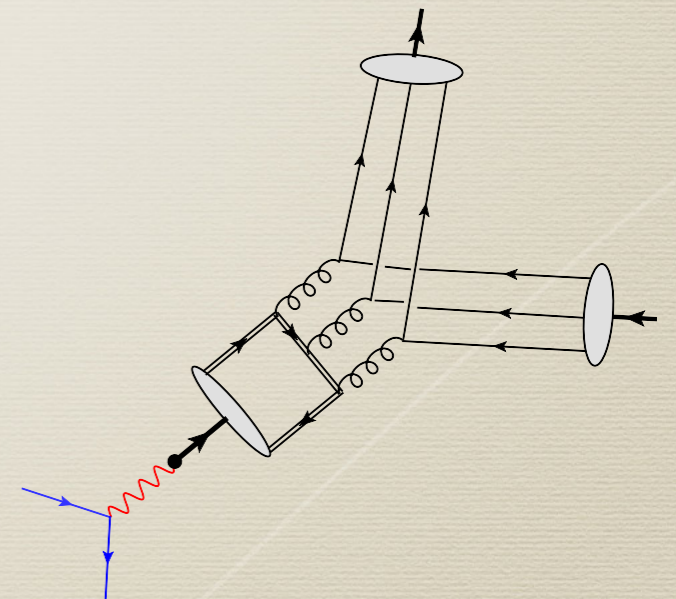


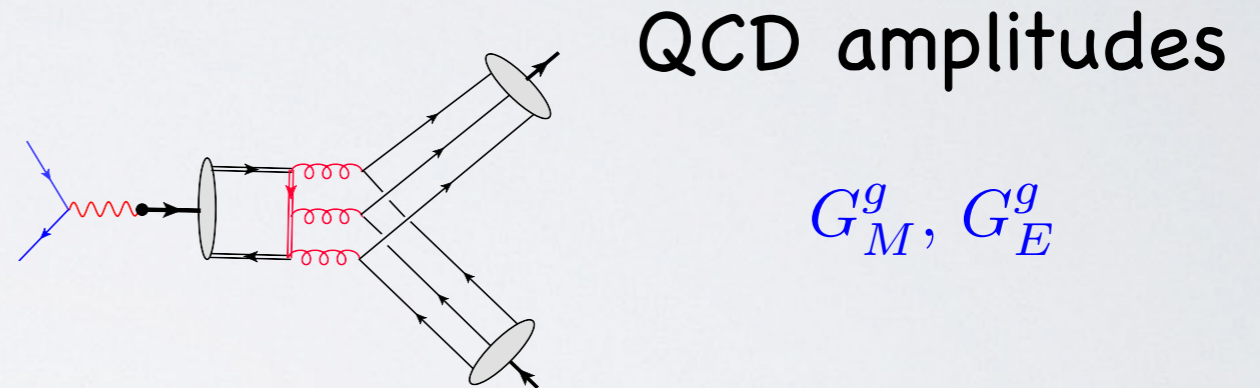
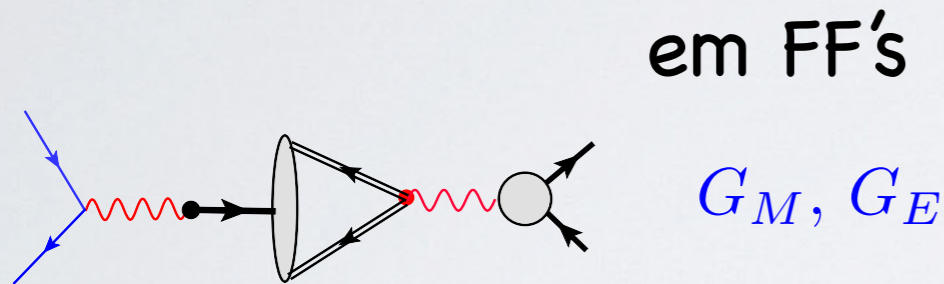
# A study of $J/\psi$ decays into baryon-antibaryon pairs

