

# Some new aspects of double parton scattering effects in the reactions with at least single charm pair production

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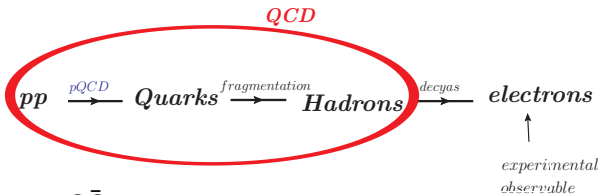


# Introduction

- Early extraction of  $\sigma_{eff} \sim$  gave 15 mb
- Recently some confusion from recent analyses
  - $\sigma_{eff} = 4.8 \pm 0.5 \pm 2.5$  mb from  $J/\psi J/\psi$  at D0
  - $\sigma_{eff} = 2.2 \pm 0.7 \pm 0.9$  mb from  $J/\psi \Upsilon$  at D0
  - $\sigma_{eff} = 60$  mb from MSSS2016 analysis of  $D^0 D^0$
- Naive geometry with smeared gluons:  $\sigma_{eff} \approx 30$  mb  
 Gaunt, Maciuła, Szczurek, Phys. Rev. **D90** (2014) 054017.
- Parton splitting effectively modifies  $\sigma_{eff}$  (down)  
 $\sigma_{eff} = \sigma_{eff}(\Delta\gamma)$
- Nonperturbative parton splitting (Blok, Strikman)
- More involved analyses regarding SPS and DPS contributions needed
- Here we consider two new processes:
  - $pp \rightarrow c\bar{c}j$  (SPS, collinear- and  $k_T$ -factorization)  
 helpful in understanding  $c\bar{c}$  production
  - $pp \rightarrow c\bar{c}jj$  (DPS and SPS, collinear factorization)  
 competition of DPS and SPS

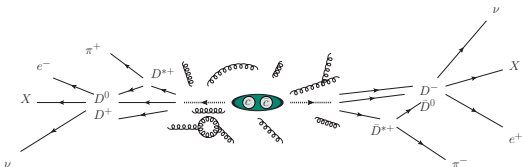


# 3-step process



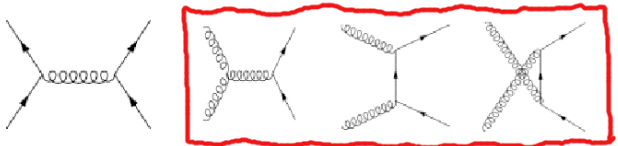
- 1 Heavy quarks  $Q\bar{Q}$  pairs production
  - $m_c = 1.5 \text{ GeV}, m_b = 4.75 \text{ GeV} \rightarrow$  perturbative QCD
- 2 Heavy quarks hadronization (fragmentation)
- 3 Semileptonic decays of D and B mesons

$$\frac{d\sigma^e}{dyd^2p} = \frac{d\sigma^Q}{dyd^2p} \otimes D_{Q \rightarrow H} \otimes f_{H \rightarrow e}$$

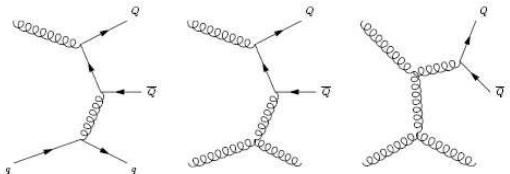


# Dominant mechanisms of $Q\bar{Q}$ production

- Leading order processes contributing to  $Q\bar{Q}$  production:



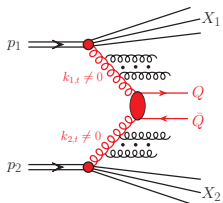
- gluon-gluon fusion** dominant at high energies
- $q\bar{q}$  annihilation important only near the threshold
- some of next-to-leading order diagrams:



NLO contributions  $\rightarrow$  K-factor



# $k_T$ -factorization (semihard) approach



- charm and bottom quarks production at high energies  
→ gluon-gluon fusion
- QCD collinear approach → only inclusive one particle distributions, total cross sections

**LO  $k_T$ -factorization approach** →  $\kappa_{1,t}, \kappa_{2,t} \neq 0$   
 ⇒  $Q\bar{Q}$  correlations

- multi-differential cross section

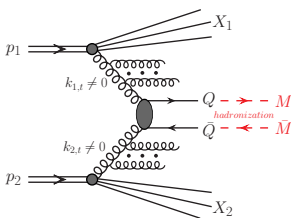
$$\frac{d\sigma}{dy_1 dy_2 d^2p_{1,t} d^2p_{2,t}} = \sum_{ij} \int \frac{d^2\kappa_{1,t}}{\pi} \frac{d^2\kappa_{2,t}}{\pi} \frac{1}{16\pi^2(x_1 x_2 s)^2} \overline{|\mathcal{M}_{j \rightarrow Q\bar{Q}}|^2} \times \delta^2(\bar{\kappa}_{1,t} + \bar{\kappa}_{2,t} - \bar{p}_{1,t} - \bar{p}_{2,t}) F_i(x_1, \kappa_{1,t}^2) F_j(x_2, \kappa_{2,t}^2)$$

- off-shell  $\overline{|\mathcal{M}_{gg \rightarrow Q\bar{Q}}|^2}$  → Catani, Ciafaloni, Hautmann (rather long formula)
- major part of **NLO corrections automatically included**
- $F_i(x_1, \kappa_{1,t}^2), F_j(x_2, \kappa_{2,t}^2)$  - unintegrated parton distributions

- $x_1 = \frac{m_{1,t}}{\sqrt{s}} \exp(y_1) + \frac{m_{2,t}}{\sqrt{s}} \exp(y_2),$   
 $x_2 = \frac{m_{1,t}}{\sqrt{s}} \exp(-y_1) + \frac{m_{2,t}}{\sqrt{s}} \exp(-y_2),$  where  $m_{i,t} = \sqrt{p_{i,t}^2 + m_Q^2}.$



# Fragmentation functions technique



- fragmentation functions extracted from  $e^+e^-$  data
- often used: Braaten et al., Kartvelishvili et al., Peterson et al.
- rescaling transverse momentum at a constant rapidity (angle)

- from heavy quarks to heavy mesons:

$$\frac{d\sigma(y, p_t^M)}{dyd^2p_t^M} \approx \int \frac{D_{Q \rightarrow M}(z)}{z^2} \cdot \frac{d\sigma(y, p_t^Q)}{dyd^2p_t^Q} dz$$

where:  $p_t^Q = \frac{p_t^M}{z}$  and  $z \in (0, 1)$

- **approximation:**

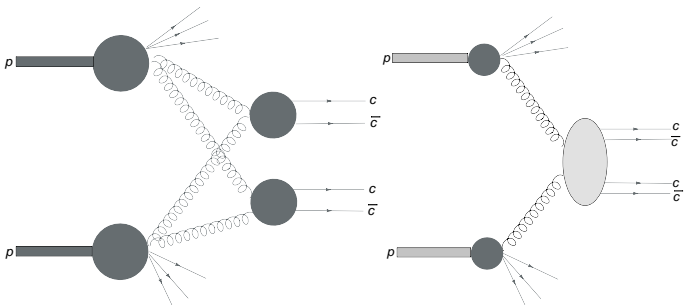
rapidity unchanged in the fragmentation process  $\rightarrow y_Q \approx y_M$

Production of  $D$  mesons in this framework:

Maciula, Szczurek, Phys. Rev. **D87** (2013) 094022.



