



# Sensitivity study of $\tau \rightarrow \eta \pi \nu$ at the Belle II experiment

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Mexico City

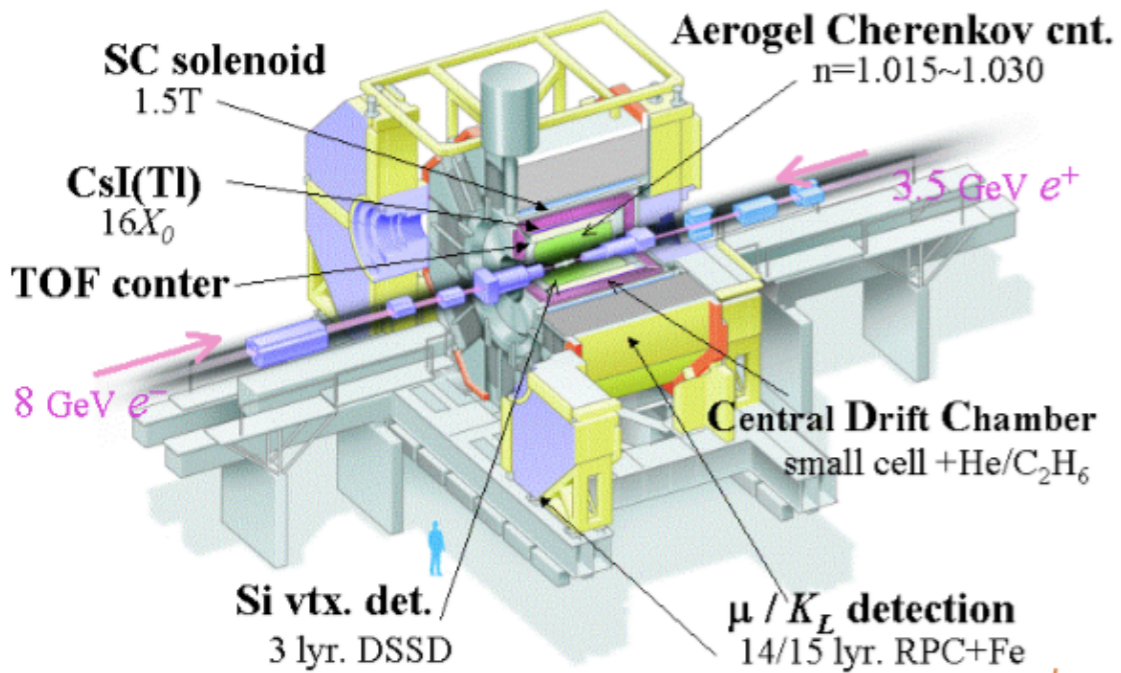
28 Sep 2017

## Outline

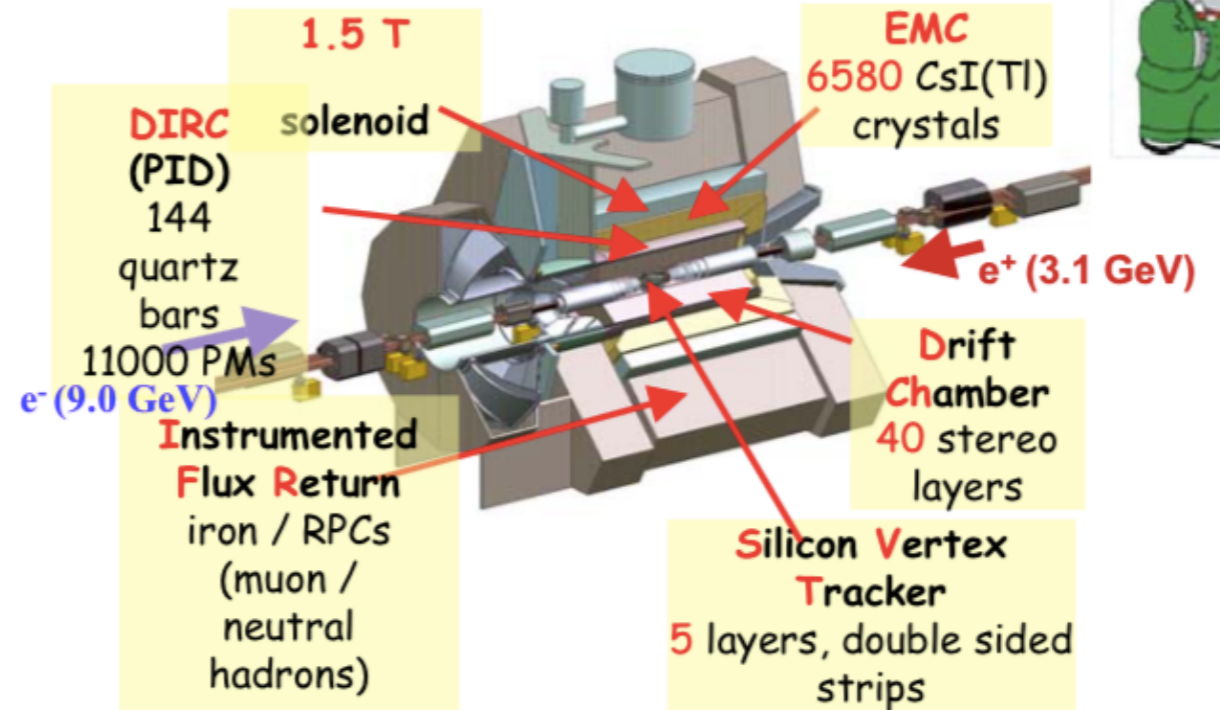
- B-factories and  $\tau$  physics.
- Second class currents
- $\tau \rightarrow \eta \pi \nu$  decay
- Outlook.

# B Factories

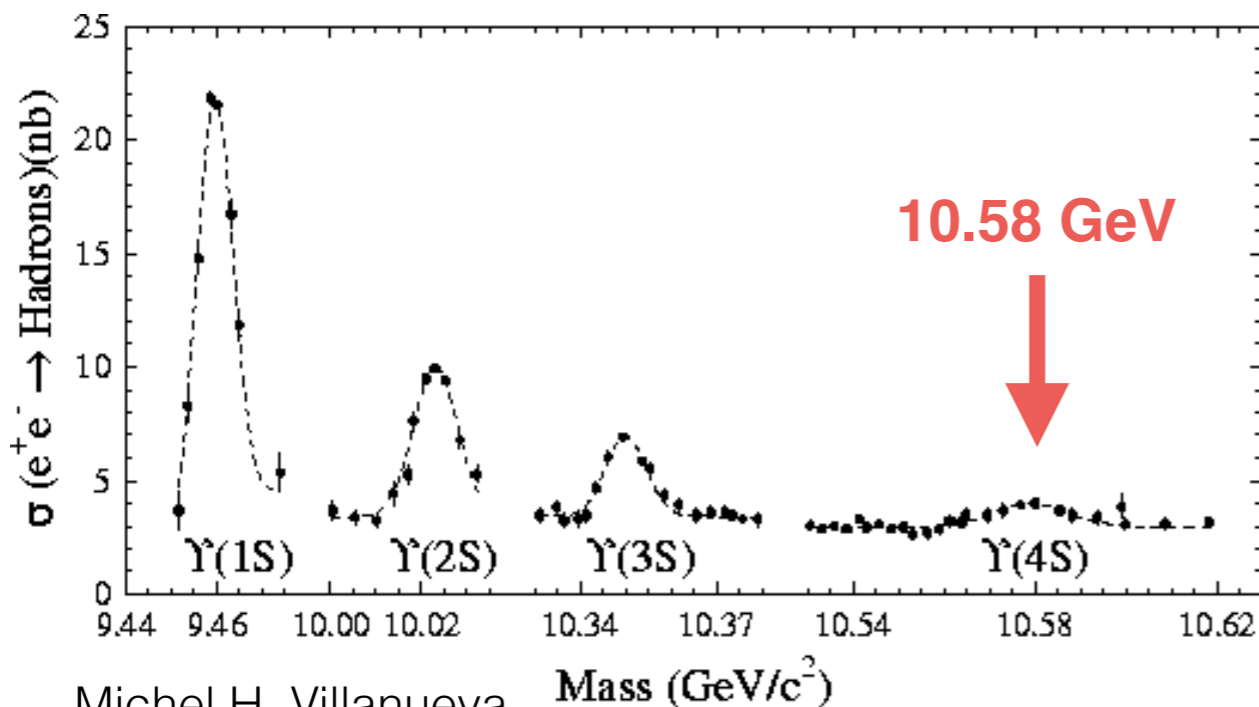
## Belle Detector



## BaBar detector

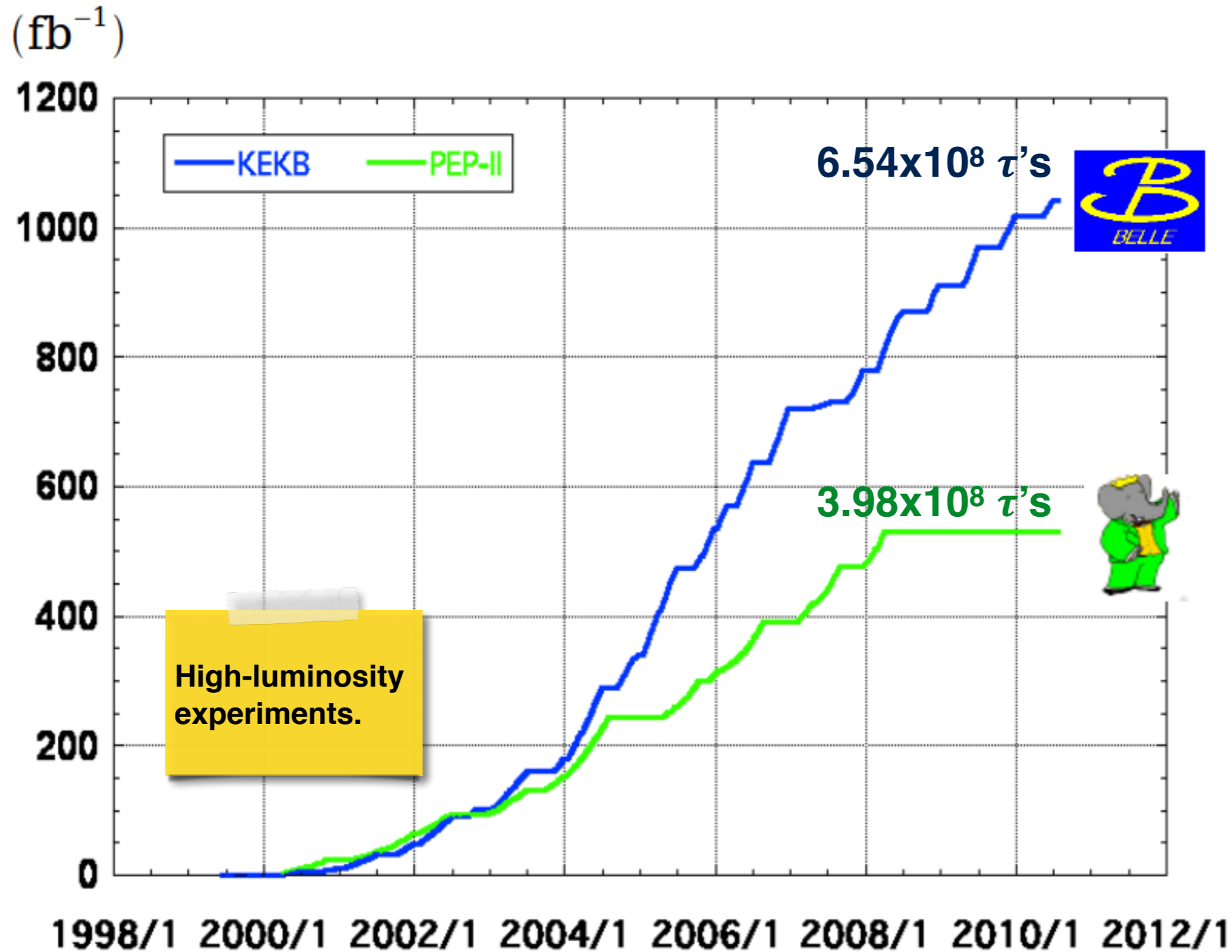


$\sqrt{s} = 10.58 \text{ GeV}$



- B-Factory  
 $BR(\Upsilon(4S) \rightarrow B\bar{B}) > 96\%$
- $\tau$  factory too!  
 $\sigma(e^+e^- \rightarrow \Upsilon(4s)) = 1.05 \text{ nb}$   
 $\sigma(e^+e^- \rightarrow \tau\tau) = 0.92 \text{ nb}$

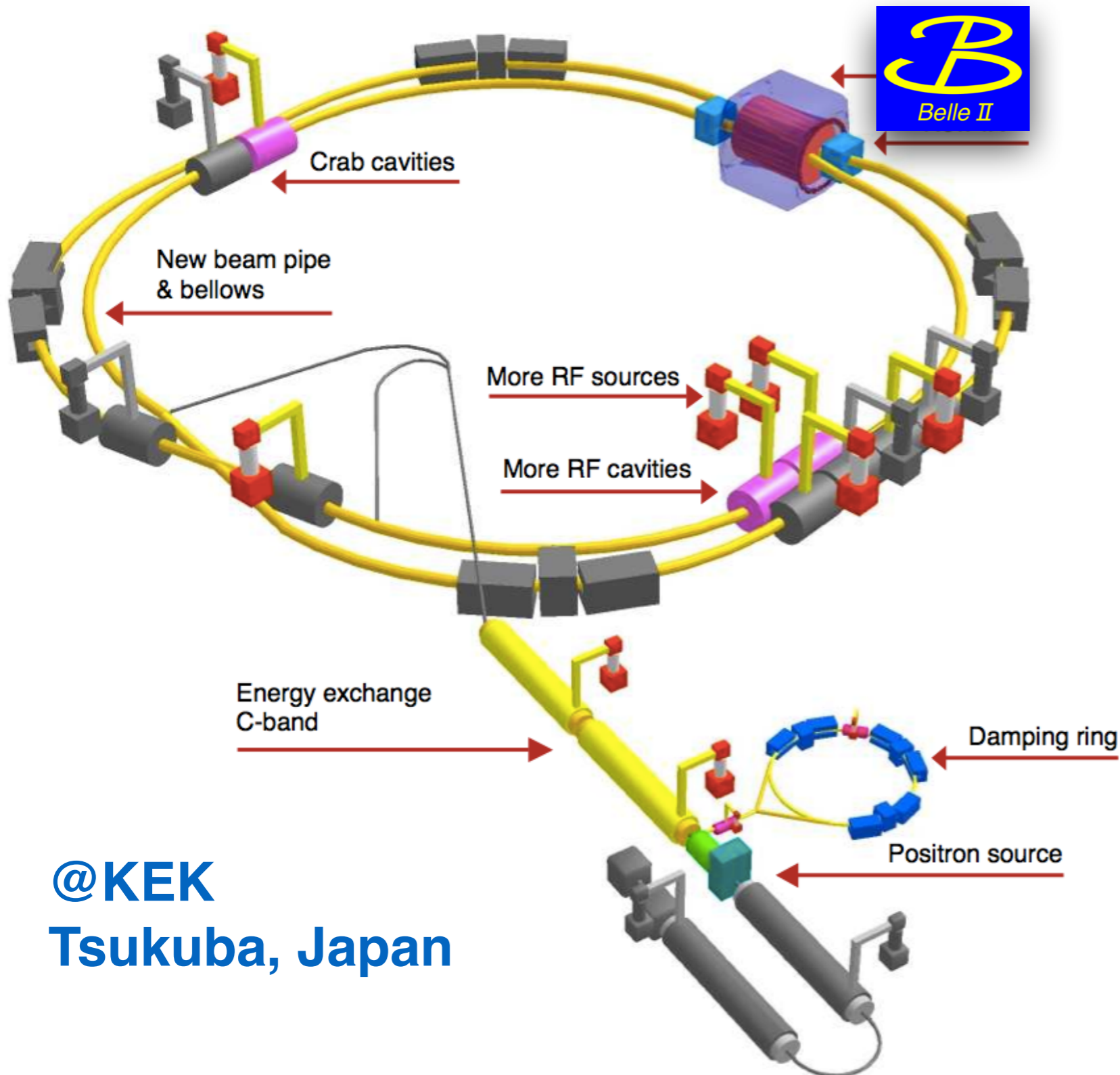
# Integrated Luminosity of B factories



**> 1  $\text{ab}^{-1}$**   
**On resonance:**  
 $\Upsilon(5S)$ : 121  $\text{fb}^{-1}$   
 $\Upsilon(4S)$ : 711  $\text{fb}^{-1}$   
 $\Upsilon(3S)$ : 3  $\text{fb}^{-1}$   
 $\Upsilon(2S)$ : 25  $\text{fb}^{-1}$   
 $\Upsilon(1S)$ : 6  $\text{fb}^{-1}$   
**Off reson./scan:**  
 $\sim 100 \text{ fb}^{-1}$

**$\sim 550 \text{ fb}^{-1}$**   
**On resonance:**  
 $\Upsilon(4S)$ : 433  $\text{fb}^{-1}$   
 $\Upsilon(3S)$ : 30  $\text{fb}^{-1}$   
 $\Upsilon(2S)$ : 14  $\text{fb}^{-1}$   
**Off resonance:**  
 $\sim 54 \text{ fb}^{-1}$

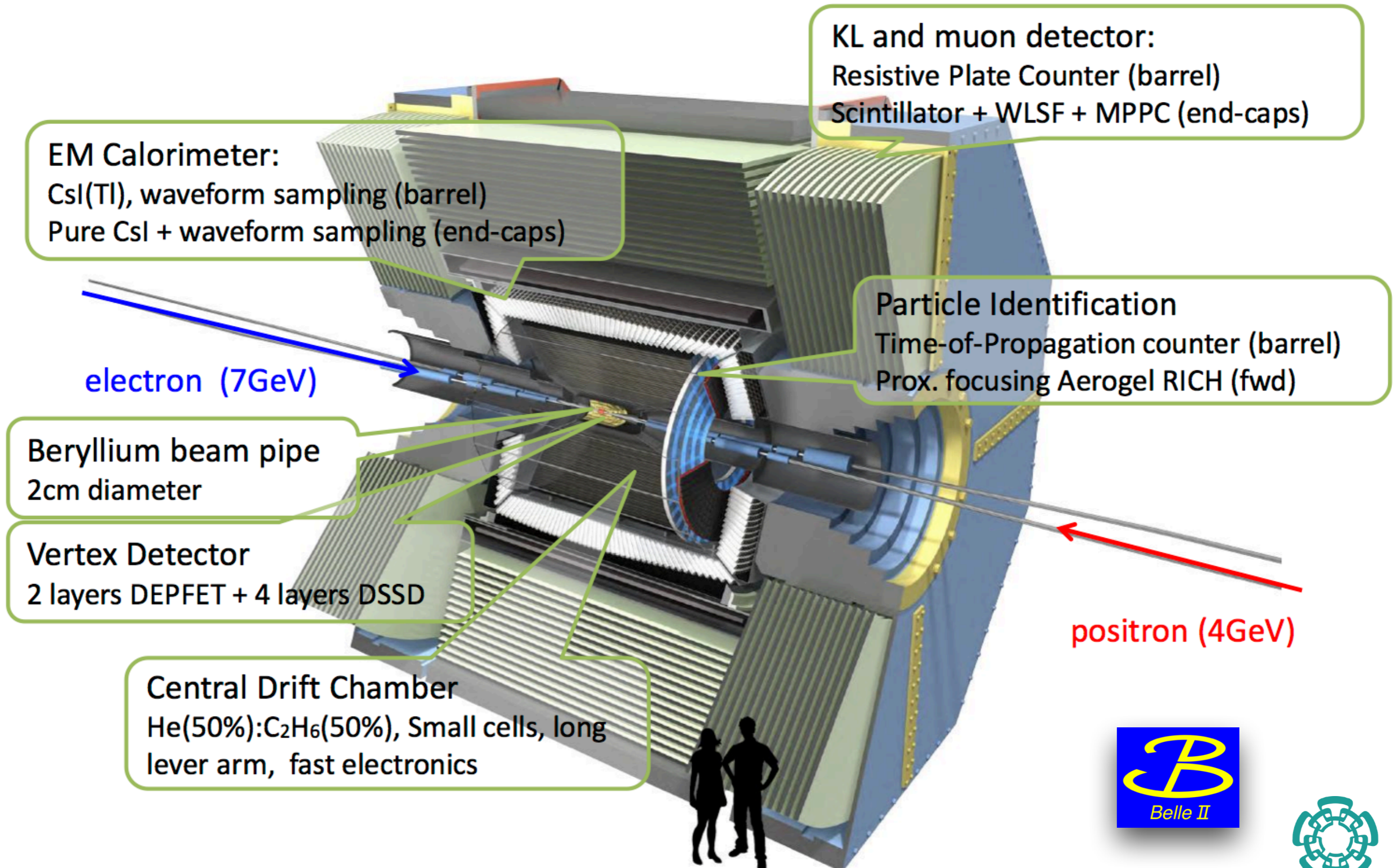
# SuperKEKB



- Super B-Factory  
**(And  $\tau$  factory too!)**
- Integrated luminosity expected:  
 **$50 \text{ ab}^{-1}$**   
**( $4.6 \times 10^{10} \tau$  pairs)**
- Full physics program starts:  
late 2018