**Nikolay Kivel**



# $J/\psi$ baryonic decays

$$\text{Br}[J/\psi \rightarrow B\bar{B}] = \frac{M_\psi \beta}{12\pi\Gamma_{tot}} |G_M^g + G_M|^2 \left( 1 + \frac{2m_B^2}{M_\psi^2} \gamma_B^2 \right) \quad \gamma_B = \left| \frac{G_E^g + G_E}{G_M^g + G_M} \right|$$



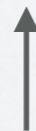
Hard kernel



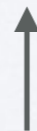
$$G_M^g \simeq R_{10}(0) \varphi_3(x_i) * H(x_i, y_i) * \varphi_3(y_i)$$

Brodsky, Lepage 1981

Chernyak, Zhitnitski 1984

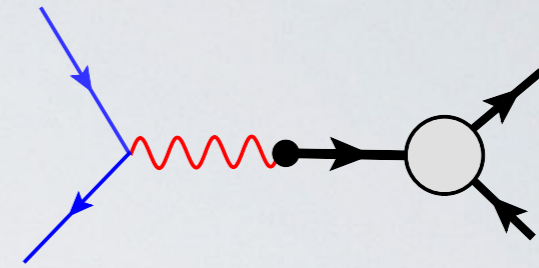


Baryon LCDA



# $J/\psi$ baryonic decays

$$\frac{dN}{d\cos\theta} = \mathcal{N}(1 + \alpha \cos^2 \theta)$$



$$\alpha_B = \frac{1 - 4m_B^2 \gamma_B^2 / M_\psi^2}{1 + 4m_B^2 \gamma_B^2 / M_\psi^2}$$

$$\gamma_B = \left| \frac{G_E^g + G_E}{G_M^g + G_M} \right|$$

$$m_Q \rightarrow \infty \quad \alpha = 1$$

Brodsky, Lepage 1981

$$\frac{4m_N^2}{M_\psi^2} \simeq 0.37$$

$$\frac{4m_N^2}{M_\gamma^2} \simeq 0.04$$

$$\gamma_N^2 = 1 \quad \alpha_N = \frac{1 - 4m_N^2 / M_\psi^2}{1 + 4m_N^2 / M_\psi^2} = 0.463$$

Claudson, Glashow, Wise 1982

# $J/\psi$ baryonic decays

## BESIII publications & PDG

| Baryon       | $\text{Br}[J/\psi \rightarrow B\bar{B}] \times 10^3$ | $\alpha_B$ | $\gamma_B = \frac{G_E^g + G_E}{G_M^g + G_M}$ | $Q_B = \frac{\text{Br}[\psi(2S) \rightarrow B\bar{B}]}{\text{Br}[J/\psi \rightarrow B\bar{B}]} \times 100$ |
|--------------|--|------------|--|--|
| $p$          | 2.121(29)  | 0.595(12)  | 0.823  | 13.86(3)   |
| $n$          | 2.09(16)   | 0.50(4)    | 0.943  | 14.64(14)  |
| $\Lambda$    | 1.89(9)  | 0.469(26)  | 0.834  | 20.43(11)  |
| $\Sigma^0$   | 1.172(32)  | -0.449(20) | 2.11   | 20.96(27)  |
| $\Sigma^\pm$ | 1.50(29)   | -0.510(20) | 2.27   | 7.22(48)   |
| $\Xi^\pm$    | 0.97(8)  | 0.58(4)    | 0.606  | 26.73(50)  |

asymptotic criteria

$$Q_B \stackrel{m_c \rightarrow \infty}{\approx} Q_l = \frac{\text{Br}[\psi(2S) \rightarrow e^+e^-]}{\text{Br}[J/\psi \rightarrow e^+e^-]} \times 100 = 13, 21$$

## Theoretical estimates

Largest amount of papers are dedicated to Br's and constrains of baryon DAs

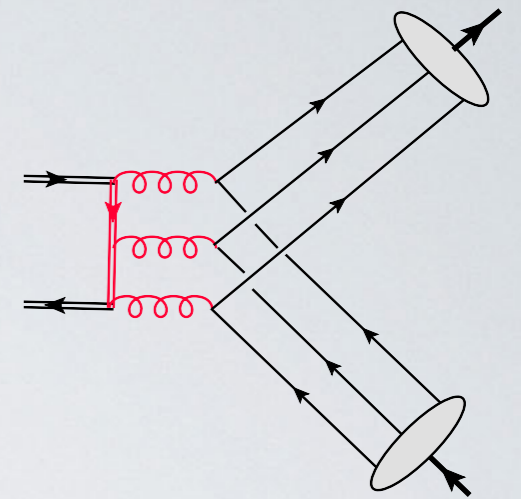
Carimalo, 1987  $\alpha_N = 0.70$  constituent quarks, non-relativistic nucleon WF