# Production of $c\bar{c}c\bar{c}$



Łuszczak, Maciuła, Szczurek, Phys. Rev. **D85** (2012) 014905.





# Formalism

Consider reaction:  $pp \rightarrow c\bar{c}c\bar{c}X$

Modeling double-parton scattering

Factorized form:

$$\sigma^{DPS}(pp \rightarrow c\bar{c}c\bar{c}X) = \frac{1}{2\sigma_{eff}} \sigma^{SPS}(pp \rightarrow c\bar{c}X_1) \cdot \sigma^{SPS}(pp \rightarrow c\bar{c}X_2).$$

In general  $\sigma_{eff}$  can depend on kinematics The simple formula above can be generalized to include differential distributions

$$\frac{d\sigma}{dy_1 dy_2 d^2p_{1t} dy_3 dy_4 d^2p_{2t}} = \frac{1}{2\sigma_{eff}} \cdot \frac{d\sigma}{dy_1 dy_2 d^2p_{1t}} \cdot \frac{d\sigma}{dy_3 dy_4 d^2p_{2t}}.$$

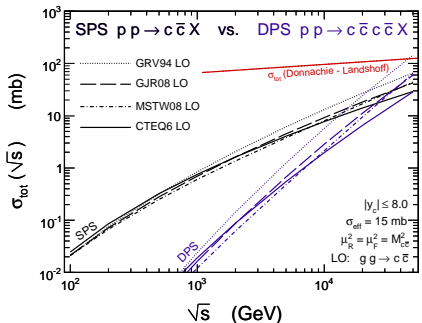
$\sigma_{eff}$  is a model parameter (15 mb).

Found e.g. from experimental analysis of four jets (see also Siódmok et al)

In principle does not need to be universal.



# Energy dependence of $c\bar{c}c\bar{c}$ production



Luszczak, Maciula, Szczurek, Phys. Rev. **C86** (2012) 014905

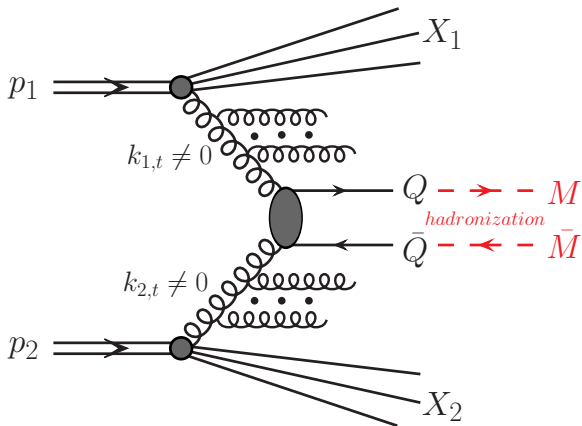
spectacular result:

Already at the LHC production of two pairs as probable as production of one pair.



# DPS in $k_T$ -factorization

each step:



## DPS in $k_T$ -factorization

Generalize the **LO collinear** approach to  **$k_T$ -factorization** approach.

More complicated (**more kinematical variables**) as momenta of outgoing partons are less correlated

We need information about each quark and antiquark

$$\frac{1}{2\sigma_{\text{eff}}} \cdot \frac{\frac{d\sigma}{dy_1 dy_2 d^2 p_{1,t} d^2 p_{2,t}}}{d\sigma} \cdot \frac{\frac{d\sigma}{dy_3 dy_4 d^2 p_{3,t} d^2 p_{4,t}}}{d\sigma} = \quad (1)$$



# DPS in $k_T$ -factorization

Each individual scattering in the  $k_T$ -factorization approach

$$\frac{d\sigma}{dy_1 dy_2 d^2 p_{1,t} d^2 p_{2,t}} = \frac{1}{16\pi^2 \hat{s}^2} \int |\overline{\mathcal{M}}_{\text{off}}|^2 \delta(\vec{k}_{1t} + \vec{k}_{2t} - \vec{p}_{1t} - \vec{p}_{2t}) \mathcal{F}(x_1, k_{1t}^2, \mu^2) \mathcal{F}(x_2, k_{2t}^2, \mu^2) \frac{d^2 k_{1t}}{\pi} \frac{d^2 k_{2t}}{\pi}$$

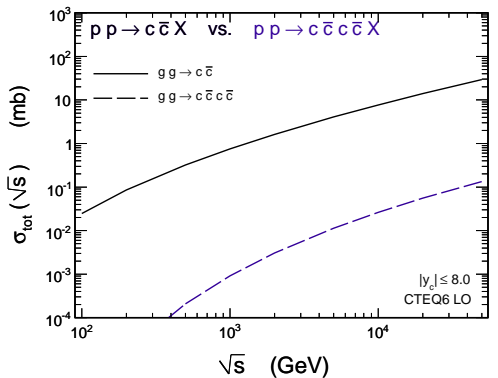
$$\frac{d\sigma}{dy_3 dy_4 d^2 p_{3,t} d^2 p_{4,t}} = \frac{1}{16\pi^2 \hat{s}^2} \int |\overline{\mathcal{M}}_{\text{off}}|^2 \delta(\vec{k}_{3t} + \vec{k}_{4t} - \vec{p}_{3t} - \vec{p}_{4t}) \mathcal{F}(x_3, k_{3t}^2, \mu^2) \mathcal{F}(x_4, k_{4t}^2, \mu^2) \frac{d^2 k_{3t}}{\pi} \frac{d^2 k_{4t}}{\pi}$$

Effectively **16 dimensions**, Monte Carlo method

Maciula-Szczurek, hep-ph-1301.4469, Phys. Rev. **D87** (2013) 074039.



# Single parton scattering $2 \rightarrow 4$ process?

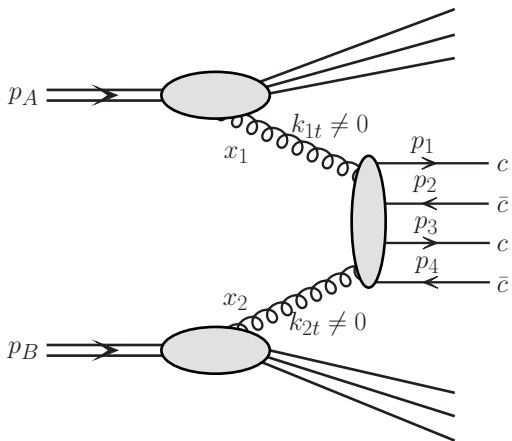


Only about 1 % at high energies

Much smaller than DPS production of  $c\bar{c}c\bar{c}$



# SPS in $k_t$ -factorization approach



include gluon transverse momenta

A. van Hameren, R. Maciula and A. Szczurek,

arXiv:1504.06490, Phys. Lett. **B748** (2015) 737.



