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Measurements of hadronic form factors at BESIII

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On behalf of BESIII Collaboration

Outline

👉 Motivations

👉 Data samples

👉 Measurement of cross sections

👉 Extraction of form factors

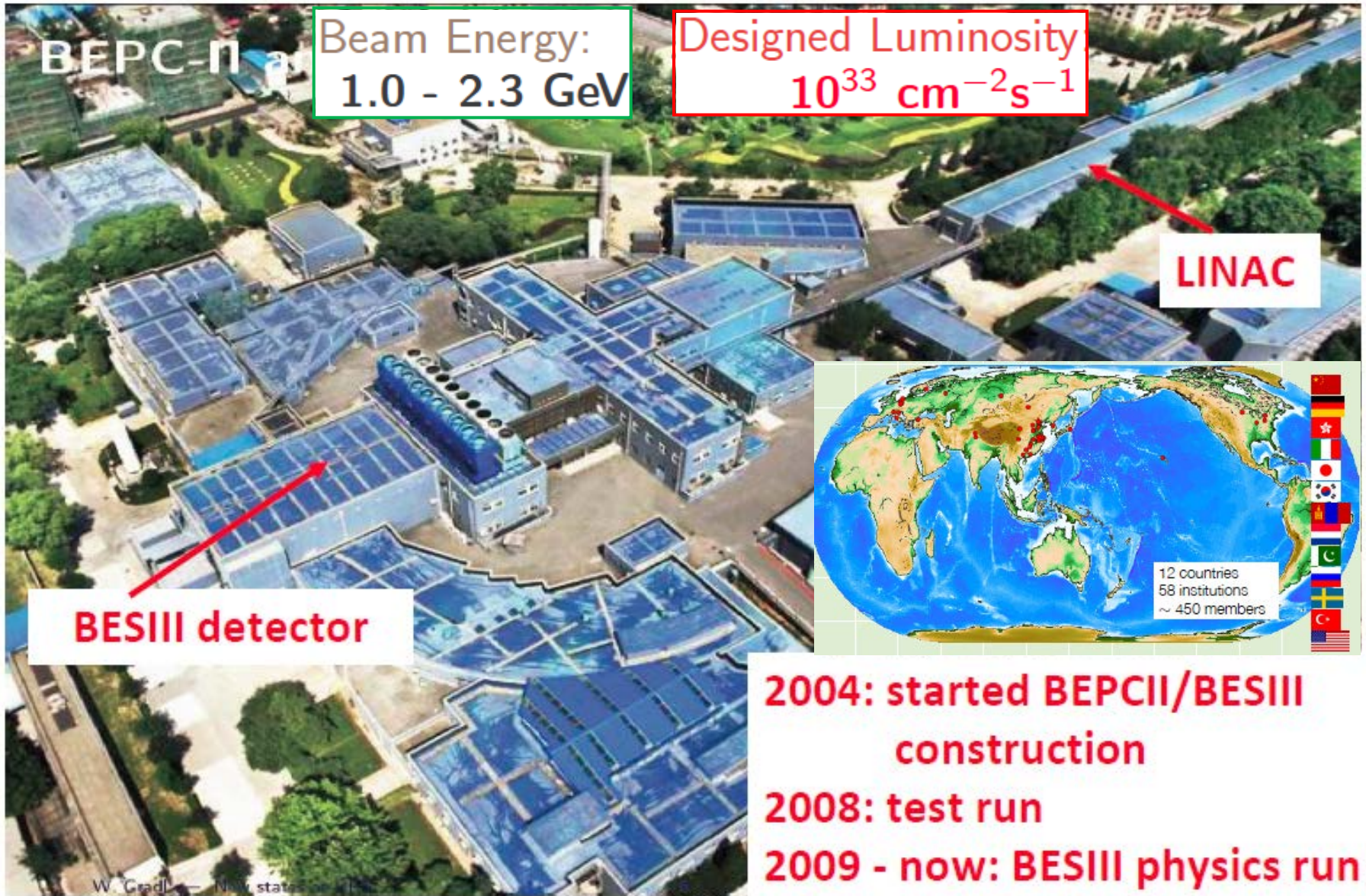
- $e^+e^- \rightarrow p\bar{p}$

- $e^+e^- \rightarrow \pi^+\pi^-$

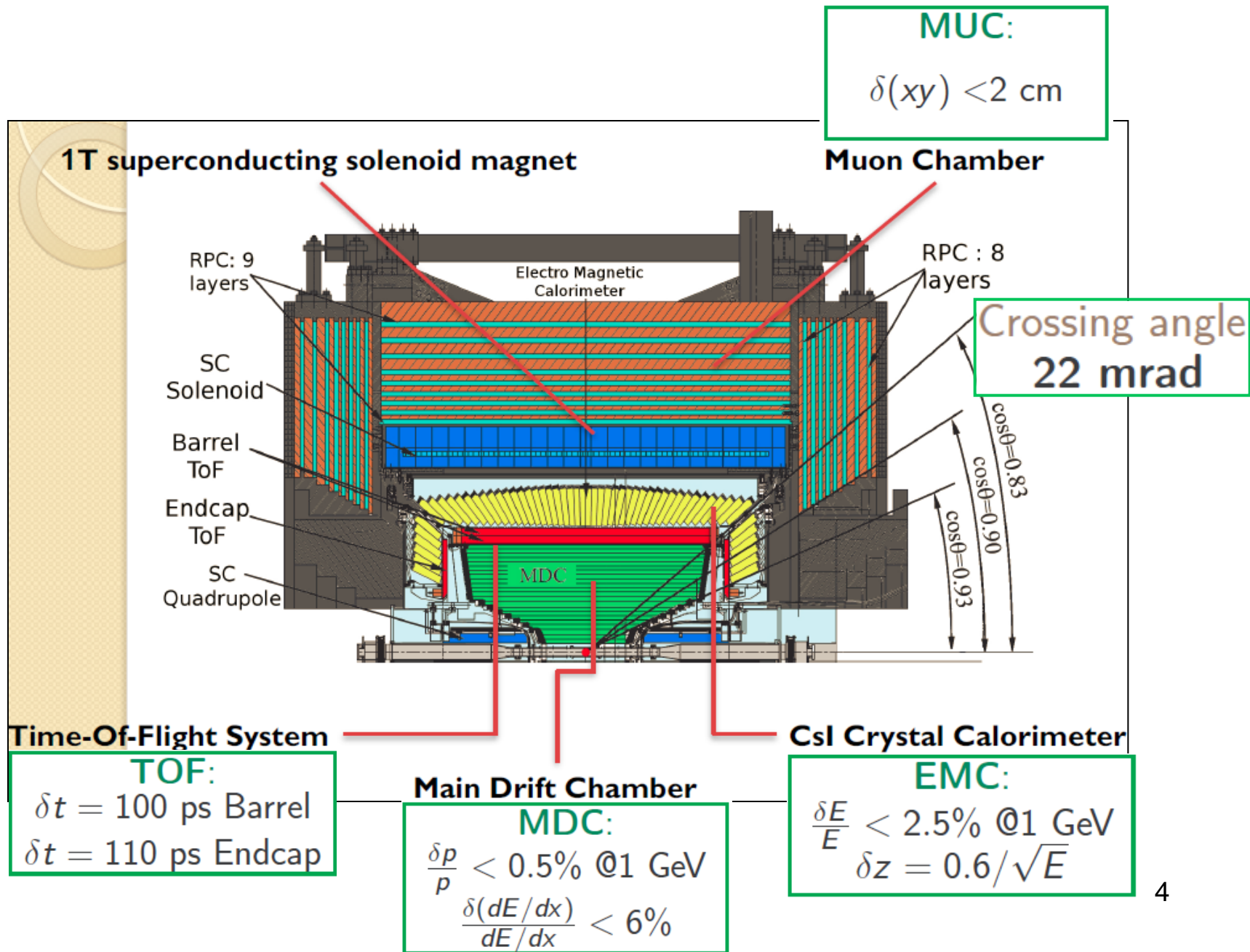
- $e^+e^- \rightarrow \Lambda_c^+\bar{\Lambda}_c^-$

👉 Summary

Beijing Electron-Positron Collider II (BEPCII)



Beijing Spectrometer III (BESIII)



Data samples of BESIII

Taking data	Total Num. / Lum.	Taking time
J/ψ	225+1086 M	2009+2012
$\psi(2S)$	106+350 M	2009+2012
$\psi(3770)$	2916 pb ⁻¹	2010~2011
τ scan	24 pb ⁻¹	2011
Y(4260)/Y(4230)/Y(4360)/scan	806/1054/523/488 pb ⁻¹	2012~2013
4600/4470/4530/4575/4420	506/100/100/42/993 pb ⁻¹	2014
J/ψ line-shape scan	100 pb ⁻¹	2012
R scan (2.23, 3.40) GeV	12 pb ⁻¹	2012
R scan (3.85, 4.59) GeV	795 pb ⁻¹	2013~2014
R scan (2.0, 3.08) GeV	~525 pb ⁻¹	2014~2015
Y(2175)	~100 pb ⁻¹	2015


Other newly collected data samples

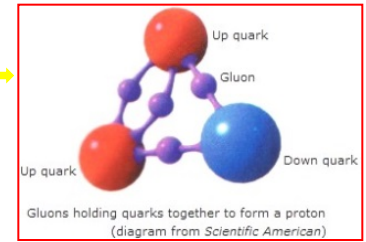


Part 1

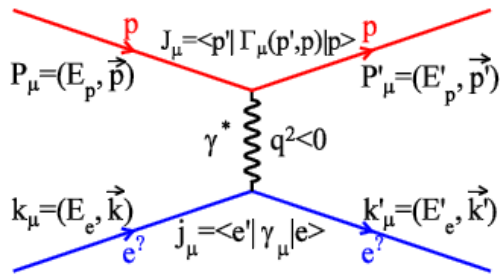
$$e^+ e^- \rightarrow p \bar{p}$$

Motivation

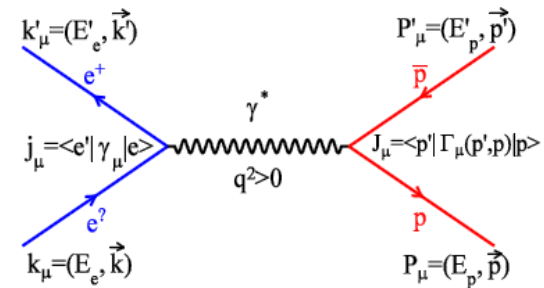
- The valence-quark picture of proton in quark model: 
- The structure of proton can be measured in two processes:



$$e^\pm p \rightarrow e^\pm p \quad (\text{space-like } q^2 < 0)$$



$$e^+e^- \rightarrow p \bar{p} \quad (\text{time-like } q^2 > 0)$$



BESIII

- Vector current of the interaction vertex with hadronic structure

$$\Gamma_\mu(p', p) = \gamma_\mu F_1(q^2) + \frac{i\sigma_{\mu\nu}q^\nu}{2m_p} F_2(q^2)$$

