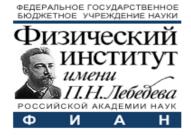
ATLAS measurements of CP Violation and Rare decays processes with Beauty mesons







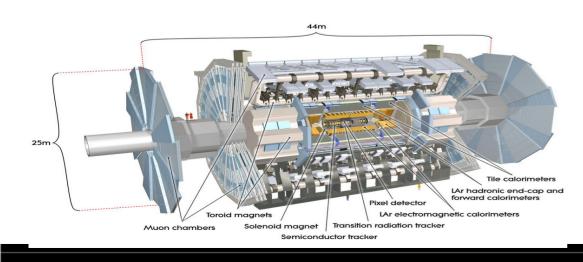
Oleg Meshkov (MSU & Lebedev PI)

10th International Workshop on Charm Physics (Charm 2020)

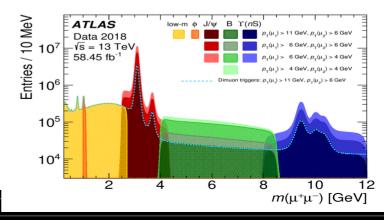
On behalf of the ATLAS Collaboration

### **B-physics at ATLAS**

- ATLAS Run 2: 139 fb<sup>-1</sup> of pp collisions at  $\sqrt{s}$  = 13 TeV collected in 2015-2018
- Producing ~2.5 million  $b\overline{b}$  pairs/second,  $B_s$ ,  $B_c$ ,  $\Lambda_b$ , etc. available
- Program focused mostly on muonic final states, fully reconstructable
- Typical trigger: low- $p_T$  di-muons at low invariant mass, using information from inner tracker(pT > 0.4 GeV,  $|\eta| < 2.5$ ) and muon detectors(triggering ( $|\eta| < 2.4$ ), precision tracking ( $|\eta| < 2.7$ )).
- In Run2: Insertable B-Layer (IBL) resolution in b-hadron proper decay time was  $\sim$ 70 fs
- B-physics trigger rate up to ~ 200 Hz



ATLAS Run-1 analysis: CP-violation:JHEP 08 (2016) 147 Rare decays: Eur. Phys. J. C 76 (2016) 513



### Latest results on rare decays and CP-violation

- Measurement of CP-violating phase  $\phi_s$  (and other parameters) in the  $B_s \to J/\psi \varphi$  decay using 2015-2017 data (80.5 fb^-1)
  - Eur. Phys. J. C 81 (2021) 342
- Measurement of the branching ratio of  $B_s \rightarrow \mu\mu$  decays using 2015-2016 data (26.3 fb<sup>-1</sup>), combination with CMS and LHCb (ATLAS-CONF-2020-049)
  - JHEP 04 (2019) 098

## Measurement of the CP-violating phase $\phi_s$ in $B_s \rightarrow J/\psi\phi$ decays in ATLAS at 13 TeV

## CP violation in $B_s \rightarrow J/\psi\phi$

• Interference of direct decay and decay with mixing into the same final state of  $B_s \rightarrow J/\psi \phi$  decay gives rise to time-dependent CP violation (CPV)



- CPV phase  $\phi_s$  is weak phase difference between the  $B_s \overline{B}_s$  mixing amplitude and the b  $\rightarrow c\overline{c}s$  decay amplitude
- In the SM the phase  $\varphi_s$  is small and is related to CKM quark matrix:  $\varphi_s \equiv -2\beta_s = -2\arg(\frac{-V_{ts}V_{*_{cb}}}{V_{cs}V_{*_{cb}}}) = -0.03696 \frac{+0.00072}{-0.00082} rad$  Phys. Rev. D 91 (2015) 073007
- New Physics (NP) processes could contribute to the mixing box diagrams, potentially allowing for large deviations in  $\phi_s$  from the SM prediction
- Alongside  $\phi_s$ , other quantities are describing the differential decay rate:
  - Decay widths of the two mass eigenstates
  - CP even/odd state amplitudes and phases

## **Data Analysis**

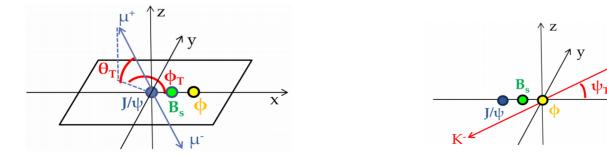
#### Data:

