



IFSC UNIVERSIDADE
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Limits on Lorentz Invariance Violation from ultra high energy astrophysics

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28-30 mayo 2018
ICN-UNAM
México

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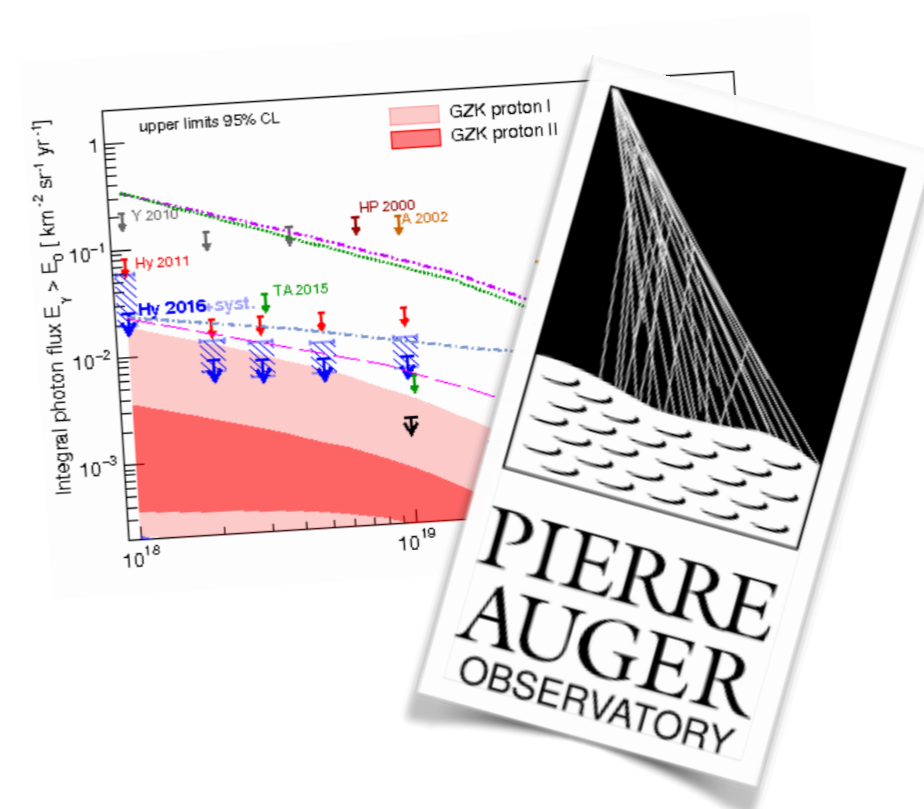
I. Lorentz invariance violation (LIV)

II. LIV + gamma-rays

III. Optical Depth + LIV

IV. GZK photon flux + LIV

V. LIV limits



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I. Lorentz invariance violation (LIV)

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Fundamental Forces of Nature

Strong

Electromagnetism

Weak

Gravity

Standard Model (SM)



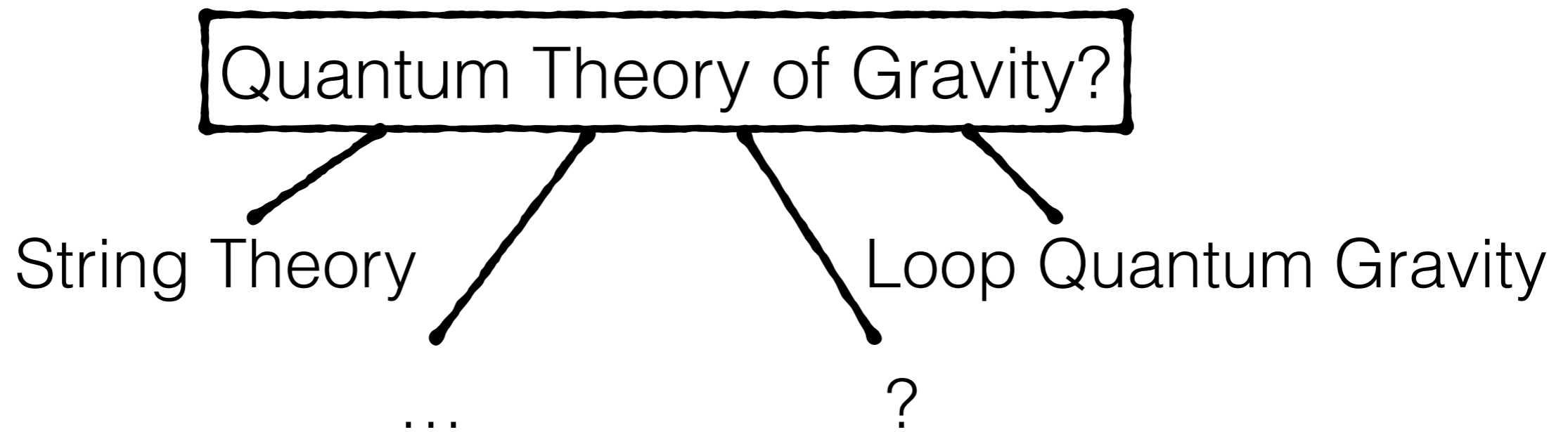
Quantum Theory

General Relativity (GR)



Geometrical Theory

- SM & GR: the best theories describing the 4-fundamental Forces.
- No conflict with predictions from either of them.
- **They are fundamentally different.**



New Physics involves new features, such as:

- Higher Dimensions of s-t
- Brane World scenarios
- Noncommutative geometries
- ...
- The law of relativity might not hold exactly at all energy scales \longrightarrow Lorentz Invariance Violation (LIV)

?

...LI may not be an exact symmetry of Nature



...VHE-UHE

Generic LIV dispersion relation

$$E^2 - p^2 \pm \epsilon A^2 = m^2,$$

$$E \gg m,$$

$$A = \{E, p\}$$

$$\epsilon \rightarrow \epsilon(A)$$

A general modification to the dispersion relation would rather involve a general function of energy and momentum

$$\epsilon(A)A^2 = \epsilon(0)A^2 + \epsilon'(0)A^{(2+1)} + \frac{\epsilon''(0)}{2!}A^{(2+2)} + \frac{\epsilon'''(0)}{3!}A^{(2+3)} + \dots$$

The dispersion relation:

$$E^2 - p^2 \pm \delta_n A^{n+2} = m^2, \quad \delta_n \stackrel{n \geq 1}{=} \epsilon^{(n)} / M^n = 1 / (E_{LIV}^{(n)})^n$$

it is not necessarily bound to a particular LIV-model, which allows to generalize to some point the search of LIV-signatures.

LIV negligible at the lower standard energies

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n=2

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$$\gamma_{VHE} \gamma_{BKG} \rightarrow e^+ e^-$$

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V. LIV limits

Pair Production

$$\gamma_{VHE} \gamma_{BKG} \rightarrow e^+ e^-$$

$$\Lambda_{\gamma,n} x_{\gamma}^{n+2} + x_{\gamma} - 1 = 0$$

$$x_{\gamma} = \frac{E_{\gamma}}{E_{\gamma}^{LI}}, \quad \Lambda_{\gamma,n} = \frac{E_{\gamma}^{LI(n+1)}}{4\epsilon} \delta_{\gamma,n}$$

$$\Lambda_n < 0$$

Threshold-shifts

$$\Lambda_n = 0$$

LI scenario

$$\Lambda_n > 0$$

+2nd Threshold

The threshold equation

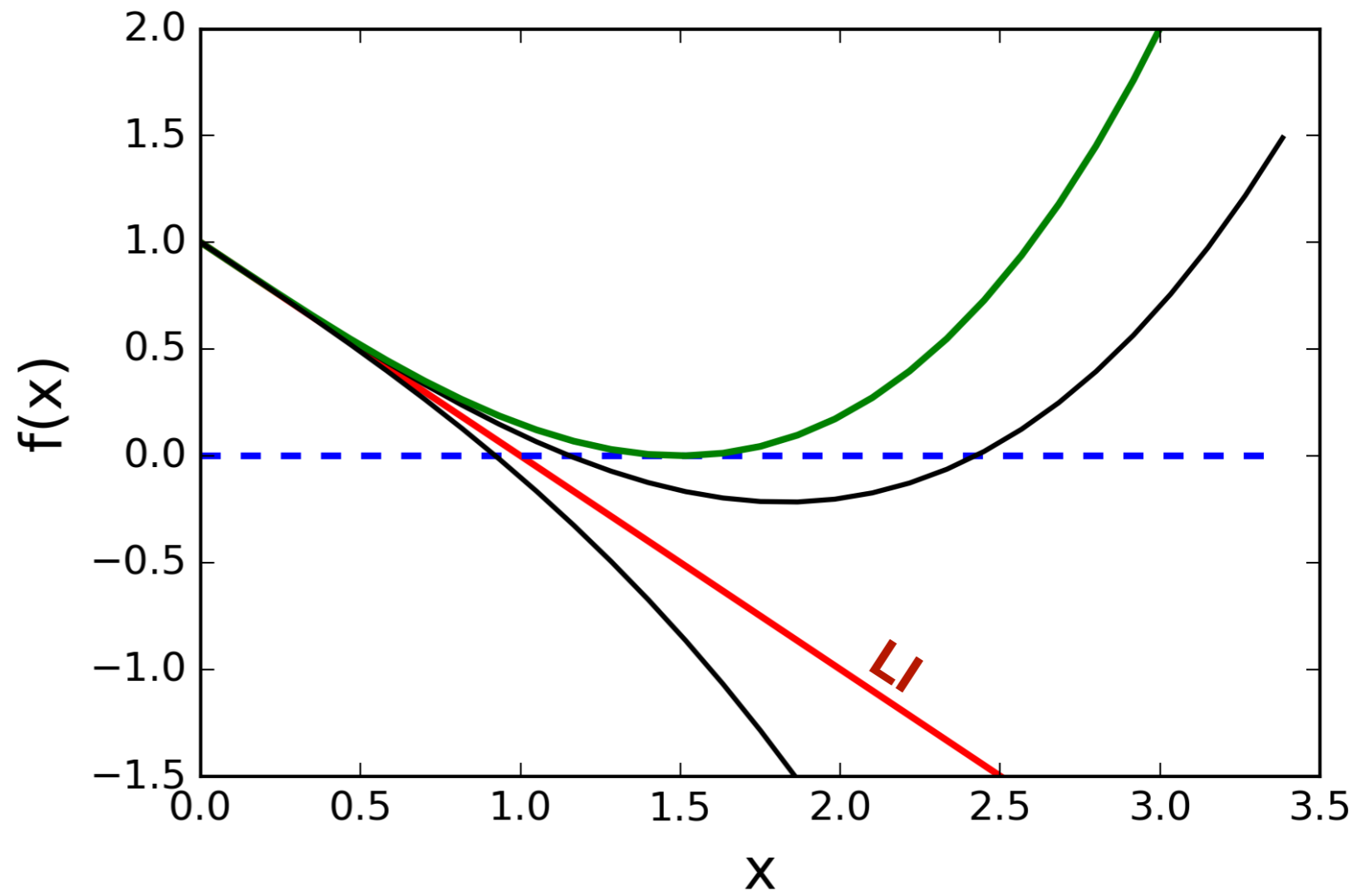
$$\delta_{\gamma,n} E_{\gamma}^{n+2} + 4E_{\gamma}\epsilon - m_e^2 \frac{1}{K(1-K)} = 0$$

Critical point

$$\delta_{\gamma,n}^{lim} = -4 \frac{\epsilon}{E_{\gamma}^{LI(n+1)}} \frac{(n+1)^{n+1}}{(n+2)^{n+2}}$$

Background:

$$\epsilon_{th}^{LIV} = \frac{m_e^2}{4E_{\gamma}K(1-K)} - \frac{\delta_{\gamma,n}E_{\gamma}^{n+1}}{4}$$



