

Charm (and bottom) baryons and charmonium excitations from the lattice

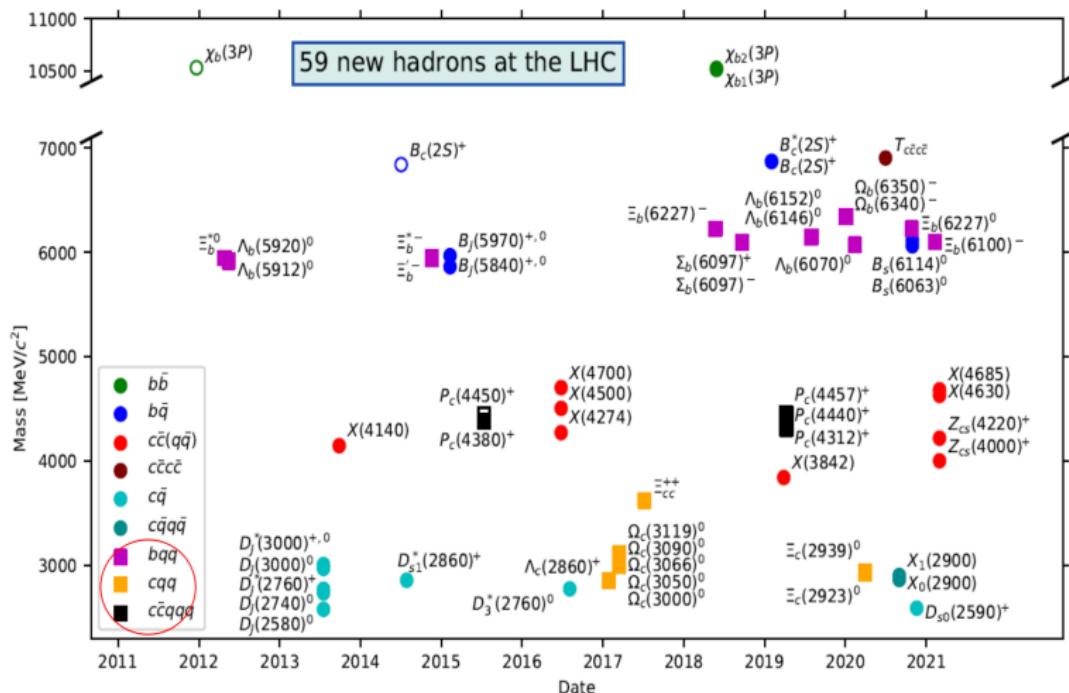
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Mainz, Germany

10th International Workshop on Charm Physics
02nd June, 2021

Charm and bottom baryons

Heavy baryons



A significant fraction of them are heavy baryons. LHCb public: <https://lhcb-public.web.cern.ch/>
An equally similar collection from Belle and interesting prospects at STCF.

Hadron spectroscopy on the lattice

- Euclidean two point current-current correlation functions

$$C_{ji}(t_f - t_i) = \langle 0 | O_j(t_f) \bar{O}_i(t_i) | 0 \rangle = \sum_n \frac{Z_i^{n*} Z_j^n}{2E_n} e^{-E_n(t_f - t_i)}$$

- Quark smearing to improve the overlap with ground states!

$$q(x, t) = \sum_y S(x, y) q_b(y, t)$$

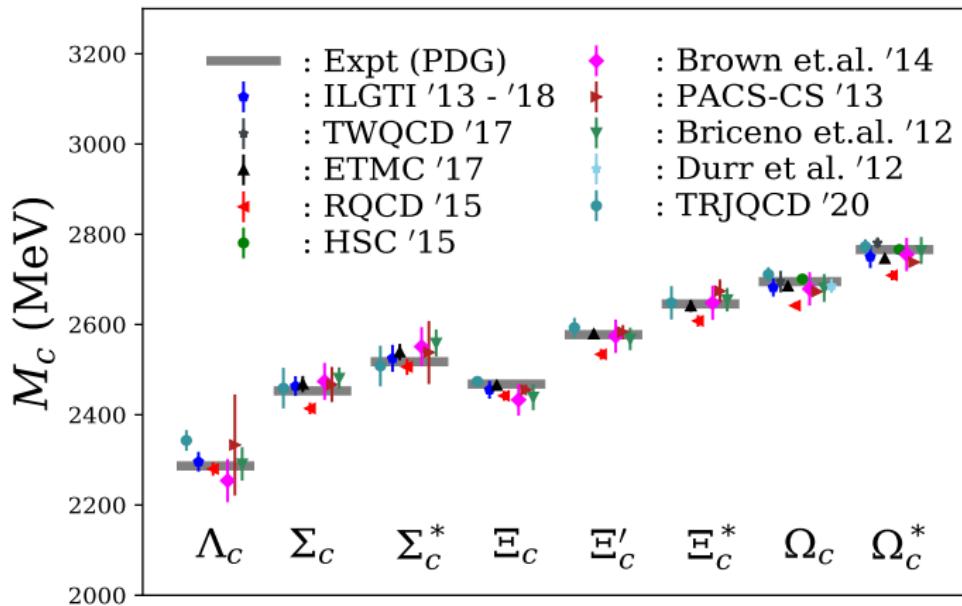
- Correlation matrices out of large basis of hadron interpolating operators ($O_j(t)$) with desired quantum numbers.

$$O_j(t) = \sum_x \bar{q}(x, t) \Gamma_j(x, t) q(x, t)$$

- Variational study (GEVP) to extract physical information

$$C_{ji}(t) v_i^n = \lambda^n(t, t_0) C_{ji}(t_0) v_i^n$$

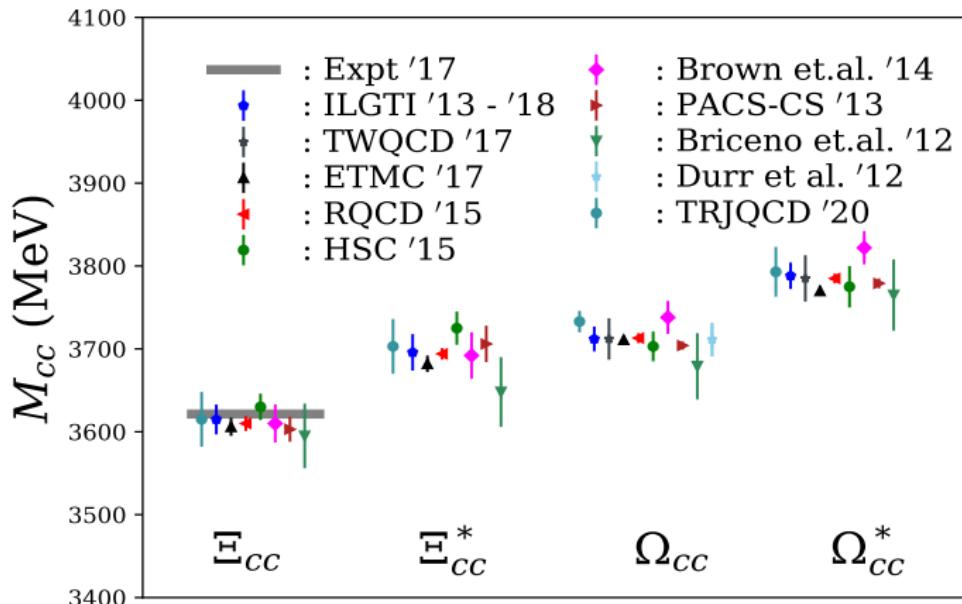
Singly charm baryons



Early quenched lattice calculations : [Lewis et al. '01; Mathur et al. '02; Flynn et al. '03](#)

Dynamical (light quark) investigations : [Liu et al. '10](#)

