

Exotics Interpretation

Towards Theoretical Understanding of Exotic Heavy Hadrons from QCD

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research support from Department of Energy

Towards Theoretical Understanding of Exotic Heavy Hadrons from QCD

- Exotic heavy (XYZ) hadrons
- Lattice QCD and Effective Field Theories
- Born-Oppenheimer approach
- Summary

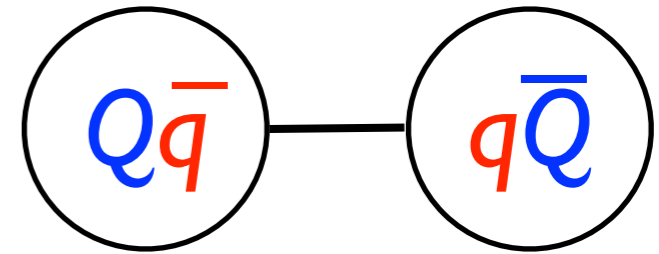
Exotic Heavy Hadrons

more than 2 dozen new $c\bar{c}$ and $b\bar{b}$ mesons
and several new $c\bar{c}$ baryons
discovered since 2003

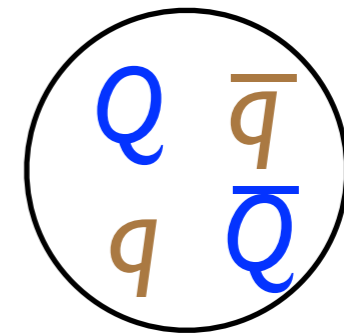
- contain heavy quark and antiquark
plus additional light constituents
- tetraquark mesons with light quark, antiquark
pentaquark baryons with three light quarks
- many are surprisingly narrow
- major challenge to our understanding of QCD spectrum!

Models for XYZ Mesons

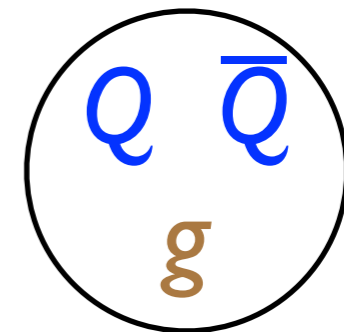
- meson molecule



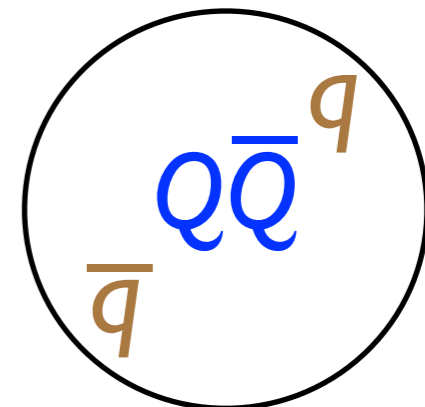
- quarkonium tetraquark



- quarkonium hybrid

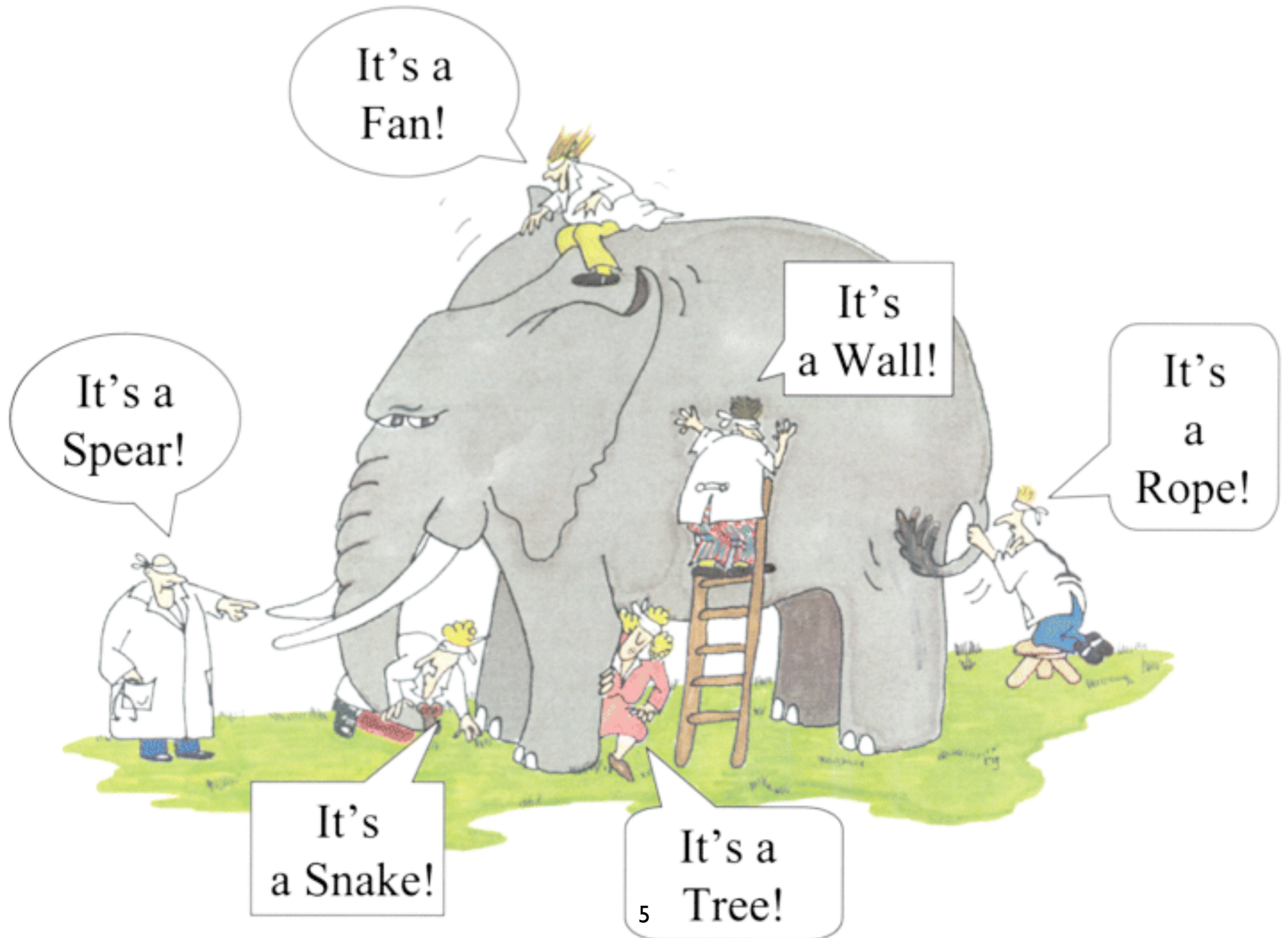


- hadro-quarkonium



- kinematic effect

Models for XYZ Mesons



Models for *XYZ* Hadrons

- little connection with fundamental theory **QCD**
constituents: degrees of freedom from **QCD**
interactions: purely phenomenological
- some success in describing individual *XYZ* hadrons
- no success in revealing pattern of *XYZ* hadrons

CHARM 2018

Novosibirsk May 2018

Steve Olsen: “The XYZ mesons: what they aren't”

Compare properties for 6 XYZ mesons with established J^{PC}
 $X(3872)$, $X(3915)$, $Y(4220)$, $Z_c(3900)$, $Z_c(4020)$, $Z(4430)$

with model expectations for

molecule, tetraquark, charmonium hybrid, hadro-charmonium, kinematic effect

“No single model can satisfactorily explain all the results.
If we are ever to have a coherent comprehensive
understanding of the XYZ particles, a new idea is needed.”

Developments since CHARM 2018

Aug 2018	BESIII	$Y(4220) \rightarrow \pi^+ D^0 D^{*-}$	1st open-charm decay of Y
Sept 2018	LHCb	$Z_c^-(4100) \rightarrow \eta_c \pi^-$	1st decay into 2 pseudoscalars
April 2019	LHCb	updated analysis of $c\bar{c}$ pentaquark decaying into $J/\psi p$ new narrow state $P_c(4312)$	
Dec 2019	Belle	$Y(4626) \rightarrow D_s^+ D_{s1}^-$	1st decay of Y into strange mesons
Sept 2020	LHCb	$X(2900) \rightarrow D^- K^+$	1st tetraquark with 4 flavors
Nov 2020	BESIII	$Z_c^-(3885) \rightarrow D_s^0 D^{*0}$	1st strange $c\bar{c}$ tetraquark
June 2020	LHCb	structure in J/ψ pair spectrum	1st $cc\bar{c}\bar{c}$ tetraquark ?

there is still no

“coherent comprehensive understanding of the XYZ particles”

Doubly Heavy Hadrons

heavy quarks: $Q = b$ or c

light quarks: $q = u$ or d or s

quarkonium: $Q \bar{Q}$
quarkonium hybrids: $Q \bar{Q} g$
quarkonium tetraquarks: $Q \bar{Q} q \bar{q}$
quarkonium pentaquarks: $Q \bar{Q} q q q$

doubly heavy baryons: $Q Q q$
doubly heavy tetraquarks: $Q Q \bar{q} \bar{q}$

coherent comprehensive framework ??