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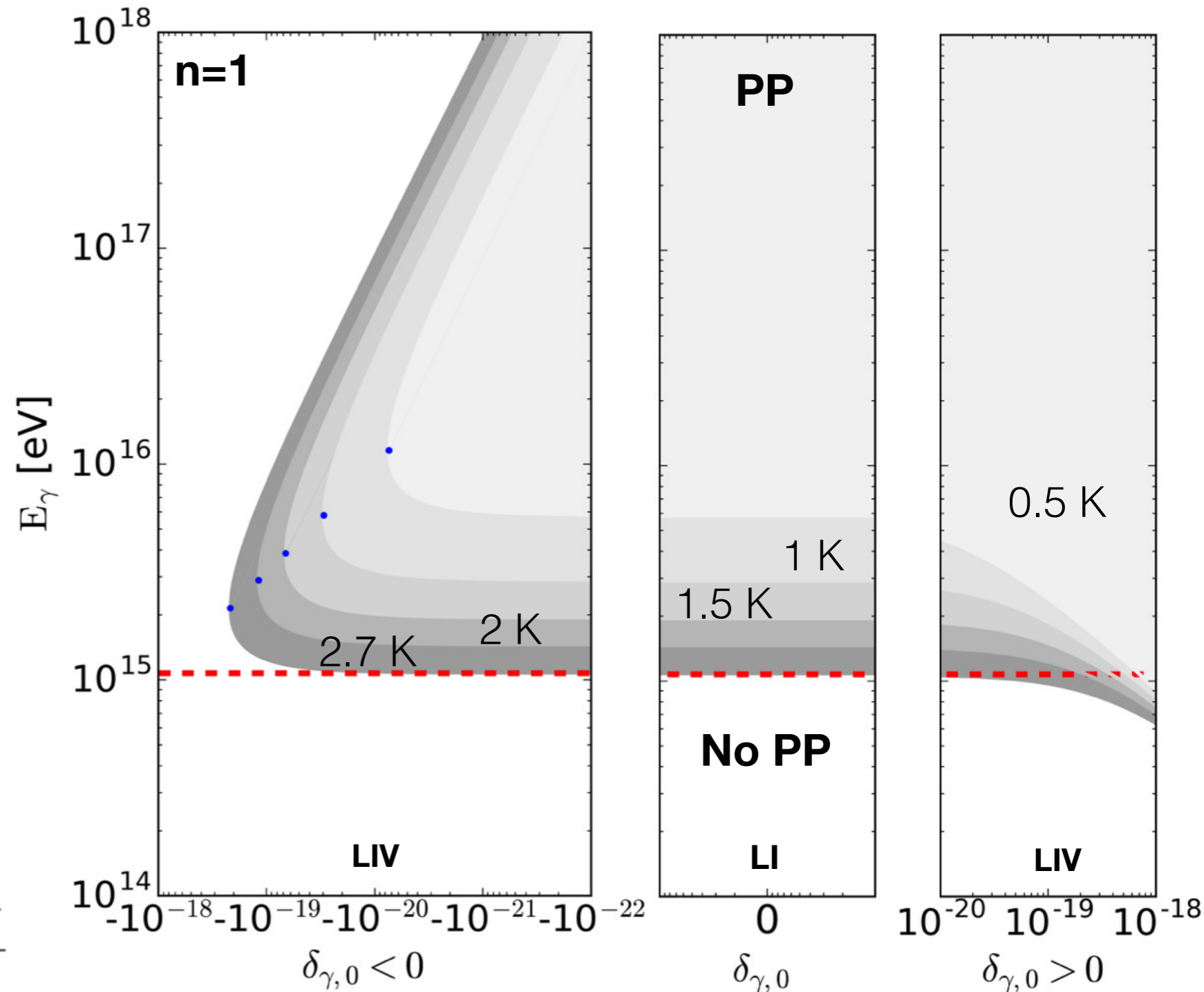
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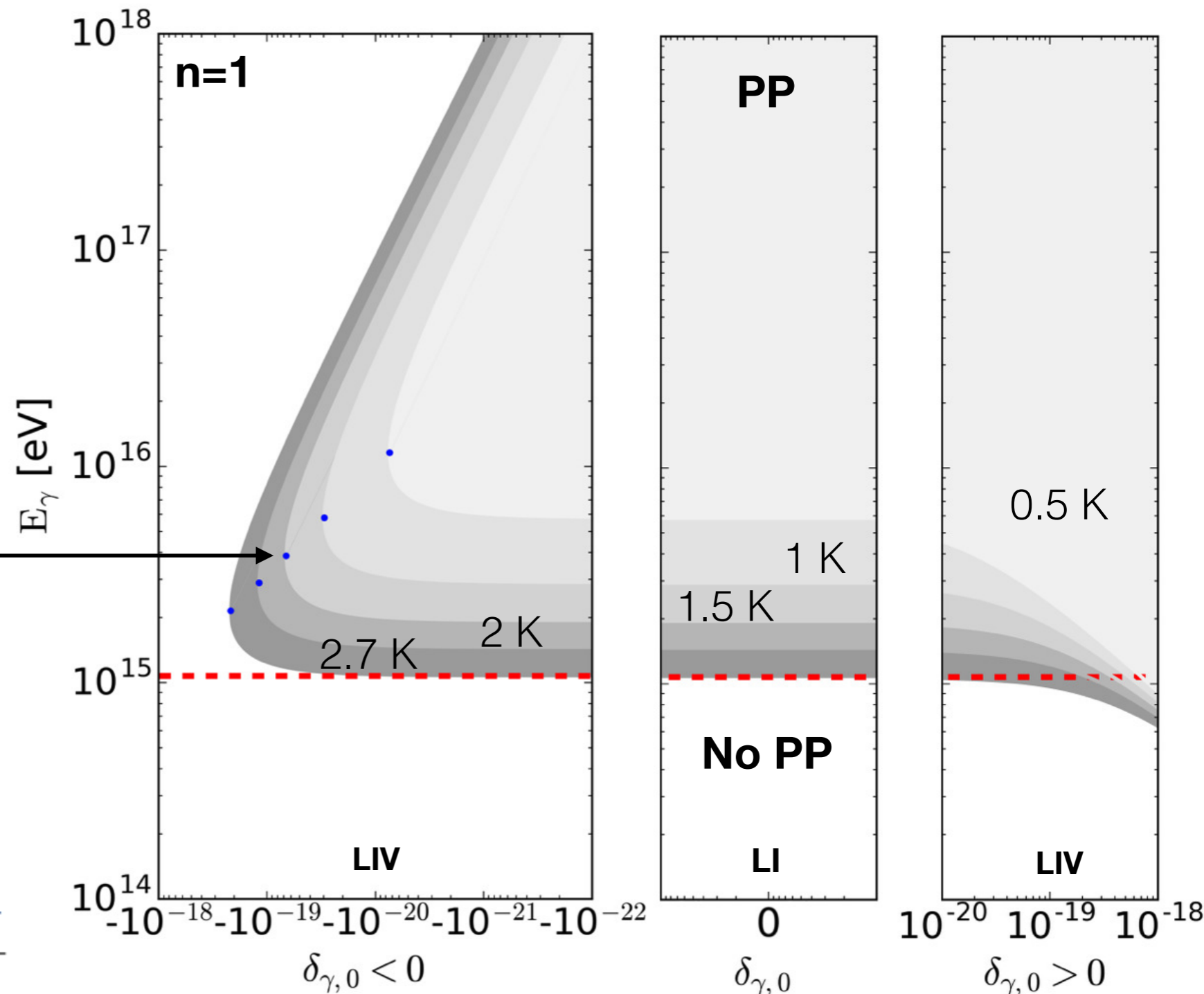
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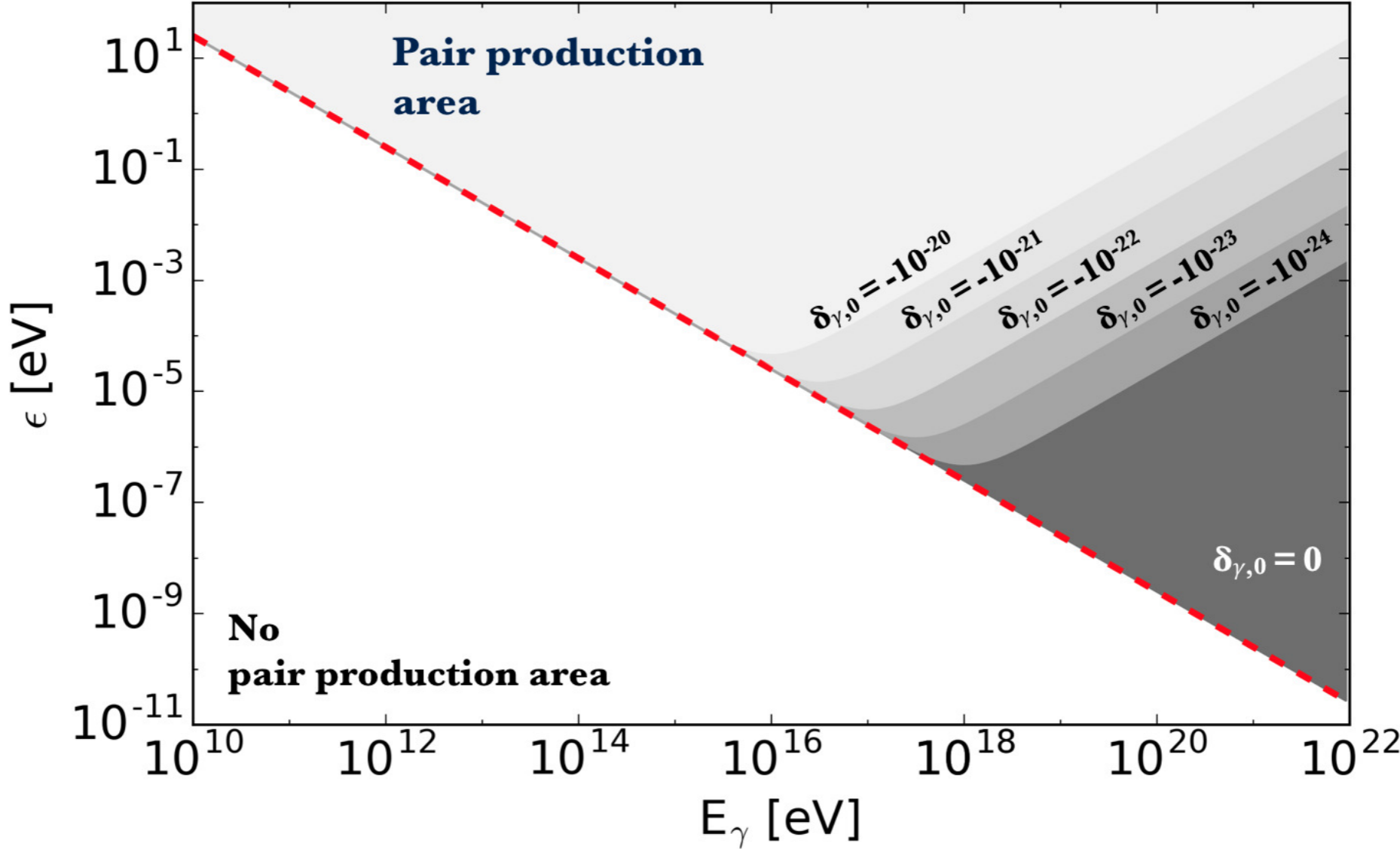
$$\epsilon_{th}^{LIV} = \frac{m_e^2}{4E_{\gamma}K(1-K)} - \frac{\delta_{\gamma,n}E_{\gamma}^{n+1}}{4}$$



Pair Production

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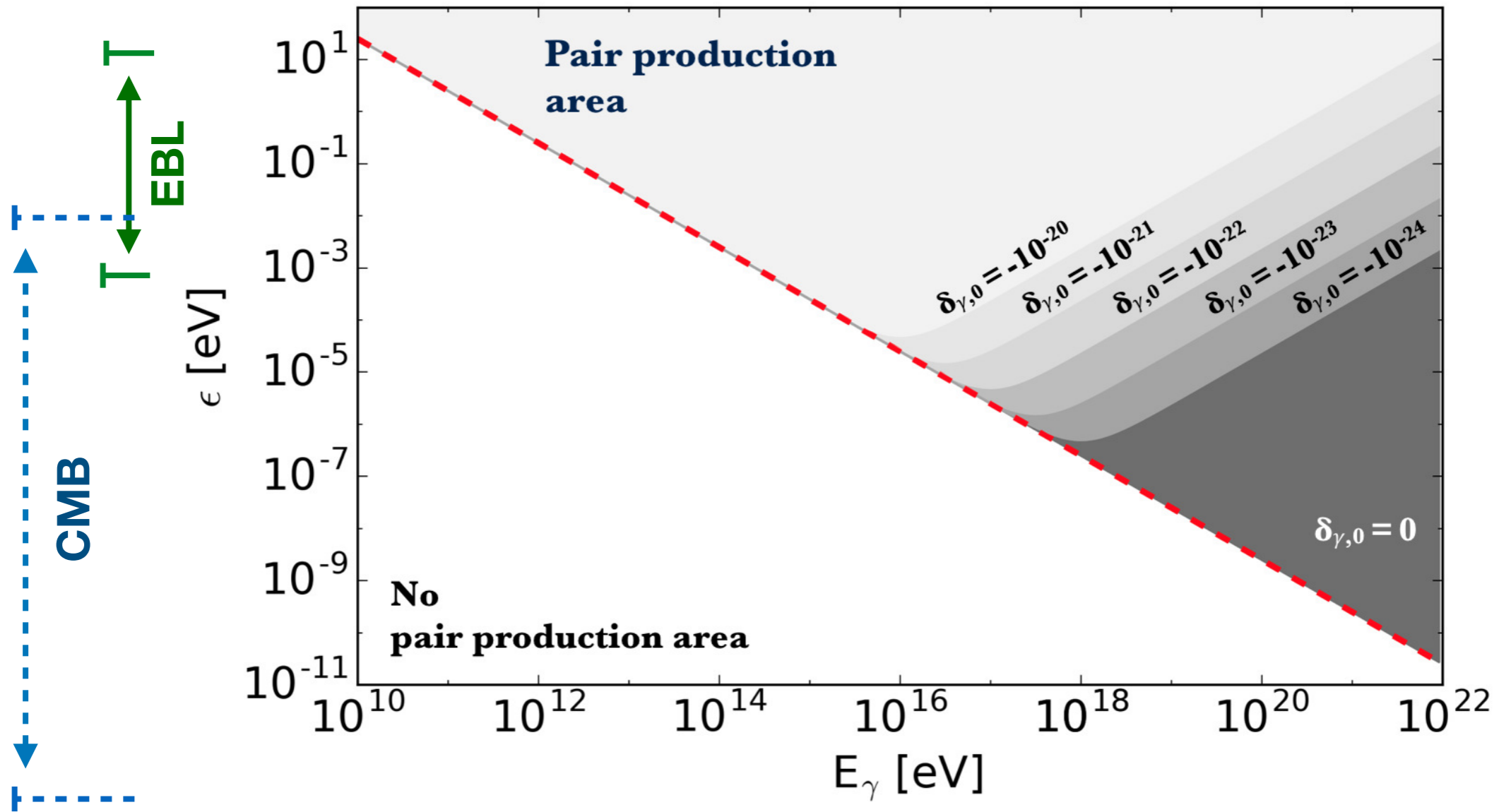
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Pair Production