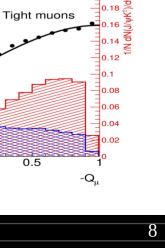
#### Eur. Phys. J. C 81 (2021) 342

- Using 80.5 fb<sup>-1</sup> of pp 2015-17 data, 13 TeV
- Statistically combined with Run1 ATLAS results:
  - 4.9 fb<sup>-1</sup> (7 TeV, pp 2011)
  - 14.3 fb<sup>-1</sup>(8 TeV, pp 2012) statistically combined with 7 TeV
- Collected by triggers based on identification of J/ $\psi$  with pT( $\mu$ ) threshold (mainly 4 and 6 GeV)
  - Including MC samples for  $B_s \to J/\psi \varphi$  and dedicated backgrounds  $B_d \to J/\psi K^*, B_d \to J/\psi K\pi$  and  $\Lambda_b \to J/\psi pK$
- No lifetime cut signal-background separation done by the fit

## Angular analysis Eur. Phys. J. C 81 (2021) 342

- $B_s \rightarrow J/\psi \phi$  decay=decay of pseudoscalar to vector-vector
- Final state: admixture of CP-odd (L = 1) and CP-even (L = 0, 2) states
- Distinguishable through time-dependent angular analysis
- Non-resonant S-wave decay  $B_s \to J/\psi KK$  contribute to the final state and is included in the differential decay rate due to interference with the  $B_s \to J/\psi(\mu\mu)\phi(KK)$  decay
- The transversity angles,  $\Omega = (\Theta_T, \Psi_T, \phi_T)$  are defined as below



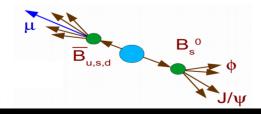


## **Opposite-side flavour tagging**

- Use b- $\overline{b}$  correlation => initial B<sub>s</sub> flavour
  - $b \rightarrow I$  transitions clean tagging method
  - diluted by oscillations and b  $\rightarrow$  c  $\rightarrow$  l ٠
- Provides probability P(B|Q) of signal candidate to be  $B_s$  or  $\overline{B}_s$
- Tagger types: tight muon, low- $p_{\tau}$  muon, electron, b-tagged jet
- Key variables: charge of  $p_{\tau}$ -weighted tracks in cone  $\Delta R$  around the leptons, b-jets  $\nabla N$  tracks  $\sigma$   $(p_{-})^{\kappa}$ P(B|Q

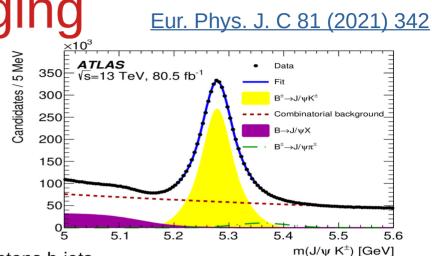
$$Q_x = \frac{\sum_i \quad q_i \cdot (p_{\mathrm{T}i})}{\sum_i^{N \, \mathrm{tracks}} (p_{\mathrm{T}i})^{\kappa}}$$

- 0.7 Search order based on best purity: tight muons, electrons, low- $p_{T}$  muons, b-jets  $_{0.6}$
- Calibrated on self-tagged  $B^{\pm} \rightarrow J/\psi K^{\pm}$  data



$\mathcal{D}(Q_x) = 2P(B Q_x) - $	- 1
$T_x = \sum_i \epsilon_{xi} \cdot (2P(B_i))$	$ Q_{xi})-1\rangle^2$