Approaches within QCD

fundamental fields: quarks and gluons

parameters: α_s , quark masses

- Lattice QCD
- Effective field theories
(NRQCD, pNRQCD, BOEFT, ...)
- QCD Sum Rules ??

QCD Sum Rules

tetraquark meson T

4-quark interpolating operator $\mathcal{T}(x)$ with $\langle T | \mathcal{T}(x) | \emptyset \rangle \neq 0$

Operator Product Expansion: $\mathcal{T}^\dagger(x)\mathcal{T}(y) = \sum_n C_n(x-y) \mathcal{O}_n((x+y)/2)$

vacuum expectation value, insert complete set of states, Fourier transform

$$\sum_X \langle \emptyset | \mathcal{T} | X \rangle \langle X | \mathcal{T}^\dagger | \emptyset \rangle = \sum_n C_n \langle \emptyset | \mathcal{O}_n | \emptyset \rangle$$

Borel transform to suppress higher energy states

assume sum over X is dominated by tetraquark state T

Lucha, Melnikov & Sazdijan arXiv:1706.06003, 1710.08316,
1810.09986, 1901.03881

Fierz transformations \Rightarrow there are meson-meson states $M_1 M_2$ with

$$\langle M_1 M_2 | \mathcal{T}(x) | \emptyset \rangle \neq 0$$

sum over X is actually dominated by meson-meson states!

fatal problem ??

for all previous applications of QCD sum rules to tetraquarks

Lattice QCD

discretize QCD on a Euclidean spacetime lattice

- lattice spacing in time direction: a_t
- lattice spacing in spatial directions: a_s

calculate cross-correlators of many operators

$$\langle \mathcal{O}_i(t) \mathcal{O}_j(0) \rangle \longrightarrow \sum_n \sqrt{Z_{in}} \sqrt{Z_{jn}} e^{-E_n t}$$

- determine discrete eigenenergies E_n
- overlap factors $\sqrt{Z_{in}}$ have information about structure

extrapolate to zero lattice spacing: $a_t \rightarrow 0, a_s \rightarrow 0$

chiral extrapolation to physical u, d quark masses:

$$m_\pi = 140 \text{ MeV}$$

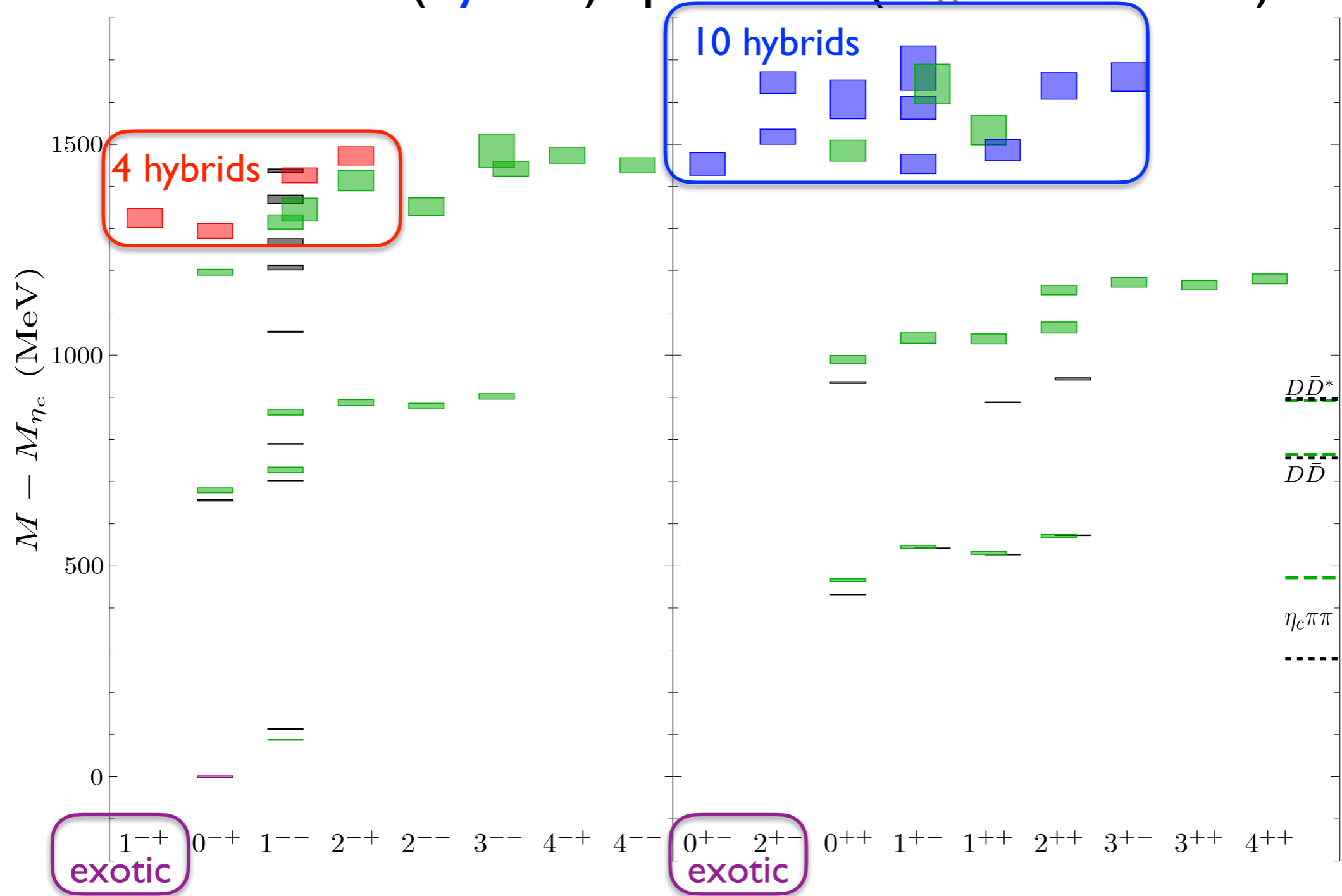
determine infinite-volume spectrum (masses, widths)
from discrete eigenenergies

Quarkonium (hybrid) Spectrum

Hadron Spectrum Collaboration

charmonium	$m_{\pi} = 391$ MeV	2012
charmonium	$m_{\pi} = 240$ MeV	2016
bottomonium	$m_{\pi} = 391$ MeV	2021

charmonium (hybrid) spectrum ($m_{\pi} = 240$ MeV)



Doubly Heavy Tetraquarks

$QQ\bar{q}\bar{q}$ tetraquark can have mass below strong decay threshold

Manohar & Wise (1997) stable in limit $M_Q \rightarrow \infty$

$bb\bar{q}\bar{q}$ ($q = u, d$) ground state: $l=0, J^P=1^+$ binding energy (MeV)

Bicudo, Scheunert & Wagner Born-Oppenheimer -59^{+30}_{-38}

Karliner & Rosner (2017) quark/diquark model $-215 (\pm 12 ?)$

Eichten & Quigg (2017) heavy quark expansion -122

BHM (2020)* $-133 \pm 25^*$

Leskovec et al. (2019) lattice QCD $-128 \pm 24 \pm 10$

* arXiv:2006.08650 (with He & Mohapatra)

error bars by taking all inputs from experiment or lattice QCD

See talk by Abhishek Mohapatra Thursday at 13:00

Doubly Heavy Tetraquarks

$bb\bar{s}\bar{q}$ ($q = u, d$): $I=1/2, J^P=1^+$

binding energy (MeV)

Eichten & Quigg (2017)

heavy quark expansion -49

BHM (2020)*

$-48 \pm 26^*$

$bc\bar{q}\bar{q}$ ($q = u, d$): $I=1/2, J^P=1^+$

Karliner & Rosner (2017)

quark/diquark model $-10 (\pm 12 ?)$

Eichten & Quigg (2017)

heavy quark expansion $+85$

BHM (2020)*

$+104 \pm 37^*$

$cc\bar{q}\bar{q}$ ($q = u, d$): $I=1/2, J^P=1^+$

Karliner & Rosner (2017)

quark/diquark model $+7 (\pm 12 ?)$

Eichten & Quigg (2017)

heavy quark expansion $+93$

BHM (2020)*

$+62 \pm 11^*$

* arXiv:2006.08650 (with He & Mohapatra)

Effective Field Theories for QCD

QCD: each quark flavor is Dirac spinor field: $\psi^i(x), i=1,2,3$

integrate out scale of heavy quark mass M

Nonrelativistic QCD (NRQCD)

heavy quark/antiquark is two Pauli spinor fields $\psi^i(\vec{r}, t), \chi^i(\vec{r}, t), i=1,2,3$

integrate out momentum scale Mv

Potential NRQCD (pNRQCD)

(for heavy-quark pair near lowest adiabatic potential)

heavy quark/antiquark pair is color-singlet field $S(R, r, t)$

color-octet field $O^a(R, r, t), i=1,2,\dots,8$

Pineda & Soto (1997), Brambilla, Pineda, Soto & Vairo (1999), Kniehl & Penin (1999)

Born-Oppenheimer EFT (BOEFT)

(for heavy-quark pair near other Born-Oppenheimer potentials)

Berwein, Brambilla, Tarrus Castella & Vairo arXiv:1510.04299

Brambilla, Krein, Tarrus Castella & Vairo arXiv:1707.09647

Soto & Tarrus Castella (2020)