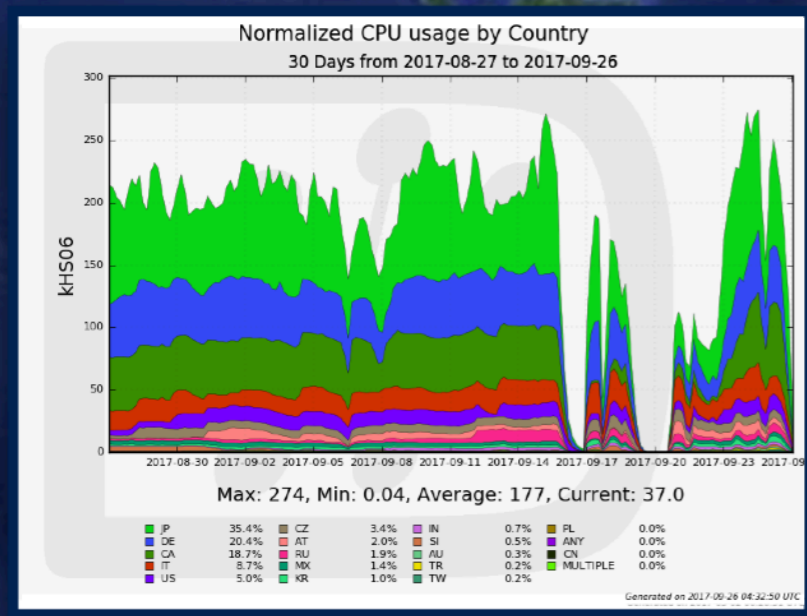
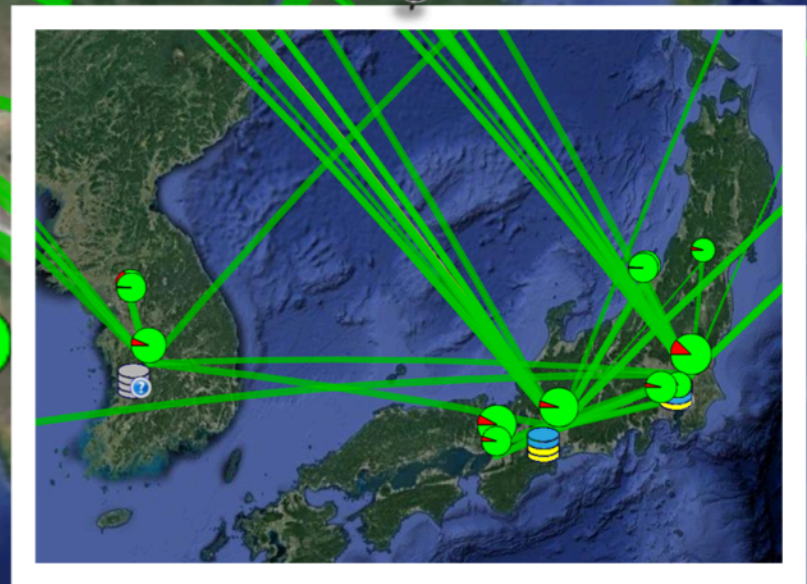
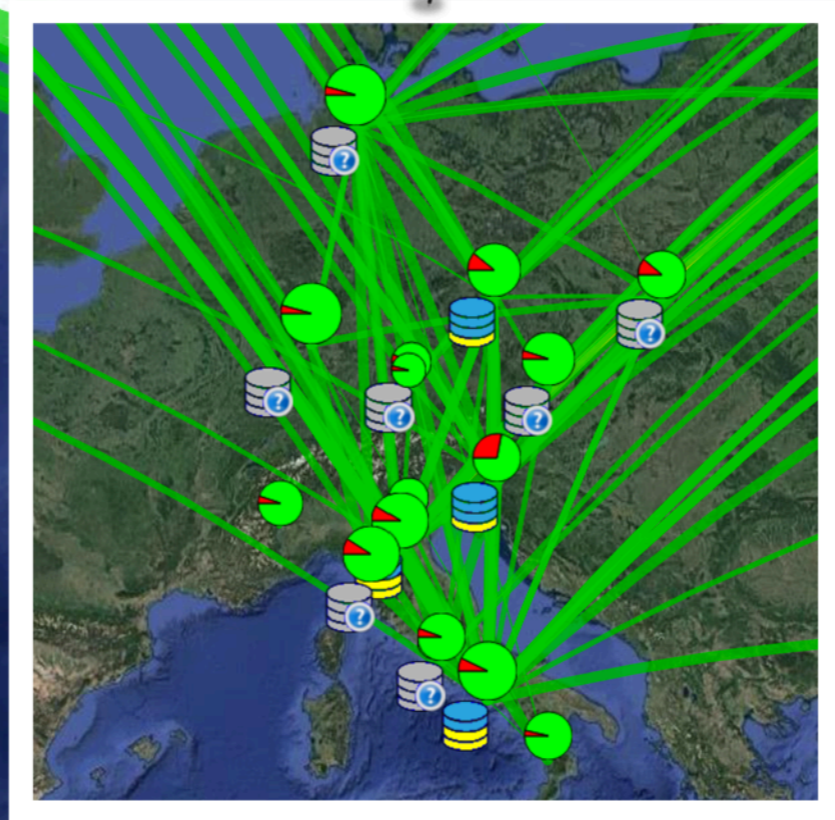
@KEK  
Tsukuba, Japan

# Belle II Detector



# Belle II MC samples

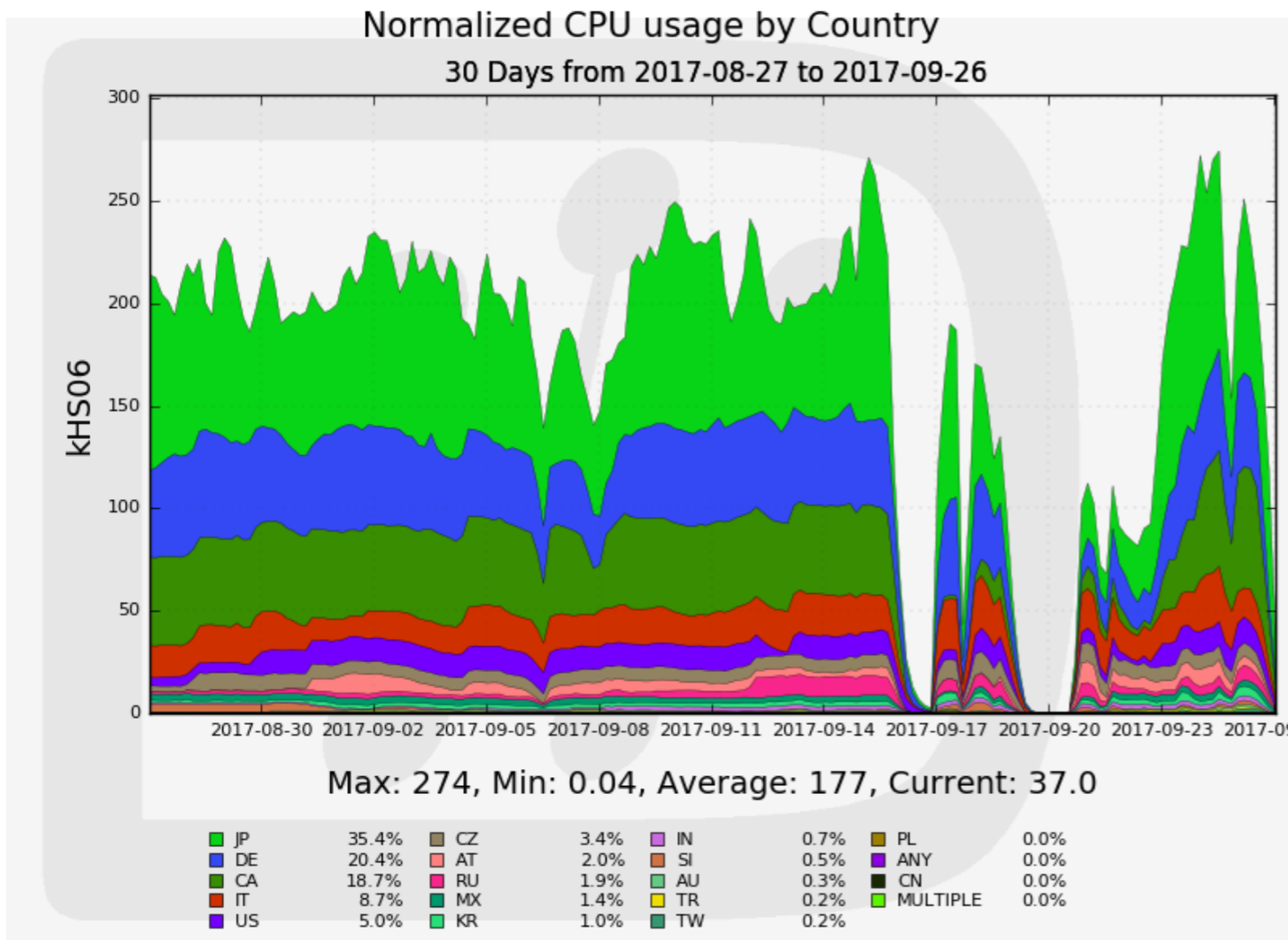
**MC Sample:**  
 $\sim 2 \text{ ab}^{-1}$   
 (1  $\text{ab}^{-1}$  for training,  
 1  $\text{ab}^{-1}$  for analysis).



# Mexican Contribution

- 504 cores  
3.7 KHS06
- ~1.4% CPU usage of the grid

70 TB storage



Generated on 2017-09-26 04:32:50 UTC



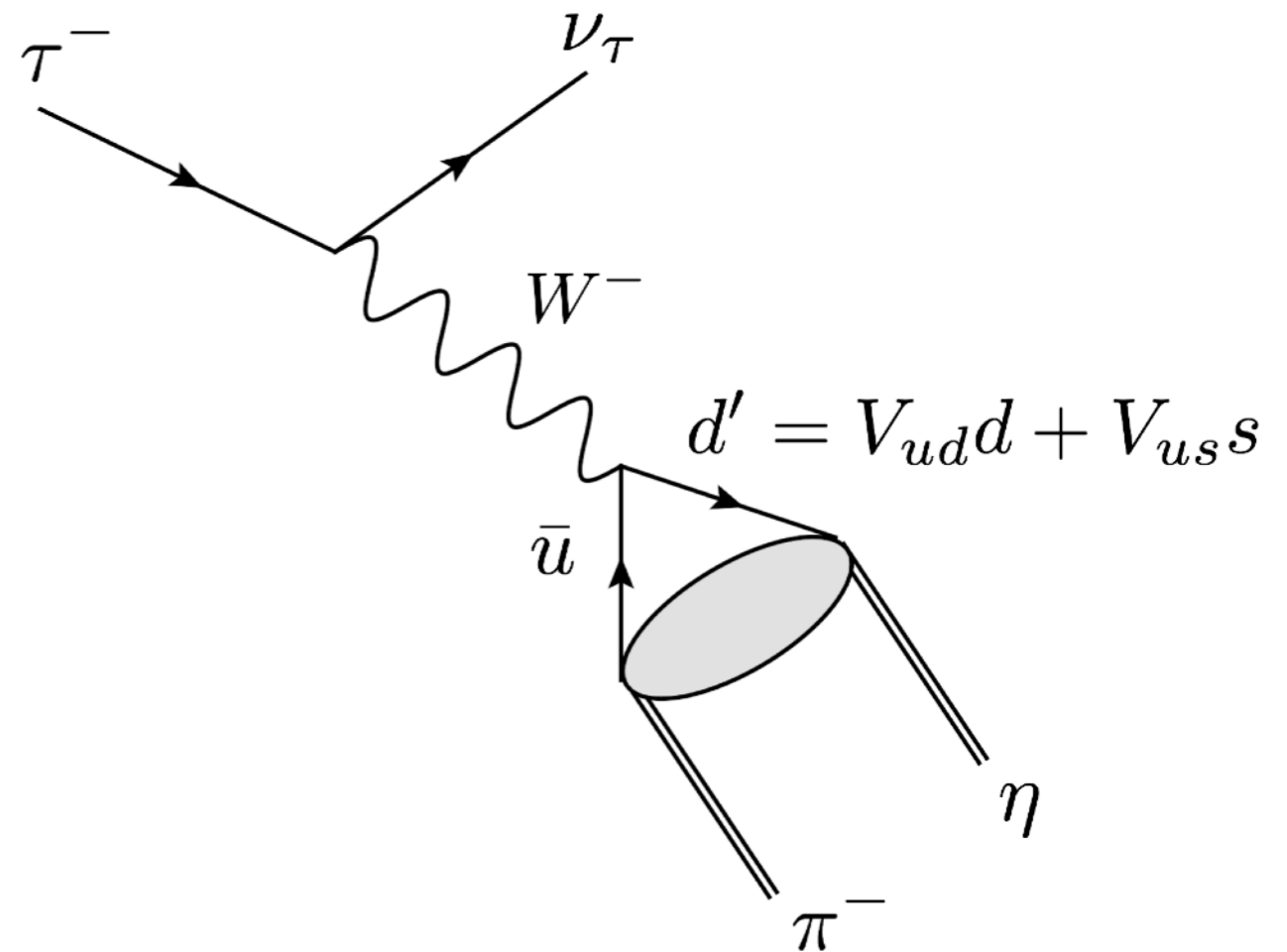
# The $\tau \rightarrow \eta \pi \nu$ decay

- In this work, we are studying the feasibility to measure the decay

$$\tau \rightarrow \eta \pi \nu,$$

in order to get information related at:

- Second class currents.
- Scalar and tensorial currents.

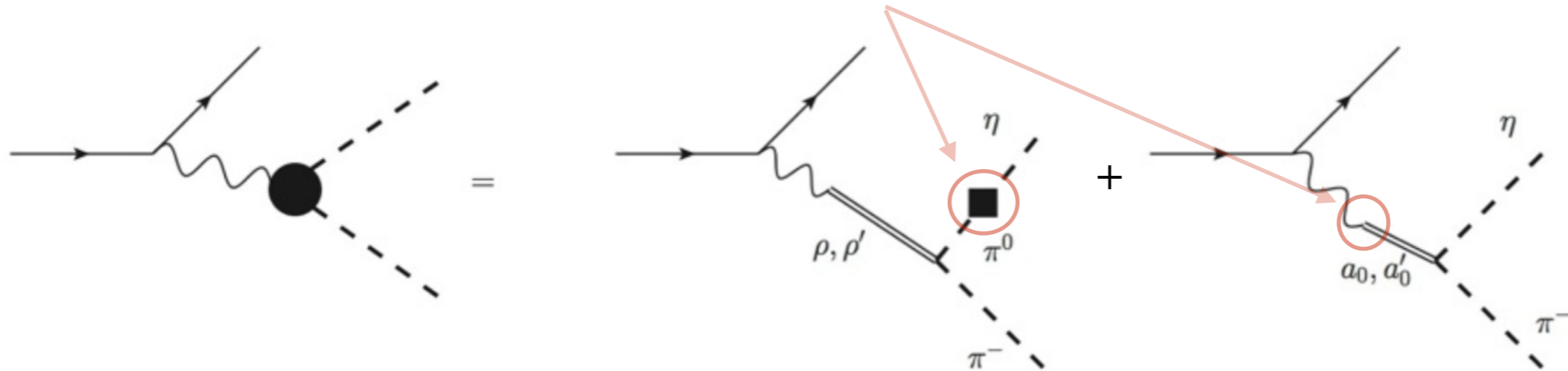


Disadvantage:  
We cannot detect  $\nu$



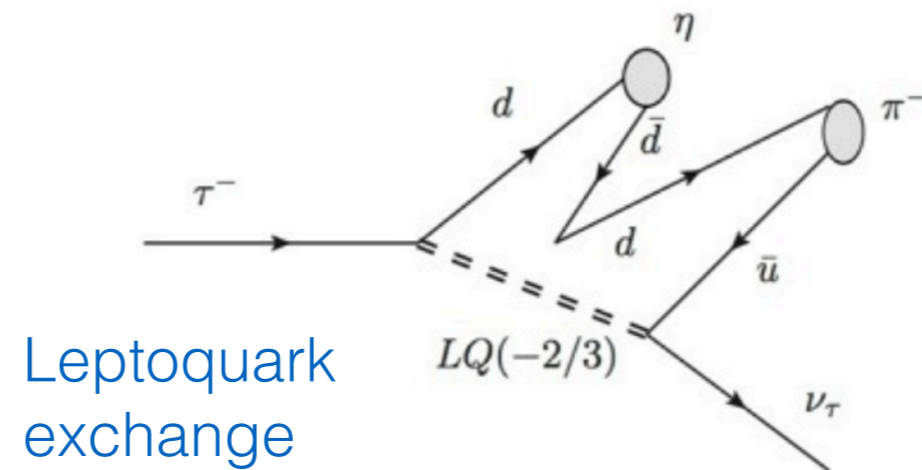
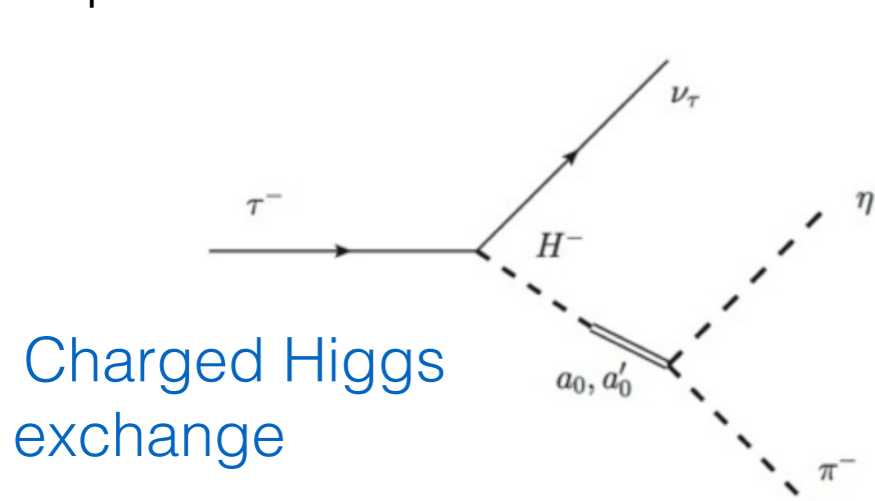
# The $\tau \rightarrow \eta \pi \nu$ decay

- Mechanisms in the SM: **isospin violation**<sup>1</sup>



$$\epsilon_{\eta\pi} = \frac{\langle \pi^0 | H | \eta \rangle}{m_\eta^2 - m_{\pi^0}^2} = \frac{\sqrt{3} m_d - m_u}{4 m_s - \bar{m}} \sim 1.5 \times 10^{-2}$$

- The corresponding suppression of the SM contribution can make new physics visible.



<sup>1</sup> R. Escribano, S. Gonzalez, P. Roig; Phys.Rev. D94 (2016) no.3, 034008

# Some recent theoretical predictions

Ref	$BR_V(x10^5)$	$BR_S(x10^5)$	$BR_{V+S}(x10^5)$	Model
[8]	0.36	1.0	1.36	MDM, 1 resonance
[9]	[0.2, 0.6]	[0.2, 2.3]	[0.4, 2.9]	MDM, 1 and 2 resonances
[10]	0.44	0.04	0.48	Nambu-Jona-Lasinio
[11]	0.13	0.20	0.33	Analiticity, Unitarity
[12]	0.26	1.41	1.67	3 coupled channels

[8] S. Nussinov + A. Soffer, PRD78, (2008)

[9] N. Paver + Riazuddin, PRD82, (2010)

[10] M. Volkov D. Kostunin, PRD82, (2012)

[11] S. Descotes-Genon+B. Moussallam, EJPC74, (2014)

[12] R. Escribano, S. Gonzalez, P. Roig; Phys.Rev. D94 (2016) no.3, 034008

Largest difference comes from scalar form factor.