Tag method	$\epsilon_x$ [%]	$D_x$ [%]	$T_x$ [%]				
Tight muon	$4.50 \pm 0.01$	$43.8 \pm 0.2$	$0.862 \pm 0.009$				
Electron	$1.57 \pm 0.01$	$41.8 \pm 0.2$	$0.274 \pm 0.004$				
Low- $p_{\rm T}$ muon	$3.12 \pm 0.01$	$29.9 \pm 0.2$	$0.278 \pm 0.006$				
Jet	$12.04 \pm 0.02$	$16.6 \pm 0.1$	$0.334 \pm 0.006$				
Total	$21.23 \pm 0.03$	$28.7 \pm 0.1$	$1.75 \pm 0.01$				



s=13 TeV, 80.5 fb<sup>-1</sup>

B<sup>−</sup>→J/ψK<sup>−</sup>

Data

 $\leq$ 

B<sup>+</sup>→J/ψK<sup>+</sup>

-0.5

0

0.5

0.9

0.8

0.5

0.4

0.3

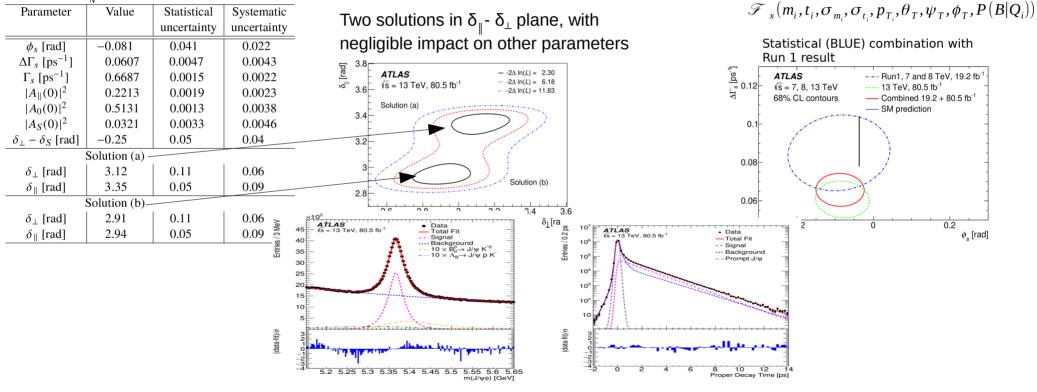
0.2

## UML fit and Results

Eur. Phys. J. C 81 (2021) 342

• An unbinned maximum likelihood (UML) fit performed for B<sub>s</sub> mass, decay time and the decay angles:

 $ln\mathscr{L} = \sum_{N}^{i-1} w_i * \ln(f_s \mathscr{F}_s + f_s f_{(B^0)} \mathscr{F}_{(B^0)} + f_s f_{(\Lambda_b)} \mathscr{F}_{(\Lambda_b)} + (1 - f_s (1 + f_{(B^0)} + f_{(\Lambda_b)})) \mathscr{F}_{bkg})$ 



Observables:

## Comparison with other experiments

ATLAS result:

 $\phi_s$ =-0.087 ± 0.036 (stat.) ± 0.021 (syst.) rad  $\Delta\Gamma_s$ =0.0657 ± 0.0043 (stat.) ± 0.0037 (syst.) ps<sup>-1</sup>

[<sup>-</sup>sd] <sup>°</sup> 0.12 [<sup>1</sup>−sd]<sup>2</sup>]0.13 ATLAS HFLAV D0 8 fb<sup>-1</sup>  $\sqrt{s} = 7, 8, and 13 \text{ TeV}$ CMS,  $J/\psi K^+ K^-$ , 116.1 fb PDG 2021 68% CL contours 68% CL contours  $(\Delta \log \mathcal{L} = 1.15)$ 0.1 CMS 116.1 fb<sup>-1</sup> 0.11 -SM LHCb,  $J/\psi K^+ K^-$ , 4.9 fb<sup>-2</sup> CDF 9.6 fb<sup>-1</sup> LHCb, all channels, 4.9 fb<sup>-1</sup> 0.09 0.08 Combined<sup>\*</sup> LHCb 4.9 fb<sup>-1</sup>  $^{*}\Delta\Gamma_{s}$  errors scaled by 1.77 0.07 ATLAS 99.7 fb<sup>-</sup> 0.06 ATLAS,  $J/\psi K^+ K^-$ , 99.7 fb<sup>-1</sup> 0.05 -0.5 -0.3 -0.1 0.1 0.3 -0.20.2  $\phi_s^{c\bar{c}s}$ [rad]  $\phi_{c}$  [rad] World average: Heavy Flavour Averaging Group  $\phi_{\rm c}$ = -0.050 ± 0.019 rad (HFLAV 2021)  $\Delta\Gamma_{c}=0.082 \pm 0.005 \text{ ps}^{-1}$ 