Murgia, Melis, 1995  $\alpha_N = 0.561 - 0.963$  constituent quark mass  $m_i = x_i m_N$   
in the LT factorisation formula

# $J/\Psi \rightarrow p\bar{p}$ decay

$A_{Q\bar{Q}}$  can be systematically computed within EFT framework

$$A_{Q\bar{Q}}[Q\bar{Q} \rightarrow 3g \rightarrow p\bar{p}] = \mathcal{A}^{(0)} \left(\frac{\Lambda^2}{m_c^2}\right)^4 + \mathcal{A}^{(1)} \left(\frac{\Lambda^2}{m_c^2}\right)^6 + \dots$$

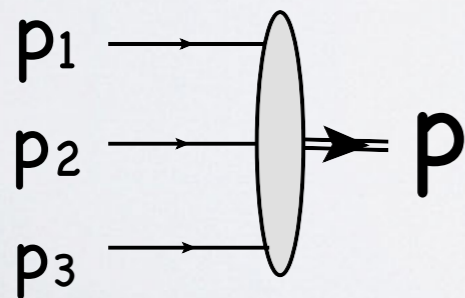


$$A_0 = \int Dx_i \varphi_3(x_i) \int Dy_i \varphi_3(y_i) T_H(x_i, y_i, m_c^2)$$

int. measure  $Dx_i = dx_1 dx_2 dx_3 \delta(x_1 + x_2 + x_3 - 1)$

## Long distance physics associated with the nucleon WF's

Distribution amplitude  $\varphi_3(x_i)$  describes how the long. momentum is shared between the constituents



$$\varphi_N(x_1, x_2, x_3) \sim \int_{k_{i\perp} \sim \Lambda} dk_{i\perp} \Psi_P(x_1, x_2, x_3, k_{i\perp})$$

$$p_i = x_i p + p_{\perp i} \quad p_i^2 \sim \Lambda^2 \quad p_{\perp i} \sim \Lambda \quad (p_i)_0 \sim (p_i)_3 \sim m_c$$

$J/\Psi \rightarrow p\bar{p}$  decay : challenges in the calculation  $G_E$

A systematic description of  $G_E$  involves higher twist nucleon DAs

$$G_E^g \simeq R_{10} \varphi_3(x_i) * \alpha_s^3 H(x_i, y_i) * \varphi_4(y_i)$$

Schematically:

twist-3

$$\langle 0 | u(a_1 z) u(a_2 z) d(a_3 z) | p \rangle_{z^2=0} \xrightarrow{\text{FT}} \varphi_3(x_i) \quad 3 \text{ quarks with } L_q = 0$$

twist-4

$$\langle 0 | u(a_1 z) [D_\perp u(a_2 z)] d(a_3 z) | p \rangle_{z^2=0} \xrightarrow{\text{FT}} \varphi_4(x_i) \quad 3 \text{ quarks with } L_q=1$$

$$\langle 0 | u(a_1 z) u(a_2 z) ] d(a_3 z) A_\perp(a_4 z) | p \rangle_{z^2=0} \xrightarrow{\text{FT}} \varphi_4(x_i) \quad 3 \text{ quarks \& gluon}$$

## Baryon LCDAs $B = N, \Lambda, \Sigma, \Xi$

|         |                      |                     |  |
|---------|----------------------|---------------------|--|
|         | chiral<br>odd        | chiral<br>even      | Braun et al, '00, '08,<br>Manashov, Anikin '13<br>Anikin '15<br>Shäfer, Wein '15 |
| twist 3 | $\Phi_{3\pm}^B(x_i)$ | $\Pi_3^B(x_i)$      |  |
| twist 4 | $\Phi_{4\pm}^B(x_i)$ | $\Xi_{4\pm}^B(x_i)$ | $\Pi_4^B(x_i)$ $\Upsilon_4^B(x_i)$   |