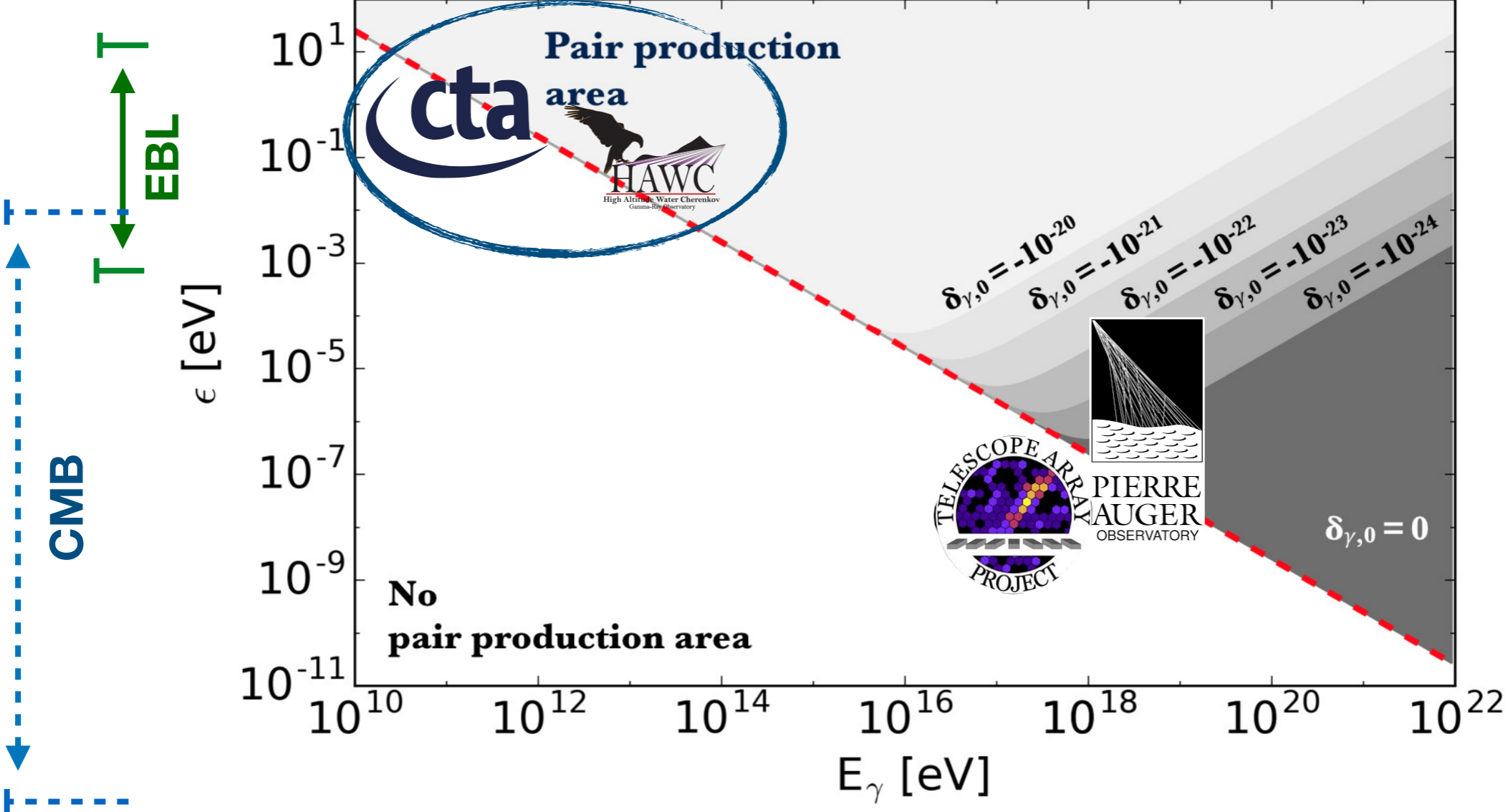
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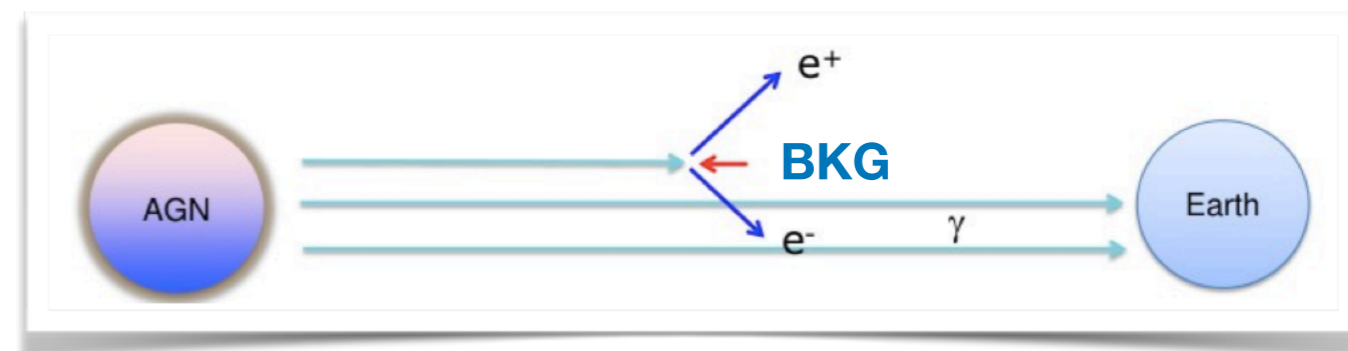
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Optical depth

$$\gamma_{VHE} \gamma_{BKG} \rightarrow e^+ e^-$$

$$\tau(E_\gamma, z; E_{LIV}^{(n)}, n) = \int_0^{z_0} dz \frac{\partial L(z)}{\partial z} \int_{\epsilon_{th}}^\infty d\epsilon \frac{\partial n(\epsilon, z)}{\partial \epsilon} \int_{-1}^1 d(\cos \theta) \frac{1 - \cos \theta}{2} \sigma_{\gamma\gamma_{EBL}}(E_\gamma, z, \epsilon, \cos \theta)$$

The
distance
element

Density of
BKG
photons

Pair Production
cross section

Optical depth + LIV

$$\gamma_{VHE} \gamma_{BKG} \rightarrow e^+ e^-$$

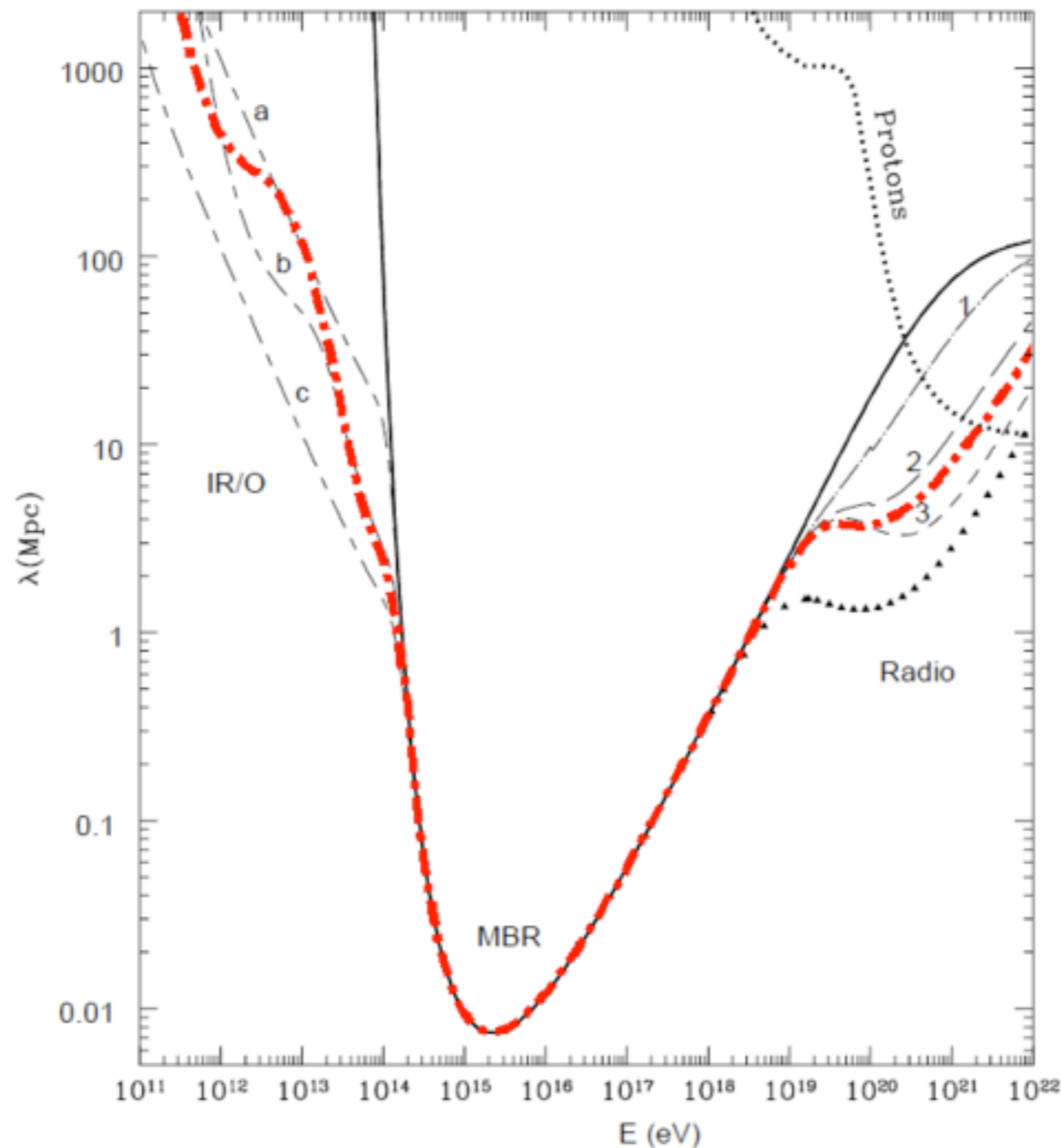
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LIV

$$\epsilon_{th}^{LIV} = \frac{m_e^2}{4E_\gamma K(1-K)} - \frac{\delta_{\gamma,n} E_\gamma^{n+1}}{4}$$

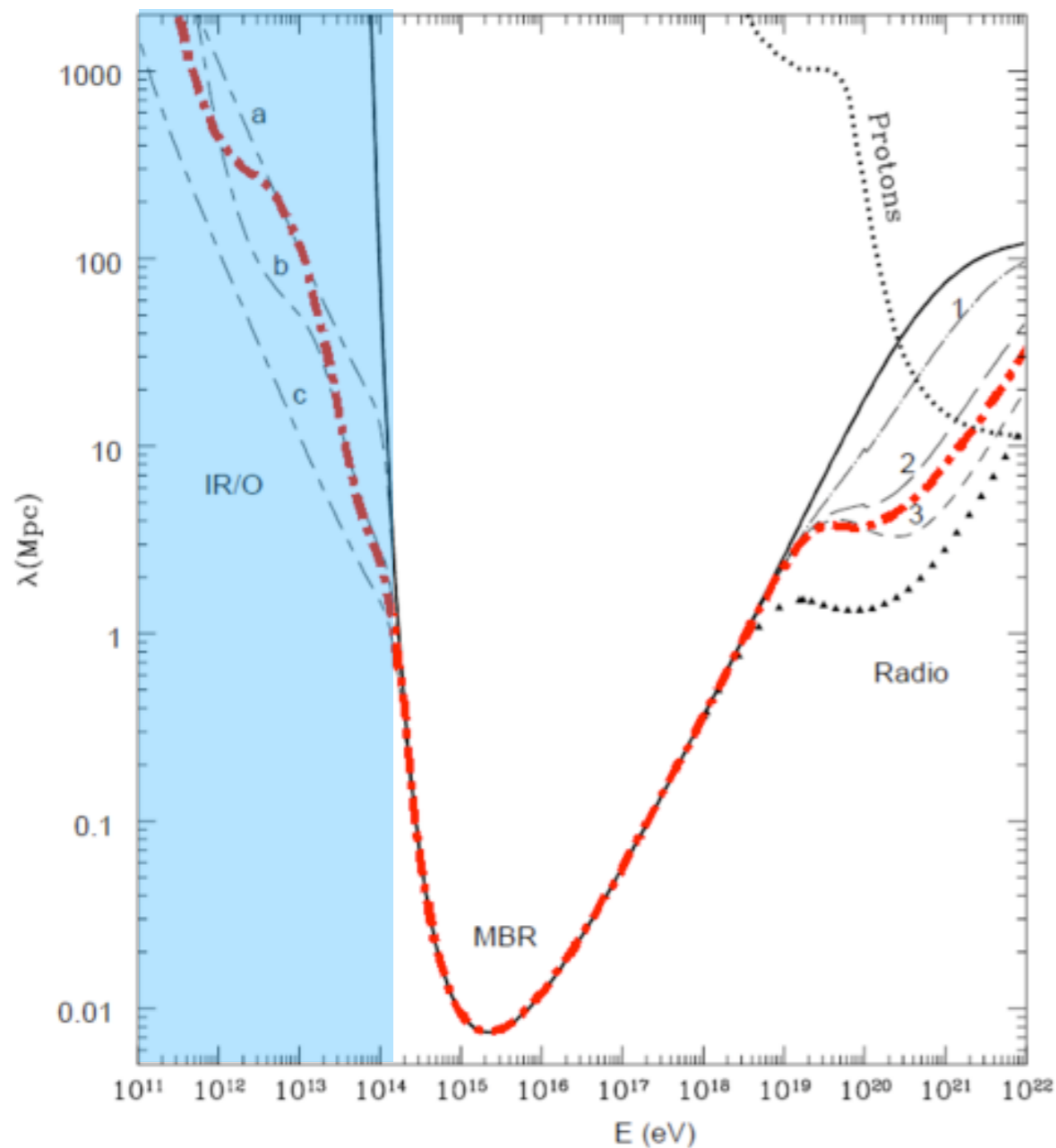
Optical depth

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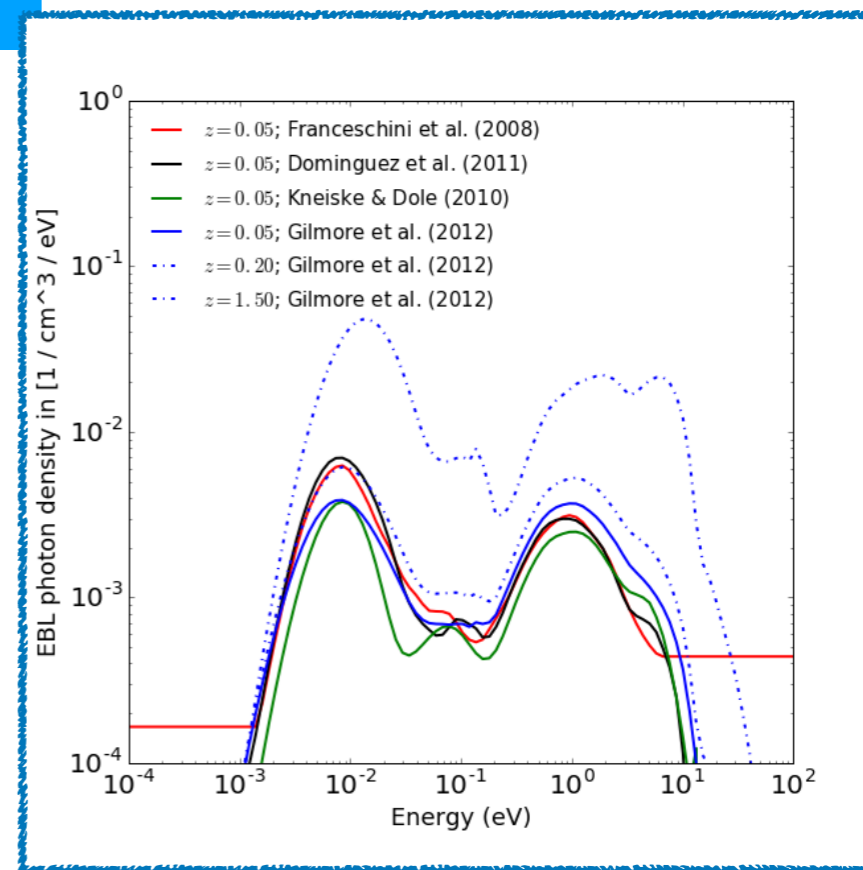