Study of the rare decays of  $B_s$  and  $B_0$  mesons into muon pairs using data collected during 2015 and 2016 with the ATLAS detector

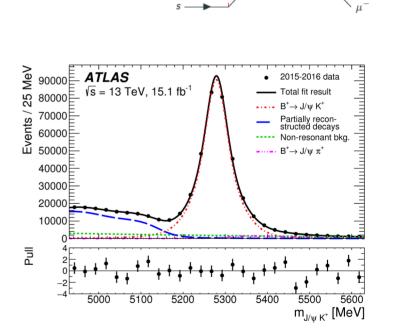
# Analysis of rare $B_{(s)} \rightarrow \mu\mu$ decays

- Flavour Changing Neutral Currents(FCNC) in the SM proceeding via loop and box diagrams, strongly suppressed (B ~10<sup>-9</sup>)
- Beyond SM can signicantly contribute, modifying the branching ratio

Mesurement(s):

$$B(B_s^0 \rightarrow \mu^+ \mu^-) = N_{d(s)} * \frac{B(B^{\pm} \rightarrow J/\psi K^{\pm}) * B(J/\psi \rightarrow \mu^+ \mu^-)}{N_{J/\psi K^{\pm}} * \frac{\varepsilon_{\mu^+ \mu^-}}{\varepsilon_{J/\psi K^{\pm}}}} * \frac{f_u}{f_{d(s)}}$$

- 36.2 fb<sup>-1</sup> dataset of 2015-2016 data taking:
  - effectively 26.3 fb<sup>-1</sup> for B  $\rightarrow \mu\mu$
- $B(B_{(s)} \rightarrow \mu\mu)$  mesurement(s) relative to  $B(B^{\pm} \rightarrow J/\psi K^{\pm})$ ,  $B_{s} \rightarrow J/\psi \phi$  as control channel
- Yields  $N_{d(s)}$  and  $N_{J/\psi K\pm}$  obtained from UML fits to the mass spectra
- Separate signal from background using boosted decision tree (BDT)
- Known branching ratios from PDG,  $f_u/f_{d(s)}$  from HFLAV



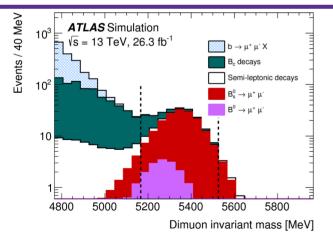
 $Z^0, H^0, h^0$ 

#### JHEP 04 (2019) 098

# Backgrounds

#### Partially reconstructed bhadron decays

- Mostly in the low di-muon mass region
- Shape parameters is free to be determined in the fit



#### **Peaking backgrounds:**

• Hadronic  $B_s$  decays

where hadrons are misidentified as muons

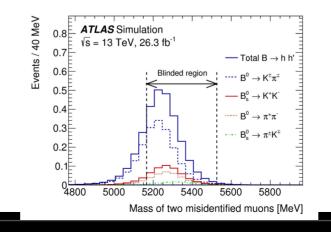
• Simulated and fixed in the mass fit

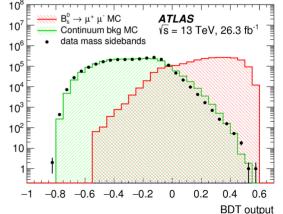
# Continuum backgrounds:

- Combinatorics of μ and uncorrelated hadron decays
- Reduced by BDT

Events / 0.05

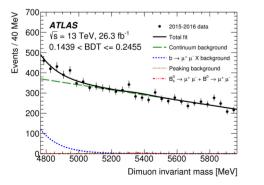
• Systematics due to  $B_c^{\pm} \rightarrow J/\psi\mu\nu$  and  $B_{(s)}/\Lambda_b \rightarrow h\mu\nu$  decays

