

$\tau \rightarrow \pi\eta^{(\prime)}\gamma\nu_\tau$  as background for SCC

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# Background

- Trying to obtain new conservation laws, T.D. Lee and C.N. Yang introduced the operator

$$G = C e^{i\pi I_2}$$

- For states with  $N_B = 0$ ,  $G = \pm 1$  and is the same for all components of an  $I$ -multiplet<sup>1</sup>.
- Thus, hadronic currents with  $\Delta S = \Delta C = \Delta B = 0$  will have a definite  $G$ -parity.

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<sup>1</sup>T.D. Lee and C.N. Yang, Nuovo Cim. 3 (1956) 749

# Background

- These currents can be divided into two classes

$G$	$S$	$P$	$V$	$A$
$1^{st}$	+1	-1	+1	-1
$2^{nd}$	-1	+1	-1	+1

- $2^{nd}$  class currents (SCC) have opposite  $G$ -parity to weak currents in SM.
- In QCD,  $G$ -parity is broken by  $u$ - $d$  mass and electric charge differences.
- eg,  $G(\eta\pi) = -1$ , and  $\mathcal{P}(\eta\pi) = +1 \Rightarrow$  a scalar  $2^{nd}$  class current must generate the  $\tau \rightarrow \pi\eta\nu_\tau$  decay.

## Background

- Therefore, isospin breaking currents are important background for genuine SCC.
- Search for SCC in  $\beta$ -decays is difficult due to the small momentum transfer and the many form factors implicated.
- However, search for these currents have been suggested<sup>2</sup> in semileptonic decays such as  $\tau \rightarrow \pi\eta\nu_\tau$  (cleanest).
- Current experimental limits  $\mathcal{B}_\eta < 10^{-4}$  and  $\mathcal{B}_{\eta'} < 10^{-5}$  are close to  $G$ -parity breaking prediction.
- Belle-II may discover  $G$ -parity breaking so that we can characterize further its structure and disentangle New Physics contributions (See Michel Hernandez's talk).

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<sup>2</sup>C. Leroy and J. Pestieau, Phys. Lett. B72 (1978) 398

# Background

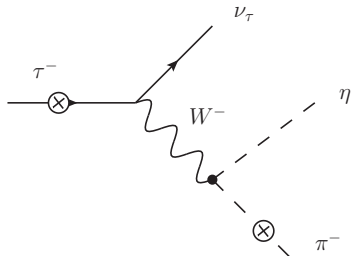
- Within the SM,  $\tau \rightarrow \pi\eta\nu_\tau$  is suppressed due to a factor

$$\left( \left[ \frac{m_{\pi^0}}{m_\eta} \cdot \frac{m_d - m_u}{m_s} \right]^2 \sim 10^{-5} \right).$$

- An important background for this process is  $\tau \rightarrow \pi\eta\nu_\tau\gamma$  with  $\gamma$  escaping detection.
- $\gamma$  does not have a definite  $I$  value  $\Rightarrow$  some contributions do not have the suppression factor.
- We study the radiative process, where we estimate this suppression to compete with the one from  $\alpha_{EM}$ .

## Main contributions to the amplitude

- We will try to find a photon energy  $E_\gamma$  cut to safely neglect this contribution in the search for SCC.



- Bremsstrahlung contributions will have both, the  $\sim 10^{-5}$  factor and the  $\alpha_{EM}$  suppression.
- Contributions involving the effective  $W^*\pi\eta\gamma$  vertex will give the main contribution to the amplitude.

# Main contribution to the decay amplitude

- The main contribution can be expressed as

$$\mathcal{M} = \frac{eG_F V_{ud}^*}{\sqrt{2}} \epsilon^{*\mu} (V_{\mu\nu} - A_{\mu\nu}) L_\tau^\nu$$