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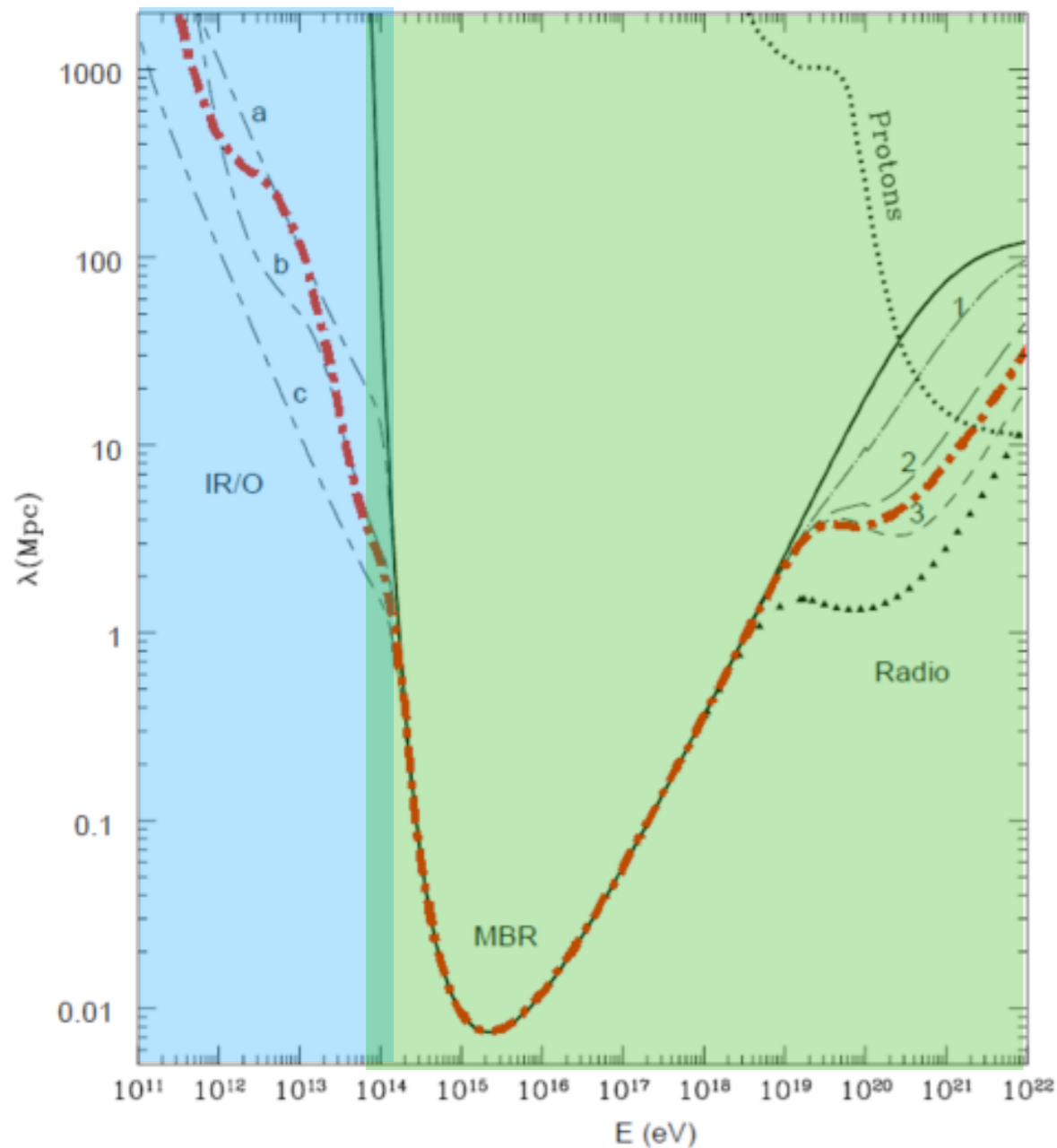


density of EBL photons

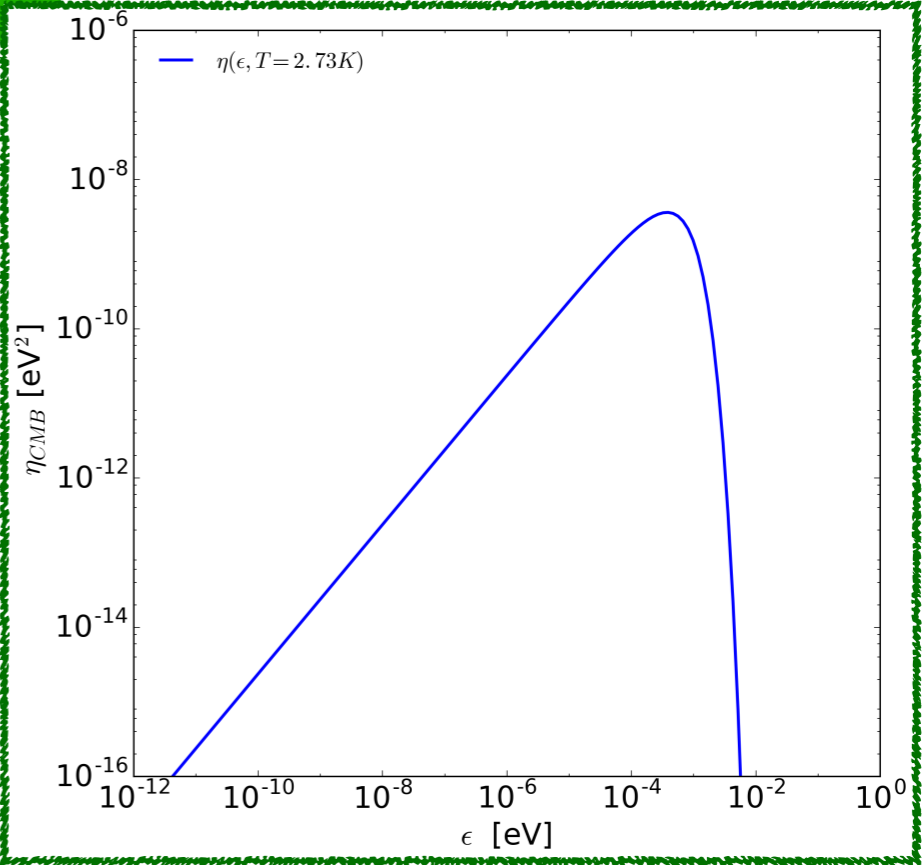


Optical depth

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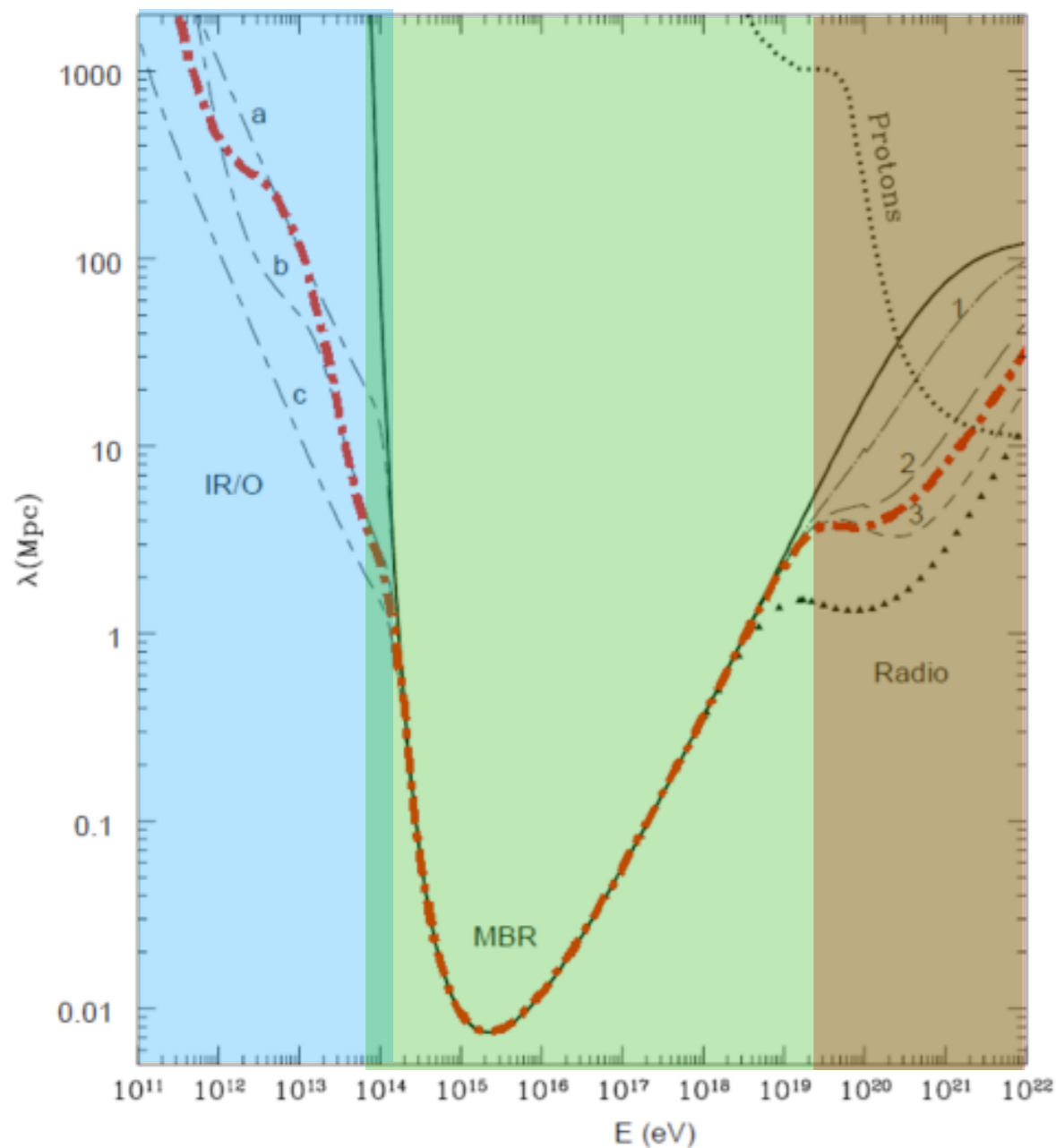