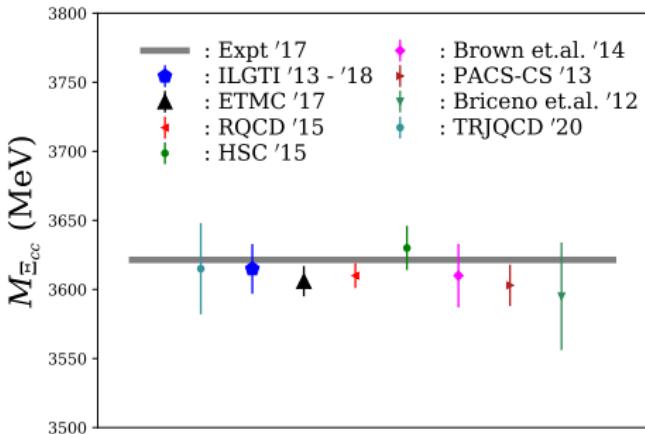
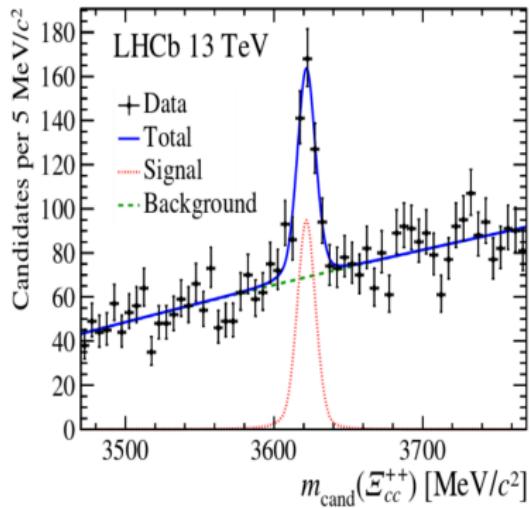
Doubly charm baryons



Another calculation of heavy baryon masses: QCDSF-UKQCD 1711.02485.
Heavy baryon mass splittings : BMW Science 347 1452 '15

Early quenched lattice calculations : Lewis et al. '01; Mathur et al. '02; Flynn et al. '03
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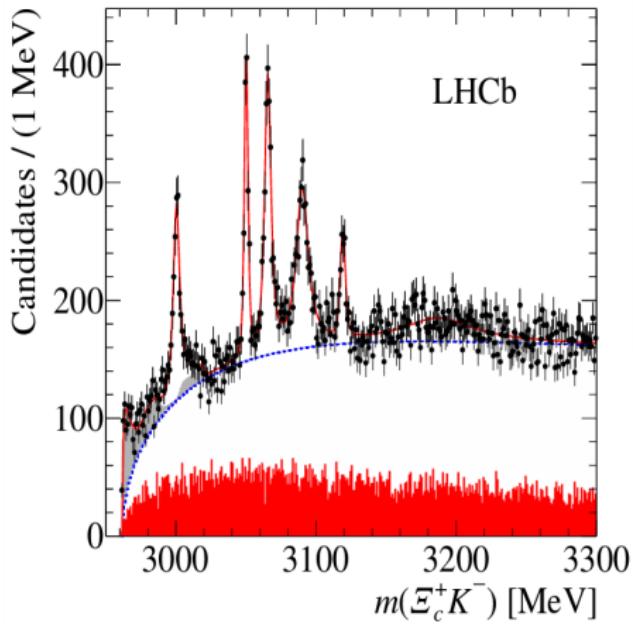
The first doubly charm baryon : Ξ_{cc}



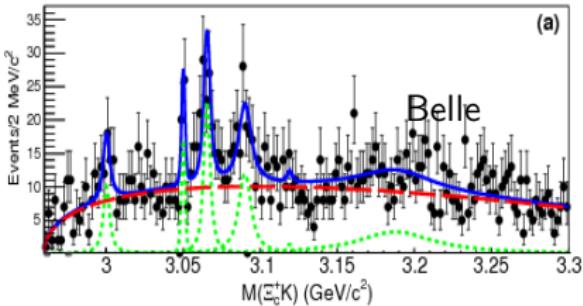
Ξ_{cc} isospin splitting (LQCD), $2.16(11)(17)$ MeV : [BMW Science 347 1452 '15](#)
SELEX measurement (3519 MeV) : [Mattson et al. PRL 89 112001 '02](#)

All lattice calculations disfavors SELEX peak to be a doubly charm baryon.

LHCb discovery of excited Ω_c^0 baryons



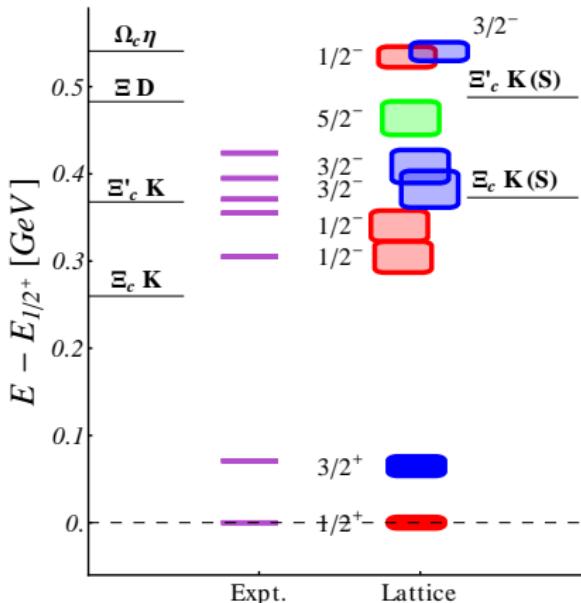
Resonance	Energy	Width	Q.no.
Ω_c^0	2695(2)	-	$1/2^+$
$\Omega_c^0(2770)$	2766(2)	-	$3/2^+$
$\Omega_c^0(3000)$	3000(1)	4.5(1)	?
$\Omega_c^0(3050)$	3050(1)	1(-)	?
$\Omega_c^0(3066)$	3066(1)	3.5(-)	?
$\Omega_c^0(3090)$	3090(1)	8.7(1)	?
$\Omega_c^0(3119)$	3119(1)	1(1)	?



Aaij *et al.* (LHCb) PRL118 182001 '17

Confirmation by Belle : Yelton *et al.* (Belle) PRD97 051102 '18

Experiment vs. lattice predictions



Here $\Delta E = E - E_{\Omega_0^0}$.

The new states correspond to the excited p -wave excitations.

MP & Mathur (HSC) PRL119 042001 '17

Energy	Expt.	Lattice
$\Delta E_{\Omega_c^0(3119)}$	422(1)	464(20)
$\Delta E_{\Omega_c^0(3090)}$	395(1)	409(19)
$\Delta E_{\Omega_c^0(3066)}$	371(1)	383(21)
$\Delta E_{\Omega_c^0(3050)}$	355(1)	341(18)
$\Delta E_{\Omega_c^0(3000)}$	305(1)	304(17)
$\Delta E_{\Omega_c^0(2770)}$	70.7(1)	65(11)
$E_{\Omega_c^0} - \frac{1}{2}E_{\eta_c}$	1203(2)	1209(7)