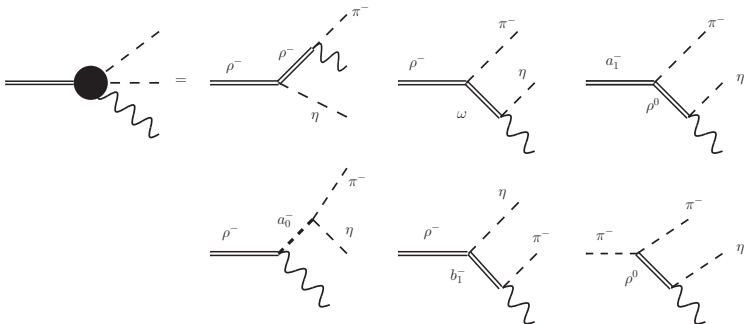
- where the hadronic tensors are parametrized as

$$\begin{aligned} V_{\mu\nu} = & \mathbf{v}_1 (p \cdot \mathbf{k} g_{\mu\nu} - p_\mu k_\nu) + \mathbf{v}_2 (g_{\mu\nu} p_0 \cdot \mathbf{k} - p_{0\mu} k_\nu) \\ & + \mathbf{v}_3 (p_\mu p_0 \cdot \mathbf{k} - p_{0\mu} p \cdot \mathbf{k}) p_\nu + \mathbf{v}_4 (p_\mu p_0 \cdot \mathbf{k} - p_{0\mu} p \cdot \mathbf{k}) p_{0\nu} \end{aligned}$$

$$\begin{aligned} A_{\mu\nu} = & i \varepsilon_{\mu\nu\rho\sigma} (\mathbf{a}_1 p_0^\rho k^\sigma + \mathbf{a}_2 k^\rho W^\sigma) \\ & + i \varepsilon_{\mu\rho\sigma\tau} k^\rho p^\sigma p_0^\tau (\mathbf{a}_3 W_\nu + \mathbf{a}_4 (p_0 + \mathbf{k})_\nu) \end{aligned}$$

# Meson Dominance Model (MDM)

- We rely on MDM to estimate the order of magnitude of the branching fraction with the following contributions.

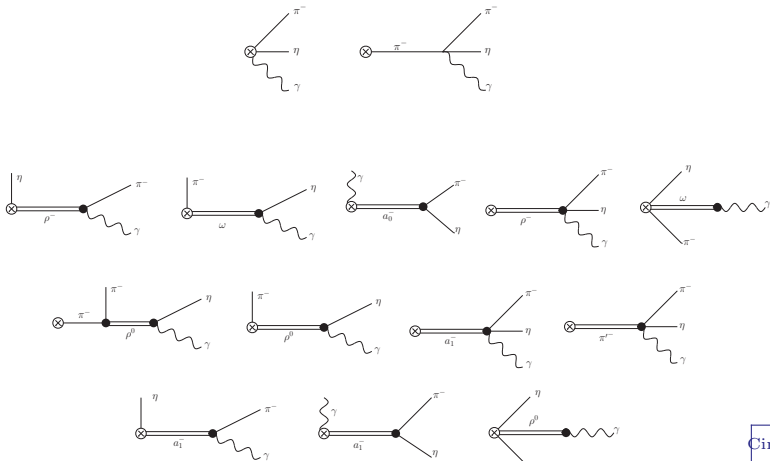


- Using MDM we estimated  $\mathcal{B}(\tau \rightarrow \pi\eta\gamma\nu_\tau) \sim \mathcal{B}(\tau \rightarrow \pi\eta\nu_\tau)$



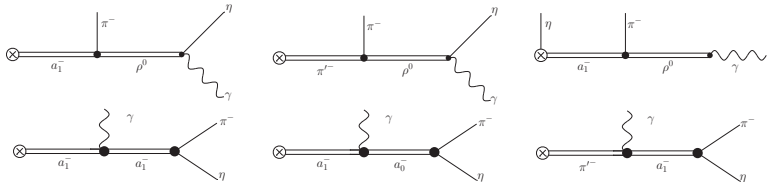
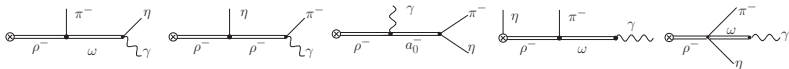
# Resonance Chiral Theory ( $R\chi T$ )

- We then computed the branching ratio using  $R\chi T$  and obtained contributions from diagrams with 0 and 1 meson resonance exchange.



## 2R Contributions

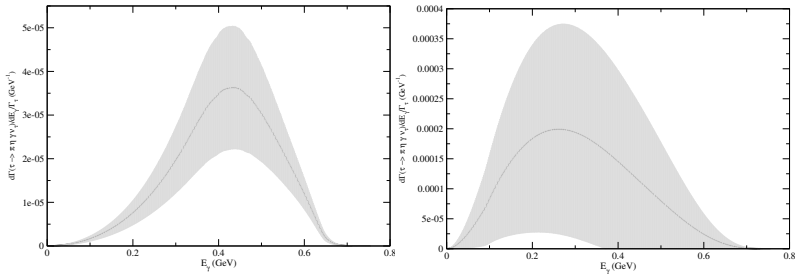
- and with two resonance exchange



- There is no *a priori* argument to neglect 2R exchange contributions, however we get that they are suppressed with respect to the 1R exchange contributions.