density of
CMB
photons



Optical depth

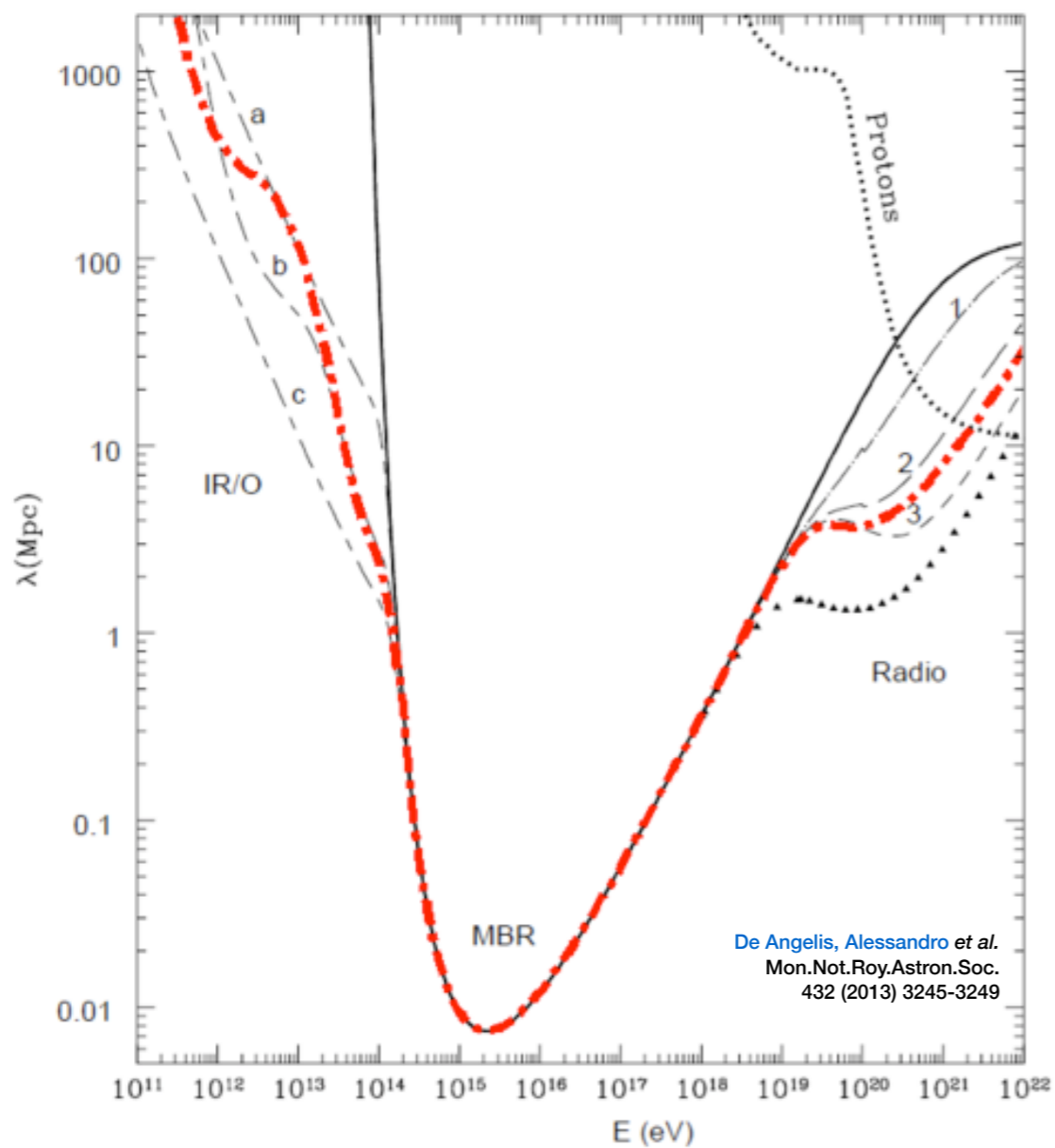
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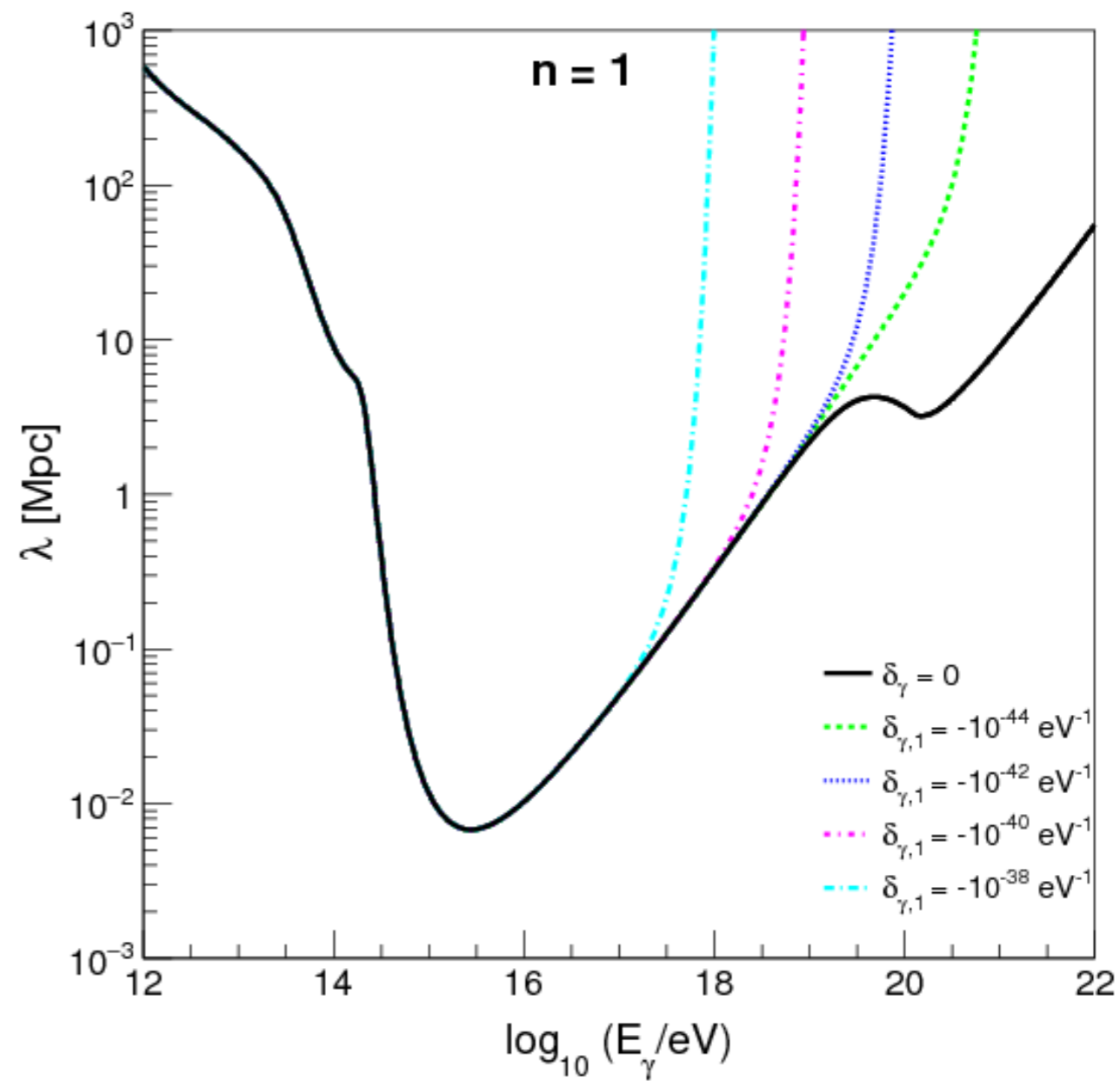
density of
Radio
photons