# Results for $k_T$ -factorization approach

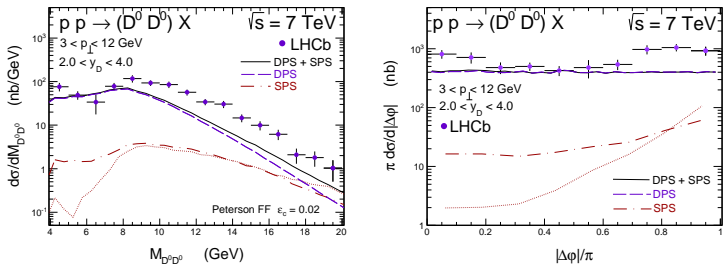


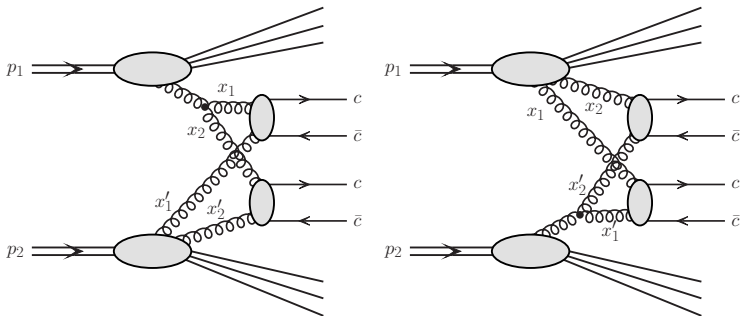
Figure: Distributions in  $D^0 D^0$  invariant mass (left) and in azimuthal angle between both  $D^0$ 's (right) within the LHCb acceptance. The DPS contribution (dashed line) and the SPS contribution within the  $k_T$ -factorization approach (dashed-dotted line). The collinear SPS result from our previous studies (dotted line).





# Parton splitting mechanism

There are perturbative mechanisms not included in conventional DPS.



Gaunt, Maciuła, Szczurek, Phys. Rev. **D90** (2014) 054017.



# A bit of formalism for parton splitting

Conventional DPS:

$$\sigma(2v2) = \frac{1}{2} \frac{1}{\sigma_{\text{eff},2v2}} \int dy_1 dy_2 d^2 p_{1\perp} dy_3 dy_4 d^2 p_{2\perp} \frac{1}{16\pi\hat{s}^2} \overline{|\mathcal{M}(gg \rightarrow c\bar{c})|^2} x_1 x'_1 x_2 x'_2 \times D^{gg}(x_1, x_2, \mu_1^2, \mu_2^2) D^{gg}(x_1, x_2, \mu_1^2, \mu_2^2)$$

Parton splitting DPS

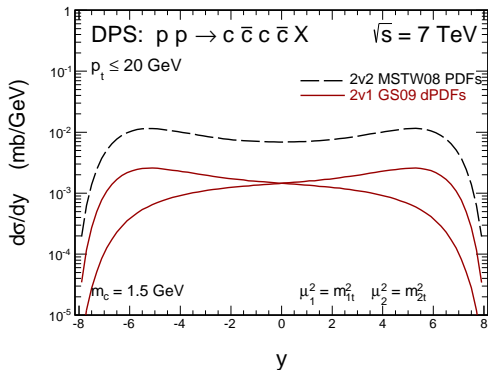
$$\sigma(2v1) = \frac{1}{2} \frac{1}{\sigma_{\text{eff},2v1}} \int dy_1 dy_2 d^2 p_{1\perp} dy_3 dy_4 d^2 p_{2\perp} \frac{1}{16\pi\hat{s}^2} \overline{|\mathcal{M}(gg \rightarrow c\bar{c})|^2} x_1 x'_1 x_2 x'_2 \times (\hat{D}^{gg}(x'_1, x'_2, \mu_1^2, \mu_2^2) D^{gg}(x_1, x_2, \mu_1^2, \mu_2^2) + D^{gg}(x'_1, x'_2, \mu_1^2, \mu_2^2) \hat{D}^{gg}(x_1, x_2, \mu_1^2, \mu_2^2))$$

There are two different normalization parameters. They are related in a geometrical picture.

Presence of the two components leads to a dependence of effective parameters on different kinematical variables.



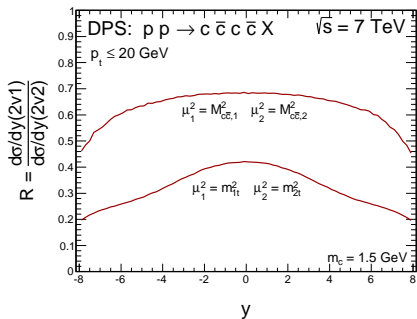
# Parton splitting vs conventional DPS



Asymmetric 1v2 and 2v1 contributions



# Parton splitting vs conventional DPS

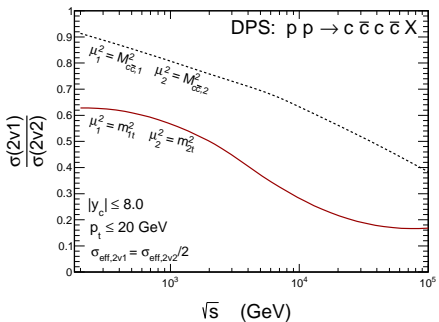


## Rapidity and factorization scale dependence

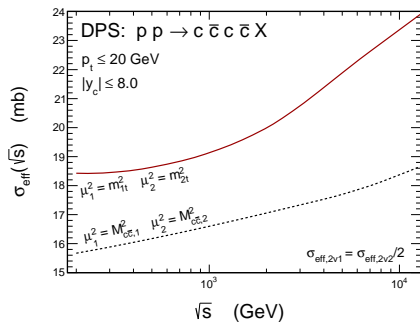
There could be also transverse momentum dependence.



# Parton splitting vs conventional DPS



# Parton splitting vs conventional DPS



$\sigma_{\text{eff}}$  is no longer a constant



# Gluon fragmentation to D mesons

- **Kniesl and Kramer** discussed several fragmentation of a parton (gluon,  $u, d, s, \bar{u}, \bar{d}, \bar{s}, c, \bar{c}$ ) to D mesons
- Important contribution to inclusive production of D mesons in  $p\bar{p}$  collisions comes from  $g \rightarrow D$  (**Kniesl, Kramer, Schienbein, Spiesberger**)
- Similar calculation in  $k_T$ -factorization by **Karpishkov, Nefedov, Saleev, Shipilova, 2015**.  
Good description of D meson transverse momentum distributions at the LHC (similar to **Maciula, Szczurek**).
- What are consequences of the "new" mechanism for **double D meson production**?  
(with **Maciula, Saleev and Shipilova** - work in preparation).