# $E_\gamma$ spectrum for $\tau \rightarrow \pi\eta\gamma\nu_\tau$

- $E_\gamma$  spectrum<sup>3</sup> for MDM (left) and R $\chi$ T (right).



<sup>3</sup>AG, G. López Castro y P. Roig, Phys. Rev. D95 (2017) 054015

# Results

- We compare our results to the non-radiative process<sup>4</sup>

Bkg	BR (no cuts)	BR ( $E_\gamma^{\text{cut}} > 100$ MeV)	BR SCC signal
$\eta$	$(3.0 \pm 0.6) \cdot 10^{-5}$	$(1.2 \pm 0.6) \cdot 10^{-6}$	$\sim 1.7 \cdot 10^{-5}$
$\eta'$	$(2.2 \pm 0.4) \cdot 10^{-6}$	$(2 \pm 1) \cdot 10^{-7}$	$[10^{-7}, 10^{-6}]$

- The radiative process can be suppressed by cutting photons with energies  $E_\gamma > 100$  MeV for  $\eta$ .
- Due to the large uncertainty in  $BR(\tau \rightarrow \pi\eta'\nu_\tau)$  we cannot say the same for the  $\eta'$  channel

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<sup>4</sup>R. Escribano, S. González-Solís and P. Roig, Phys. Rev. D**94** (2016)

## Conclusions

- We were able to suppress the background due to the radiative process by imposing a cut on  $E_\gamma$  for the  $\eta$  channel.
- A better analysis of the non-radiative process must be done to give a conclusion for the  $\eta'$ .
- We found that neglecting the two resonance exchange contribution is a very good approximation.
- This will greatly simplify the Monte Carlo code for generating the form factors and reduce the computation time.

Back up

## Constantes de acoplo MDM

- Los acoplamientos de MDM se obtienen haciendo los siguientes ajustes.
- Usamos el ancho

$$\Gamma(\tau^- \rightarrow \nu_\tau X^-) = \frac{G_F^2 |V_{ud}|^2 M_X^2}{8\pi M_\tau^3 g_X^2} (M_\tau^2 - M_X^2)^2 (M_\tau^2 + 2M_X^2)$$

- para encontrar  $g_{a_1}$ , tomando (PDG)  
 $BR(\tau^- \rightarrow a_1^- \nu_\tau) = 0.1861 \pm 0.0013$
- Para  $g_\rho$  se toma el ancho

$$\Gamma(\rho^0 \rightarrow e^+ e^-) = \frac{4\pi}{3} \left( \frac{\alpha}{g_\rho} \right)^2 \left( 1 + \frac{2m_\ell^2}{M_V^2} \right) \sqrt{M_V^2 - 4m_\ell^2}.$$

## Constantes de acoplo MDM

- El acoplamiento Vector-fotón-pseudoescalar,  $g_{V\gamma P}$ , se obtiene con los anchos medidos (PDG)  $\Gamma(\rho/\omega \rightarrow \pi/\eta \gamma)$  y de la expresión para ancho

$$\Gamma(V \rightarrow P\gamma) = \frac{|g_{VP\gamma}|^2}{96\pi M_V^3} (M_V^2 - M_P^2)^3$$

- El acoplamiento  $g_{\rho a_1 \pi}$  se obtiene del ancho ( $\lambda$  es la función de Källén)

$$\Gamma(a_1 \rightarrow \rho\pi) = \frac{|g_{\rho a_1 \pi}|^2}{96\pi M_{a_1}^3} [\lambda(M_{a_1}^2, M_\rho^2, m_\pi^2) + 6M_\rho^2 M_{a_1}^2] \times \lambda^{1/2}(M_{a_1}^2, M_\rho^2, m_\pi^2).$$

- $\text{con}^5 BR(a_1 \rightarrow \rho\pi) = 61.5\%$  y  $\Gamma_{a_1} = (475 \pm 175) \text{ MeV}$