Spin 1/2, 3/2, 5/2

Ω_{ccc} : HSC PRD90 074504 '14

Ξ_{cc} and Ω_{cc} : HSC PRD91 094502 '15

Ω_c , Σ_c , Λ_c and Ξ_c : CHARM 2013, 1311.4806

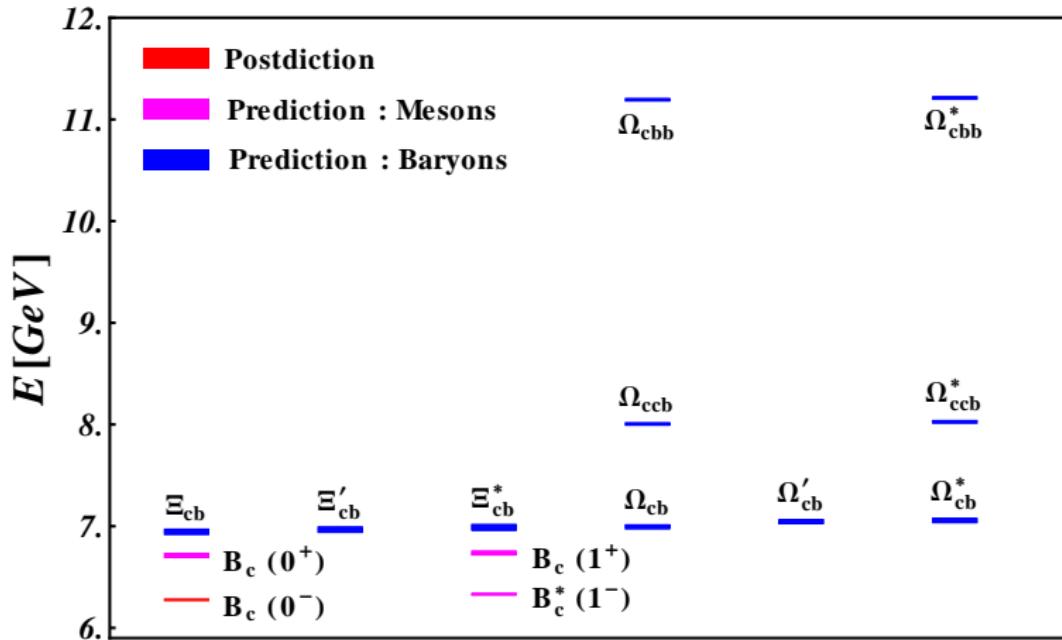
On anisotropic $N_f = 2 + 1$ lattices

$$L \sim 1.9 \text{ fm}, a_t m_c = 0.114$$

and $m_\pi = 391$ MeV

Edwards et al. PRD**78** 054501 '08

Precise determination of bc hadron masses

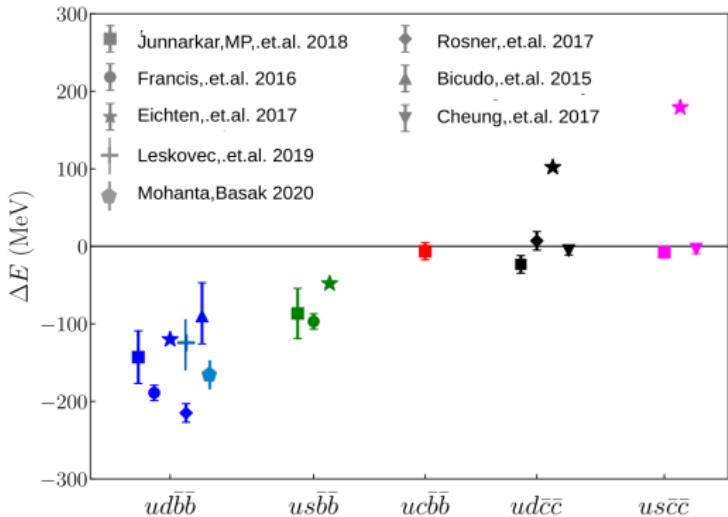


Mathur, MP, Mondal 1806.04151

Results agree with experiment* and with other lattice calculations:

Brown *et al* 1409.0497; HPQCD 1207.5149, 1010.3848; Wurtz *et al* 1505.04410

Doubly heavy tetraquarks



For a sufficiently heavy Q: a strong interaction stable $qq'\bar{Q}\bar{Q}$ tetraquark.

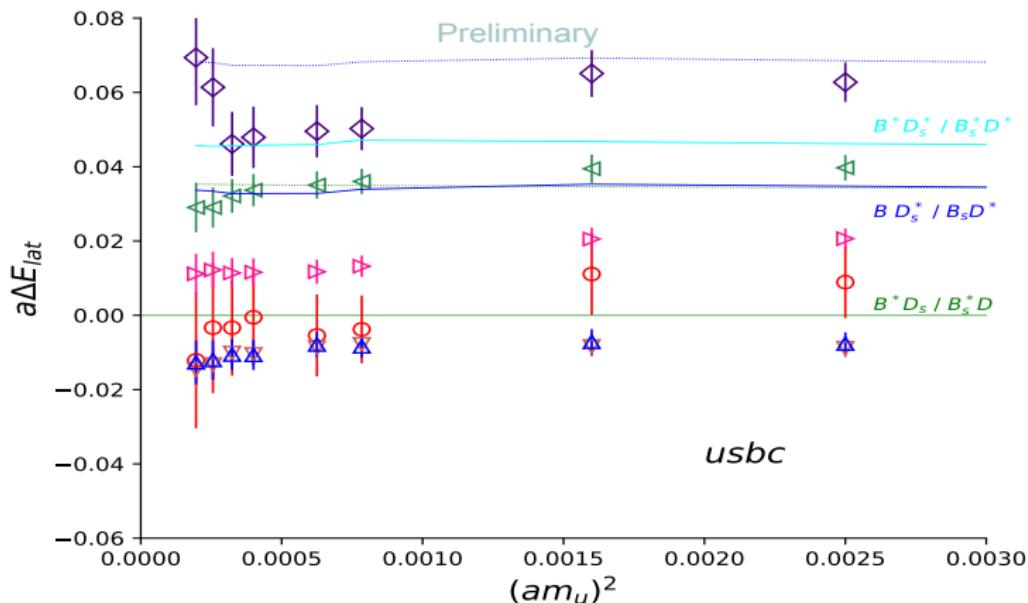
An extensive calculation of various flavor combinations: [Hudspith et al 2006.14294](#)

Argues no evidence for deeply bound states other than in doubly bottom axialvector channels.

[Bicudo et al 2101.00723](#)

Investigation on the nature of doubly bottom axialvector tetraquarks.

Bottom-charm tetraquarks

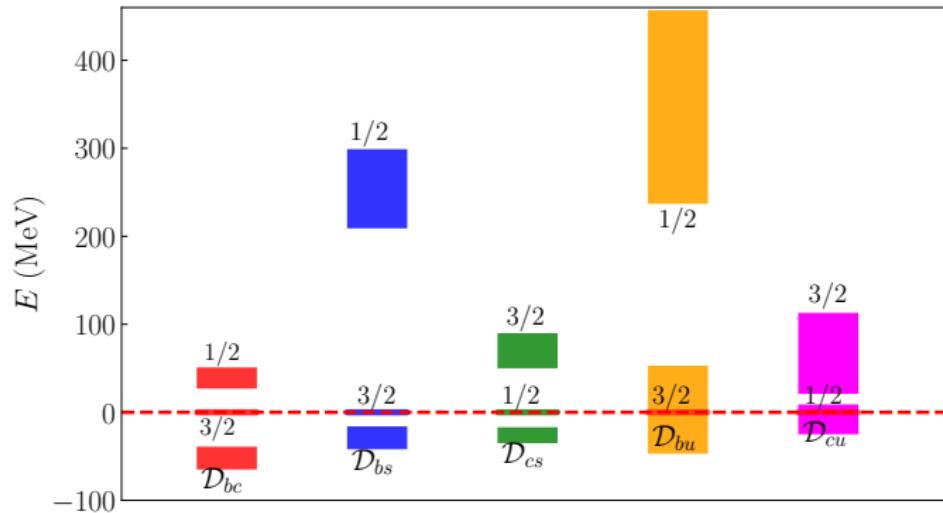


Ongoing investigation on bc tetraquarks. [MP, Mathur \(ILGTI\)](#)

Indicates several finite volume energy levels close to and below the elastic threshold.

Calls for a rigorous finite volume amplitude analysis for definitive statements.

Deuteron-like heavy dibaryons

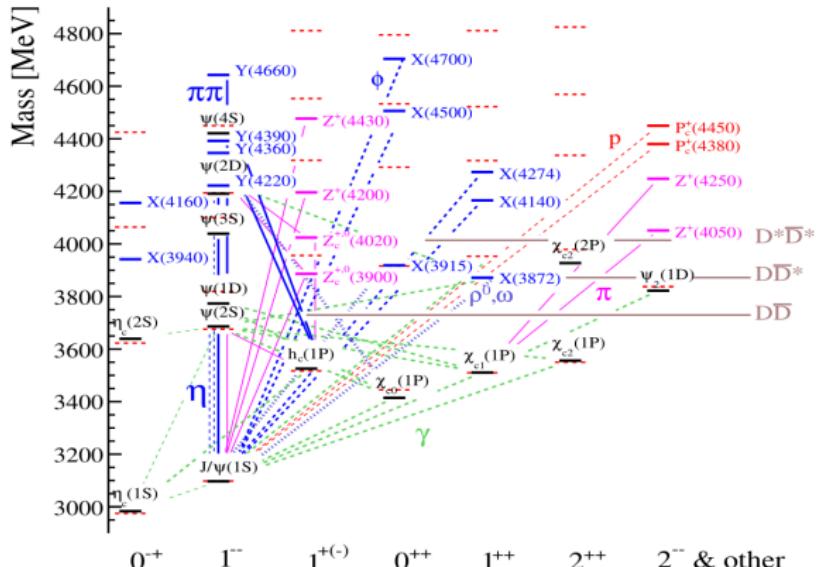


Junnarkar and Mathur 1906.06054

Find indications of large binding energy in bc system.

