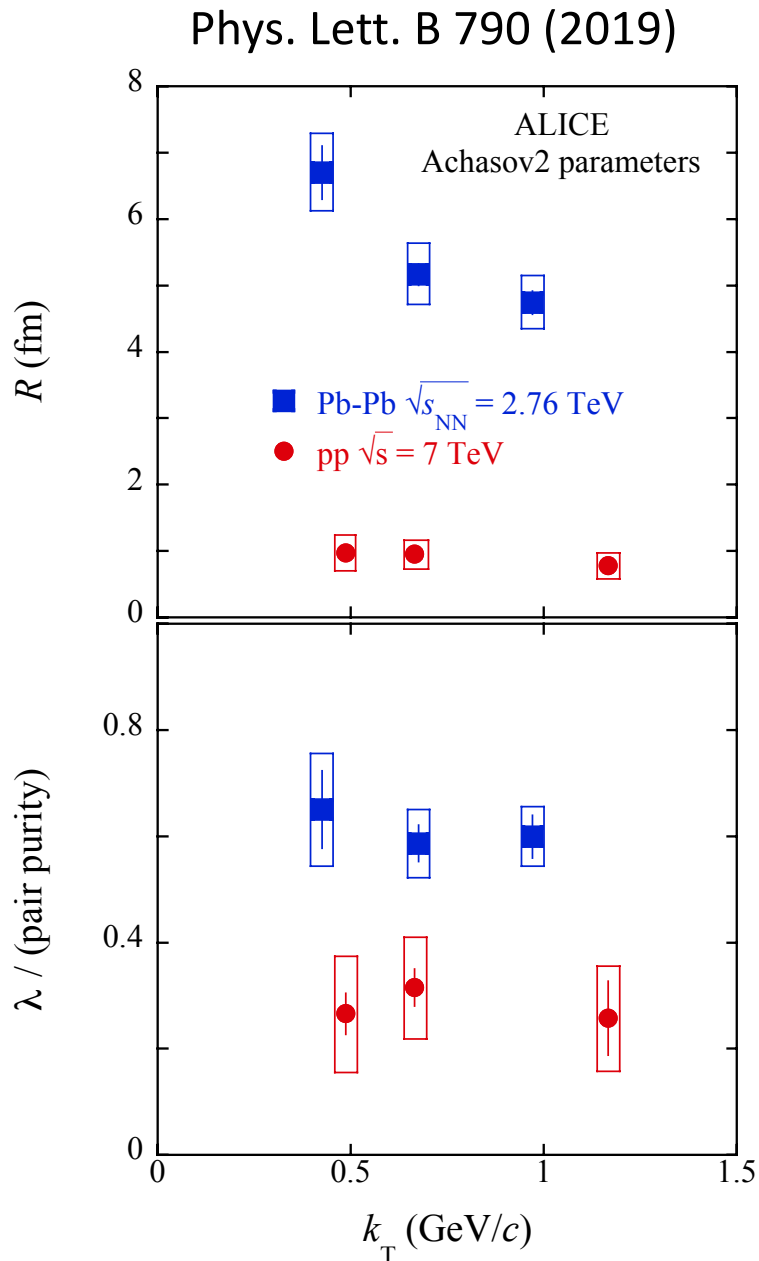
Can we see a signature of Tetraquark vs. Diquark in femtoscopy?

Examples of $K_S^0 K^\pm$ correlation functions from ALICE with Lednicky fits



The Lednicky equation with the assumption of an $a_0(980)$ FSI models the different shapes of the measured correlation functions well for both large and small systems for $K_S^0 K^\pm$ correlations!