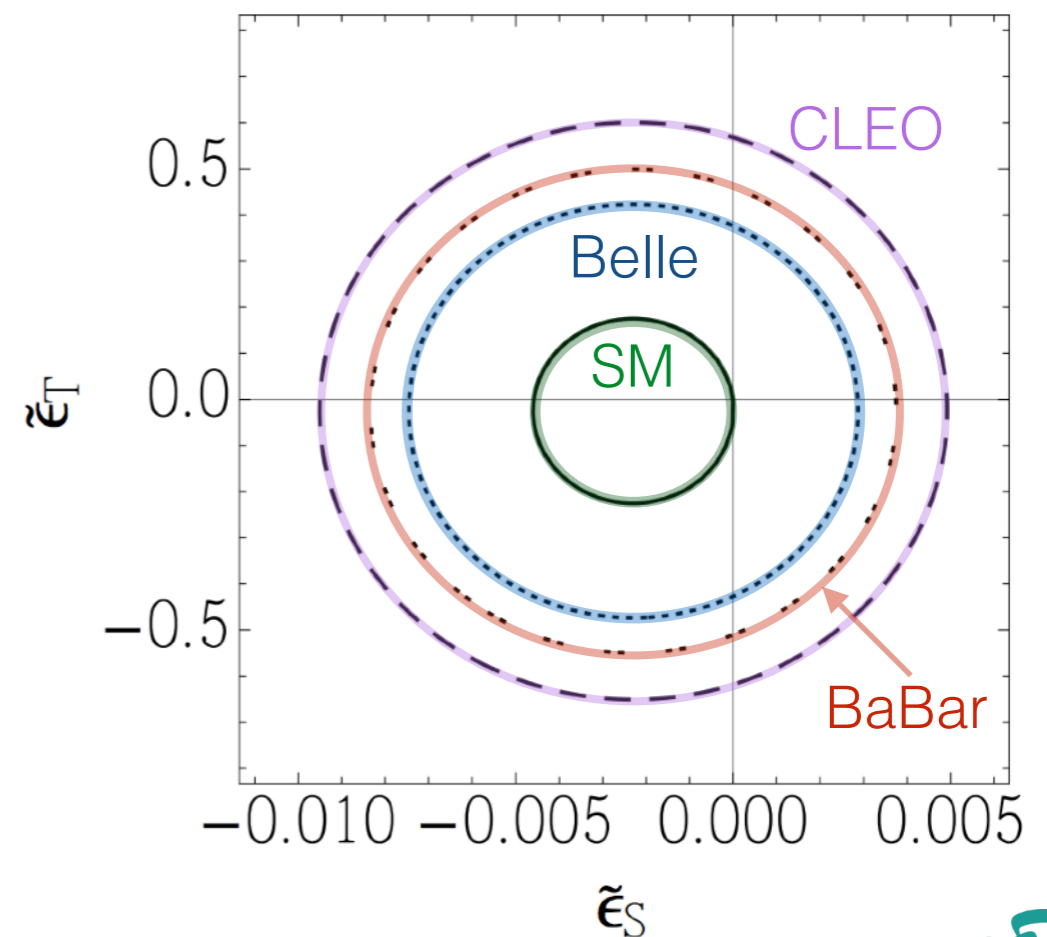
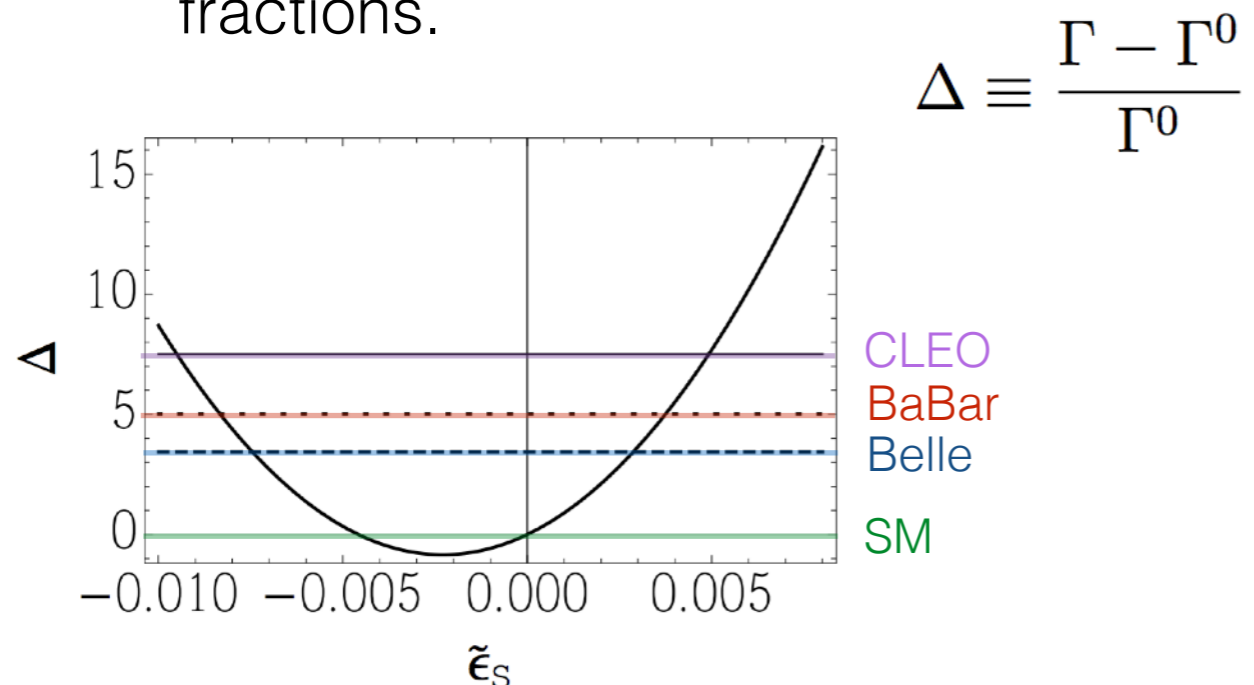
•  $BR(\tau \rightarrow \eta \pi \nu) \sim 10^{-5}$  ← Accessible at Belle II luminosity.

# The $\tau \rightarrow \eta \pi \nu$ decay

- NP contributions (scalar and tensorial currents) can be studied in the framework of an effective field theory <sup>1</sup>

$$\begin{aligned} \mathcal{M} &= \mathcal{M}_V + \mathcal{M}_S + \mathcal{M}_T \\ &= \frac{G_F V_{ud} \sqrt{S_{EW}}}{\sqrt{2}} (1 + \epsilon_L + \epsilon_R) [L_\mu H^\mu + \tilde{\epsilon}_S LH + 2\tilde{\epsilon}_T L_{\mu\nu} H^{\mu\nu}], \end{aligned}$$

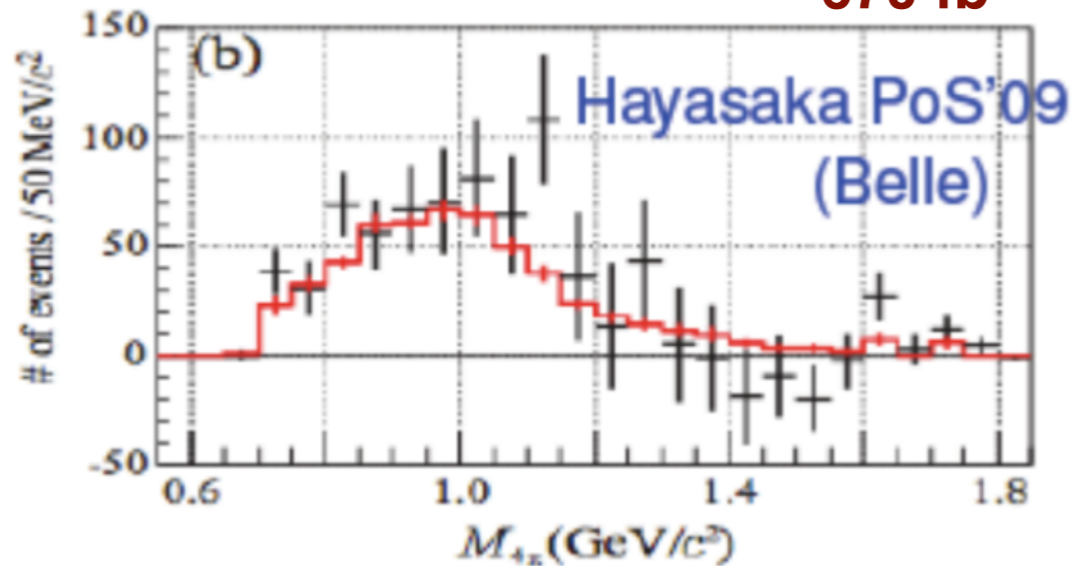
- Constraints on scalar and tensor couplings can be obtained from experimental upper limits on branching fractions.



<sup>1</sup> E. A. Garcés, MHV, G. López Castro, P. Roig; arXiv:1708.07802

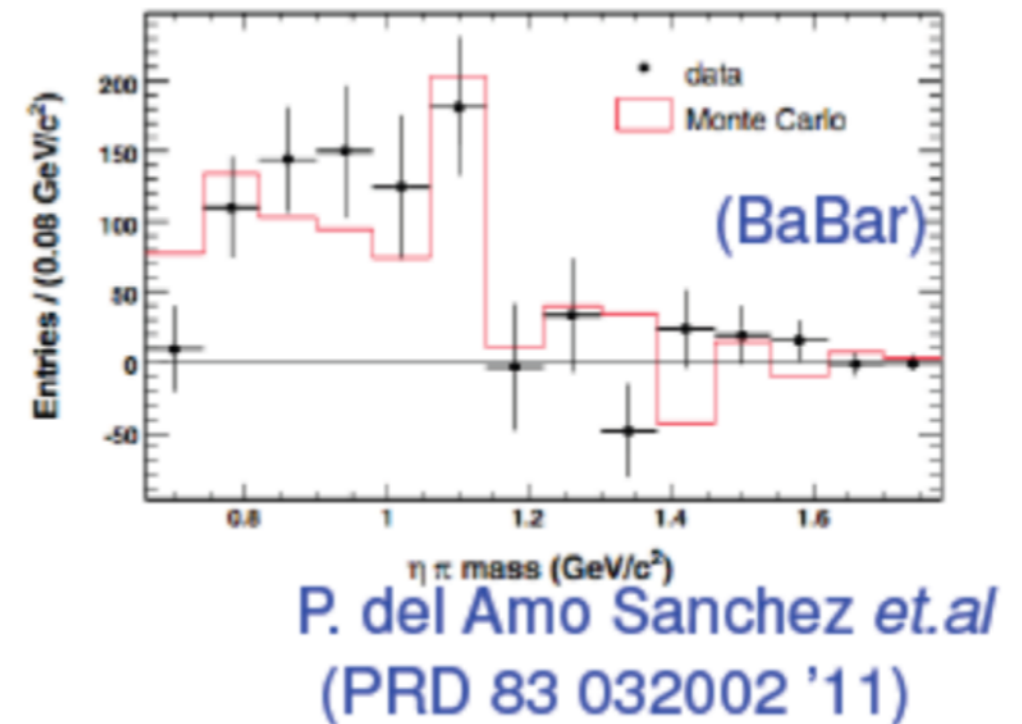
# Previous Results

670 fb<sup>-1</sup>



$$BR_{exp}^{Belle} < 7.3 \cdot 10^{-5} \quad 90\%CL$$

470 fb<sup>-1</sup>



$$BR_{exp}^{BaBar} < 9.9 \cdot 10^{-5} \quad 95\%CL$$

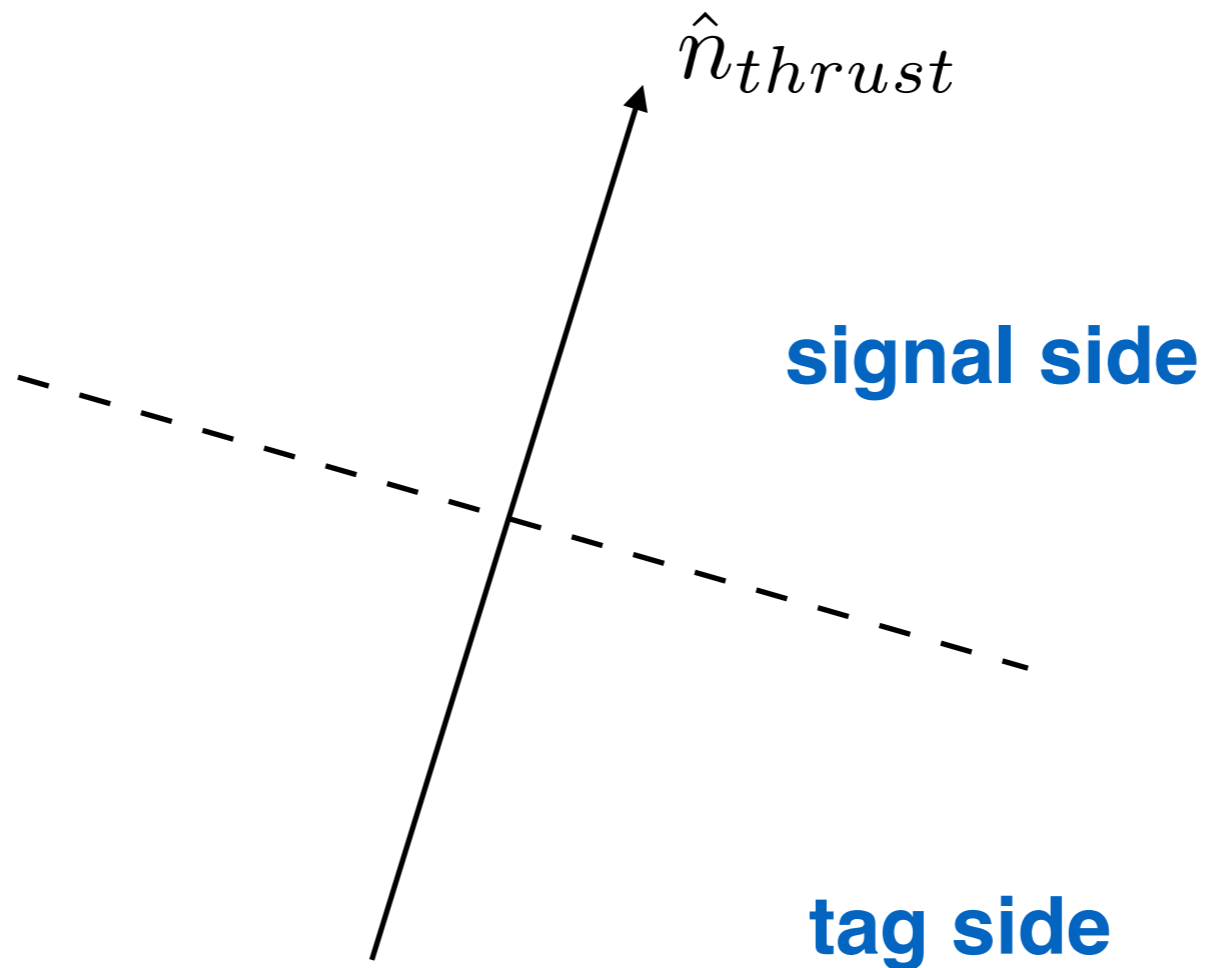
- This decay mode should have already been discovered if there were no strong background.
- Control of the background is essential.

# Thrust axis

- Thrust axis:  $\hat{n}_{thrust}$  such that  $V_{thrust}$  is maximum.

$$V_{thrust} = \frac{\sum_i |\vec{p}_i^{cm} \cdot \hat{n}_{thrust}|}{\sum_i |\vec{p}_i^{cm}|}$$

The thrust axis define a plane which splits the space in two.



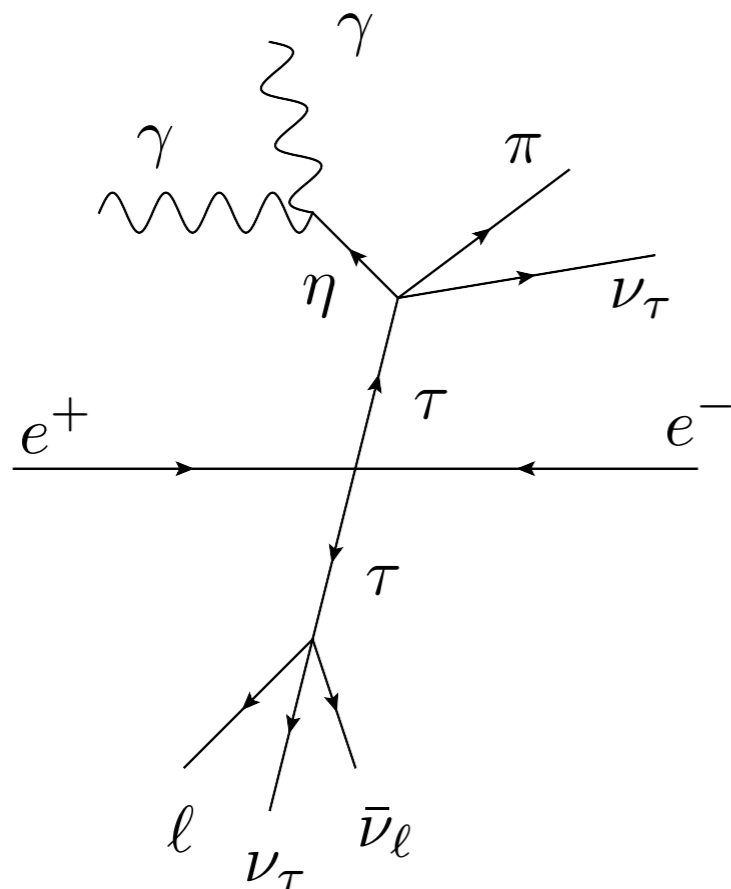
# 2 ways to reconstruct $\eta$

- Thrust axis:  $\hat{n}_{thrust}$  such that  $V_{thrust}$  is maximum.

$$V_{thrust} = \frac{\sum_i |\vec{p}_i^{cm} \cdot \hat{n}_{thrust}|}{\sum_i |\vec{p}_i^{cm}|}$$