# DGLAP evolution of fragmentation functions

Fragmentation functions fulfill the DGLAP equation:

$$\frac{d}{d\ln\mu_f^2} D_a(x, \mu_f) = \frac{a_s(\mu)}{2\pi} \sum_b \int_x^1 \frac{dy}{y} P_{a \rightarrow b}^T(y, a_s(\mu)) D_b\left(\frac{x}{y}, \mu_f\right).$$

where  $a = g, u, \bar{u}, d, \bar{d}, s, \bar{s}, c, \bar{c}$

**Initial conditions:**

$$D_c(z, \mu_0^2) = N_c \frac{z(1-z)^2}{((1-z) + \epsilon)^2}$$

$$D_g(z, \mu_0^2) = 0.$$

In our case we will take:  $\mu^2 = m_f^2$

Fragmentation functions fitted (with **massless** DGLAP evolution) to  $e^+e^-$  data (with **mass effects** in the cross section)

A consequence of the evolution is a **much smaller contribution of  $gg \rightarrow c\bar{c} \rightarrow D$  mechanism at intermediate and large  $p_T$**  and **appearance of new terms.**





# Single D meson production

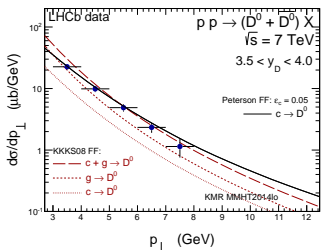
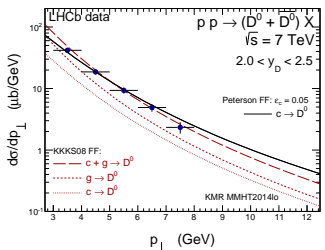


Figure: Left and right panels correspond to **two different rapidity intervals**. The Peterson  $c \rightarrow D$  FF (solid lines) are compared to the second scenario calculations with the KKKS08 FF (long-dashed lines) with  $c \rightarrow D$  (dotted) and  $g \rightarrow D$  (short-dashed) components that undergo DGLAP evolution equation.

Both methods describe the existing data



# New mechanisms

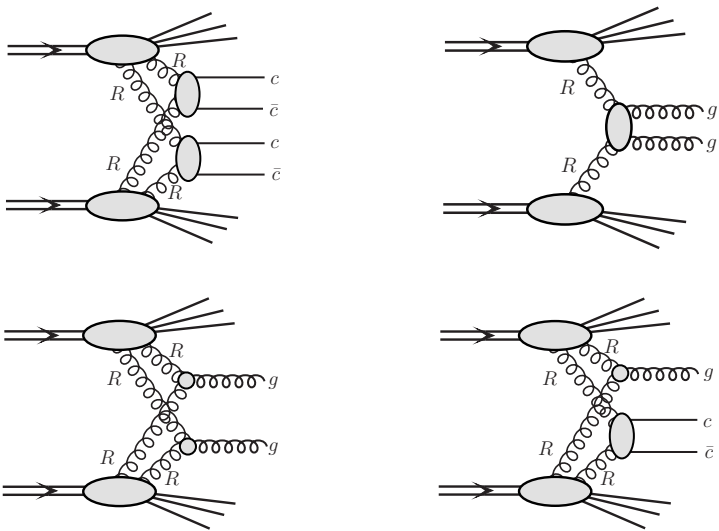


Figure: A diagrammatic illustration of the considered mechanisms. ▶



# DPS parton production mechanisms

DPS production of  $cc$  or  $gg$  system, assuming factorization of the DPS model:

$$\frac{d\sigma^{DPS}(pp \rightarrow ccX)}{dy_1 dy_2 d^2p_{1,t} d^2p_{2,t}} = \frac{1}{2\sigma_{\text{eff}}} \cdot \frac{d\sigma^{SPS}(pp \rightarrow c\bar{c}X_1)}{dy_1 d^2p_{1,t}} \cdot \frac{d\sigma^{SPS}(pp \rightarrow c\bar{c}X_2)}{dy_2 d^2p_{2,t}},$$

$$\frac{d\sigma^{DPS}(pp \rightarrow ggX)}{dy_1 dy_2 d^2p_{1,t} d^2p_{2,t}} = \frac{1}{2\sigma_{\text{eff}}} \cdot \frac{d\sigma^{SPS}(pp \rightarrow gX_1)}{dy_1 d^2p_{1,t}} \cdot \frac{d\sigma^{SPS}(pp \rightarrow gX_2)}{dy_2 d^2p_{2,t}}.$$

$$\frac{d\sigma^{DPS}(pp \rightarrow gcX)}{dy_1 dy_2 d^2p_{1,t} d^2p_{2,t}} = \frac{1}{2\sigma_{\text{eff}}} \cdot \frac{d\sigma^{SPS}(pp \rightarrow gX_1)}{dy_1 d^2p_{1,t}} \cdot \frac{d\sigma^{SPS}(pp \rightarrow c\bar{c}X_2)}{dy_2 d^2p_{2,t}}.$$

## SPS parton production mechanisms

In the  $k_T$ -factorization approach, the cross section for relevant SPS cross sections:

$$\frac{d\sigma^{SPS}(pp \rightarrow c\bar{c}X)}{dy_1 dy_2 d^2p_{1,t} d^2p_{2,t}} = \frac{1}{16\pi^2(x_1 x_2 S)^2} \int \frac{d^2k_{1t}}{\pi} \frac{d^2k_{2t}}{\pi} \overline{|\mathcal{M}_{RR \rightarrow c\bar{c}}|^2} \\ \times \delta^2(\vec{k}_{1t} + \vec{k}_{2t} - \vec{p}_{1t} - \vec{p}_{2t}) \mathcal{F}(x_1, k_{1t}^2, \mu^2) \mathcal{F}(x_2, k_{2t}^2, \mu^2),$$

$$\frac{d\sigma^{SPS}(pp \rightarrow ggX)}{dy_1 dy_2 d^2p_{1,t} d^2p_{2,t}} = \frac{1}{16\pi^2(x_1 x_2 S)^2} \int \frac{d^2k_{1t}}{\pi} \frac{d^2k_{2t}}{\pi} \overline{|\mathcal{M}_{RR \rightarrow gg}|^2} \\ \times \delta^2(\vec{k}_{1t} + \vec{k}_{2t} - \vec{p}_{1t} - \vec{p}_{2t}) \mathcal{F}(x_1, k_{1t}^2, \mu^2) \mathcal{F}(x_2, k_{2t}^2, \mu^2),$$

$$\frac{d\sigma^{SPS}(pp \rightarrow gX)}{dy d^2p_t} = \frac{\pi}{(x_1 x_2 S)^2} \int \frac{d^2k_{1t}}{\pi} \frac{d^2k_{2t}}{\pi} \overline{|\mathcal{M}_{RR \rightarrow g}|^2} \\ \times \delta^2(\vec{k}_{1t} + \vec{k}_{2t} - \vec{p}_t) \mathcal{F}(x_1, k_{1t}^2, \mu^2) \mathcal{F}(x_2, k_{2t}^2, \mu^2).$$



# Fragmentation

In order to calculate correlation observables for two mesons we follow the fragmentation function technique for hadronization process:

$$\begin{aligned} \frac{d\sigma_{cc}^{DPS}(pp \rightarrow DDX)}{dy_1 dy_2 d^2 p_{1t}^D d^2 p_{2t}^D} &= \int \frac{D_{c \rightarrow D}(z_1)}{z_1} \cdot \frac{D_{c \rightarrow D}(z_2)}{z_2} \cdot \frac{d\sigma^{DPS}(pp \rightarrow ccX)}{dy_1 dy_2 d^2 p_{1t}^c d^2 p_{2t}^c} dz_1 dz_2 \\ &+ \int \frac{D_{g \rightarrow D}(z_1)}{z_1} \cdot \frac{D_{g \rightarrow D}(z_2)}{z_2} \cdot \frac{d\sigma^{DPS}(pp \rightarrow ggX)}{dy_1 dy_2 d^2 p_{1t}^g d^2 p_{2t}^g} dz_1 dz_2 \\ &+ \int \frac{D_{g \rightarrow D}(z_1)}{z_1} \cdot \frac{D_{c \rightarrow D}(z_2)}{z_2} \cdot \frac{d\sigma^{DPS}(pp \rightarrow gcX)}{dy_1 dy_2 d^2 p_{1t}^g d^2 p_{2t}^c} dz_1 dz_2 \end{aligned}$$

where:  $p_{1t}^{g,c} = \frac{p_{1t}^D}{z_1}$ ,  $p_{2t}^{g,c} = \frac{p_{2t}^D}{z_2}$  and meson longitudinal fractions  $z_1, z_2 \in (0, 1)$ .