- Structure functions F_1 and F_2 can be recombined into two form factors

- **Electronic:** $G_E(q^2) = F_1(q^2) + \tau \kappa_p F_2(q^2)$

- **Magnetic:** $G_M(q^2) = F_1(q^2) + \kappa_p F_2(q^2)$

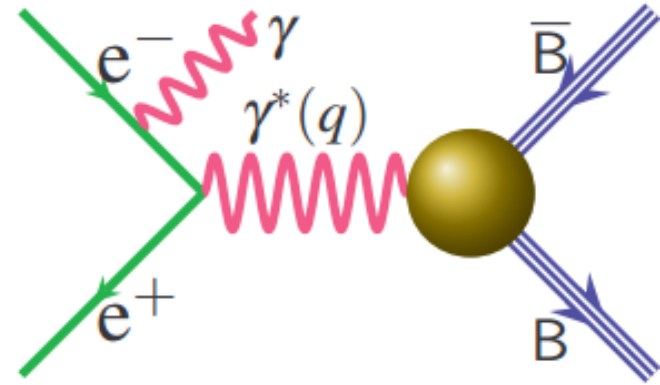
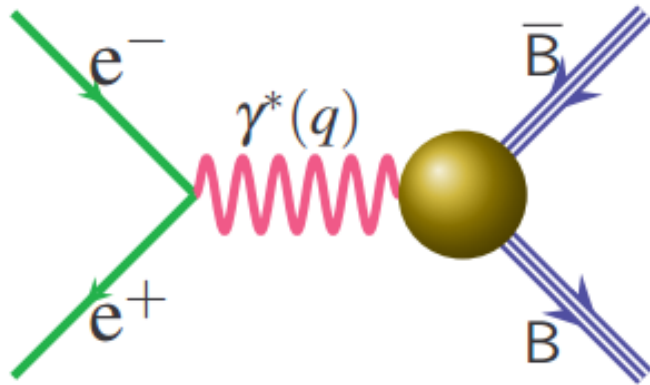
$$\tau = \frac{q^2}{4m_p^2}, \quad \kappa_p = \frac{g_p - 2}{2} = \mu_p - 1$$

- G_E and G_M relate to the spatial distribution of charge and magnetization in Breit-frame, the charge density distribution:

$$\rho(\vec{r}) = \int \frac{d^3q}{2\pi^3} e^{-i\vec{q}\cdot\vec{r}} \frac{M}{E(\vec{q})} G_E(\vec{q}^2)$$

Two methods

For time-like process



$$x \equiv 2E_\gamma / \sqrt{s}$$

	Energy Scan	Initial State Radiation
E_{beam}	discrete	fixed
\mathcal{L}	low at each beam energy	high at one beam energy
σ	$\frac{d\sigma_{p\bar{p}}}{d(\cos\theta)} = \frac{\alpha^2 \beta C}{2 q^2} [G_M ^2 (1 + \cos^2\theta) + \frac{4m_p^2}{q^2} G_E ^2 \sin^2\theta]$	$\frac{d^2\sigma_{p\bar{p}\gamma}}{dx d\theta_\gamma} = W(s, x, \theta_\gamma) \sigma_{p\bar{p}}(q^2)$ $W(s, x, \theta_\gamma) = \frac{\alpha}{\pi x} \left(\frac{2 - 2x + x^2}{\sin^2\theta_\gamma} - \frac{x^2}{2} \right)$
q^2	single at each beam energy	from threshold to s

This talk

In progress

Cross section

- For the reaction $e^+e^- \rightarrow p\bar{p}$, differential cross section:

$$\frac{d\sigma}{d\Omega} = \frac{\alpha^2\beta}{4s} C [|G_M(s)|^2 (1 + \cos^2\theta) + \frac{1}{\tau} |G_E(s)|^2 \sin^2\theta]$$

$$\beta = \sqrt{1 - 4M^2/s}$$

$$\tau = s/4M^2,$$

$$y = \pi\alpha M/\beta\sqrt{s}$$

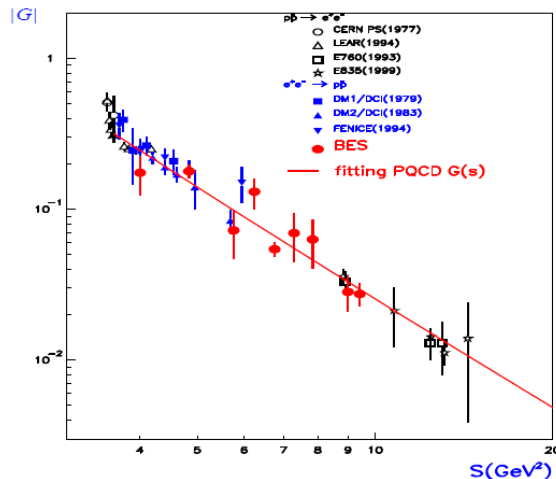
- the Born cross section

$$\sigma = \frac{4\alpha^2\pi\beta}{3s} C [|G_M(s)|^2 + \frac{1}{2\tau} |G_E(s)|^2]$$

- Coulomb correction C is subtle and important near threshold ($\beta \rightarrow 0$).

$$C = \frac{y}{1 - \exp(-y)}$$

- Due to the limited statistics, early experiments assume $|G_E| = |G_M| \equiv |G|$



BES Collaboration, Phys. Lett. B630, (2005)14

- BESII measured $|G|$ and parameterized as (Λ : QCD scale, A : free parameter)

$$|G(s)| = \frac{A}{s^2 \ln^2(s/\Lambda^2)}$$

Some question to make clear

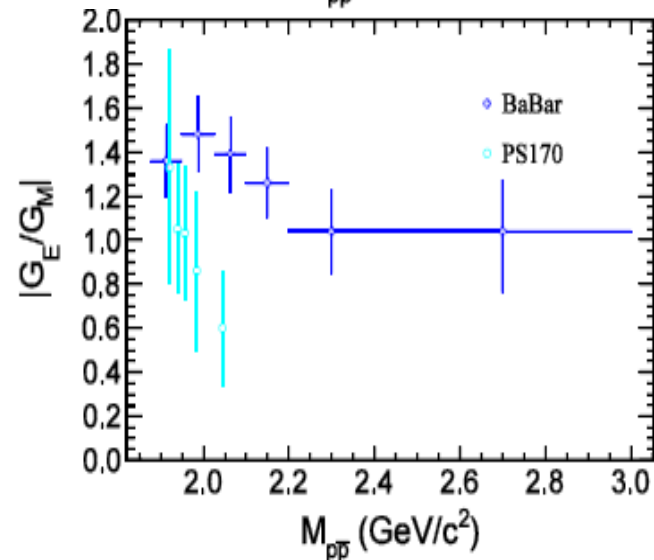
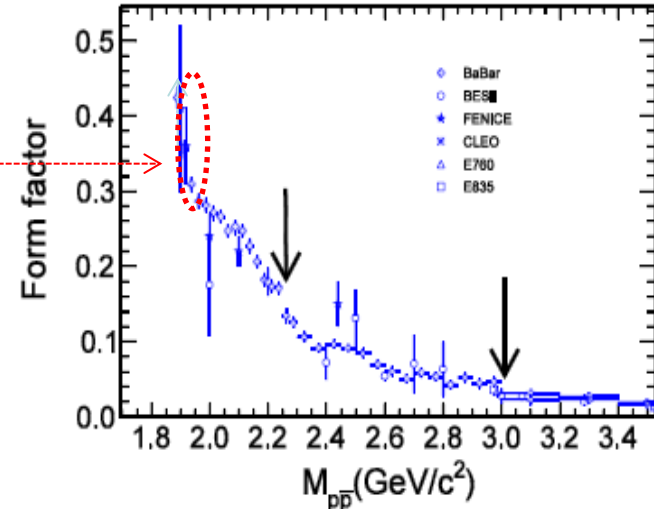
- Recent years, statistics of data samples increased, the behavior of form factor seems clear, but some questions still left:

- steep rise toward threshold ?
- two rapid decreases around 2.25 and 3.0 GeV ?

Are they true?

- ratio $|G_E/G_M|$ disagreement by PS170 and BaBar
- poor precision ($\sim 11\%$, 43%)
- limited energy range

which one is reliable?

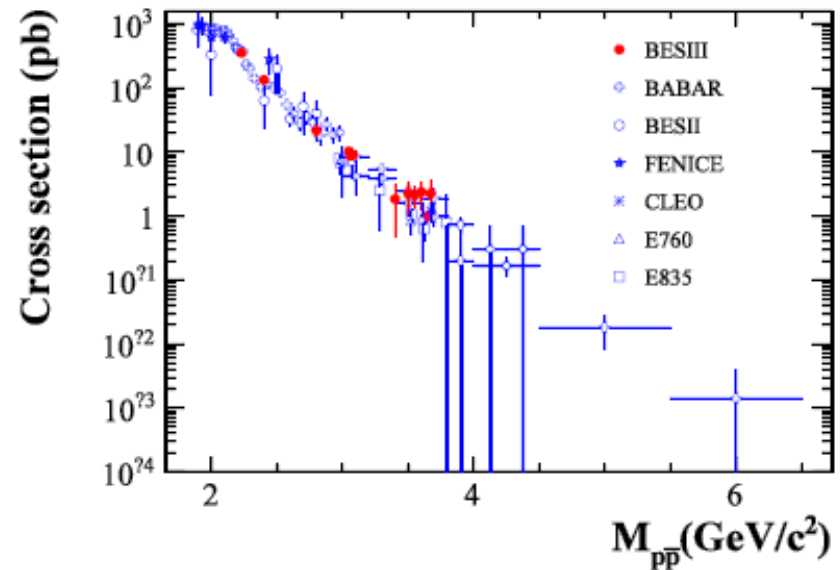
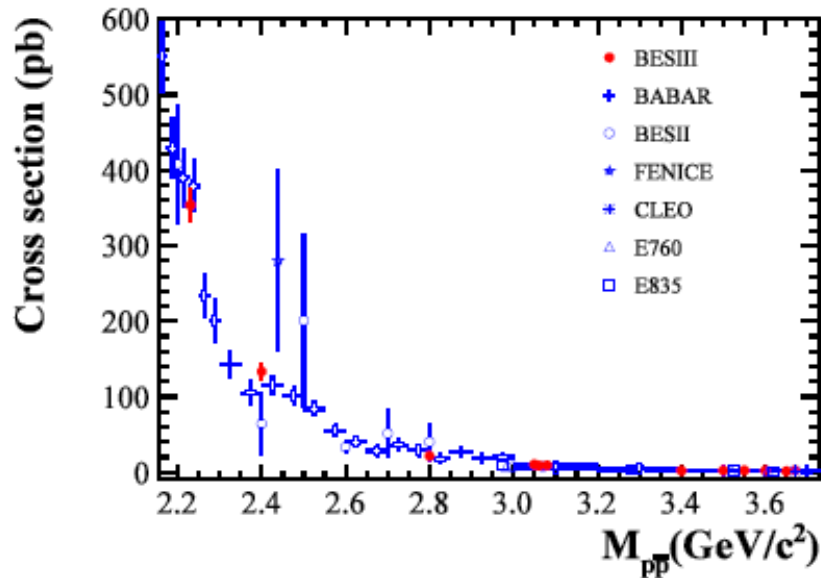


Measurement of cross section

Experimental formula for cross section:

$$\sigma_{\text{Born}} = \frac{N_{\text{obs}} - N_{\text{bkg}}}{L \cdot \epsilon \cdot (1 + \delta)}$$

- N_{obs} : the observed number of signal in data
- N_{bkg} : the number of background evaluated from MC
- L : the integral luminosity
- ϵ : detection efficiency by MC sample, with Conexc generator
- $(1 + \delta)$: radiative correction factor