Optical Depth + LIV

LI

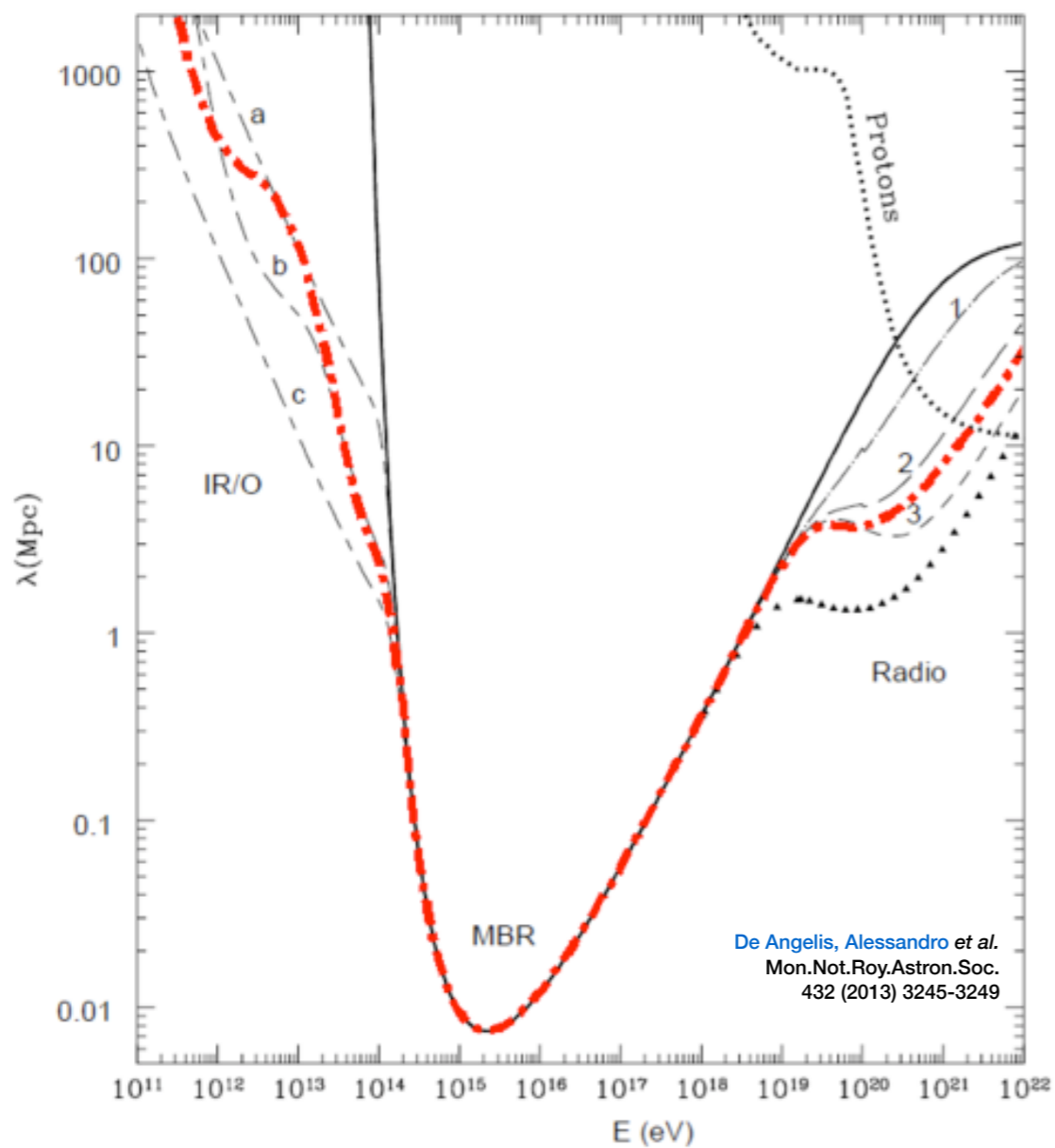


LIV

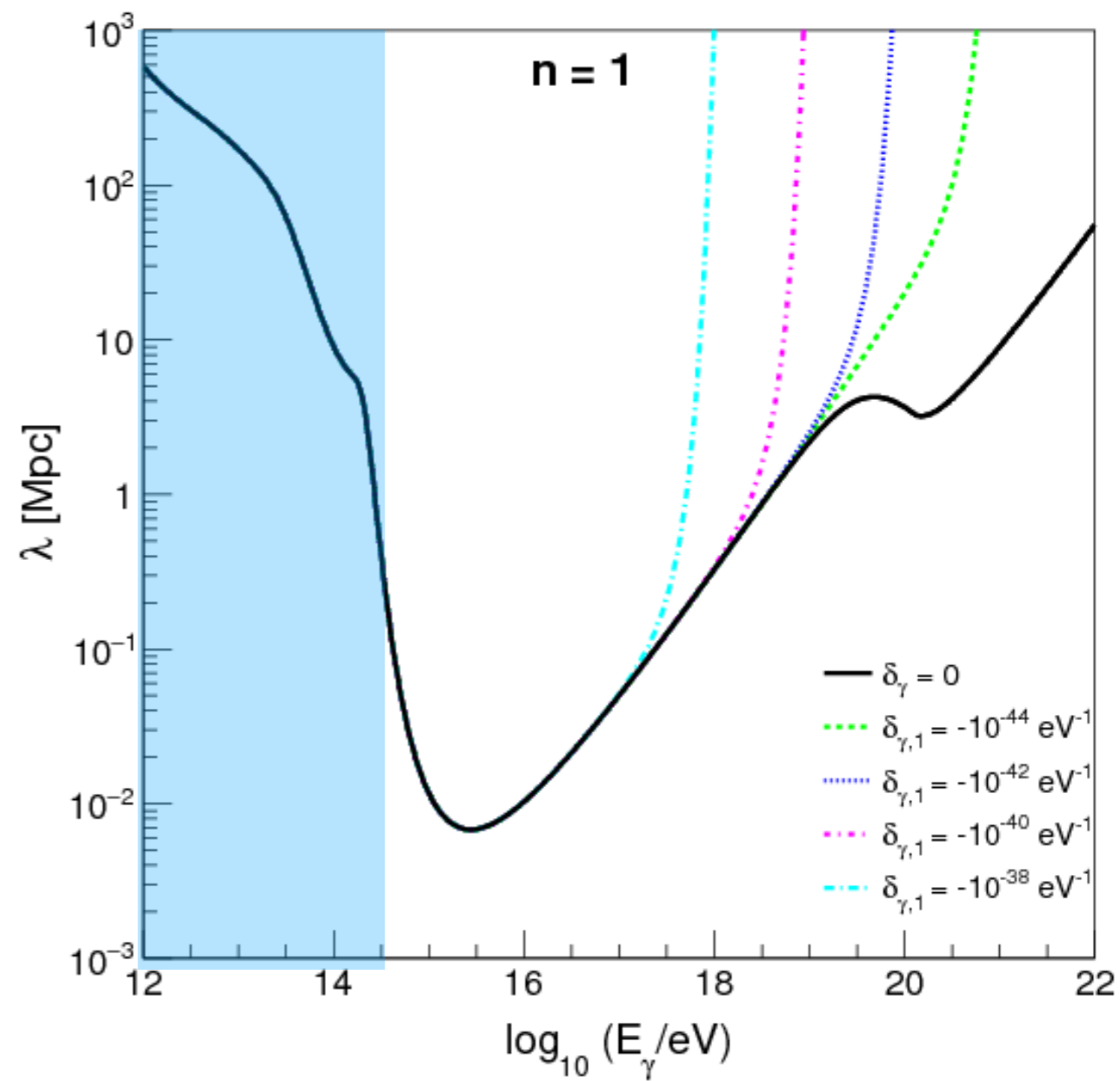


Optical Depth + LIV

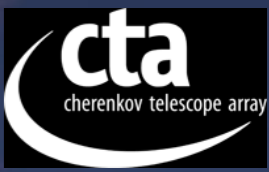
LI



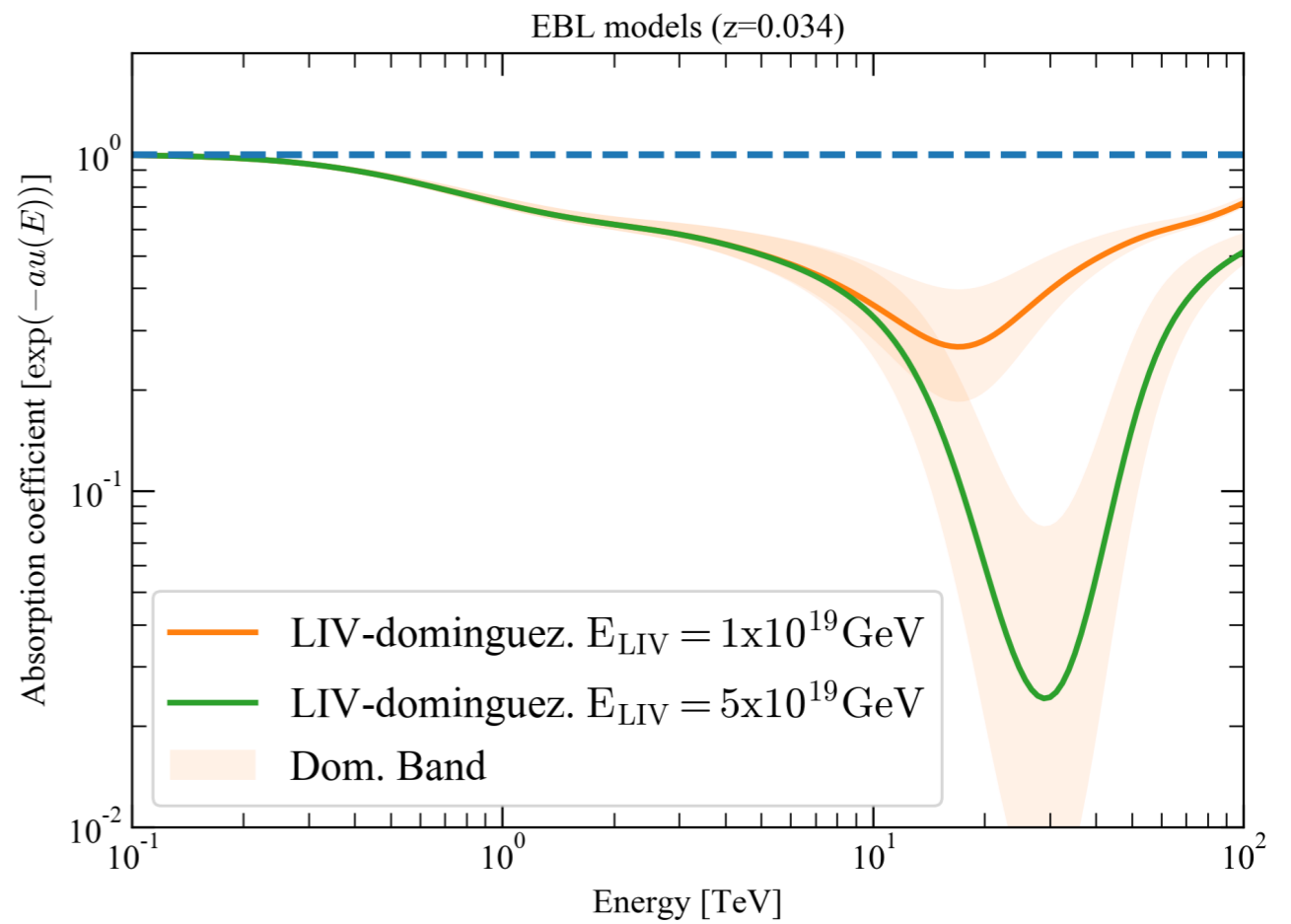
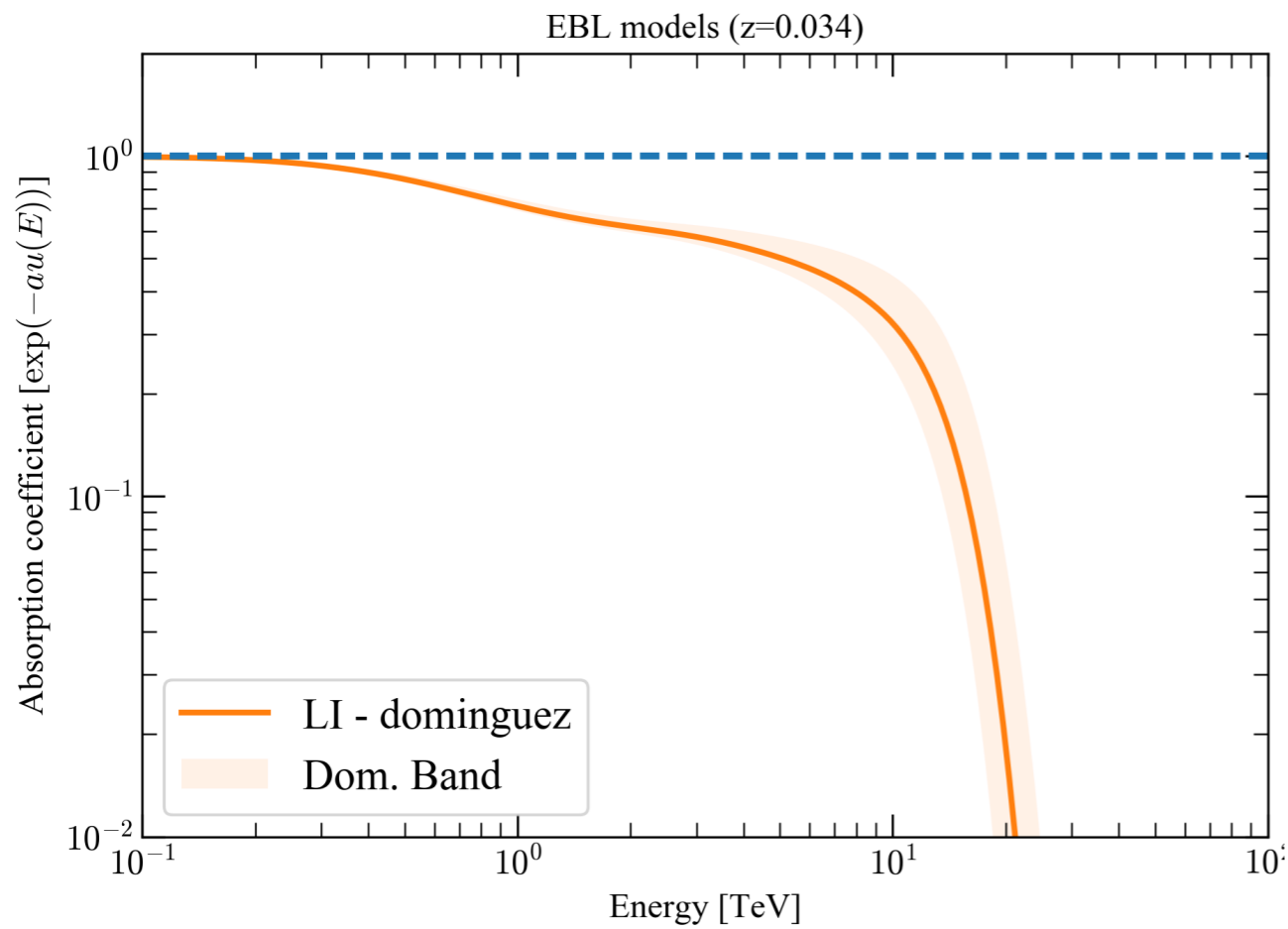
LIV



Optical Depth + LIV

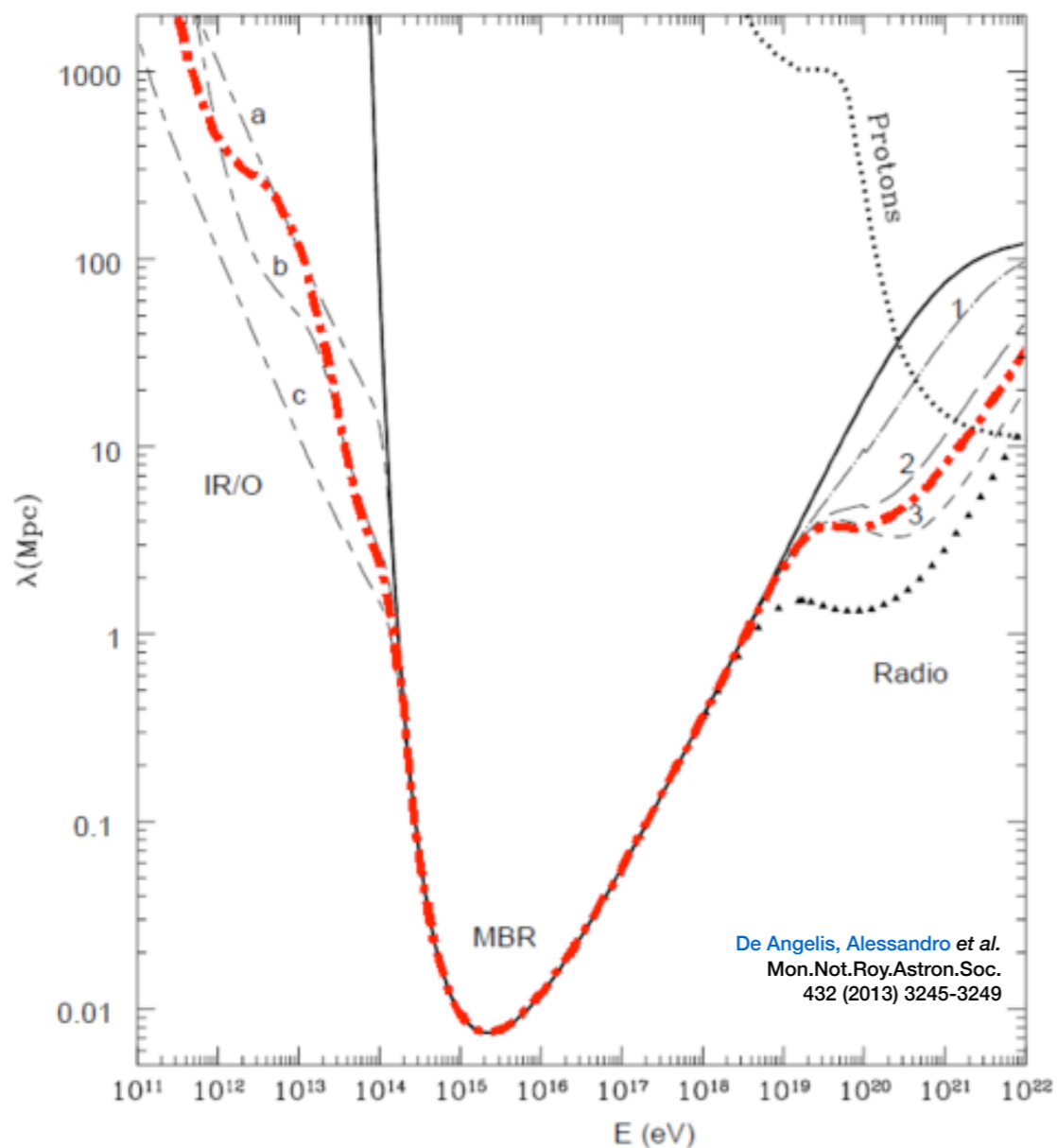


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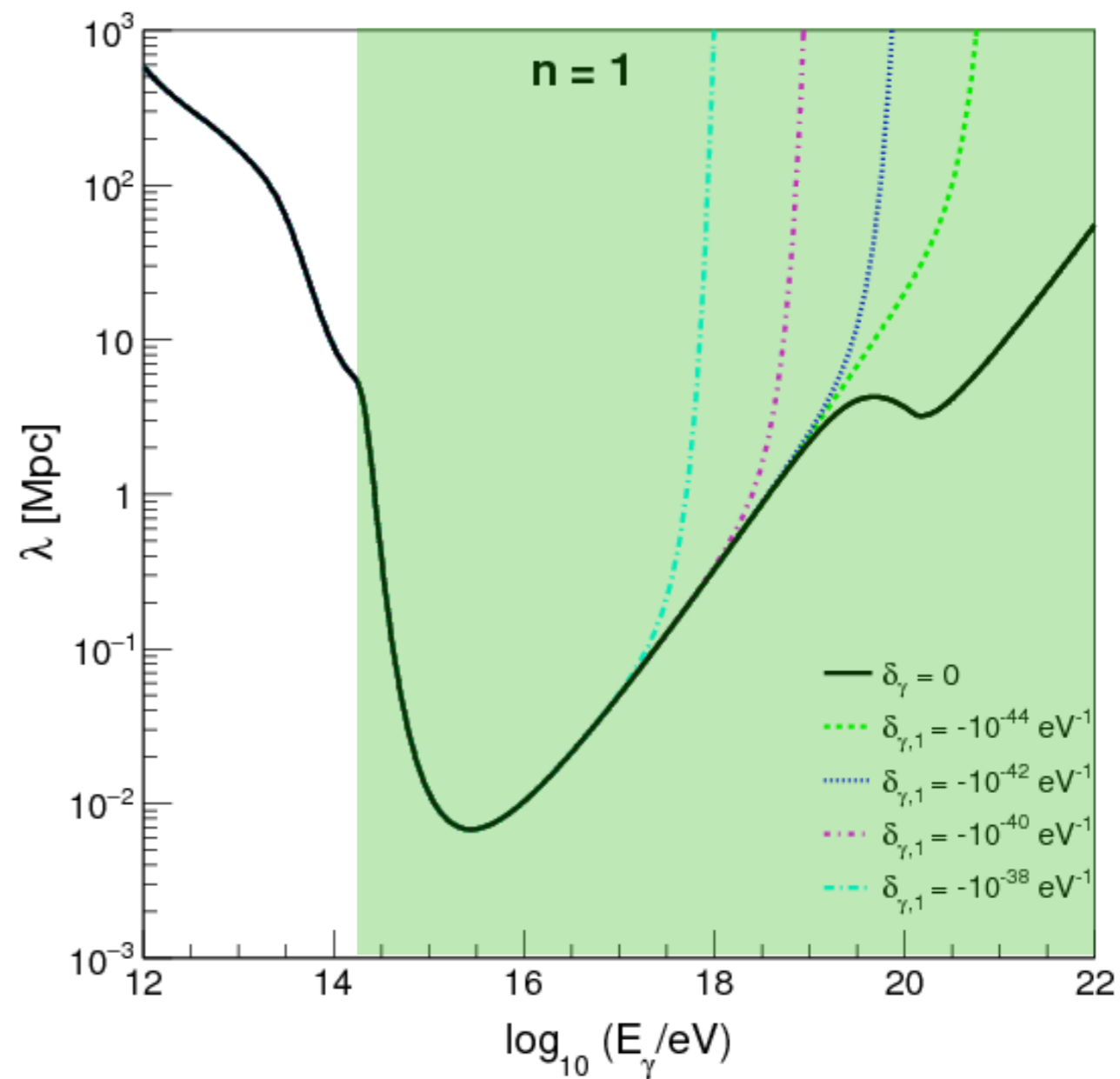