Charmonium spectra

Charmonium spectra



Rich energy spectrum. XYZ states.

$\bar{c}c$ picture works well for states below open charm threshold.

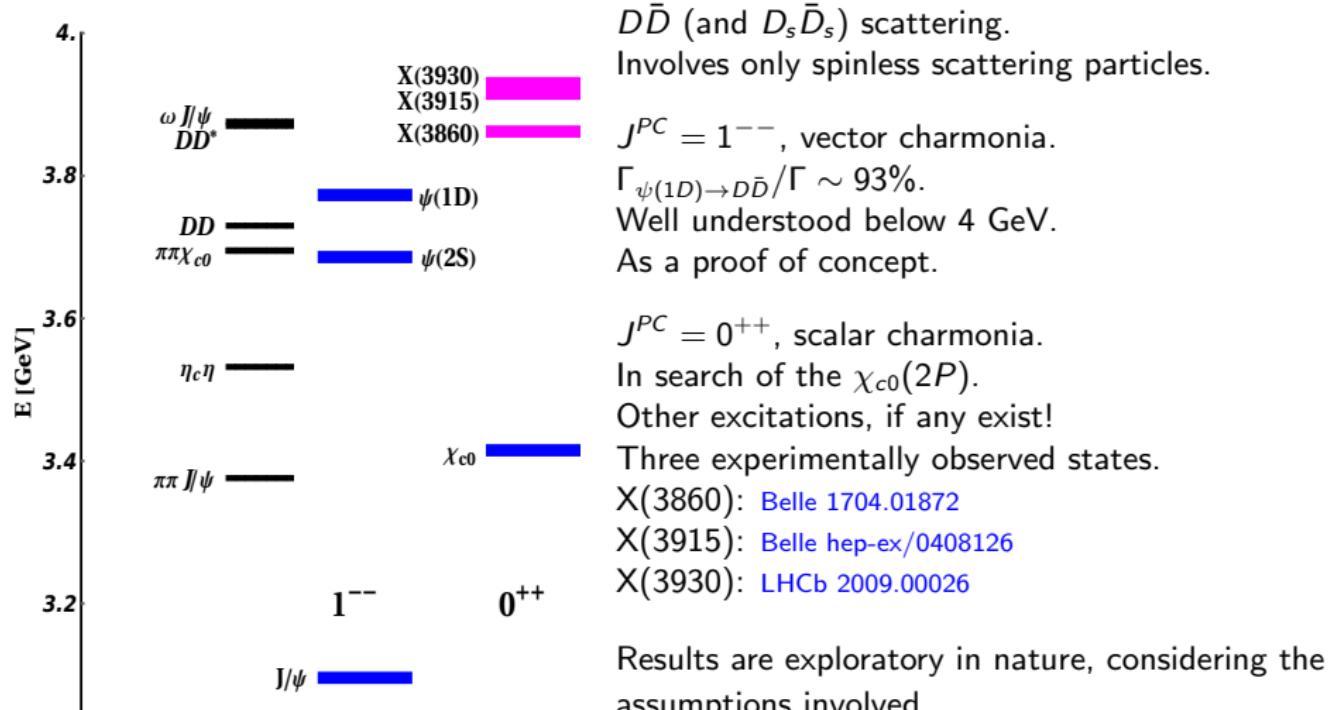
No single description for states above the open charm threshold.

Olsen *et al* 1708.04012

Several lattice calculations assuming a $\bar{c}c$ picture.

RQCD 2018; HSC 2012, 2016; Mohler *et al* 2013, Bali *et al* 2011

Charmonium: channels focussed



Currently we ignore $\eta_c\eta$ and all three particle channels in our entire analysis.

How do we do?

- Ensemble : CLS
 - U101 $N_f = 2 + 1$, $L \sim 2$ fm, $N_{ev} = 90$
 - H105 $N_f = 2 + 1$, $L \sim 2.7$ fm, $N_{ev} = 150$
 - $m_\pi \sim 280$ MeV, $m_K \sim 467$ MeV
 - Two charm quark masses: $m_D \sim 1762$ MeV and 1927 MeV
- Multiple excited state extraction
Correlation matrices using a large basis of interpolating operators

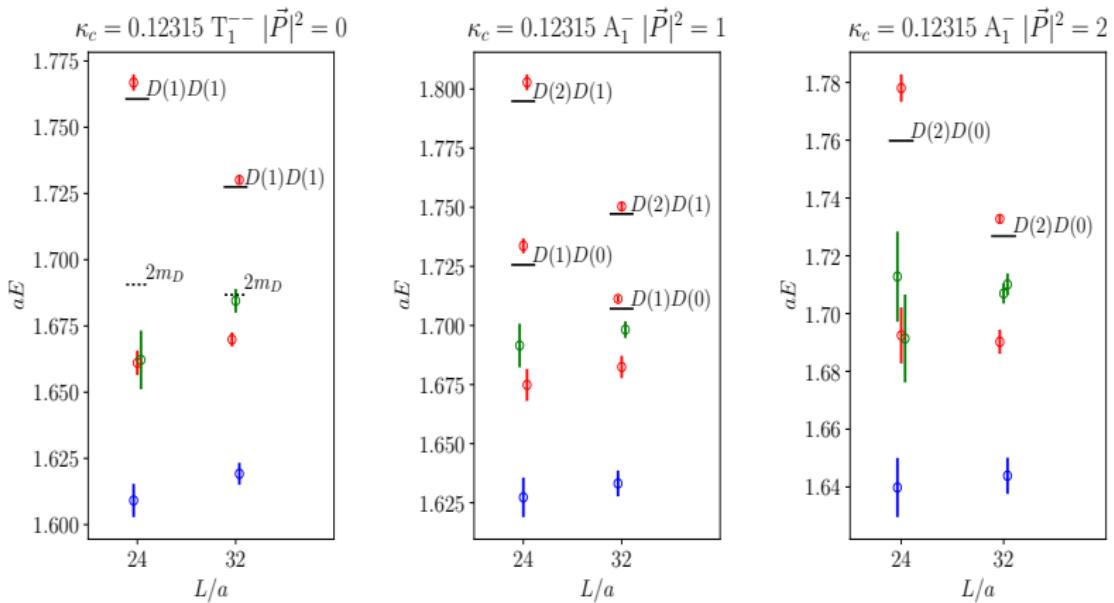
$$C_{ji}(t_f - t_i) = \langle 0 | O_j(t_f) \bar{O}_i(t_i) | 0 \rangle = \sum_n \frac{Z_n^{i*} Z_n^j}{2E_n} e^{-E_n(t_f - t_i)}$$

Operator state overlap factors : $Z_n^j = \langle 0 | O_j | n \rangle$.

Physical state information from variational analysis of $C_{ji}(t_f - t_i)$.

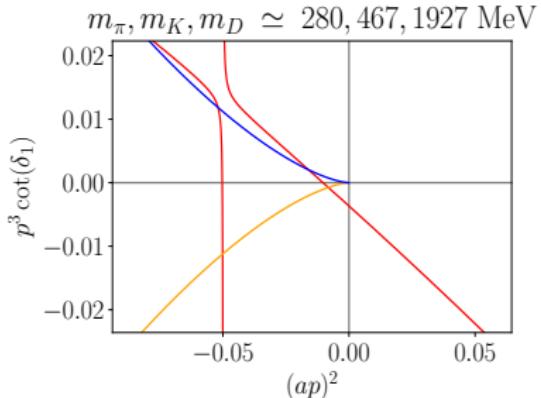
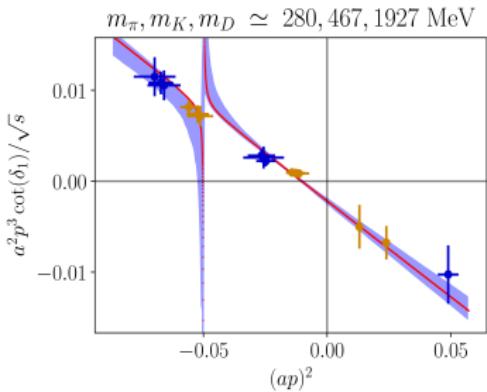
- Finite volume spectrum including all relevant two-meson operators
 $\mathcal{O} = \bar{Q}\Gamma Q$, $(\bar{Q}\Gamma_1 q)_1 (\bar{q}\Gamma_2 Q)_1$, $(\bar{Q}\Gamma_1 Q)_1 (\bar{q}\Gamma_2 q)_1$.
- Determination of scattering amplitudes:
Utilize “TwoHadronsInBox” toolbox. [Morningstar et al. 1707.05817](#)