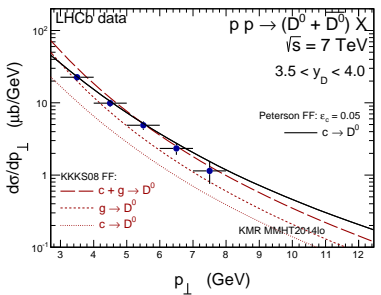
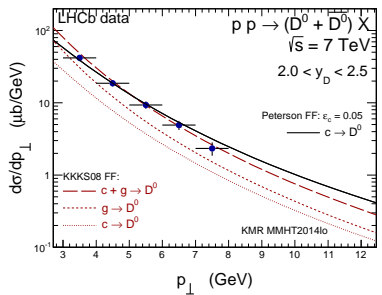
For SPS  $DD$ -production via digluon fragmentation:

$$\frac{d\sigma_{gg}^{SPS}(pp \rightarrow DDX)}{dy_1 dy_2 d^2 p_{1t}^D d^2 p_{2t}^D} \approx \int \frac{D_{g \rightarrow D}(z_1)}{z_1} \cdot \frac{D_{g \rightarrow D}(z_2)}{z_2} \cdot \frac{d\sigma^{SPS}(pp \rightarrow ggX)}{dy_1 dy_2 d^2 p_{1t}^g d^2 p_{2t}^g} dz_1 dz_2$$

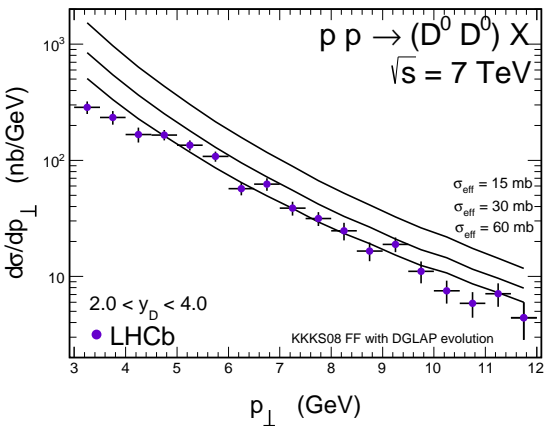
where:  $p_{1t}^g = \frac{p_{1t}^D}{z_1}$ ,  $p_{2t}^g = \frac{p_{2t}^D}{z_2}$  and meson longitudinal fractions  $z_1, z_2 \in (0, 1)$ .



# First results in the new approach



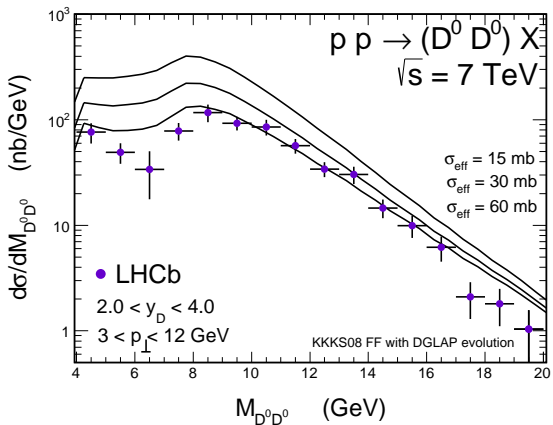
# Larger $\sigma_{\text{eff}}$



$\sigma_{\text{eff}} = 60 \text{ mb}$  describes the data



# Larger $\sigma_{\text{eff}}$

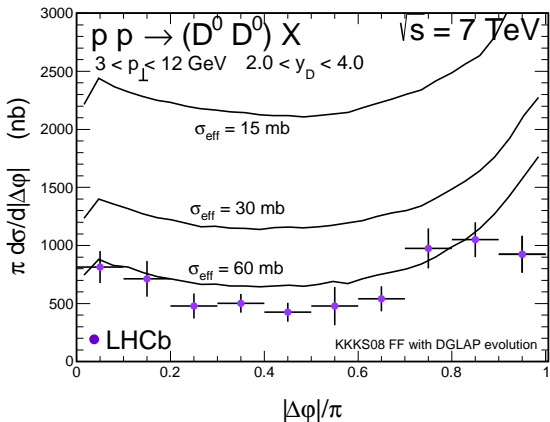


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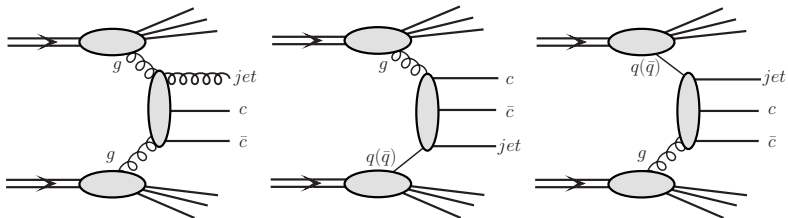
# Larger $\sigma_{\text{eff}}$



$\sigma_{\text{eff}} = 60 \text{ mb}$  describes the data



# First exploration of $c\bar{c}j$



Only SPS mechanisms  
full phase space



## Production of $c\bar{c}j$ in collinear factorization

$$\begin{aligned}
 d\sigma(pp \rightarrow c\bar{c} + jet) = & \int dx_1 dx_2 [g(x_1, \mu_F^2)g(x_2, \mu_F^2) d\hat{\sigma}_{gg \rightarrow c\bar{c}g} \\
 + & \Sigma_f q_f(x_1, \mu_F^2)g(x_2, \mu_F^2) d\hat{\sigma}_{qg \rightarrow c\bar{c}q} + g(x_1, \mu_F^2)\Sigma_f q_f(x_2, \mu_F^2) d\hat{\sigma}_{gq \rightarrow c\bar{c}q} \\
 + & \Sigma_f \bar{q}_f(x_1, \mu_F^2)g(x_2, \mu_F^2) d\hat{\sigma}_{\bar{q}g \rightarrow c\bar{c}\bar{q}} + g(x_1, \mu_F^2)\Sigma_f \bar{q}_f(x_2, \mu_F^2) d\hat{\sigma}_{g\bar{q} \rightarrow c\bar{c}\bar{q}}] ,
 \end{aligned}
 \tag{4}$$

where  $g(x_{1,2}, \mu_F^2)$ ,  $q_f(x_{1,2}, \mu_F^2)$  and  $\bar{q}_f(x_{1,2}, \mu_F^2)$  are the standard collinear parton distribution functions (PDFs) for gluons, quarks and antiquarks, respectively, carrying  $x_{1,2}$  momentum fractions of the proton and evaluated at the factorization scale  $\mu_F$ . Here,  $d\hat{\sigma}$  are the elementary partonic cross sections for a given  $2 \rightarrow 3$  subprocess