ALICE results for $K^0_S K^\pm$ femtoscopy in pp and Pb-Pb collisions



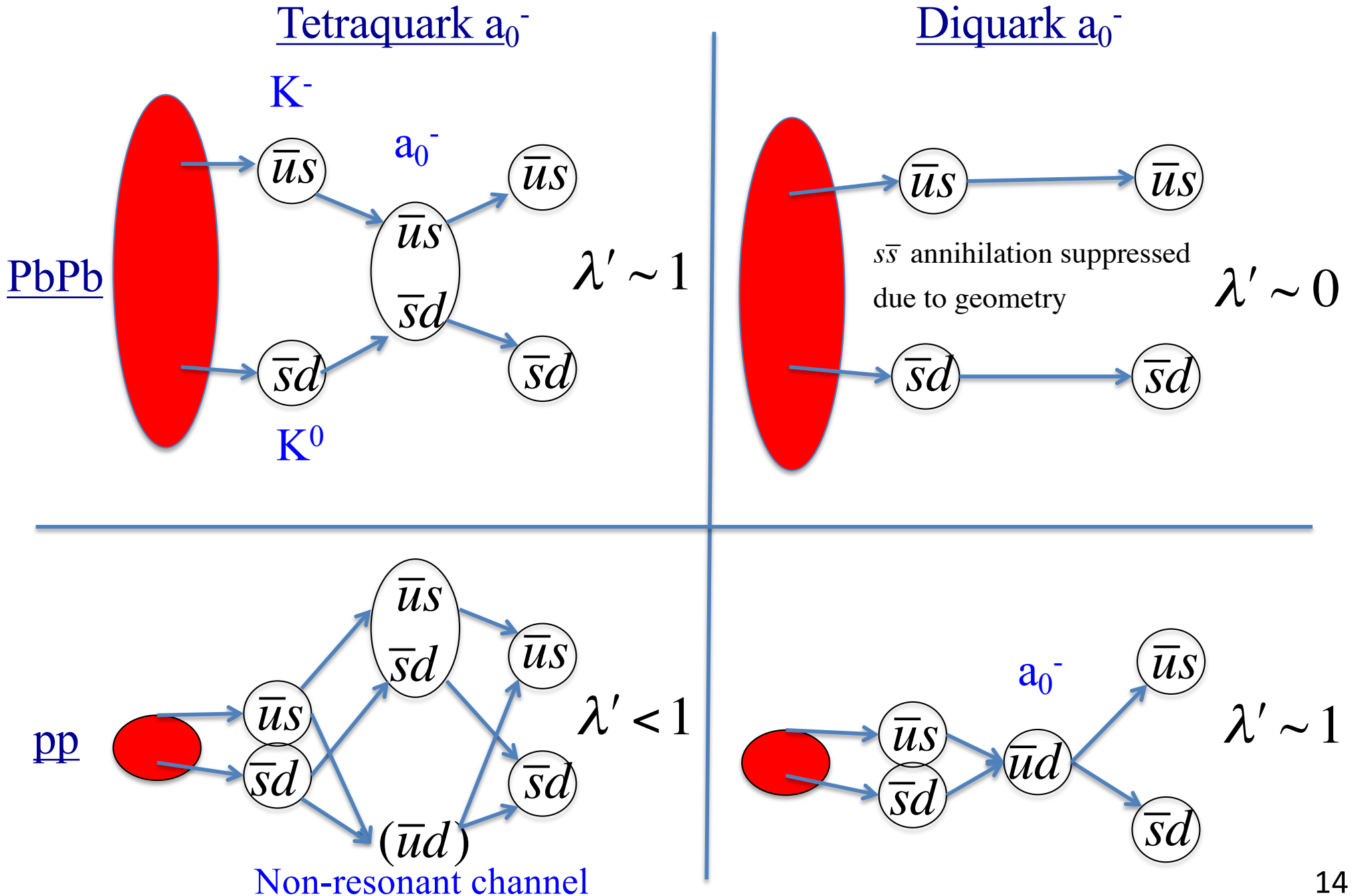
Observations for R :

- $R(\text{Pb-Pb}) > R(\text{pp})$
- $R(\text{Pb-Pb}) \sim 5\text{-}6$ fm, $R(\text{pp}) \sim 1$ fm, both as expected from $r_0 A^{1/3}$
- For Pb-Pb, R decreases significantly for increasing k_T , as expected for hydrodynamic flow effects
- For pp, R is not sensitive to changes in k_T as expected since flow mostly not present for pp