Optical Depth + LIV

LI



LIV



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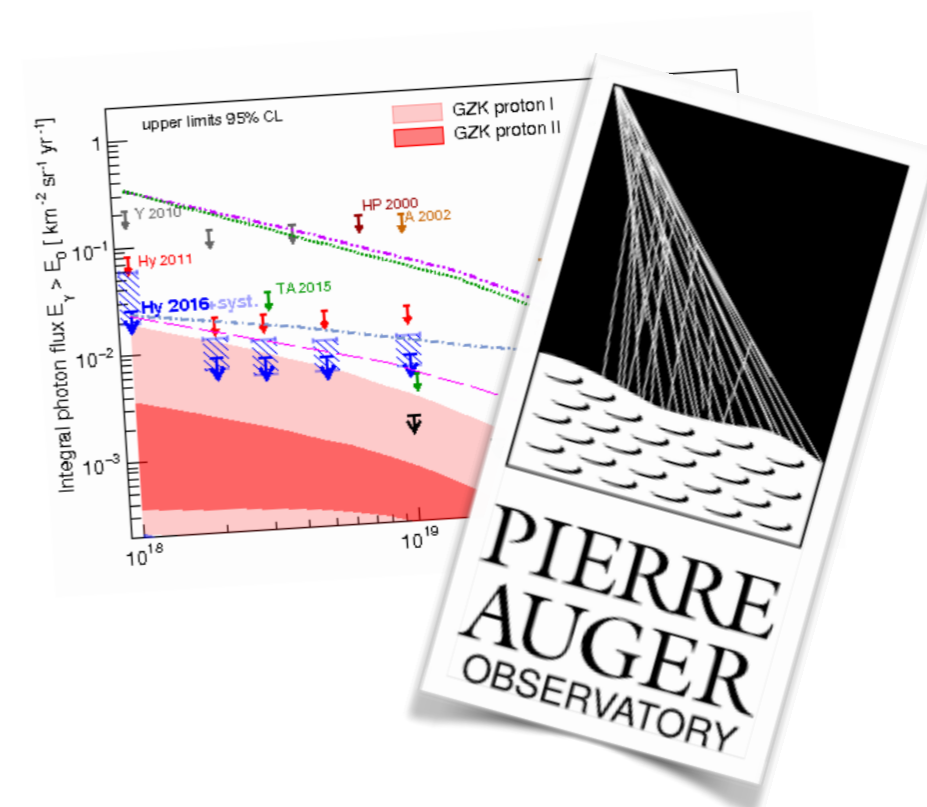
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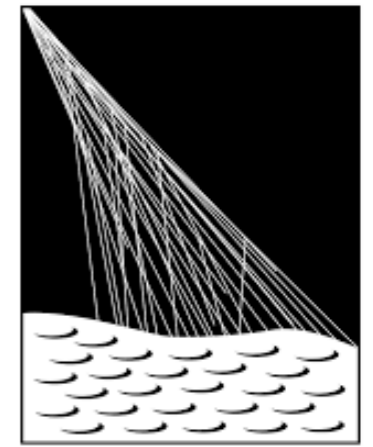
III. Optical Depth + LIV

IV. GZK photon flux + LIV

V. LIV limits



GZK photon flux



PIERRE
AUGER
OBSERVATORY

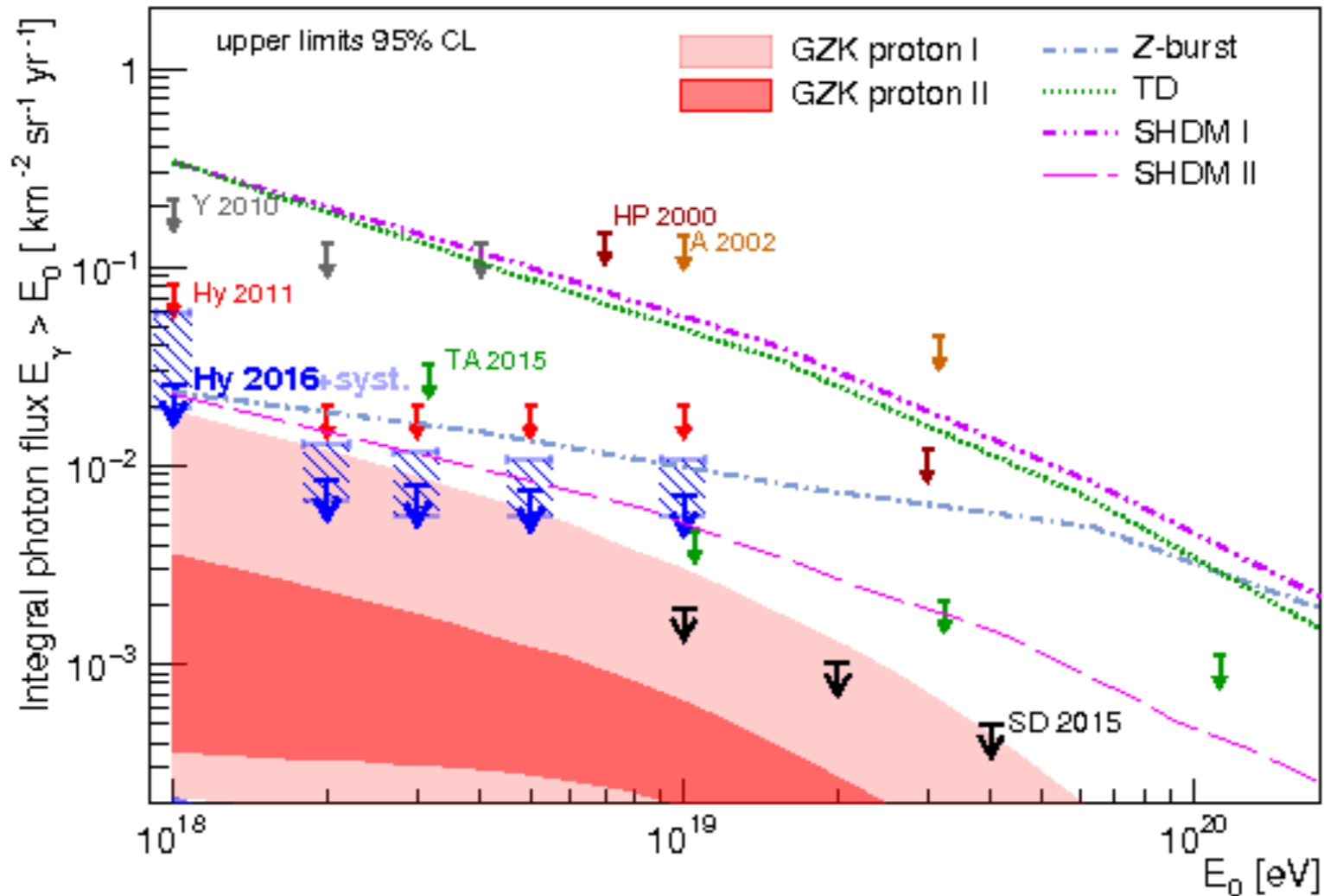


Figure 6. Upper limits on the integral photon flux derived from 9 years of hybrid data (blue arrows, Hy 2016) for a photon flux E^{-2} and no background subtraction. The limits obtained when the detector systematic uncertainties are taken into account are shown as horizontal segments (light blue) delimiting a dashed-filled box at each energy threshold. Previous limits from Auger: (SD [20] and Hybrid 2011 [19]), for Telescope Array (TA) [59], AGASA (A) [60], Yakutsk (Y) [61] and Haverah Park (HP) [62] are shown for comparison. None of them includes systematic uncertainties. The shaded regions and the lines give the predictions for the GZK photon flux [14, 16] and for top-down models (TD, Z-Burst, SHDM I [63] and SHDM II [21]).

Parameters of the Four Source Models Used in This Paper

Model	Γ	$\log_{10}(R_{\text{cut}}/V)$	$f\text{H}$	$f\text{He}$	$f\text{N}$	$f\text{Si}$	$f\text{Fe}$
C_1	1	18.699	0.7692	0.1538	0.0461	0.0231	0.00759
C_2	1	18.5	0	0	0	1	0
C_3	1.25	18.5	0.365	0.309	0.121	0.1066	0.098
C_4	2.7	∞	1	0	0	0	0

Note. Γ is the spectral index, R_{cut} is the rigidity cutoff and $f\text{H}$, $f\text{He}$, $f\text{N}$, $f\text{Si}$, and $f\text{Fe}$ are the fractions of each nuclei.

1. C_1 : Aloisio et al. (2014);
2. C_2 : Unger, Farrar, & Anchordoqui (2015)—Fiducial model (Unger et al. 2015);
3. C_3 : Unger et al. (2015) with the abundance of galactic nuclei from (Olive & Group 2014);
4. C_4 : Berezhinsky, Gazizov, & Grigorieva (2007)—Dip model (Berezhinsky et al. 2006).

$$\frac{dN}{dE_s} = \begin{cases} E_s^{-\Gamma}, & \text{for } R_s < R_{\text{cut}} \\ E_s^{-\Gamma} e^{1-R_s/R_{\text{cut}}}, & \text{for } R_s \geq R_{\text{cut}} \end{cases},$$

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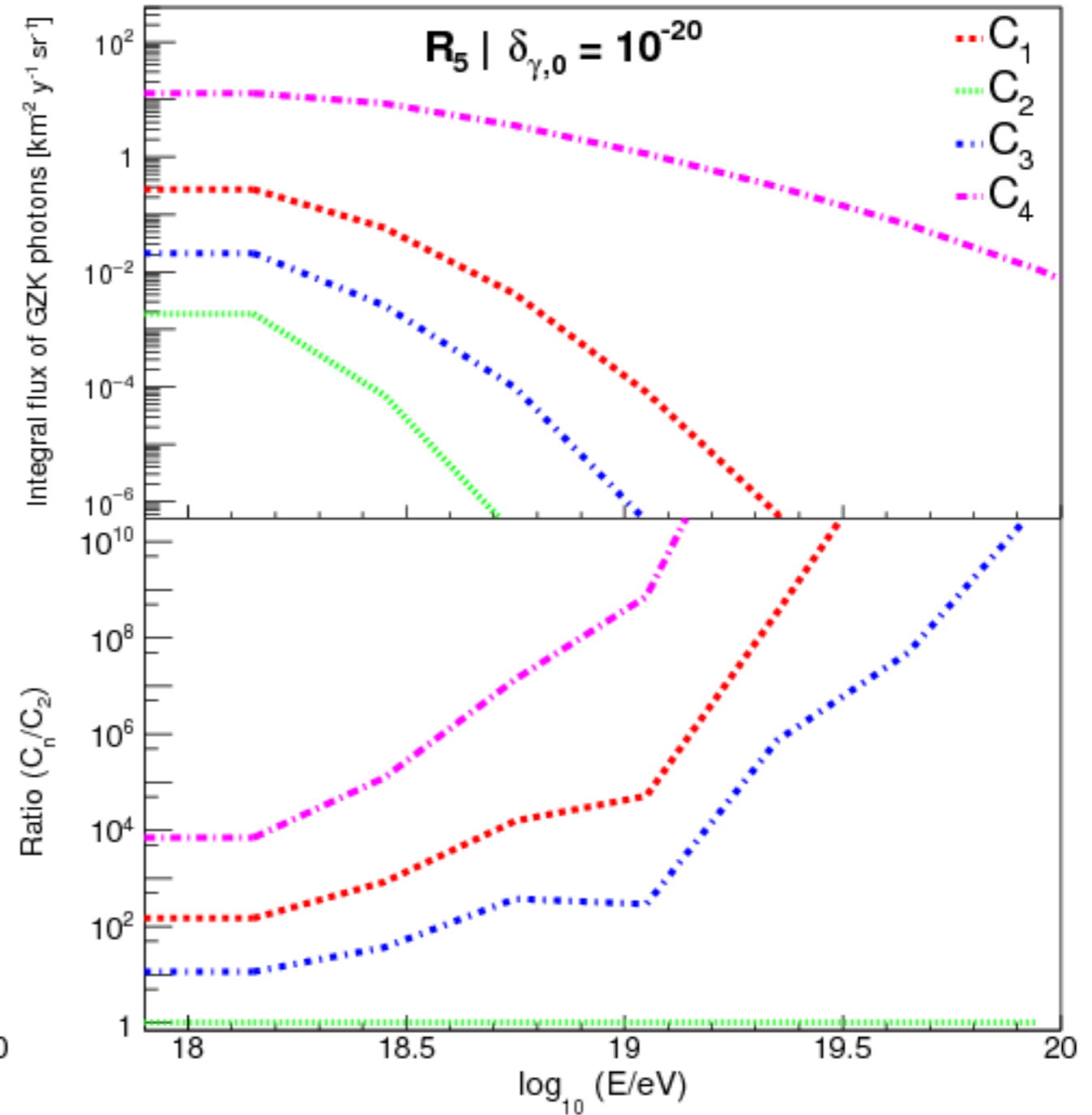
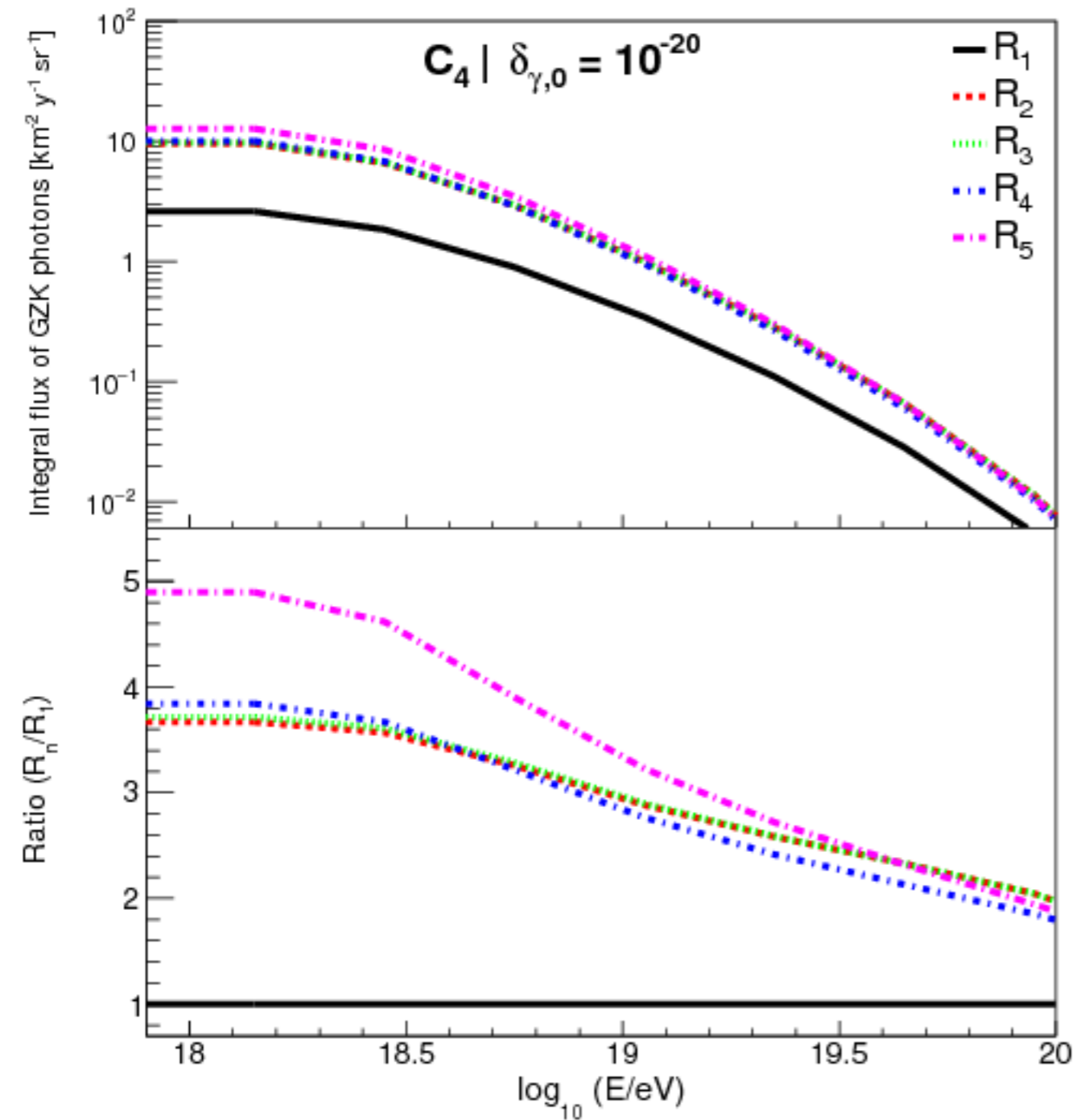
Models of Source Distribution