## Production of $c\bar{c}$ in $k_T$ -factorization

$$\begin{aligned}
 d\sigma(pp \rightarrow c\bar{c} + jet) = & \int dx_1 \frac{d^2k_{1t}}{\pi} dx_2 \frac{d^2k_{2t}}{\pi} [\mathcal{F}_g(x_1, k_{1t}^2, \mu_F^2) \mathcal{F}_g(x_2, k_{2t}^2, \mu_F^2) d\hat{\sigma}_{g^*g^* \rightarrow c\bar{c}} \\
 & + \mathcal{F}_q(x_1, k_{1t}^2, \mu_F^2) \mathcal{F}_g(x_2, k_{2t}^2, \mu_F^2) d\hat{\sigma}_{q^*g^* \rightarrow c\bar{c}q} + \mathcal{F}_g(x_1, k_{1t}^2, \mu_F^2) \mathcal{F}_q(x_2, k_{2t}^2, \mu_F^2) d\hat{\sigma}_{g^*q^* \rightarrow c\bar{c}q} \\
 & + \mathcal{F}_{\bar{q}}(x_1, k_{1t}^2, \mu_F^2) \mathcal{F}_g(x_2, k_{2t}^2, \mu_F^2) d\hat{\sigma}_{\bar{q}^*g^* \rightarrow c\bar{c}\bar{q}} + \mathcal{F}_g(x_1, k_{1t}^2, \mu_F^2) \mathcal{F}_{\bar{q}}(x_2, k_{2t}^2, \mu_F^2) d\hat{\sigma}_{g^*\bar{q}^* \rightarrow c\bar{c}\bar{q}}]
 \end{aligned}$$

Here,  $k_{1,2t}$  are transverse momenta of incident partons (new degrees of freedom) and  $\mathcal{F}(x, k_t^2, \mu_F^2)$ 's are transverse momentum dependent, so-called, unintegrated parton distribution functions (uPDFs)



# Results, collinear factorization

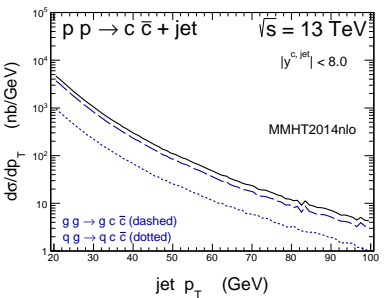
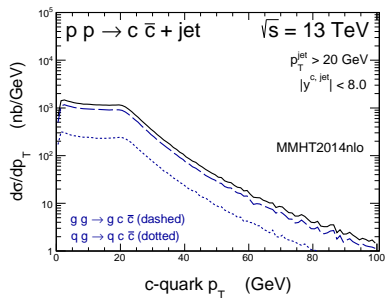


Figure: Transverse momentum distribution of c-quark (left panel) and associated jet (right panel) in the **collinear approach**.



## Results, collinear factorization

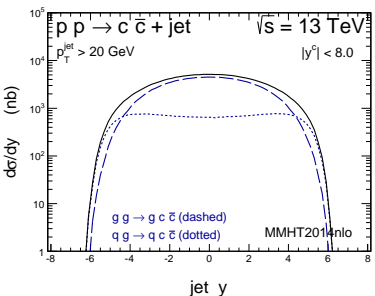
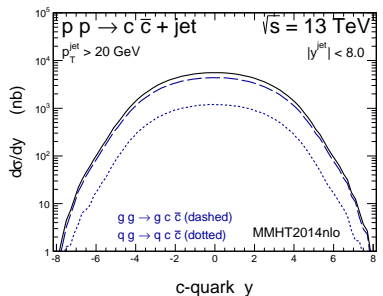


Figure: Rapidity distribution of c-quark (left panel) and associated jet (right panel) in the [collinear approach](#).



# Results, collinear factorization

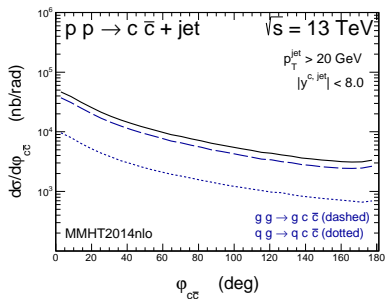
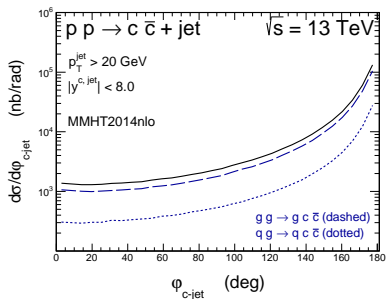


Figure: Distribution in azimuthal angle between c-quark and jet (left panel) and between c-quark and  $\bar{c}$ -antiquark (right panel) in the collinear approach.



# Results, $k_T$ -factorization

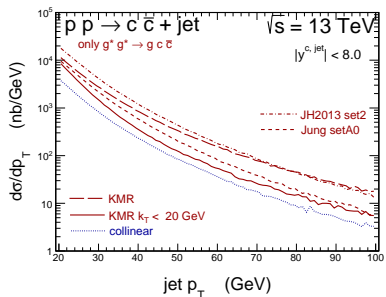
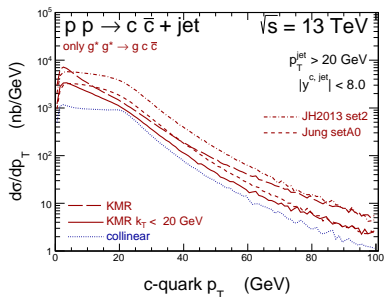


Figure: Transverse momentum distribution of c-quark (left panel) and associated jet (right panel) in the  $k_T$ -factorization approach with different uGDFs.





## Results, $k_T$ -factorization

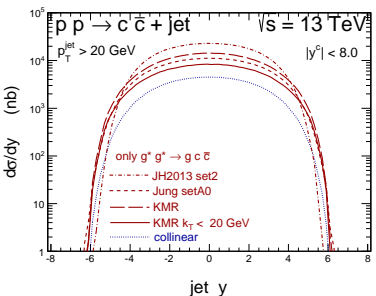
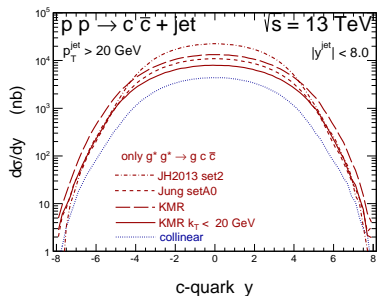


Figure: Rapidity distribution of c-quark (left panel) and associated jet (right panel) in the  $k_T$ -factorization approach with different uGDFs.