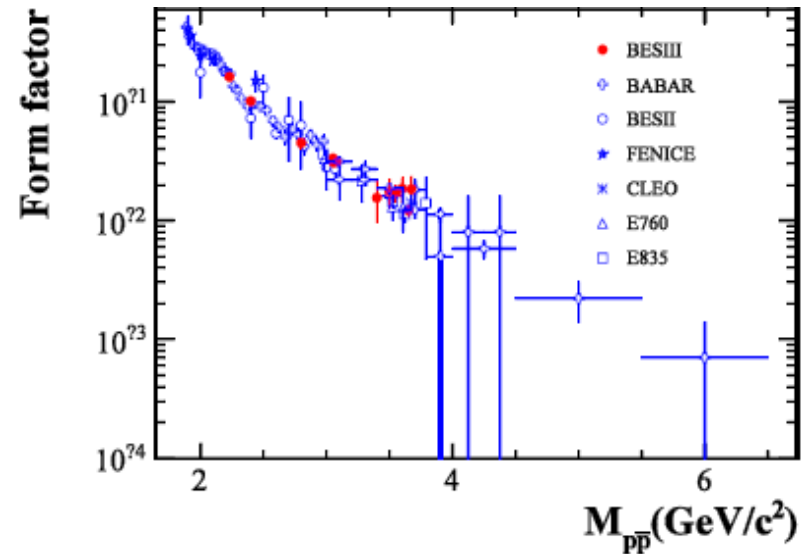
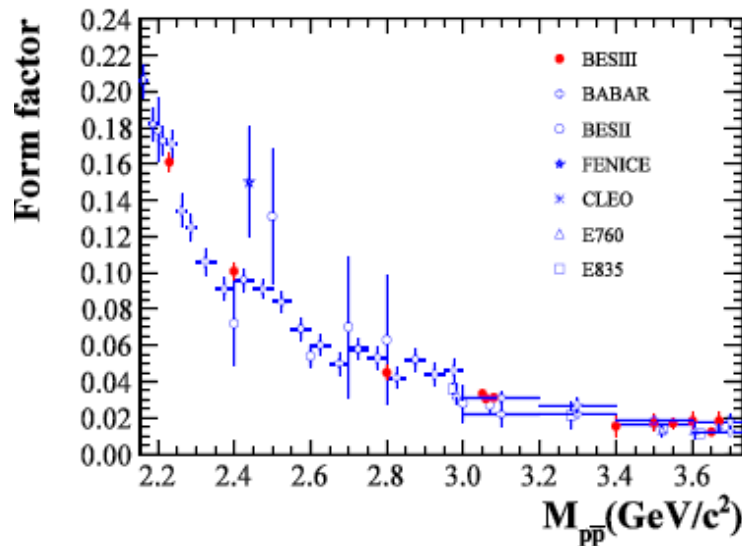
Extraction of effective form factor

- In order to compare with earlier measurements, it is still assumed $|G_E|=|G_M|\equiv|G_{eff}|$, and the cross section reads

$$\sigma = \frac{\pi\alpha^2}{3m_p^2\tau} \left[1 + \frac{1}{2\tau} \right] |G_{eff}|^2$$

- The effective form factor could be extracted

$$G_{eff} = \sqrt{\frac{\sigma_{Born}}{86.83 \cdot \frac{\beta}{s} \left(1 + \frac{2m_p^2}{s} \right)}}$$



- The BESIII results are consistent with other measurements within errors.

Extraction of electromagnetic $|G_E/G_M|$ ratio

- Angular distribution:

$$\frac{d\sigma}{d\Omega}(q^2) = \frac{\alpha^2\beta}{4s} |G_M(s)|^2 \left[(1 + \cos^2\theta_p) + R_{em}^2 \frac{1}{\tau} \sin^2\theta_p \right]$$

- $R_{em} = G_E(q^2)/G_M(q^2)$
- θ_p : polar angle of proton

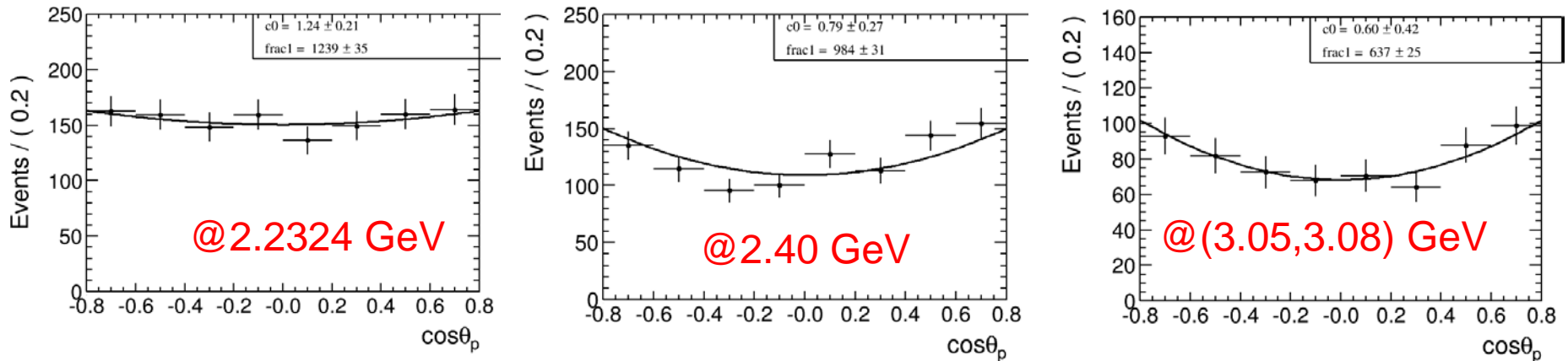
- Fit function:

$$\frac{dN}{d\cos\theta_p} = N_{norm} \left[(1 + \cos^2\theta_p) + R_{em}^2 \frac{1}{\tau} \sin^2\theta_p \right]$$

the overall normalization

$$N_{norm} = \frac{2\pi\alpha^2\beta L}{4s} \left[1.94 + 5.04 \frac{m_p^2}{s} R^2 \right] G_M(s)^2$$

- Results:



Extraction of electromagnetic $|G_E/G_M|$ ratio

- Moment method:

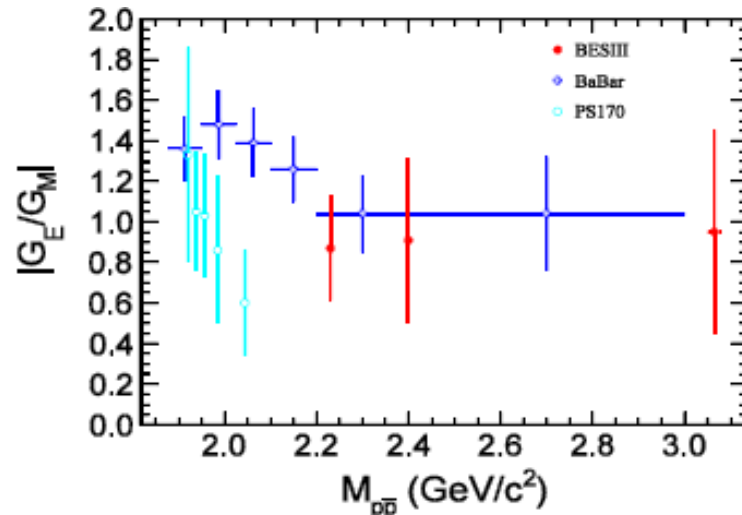
- second moment of $\cos\theta_p$: $\langle \cos^2\theta_p \rangle = \frac{1}{N_{\text{norm}}} \int \cos^2\theta_p \frac{d\sigma}{d\Omega} d\cos\theta_p$

- Estimator of $\cos\theta_p$: $\langle \cos^2\theta_p \rangle = \overline{\cos^2\theta_p} = \frac{1}{N} \sum_{i=1}^N \cos^2\theta_{p_i} / \epsilon_i$

- Extraction of $|G_E/G_M| = R = \sqrt{\frac{s}{4m_p^2} \frac{\langle \cos^2\theta_p \rangle - 0.243}{0.108 - 0.648 \langle \cos^2\theta_p \rangle}}$

- Uncertainty: $\langle \cos^2\theta_p \rangle: \sigma_{\langle \cos^2\theta_p \rangle} = \sqrt{\frac{1}{N-1} [\langle \cos^4\theta_p \rangle - \langle \cos^2\theta_p \rangle^2]}$

- Result:



- BESIII measurements are consistent with BaBar's, but not with PS170.

The electromagnetic ratio $|G_E/G_M|$

\sqrt{s} (MeV)	$ G_E/G_M $	$ G_M $ ($\times 10^{-2}$)	χ^2/ndf
		Fit on $\cos \theta_p$	
2232.4	$0.87 \pm 0.24 \pm 0.05$	$18.42 \pm 5.09 \pm 0.98$	1.04
2400.0	$0.91 \pm 0.38 \pm 0.12$	$11.30 \pm 4.73 \pm 1.53$	0.74
(3050.0, 3080.0)	$0.95 \pm 0.45 \pm 0.21$	$3.61 \pm 1.71 \pm 0.82$	0.61
		<i>method of moment</i>	
2232.4	0.83 ± 0.24	18.60 ± 5.38	-
2400.0	0.85 ± 0.37	11.52 ± 5.01	-
(3050.0, 3080.0)	0.88 ± 0.46	3.34 ± 1.72	-

Phys. Rev. D 91, 112004. (June 9, 2015)



Part 2

$$e^+ e^- \rightarrow \pi^+ \pi^- \gamma$$

Motivation

The Dirac equation of a charged fermion in electromagnetic field (\vec{A}, \vec{B})

$$i\hbar \frac{\partial}{\partial t} \varphi = \left[\frac{1}{2m} \left(\vec{P} + \frac{e}{c} \vec{A} \right)^2 + \frac{e\hbar}{2mc} \vec{\sigma} \cdot \vec{B} - e\phi \right] \varphi$$

- point-like fermion has magnetic moment

$$\vec{\mu} = -\frac{e\hbar}{2mc} \vec{\sigma} = -\frac{e}{mc} \vec{S}$$

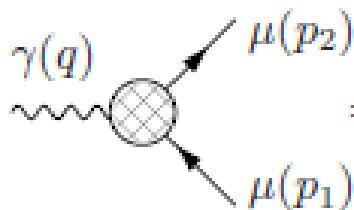
- define Bohr magneton:

$$\mu_B = \frac{e\hbar}{2mc}$$

- the magnetic moment of bare fermion:

$$\mu = g\mu_B S \quad \boxed{g = 2}$$

- considering the radiative correction of the vertex



$\Rightarrow g \neq 2 \Rightarrow$ anomalous magnetic moment: $a_\mu = (g_\mu - 2)/2$

Motivation

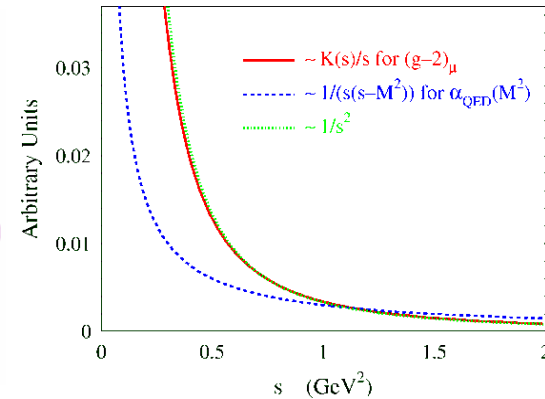
The Standard Model (SM) prediction for muon ($g-2$):

$$\begin{aligned}
 a_{\mu}^{\text{SM}} &= a_{\mu}^{\text{QED}} + a_{\mu}^{\text{had,LO}} + a_{\mu}^{\text{had,HO}} + a_{\mu}^{\text{had,LBL}} + a_{\mu}^{\text{weak}} \\
 &= \text{[Diagrams]} \\
 &= \text{(QED)} \quad (11\,658\,470.35 \pm 0.28) 10^{-10} \text{ (5-loop!)} \\
 &+ \text{(had,LO)} \quad (684.7 \text{ to } 709.0 \pm 6) 10^{-10} \text{ (Big spread, largest error)} \\
 &+ \text{(had,HO)} \quad (-10.0 \pm 0.6) 10^{-10} \\
 &+ \text{(had,LBL)} \quad (8.0 \pm 4.0) 10^{-10} \text{ (sign change since 1998)} \\
 &+ \text{(weak)} \quad (15.4 \pm 0.2) 10^{-10} \text{ (2-loop)}
 \end{aligned}$$

$a_{\mu}^{\text{had,LO}}$ from data via dispersion integral

$$a_{\mu}^{\text{had,LO}} = \frac{1}{4\pi^3} \int_{4m_{\pi}^2}^{\infty} \sigma_{\text{had}}^0(s) K(s) ds$$

Recent data included CMD-2,
SND, BES 2-5 GeV, ALEPH τ .
NEW: CMD-2 prelim update



σ_{had}^0 bare cross-section for $e^+e^- \rightarrow \text{hadrons}$, i.e. taking out radiative corrections.
QED kernel $K(s) \sim m_{\mu}^2/3s$, gives strong weight to low energy data.