Vector charmonium: finite volume spectrum



Piemonte *et al*, 1905.03506

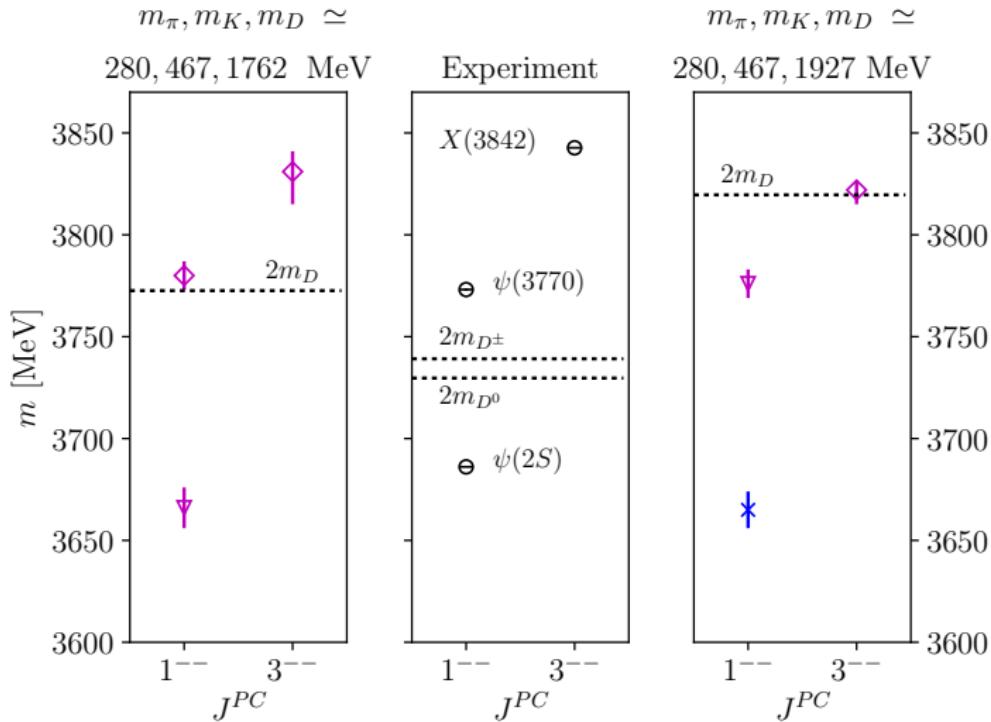
Elastic analysis: Vector charmonia



- 1^{--} channel in $\bar{D}D$ scattering in p -wave.
- Reaction matrix(K): $S = (1 + iK)(1 - iK)^{-1}$): $K_1^{-1} = \left(\frac{G_1^2}{m_1^2 - s} + \frac{G_2^2}{m_2^2 - s} \right)^{-1}$
- (Virtual) bound state constraint: $p^3 \cot \delta_1 = (-)(p^2) \sqrt{-p^2}$.
- Results presented for heavier than physical charm quark mass.

Piemonte *et al.*, 1905.03506

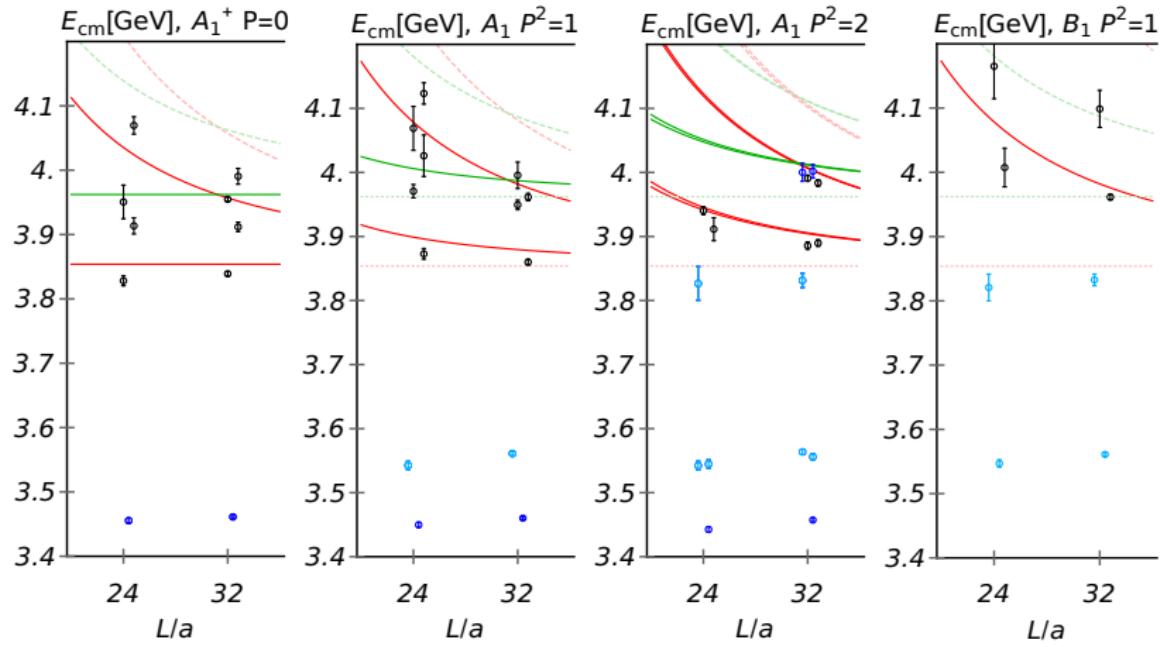
Spectrum summary: Vector charmonia



The coupling $g_{\psi(1D) \rightarrow \bar{D}D} = 18.9^{+0.8}_{-0.7}$ for light m_c : $g_{exp} = 18.7(9)$

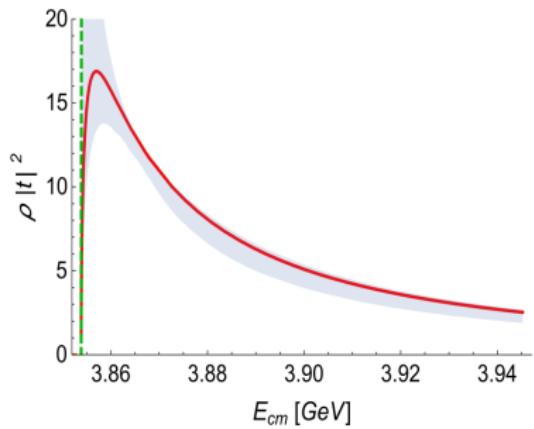
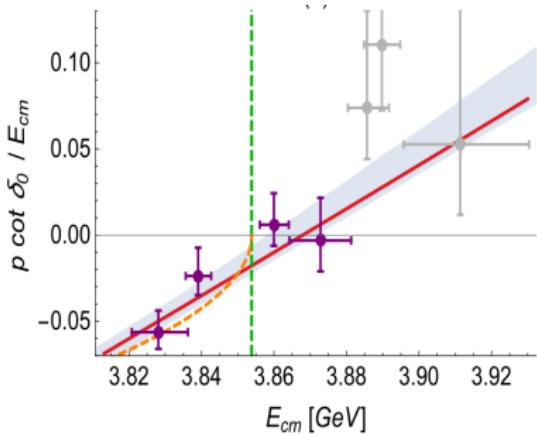
Piemonte et al, 1905.03506