## Results, $k_T$ -factorization

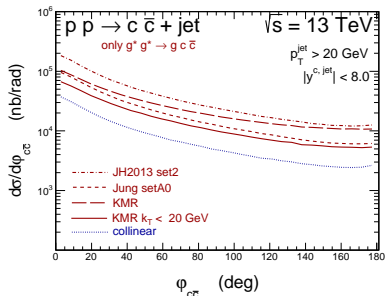
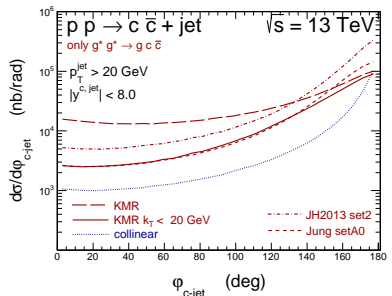


Figure: Distribution in azimuthal angle between c-quark and jet (left panel) and between c-quark and  $\bar{c}$ -antiquark (right panel) in the  $k_T$ -factorization approach with different uGDFs.



## Results, comparison of both methods

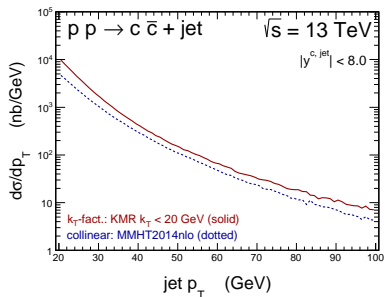
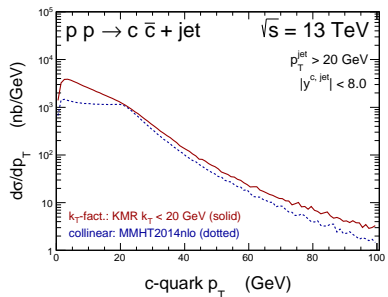


Figure: Comparison of transverse momentum distributions of c-quark (left panel) and associated jet (right panel) for collinear approach (dotted) and the  $k_T$ -factorization approach with the **KMR uGDF** and **extra cut on initial gluon transverse momenta** (solid).



## Results, comparison of both methods

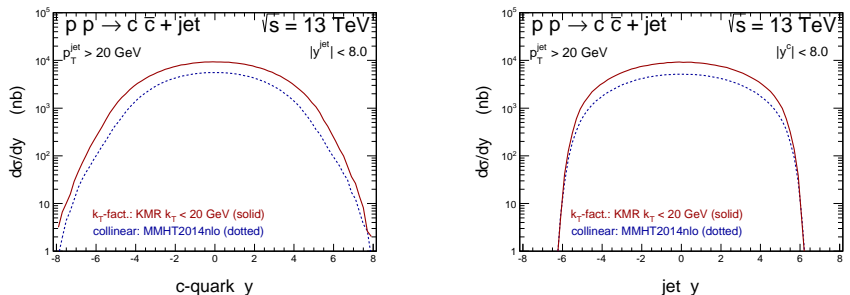


Figure: Comparison of rapidity distribution of c-quark (left panel) and associated jet (right panel) in the collinear approach (dotted) and the  $k_T$ -factorization approach with the **KMR  $u$ GDF** and **extra cut on initial gluon transverse momenta** (solid).



## Results, comparison of both methods

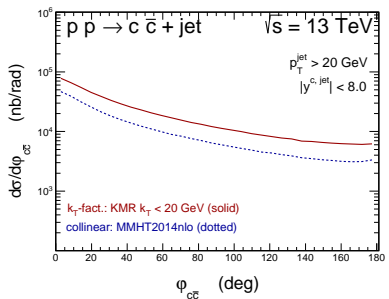
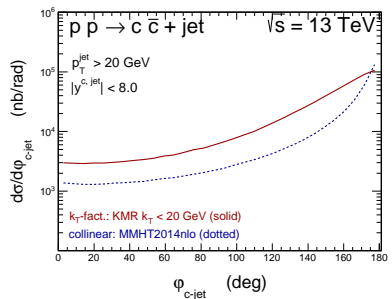


Figure: Comparison of distribution in azimuthal angle between c-quark and jet (left panel) and between c-quark and  $\bar{c}$ -antiquark (right panel) in the **collinear** approach (dotted) and in the  **$k_T$ -factorization** approach with the KMR uGDF and **extra cut on initial gluon transverse momenta** (solid).



# Predictions for $D^0 + jet$ production at the LHC

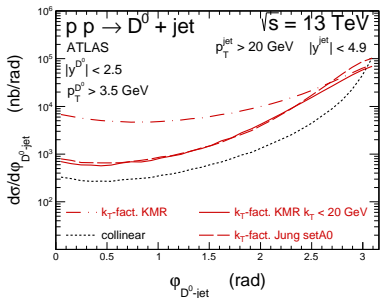


Figure: Azimuthal angle correlation between  $D^0$  meson and jet for [collinear](#) and  [\$k\_T\$ -factorization](#) approaches. The cuts are specified in the figure caption.



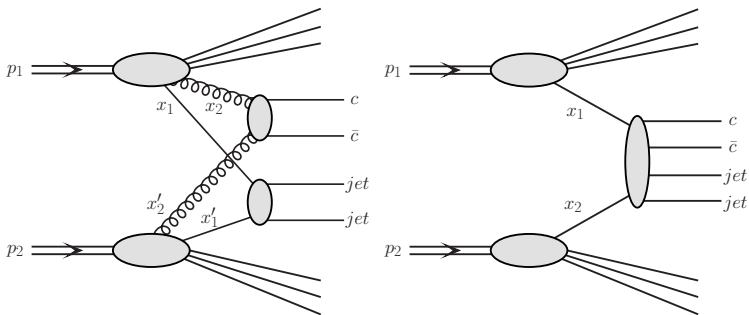
# Predictions for $D^0 + jet$ production at the LHC

**Table:** The calculated cross sections in microbarns for inclusive  $D^0 + jet$  production in  $pp$ -scattering at  $\sqrt{s} = 13$  TeV Here, the  $D^0$  meson is required to have  $|y^{D^0}| < 2.5$  and  $p_T^{D^0} > 3.5$  GeV and the rapidity of the associated jet is  $|y^{jet}| < 4.9$ , that corresponds to the ATLAS detector acceptance.