Motivation

Ratio of the contribution to theoretical uncertainty of $(g-2)$ from the measured hadronic cross section in different energy region:

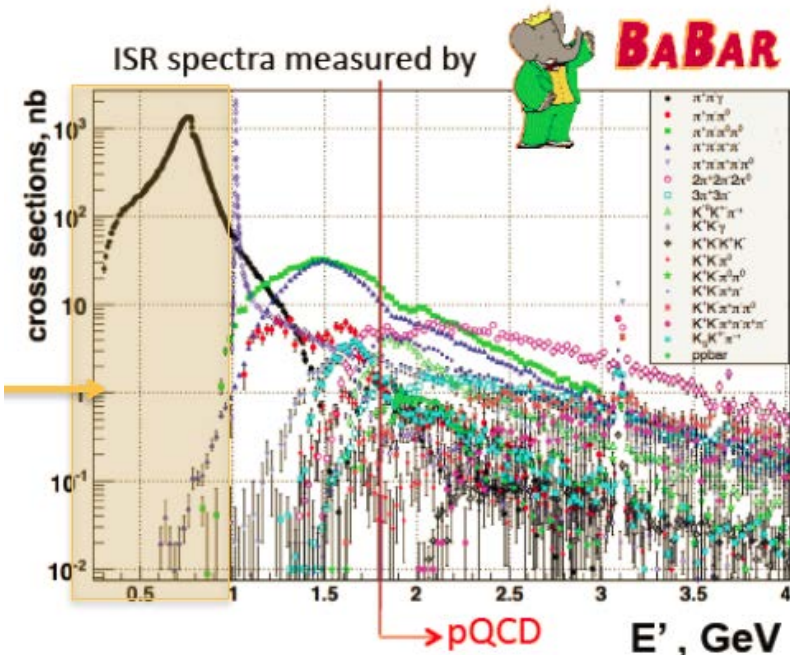
$a_\mu^{\text{had,LO}}$ from data via dispersion integral

$$a_\mu^{\text{had,LO}} = \frac{1}{4\pi^3} \int_{4m_\pi^2}^{\infty} \sigma_{\text{had}}^0(s) K(s) ds$$

$$K(s) \propto 1/s \quad \sigma(s) \propto 1/s$$

The largest contribution is below 1 GeV.

Channel $e^+e^- \rightarrow \pi^+\pi^-$ is the most important one



Motivation

Discrepancy between SM and experiments:

$$a_\mu^{\text{EXP}} = 116592089 (63) \times 10^{-11}$$

E821 - Final Report: PRD73 (2006) 072
with latest value of $\lambda = \mu_b/\mu_p$ (Codata '06)

$a_\mu^{\text{SM}} \times 10^{11}$	$(\Delta a_\mu = a_\mu^{\text{EXP}} - a_\mu^{\text{SM}}) \times 10^{11}$	σ
[1] 116 591 773 (53)	316 (82)	3.8
[2] 116 591 782 (59)	307 (86)	3.6
[3] 116 591 834 (49)	255 (80)	3.2
[4] 116 591 773 (48)	316 (79)	4.0
[5] 116 591 929 (52)	160 (82)	2.0

[1] HMNT06, PLB649 (2007) 173.

[2] F. Jegerlehner and A. Nyffeler, arXiv:0902.3360.

[3] Davier et al, arXiv:0908.4300 August 2009 (includes BaBar)

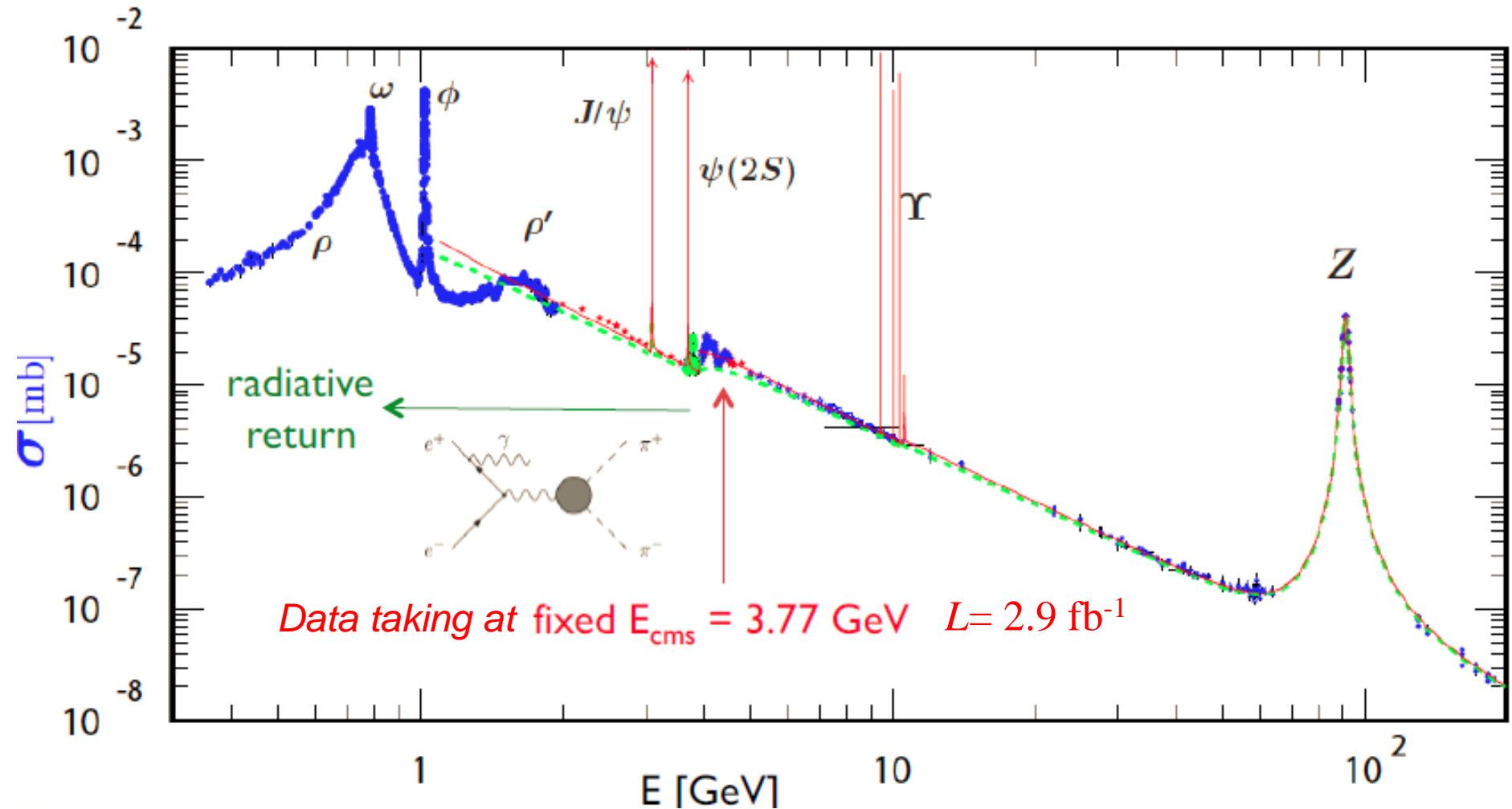
[4] Hagiwara, Liao, Martin, Nomura, Teubner, Oct '09 (preliminary)

[5] Davier et al, arXiv:0906.5443v2 August 2009 (τ data).

with $a_\mu^{\text{HMO}}(|b|) = 105 (26) \times 10^{-11}$

Initial state radiation (ISR return)

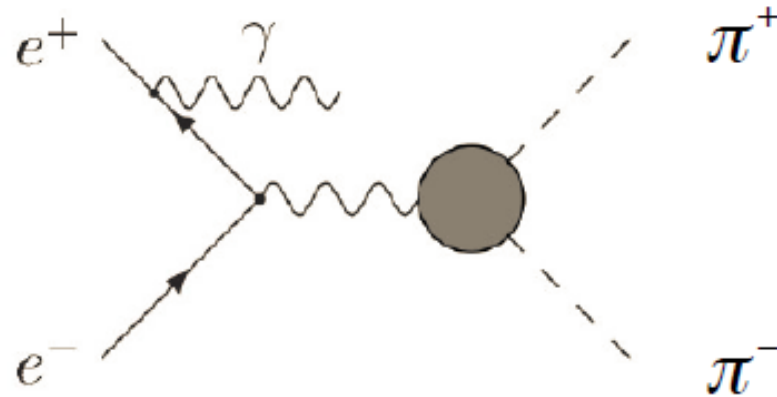
For e^+e^- collision, photons emitting from initial e^\pm decrease the effective energy $s' = s(1 - E_\gamma/E)$ continuously, this makes measurement at lower energies possible (ISR return).



Initial state radiation (ISR return)

Study the channel

$$e^+e^- \rightarrow \pi^+\pi^-\gamma_{ISR}$$



to measure the cross section of $e^+e^- \rightarrow \pi^+\pi^-$

via

$$\frac{d\sigma_{ISR}(M_{2\pi})}{dM_{2\pi}} = \frac{2M_{2\pi}}{s} W(s, x, \theta_\gamma) \cdot \sigma(M_{2\pi})$$

(neglecting FSR)

invariant mass of 2π

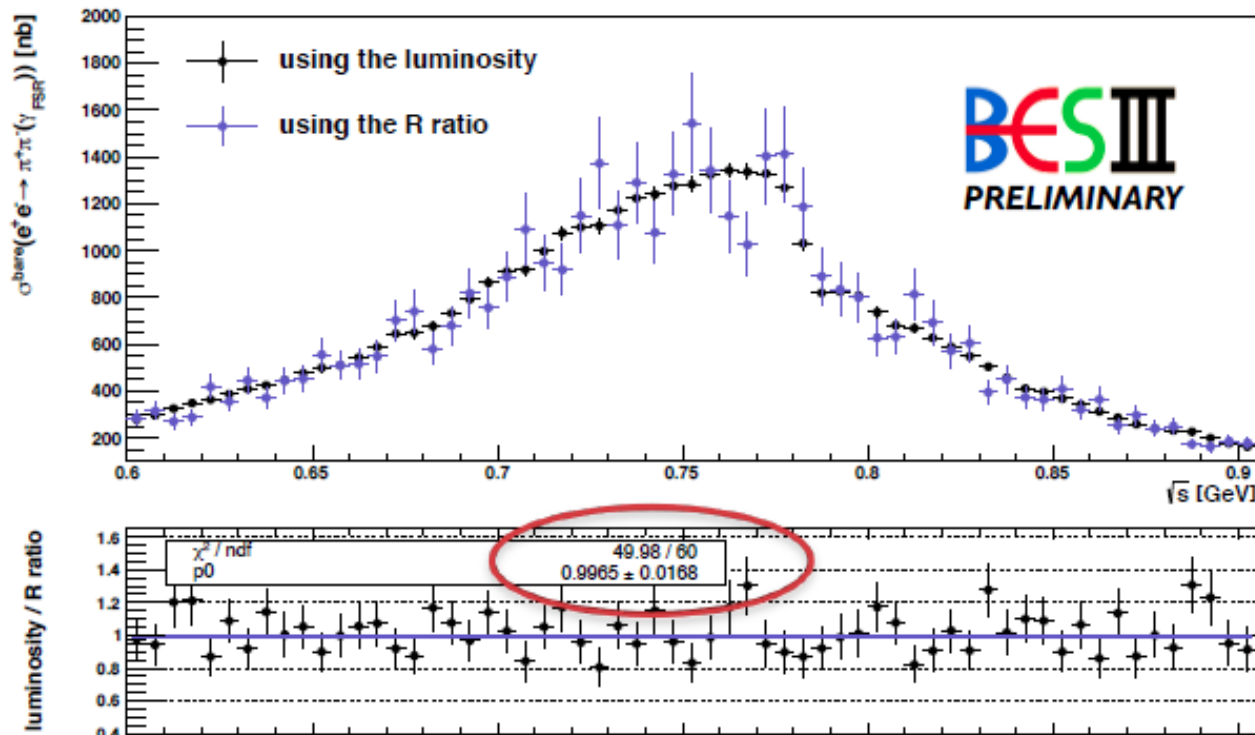
Radiator function

Two normalization methods

- Normalization to integrated luminosity

$$\sigma^{bare}(e^+e^- \rightarrow \pi^+\pi^-(\gamma_{FSR})) = \frac{N_{\pi\pi\gamma} / \varepsilon}{L_{int} \cdot H_{rad} \cdot \delta_{vac} \cdot (1 + \delta_{FSR})}$$