Scalar charmonium: finite volume spectrum



Prelovsek *et al*, 2011.02542

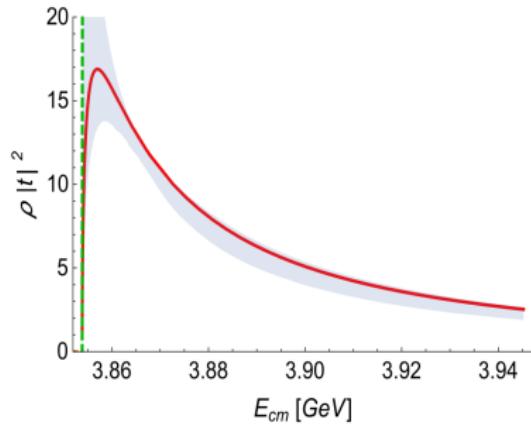
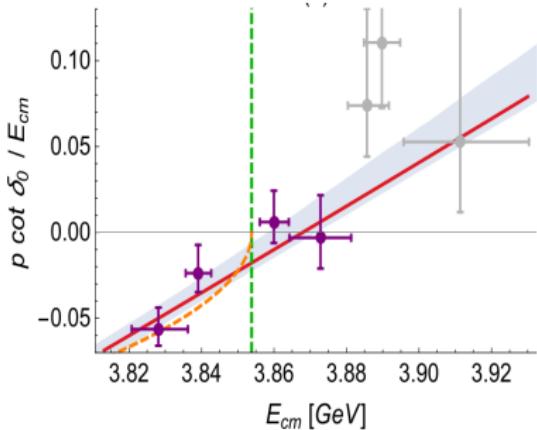
Scalar charmonia around the $D\bar{D}$ threshold



- 0^{++} channel in $D\bar{D}$ scattering in *s*-wave.
- Reaction matrix(K : $S = (1 + iK)(1 - iK)^{-1}$): $K_1^{-1}/\sqrt{s} = a + b s$
- Bound state constraint: $p \cot \delta_0 = -\sqrt{-p^2}$.
- A shallow bound state with B.E.: $m - 2m_D = -4.0^{+3.7}_{-5.0}$ MeV
- Results presented for heavier than physical charm quark mass.

Prelovsek *et al*, 2011.02542

Scalar charmonia around the $D\bar{D}$ threshold

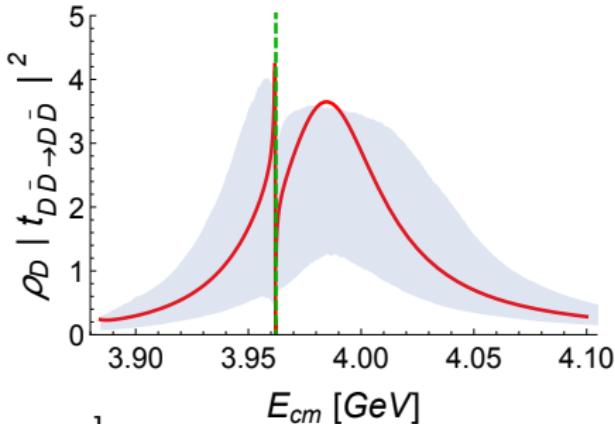
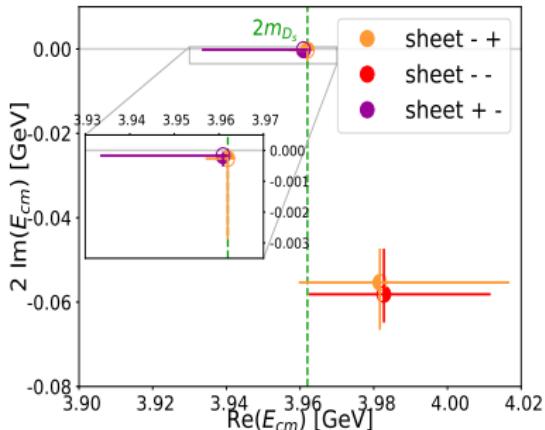


- Signal: An enhancement in the $D\bar{D}$ rate just above threshold.
 $N_{D\bar{D}} \propto \rho |t|^2$
- Physics in a simulation with physical quark masses is yet to be performed.
- Predictions from phenomenological models.
- Evidences in the experiments

[hep-ph/0612179](#), [1305.4487](#), [1605.09649](#)

[0708.3812](#), [0712.1758](#)

Scalar charmonia around the $D_s^+ D_s^-$ threshold



- Coupled channel $\bar{D}D - D_s^+ D_s^-$ scattering [s-wave].

$J/\psi - \omega$ and $\eta_c \eta$ are not included in the amplitude analysis.

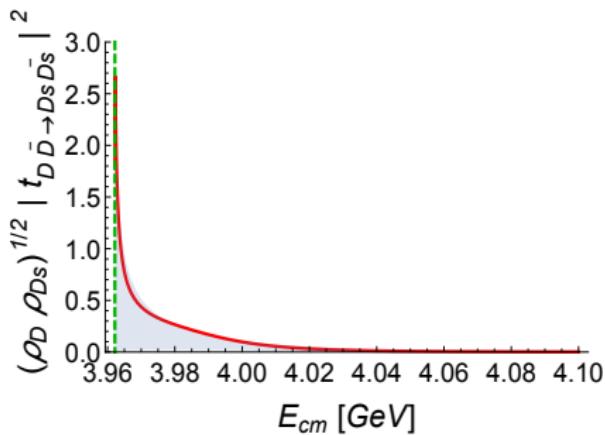
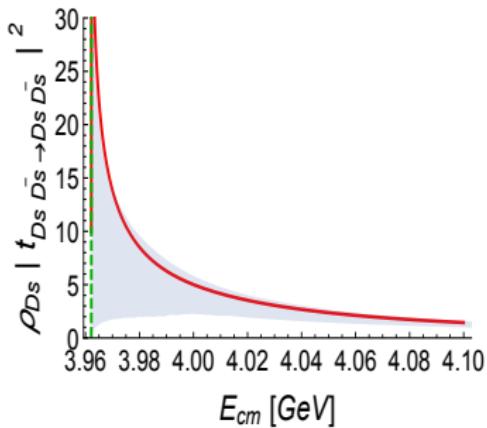
- Reaction matrix (K : $S = (1 + iK)(1 - iK)^{-1}$):

$$\frac{(\tilde{K}^{-1})^{I=0}}{\sqrt{s}} = \begin{pmatrix} a_{11} + b_{11}s & a_{12} \\ a_{12} & a_{22} + b_{22}s \end{pmatrix}$$

- The near threshold pole leads to a dip in $D\bar{D} \rightarrow D\bar{D}$ rate and an enhancement in $D_s^+ D_s^- \rightarrow D_s^+ D_s^-$ and $D\bar{D} \rightarrow D_s^+ D_s^-$ rates.

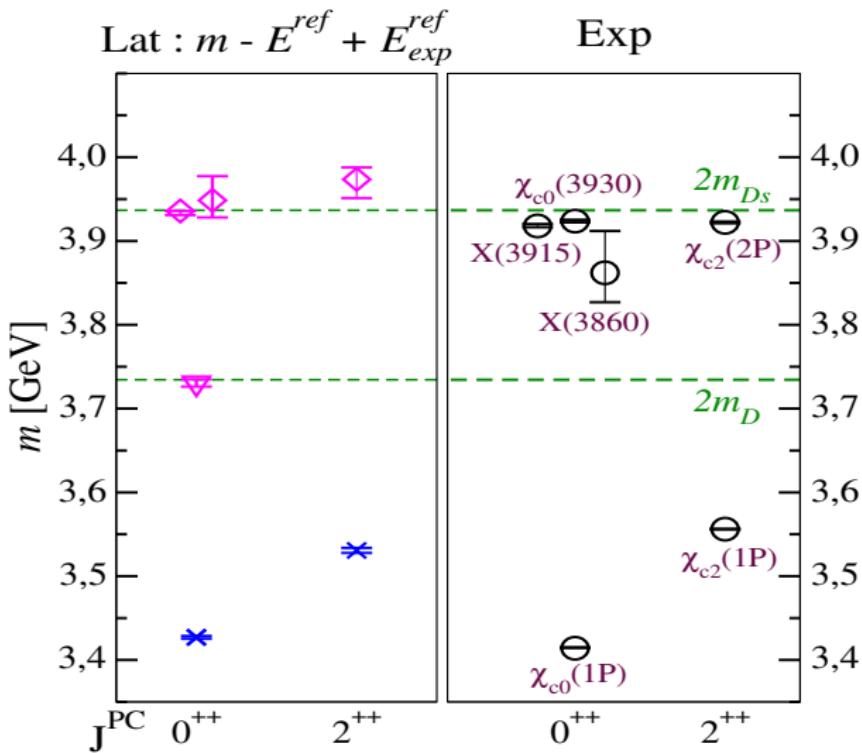
Prelovsek et al, 2011.02542

Scalar charmonia around the $D_s^+ D_s^-$ threshold



- The near threshold pole couples strongly (weakly) to $D_s^+ D_s^-$ ($D \bar{D}$). Possibly related to X(3915) and/or X(3930).
- Another pole in sheet -- with strong coupling to $D \bar{D}$. Responsible for the peak structure in $D \bar{D} \rightarrow D \bar{D}$ rate above the threshold.
- This pole could be related to the X(3860) observed by Belle.