1-prong

**BR( $\eta \rightarrow \gamma\gamma$ ) = 39.41%**

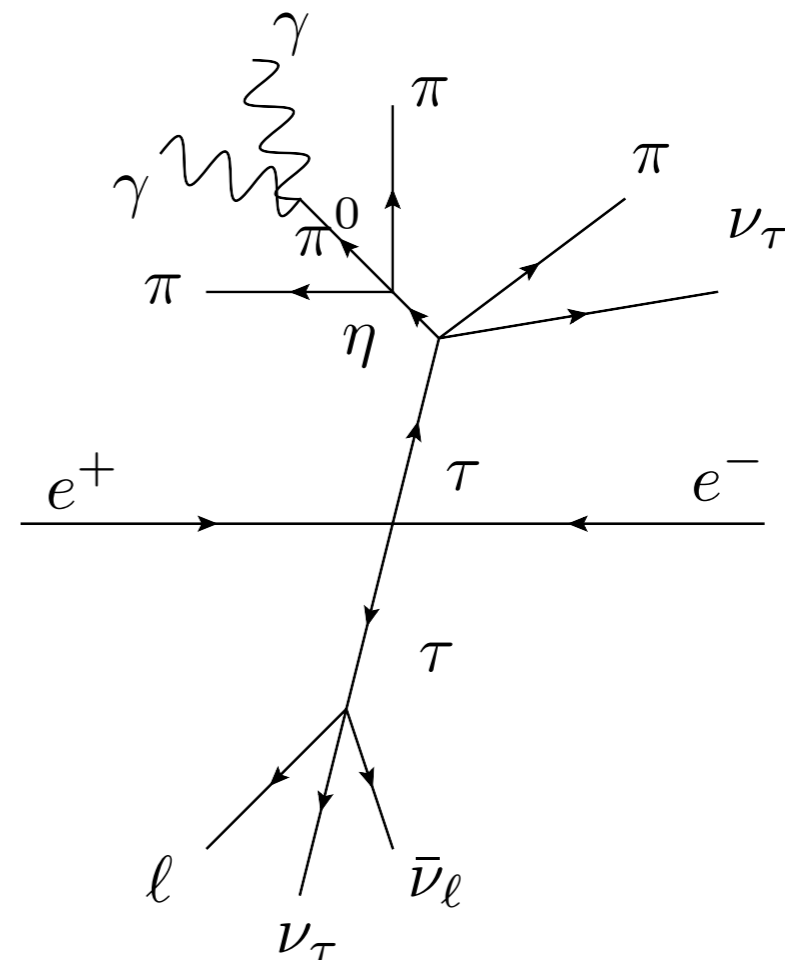


Signal side

Tag side

3-prong

**BR( $\eta \rightarrow \pi\pi\pi^0$ ) = 22.92%**

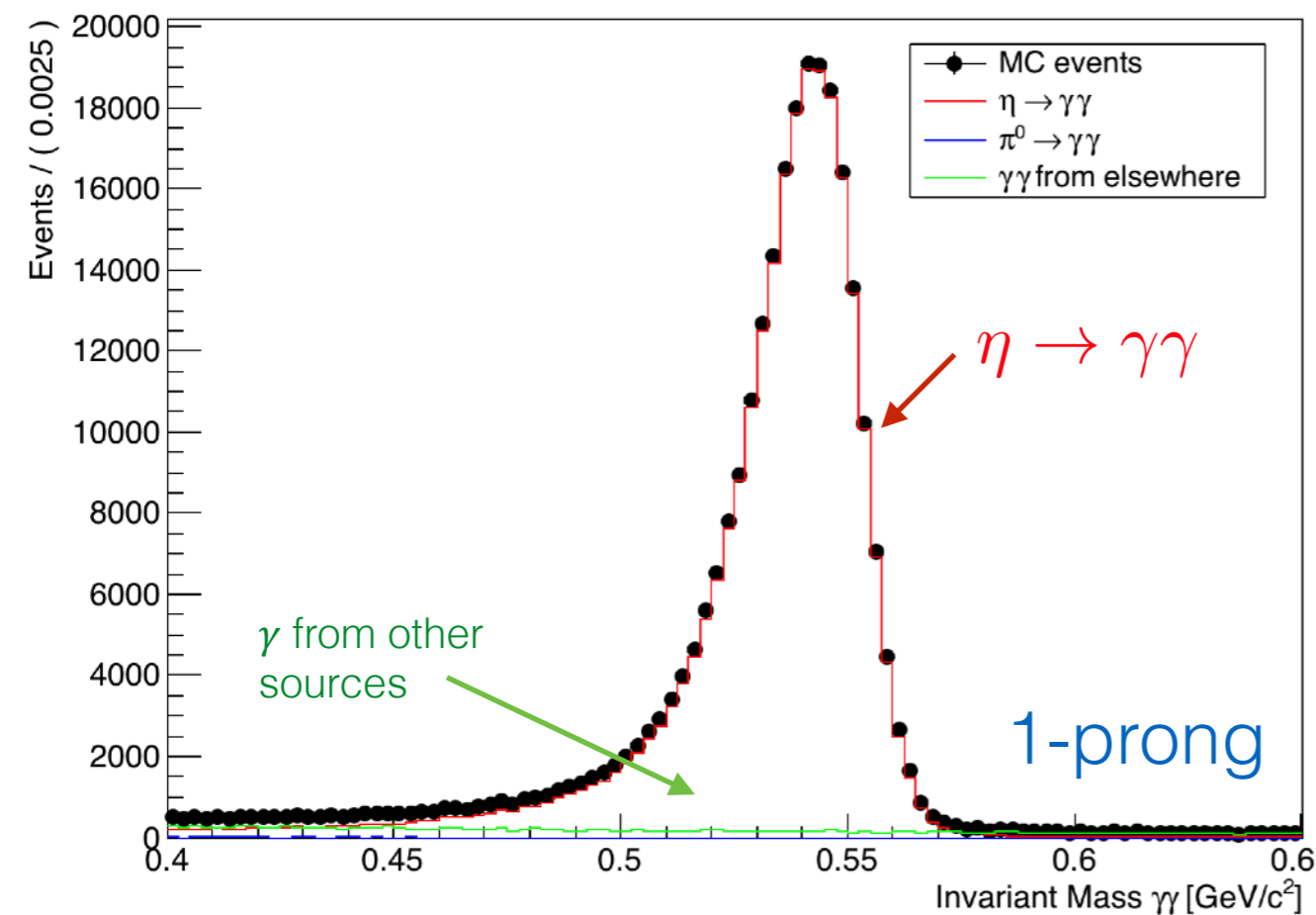


# $\tau \rightarrow \eta \pi \nu$ signal events

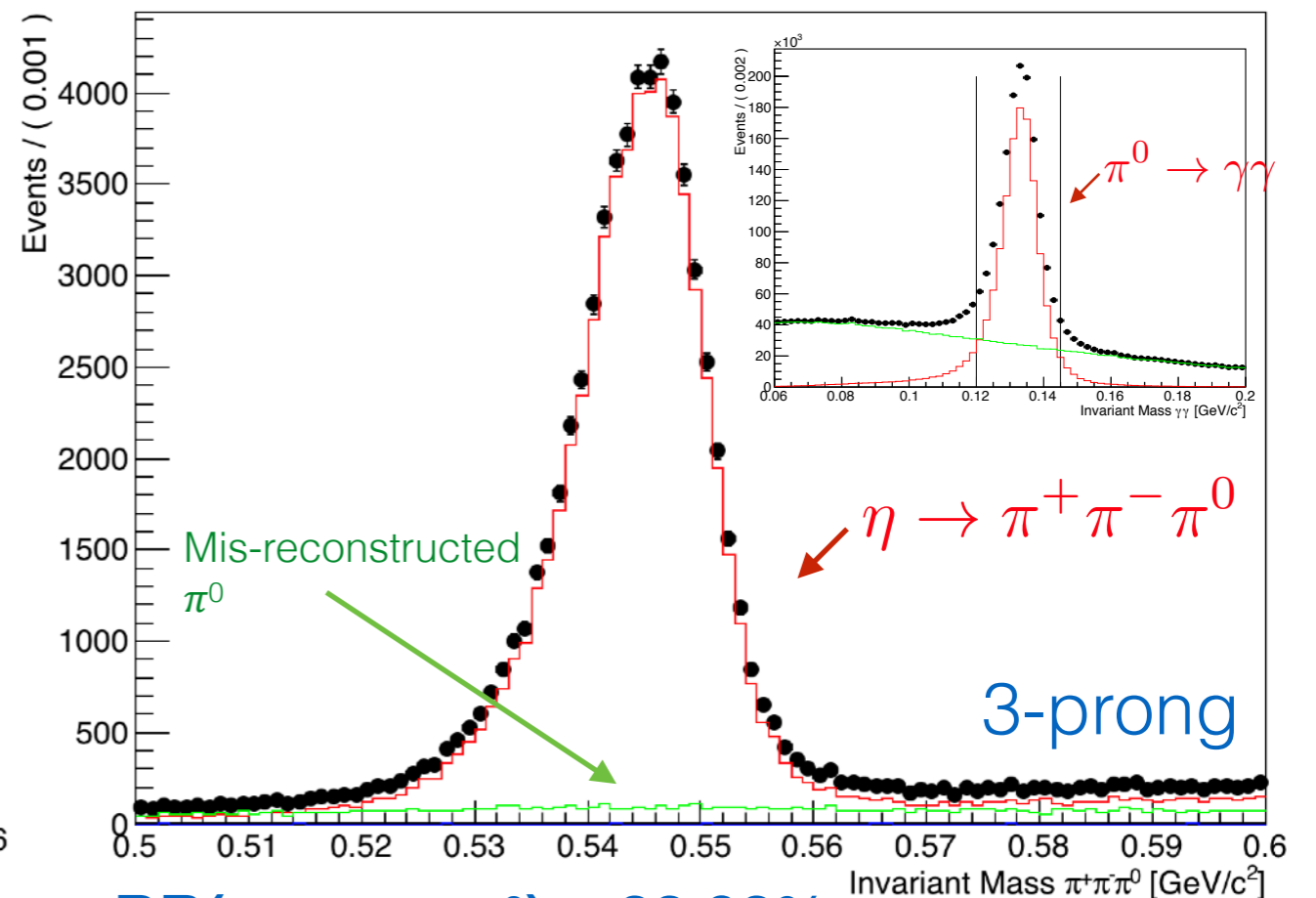
- Selection criteria :tag + 1 or 3 charged + 2 or 3  $\gamma$ .
- Signal events generated: 4M.  
(2M for training and 2M for sensitivity study).

Eff: 13.56%

Eff: 3.70%



$$\text{BR}(\eta \rightarrow \gamma\gamma) = 39.41\%$$



$$\text{BR}(\eta \rightarrow \pi\pi\pi^0) = 22.92\%$$

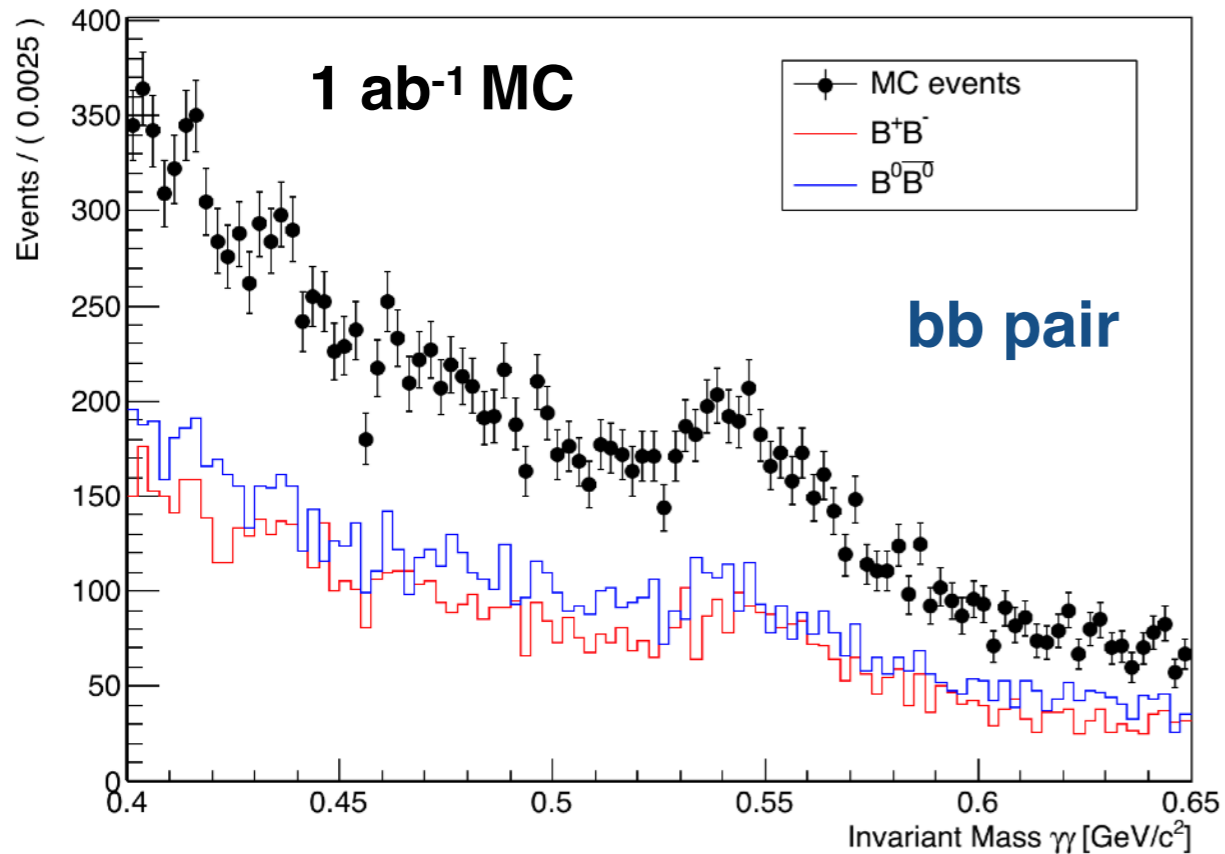
# $\tau \rightarrow \eta \pi \nu$ bkg events

## 1-prong

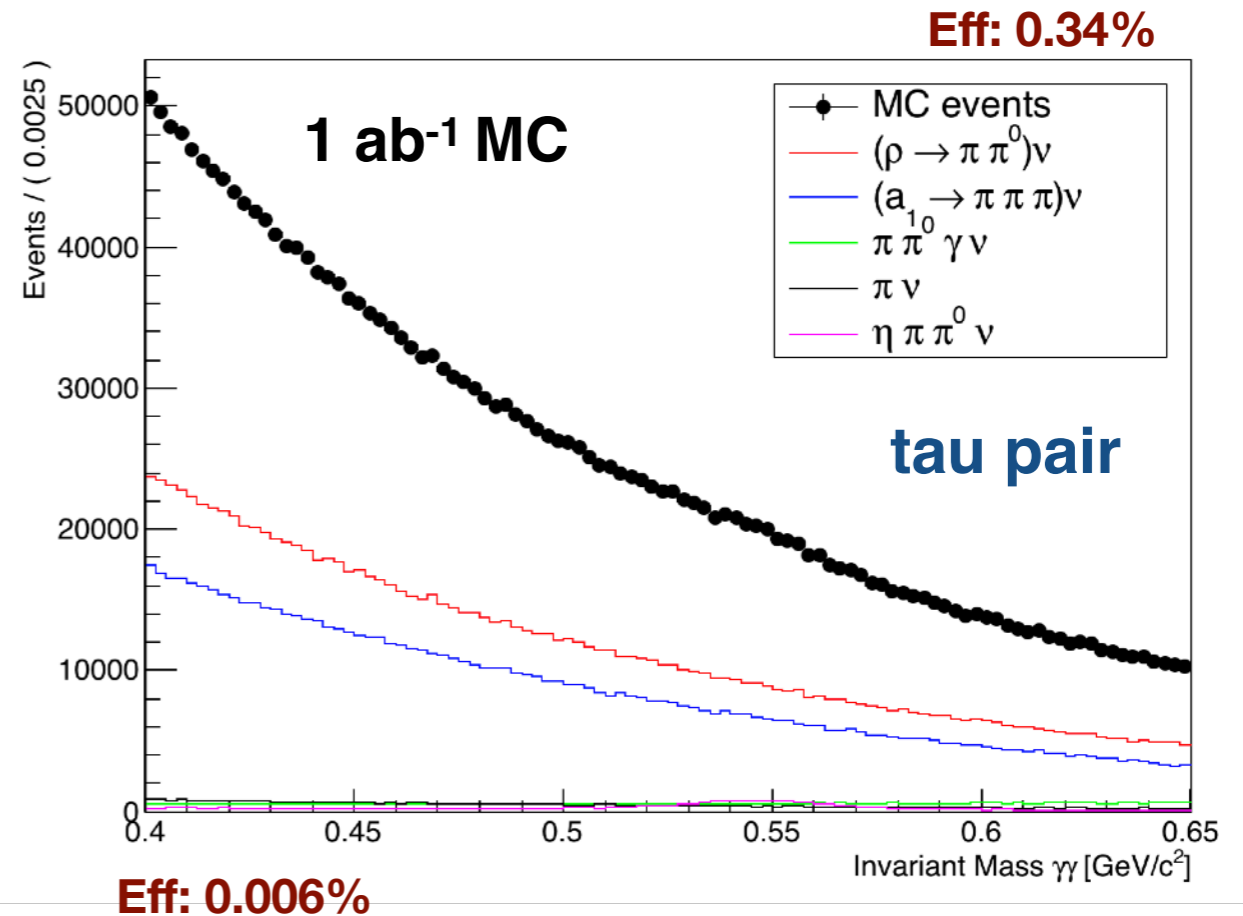
- Background sources:
  - $\tau\tau$  pair
  - $b\bar{b}$  pair
  - $q\bar{q}$  pair

$\pi^0$  veto applied.

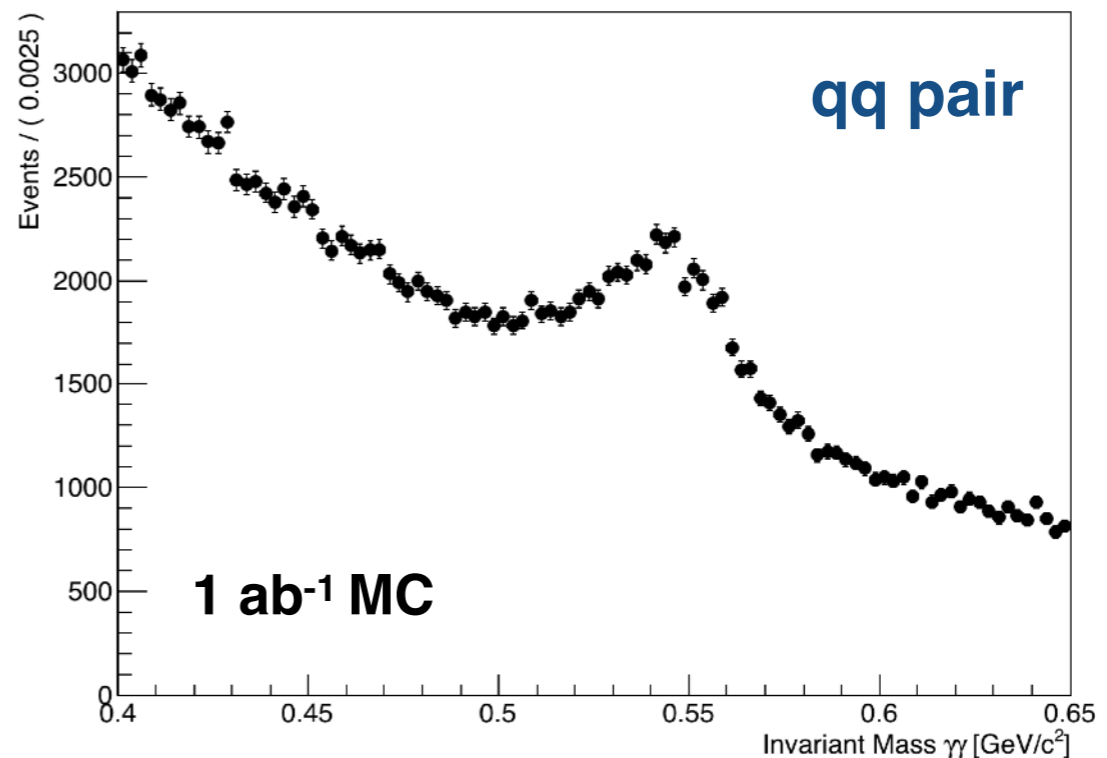
Eff: 0.002%



Michel H. Villanueva



Eff: 0.006%

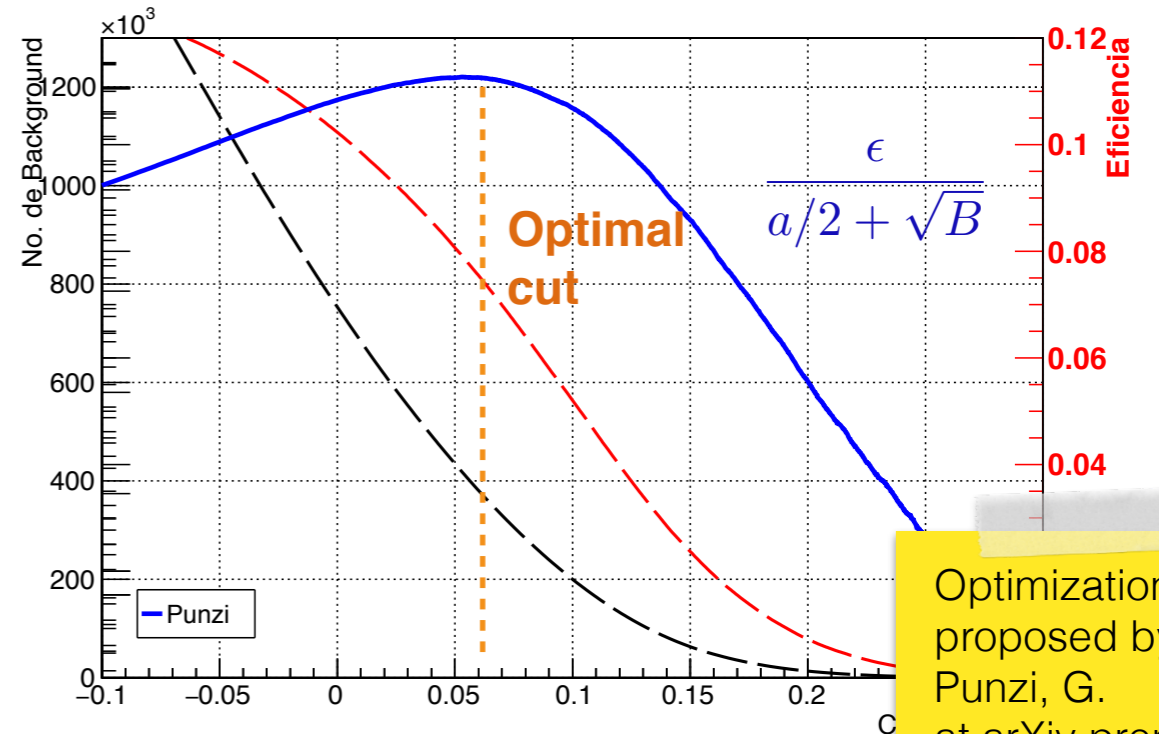




# BDT variables (1-prong)

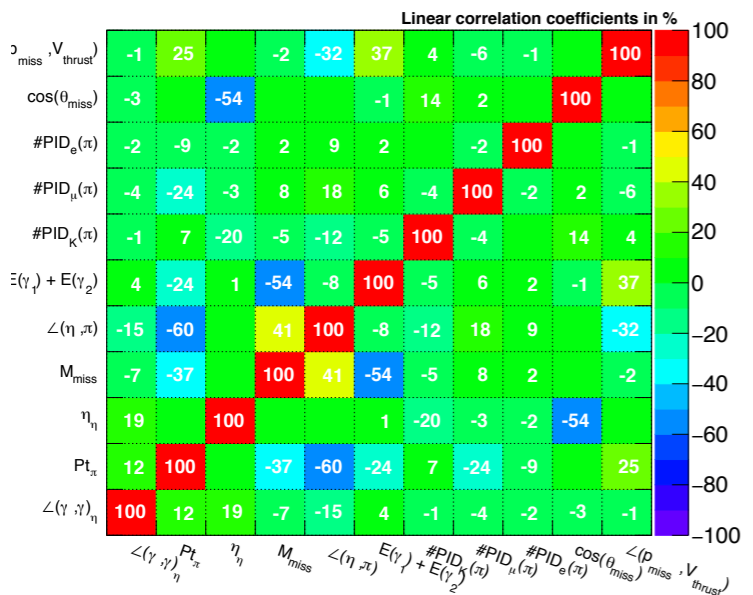
TMVA used for this test.