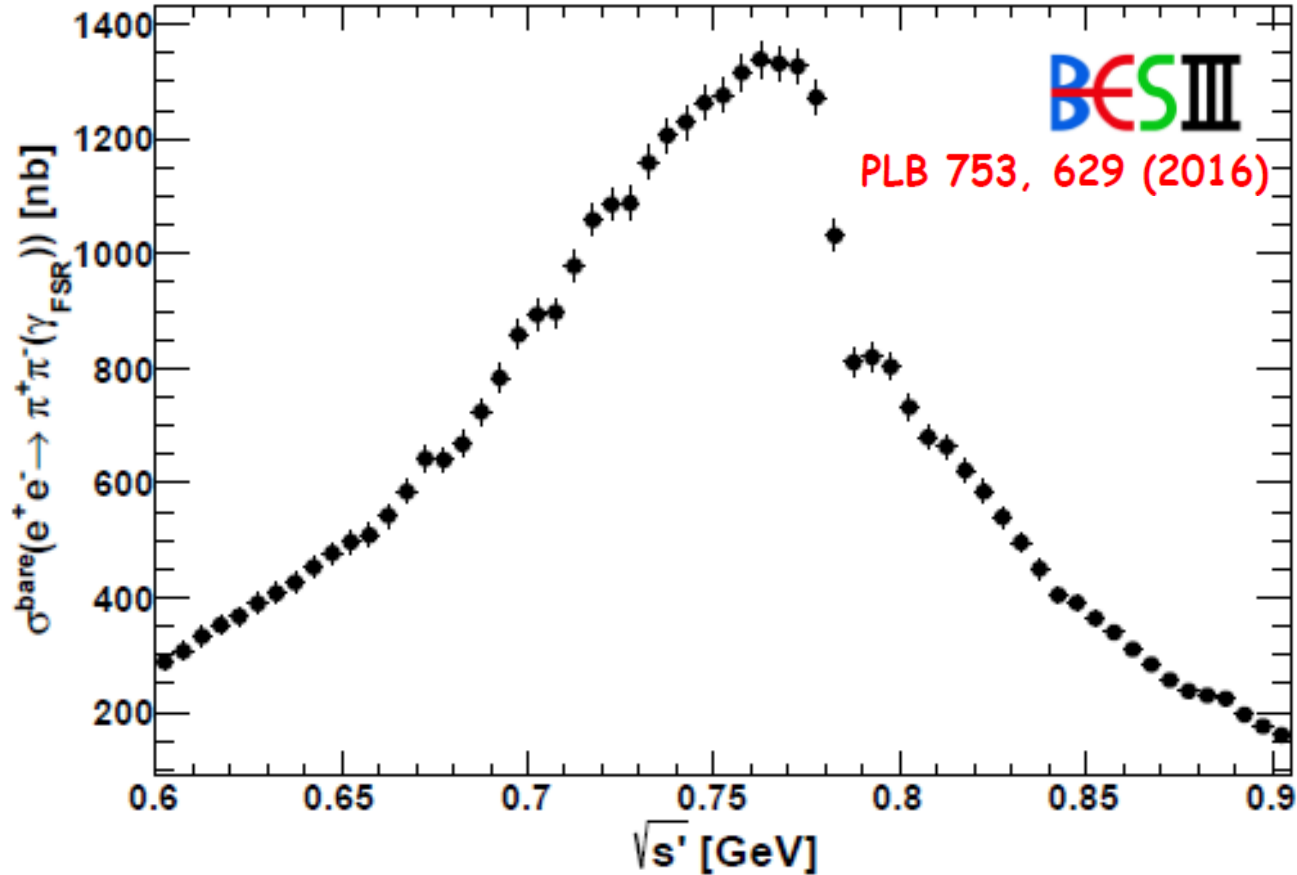
- Normalization to $\mu^+\mu^-\gamma$ events, i.e. R ratio $\pi^+\pi^-\gamma/\mu^+\mu^-\gamma$
 → $L_{int}, H_{rad}, \delta_{vac}$ canceled, uncertainty decreased.



**Luminosity / R ratio – 1
 = (0.35 ± 1.68) %**

limited by $\mu^+\mu^-\gamma$ statistics


Cross section of $\pi^+\pi^-$

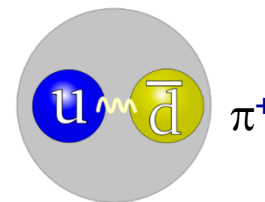


$$\sigma^{\text{bare}}(\sqrt{s'}) = \frac{1}{\frac{2\sqrt{s'}}{s} W(s, x) \epsilon(\sqrt{s'}) \mathcal{L} \delta_{\text{vac}} \delta_{\text{FSR}}} \frac{dN}{d\sqrt{s'}}$$

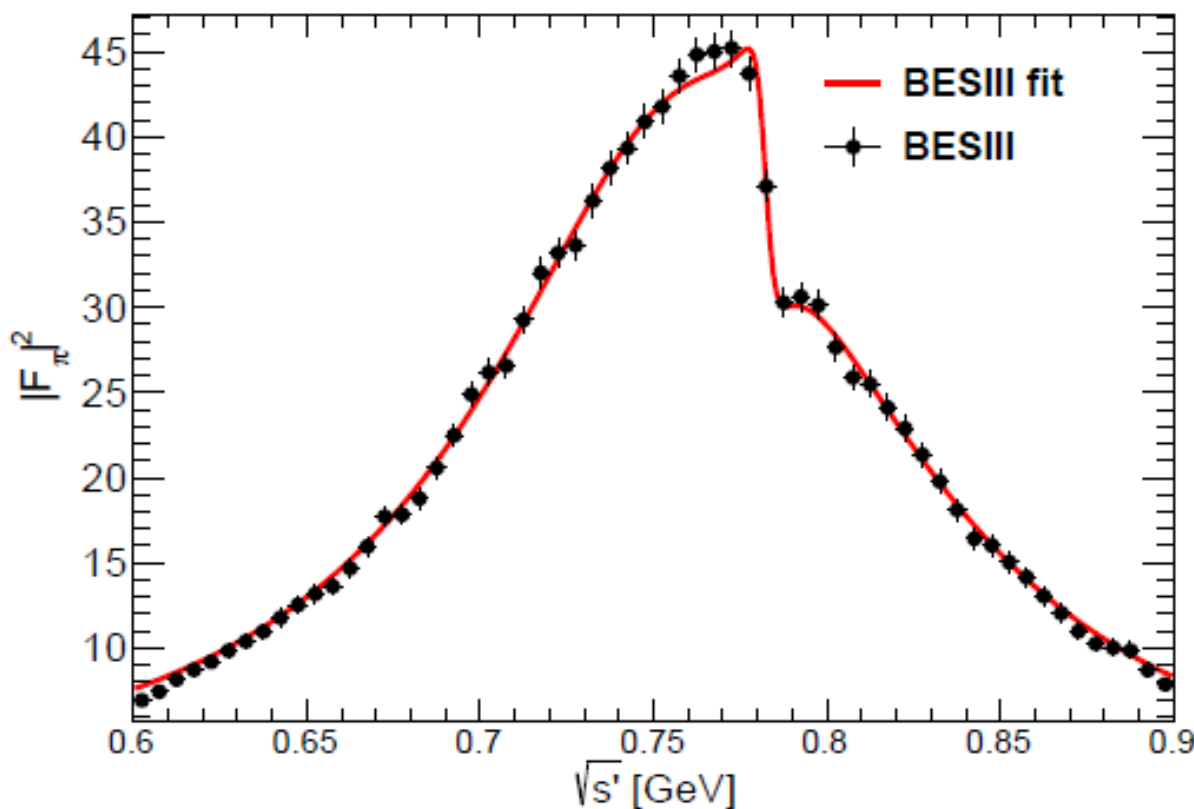
- ρ - ω interference clearly visible

Extraction of form factor

- The picture of pion structure in quark model: 
- Non point-like particle \Rightarrow pion form factor:



$$|F_\pi|^2(s') = \frac{3s'}{\pi\alpha\beta_\pi^3(s')} \sigma(e^+e^- \rightarrow \pi^+\pi^-)(s') \quad , \quad \beta_\pi(s') = \sqrt{1 - \frac{4m_\pi^2}{s'}}$$