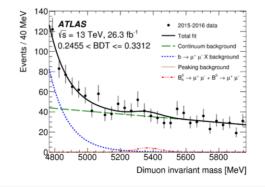


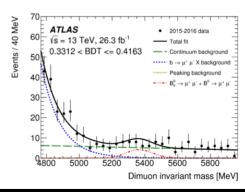


# **BDT** and signal extraction

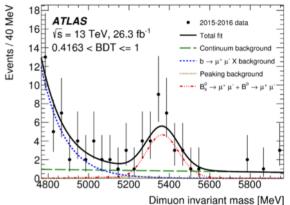
- BDT formed from 15 variables
  - Kinematics, isolation, B-vertex separation from PV
- BDT output validated on reference  $B^{\pm} \rightarrow J/\psi K^{\pm}$  and control  $B_s \rightarrow J/\psi \phi$  channels observed difference applied as the correction is on the efficiency ratio
- Signal region divided into four BDT bins with constant signal efficiency
- Simultaneous extraction of  $B_s \rightarrow \mu\mu$  and  $B_d \rightarrow \mu\mu$  yields from UML fit to di-muon mass distributions in the four BDT bins



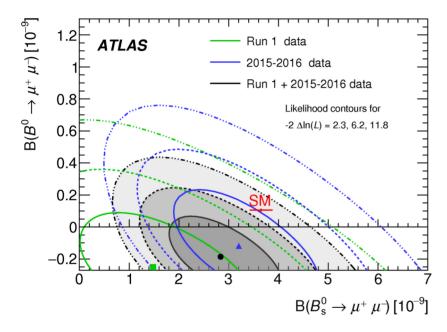




#### JHEP 04 (2019) 098



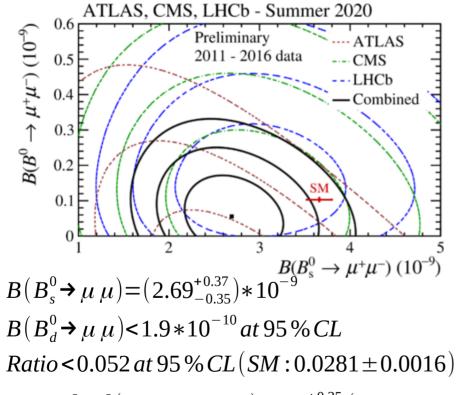
## Results



JHEP 04 (2019) 098 Standard model:  $B(B_s^0 \rightarrow \mu \mu) = (3.66 \pm 0.14) * 10^{-9}$ B(B\_d^0 \rightarrow \mu \mu) = (1.03 \pm 0.05) \* 10^{-9} arXiv:1908.07011 ATLAS 2015+2016 data:  $B(B_s^0 \rightarrow \mu \mu) = (3.2^{+1.1}_{-1.0}) * 10^{-9}$  $B(B_d^0 \rightarrow \mu \mu) < 4.3 * 10^{-10} at 95 \% CL$ ATLAS Run1+2015+2016 data:  $B(B_{c}^{0} \rightarrow \mu \mu) = (2.8_{-0.7}^{+0.8}) * 10^{-9}$  $B(B_d^0 \rightarrow \mu \mu) < 2.1 * 10^{-10} at 95 \% CL$ 

- Combined measurement compatible with SM at  $2.4\sigma$
- Statistic uncertainties dominate

## Combination of ATLAS+CMS+LHCb



 $\tau_{B_{c}^{0} \rightarrow \mu \mu}[ps](LHCb+CMS) = 1.9^{+0.35}_{-0.37}(SM:1.609\pm0.010)$ 

CMS-PAS-BPH-20-003 ; LHCb-CONF-2020-002 ; ATLAS-CONF-2020-049

- Combination from binned two-dimensional profile likelihoods
- Independent systematics, except for ratio of fragmentation fractions  $f_d/f_s$ , common nuisance parameter and only correlation
  - among experiments
- fd/fs profiled separately and its uncertainty included in a single likelihood
- The results compatible with the SM predictions within 2.1 standard deviations in the 2d plane of the branching fractions

### Summary

- Latest ATLAS result measurement of CPviolation in  $B_s \rightarrow J/\psi \phi$  decay and branching ratio measurement of rare  $B_{s(d)} \rightarrow \mu \mu$  decays compatible with Standart Model predictions
- Full Run 2 data analyses in progress