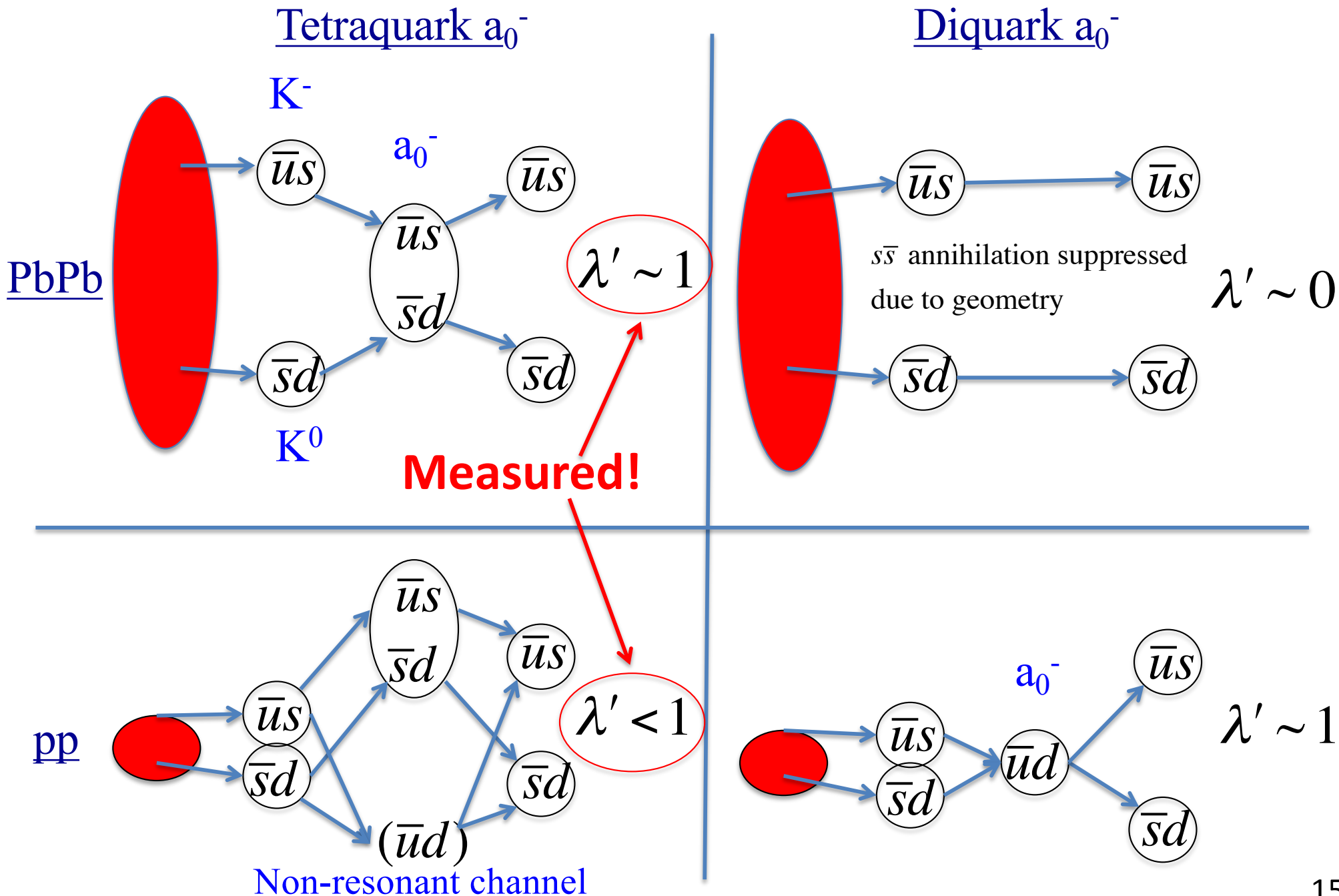
Observations for λ :

- $\lambda(\text{Pb-Pb}) > \lambda(\text{pp})$
- $\lambda(\text{Pb-Pb}) \sim 0.6$, $\lambda(\text{pp}) \sim 0.3$
- For Pb-Pb, λ is about the same as is measured for $K^0_S K^0_S$
- For pp, λ is also significantly less than what is measured in pp for $K^0_S K^0_S$

$\lambda' \equiv \lambda_{K^0 K^-} / \lambda_{KK}$ for $\bar{u}s\bar{s}d$ vs. $\bar{u}d$ a_0^- expected from geometry



$\lambda' \equiv \lambda_{K^0 K^-} / \lambda_{KK}$ for $\bar{u}s\bar{s}d$ vs. $\bar{u}d$ a_0^- expected from geometry