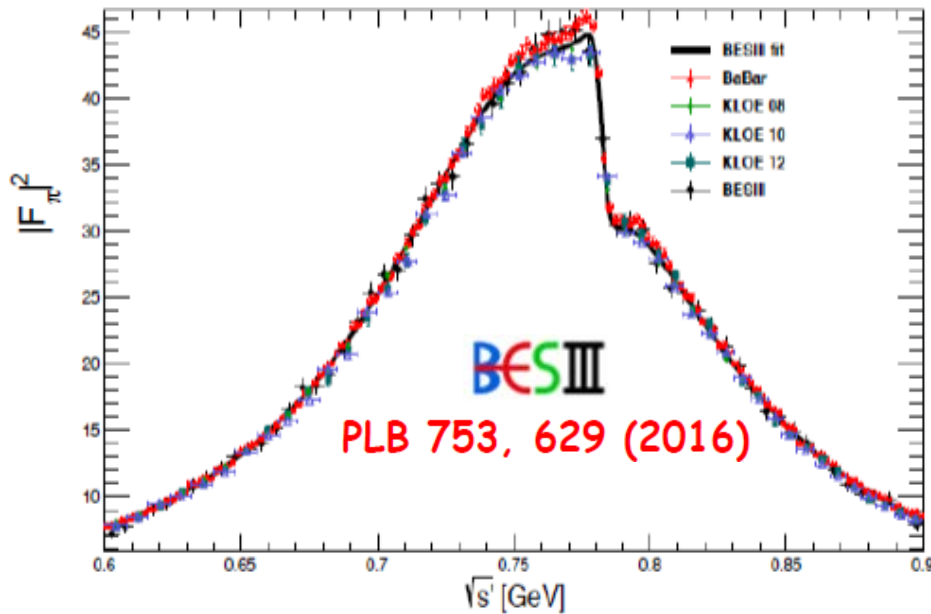


Fit function: Gounaris-Sakurai Parameterization

$$\chi^2 / \text{ndf} = 33.2 / 51$$

Comparisons between BESIII and BaBar/ KLOE

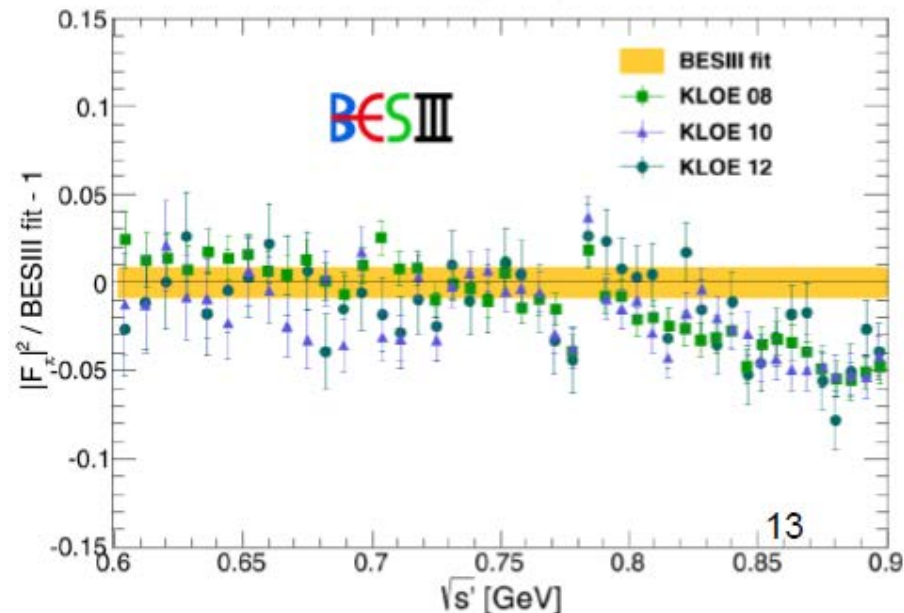
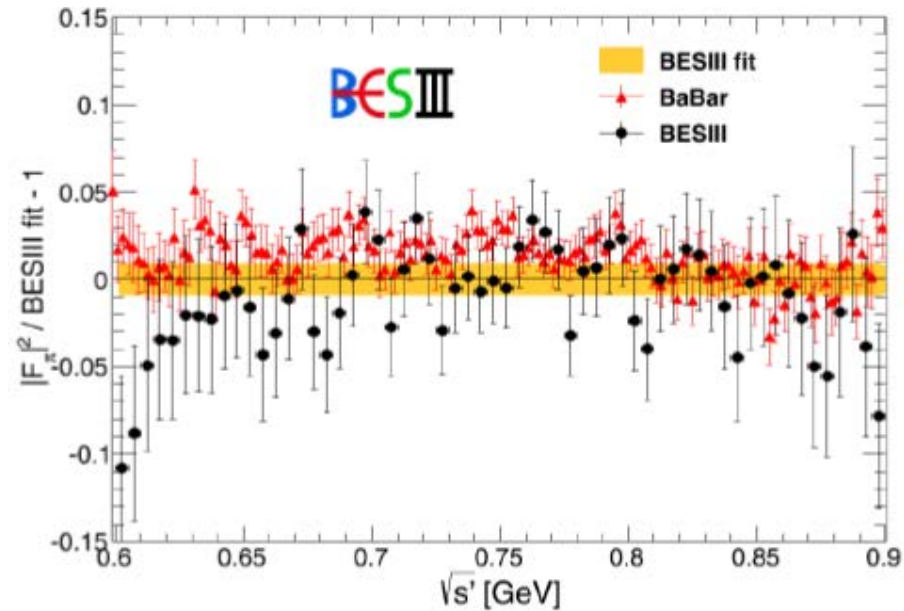
- Pion form factor F_π



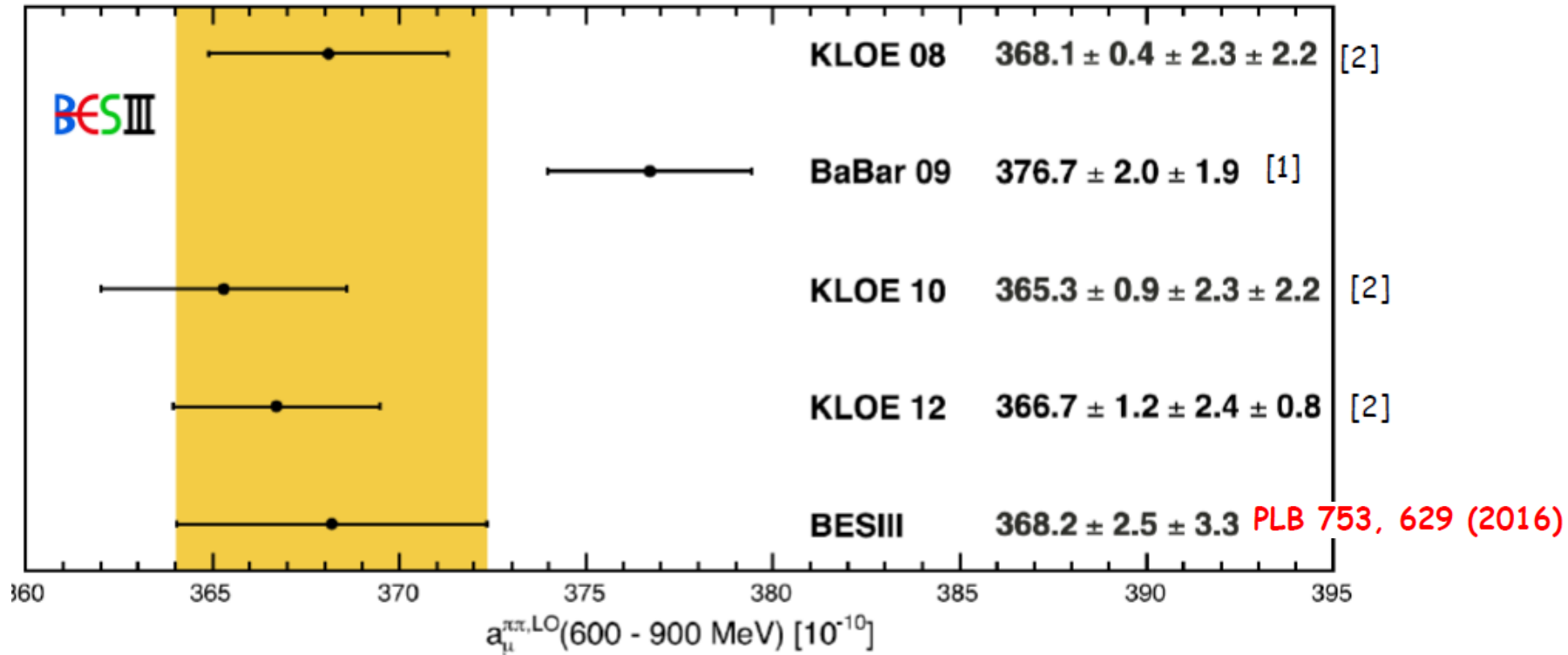
- New BESIII measurement agree with KLOE^[1] and BaBar^[2]
- Small shift wrt BaBar's results above ρ - ω interference

[1] B. Aubert et al., Phys. Rev. Lett. 103, 231801 (2009).
J.P. Lees et al., Phys. Rev. D86, 032013 (2012)

[2] F. Ambrosino et al. Phys. Lett. B 670, 285 (2009).
F. Ambrosino et al. Phys. Lett. B 700, 102-110 (2011).
D. Babusci et al. Phys. Lett. B 720, 336-343 (2013).



Contribution of $\pi^+\pi^-$ to a_μ



- Precision compatible with previous measurements
- $a_\mu^{(\pi\pi, LO)} = (370.0 \pm 2.5_{\text{stat}} \pm 3.3_{\text{sys}}) \times 10^{-10}$
- Confirm deviation of $(g-2)$ between experiment and theory larger than 3σ

[1] B. Aubert et al., Phys. Rev. Lett. 103, 231801 (2009). J.P. Lees et al., Phys. Rev. D86, 032013 (2012)

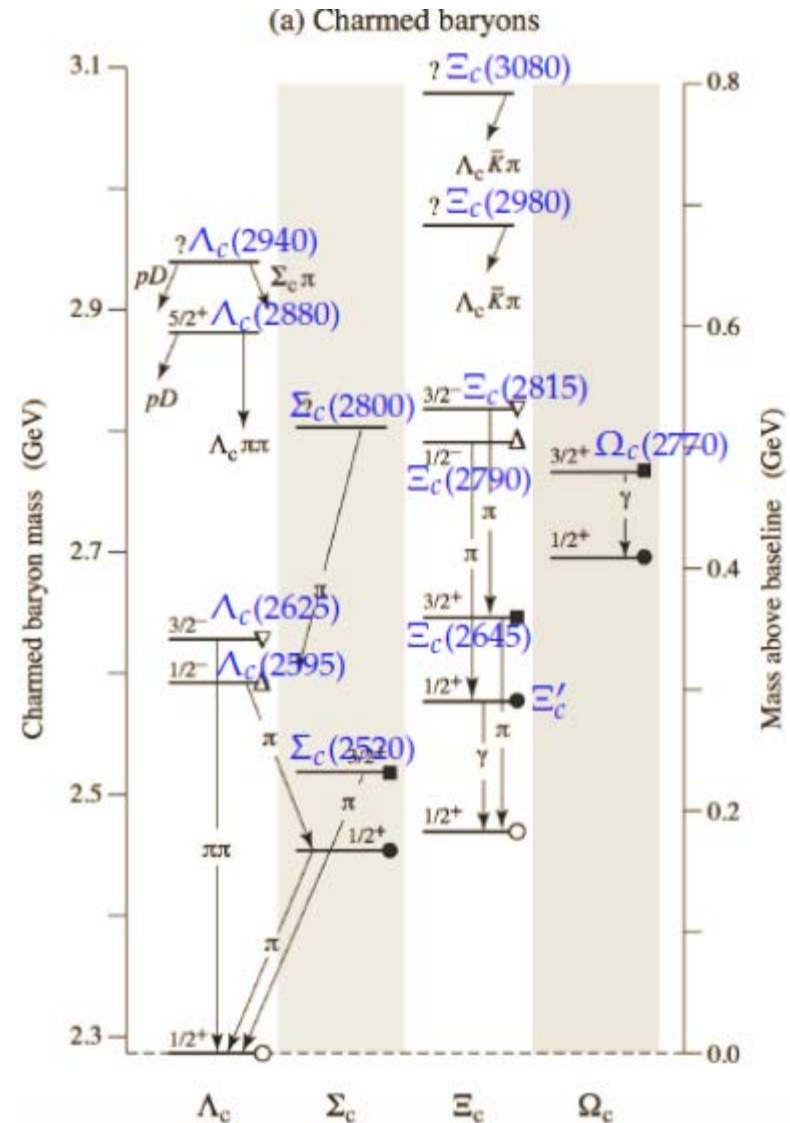
[2] F. Ambrosino et al. Phys. Lett. B 670, 285 (2009). F. Ambrosino et al. Phys. Lett. B 700, 102-110 (2011).
D. Babusci et al. Phys. Lett. B 720, 336-343 (2013).

Part 3

$$e^+e^- \rightarrow \Lambda_c^+ \bar{\Lambda}_c^-$$

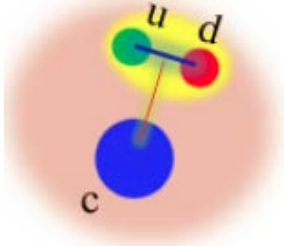
Charmed baryon family

- Singly charmed baryons
 - ground states: Λ_c^+ , Σ_c , $\Xi_c^{(\prime)}$, Ω_c
 - excited states
 - LHCb Collaboration observed doubly charmed baryon Ξ_{cc}^{++} via decay $\Xi_{cc}^{++} \rightarrow \Lambda_c^+ K^- \pi^+ \pi^+$, $\Lambda_c^+ \rightarrow p K^- \pi^+$ arXiv:1707.01621
 - No triply charmed baryon observed
- Λ_c^+ : decays only weakly
 - Σ_c : $B(\Sigma_c \rightarrow \Lambda_c^+ \pi) \sim 100\%$
 - Ξ_c : decays only weakly; no absolute BF measured, most are ratios relative to $\Xi^- \pi^+ (\pi^+)$
 - Ω_c : decays only weakly; no absolute BF measured