¹⁶ arXiv:2005.00552

Born-Oppenheimer Approximation for Quarkonium Hybrids

pioneered by Juge, Kuti, Morningstar 1999

- heavy quark mass $\gg \Lambda_{\text{QCD}}$
- Q and \bar{Q} move nonrelativistically
- gluons respond almost instantaneously to the motion of the Q and \bar{Q}

B-O approximation: hybrids

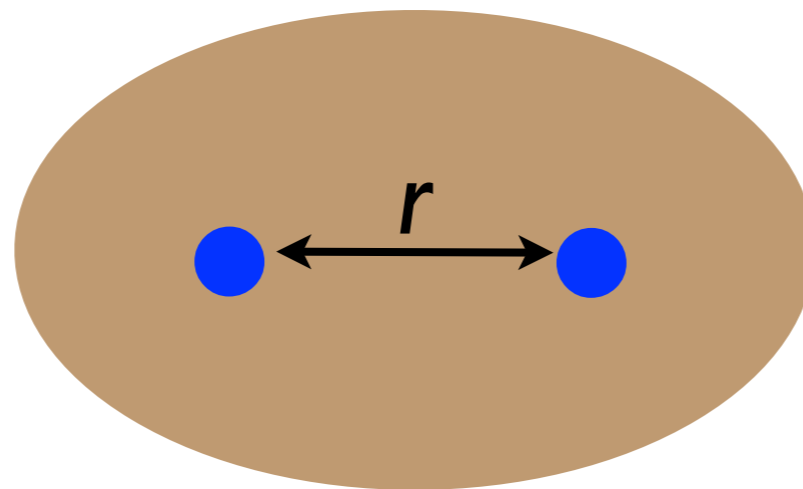
- given the positions of the Q and \bar{Q} , the **gluon** fields are in a **stationary state** in the presence of static Q and \bar{Q} sources



- as the positions of the Q and \bar{Q} change, the **gluon** fields remain adiabatically in that **stationary state**

B-O approximation: hybrids

- energy of stationary state of gluon fields in presence of static Q and \bar{Q} sources separated by distance r defines Born-Oppenheimer potential $V(r)$

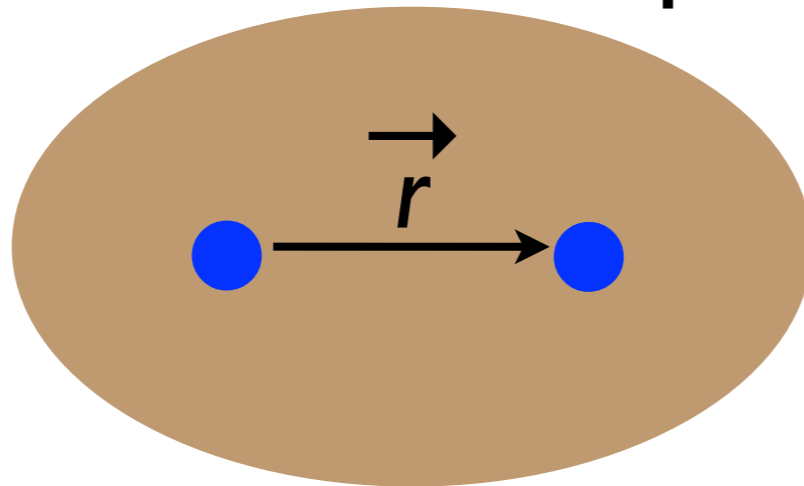


- Born-Oppenheimer approximation: motion of Q and \bar{Q} is described by Schroedinger equation in potential $V(r)$

B-O approximation: hybrids

stationary states for gluon fields

in presence of static Q and \bar{Q} sources
separated by vector \vec{r}



conserved quantum numbers: $\Lambda_{\eta}^{\varepsilon}$

- absolute value of component of angular momentum

$$|\hat{r} \cdot \vec{J}_{\text{light}}| \equiv \Lambda = 0, 1, 2, \dots \quad (\text{or } \Sigma, \Pi, \Delta, \dots)$$

- product of charge conjugation and parity

$$(CP)_{\text{light}} \equiv \eta = +1, -1 \quad (\text{or } g, u)$$

- reflection through plane containing sources

$$R_{\text{light}} \equiv \varepsilon = +1, -1 \quad (\text{or } +, -)_{20}$$

B-O approximation: hybrids

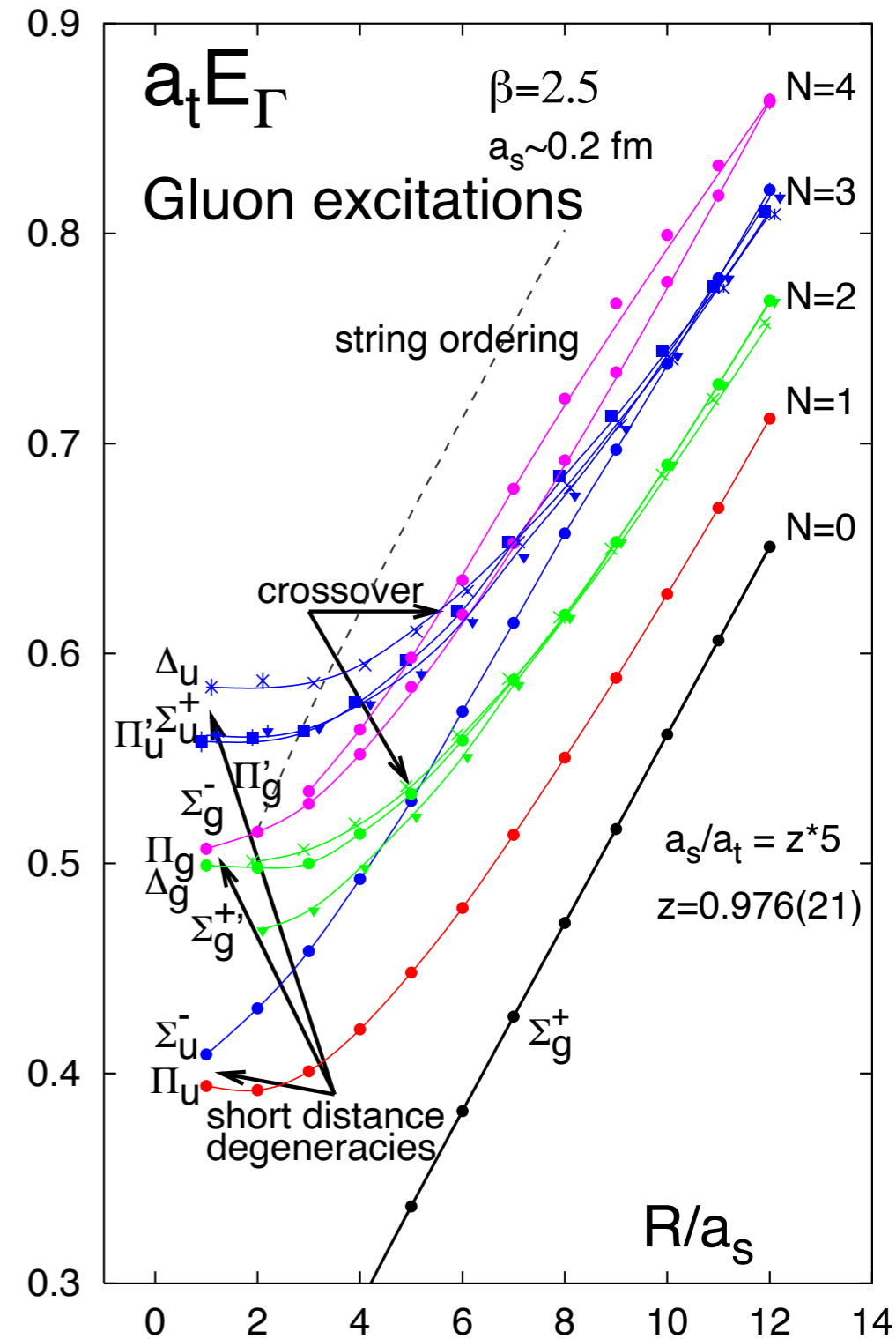
Born-Oppenheimer potentials

labelled by $\Lambda_{\eta}^{\epsilon} = \Sigma_g^+, \Pi_u^{\pm}, \Sigma_u^-, \dots$

calculate using lattice QCD

Juge, Kuti, Morningstar 1999

- anisotropic lattice: $10^3 \times 30$
- lattice spacing: $a = 0.2 \text{ fm}$
- quenched: no virtual quark-antiquark pairs!