# Backup

## **Tagging performance**

Tag method	$\epsilon_x$ [%]	$D_x$ [%]	$T_x$ [%]
Tight muon	$4.50 \pm 0.01$	$43.8 \pm 0.2$	$0.862 \pm 0.009$
Electron	$1.57 \pm 0.01$	$41.8 \pm 0.2$	$0.274 \pm 0.004$
Low- $p_{\rm T}$ muon	$3.12 \pm 0.01$	$29.9 \pm 0.2$	$0.278 \pm 0.006$
Jet	$12.04 \pm 0.02$	$16.6 \pm 0.1$	$0.334 \pm 0.006$
Total	$21.23 \pm 0.03$	$28.7 \pm 0.1$	$1.75 \pm 0.01$

- Efficiency: Fraction of signals with specific tagger,  $\varepsilon = \frac{N_{tagged}}{N_{Bcand}}$
- Dilution: D = (1 2w), where w is the miss-tag probability
- Tagging Power: figure of merit of tagger performance
  - Depends on dilution and efficiency:  $TP = \epsilon D^2 = \epsilon (1 - 2w)^2$

## **Reconstruction and candidate selection**

#### Event

- Triggers and good quality data
- At least one PV formed from at least 4 ID tracks
- At least one pair of ID+MS identified  $\mu^+\mu^-$

#### $J/\psi \to \mu^+ \mu^-$

- Dimuon vertex fit  $\chi^2/d.o.f. < 10$
- Three dimuon invariant mass windows for BB/BE/EE (barrel,endcap) muon combinations

#### $\phi \rightarrow K^+K^-$

- p<sub>T</sub>(K) > 1 GeV
- 1008.5 MeV < m(KK) < 1030.5 MeV</li>

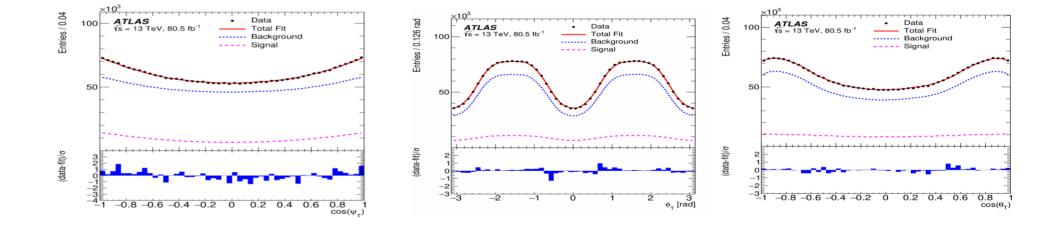
#### $B_s \rightarrow J/\psi(\mu\mu)\phi(KK)$

- p<sub>T</sub>(B<sub>s</sub>) > 10 GeV
- Four-track vertex fit  $\chi^2/d.o.f. < 3$  (J/ $\psi$  mass constrained)
- Keep only the candidate with best vertex fit  $\chi^2/d.o.f.$  in event
- 5150 MeV < m(B<sub>s</sub>) < 5650 MeV  $\rightarrow$  in total 3 210 429 B<sub>s</sub> candidates