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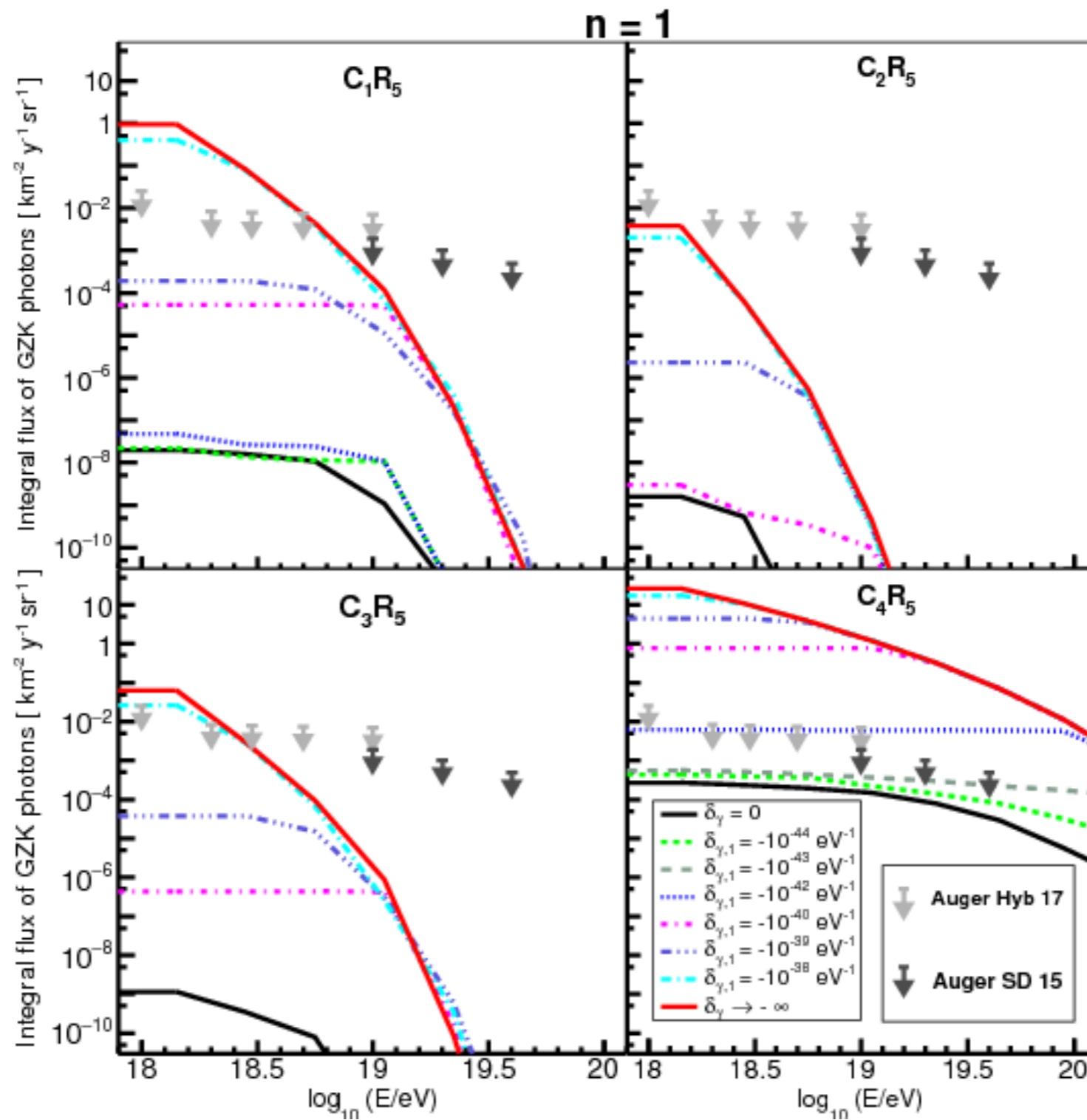
$$\frac{dN}{dE_s} = \begin{cases} E_s^{-\Gamma}, & \text{for } R_s < R_{\text{cut}} \\ E_s^{-\Gamma} e^{1-R_s/R_{\text{cut}}}, & \text{for } R_s \geq R_{\text{cut}} \end{cases},$$

1. R_1 : sources are uniformly distributed in a comoving volume;
2. R_2 : sources follow the star formation distribution given in Hopkins & Beacom (2006). The evolution is proportional to $(1+z)^{3.4}$ for $z < 1$, to $(1+z)^{-0.26}$ for $1 \leq z < 4$ and to $(1+z)^{-7.8}$ for $z \geq 4$;
3. R_3 : sources follow the star formation distribution given in Yüksel et al. (2008). The evolution is proportional to $(1+z)^{3.4}$ for $z < 1$, to $(1+z)^{-0.3}$ for $1 \leq z < 4$ and to $(1+z)^{-3.5}$ for $z \geq 4$;
4. R_4 : sources follow the GRB rate evolution from Le & Dermer (2007). The evolution is proportional to $(1+8z)/[1+(z/3)^{1.3}]$;
5. R_5 : sources follow the GRB rate evolution from Le & Dermer (2007). The evolution is proportional to $(1+11z)/[1+(z/3)^{0.5}]$.

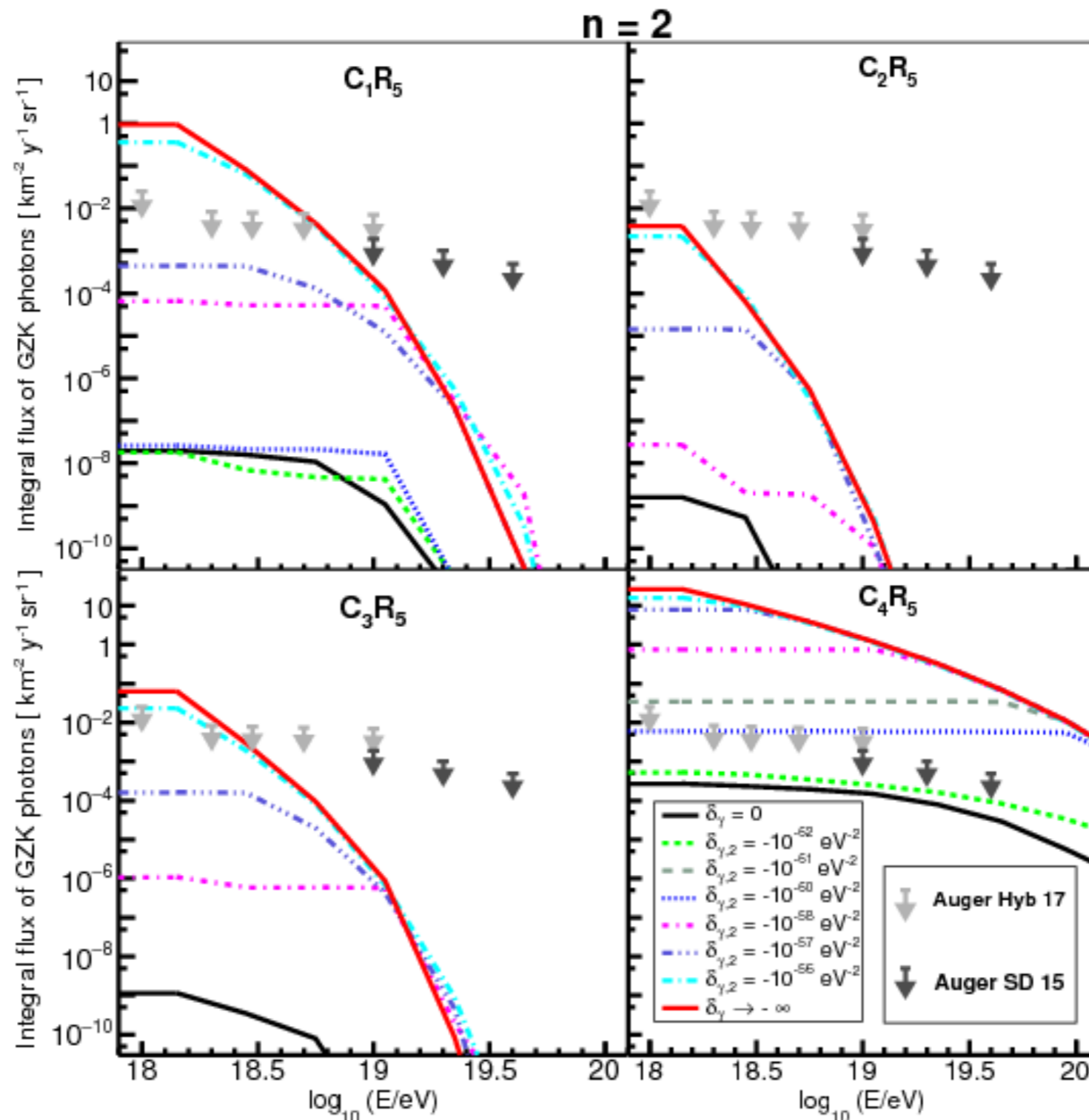
GZK photon flux + LIV



GZK photon flux + LIV



GZK photon flux + LIV



Model C_3R_5 was shown to (best) describe the energy spectrum, composition, and arrival direction of UHECR*

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Limits on the LIV Coefficients Imposed by This Work for Each Source Model and LIV Order (n)

Model	$\delta_{\gamma,0}^{\text{limit}}$	$\delta_{\gamma,1}^{\text{limit}} (\text{eV}^{-1})$	$\delta_{\gamma,2}^{\text{limit}} (\text{eV}^{-2})$
C_1R_5	$\sim -10^{-20}$	$\sim -10^{-38}$	$\sim -10^{-56}$
C_2R_5
C_3R_5	$\sim -10^{-20}$	$\sim -10^{-38}$	$\sim -10^{-56}$
C_4R_5	$\sim -10^{-22}$	$\sim -10^{-42}$	$\sim -10^{-60}$

Limits on the LIV Coefficients Imposed by Other Works Based on Gamma-Ray Propagation

Model	$\delta_{\gamma,0}^{\text{limit}}$	$\delta_{\gamma,1}^{\text{limit}} (\text{eV}^{-1})$	$\delta_{\gamma,2}^{\text{limit}} (\text{eV}^{-2})$
Galaverni & Sigl (2008a)	...	-1.97×10^{-43}	-1.61×10^{-63}
H.E.S.S.—PKS 2155–304 (2011)	...	-4.76×10^{-28}	-2.44×10^{-40}
Fermi—GRB 090510 (2013)	...	-1.08×10^{-29}	-5.92×10^{-41}
H.E.S.S.—Mrk 501 (2017)	...	-9.62×10^{-29}	-4.53×10^{-42}

Conclusions and remarks

- ❖ We studied the effect of possible LIV in the propagation of photons in the universe.
- ❖ The mean-free path of the pair production interaction was calculated considering LIV effects.
- ❖ We found that even moderate LIV coefficients introduce a significant change in the mean-free path of the interaction
- ❖ Stringent limits to the LIV coefficient were established based on source models compatible with the most updated data of UHECR.
- ▶ The limits presented here are several orders of magnitude more restrictive than previous calculations based on the arrival time of TeV photons; however, the comparison is not straightforward due to different systematics of the measurements and energy of the photons.

Thanks!