B-O approximation: hybrids

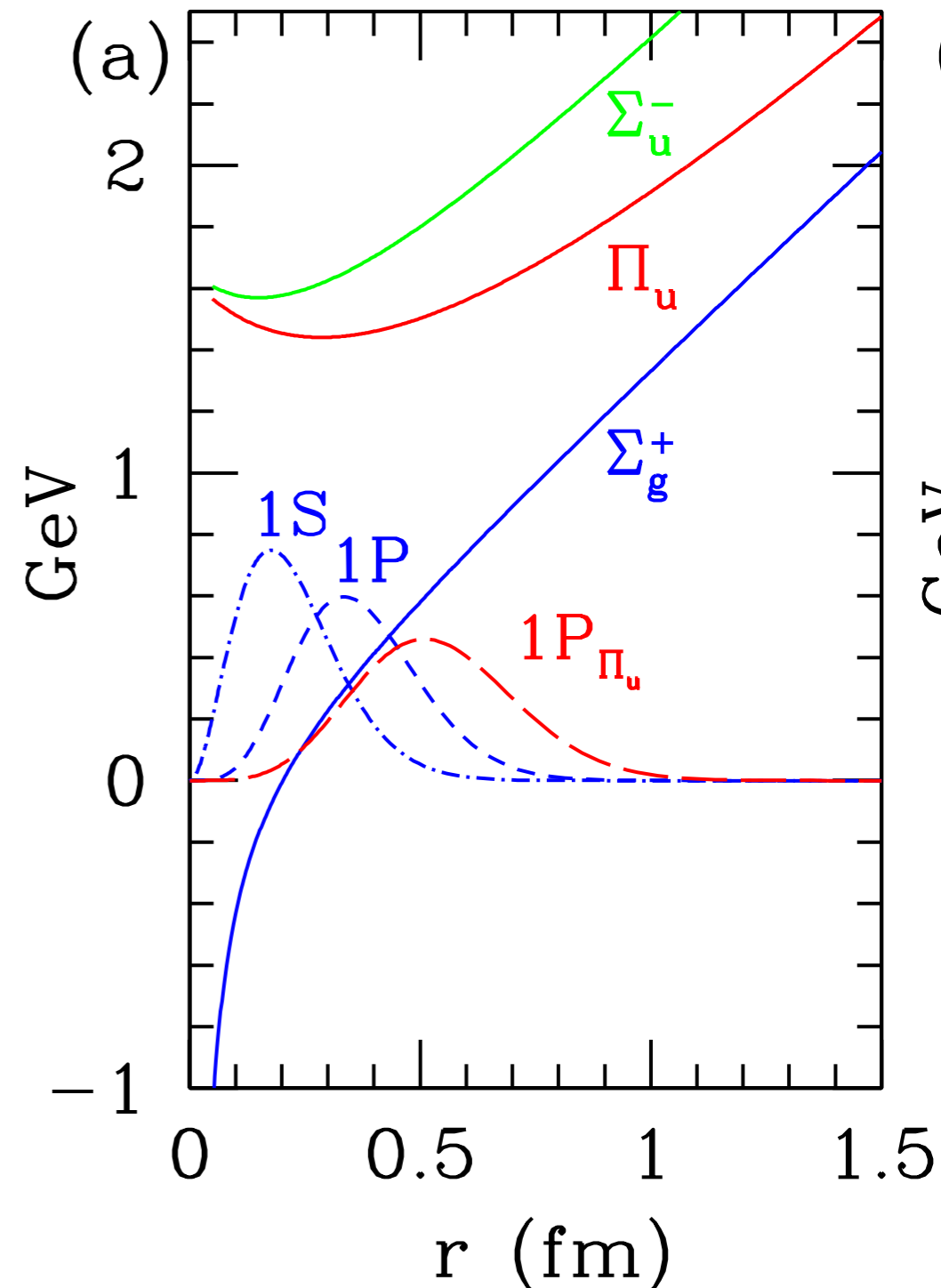
solve Schroedinger equation in Born-Oppenheimer potentials
Juge, Kuti, Morningstar 1999

energy levels labelled by nL
radial quantum number: $n = 1, 2, 3, \dots$
orbital angular momentum: $L \geq \Lambda$
 $L = 0, 1, 2, \dots$ or S, P, D, \dots

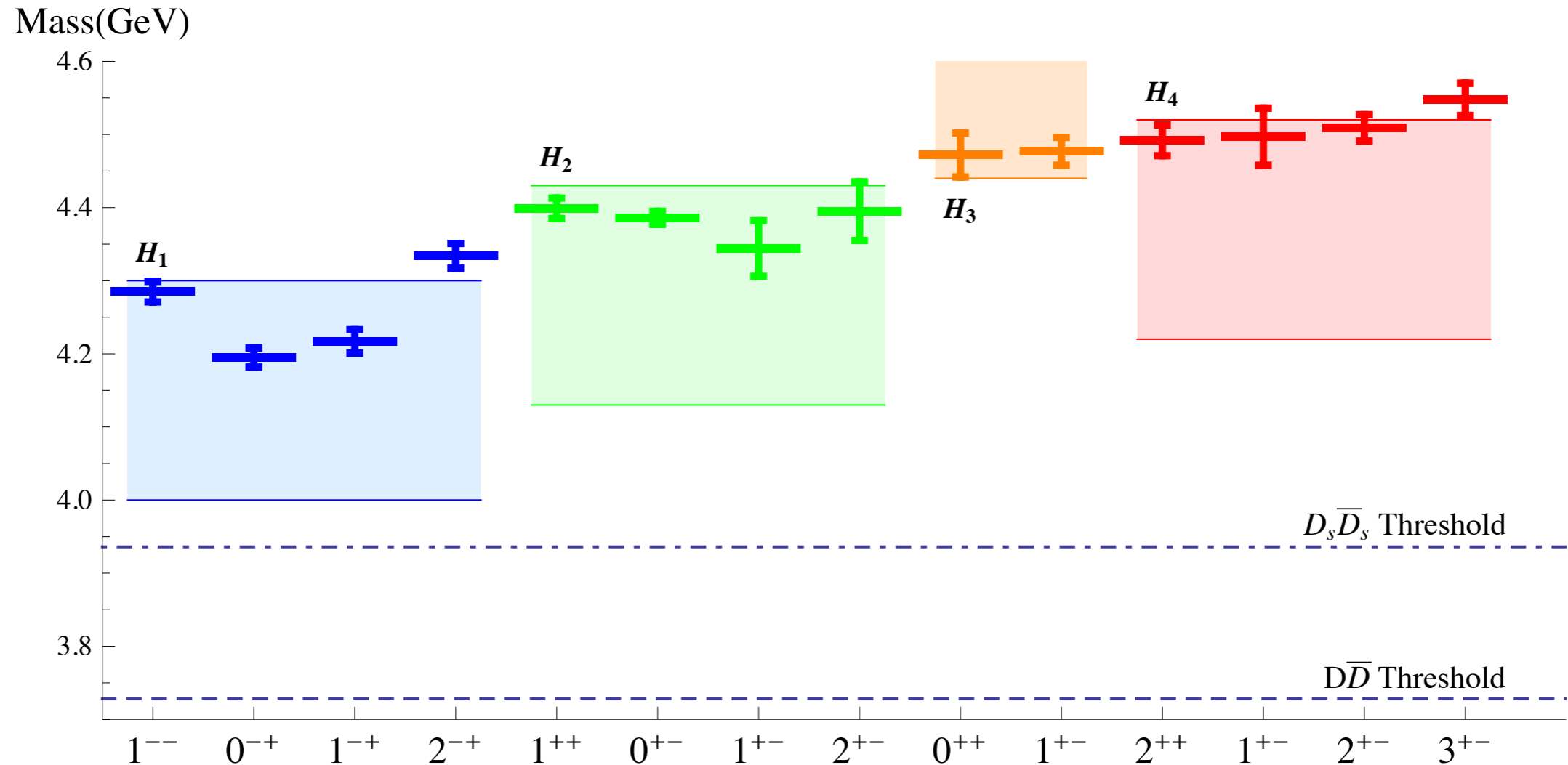
energy levels in Σ_g^+ potential:
quarkonium