Λ_c^+ : Charmed baryon family

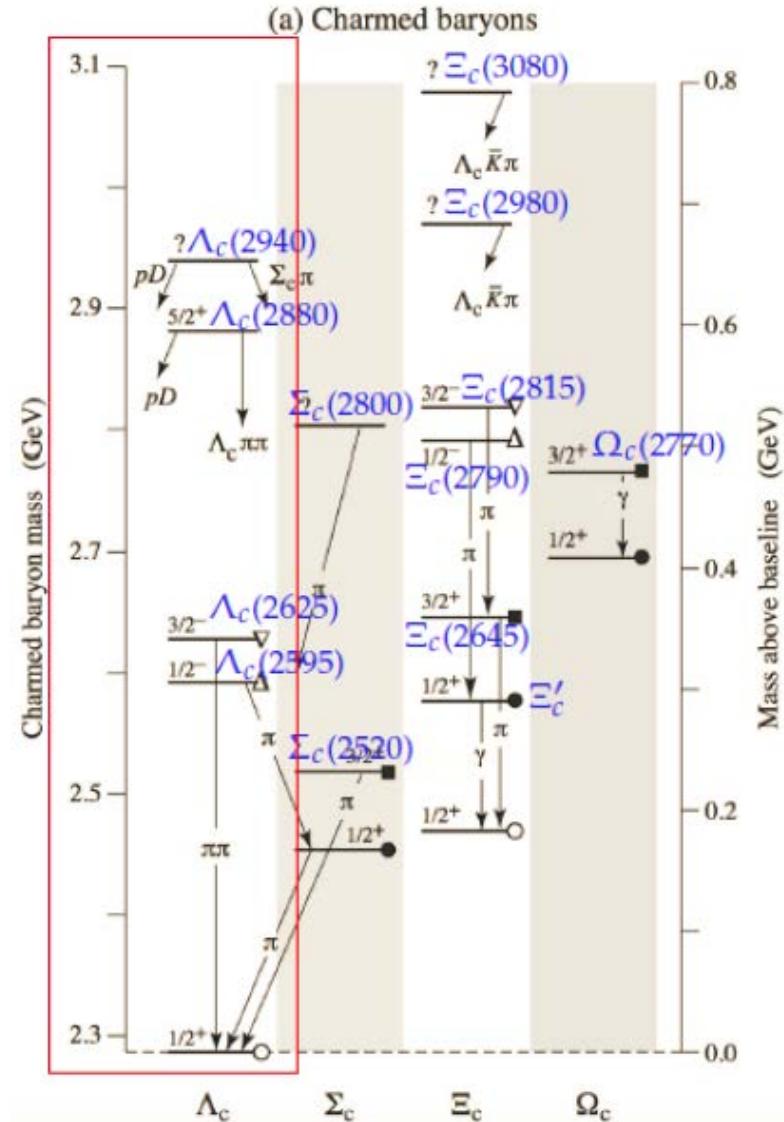
- Quark component: $ud-c$



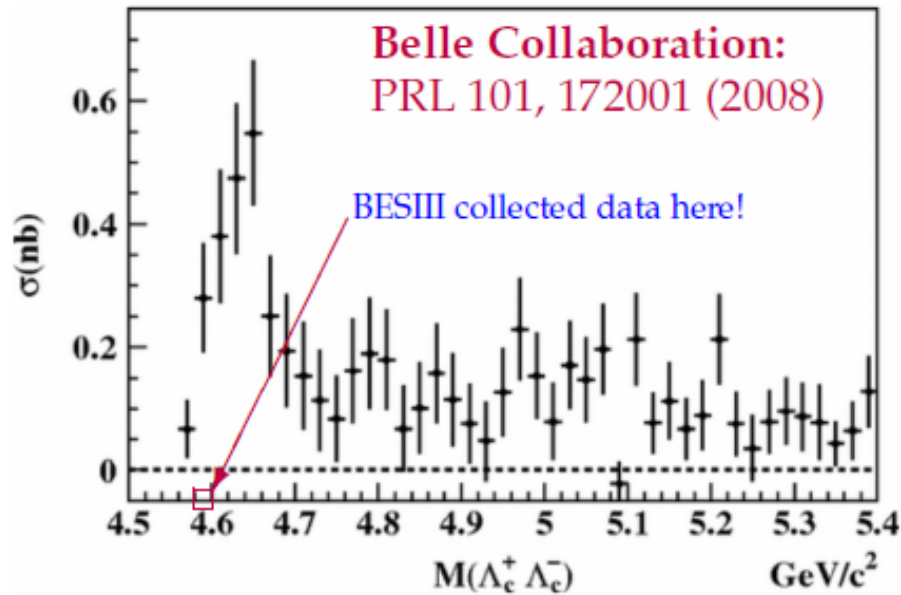
- The lightest charmed baryon:

$$m_{\Lambda_c} = 2286.48 \text{ MeV}$$

- Most of charmed baryons decay to Λ_c
- Λ_c is important tagging charmed baryon in high energy production.
- $\text{Br}(\Lambda_c \rightarrow pK^-\pi^+)$ contributes dominant error for V_{ub} via Λ_b decay



Data samples used for $\Lambda_c^+ \bar{\Lambda}_c^-$ measurements



BESIII data samples

\sqrt{s} (GeV)	\mathcal{L}_{int} (pb $^{-1}$)
4.5745	47.67
4.580	8.545
4.590	8.162
4.5995	566.9

- ▶ At $\sqrt{s} = 4.5995$ GeV, the **hadronic, semi-leptonic** and **inclusive decays** of Λ_c^+ can be measured directly
- ▶ The samples make precise measurement of the **Born cross section line-shape** of $e^+e^- \rightarrow \Lambda_c^+ \bar{\Lambda}_c^-$ near threshold possible
- ▶ At $\sqrt{s} = 4.5745$ and 4.5995 GeV, the **polar angular distribution** of Λ_c can be studied and the $|G_E|/|G_M|$ ratios can be extracted

Production cross sections of baryon pairs

- Born cross section for the process $e^+e^- \rightarrow \gamma^* \rightarrow B\bar{B}$

$$\sigma_{B\bar{B}}(q) = \frac{4\pi\alpha^2 C\beta}{3q^2} [|G_M(q)|^2 + \frac{1}{2\tau} |G_E(q)|^2]$$

- Baryon speed $\beta = \sqrt{1 - 4m_B^2c^4/q^2}$, $\tau = q^2/(4m_B^2c^4)$

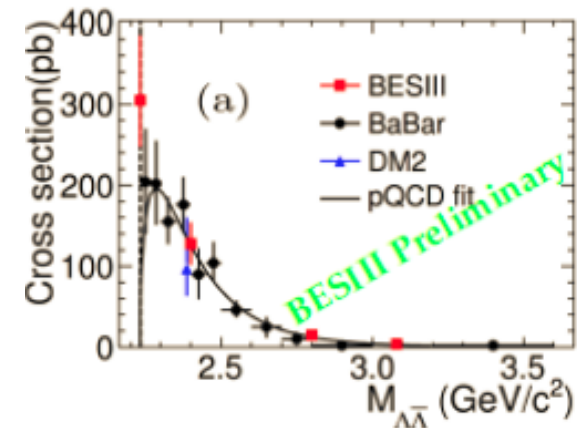
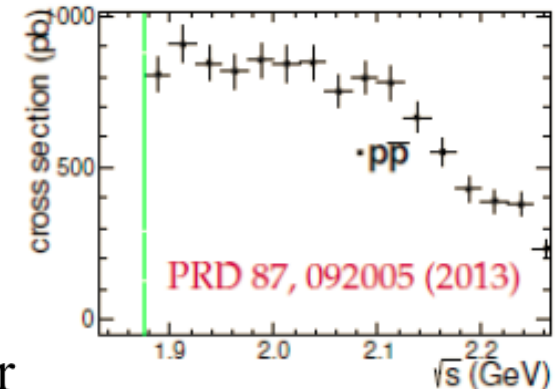
- Coulomb factor C results in a **non-zero** cross section at threshold

- $e^+e^- \rightarrow p\bar{p}$: an enhancement and wide plateau

- $e^+e^- \rightarrow \Lambda\bar{\Lambda}$: non-zero cross section near threshold

- It could be anticipated that behaviour of Λ_c is similar to that of proton

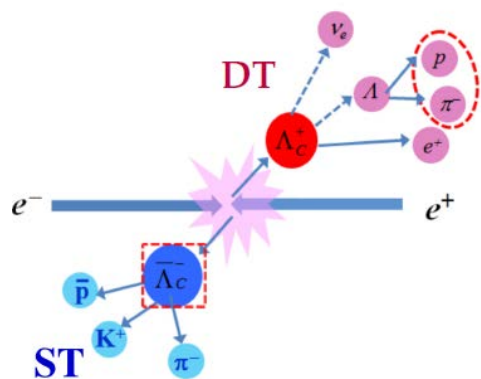
- Belle Collaboration has measured the cross section of $e^+e^- \rightarrow \Lambda_c^+\bar{\Lambda}_c^-$ using ISR return method
PRL101, 172001(2008)



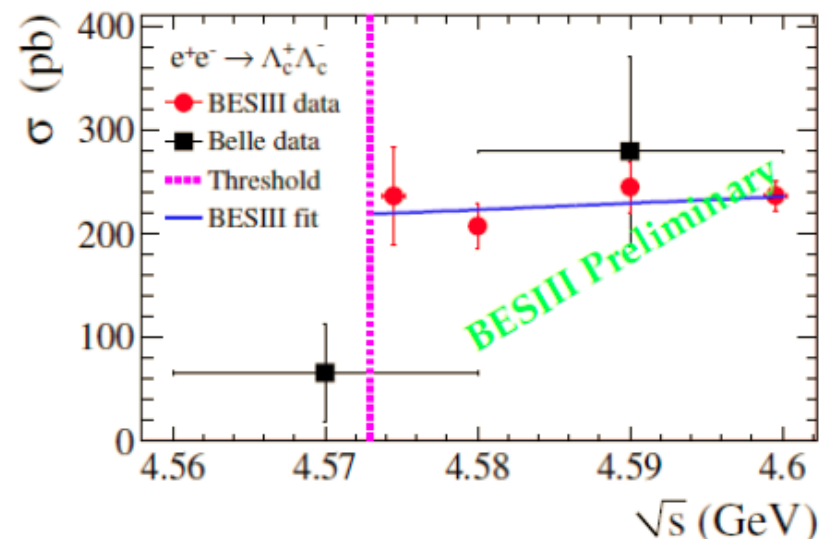
Cross section of $\Lambda_c^+ \bar{\Lambda}_c^-$

BESIII preliminary results:

\sqrt{s} (GeV)	σ (pb)
4.5745	$236 \pm 11 \pm 46$
4.580	$207 \pm 17 \pm 13$
4.590	$245 \pm 19 \pm 16$
4.5995	$237 \pm 3 \pm 15$

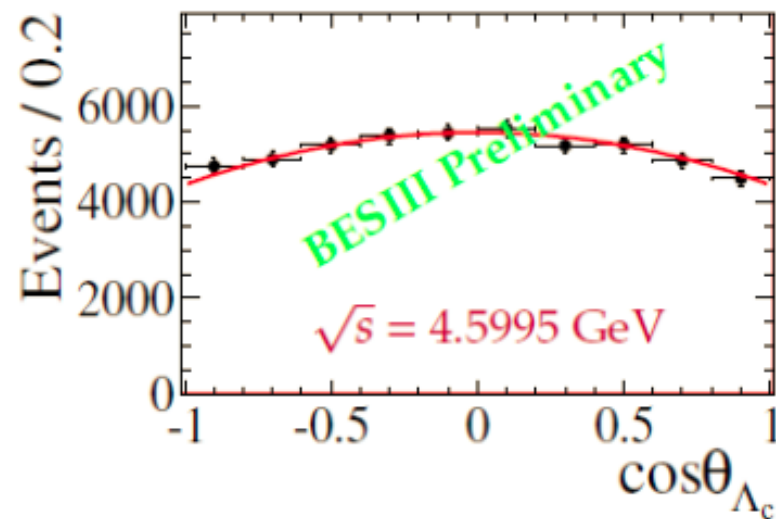
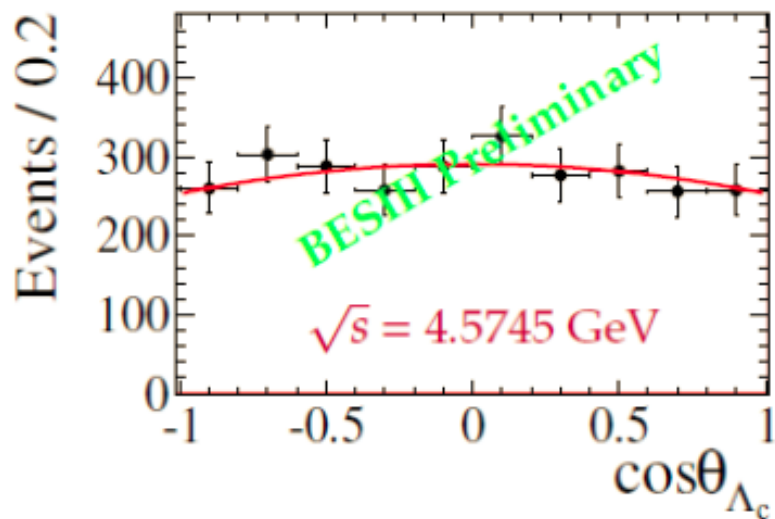


- ▶ 10 hadronic decays of Λ_c are employed
- ▶ Single Tag method (ΔE & M_{BC}) is used
- ▶ Λ_c^+ and $\bar{\Lambda}_c^-$ are **reconstructed independently**
- ▶ Total cross sections are obtained from **weighted average**



- The cross sections are measured with unprecedented precision
- Enhanced cross section of process $e^+e^- \rightarrow \Lambda_c^+ \bar{\Lambda}_c^-$ close to threshold is discerned for the first time
- The enhancement: the Coulomb effect or dynamics?