# Signal time-angular PDF

k	$O^{(k)}(t)$	$g^{(k)}( heta_T,\psi_T,\phi_T)$
1	$\frac{1}{2} A_0(0) ^2 \left[ (1+\cos\phi_s) \mathrm{e}^{-\Gamma_{\mathrm{L}}^{(s)}t} + (1-\cos\phi_s) \mathrm{e}^{-\Gamma_{\mathrm{H}}^{(s)}t} \pm 2\mathrm{e}^{-\Gamma_s t} \sin(\Delta m_s t) \sin\phi_s \right]$	$2\cos^2\psi_T(1-\sin^2\theta_T\cos^2\phi_T)$
2	$\frac{1}{2} A_{\parallel}(0) ^{2}\left[(1+\cos\phi_{s})\mathrm{e}^{-\Gamma_{\mathrm{L}}^{(s)}t}+(1-\cos\phi_{s})\mathrm{e}^{-\Gamma_{\mathrm{H}}^{(s)}t}\pm2\mathrm{e}^{-\Gamma_{s}t}\sin(\Delta m_{s}t)\sin\phi_{s}\right]$	$\sin^2\psi_T(1-\sin^2\theta_T\sin^2\phi_T)$
3	$\frac{1}{2} A_{\perp}(0) ^{2}\left[(1-\cos\phi_{s})\mathrm{e}^{-\Gamma_{\mathrm{L}}^{(s)}t}+(1+\cos\phi_{s})\mathrm{e}^{-\Gamma_{\mathrm{H}}^{(s)}t}\mp2\mathrm{e}^{-\Gamma_{s}t}\sin(\Delta m_{s}t)\sin\phi_{s}\right]$	$\sin^2\psi_T\sin^2\theta_T$
4	$\frac{1}{2} A_0(0)  A_{\parallel}(0) \cos\delta_{\parallel}\left[(1+\cos\phi_s)\mathrm{e}^{-\Gamma_{\mathrm{L}}^{(s)}t}+(1-\cos\phi_s)\mathrm{e}^{-\Gamma_{\mathrm{H}}^{(s)}t}\pm2\mathrm{e}^{-\Gamma_s t}\sin(\Delta m_s t)\sin\phi_s\right]$	$\frac{1}{\sqrt{2}}\sin 2\psi_T \sin^2 \theta_T \sin 2\phi_T$
5	$ A_{\parallel}(0)  A_{\perp}(0) \left[\frac{1}{2}(\mathrm{e}^{-\Gamma_{\mathrm{L}}^{(s)}t}-\mathrm{e}^{-\Gamma_{\mathrm{H}}^{(s)}t})\cos(\delta_{\perp}-\delta_{\parallel})\sin\phi_{s}\pm\mathrm{e}^{-\Gamma_{s}t}(\sin(\delta_{\perp}-\delta_{\parallel})\cos(\Delta m_{s}t)-\cos(\delta_{\perp}-\delta_{\parallel})\cos\phi_{s}\sin(\Delta m_{s}t))\right]$	$-\sin^2\psi_T\sin 2\theta_T\sin\phi_T$
6	$ A_0(0)  A_{\perp}(0)  \left[\frac{1}{2}(\mathrm{e}^{-\Gamma_{\mathrm{L}}^{(s)}t} - \mathrm{e}^{-\Gamma_{\mathrm{H}}^{(s)}t})\cos\delta_{\perp}\sin\phi_s \pm \mathrm{e}^{-\Gamma_s t}(\sin\delta_{\perp}\cos(\Delta m_s t) - \cos\delta_{\perp}\cos\phi_s\sin(\Delta m_s t))\right]$	$\frac{1}{\sqrt{2}}\sin 2\psi_T \sin 2\theta_T \cos \phi_T$
7	$\frac{1}{2} A_{s}(0) ^{2}\left[(1-\cos\phi_{s})e^{-\Gamma_{L}^{(s)}t}+(1+\cos\phi_{s})e^{-\Gamma_{H}^{(s)}t}\mp 2e^{-\Gamma_{s}t}\sin(\Delta m_{s}t)\sin\phi_{s}\right]$	$\frac{2}{3}\left(1-\sin^2\theta_T\cos^2\phi_T\right)$
8	$\alpha  A_{\mathcal{S}}(0)  A_{\parallel}(0)  \left[\frac{1}{2}(\mathrm{e}^{-\Gamma_{\mathrm{L}}^{(s)}t} - \mathrm{e}^{-\Gamma_{\mathrm{H}}^{(s)}t})\sin(\delta_{\parallel} - \delta_{\mathcal{S}})\sin\phi_{s} \pm \mathrm{e}^{-\Gamma_{s}t}(\cos(\delta_{\parallel} - \delta_{\mathcal{S}})\cos(\Delta m_{s}t) - \sin(\delta_{\parallel} - \delta_{\mathcal{S}})\cos\phi_{s}\sin(\Delta m_{s}t))\right]$	$\frac{1}{3}\sqrt{6}\sin\psi_T\sin^2\theta_T\sin 2\phi_T$
9	$\frac{1}{2}\alpha A_{\mathcal{S}}(0)  A_{\perp}(0) \sin(\delta_{\perp}-\delta_{\mathcal{S}})\left[(1-\cos\phi_{s})e^{-\Gamma_{\rm L}^{(s)}t}+(1+\cos\phi_{s})e^{-\Gamma_{\rm H}^{(s)}t}\mp 2e^{-\Gamma_{s}t}\sin(\Delta m_{s}t)\sin\phi_{s}\right]$	$\frac{1}{3}\sqrt{6}\sin\psi_T\sin 2\theta_T\cos\phi_T$
10	$\alpha  A_0(0)   A_S(0)  \left[ \frac{1}{2} (\mathrm{e}^{-\Gamma_{\mathrm{H}}^{(s)}t} - \mathrm{e}^{-\Gamma_{\mathrm{L}}^{(s)}t}) \sin \delta_S \sin \phi_s \pm \mathrm{e}^{-\Gamma_s t} (\cos \delta_S \cos(\Delta m_s t) + \sin \delta_S \cos \phi_s \sin(\Delta m_s t)) \right]$	$\frac{4}{3}\sqrt{3}\cos\psi_T\left(1-\sin^2\theta_T\cos^2\phi_T\right)$