energy levels in $\Pi_u^\pm, \Sigma_u^-, \dots$ potentials:
quarkonium hybrids

energy splittings: semiquantitative
agreement with lattice NRQCD



Charmonium Hybrids



BOEFT

error bands from lattice QCD calculation of gluelump mass

Berwein, Brambilla, Tarrus Castella & Vairo arXiv:1510.04299

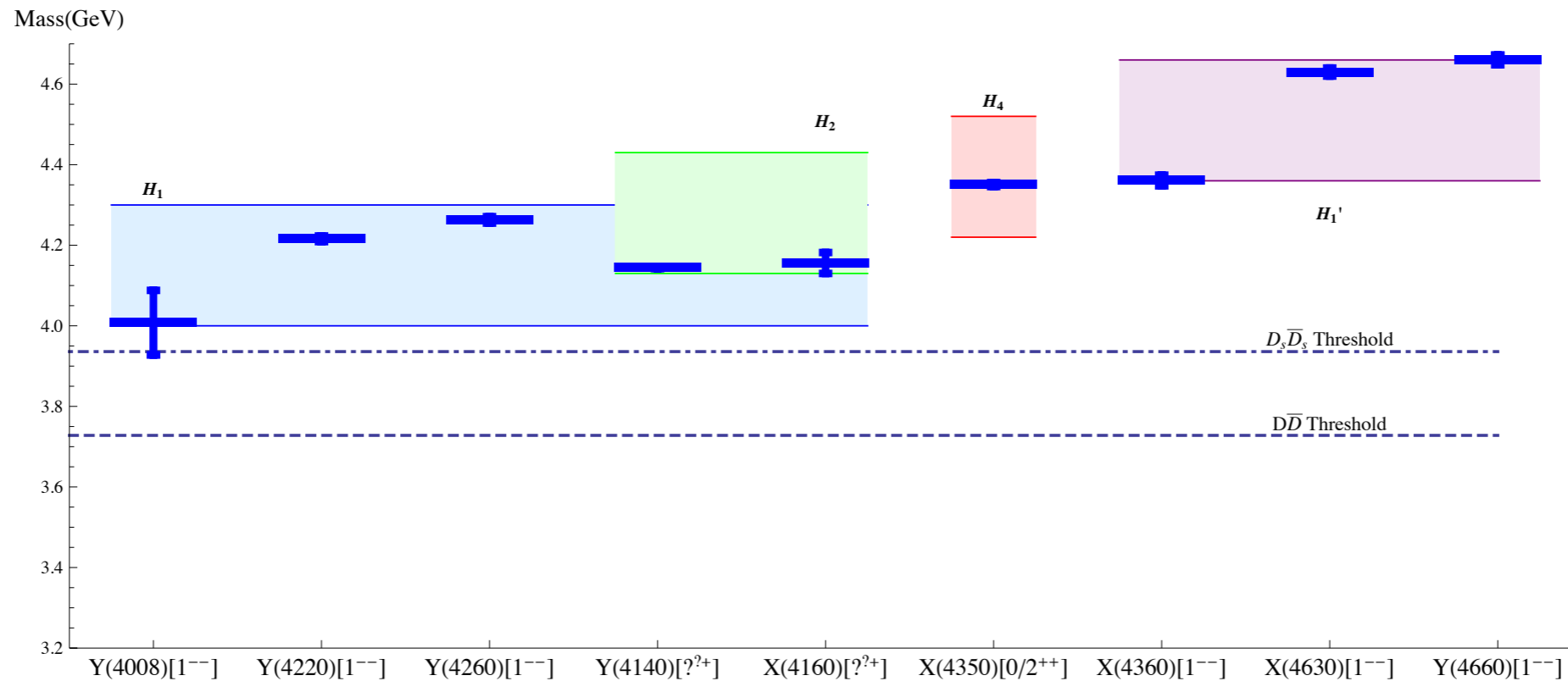
Lattice QCD

points with error bars for $m_\pi = 400$ MeV

Hadron Spectrum collaboration arXiv:1204.5425

Charmonium Hybrids

possible identifications with X and Y mesons



BOEFT error bands

Berwein, Brambilla, Tarrus Castella & Vairo [arXiv:1510.04299](https://arxiv.org/abs/1510.04299)

Lattice QCD data points

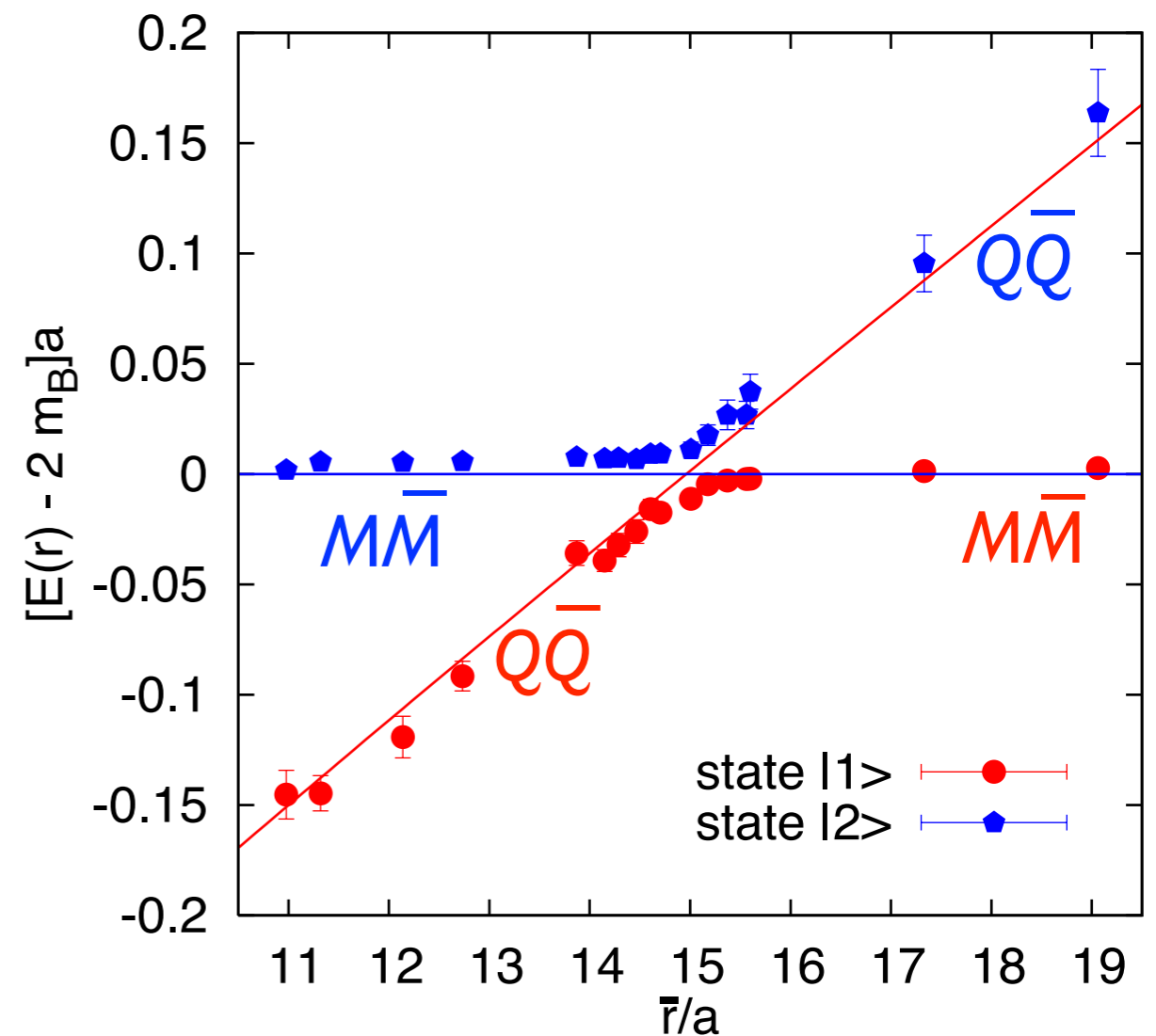
Hadron Spectrum collaboration [arXiv:1204.5425](https://arxiv.org/abs/1204.5425)

Born-Oppenheimer potentials

B-O potentials

- include **potentials** that approach **meson-pair thresholds** at large r
- have avoided crossings
- both can be calculated using **lattice QCD**

$Q\bar{Q}$ (Σ_g^+) and $M\bar{M}$ potentials
SESAM hep-lat/0505012



Quarkonium Tetraquarks

XYZ mesons with positive electric charge have constituents $Q\bar{Q}u\bar{d}$

first discoveries

$c\bar{c}$ tetraquarks: $Z^+(4430)$

Belle (2007)

$b\bar{b}$ tetraquarks: $Z_b^+(10610)$, $Z_b^+(10650)$

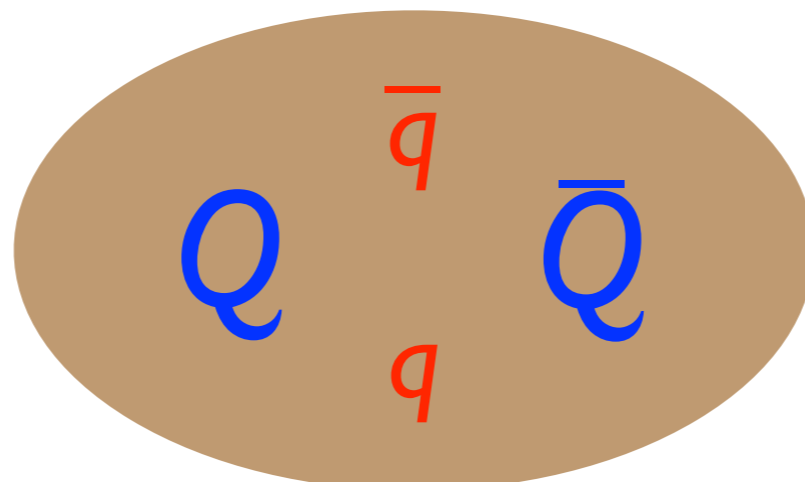
Belle (2011)

$c\bar{c}$ tetraquarks: $Z_c^+(3900)$, ...

BESIII (2013)

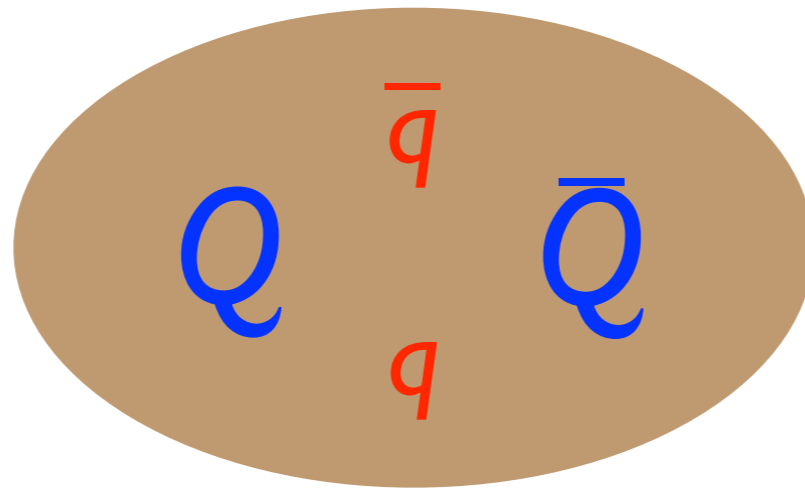
Q. How can **charged quarkonium tetraquarks** be reconciled with **Born-Oppenheimer approximation** for **QCD**?