## WW decomposition:

$$\Phi_{4\pm}^B = \Phi_{4\pm}^{B,WW} + \bar{\Phi}_{4\pm}^B \quad \Pi_4^B = \Pi_4^{B,WW} + \bar{\Pi}_4^B$$

models:  
(examples)

$$\phi_{3+}^B = f_B x_1 x_2 x_3 (1 + \phi_{11}^B (x_1 - 2x_2 + x_3) + \dots)$$

$$\bar{\Phi}_{4+}^B(x_i) = \lambda_1^B 24x_1x_2 \left( -\eta_{11}^B (2x_1 - x_2 - 2x_3) \right)$$

$$\bar{\Phi}_{4-}^B(x_i) = \lambda_1^B 24x_1x_2 \left( 1 + \eta_{10}^B (4 - 10x_2) \right)$$

quark-gluon operators contribute starting from  $\eta_{2i}^B$  and will be neglected

# $J/\psi$ baryonic decays: hard kernels N.Kivel, 2019/21 (updated in Arxiv)

**Result** 
$$G_E^g = \frac{f_\psi}{m_c^2} \frac{f_B^2}{m_c^4} \frac{10\pi^3}{81} \int Dx_i \varphi_3^B(x_i) \int Dy_i \varphi_4^B(y_i) \alpha_s^3 H_B(x_i, y_j)$$

$m_c \rightarrow \infty \quad \gamma_B = G_E^g / G_M^g \sim \mathcal{O}(1) \quad \text{multiplicative factors cancel}$

**NRQCD m.e.**  $\langle 0 | \chi_\omega^\dagger(0) \gamma^\mu \psi_\omega(0) | P \rangle = \epsilon_\psi^\mu f_\psi. \quad f_\psi = \sqrt{2M_{J/\psi}} \sqrt{\frac{3}{2\pi}} R_{10}(0)$

**Nucleon m.e.**  $\langle 0 | [u(0) C \not{z} u(0)] \gamma_5 \not{z} d(0) | p_N \rangle = f_N(pz) \not{z} N(p_N) \quad z^2 = 0$

**Comments to the hard kernel calculations:**  $\text{Im } G_E = 0$  absence of phys. cuts

Twist-4 projection of the m.e. includes the derivatives with respect to quark transverse momenta, which makes the calc to be more involved comparing to  $G_M$

Individual diagrams have the IR end-point singularities (soft gluon limit), which cancel in the sum of all diagrams (color neutrality). Hence collinear factorisation is not violated.

4-dim integrals over the mom. fractions can be easily computed in `mathematica` using the standard integration package



$J/\Psi \rightarrow p\bar{p}$  **decay** non-perturbative input

$$f_\psi = \sqrt{2M_{J/\psi}} \sqrt{\frac{3}{2\pi}} R_{10}(0)$$

$$\Gamma[J/\psi \rightarrow e^+e^-] = \frac{16}{9} \frac{\alpha_{em}^2}{M_\psi^2} |R_{10}(0)|^2 \left(1 - \frac{16}{3} \frac{\alpha_s}{\pi}\right)$$

$$|R_{10}(0)|^2 \simeq 0.81 \text{GeV}^3$$

$$m_c = 1.5 \text{ GeV}^2,$$

Eichten, Quigg 1995 (Buchmüller-Tye potential)

Renormalisation scale:

$$\mu^2 = 2m_c^2 - 1.5 \text{ GeV}^2 \quad \alpha_s(\mu^2) = 0.30-0.35$$

These parameters are important for the description of the branching ratios and remain the same for all baryons

$J/\psi \rightarrow N\bar{N}$  **decay** non-perturbative input

Nucleon DAs are fixed from LCSR analysis of nucleon FF's

Anikin, Braun, Offen (NLO LCSR), 2013

overlap with lattice calc Bali et al (RQCD), 2019

|       | twist-3              | $\mu^2 = 4 \text{ GeV}^2$ |                |                |                |                | twist-4         |             |             |
|-------|----------------------|---------------------------|----------------|----------------|----------------|----------------|-----------------|-------------|-------------|
| model | $f_N, \text{GeV}^2$  | $\varphi_{10}$            | $\varphi_{11}$ | $\varphi_{20}$ | $\varphi_{21}$ | $\varphi_{22}$ | $\lambda_1/f_N$ | $\eta_{10}$ | $\eta_{11}$ |
| ABO   | $4.8 \times 10^{-3}$ | 0.047                     | 0.047          | 0.069          | -0.024         | 0.15           | -6.27           | -0.037      | 0.13        |