- $\angle(\eta, \pi)$
- $\angle(p_{\text{miss}}, V_{\text{thrust}})$
- $M_{\text{miss}}$
- $P_t(\pi)$
- $\eta(\eta)$
- $\angle(\gamma, \gamma)_\eta$
- $\cos(\theta_{\text{miss}})$
- $\text{PID}_e(\pi)$
- $\text{PID}_\mu(\pi)$
- $\text{PID}_K(\pi)$
- $E(\gamma)$

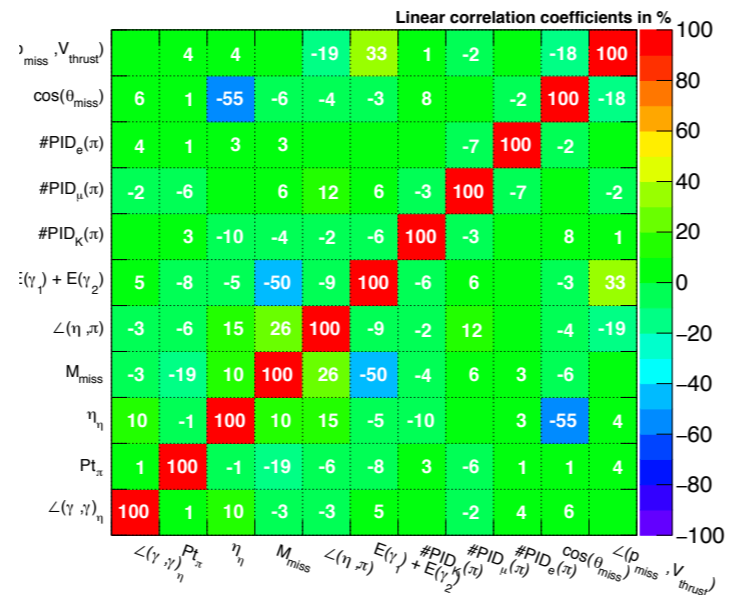


Optimization proposed by Punzi, G. at arXiv preprint physics/0308063

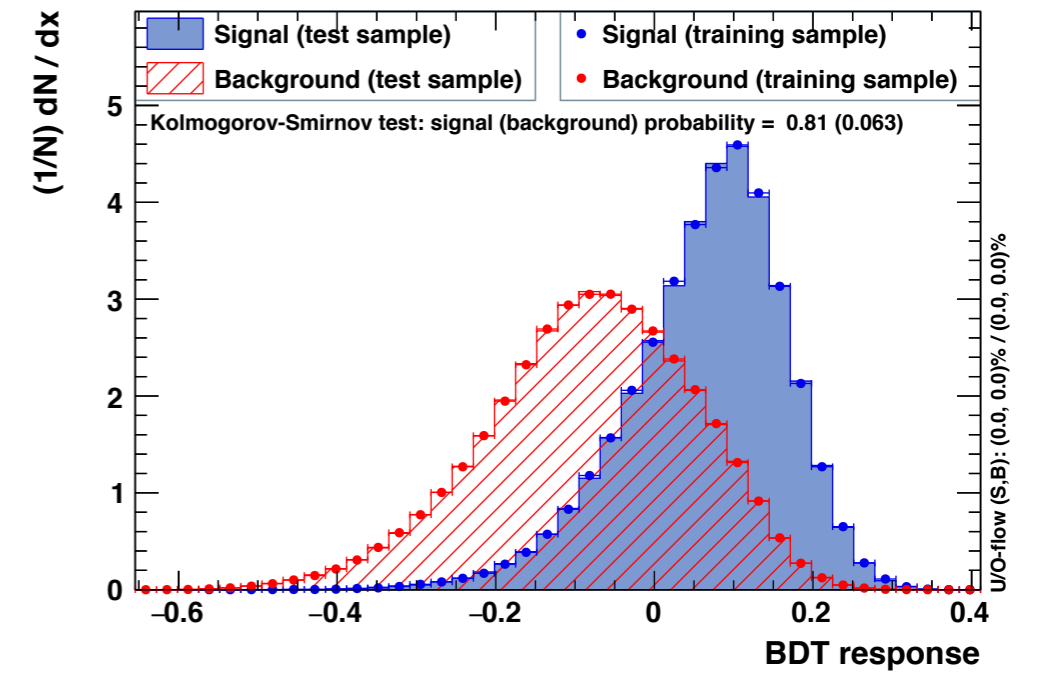
Correlation Matrix (signal)



Correlation Matrix (background)



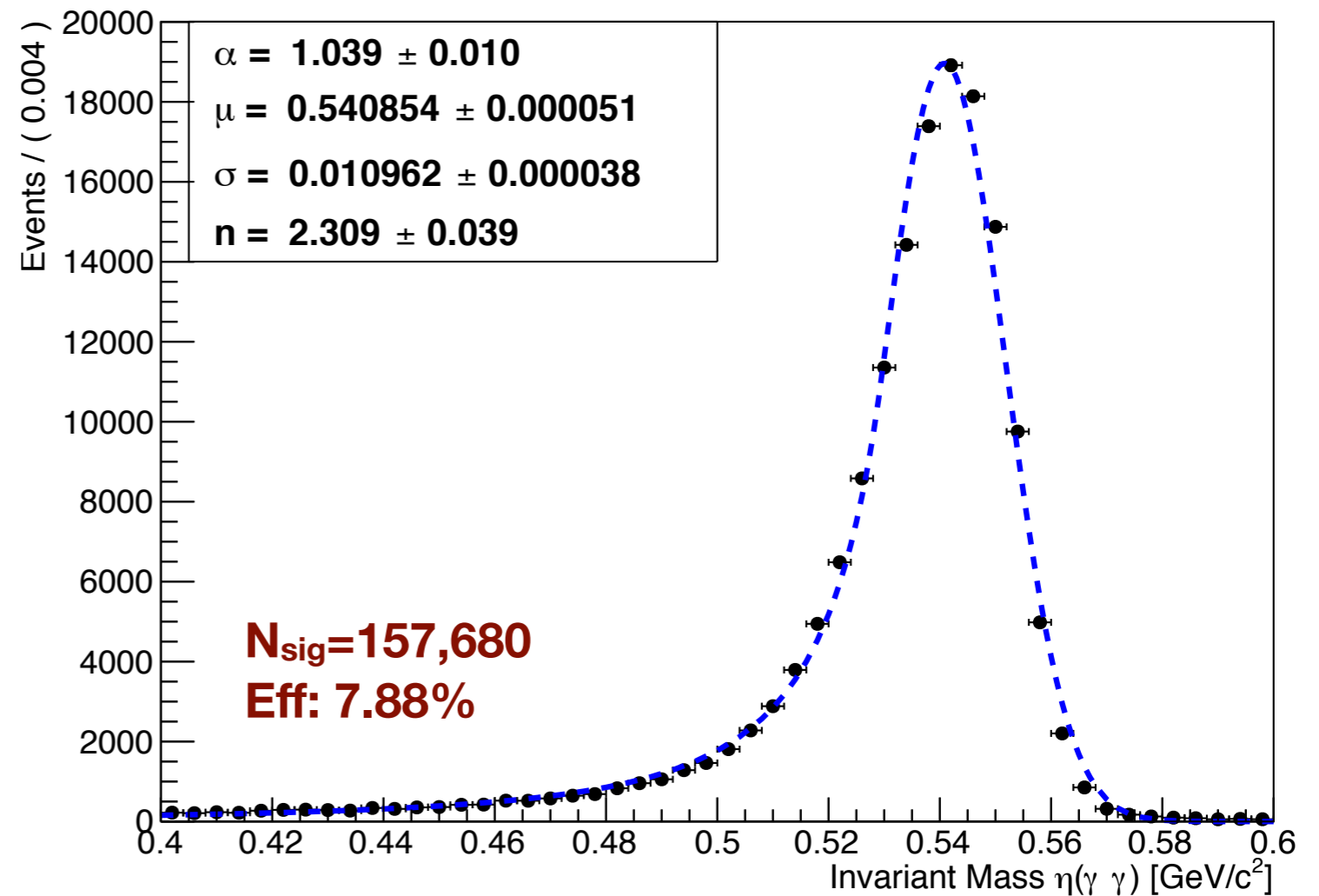
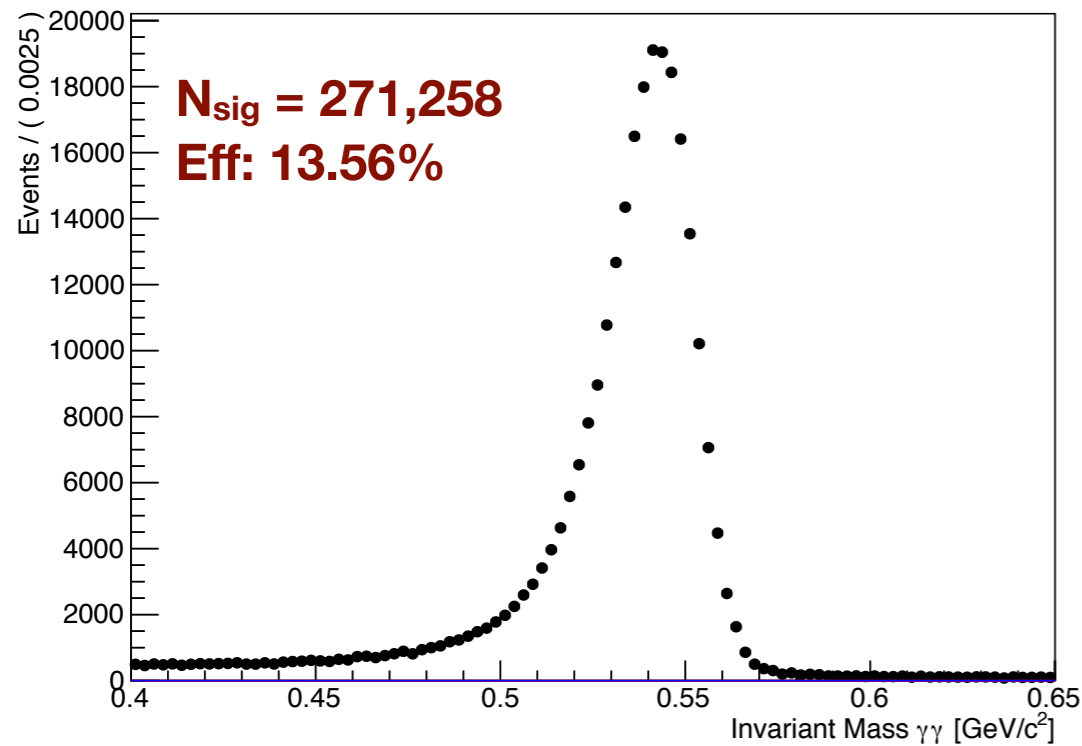
TMVA overtraining check for classifier: BDT



# Optimal BDT cut

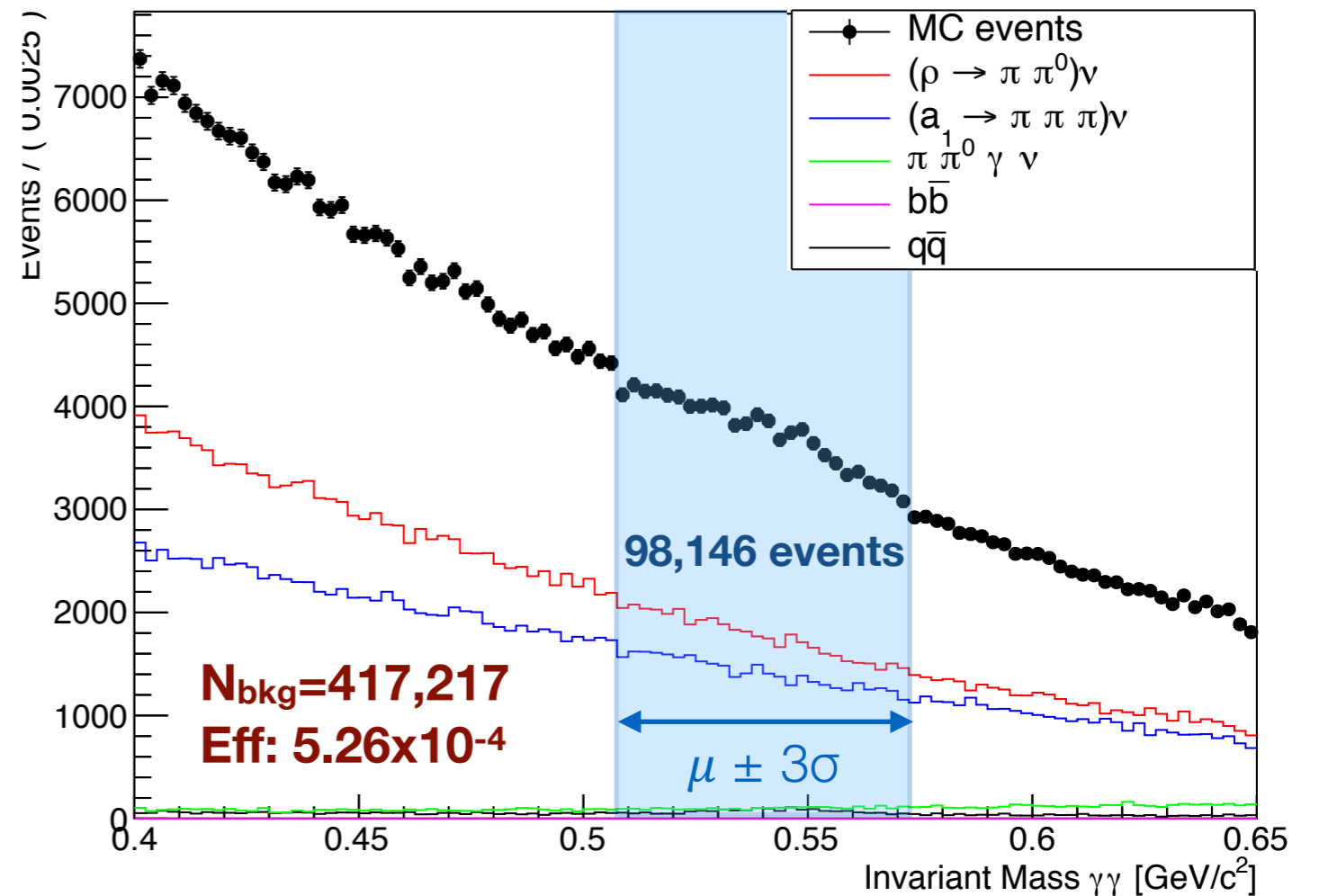
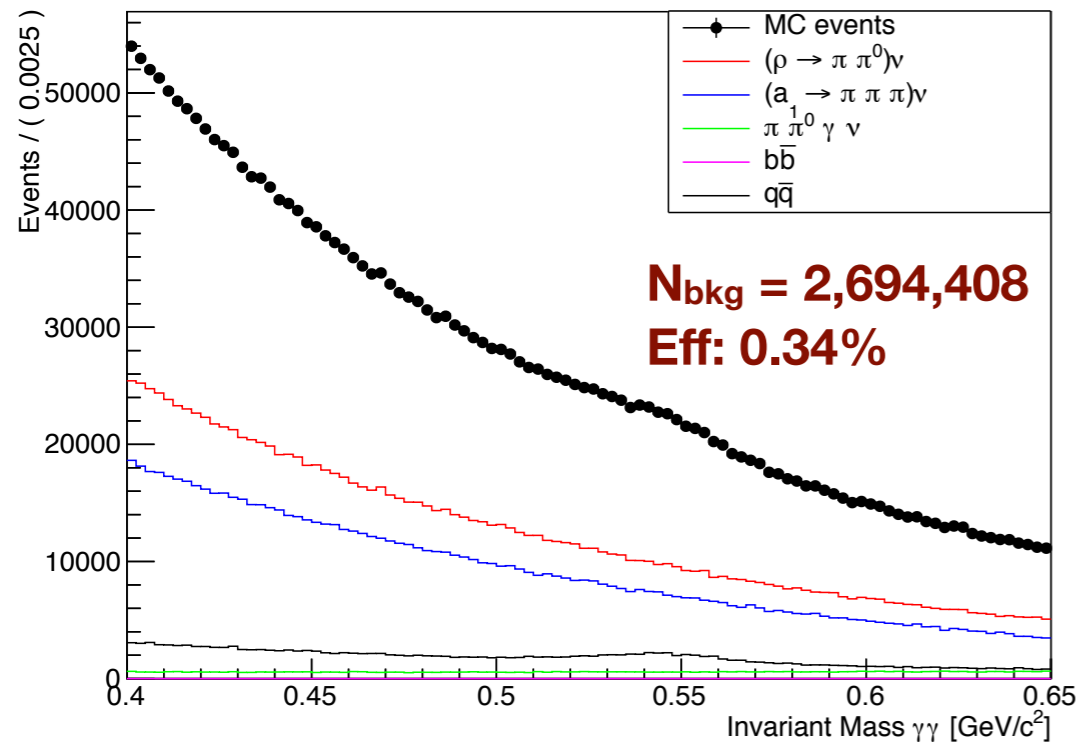
Signal  
1-prong

$\text{Eff}_{\text{cut}} = 41.87\%$



# Optimal BDT cut

## Background 1-prong



**Eff<sub>cut</sub> = 84.51%**

# $\tau \rightarrow \eta \pi \nu$ bkg events

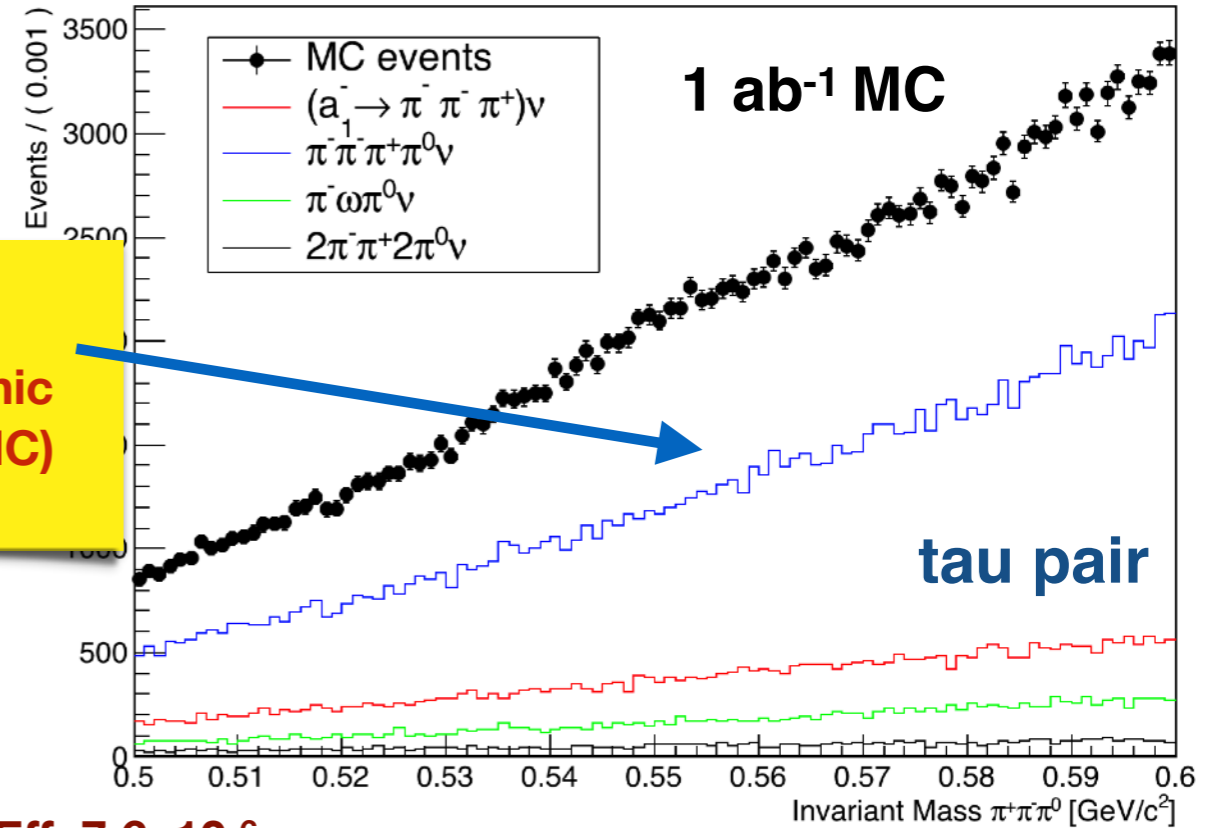
## 3-prong

• Background sources:

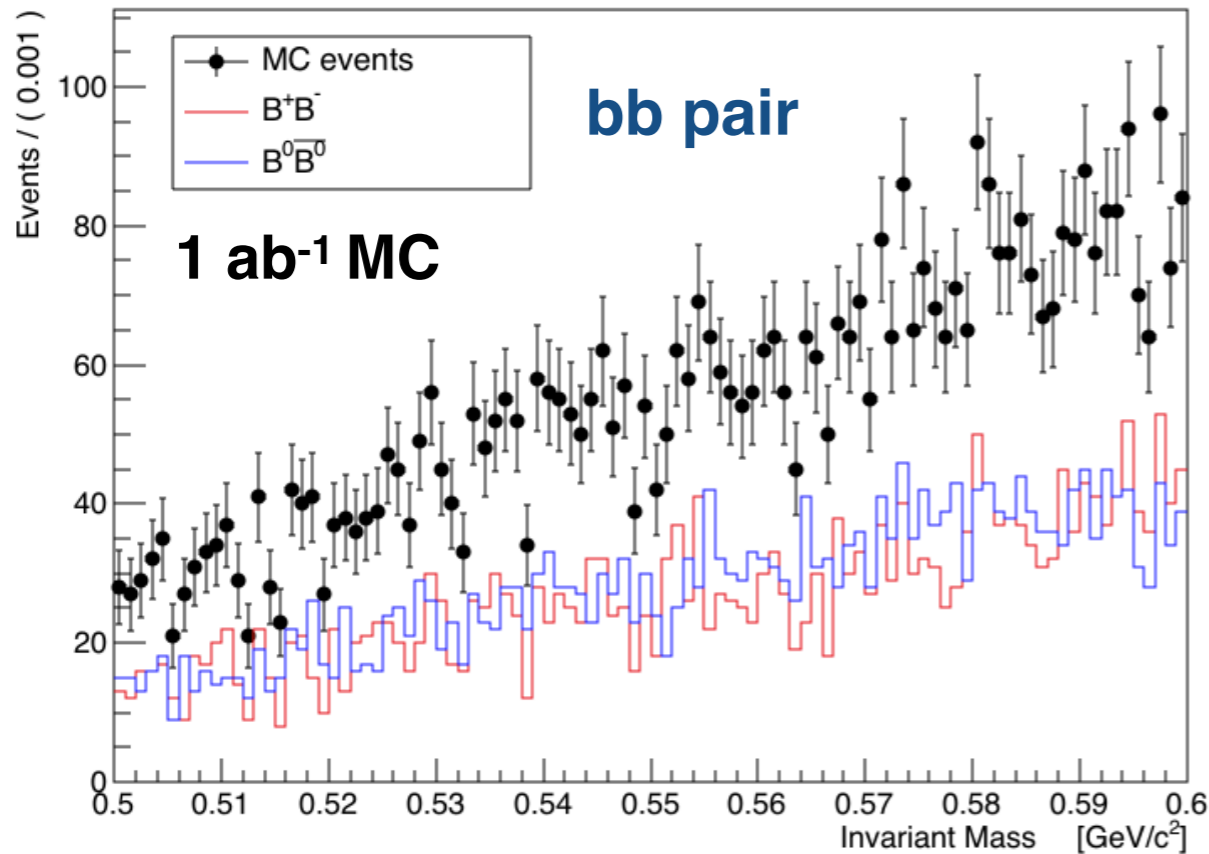
- $\tau\tau$  pair
- $bb$  pair
- $qq$  pair