## **Projections on angles**



# Systematic Uncertainties

	$\phi_s$	$\Delta\Gamma_s$	$\Gamma_s$	$ A_{\parallel}(0) ^2$	$ A_0(0) ^2$	$ A_{S}(0) ^{2}$	$\delta_{\perp}$	$\delta_{\parallel}$	$\delta_{\perp} - \delta_{z}$
	[10 <sup>-3</sup> rad]	$[10^{-3} \text{ ps}^{-1}]$	$[10^{-3} \text{ ps}^{-1}]$	$[10^{-3}]$	$[10^{-3}]$	$[10^{-3}]$	$[10^{-3} \text{ rad}]$	$[10^{-3} \text{ rad}]$	[10 <sup>-3</sup> ra
Tagging	19	0.4	0.3	0.2	0.2	1.1	17	19	2.3
Tagging									
Acceptance	0.5	< 0.1	< 0.1	1.0	0.8	2.6	30	50	11
ID alignment	0.8	0.2	0.5	< 0.1	< 0.1	< 0.1	11	7.2	< 0.1
Best candidate selection	0.5	0.4	0.7	0.5	0.2	0.2	12	17	7.5
Background angles model:									
Choice of fit function	2.5	< 0.1	0.3	1.1	< 0.1	0.6	12	0.9	1.1
Choice of $p_{\rm T}$ bins	1.3	0.5	< 0.1	0.4	0.5	1.2	1.5	7.2	1.0
Choice of mass interval	0.4	0.1	0.1	0.3	0.3	1.3	4.4	7.4	2.3
Dedicated backgrounds:									
$B^0_d$	2.3	1.1	< 0.1	0.2	3.0	1.5	10	23	2.1
$\Lambda_{b}^{a}$	1.6	0.3	0.2	0.5	1.2	1.8	14	30	0.8
Fit model:									
Time res. sig frac	1.4	1.1	0.5	0.5	0.6	0.8	12	30	0.4
Time res. $p_{\rm T}$ bins	0.7	0.5	0.8	0.1	0.1	0.1	2.2	14	0.7
S-wave phase	0.2	< 0.1	< 0.1	0.3	< 0.1	0.3	11	21	8.4
Fit bias	4.1	1.7	0.9	1.4	< 0.1	1.5	19	0.9	7.0
Total	20	2.5	1.6	2.3	3.5	4.5	50	79	18

Uncertainty in the calibration of the  $B_s$ -tag probability; MC statistical uncertainty included in fit stat. error Alternative detector acceptance fit-functions and binning determined from MC Radial expansion uncertainties determined from their effect on tracks  $d_0$  in the data

Background angles model (fixed in UML fit) extracted from data with varying sidebands size and binning Uncertainties of relative fraction; fit-model and P-wave contribution Uncertainties of relative fraction; fit-model and contributions from  $\Lambda_{h} \rightarrow J/\psi$ Kp decays

Toy-MC studies; pulls of the default fit model, default fit on toy-data generated with modified PDFs