Cuts	collinear MMHT2014nlo	KMR	KMR $k_T < 20$
$p_T^{jet} > 20$ GeV	22.36	49.20	33.12
$p_T^{jet} > 35$ GeV	3.70	9.60	4.90
$p_T^{jet} > 50$ GeV	1.14	3.32	1.49



# First exploration of $pp \rightarrow c\bar{c}jj$



Both DPS and SPS mechanisms  
 full phase space





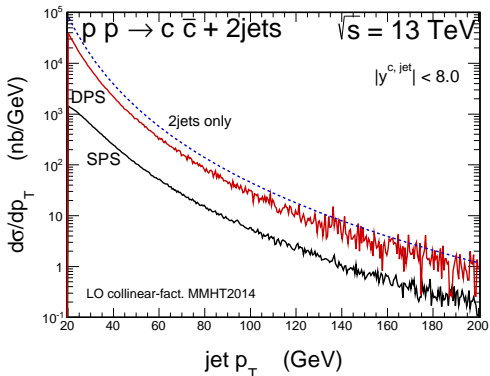
# Processes included in SPS

9 types:

- $gg \rightarrow ggc\bar{c}$
- $gg \rightarrow q\bar{q}c\bar{c}$
- $gq/\bar{q} \rightarrow gq/\bar{q}c\bar{c}$
- $q/\bar{q}g \rightarrow gq/\bar{q}c\bar{c}$
- $q\bar{q} \rightarrow q'\bar{q}'c\bar{c}$
- $q\bar{q} \rightarrow ggc\bar{c}$
- $qq \rightarrow qqc\bar{c}$
- $qq' \rightarrow qq'c\bar{c}$



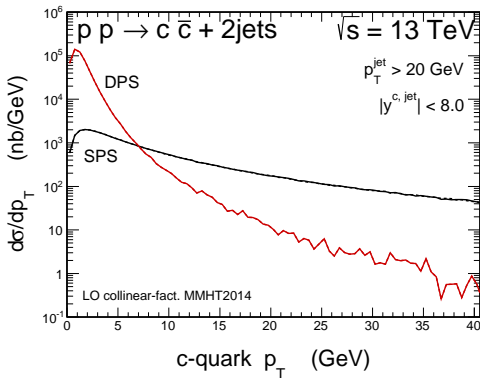
# Jet transverse momentum distribution



The cross section for dijets **only slightly bigger** than that for dijets associated with charm



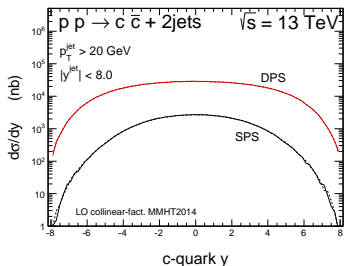
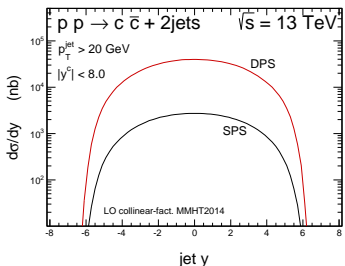
# Charm transverse momentum distribution



DPS dominates at low transverse momenta



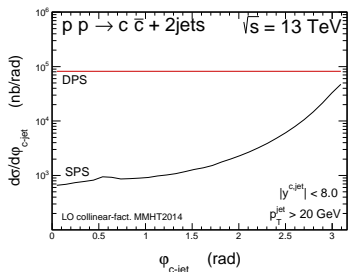
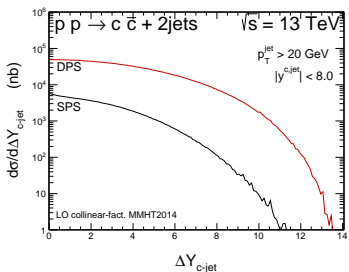
# Rapidity distributions



The charm DPS distribution broader than charm SPS distribution



## Other distributions

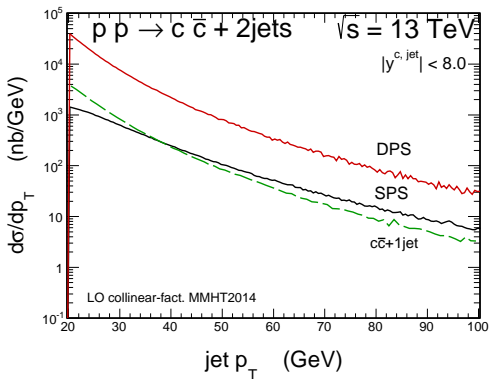


The DPS distribution in  $\Delta\eta_{c_j}$  is broader than its SPS counterpart

The distribution in  $\phi_{c_j}$  should be **very flat**.



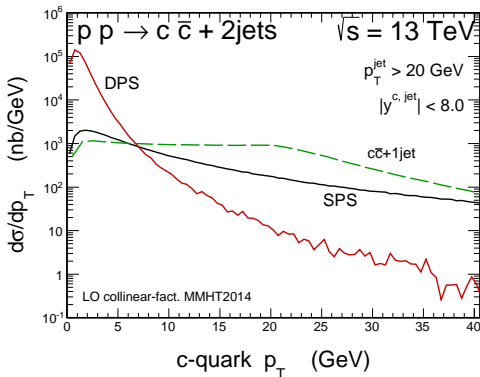
# Comparison of $c\bar{c}j$ and $c\bar{c}jj$



$c\bar{c}jj$  much bigger than  $c\bar{c}j$



# Comparison of $c\bar{c}j$ and $c\bar{c}jj$



Summary:

$c\bar{c} > c\bar{c}jj(\text{DPS}) \sim jj > c\bar{c}jj(\text{SPS}) \sim c\bar{c}j$



# Conclusions

- $k_T$ -factorization provides good description of charm production at RHIC and LHC.
- Surprisingly large cross sections for inclusive  $c\bar{c}c\bar{c}$  due to DPS.
- Relatively small cross sections for SPS  $c\bar{c}c\bar{c}$ .
- **Multiple  $c\bar{c}$  pairs** can be produced in p p collisions at the LHC and FCC.
- Look at correlations between **same flavour charmed mesons** such as  $D^0D^0$ .
- Look at correlations between  $e^+\mu^+$  or  $e^-\mu^-$  from semileptonic decays (ALICE, CMS).
- **Enhancement of the number of  $c\bar{c}$  pairs in AA collisions**
  - important for recombination/coalescence
  - further **enhancement of hidden-charm meson production** ( $J/\psi, \psi'$ ) at higher energies.





## Conclusion, continued

- Gluon fragmentation changes the picture.
- Several new contributions (both DPS and SPS)
- $d\sigma/d\phi_{DD} \neq \text{const}$   
Difficult to get it from DPS mechanisms (Echevarria, Kasemets, Mulders, Pisano) as spin correlations.
- Too big  $D^0\bar{D}^0$  cross section with canonical value  $\sigma_{\text{eff}} = 15 \text{ mb}$ .
- Possible solutions:
  - larger  $\sigma_{\text{eff}}$  (good reasons) (larger rapidity)
  - wrong small-x UGDF, saturation? (strong effect)
  - wrong large-x UGDF ?
  - problems with massless evolution of FF ?
- We can describe the LHCb data with strongly reduced  $\sigma_{\text{eff}}$  and strongly modified low-x glue. Are the strong low-x modifications consistent with other processes?



## Conclusion, continued

- First theoretical study related to associated production of charm and single jet production.
- We have limited to  $c$  ( $\bar{c}$ ) quark level and full phase space.
- The results, one dimensional and two-dimensional distributions, with the KMR uGDF and a practical correction to exclude production of more than one jet are very similar as those obtained within the collinear approach.
- We have performed first feasibility studies for ATLAS (and/or CMS) cuts. We have obtained rather large cross section.
- We have presented first calculations for  $c\bar{c}jj$  within [collinear factorization approach](#)
- DPS contribution much larger than SPS contribution
- SPS  $c\bar{c}jj$  [of the same order as](#) SPS  $c\bar{c}j$
- $\sigma(jj) \sim \sigma(jj c\bar{c})$  - search for associated production of charm outside of the jets to identify DPS.