**$3\pi\pi^0$  is the mayor issue.**  
**(This depends of the hadronic input in the generation of MC)**

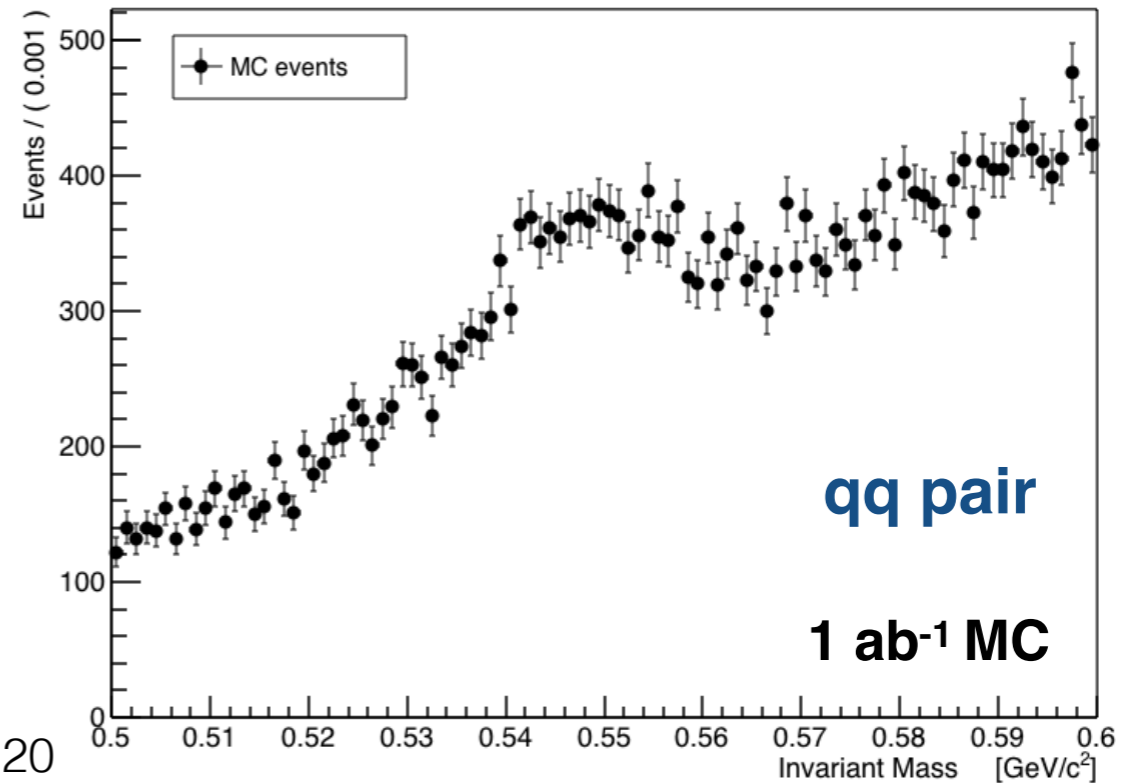
Eff: 0.028%



Eff:  $5.6 \times 10^{-6}$

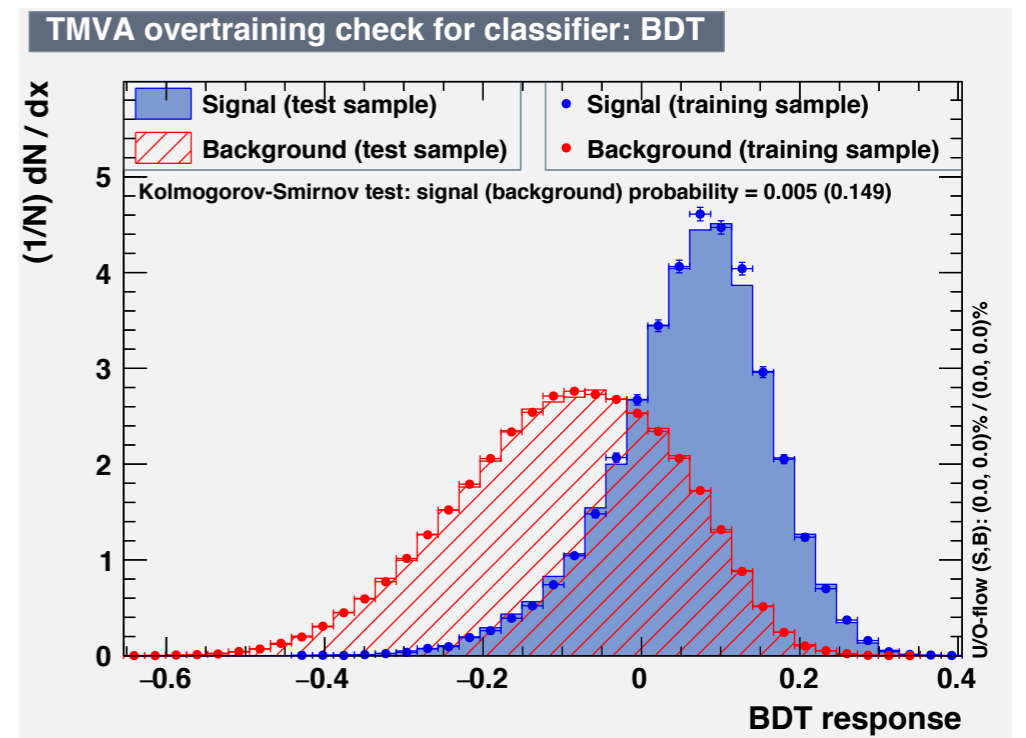
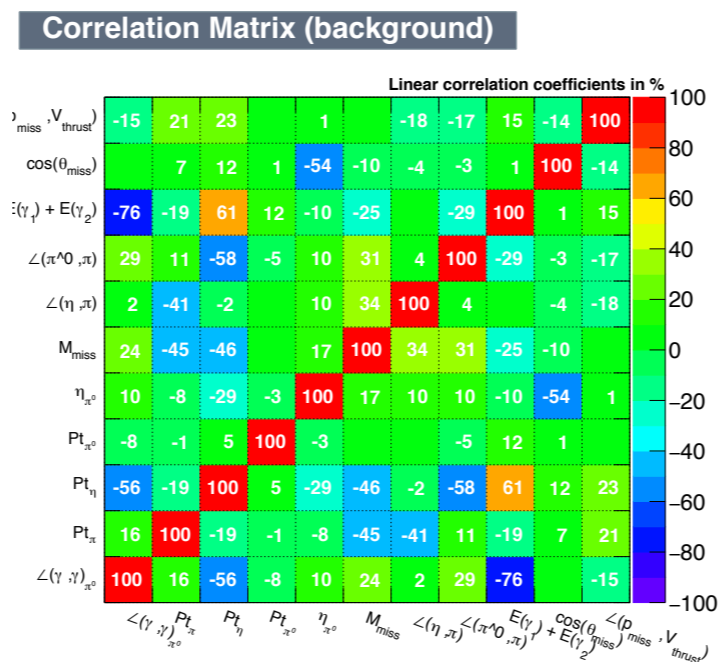
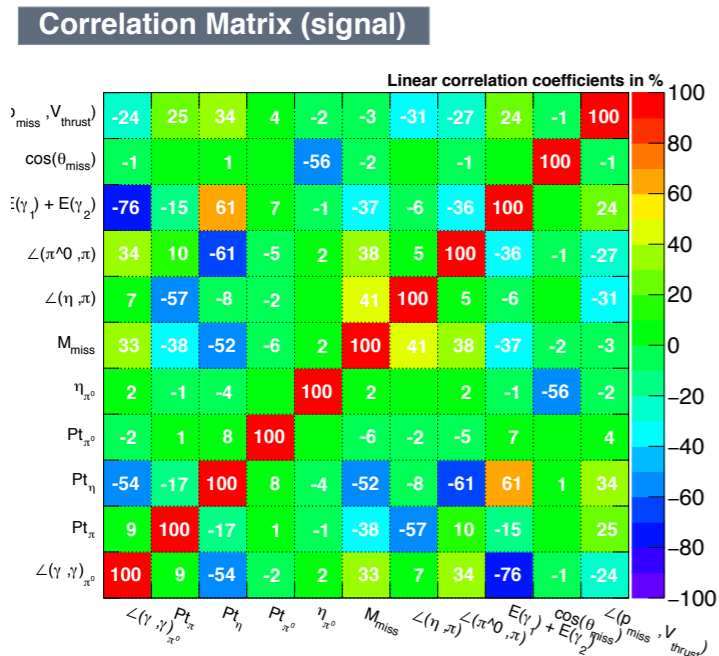
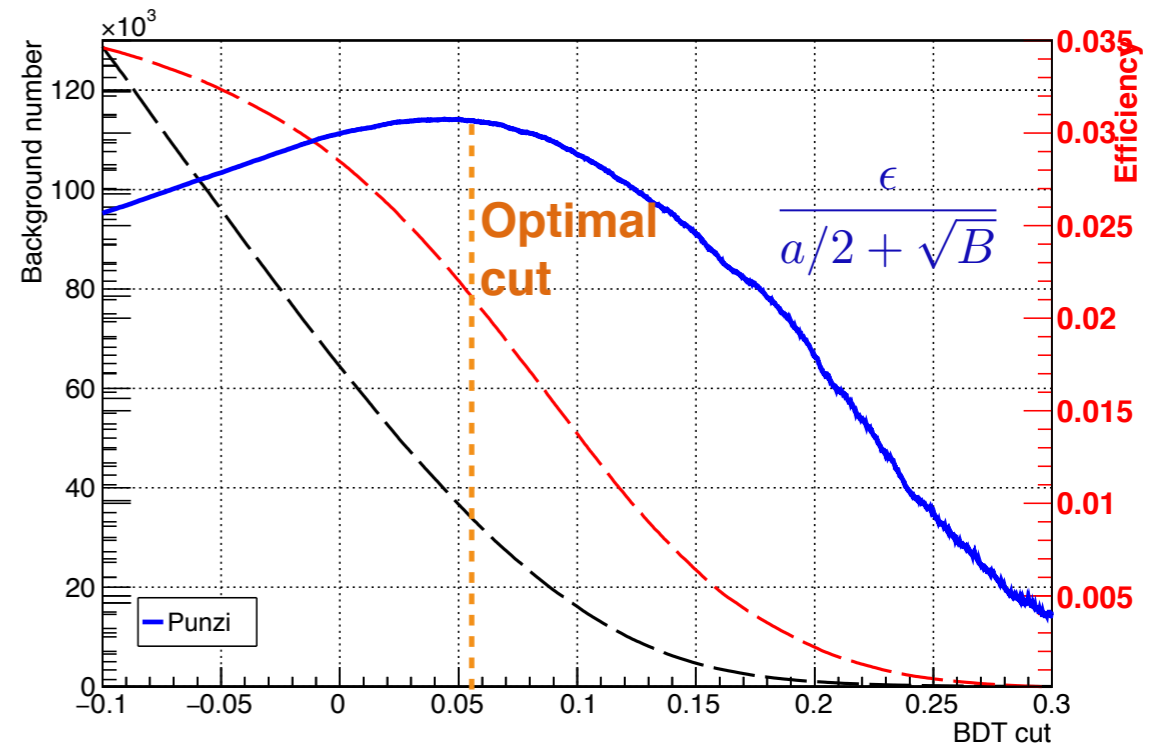


Eff:  $7.6 \times 10^{-6}$



# BDT variables (3-prong)

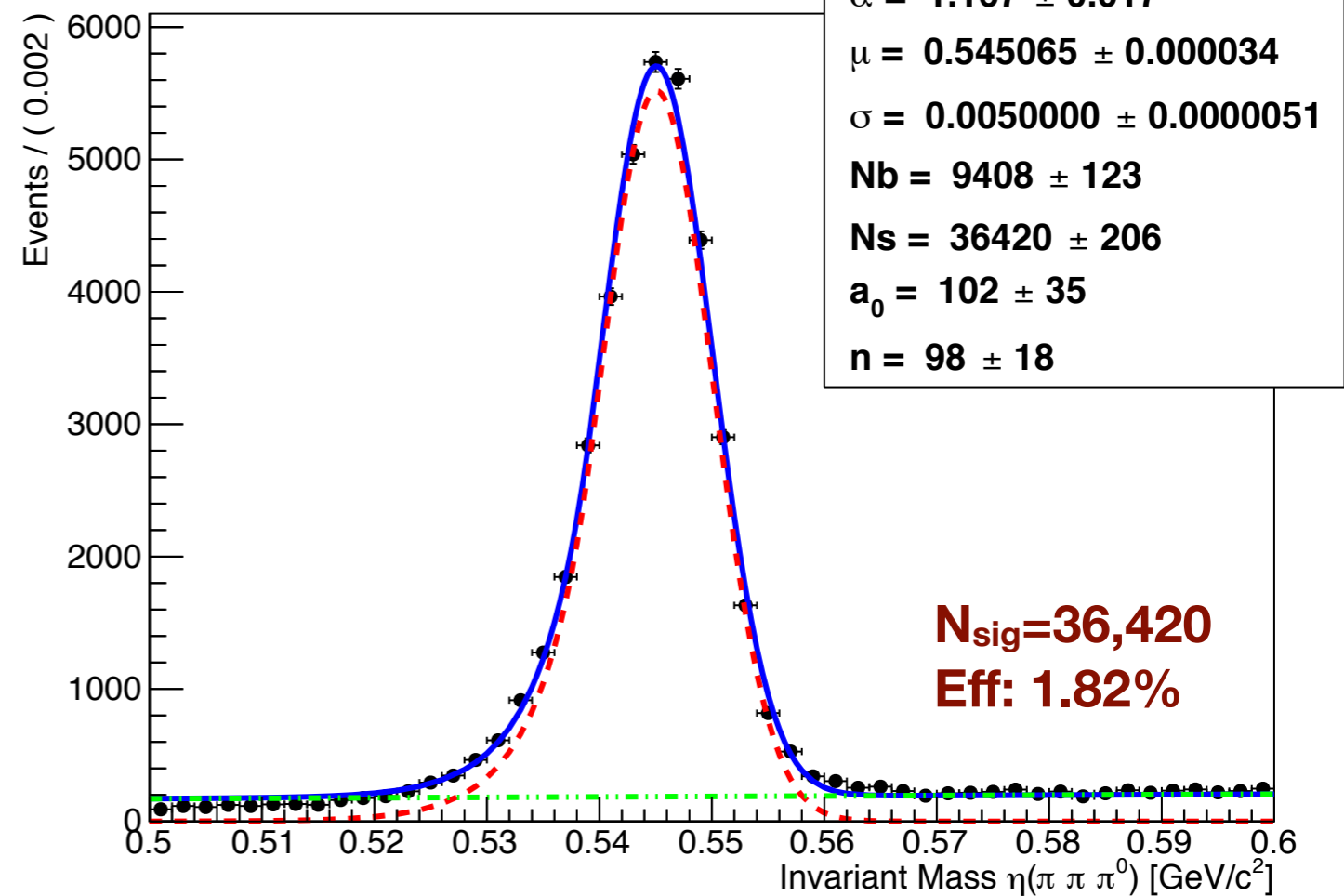
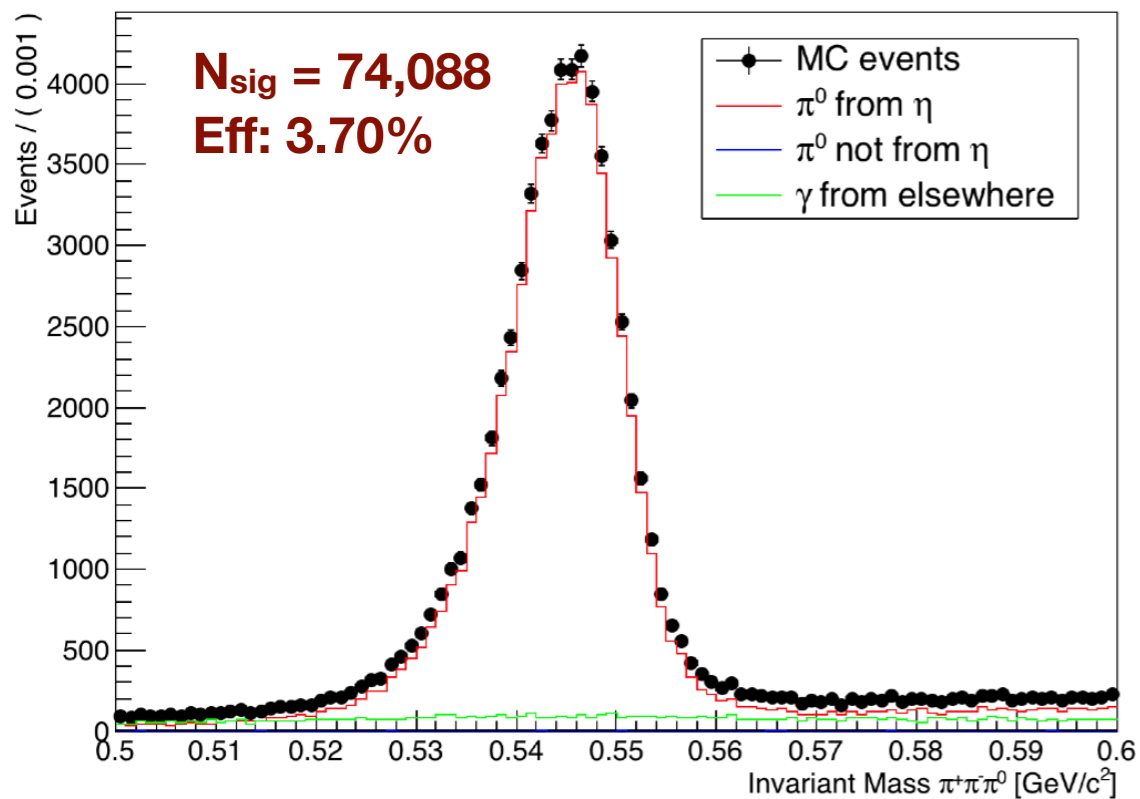
- $\angle(\eta, \pi)$
- $\angle(p_{\text{miss}}, V_{\text{thrust}})$
- $\angle(\pi, \pi^0)$
- $\angle(\gamma, \gamma)\pi^0$
- $M_{\text{miss}}$
- $P_t(\pi)$
- $P_t(\eta)$
- $P_t(\pi^0)$
- $\eta(\pi^0)$
- $E(\gamma)$