Spectrum summary: 0^{++} charmonia



Results presented for the heavier than physical charm quark mass.

Prelovsek *et al*, 2011.02542

Remarks and future plans

* Lattice results for heavy baryons and more:

- Singly and doubly charmed baryons.
- Charmed-bottom hadrons.
- Doubly heavy tetraquarks.
- Heavy dibaryons.

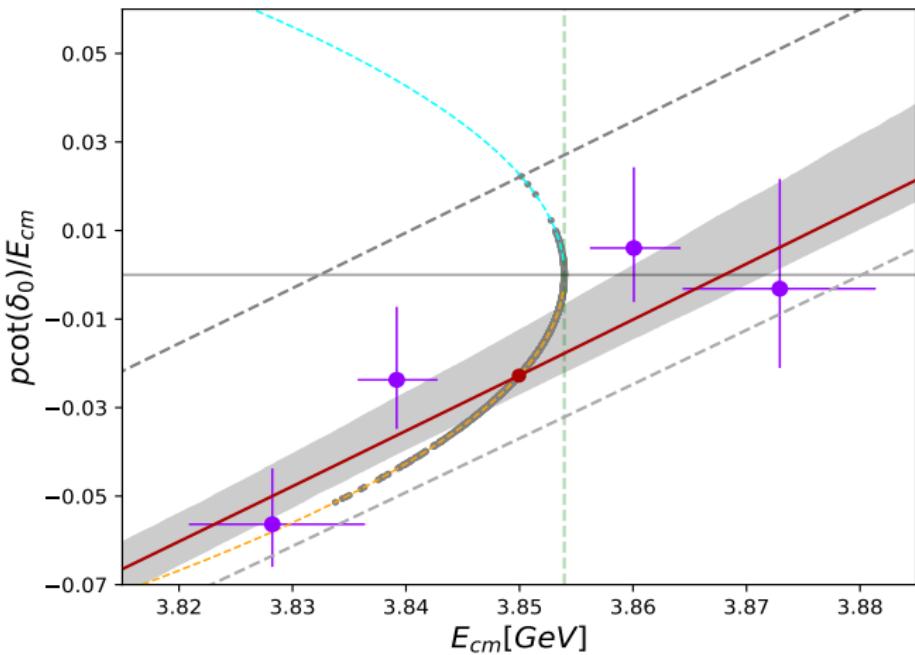
* Charmonium studies:

- Several lattice calculations assuming $\bar{c}c$ picture.
- Beyond the $\bar{c}c$ picture: Vector channel as a proof of concept.
- Beyond the $\bar{c}c$ picture: Scalar channel.
 - A shallow (virtual) bound state pole near $D\bar{D}$ threshold.
 - A pole near $D_s^+ D_s^-$ threshold leading to a dip in $D\bar{D}$ rate.
Possibly related to X(3915) and/or X(3930).
 - A resonance pole with strong coupling to $D\bar{D}$ channel.
Possibly related to X(3860).

Thank you

Back up slides

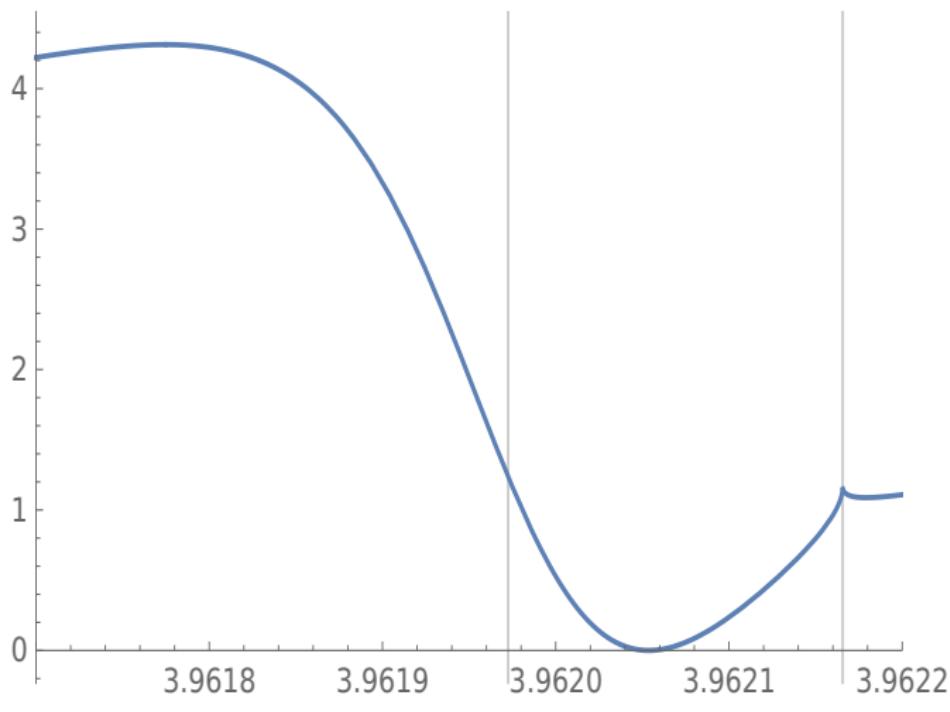
Scalar charmonia around the $D\bar{D}$ threshold



Pole distribution of shallow (virtual) bound state in $D\bar{D}$.

Prelovsek et al, 2011.02542

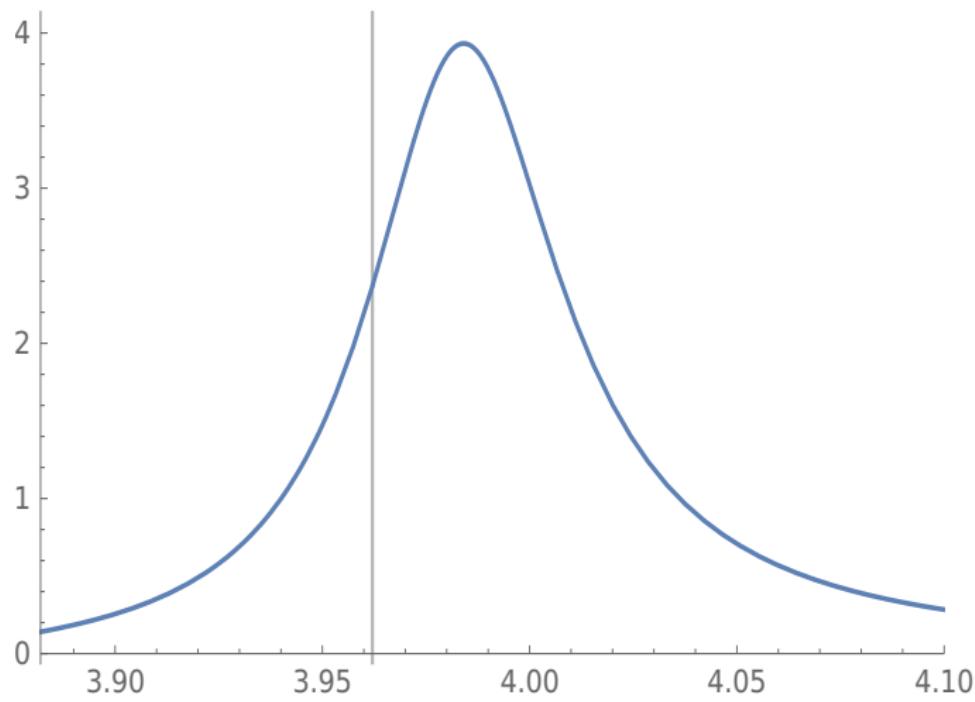
Dip in the $\rho|t_{D\bar{D} \rightarrow D\bar{D}}|^2$



Dip in the $D\bar{D} \rightarrow D\bar{D}$ rate.