<sup>5</sup>D. M. Asner *et al.* [CLEO Collaboration], Phys. Rev. D**61** (2000)



## Constantes de acoplo MDM

- Para los acoplos de  $a_0$  se usa

$$\Gamma(a_0 \rightarrow \gamma\gamma) = \frac{|g_{a_0\gamma\gamma}|^2}{32\pi} M_{a_0}^3,$$

$$\Gamma(a_0 \rightarrow \pi\eta) = \frac{|g_{a_0\pi\eta}|^2}{16\pi M_{a_0}^3} \lambda^{1/2}(M_{a_0}^2, m_\eta^2, m_\pi^2),$$

- Donde se reporta (PDG)

$$\Gamma(a_0 \rightarrow \gamma\gamma) \times \frac{\Gamma(a_0 \rightarrow \pi\eta)}{\Gamma_{a_0}} = (0.21_{-0.04}^{+0.08}) \text{ keV}.$$

- y usando<sup>6</sup>  $\Gamma_{a_0} = (75.6 \pm 1.6_{-10.0}^{+17.4}) \text{ MeV}$

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<sup>6</sup>S. Uehara *et al.* [Belle Collaboration], Phys. Rev. D **80** (2009) 032001

# Constantes de acoplo MDM

- Las demás constantes se obtienen de simetrías del modelo<sup>7</sup>

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<sup>7</sup>Alaín Flores Tlalpa, PhD Thesis, *Modelo de dominancia de mesones para decaimientos semileptónicos de sabores pesados*. (2008) Cinvestav, México, DF

# MDM

- Las reglas para los diferentes vértices vienen dadas por

$$V'^{\mu}(r) \rightarrow V^{\alpha}(s)P(t) : ig_{V'VP} \epsilon^{\mu\alpha\rho\sigma} s_{\rho} t_{\sigma},$$

$$V^{\mu}(r) \rightarrow \gamma^{\alpha}(s)P(t) : ig_{VP\gamma} \epsilon^{\mu\alpha\rho\sigma} s_{\rho} t_{\sigma},$$

$$A^{\mu}(r) \rightarrow V^{\alpha}(s)P(t) : ig_{VAP} (r \cdot s g^{\mu\alpha} - r^{\alpha} s^{\mu}),$$

$$V^{\mu}(r) \rightarrow \gamma^{\alpha}(s)S(t) : ig_{VS\gamma} (r \cdot s g^{\mu\alpha} - r^{\alpha} s^{\mu}),$$

$$S(r) \rightarrow P(s)P'(t) : ig_{SPP'}.$$

- Los acoplamientos se determinan de procesos independientes.

$$BR(\tau \rightarrow \pi \eta \gamma \nu_\tau)$$

- $BR$  calculado con  $R\chi T$

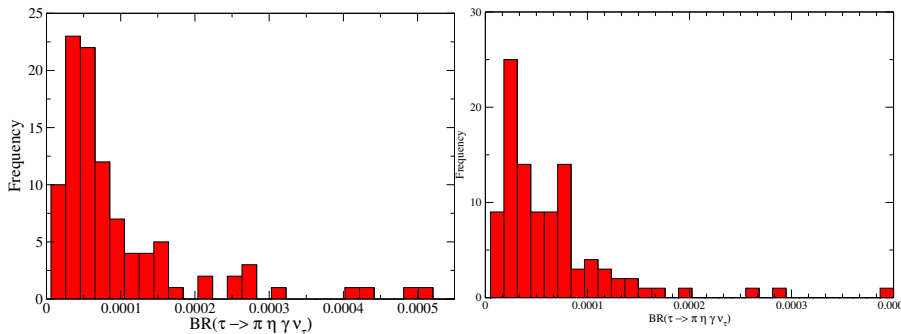
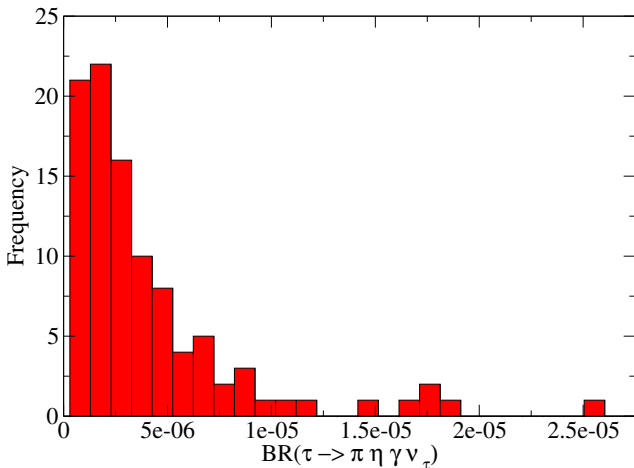