$$\varphi_3(x_i) \simeq 120x_1x_2x_3 (1 + \varphi_{10}\mathcal{P}_{10}(x_i) + \varphi_{11}\mathcal{P}_{11}(x_i) + \varphi_{20}\mathcal{P}_{20}(x_i) + \varphi_{21}\mathcal{P}_{21}(x_i) + \varphi_{22}\mathcal{P}_{22}(x_i))$$

$$\Phi_{4\pm}^N \quad \Pi_4^N \quad \left| \quad \begin{aligned} \bar{\Phi}_4(x_1, x_2, x_3) &= 24x_1x_2 (1 + \eta_{10}\mathcal{R}_{10}(x_3, x_1, x_2) - \eta_{11}\mathcal{R}_{11}(x_3, x_1, x_2)) \\ \bar{\Psi}_4(x_1, x_2, x_3) &= 24x_1x_3 (1 + \eta_{10}\mathcal{R}_{10}(x_2, x_3, x_1) + \eta_{11}\mathcal{R}_{11}(x_2, x_3, x_1)) \end{aligned}$$

$\Upsilon_4^N \quad \Xi_{4\pm}^N$  do not contribute at this order

## $J/\psi \rightarrow N\bar{N}$ decay


$$\text{Br}[J/\psi \rightarrow B\bar{B}] = \frac{M_\psi \beta}{12\pi\Gamma_{tot}} |G_M^g + G_M|^2 \left( 1 + \frac{2m_B^2}{M_\psi^2} \gamma_B^2 \right) \quad \gamma_B = \left| \frac{G_E^g + G_E}{G_M^g + G_M} \right|$$


exp. data

|   |                       |
|---|-----------------------|
| $10^3 \text{Br}[J/\psi \rightarrow p\bar{p}] = 2.121(29)$ | $\gamma_p = 0.823(9)$ |
| $10^3 \text{Br}[J/\psi \rightarrow n\bar{n}] = 2.09(16)$  | $\gamma_n = 0.94(10)$ |

$$G_E = G_M = 0 \quad 10^3 \text{Br}[J/\psi \rightarrow N\bar{N}] = 0.47-1.43 \quad \gamma_N^g = 0.66-0.68$$

$\mu^2 = 2m_c^2 - 1.5 \text{ GeV}^2$      small scale gives a better description for Br

  $\gamma_N$  is sufficiently stable (as expected) and quite sensitive to the value of the twist-4 moment  $\eta_{11}$

 The numerical effect from the interference with em FF's can also provide a sizable impact

$J/\psi \rightarrow B\bar{B}$  decays

Anikin '15  
Shäfer, Wein '15

|            |    |             |                          |                        |                    |                       |                     |                     |                         |                      |
|------------|----|-------------|--------------------------|------------------------|--------------------|-----------------------|---------------------|---------------------|-------------------------|----------------------|
| $\Lambda$  | DA | twist-3     | $\varphi_{3\pm}^\Lambda$ | $\Pi_3^\Lambda$        | twist-4            | $\Phi_{4\pm}^\Lambda$ | $\Pi_4^\Lambda$     |                     |                         |                      |
| parameters |    | $f_\Lambda$ | $\varphi_{10}^\Lambda$   | $\varphi_{11}^\Lambda$ | $\pi_{10}^\Lambda$ | $\lambda_1^\Lambda$   | $\eta_{10}^\Lambda$ | $\eta_{11}^\Lambda$ | $\lambda_\perp^\Lambda$ | $\zeta_{10}^\Lambda$ |