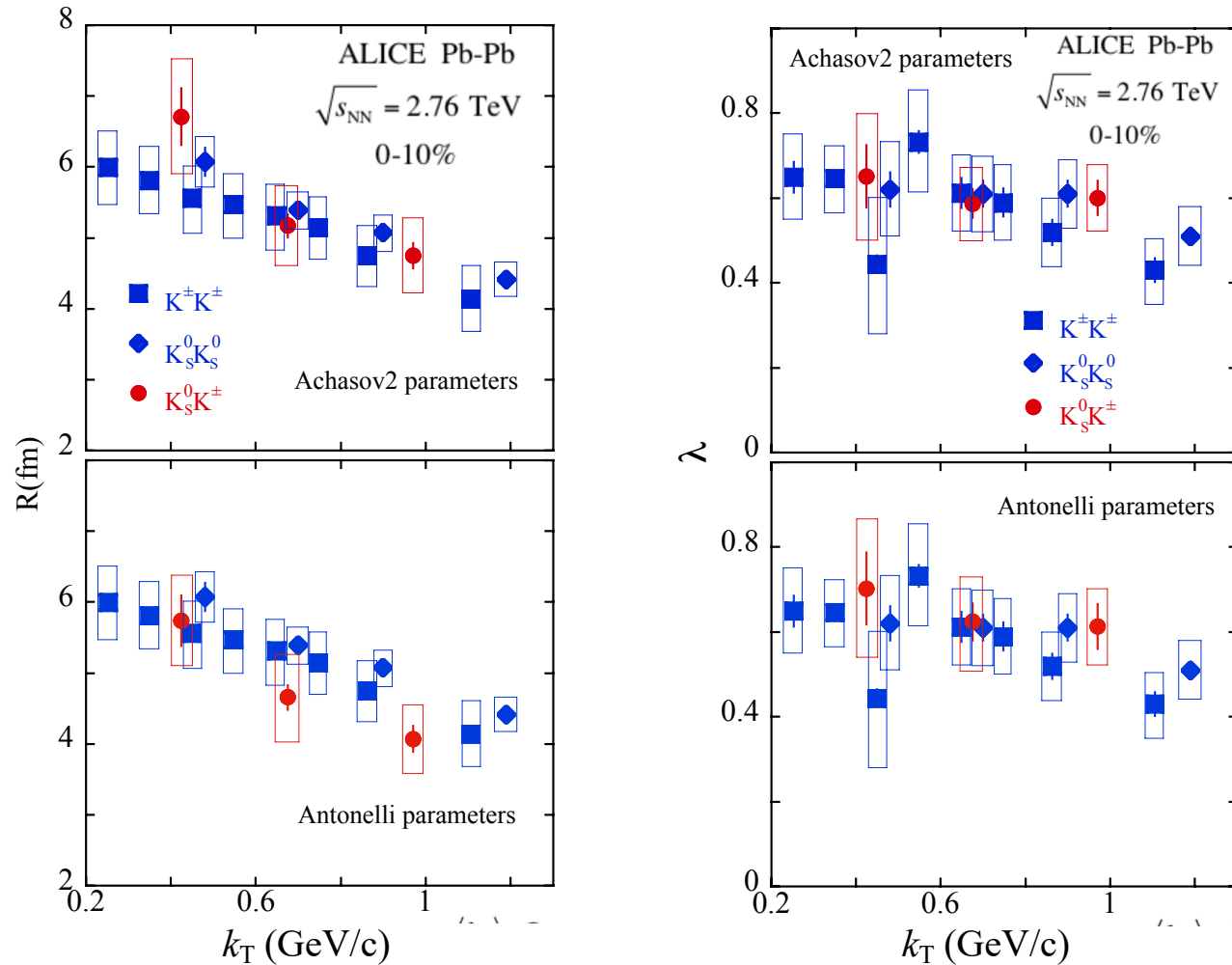
Summary

- $K^0_S K^\pm$ femtoscopic analyses in $\sqrt{s_{NN}} = 2.76$ TeV Pb-Pb and $\sqrt{s} = 7$ TeV pp collisions from ALICE were shown
- Main physics take-aways from the $K^0_S K^\pm$ analyses:
 - 1) The extracted R parameters are as expected in Pb-Pb and pp collisions
 - 2) $\lambda(pp) < \lambda(\text{Pb-Pb})$, whereas $\lambda(\text{Pb-Pb})$ agrees with the values extracted in $K^0_S K^0_S$ measurements
 - 3) A simple geometric model used to explain the results presented in 2) is suggestive of the $a_0(980)$ being a tetraquark state.**

