Caltech

Current anomalies in semileptonic B decays into charm: Global EFT analysis

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In collaboration with Martin Jung, Rusa Mandal, Ana Peñuelas and Antonio Pich

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Accessing High Energies

$$\mathcal{L} = \mathcal{L}_{\rm SM} + \mathcal{O}\left(\frac{\rm Energy}{\Lambda_{\rm NP}}\right)^n$$





[Based on Refs. 1904.09311 and 2004.06726, in collaboration with Martin Jung, Rusa Mandal, Ana Peñuelas and Antonio Pich.]





$$\triangleright \mathcal{R}_{D^{(*)}} \equiv \frac{\mathcal{B}(B \to D^{(*)} \tau \bar{\nu}_{\tau})}{\mathcal{B}(B \to D^{(*)} \ell \bar{\nu}_{\ell})}$$

Status 2021



Pattern of deviations in B-meson decays involving b to c transitions pointing to "the same direction"

$$\begin{array}{l} \clubsuit \quad \mathcal{R}_{D^{(*)}} \equiv \frac{\mathcal{B}(B \to D^{(*)}\tau\bar{\nu}_{\tau})}{\mathcal{B}(B \to D^{(*)}\ell\bar{\nu}_{\ell})} & \textbf{3.1 } \sigma \\ \\ \text{HFLAV, up to date} \\ \cr \clubsuit \quad \mathcal{R}_{J/\Psi} \equiv \frac{\mathcal{B}(B_c \to J/\Psi\tau\bar{\nu}_{\tau})}{\mathcal{B}(B_c \to J/\Psi\mu\bar{\nu}_{\mu})} = 0.71 \pm 0.17 \pm 0.18 \\ \\ \text{LHCb, 2017} & \textbf{1.7 } \sigma \\ \\ R_{J/\Psi_{SM}} \sim 0.25 - 0.28 \\ \cr \clubsuit \quad \bar{\mathcal{P}}_{\tau}^{D^*} = -0.38 \pm 0.51^{+0.21}_{-0.16} \\ \\ \text{Belle, 2016} \\ \mathcal{P}_{\tau}(D^*)_{SM} = -0.499 \pm 0.003 \\ \cr \clubsuit \quad \bar{F}_{L}^{D^*} = 0.60 \pm 0.08 \pm 0.04 \\ \\ \text{Belle, 2019} \\ \end{array} \begin{array}{l} \textbf{1.6 } \sigma \\ \\ \hline{\nu}_{\overline{\nu}}(p_{\nu}) \end{array}$$

 \bullet Most general effective dim 6 Hamiltonian:

 $\mathcal{H}_{\text{eff}}^{b \to c\ell\nu} = \frac{4 G_F}{\sqrt{2}} V_{cb} [(1 + C_{V_L})\mathcal{O}_{V_L} + C_{V_R}\mathcal{O}_{V_R} + C_{S_R}\mathcal{O}_{S_R} + C_{S_L}\mathcal{O}_{S_L} + C_T \mathcal{O}_T] + \text{h.c.}$



$$\mathcal{O}_{V_L} = (\bar{c} \,\gamma^{\mu} P_L b) (\bar{\ell} \,\gamma_{\mu} P_L \nu_{\ell}),$$

$$\mathcal{O}_{S_R} = (\bar{c} \,P_R b) (\bar{\ell} \,P_L \nu_{\ell}),$$

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• Assumptions:

$$\blacktriangleright$$
 EFT \checkmark \blacktriangleright New physics only in the third generationNP effects negligible in $b \rightarrow c(e, \mu)\bar{\nu}_{(e,\mu)}$ analysis [Jung, Straub, 1801.01112]

$$\mathcal{O}_{V_L} = (\bar{c} \,\gamma^{\mu} P_L b) (\bar{\tau} \,\gamma_{\mu} P_L \nu_{\tau}),$$

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• Assumptions:

 $\begin{array}{c} \overleftarrow{} & \text{EFT} \\ \hline{} & \overleftarrow{} \\ \end{array} \\ \hline & \text{New physics only in the third generation,} \\ \hline{} & \overleftarrow{} \\ & C_{V_R} \text{ lepton flavour universal } \Rightarrow C_{V_R}^{\tau} \sim 0 \\ \\ & C_{V_R}^{\ell} \equiv C_{V_R} + \mathcal{O}\left(\frac{v^4}{\Lambda_{\text{NP}}^4}\right) \end{array}$

Assuming SMEFT and no significant effect from NP in $b \to c(e,\mu)\bar{\nu}_{(e,\mu)}$ [Jung, Straub, 1801.01112]

$$\mathcal{O}_{V_L} = (\bar{c} \,\gamma^{\mu} P_L b) (\bar{\tau} \,\gamma_{\mu} P_L \nu_{\tau}),$$

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$$\mathcal{H}_{\text{eff}}^{b \to c\ell\nu} = \frac{4\,G_F}{\sqrt{2}} V_{cb} [(1 + C_{V_L})\mathcal{O}_{V_L} + C_{V_R}\mathcal{O}_{V_R} + C_{S_R}\mathcal{O}_{S_R} + C_{S_L}\mathcal{O}_{S_L} + C_T \mathcal{O}_T] + \text{h.c.}$$

• Assumptions:

Fitted complex W.C. without significant improvement

$$\mathcal{O}_{V_L} = (\bar{c} \,\gamma^{\mu} P_L b) (\bar{\tau} \,\gamma_{\mu} P_L \nu_{\tau}),$$

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• Assumptions:

 $\begin{array}{c} \longleftrightarrow \\ FT \\ \hline \\ \end{array} \end{array}$ New physics only in the third generation, $\begin{array}{c} \longleftrightarrow \\ C_{V_R} \\ \end{array}$ lepton flavour universal $\Rightarrow C_{V_R}^{\tau} \sim 0$ $\begin{array}{c} \longleftrightarrow \\ CP \\ \end{array}$ CP conserving W.C.



$$\mathcal{O}_{V_L} = (\bar{c} \,\gamma^{\mu} P_L b) (\bar{\tau} \,\gamma_{\mu} P_L \nu_{\tau}),$$

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$$\mathcal{H}_{\text{eff}}^{b \to c\ell\nu} = \frac{4 G_F}{\sqrt{2}} V_{cb} [(1 + C_{V_L})\mathcal{O}_{V_L} + C_{S_R} \mathcal{O}_{S_R} + C_{S_L} \mathcal{O}_{S_L} + C_T \mathcal{O}_T] + \text{h.c.}$$







Image borrowed from [Celis et al., 2016]

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$$\mathcal{B}(B_c \to \tau \bar{\nu}_{\tau}) = \# |V_{cb}|^2 \times \left| 1 + C_{V_L} - C_{V_R} + \frac{m_{B_c}^2}{m_{\tau}(m_b + m_c)} \left(C_{S_R} - C_{S_L} \right) \right|^2$$

 \bullet Most general effective dim 6 Hamiltonian:

 $\mathcal{H}_{\text{eff}}^{b \to c\ell\nu} = \frac{4 G_F}{\sqrt{2}} V_{cb} [(1 + C_{V_L})\mathcal{O}_{V_L} + C_{S_R} \mathcal{O}_{S_R} + C_{S_L} \mathcal{O}_{S_L} + C_T \mathcal{O}_T] + \text{h.c.}$

• Inputs:

$$\begin{array}{c} \blacktriangleright & \mathcal{R}_D \\ \hline & \swarrow & \mathcal{R}_{D^*} \\ \hline & \frown & \Gamma(B \to D^{(*)} \tau \bar{\nu}_{\tau}) \\ \hline & \blacksquare & B_c \to \tau \bar{\nu}_{\tau} \end{array}$$

• Bc lifetime:

 $\Rightarrow \operatorname{Br}(B_c \to \tau \bar{\nu}_{\tau}) \le 30 - 40\%$ [Alonso et al., 2016]

• Bound LEP Z peak:
[Akeroyd et al., 2017]

$$\Rightarrow Br(B_c \rightarrow \tau \bar{\nu}_{\tau}) \leq 10\%$$

$$\mathcal{B}(B_c \to \tau \bar{\nu}_{\tau}) = \# |V_{cb}|^2 \times \left| 1 + C_{V_L} - C_{V_R} + \frac{m_{B_c}^2}{m_{\tau}(m_b + m_c)} \left(C_{S_R} - C_{S_L} \right) \right|^2$$

 \bullet Most general effective dim 6 Hamiltonian:

$$\mathcal{H}_{\text{eff}}^{b \to c\ell\nu} = \frac{4 G_F}{\sqrt{2}} V_{cb} [(1 + C_{V_L})\mathcal{O}_{V_L} + C_{S_R} \mathcal{O}_{S_R} + C_{S_L} \mathcal{O}_{S_L} + C_T \mathcal{O}_T] + \text{h.c.}$$

• Inputs:





 $-C_{V_L} - C_{V_R} - C_{S_R} - C_{S_L} - C_T$ $\pm 1 \sigma \qquad \pm 2 \sigma$

$$\Rightarrow \mathcal{R}_{D^*} = \mathcal{R}_{D^*} [\underbrace{(1 + C_{V_L} - C_{V_R})}_{\text{axial} \equiv C_A}, \underbrace{(C_{S_R} - C_{S_L})}_{\text{pseudo-scalar} \equiv C_P}, C_T]$$

• Inputs:

$$\begin{array}{c} \blacktriangleright & \mathcal{R}_{D^*}(C_A) & \mathcal{C}_P & \mathcal{C}_T \\ \hline & \bullet & \Gamma(B \to D^{(*)}\tau\bar{\nu}_{\tau}) \\ \hline & \bullet & B_c \to \tau\bar{\nu}_{\tau} & \mathcal{C}_A & \mathcal{C}_P \\ \hline & \bullet & F_L^{D^*} & \mathcal{C}_A & \mathcal{C}_P & \mathcal{C}_T \end{array}$$





Global Fit: inputs

 \bullet Most general effective dim 6 Hamiltonian:

$$\mathcal{H}_{\text{eff}}^{b \to c\ell\nu} = \frac{4 G_F}{\sqrt{2}} V_{cb} [(1 + C_{V_L})\mathcal{O}_{V_L} + C_{S_R} \mathcal{O}_{S_R} + C_{S_L} \mathcal{O}_{S_L} + C_T \mathcal{O}_T] + \text{h.c.}$$

• Inputs:



$$\chi^2 = \underbrace{\chi^2_{\exp}}_{exp} + \underbrace{\chi^2_{FF}}_{exp}$$

$$\begin{split} \mathcal{R}_D, \mathcal{R}_{D^*} \ 2 \ \mathrm{d.o.f.} & \quad 10 \ \mathrm{d.o.f.} \\ \Gamma(B \to D^{(*)}) \ 58 \ \mathrm{d.o.f.} \\ F_L^{D^*} \ 1 \ \mathrm{d.o.f.} \end{split}$$

Global fit: Form Factors



Global Fit: Goodness of the fit

• Standard Model $(\forall C_i = 0)$ $\chi^2_{SM} = 65.5/57$ d.o.f.

$$\chi^2_{R_D,R_{D^*}} = 22.6/2 \rightarrow \text{Reproduce the well-known tension}$$

$$\chi_{\Gamma[q^2]}^2 = 43/54$$

Conservative uncertainties
Misleading χ^2 contribution
$$\int_{-20}^{60} \int_{-20}^{\text{Belle}} \int_{-20}^{10} \int_{-20}^{0} \int_{-20}^{0}$$

Quality of the fit: Pull w.r.t. the SM

Global Fit: Results

• SM:
$$\chi^2_{SM} = 65.5/57$$
 d.o.f.