Figura: Fracción de decaimiento con todas las contribuciones (izq.) y sin intercambio de dos resonancias.

$$BR(\tau \rightarrow \pi \eta \gamma \nu_\tau) \quad E_\gamma < 100 \text{ MeV}$$

- $BR$  calculado con  $R\chi T$  con corte en  $E_\gamma = 100 \text{ MeV}$



$$BR(\tau \rightarrow \pi \eta' \gamma \nu_\tau)$$

- $BR$  calculado con  $R\chi T$

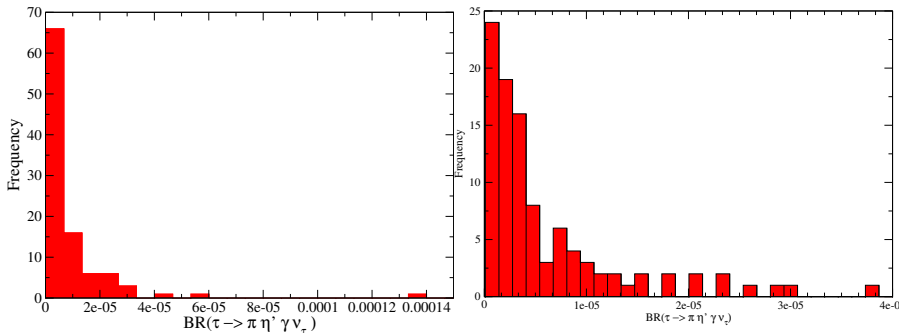
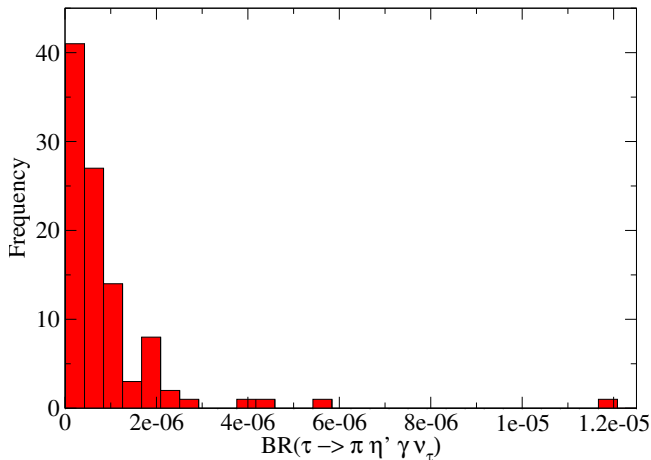


Figura: Fracción de decaimiento con todas las contribuciones (izq.) y sin intercambio de dos resonancias.

$$BR(\tau \rightarrow \pi \eta' \gamma \nu_\tau) \quad E_\gamma < 100 \text{ MeV}$$

- $BR$  calculado con R $\chi$ T con corte en  $E_\gamma = 100 \text{ MeV}$



# Bremsstrahlung contribution to $\tau \rightarrow \pi\eta^{(\prime)}\gamma\nu_\tau$

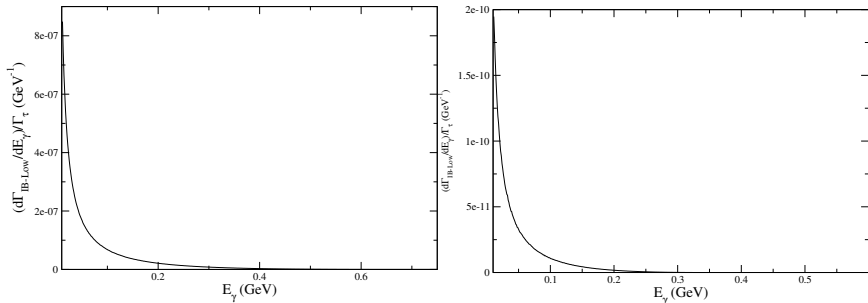
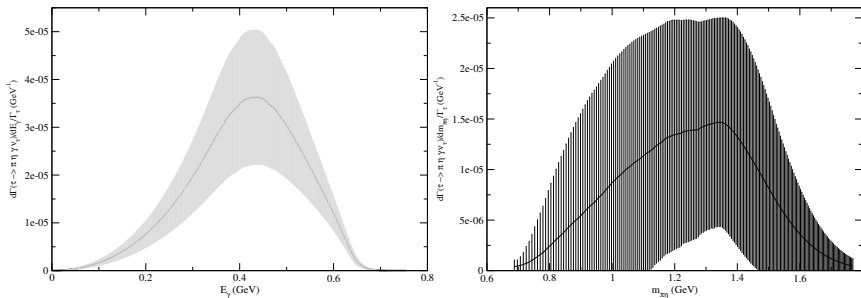