A. Light **QCD** fields in the presence of static $Q\bar{Q}$ sources can have **light-quark flavors $q\bar{q}$** ! *Braaten arXiv:1305.6905*



B-O approximation: **tetraquarks**

Light quarks can respond almost instantaneously
to the motion of the **heavy quarks**,
just like **gluon fields**

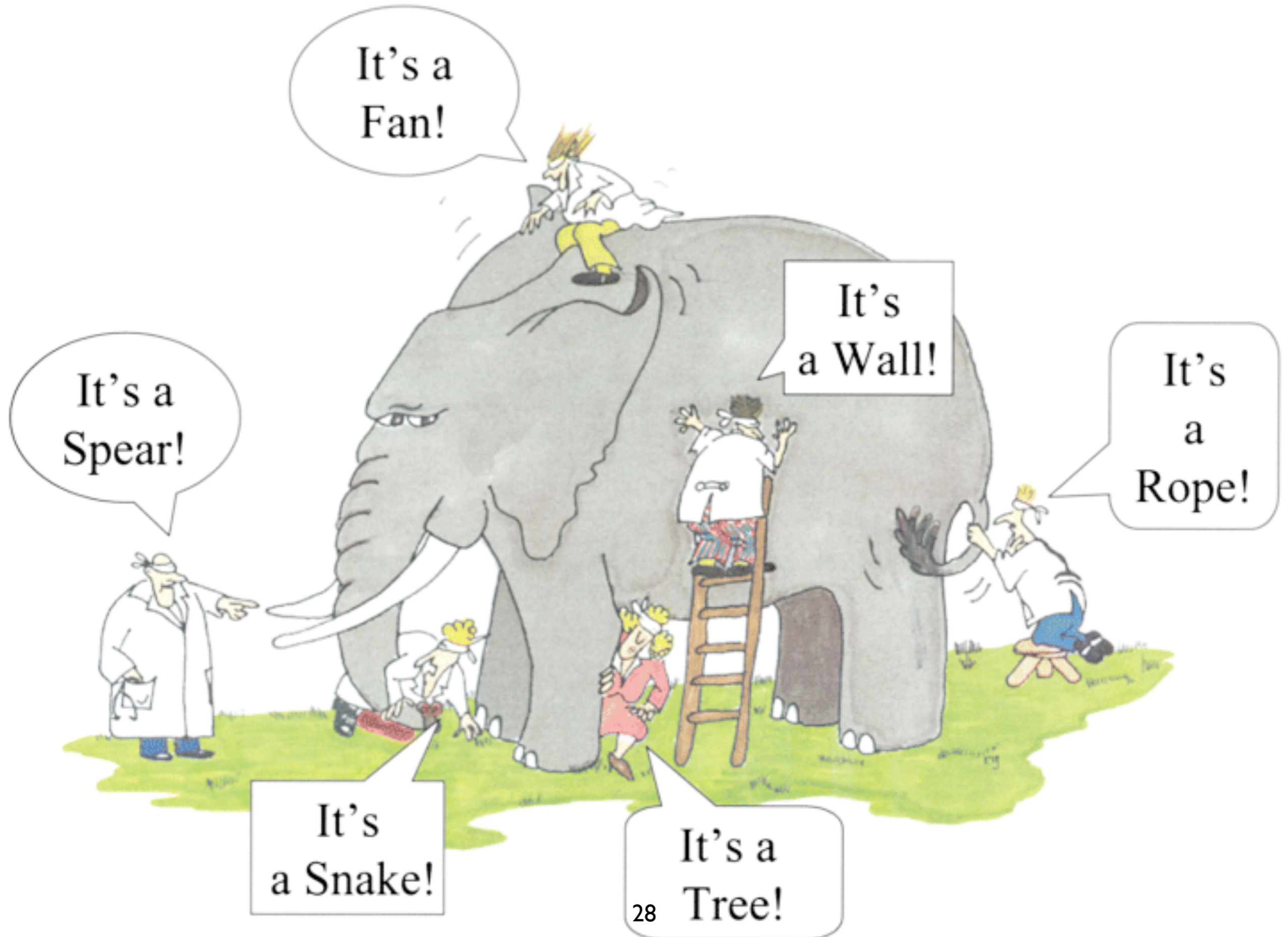


Quarkonium Tetraquarks

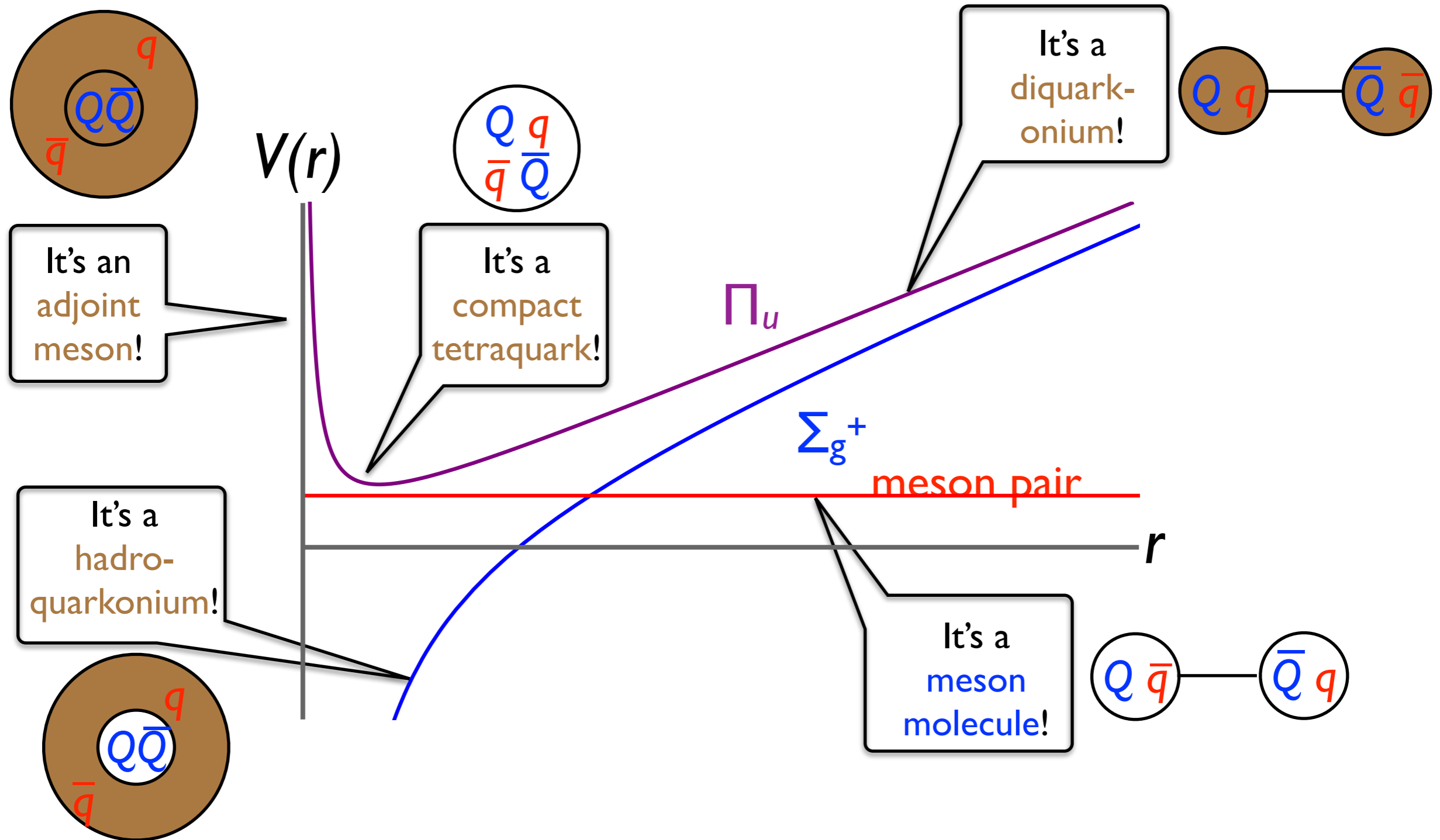
can be treated using the **Born-Oppenheimer** approximation
just like **Quarkonium Hybrids**
except that the **stationary state** of gluons and light quarks
has B-O quantum numbers $\Lambda_{\eta}^{\epsilon}$
and also light-quark flavors

Braaten arXiv:1305.6905

What is an **XYZ** Meson?



What is an XYZ Meson?