• New Physics:
$$\chi^2_{min1} = 34.1/53_{\text{d.o.f.}} \qquad \chi^2_{min2} = 37.5/53_{\text{d.o.f.}} \qquad \chi^2_{min3} = 58.6/53_{\text{d.o.f.}}$$



Global Fit: Results



Global Fit: Predictions



Global Fit: Predictions

 Λ_c

2

 $\overline{\mathcal{J}_{n}}$

C



Global Fit: Results



• Theory assumptions:

\rightarrow EFT

 \blacktriangleright New physics only in the third generation

 $ightarrow C_{V_R}$ flavour universal

 \clubsuit CP conserving W.C.

• Experimental measurements

• Theory assumptions:

EFT

 \checkmark New physics only in the third generation of leptons

 $ightarrow C_{V_R}$ flavour universal

 \clubsuit CP conserving W.C.

No significant improvement of χ^2 by promoting the W.C. to be complex

• Experimental measurements

• Theory assumptions:

\rightarrow EFT

 \checkmark New physics only in the third generation of leptons



EW breaking is non-linear?

• Experimental measurements

Global fit + C_{V_R}



• Theory assumptions:



 \checkmark New physics only in the third generation of leptons

 $ightarrow C_{V_R}$ flavour universal

 \clubsuit CP conserving W.C.

• Experimental measurements

• Theory assumptions:

EFT New light d.o.f. [C. Bobeth et al., a month ago]

 \checkmark New physics only in the third generation of leptons

??

 $ightarrow C_{V_R}$ flavour universal

 \checkmark CP conserving W.C.

• Experimental measurements

• Theory assumptions:

 \rightarrow EFT New light d.o.f.

 \blacksquare New physics only in the third generation of leptons

 $ightarrow C_{V_R}$ flavour universal

 \checkmark CP conserving W.C.

• Experimental measurements

Bounds on $Br(B_c \rightarrow \tau \bar{\nu})$

Resurrection of the scalar candidates ?



 $\mathcal{B}(B_c \to \tau \bar{\nu}) < 60\%$



See discussion in [M. Blanke et al., 2019]

[Akeroyd et al., 2017]

Implications of new measurements?



[Speculating...]

Belle-II	5 ab^{-1}	$50 {\rm ~ab}^{-1}$
\mathcal{R}_{D^*}	$(\pm 3.0 \pm 2.5)\%$	$(\pm 1.0 \pm 2.0)\%$
$ar{P}^{D^*}_{ au}$	$\pm 0.18 \pm 0.08$	$\pm 0.06 \pm 0.04$

My guess:	$F_L^{D^*}$	$\sim 15\%$	\Rightarrow	5%
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Thank you!



SLIDES

Global Fit: Goodness of the fit

• P-value

$$p(\chi^2_{\rm min}, n) \equiv \int_{\chi^2_{\rm min}}^{\infty} dz \, \chi^2(z, n)$$

• Pull [# of standard deviations]

$$\text{Pull}_{\text{SM}} \equiv \text{prob}(\Delta \chi_i^2, \Delta n_i)[\sigma] = \sqrt{2} \text{Erf}^{-1}[\text{CDF}(\Delta \chi_i^2, \Delta n_i)]$$

Global Fit: New Physics interpretations



• Effect of the running between WET and SMEFT W.C ($\Lambda = 1$ TeV)

$$C_{V_{L}}(\mu_{b}) = -1.503 \ \tilde{C}_{V_{L}}(\Lambda) ,$$

$$C_{S_{L}}(\mu_{b}) = -1.257 \ \tilde{C}_{S_{L}}(\Lambda) + 0.2076 \ \tilde{C}_{T}(\Lambda) ,$$

$$C_{S_{R}}(\mu_{b}) = -1.254 \ \tilde{C}_{S_{R}}(\Lambda) ,$$

$$C_{T}(\mu_{b}) = 0.002725 \ \tilde{C}_{S_{L}}(\Lambda) - 0.6059 \ \tilde{C}_{T}(\Lambda) .$$