Figura: Contribution for the  $\tau \rightarrow \pi\eta\gamma\nu_\tau$  (left) and for  $\tau \rightarrow \pi\eta'\gamma\nu_\tau$  (right)



# Spectra for $\tau \rightarrow \pi\eta\gamma\nu_\tau$ in MDM



**Figura:** Invariant mass spectrum (right) and photon energy spectrum (left)

# Spectra for $\tau \rightarrow \pi\eta'\gamma\nu_\tau$ in MDM

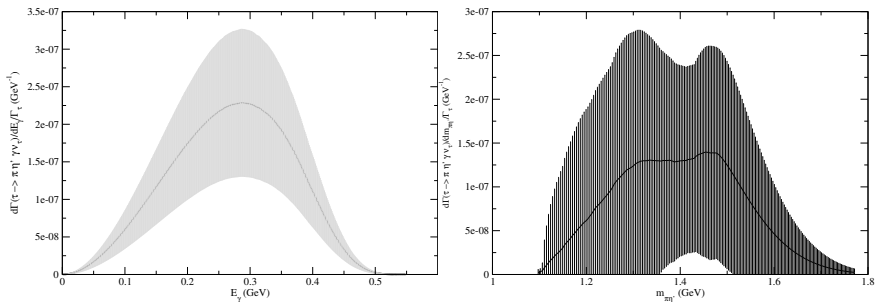


Figura: Invariant mass spectrum (right) and photon energy spectrum (left)

# Spectra for $\tau \rightarrow \pi\eta\gamma\nu_\tau$ in R $\chi$ T

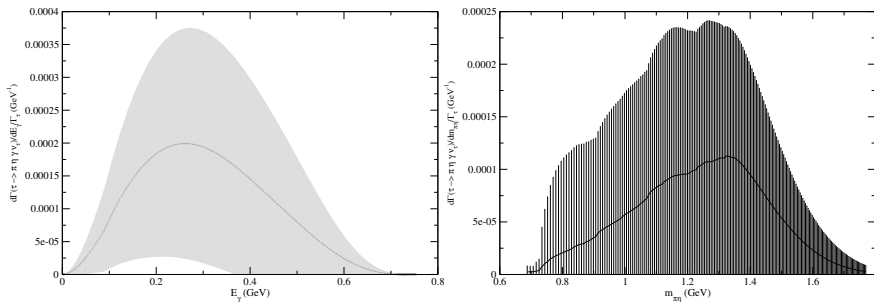
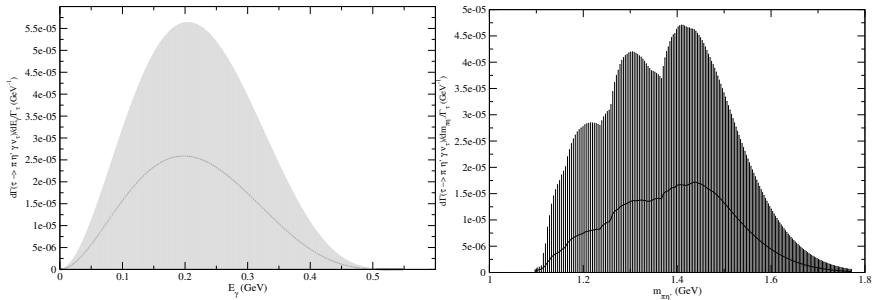


Figura: Invariant mass spectrum (right) and photon energy spectrum (left)

# Spectra for $\tau \rightarrow \pi\eta'\gamma\nu_\tau$ in $R\chi T$



**Figura:** Invariant mass spectrum (right) and photon energy spectrum (left)