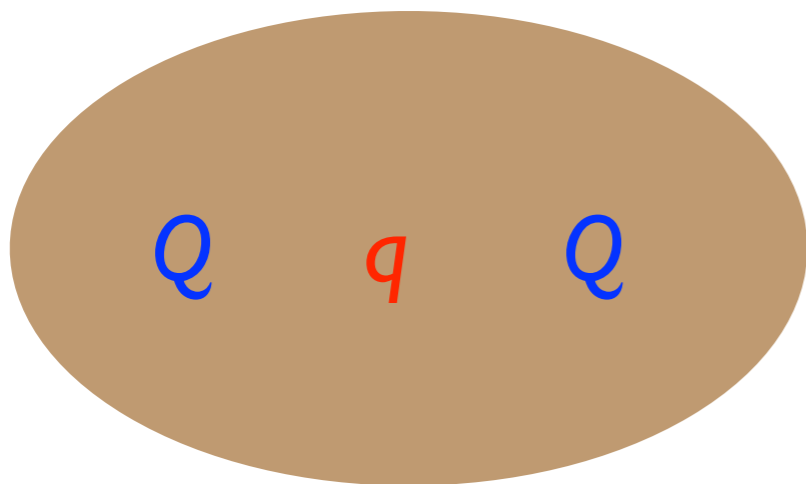
Each model describes some region of the **Born-Oppenheimer** wavefunction

Doubly Heavy Hadrons

Born-Oppenheimer approximation

Light **QCD** fields in the presence of static $Q Q$ sources
can have **light-quark flavor** q or $\bar{q} \bar{q}$!

doubly heavy baryon



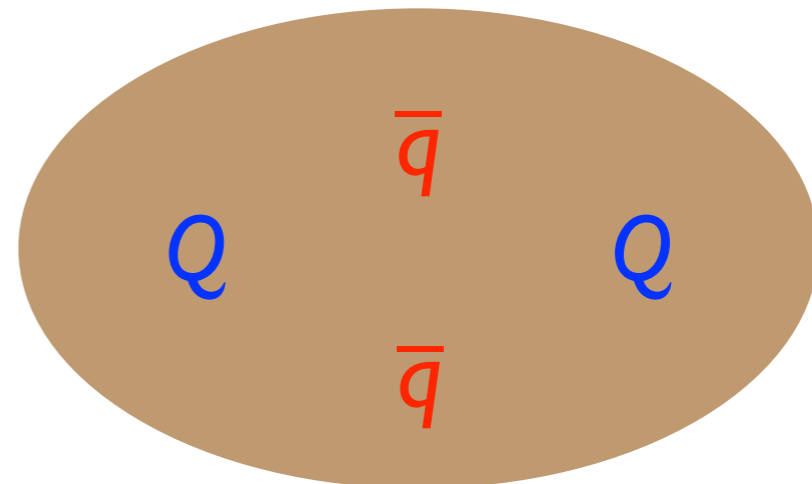
Maiani, Polosa & Riquer

arXiv:1903.10253

Soto & Tarrus Castella

arXiv:2005.00551

doubly heavy tetraquark



Bicudo & Wagner

arXiv:1209.6724

Maiani, Polosa & Riquer

arXiv:1903.10253

Diabatic Representation

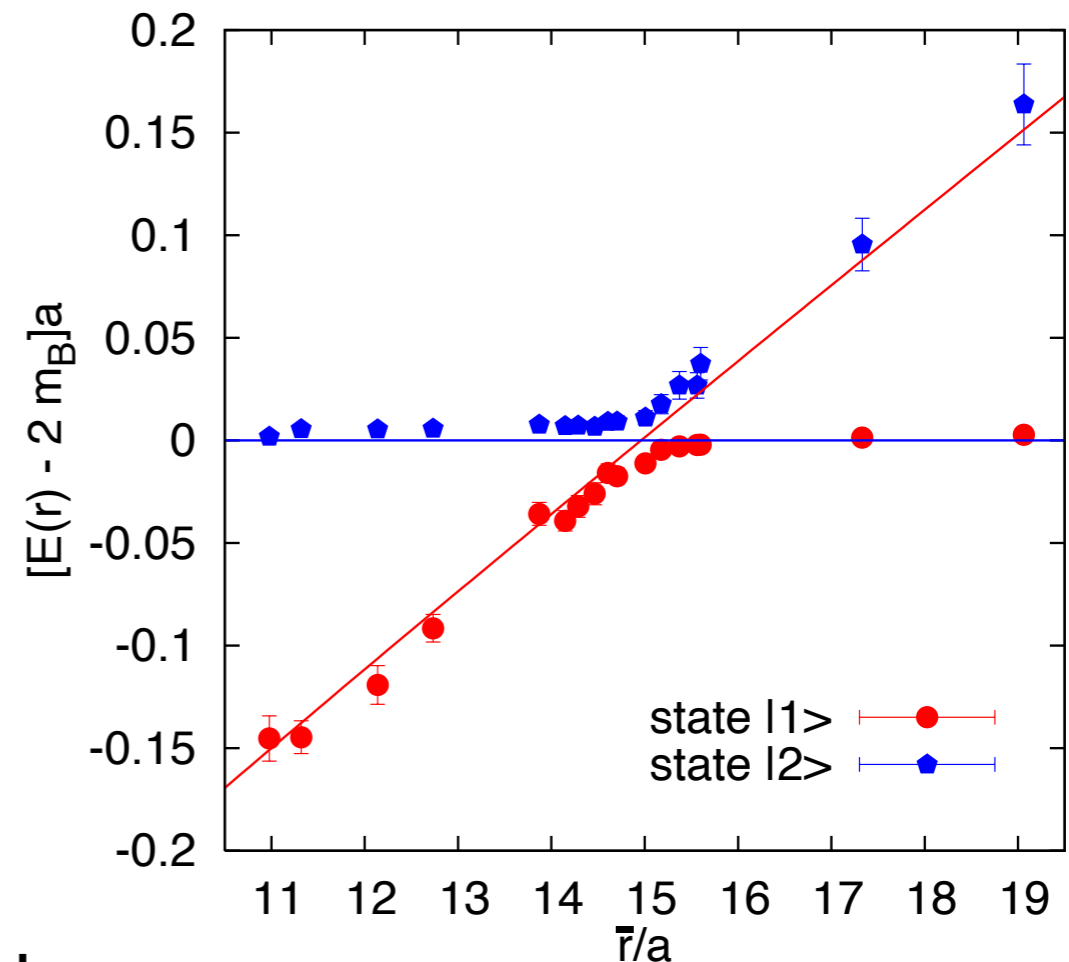
Bruschini & Gonzales arXiv:2007.07693, 2101.04636, 2105.04401

Adiabatic representation

- heavy particles interact through Born-Oppenheimer potentials with avoided crossings

Diabatic representation

- heavy particles interact through Born-Oppenheimer potentials that cross
- can be obtained by a unitary transformation
- allows more accurate treatment of scattering states



may be essential for **XYZ hadrons** near hadron-pair thresholds

Dynamical Diquark Model

Lebed

arXiv:1709.06097

Giron et al.

arXiv:1903.04551, 1907.08546

Giron & Lebed

arXiv:2005.07100

Gens et al.

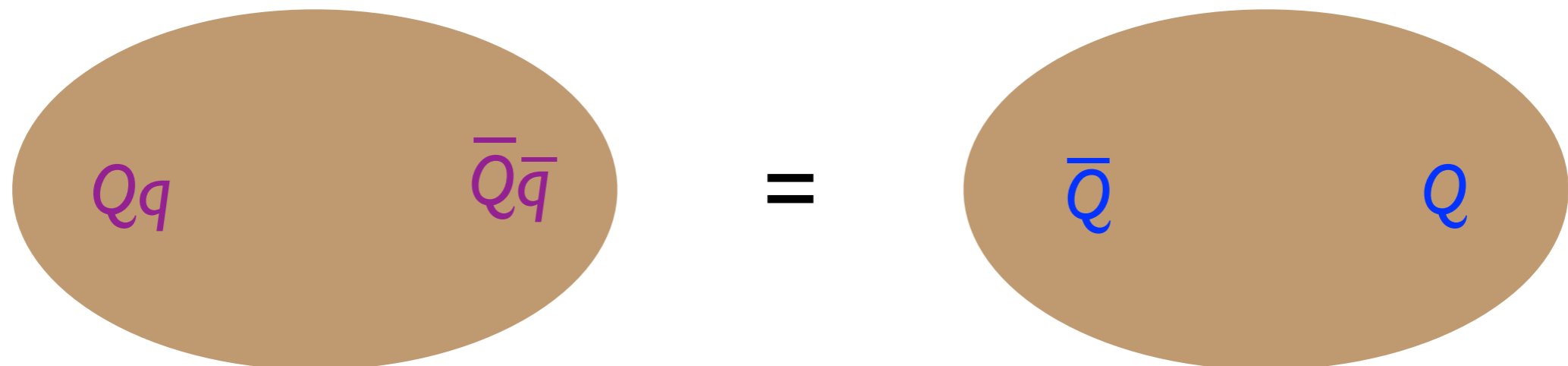
arXiv:2102.1259

Model for Quarkonium Tetraquarks:

diquark Qq and anti-diquark $\bar{Q}\bar{q}$ are assumed to interact

through same B-O potentials Σ_g^+ , Π_u^\pm , Σ_u^- , ...