Global Fit: New Physics interpretations



• Global minimum:

 $C_{V_L} = 0.09^{+0.13}_{-0.11}, \quad C_{S_R} = 0.14^{+0.06}_{-0.67}, \quad C_{S_L} = -0.20^{+0.58}_{-0.03}, \quad C_T = 0.007^{+0.046}_{-0.044}$

• New gauge mediator: $W' \sim (1,3,0)$ $\mathcal{L}_{\text{eff}} \supset -\frac{\tilde{g}_{\ell\nu_{\ell}}\tilde{g}_{du}^{\dagger}}{M_{W'}^2} (\bar{\ell}_L \gamma_{\mu} \nu_{\ell L}) (\bar{u}_L \gamma^{\mu} d_L) \qquad \Rightarrow M_{W'} = 0.22 \text{ TeV}$



(sequential W')

 $\mathcal{B}(B_c \to \tau \nu) \le 10\%$



• Motivated scenarios:

$$C_{LL}^V + \text{All RH}$$

All

All RH
$$u_R$$

$$\begin{array}{l} \Phi \sim (1,2,1/2) \\ S_1 \sim (\bar{3},1,1/3) \\ \tilde{R}_2 \sim (3,2,1/6) \end{array} \begin{array}{l} {\rm Scalar} \\ \tilde{R}_2 \sim (3,2,1/6) \\ U_1^{\mu} \sim (3,1,2/3) \\ U_3^{\mu} \sim (3,3,2/3) \\ \tilde{V}_2^{\mu} \sim (\bar{3},2,-1/6) \\ V^{\mu} \sim (1,1,-1) \end{array} \begin{array}{l} {\rm Scalar} \\ {\rm Scalar} \\$$

 $\mathcal{B}(B_c \to \tau \nu) \le 30\%$



• Motivated scenarios:

$$C_{LL}^V + \text{All RH}$$

All

All RH
$$u_R$$

$$\begin{array}{l} \Phi \sim (1,2,1/2) \\ S_1 \sim (\bar{3},1,1/3) \\ \tilde{R}_2 \sim (3,2,1/6) \end{array} \begin{array}{l} {\rm Scalar} \\ \tilde{R}_2 \sim (3,2,1/6) \\ U_1^{\mu} \sim (3,1,2/3) \\ U_3^{\mu} \sim (3,3,2/3) \\ \tilde{V}_2^{\mu} \sim (\bar{3},2,-1/6) \\ V^{\mu} \sim (1,1,-1) \end{array} \begin{array}{l} {\rm Scalar} \\ {\rm Scalar} \\$$









 $[\]Delta \mathcal{R}_D$







 $Pull_{SM}$ – p-value

Angular observables (D^*)

 $D^{*}(p_{D^{*}})$ $\tau(p_{\tau})$ $W^*_{\mu}(q)$ $\overline{\nu}(p_{\nu})$ $F_L^{D^*} = \frac{1}{\Gamma} \int_{q^2}^{q^2_{\text{max}}} dq^2 \frac{d\Gamma_{\lambda_D^*} = 0}{dq^2}$ $\mathcal{P}_{\tau}^{D^*} = \frac{1}{\Gamma} \int_{q_{\text{max}}^2}^{q_{\text{max}}^2} dq^2 \left(\frac{d\Gamma_{\lambda_{\tau}=1/2}}{dq^2} - \frac{d\Gamma_{\lambda_{\tau}=-1/2}}{dq^2} \right)$ $\mathcal{A}_{\mathrm{FB}}^{D^*} = \frac{1}{\Gamma} \int_{q_{\mathrm{min}}^2}^{q_{\mathrm{max}}^2} dq^2 \left[\int_0^1 - \int_{-1}^0 \right] d\cos\theta_\tau \frac{d^2\Gamma}{dq^2 d\cos\theta_\tau}$