|                   |    |         |                    |                  |             |                    |               |               |               |                |
|-------------------|----|---------|--------------------|------------------|-------------|--------------------|---------------|---------------|---------------|----------------|
| $B = \Sigma, \Xi$ | DA | twist-3 | $\varphi_{3\pm}^B$ | $\Pi_3^B$        | twist-4     | $\Phi_{4\pm}^B$    | $\Pi_4^B$     |               |               |                |
| parameters        |    | $f_B$   | $\varphi_{10}^B$   | $\varphi_{11}^B$ | $f_\perp^B$ | $\pi_{11}^\Lambda$ | $\lambda_1^B$ | $\eta_{10}^B$ | $\eta_{11}^B$ | $\zeta_{11}^B$ |

numerical estimates are from lattice calc Bali et al (RQCD), 2019

SU(3) estimates

$$\lambda_1^\Lambda \eta_{10}^\Lambda \simeq \lambda_1^\Lambda \zeta_{10}^\Lambda \simeq \lambda_1^N \eta_{10}^N \quad \lambda_1^B \eta_{11}^B \simeq \lambda_1^N \eta_{11}^N$$

$B = \Sigma, \Xi$

$$\lambda_1^B \eta_{11}^B \simeq \lambda_1^B \zeta_{11}^B \simeq \lambda_1^N \eta_{11}^N \quad \lambda_1^B \eta_{10}^B \simeq \lambda_1^N \eta_{10}^N$$

$J/\psi \rightarrow B\bar{B}$  decays: results

$$G_E = G_M = 0$$

N.Kivel, in preparation

$$\text{Br}[J/\psi \rightarrow B\bar{B}] = \frac{M_\psi \beta}{12\pi\Gamma_{tot}} |G_M^g + G_M|^2 \left( 1 + \frac{2m_B^2}{M_\psi^2} \gamma_B^2 \right) \quad \gamma_B = \left| \frac{G_E^g + G_E}{G_M^g + G_M} \right|$$

|              | $\text{Br} \times 10^3, \text{exp}$ | $\mu^2 = 2m_c^2 - 1.5$<br>$\text{Br} \times 10^3, \text{th}$ | $\gamma_B, \text{exp}$ | $\gamma_B^g, \text{th}$ | $\frac{2m_B^2}{M_\psi^2}  \gamma_B ^2$ |
|--------------|-------------------------------------|--|------------------------|-------------------------|--|
| $p$          | 2.12                                |  | 0.82                   |                         |  |
|              |                                     | 0.47-1.43  |                        | 0.66-0.68               | 0.13                                   |
| $n$          | 2.09                                |  | 0.94                   |                         |  |
|              |                                     | 0.47-1.43  |                        | 0.66-0.68               | 0.13                                   |
| $\Lambda$    | 1.94                                |  | 0.83                   |                         |  |
|              |                                     | 0.27-0.81  |                        | 0.81-0.84               | 0.18                                   |
| $\Sigma^0$   | 1.16                                |  | 2.10                   |                         |  |
|              |                                     | 0.51-1.42  |                        | (0.81-0.84)*            | 1.53!                                  |
| $\Sigma^\pm$ | 1.50                                |  | 2.27                   |                         |  |
|              |                                     | 0.51-1.42  |                        | 1.30-1.36               | 1.31!                                  |
| $\Xi^\pm$    | 1.04                                |  | 0.61                   |                         |  |
|              |                                     | 0.52-1.48  |                        | 0.51-0.53               | 0.22                                   |

👉  $G_E$  &  $G_M$  are important for a better description Br and the ratio  $\gamma_B$

# Conclusions

Both decay amplitudes  $G_E$  &  $G_M$ , associated with the  $3g$  annihilation, are computed within the QCD EFT framework.

The existing models for baryon DAs provide reliable description of Br's for the relatively low norm. scale only

The interference of the QCD amplitudes and the e.m. baryon FF's are important! However includes unknown relative phases and e.m.  $|G_E|$  (in preparation)

The numerical ratios of these  $3g$ -amplitudes are in agreement with the exp. data within 10-30% accuracy, except for the  $\Sigma$ -channel.

A description of the  $\Sigma$ -channels requires a much stronger SU(3) violation, which can only give a very large ratio  $|G_E/G_M| \approx 2$ . Dynamical origin of this effect is not clear, perhaps a final state interaction?

The power corrections of order  $\Lambda^2/m_c^2$  to  $G_M$  are also computed (higher twist  $3q$  DAs). Preliminary: they give about 9% effect for  $N/\Lambda$ , which is not large. (in progress)

*Thanks!*