as \bar{Q} and Q in quarkonium and quarkonium hybrid

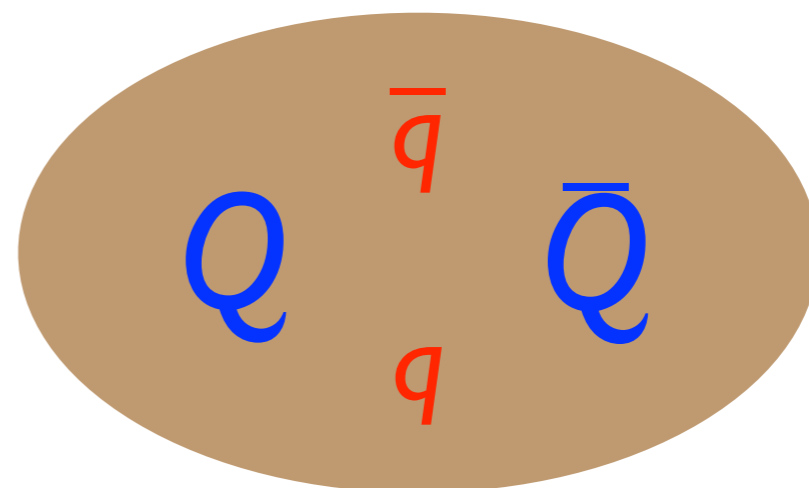
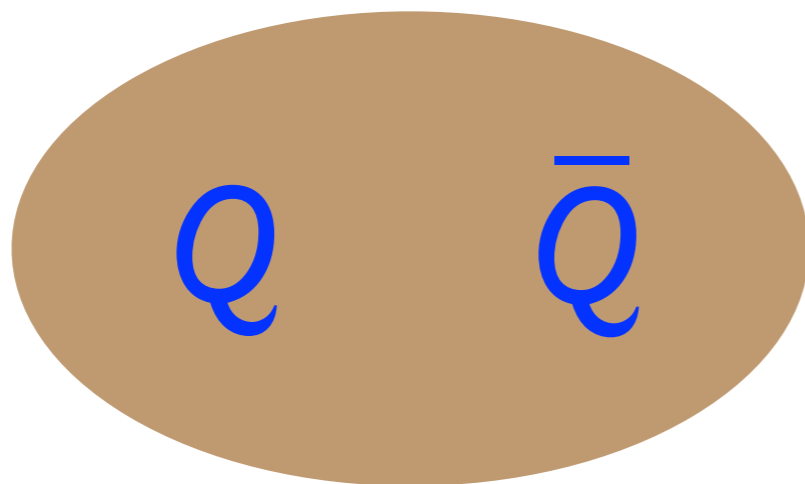


Conclusions

The discoveries of **Exotic Heavy (XYZ) Hadrons** have revealed a serious gap in our understanding of the **QCD** spectrum

Constituent models for the **XYZ mesons** have not provided a compelling pattern and make little contact with **QCD**

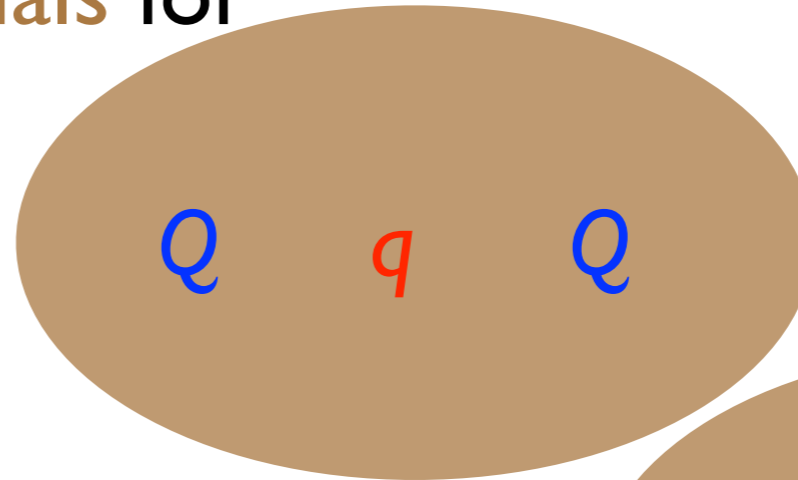
Born-Oppenheimer Effective Field Theory has not yet provided a compelling pattern for the **XYZ hadrons** but it is based firmly on **QCD**



What is needed from Lattice QCD

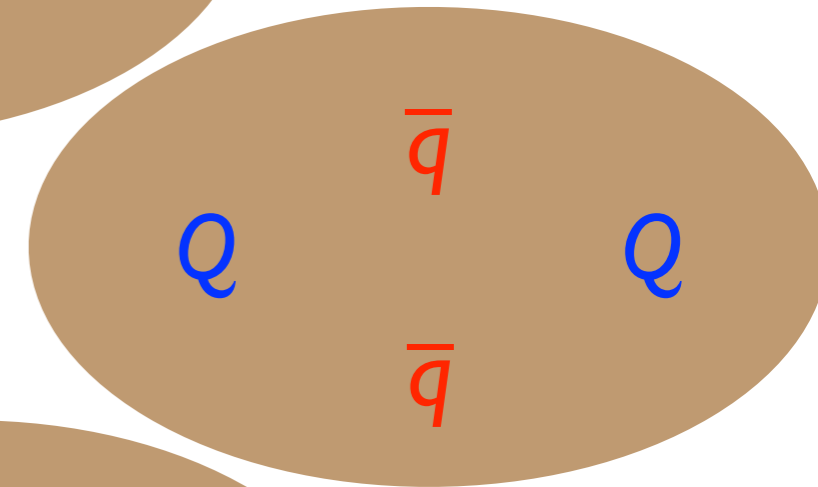
- Born-Oppenheimer potentials for

doubly heavy baryons



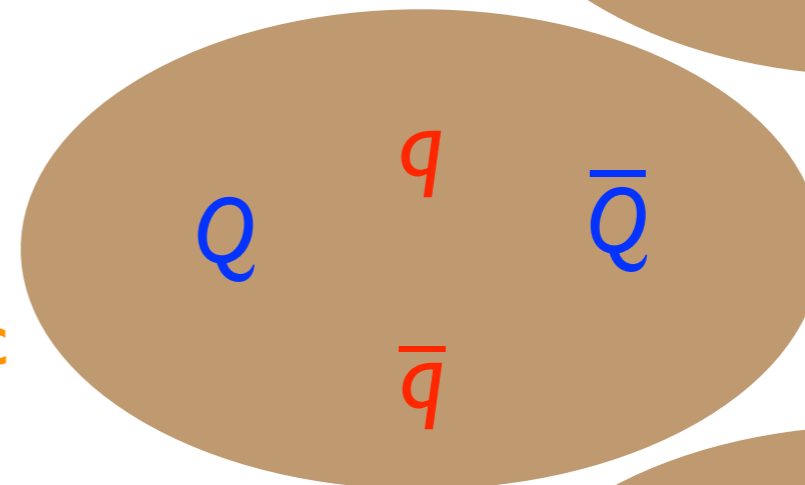
doubly heavy tetraquarks

Bicudo, Wagner et al.

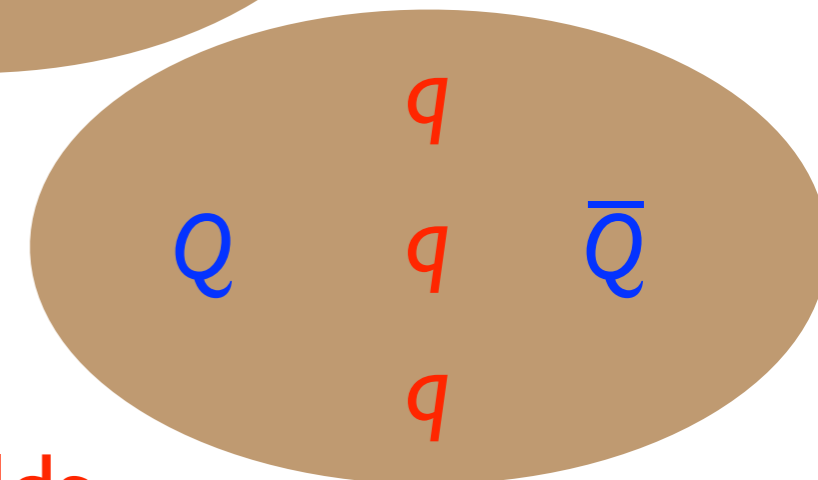


quarkonium tetraquarks

Prelovsek, Bahtiyar & Petkovic



quarkonium pentaquarks



- avoided crossings with meson-pair thresholds

Future experiments on the *XYZ* hadrons

- e^+e^- experiments
 - BESIII
 - Belle II
- LHC experiments
 - ATLAS and CMS
 - LHCb
- PANDA: $p\bar{p}$ annihilation at resonance into charmonium (and hybrids and tetraquarks)

What is needed from experiment

- more J^{PC} 's
- more transitions (hadronic and radiative)
- more *XYZ* hadrons ³⁵

Conclusions

What is needed from non-lattice **theory**

use **Born-Oppenheimer EFT** to calculate

- spectrum of **doubly heavy baryons**
doubly heavy tetraquarks
quarkonium hybrids
quarkonium tetraquarks
quarkonium pentaquarks
- radiative and hadronic transitions to **quarkonium**

there is hope for a

“coherent comprehensive understanding of the **XYZ particles**”
that is based firmly on **QCD**