# Optimal BDT cut

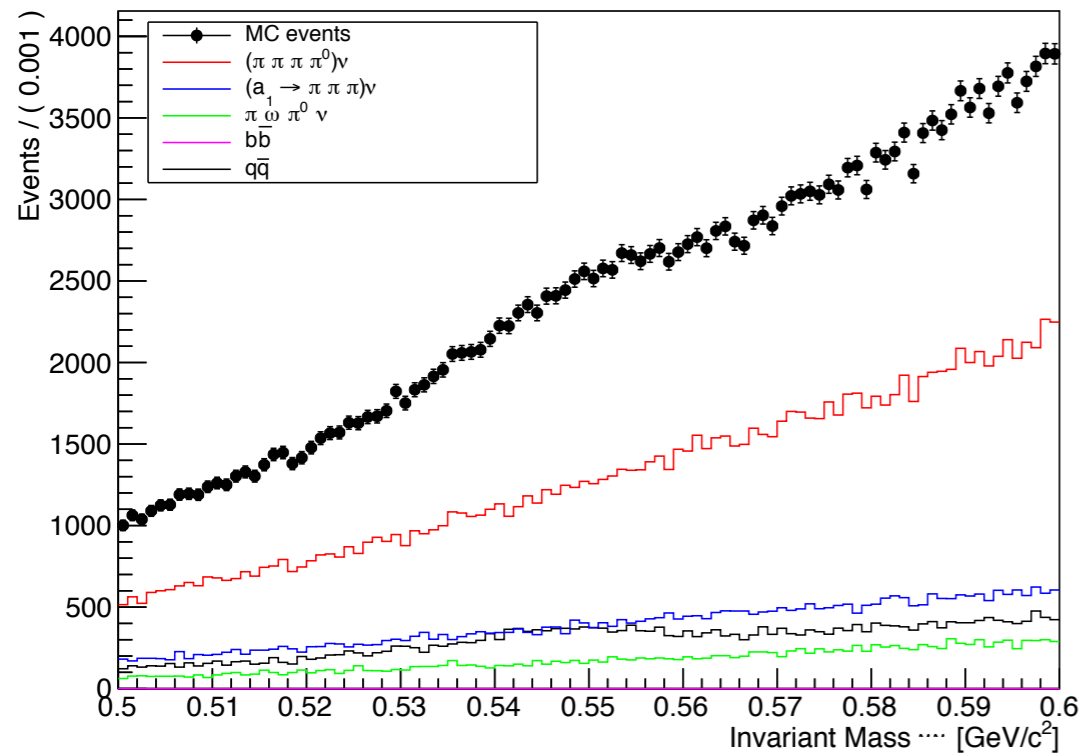
Signal  
3-prong

$\text{Eff}_{\text{cut}} = 38.14\%$



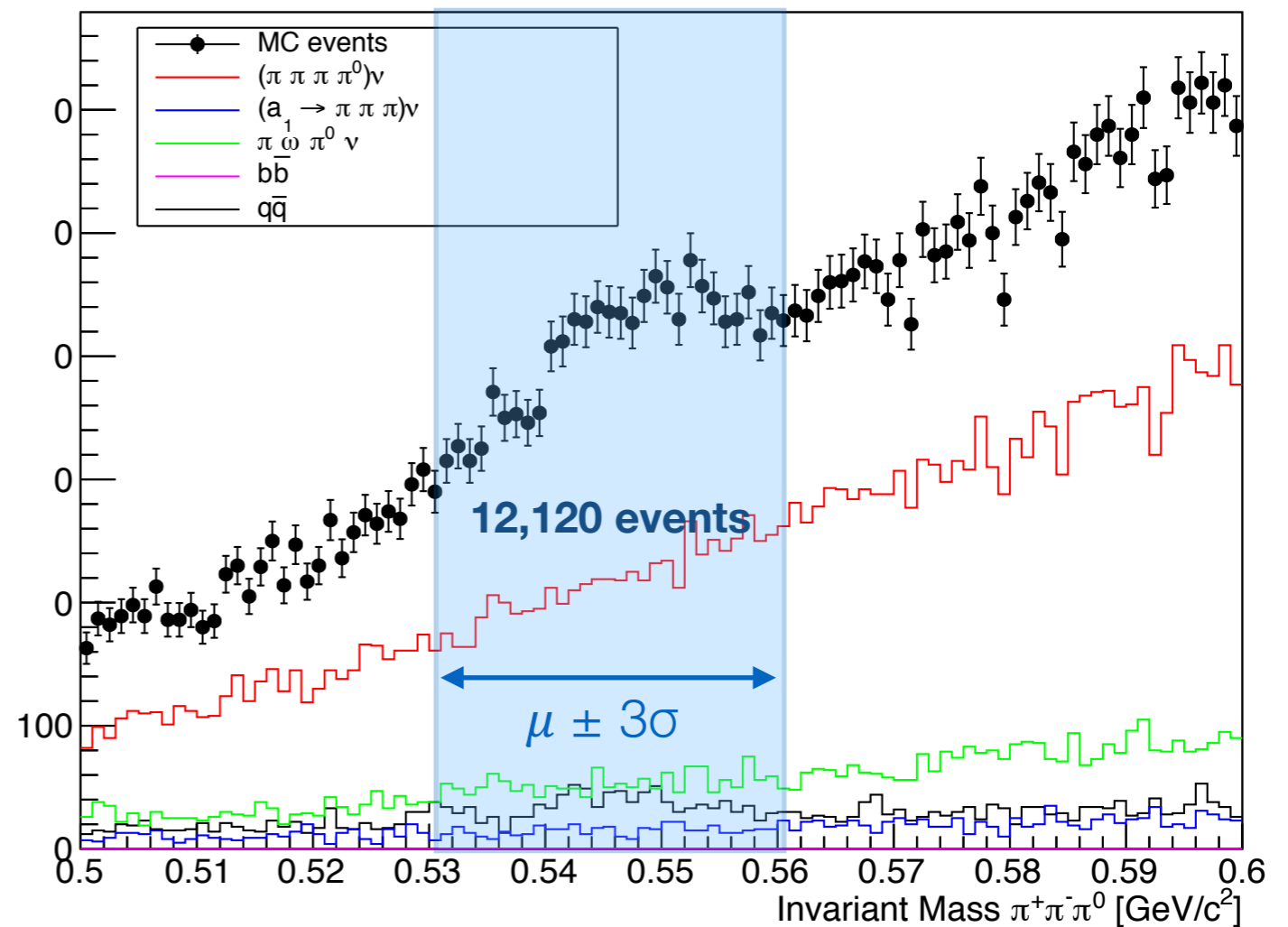
# Optimal BDT cut

## Background 3-prong



**$N_{\text{bkg}} = 240,438$**   
**Eff:  $3.03 \times 10^{-4}$**

**Eff<sub>cut</sub> = 83.52%**



**$N_{\text{bkg}} = 39,634$**   
**Eff:  $5.0 \times 10^{-5}$**

# Estimation @ 1 ab<sup>-1</sup>

- $BR(\tau \rightarrow \eta \pi \nu) \sim 10^{-5}$

$$N_{sig} = \epsilon \cdot \sigma_{\tau\tau} \cdot BR(\tau \rightarrow \ell \nu \bar{\nu}) \cdot L \cdot BR(\tau \rightarrow \eta \pi \nu)$$

## 1-prong

In the mass window of  $\eta$ :

- $N_{bkg} = 98,146$

$$\frac{N_{sig}}{\sqrt{N_{bkg}}} \simeq 0.786$$

## 3-prong

In the mass window of  $\eta$ :

- $N_{bkg} = 12,120$

$$\frac{N_{sig}}{\sqrt{N_{bkg}}} \simeq 0.516$$



# Estimation @ 50 ab<sup>-1</sup>

- $BR(\tau \rightarrow \eta \pi \nu) \sim 10^{-5}$

$$N_{sig} = \epsilon \cdot \sigma_{\tau\tau} \cdot BR(\tau \rightarrow \ell \nu \bar{\nu}) \cdot L \cdot BR(\tau \rightarrow \eta \pi \nu)$$

## 1-prong

In the mass window of  $\eta$ :

- $N_{bkg} \approx 4.9 \times 10^6$

$$\frac{N_{sig}}{\sqrt{N_{bkg}}} \simeq 5.56$$

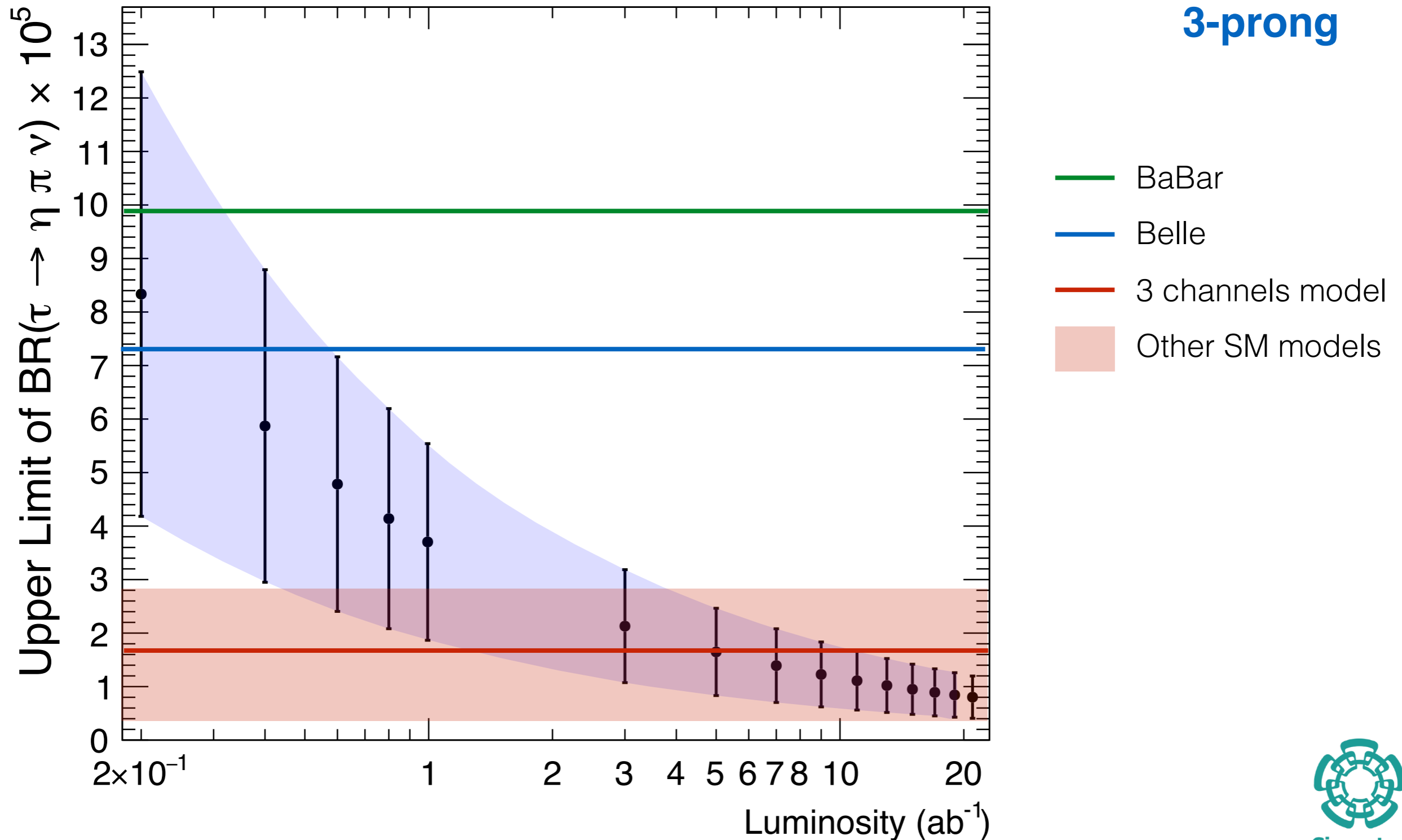
## 3-prong

In the mass window of  $\eta$ :

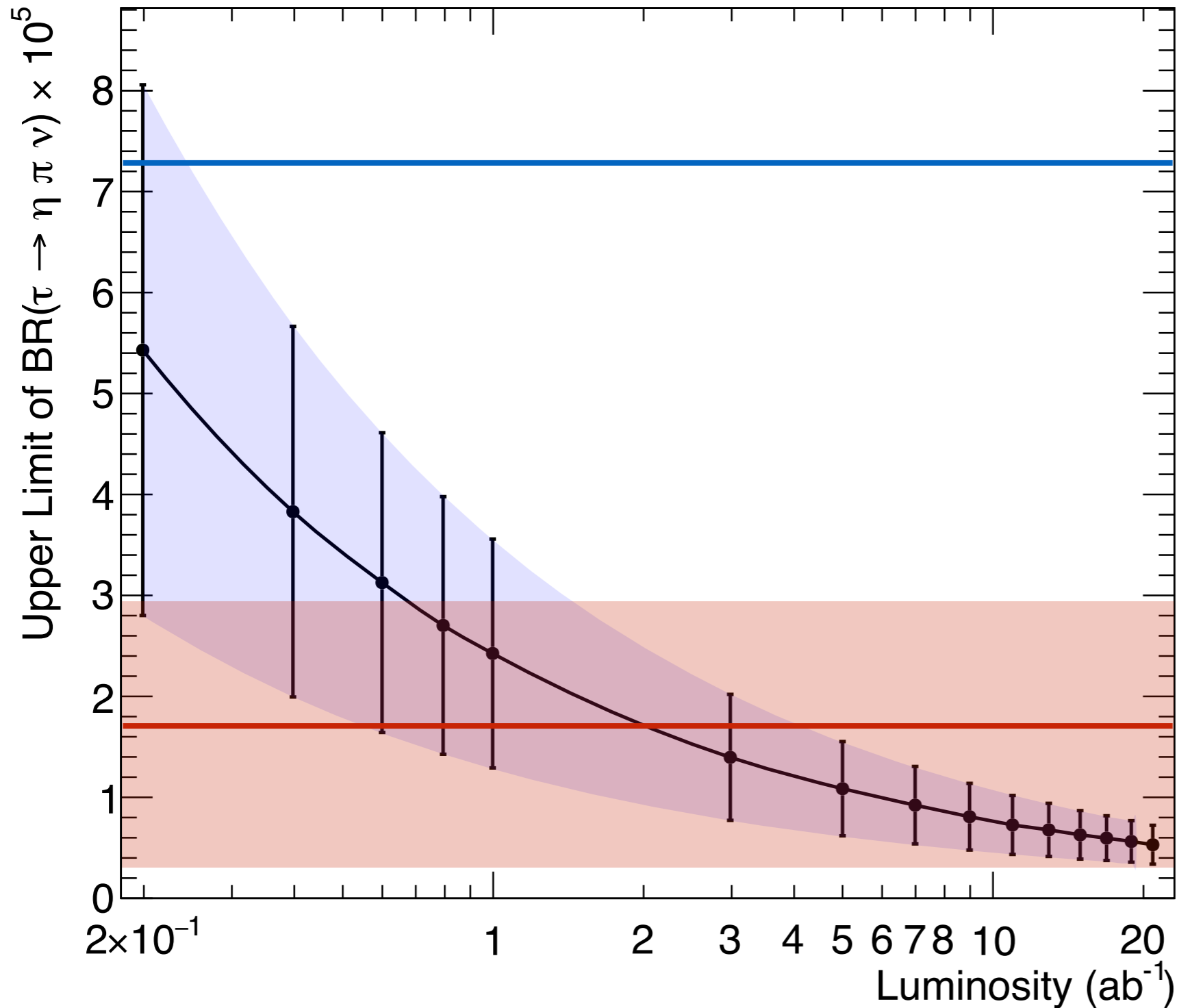
- $N_{bkg} \approx 6.06 \times 10^5$

$$\frac{N_{sig}}{\sqrt{N_{bkg}}} \simeq 3.65$$

# Estimated Upper Limits



# Estimated Upper Limits



1-prong

- BaBar
- Belle
- 3 channels model
- Other SM models

# Summary

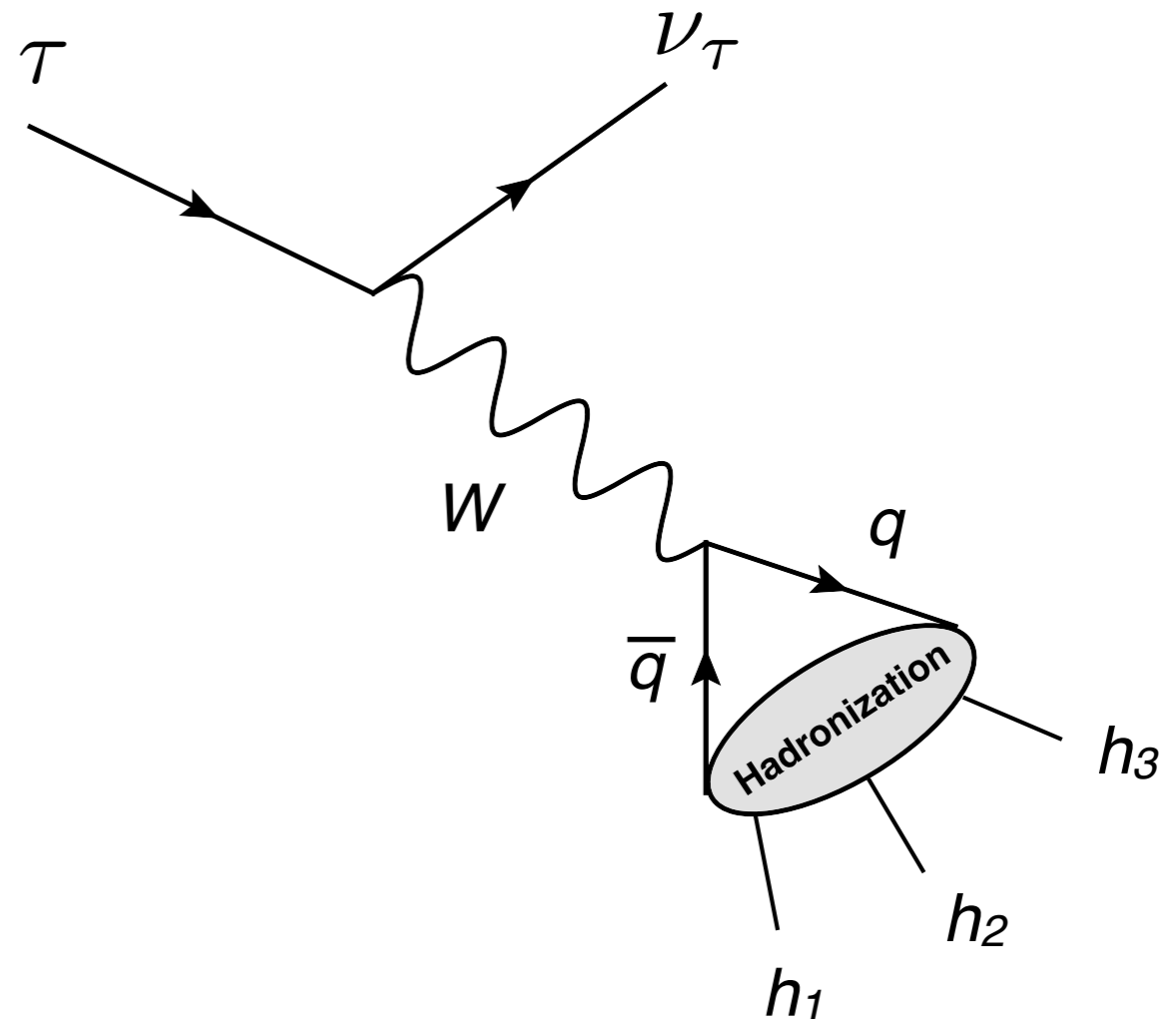
- SuperKEKB will produce a sample of  $\tau$  pairs 50 times larger than previous B-factories.  $\tau$  physics is now considered “precision physics”.
- BR measurement (or upper limit), invariant mass of  $\eta\pi$ , and Dalitz plots will be very important to disentangle models.
- Better selection of variables or more MVA techniques have to be tested.
- Some extra contributions to the background has to be studied.
- The comparison of channels generated, with the data obtained in the beginning of the experiment, is important to control the bkg.

# Thank you

# Backup

# Semileptonic decays of $\tau$ lepton

- The  $\tau$  lepton is the only lepton massive enough to decay into hadrons.
- Semileptonic decay channels  $\tau \rightarrow H \nu_\tau$  allow a clean theoretical analysis of the hadronization, determination of SM parameters and properties of weak currents<sup>1</sup>:
  - $\alpha_s$
  - CKM parameters
  - CPV
  - LNV and LFV
  - SM and NP interactions
  - etc.
- **B-factories** provide a large dataset of  $\tau$  leptons to precision studies.



> 200 hadronic channels

Disadvantage:  
We cannot detect  $\nu$

<sup>1</sup>Pich, A. *Progress in Particle and Nuclear Physics*, 75, 41-85 (2014).

# Hadronic Currents

- V-A currents can be classified by their transformation properties under  $G$ -parity <sup>1</sup>.

$$G = C e^{i\pi I_2}$$

- First-class currents:

$$G V_\mu G^{-1} = +V_\mu$$

$$G A_\mu G^{-1} = -A_\mu$$

$$J^{PG} = 0^{++}, 0^{--}, 1^{-+}, 1^{+-}, \dots$$

Standard Model

- Second-class currents (SCC):

$$G S G^{-1} = -S$$

$$G A'_\mu G^{-1} = +A'_\mu$$

$$J^{PG} = 0^{+-}, 0^{-+}, 1^{++}, 1^{--}, \dots$$

New physics

<sup>1</sup>S. Weinberg. *Physical Review*, 112(4), 1375 (1958).



# Second-class currents

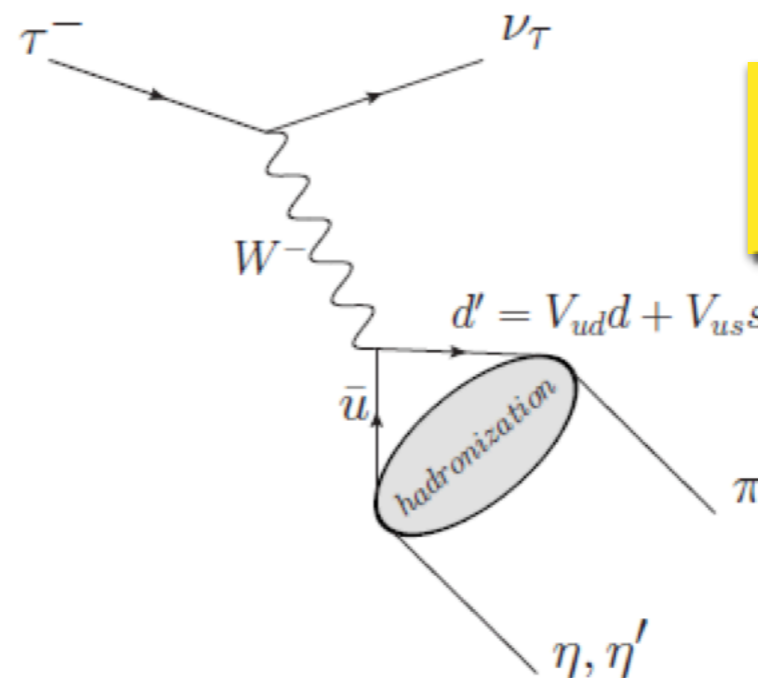
- SCC are isospin violating processes, suppressed by isospin symmetry.

$$G \sim SU(2) \sim \frac{m_d - m_u}{\Lambda}$$

- Unsuccessful searches of SCC in nuclear Physics.

- Another possibility:  
Search in tau decays<sup>1</sup>

$$\tau^- \rightarrow \eta \pi^- \nu_\tau$$



$$G|\bar{d}\gamma^\mu u\rangle = +|\bar{d}\gamma^\mu u\rangle$$

$$G|\pi\rangle = -|\pi\rangle$$

$$G|\eta\rangle = +|\eta\rangle$$

<sup>1</sup>Leroy, C., & Pestieau, J. (1978). Physics Letters B, 72(3), 398-399.

# G-parity

- G-parity is defined by<sup>1</sup>  $G = C e^{i\pi I_2}$
- Is a good symmetry of the strong interactions

$$[H_{str}, I_i] = 0; \quad [H_{str}, C] = 0$$

Convenient to analyze process where the initial or final state contains only mesons

$$G|\pi\rangle = -|\pi\rangle$$

$$G|\eta\rangle = +|\eta\rangle$$

$$G|\rho\rangle = +|\rho\rangle \quad \rho \rightarrow \pi\pi, 4\pi; \quad \not\rightarrow 3\pi, \eta\pi$$

$$G|\omega\rangle = -|\omega\rangle \quad \omega \rightarrow 3\pi, \rho\pi; \quad \not\rightarrow 2\pi, 4\pi$$

$$G|a_0\rangle = -|a_0\rangle \quad a_0 \rightarrow \eta\pi; \quad \not\rightarrow 2\pi$$

- However, G-Parity is not exact.  $[H_{tot}, I_i] \neq 0;$

<sup>1</sup>T. D. Lee, and Chen Ning Yang. *Il Nuovo Cimento* 3.4 (1956): 749-753.