Prelovsek et al, 2011.02542

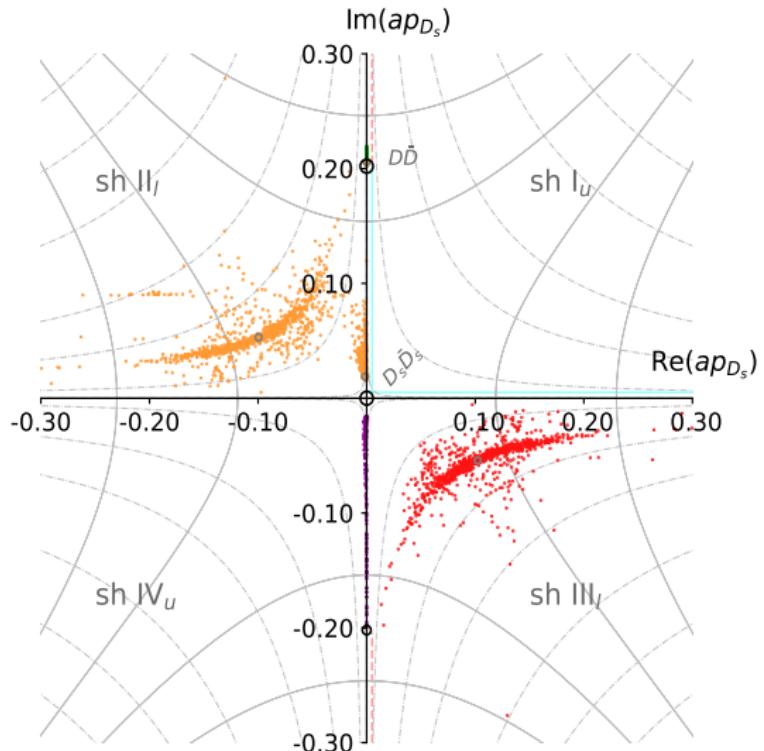
No dip in the $\rho|t_{D\bar{D} \rightarrow D\bar{D}}|^2$



No dip in the $D\bar{D} \rightarrow D\bar{D}$ rate, when $K_{12} = 0$.

Prelovsek et al, 2011.02542

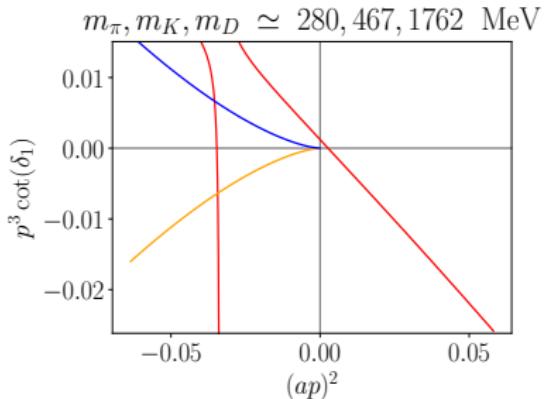
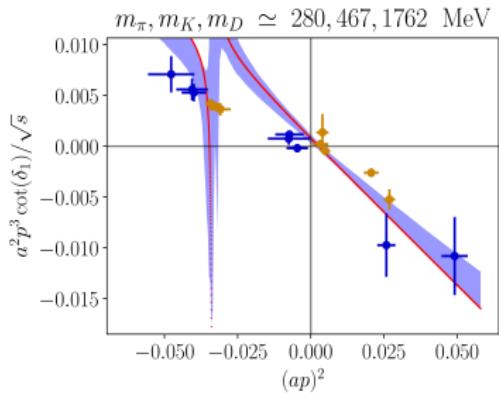
Scalar charmonia around the $D_s^+ D_s^-$ threshold



Pole distribution in $D_s^+ D_s^-$ complex momentum plane.

Prelovsek et al, 2011.02542

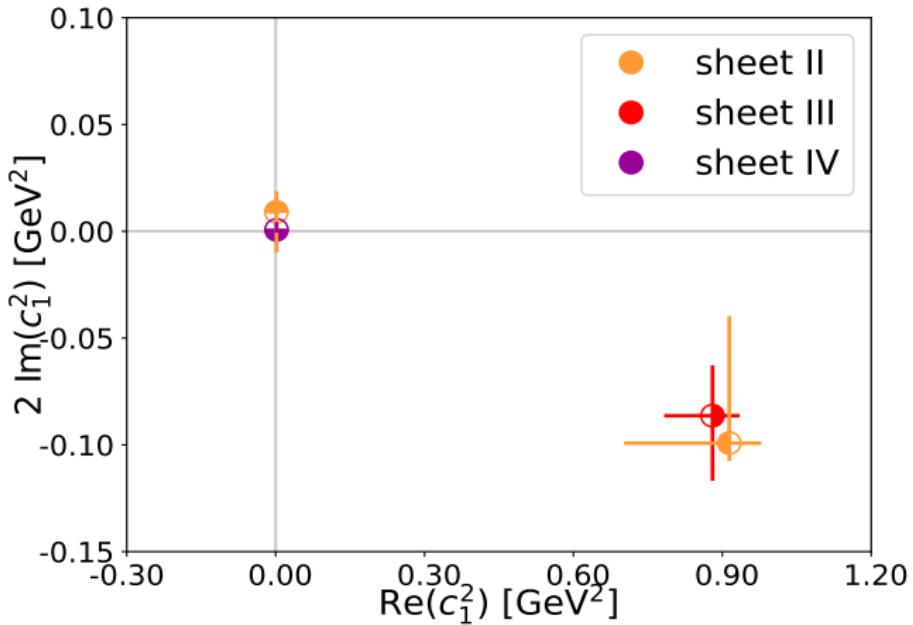
Elastic analysis: vector charmonia



- (Virtual) bound state constraint: $p^3 \cot\delta_I = (-)(p^2)\sqrt{-p^2}$
- Two bound states at heavier charm quark mass.
- A bound state and a resonance at lighter charm quark mass.
- An inevitable contamination $J^{PC} = 3^{--}$ excitation and $I = 3$ partial wave in the lattice spectra.
- Reaction matrix, $K = \begin{pmatrix} K_1 & 0 \\ 0 & K_3 \end{pmatrix}$, with $K_3 = \frac{G_3^2}{m_3^2 - s}$

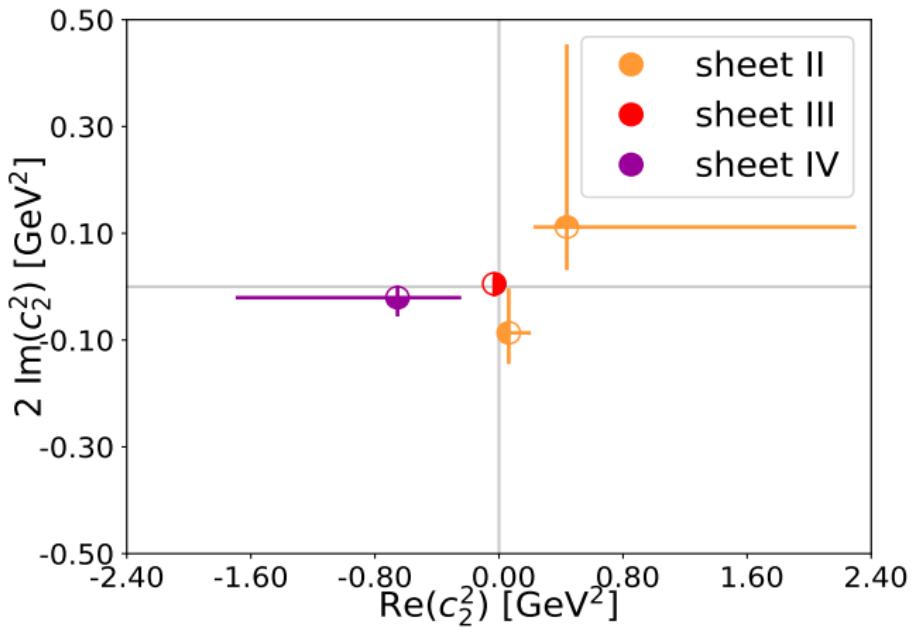
Piemonte *et al*, 1905.03506

Residues (c1): scalar charmonia



Prelovsek et al, 2011.02542

Residues (c2): scalar charmonia



Prelovsek et al, 2011.02542