Backup slides

Results for R and λ from 2.76 TeV Pb-Pb for $K_S^0 K^\pm$ vs. $K_S^0 K_S^0$ and $K^\pm K^\pm$

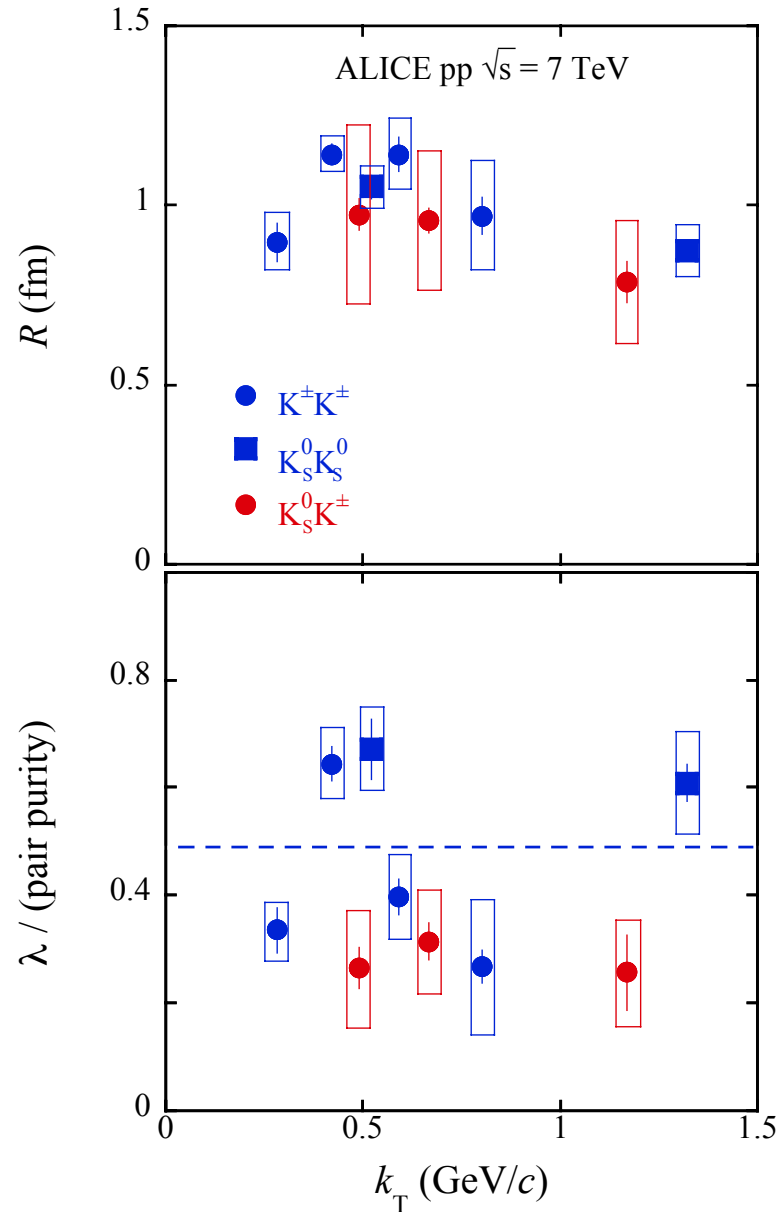
ALICE Collaboration, S. Acharya *et al.*, *Phys. Lett. B* 774 (2017)



- * $K_S^0 K^\pm$ R and λ agree with identical kaon results best for Achasov parameters
- * $\lambda < 1$ due to long-lived resonance decay (e.g. $K^* \rightarrow K\pi$, estimate $\lambda \sim 0.55$ from K^*)
- Agreement of $K_S^0 K^\pm$ λ with identical kaons \rightarrow FSI goes solely through a_0 channel**
- \rightarrow no non-resonant channel present**

Results for R and λ from 7 TeV pp for $K_S^0 K^\pm$ vs. $K_S^0 K_S^0$ and $K^\pm K^\pm$

ALICE Collaboration, S. Acharya *et al.*, *Phys. Lett. B* 790 (2019)



* The R values all agree within uncertainties

* $\lambda(K_S^0 K^\pm) < \lambda(K_S^0 K_S^0)$

The dashed line is the average of the identical-kaon λ parameters.