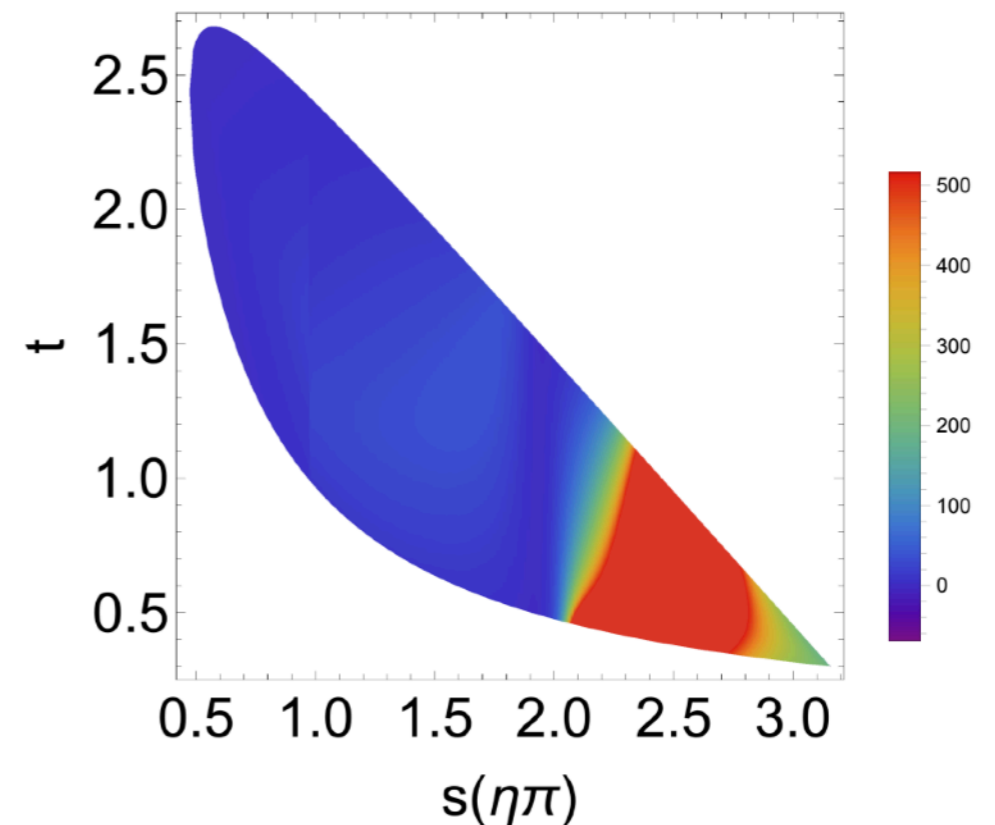
# The $\tau \rightarrow \eta \pi \nu$ decay

- NP contributions (scalar and tensorial currents) can be studied in the framework of an effective field theory <sup>1</sup>

$$\begin{aligned} \mathcal{M} &= \mathcal{M}_V + \mathcal{M}_S + \mathcal{M}_T \\ &= \frac{G_F V_{ud} \sqrt{S_{EW}}}{\sqrt{2}} (1 + \epsilon_L + \epsilon_R) [L_\mu H^\mu + \tilde{\epsilon}_S LH + 2\tilde{\epsilon}_T L_{\mu\nu} H^{\mu\nu}], \end{aligned}$$

- New Physics effects can appear in the distribution of Dalitz plots, with a large enhancement expected towards large values of the hadronic invariant mass<sup>1</sup>.

$$R(\tilde{\epsilon}_S, \tilde{\epsilon}_T) = \frac{|\overline{\mathcal{M}}|^2}{|\overline{\mathcal{M}}|_{00}^2}$$

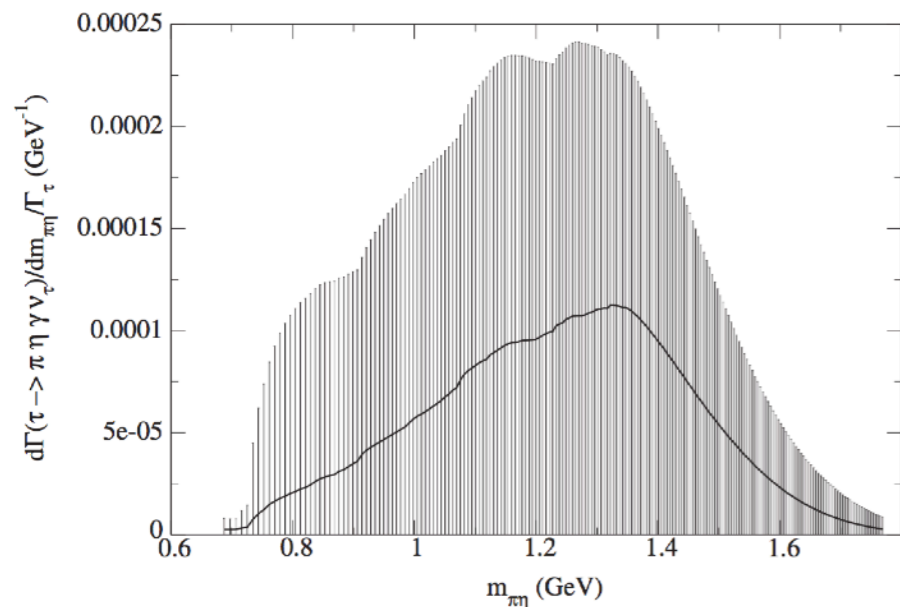
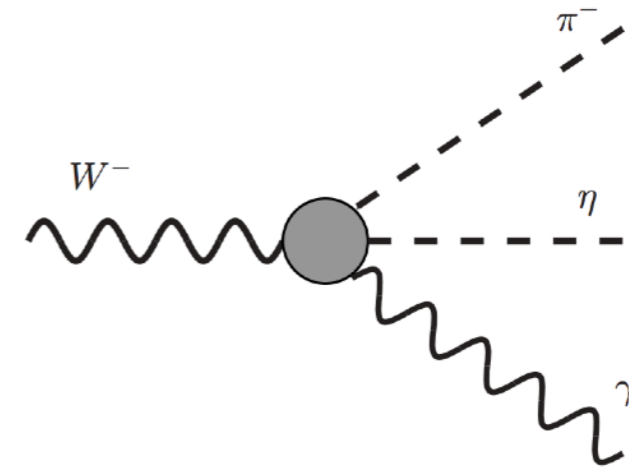


Ratio between the squared amplitude of EFT with  $\epsilon_T = 0.3$  and squared amplitude of SM.

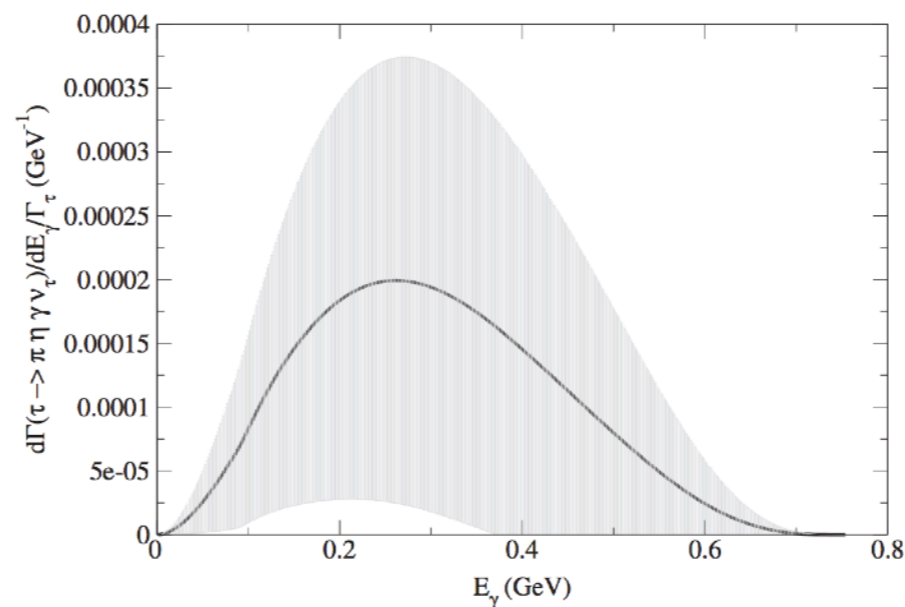
<sup>1</sup> E. A. Garcés, MHV, G. López Castro, P. Roig; arXiv:1708.07802

# A new bkg source<sup>1</sup>

- $\tau^- \rightarrow \eta\pi^- \nu_\tau \gamma$
- BR  $\sim 10^{-5}$ !  
(Not suppressed by G-parity, unlike the channel without photon.)



(a) Normalized spectrum (corresponding to the data in Fig. 14) in the invariant mass of the  $\eta\pi^-$  system is plotted.



(b) For the same points as in (a), the normalized spectrum in  $E_\gamma$  is drawn.

FIG. 15. Normalized spectra of the  $\tau^- \rightarrow \eta\pi^- \nu_\tau \gamma$  decays according to  $R\chi L$ .

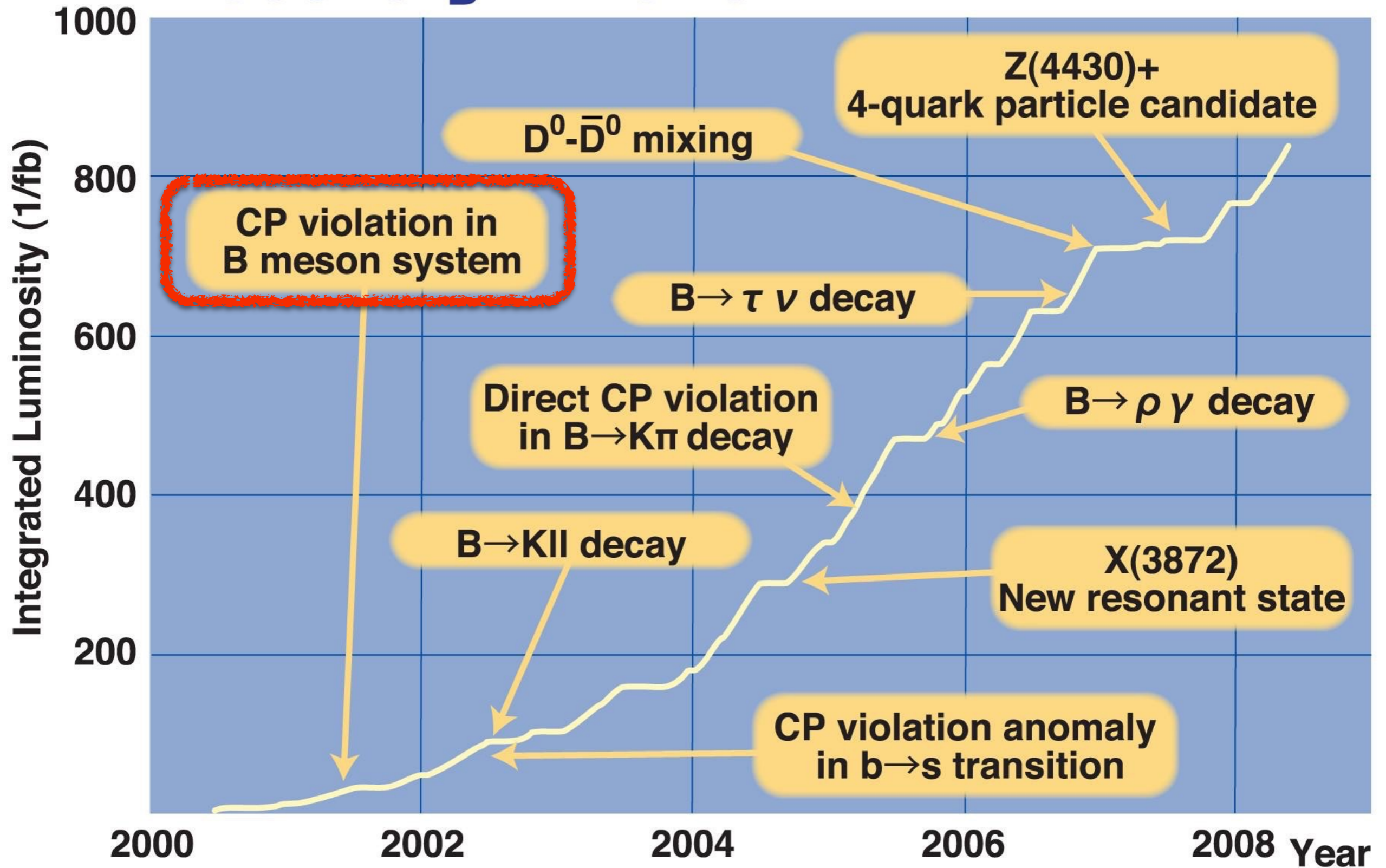
- Veto of photons with  $E_\gamma > 100$  MeV should get rid of this background.

<sup>1</sup>A. Guevara, G. López-Castro, P. Roig (2016). Phys.Rev. D95 no.5, 054015 (2017)

# B-Factories

	PEP-II	KEKB	SuperKEKB
Detector	BaBar	Belle	Belle II
Año de inicio	1999	1999	2016
Fin de operaciones	2008	2010	-
Energía del haz (GeV)	e-: 9.0 e+: 3.1	e-: 8.0 e+: 3.5	e-: 7.0 e+: 4.0
Luminosidad max	550 fb <sup>-1</sup>	1 ab <sup>-1</sup>	50 ab <sup>-1</sup>

# Discovery in Belle



- Hadronic matrix element: 2 form factors

$$H_\mu(p_0, p_-) \equiv \langle \eta\pi | \bar{d}\gamma_\mu u | 0 \rangle = f_+(t) \left( (p_0 - p_-)_\mu - \frac{\Delta^2}{t} q_\mu \right) + f_0(t) \frac{\Delta^2}{t} q_\mu$$

$$t = (p_- + p_0)^2$$

- Invariant mass distribution

$$\frac{d\Gamma}{dt} = \frac{G_F^2 |V_{ud}|^2}{768\pi^3 m_\tau^3} \times \frac{(m_\tau^2 - t)^2}{t^3} \lambda^{1/2}(t, m_\eta^2, m_\pi^2) I(t)$$

$$I(t) = |f_+(t)|^2 (m_\tau^2 + 2t) \lambda(t, m_\eta^2, m_\pi^2) + 3|f_0(t)|^2 \Delta^4 m_\tau^2$$

Spin-1 (V)

Spin-0 (S)

spin of  $\eta\pi$   
system in  
its rest frame

- Form factors

$$f_+(0) = f_0(0) \quad (m_\eta + m_\pi)^2 \leq t \leq m_\tau^2$$

- MDM: Meson dominance models.
- Sum of Breit-Wigner formulae
- Chiral theory, etc.

$$\begin{array}{l}
 f_+^{\text{I}}(t) = \frac{\sqrt{2}\epsilon_{\eta\pi}}{1 + \beta_\rho} \left[ \text{BW}_\rho(t) + \beta_\rho \text{BW}_{\rho'}(t) \right] \\
 f_0^{\text{I}}(t) = \frac{\sqrt{2}\epsilon_{\eta\pi}}{1 + \beta_a} \left[ \text{BW}_{a_0}(t) + \beta_a \text{BW}_{a'_0}(t) \right] \\
 \text{BW}_X(t) = m_X^2 / (m_X^2 - t - im_X\Gamma_X(t))
 \end{array}
 \left|
 \begin{array}{l}
 f_+^{\text{II}}(t) = \sqrt{2}\epsilon_{\eta\pi} \left[ 1 + \frac{f_\rho g_{\rho\pi\pi}}{m_\rho^2} \left( \widetilde{\text{BW}}_\rho(t) + \beta_\rho \widetilde{\text{BW}}_{\rho'}(t) \right) \right] \\
 f_0^{\text{II}}(t) = \sqrt{2}\epsilon_{\eta\pi} \left[ 1 + \frac{f_{a_0} g_{a_0\eta\pi}}{m_\eta^2 - m_\pi^2} \left( \widetilde{\text{BW}}_{a_0}(t) + \beta_a \widetilde{\text{BW}}_{a'_0}(t) \right) \right] \\
 \widetilde{\text{BW}}_X(t) = t / (m_X^2 - t - im_X\Gamma_X(t))
 \end{array}
 \right.$$

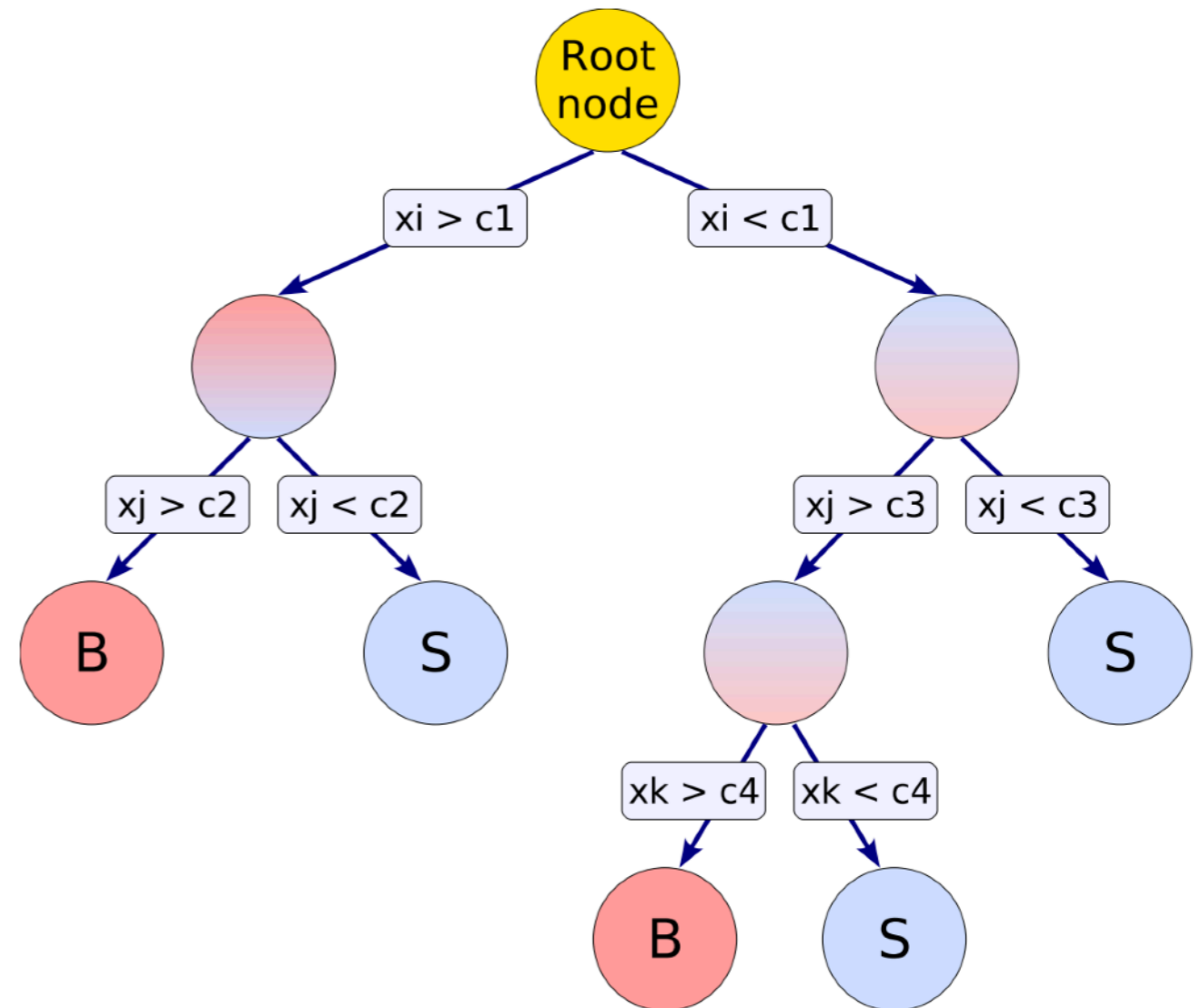


# TinyDST

- For tau physics study, roughly TinyDST (tdst) is designed<sup>1</sup>.
- Events having:
  - Less than 6 charged tracks with  $|dr| < 0.5$  cm,  $|dz| < 3.0$  cm,  $p_t > 0.1$  GeV/c and  $-0.8660 < \cos \theta < 0.9535$ .
  - Less than 10 photons with  $E_\gamma > 50$  MeV and  $-0.8660 < \cos \theta < 0.9535$ .
- Thrust vector information contained.
- To squeeze the size, one lepton is required.
  - In SM precise measurement, to avoid qq BG, usually, leptonic decay is required for tag tau (tau with non-signal decay).
- 50MBytes for 200k events. (In original mdst, 50MBytes for 20k events.)

# Boosted Decision Trees

- What is a Decision Tree?
  - Consecutive set of questions (nodes).
  - Two possible answers per node.
  - Final verdict (**leaf**) is reached after a defined maximum of nodes.
- Advantages
  - Easy to understand.
  - Fast training.
- Disadvantages
  - Single tree not strong (that's why we use **Random Forests**).



# Boosted Decision Trees

- Random Forest is an ensemble method that combines different trees.
- Final output is determined by the majority vote of all the trees.
- Boosting:
  - Misclassified events are weighted higher so that future learners concentrate on these.



The score of an event is a weighted average of the scores the event receives from each tree in the forest.

$$bdt = \frac{\sum_i w_i N_i}{\sum_i w_i}; \quad N_i = -1 \text{ or } 1$$

# BDT tests

Background rejection versus Signal efficiency