Fit of angular distribution of $\Lambda_c^+ \bar{\Lambda}_c^-$



- ▶ Studied at 4.5745 and 4.5995 GeV only
- ▶ The bin-by-bin efficiency correction is applied on the total yields
- ▶ Combined the corrected yields from Λ_c^+ and $\bar{\Lambda}_c^-$ bins
- ▶ The χ^2 fit on the angular distribution with shape $1 + \alpha_{\Lambda_c} \cos^2 \theta$

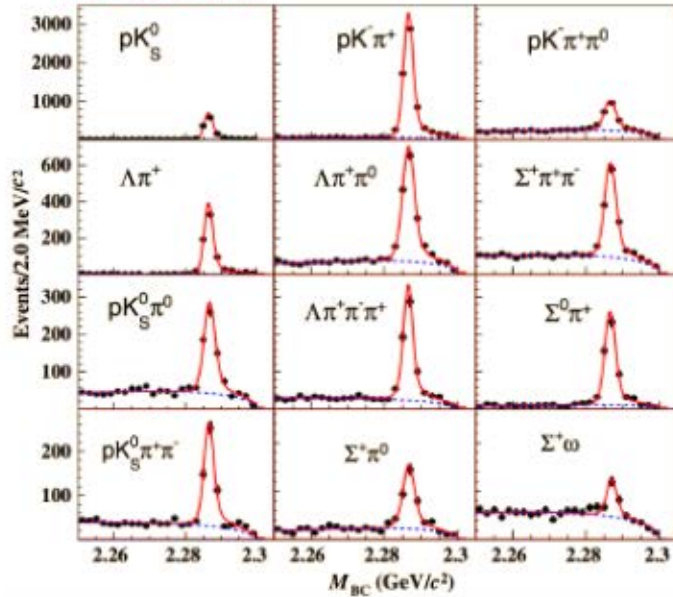
- BESIII preliminary fit

\sqrt{s} (MeV)	α_{Λ_c}	$ G_E/G_M $
4.5745	$-0.13 \pm 0.12 \pm 0.08$	$1.14 \pm 0.14 \pm 0.07$
4.5995	$-0.20 \pm 0.04 \pm 0.02$	$1.23 \pm 0.05 \pm 0.03$

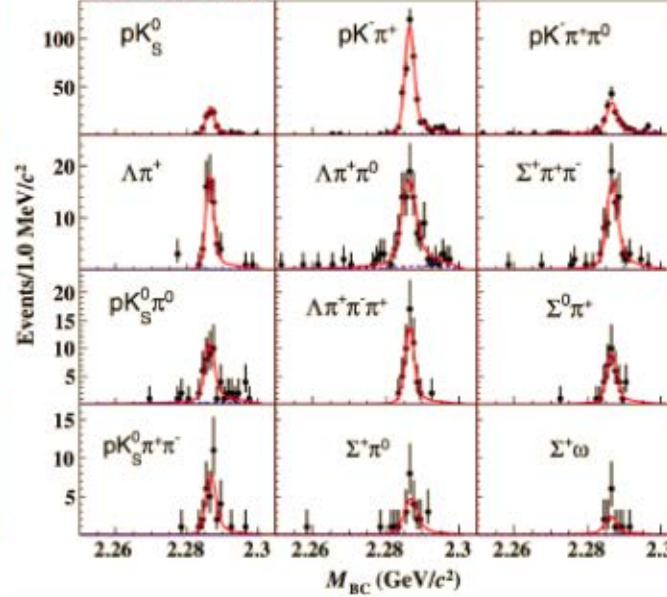
- First time that ratios $|G_E/G_M|$ of Λ_c are measured near threshold

Cabibbo Favored hadronic decays of Λ_c^+

ST events:



DT events:



$$\blacktriangleright N_j^{ST} = N_{Tot.} \mathcal{B}_j \varepsilon_j$$

$$\blacktriangleright N_{ij}^{DT} = N_{Tot.} \mathcal{B}_i \mathcal{B}_j \varepsilon_{ij}$$

$$\blacktriangleright \mathcal{B}_i = \frac{N_{ij}^{DT}}{N_j^{ST}} \frac{\varepsilon_j}{\varepsilon_{ij}}$$

PRL 116, 052001 (2016)

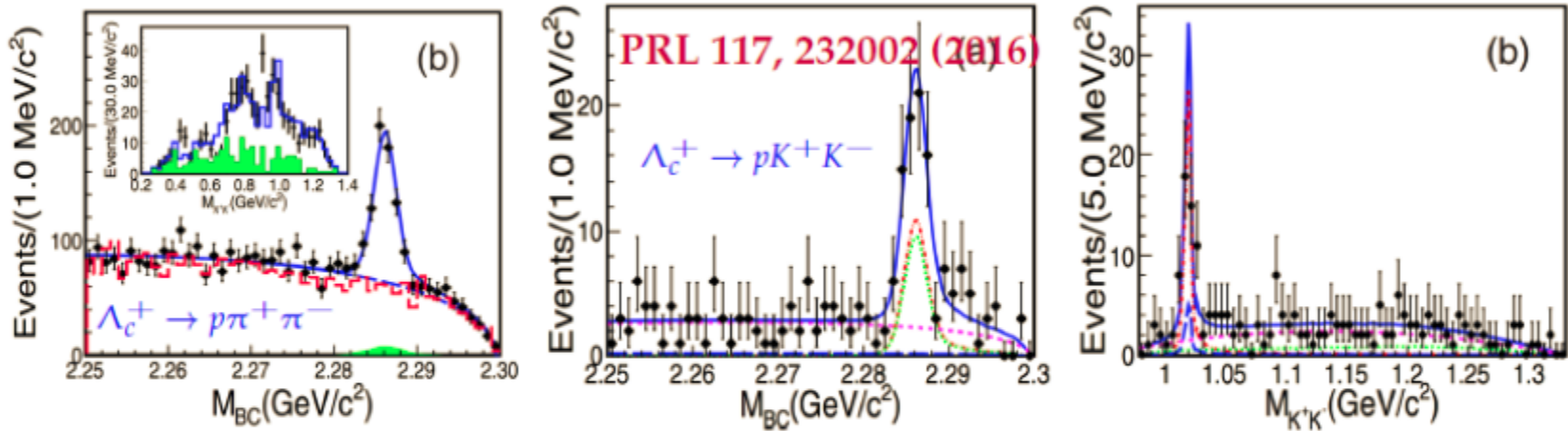
Branch ratios \mathcal{B}_i of Λ_c^+ hadronic decay

Mode	This work (%)	PDG (%)
pK_S^0	$1.52 \pm 0.08 \pm 0.03$	1.15 ± 0.30
$pK^- \pi^+$	$5.84 \pm 0.27 \pm 0.23$	5.0 ± 1.3
$pK_S^0 \pi^0$	$1.87 \pm 0.13 \pm 0.05$	1.65 ± 0.50
$pK_S^0 \pi^+ \pi^-$	$1.53 \pm 0.11 \pm 0.09$	1.30 ± 0.35
$pK^- \pi^+ \pi^0$	$4.53 \pm 0.23 \pm 0.30$	3.4 ± 1.0
$\Lambda \pi^+$	$1.24 \pm 0.07 \pm 0.03$	1.07 ± 0.28
$\Lambda \pi^+ \pi^0$	$7.01 \pm 0.37 \pm 0.19$	3.6 ± 1.3
$\Lambda \pi^+ \pi^- \pi^+$	$3.81 \pm 0.24 \pm 0.18$	2.6 ± 0.7
$\Sigma^0 \pi^+$	$1.27 \pm 0.08 \pm 0.03$	1.05 ± 0.28
$\Sigma^+ \pi^0$	$1.18 \pm 0.10 \pm 0.03$	1.00 ± 0.34
$\Sigma^+ \pi^+ \pi^-$	$4.25 \pm 0.24 \pm 0.20$	3.6 ± 1.0
$\Sigma^+ \omega$	$1.56 \pm 0.20 \pm 0.07$	2.7 ± 1.0

- The first direct measurement of the Λ_c near the production threshold
- Branch ratio of $pK^- \pi^+$ is consistent with Belle's results
- Measurements of the 11 modes of semi-leptonic decay improved

Decay $\Lambda_c^+ \rightarrow p\pi^+\pi^-$ and pK^+K^-

- Sensitive to nonfactorizable contributions from W-exchange diagrams
- $\Lambda_c^+ \rightarrow p\phi$ is particular interest due to only internal W-emission diagrams



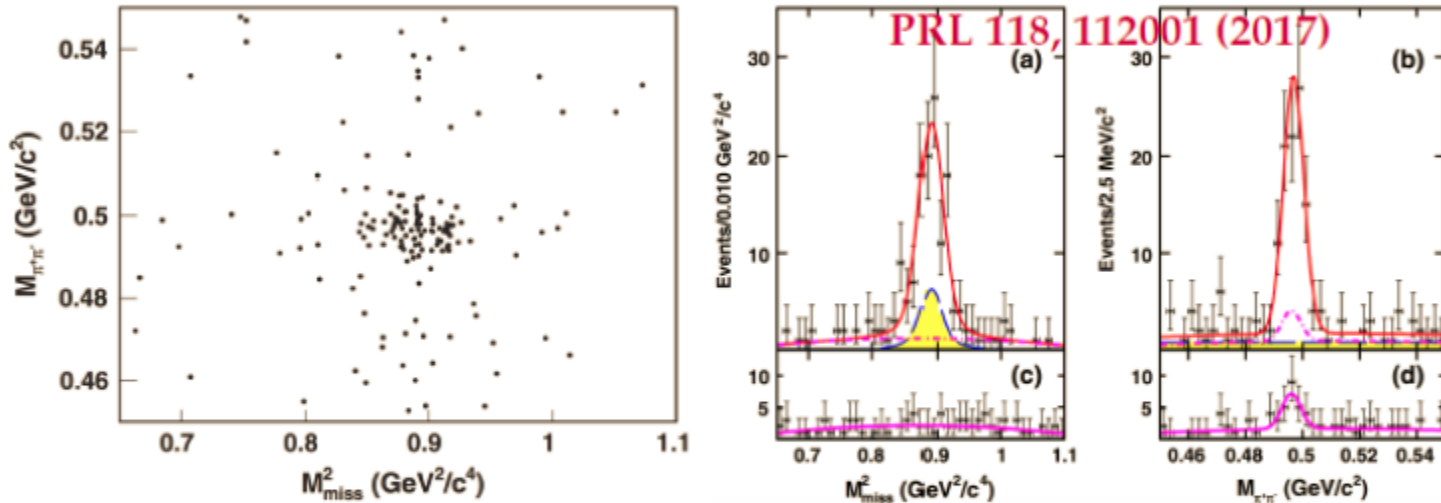
Decay modes	$\mathcal{B}_{\text{mode}}/\mathcal{B}_{\text{ref}}$ (This work)	$\mathcal{B}_{\text{mode}}/\mathcal{B}_{\text{ref}}$ (PDG average)
$\Lambda_c^+ \rightarrow p\pi^+\pi^-$	$(6.70 \pm 0.48 \pm 0.25) \times 10^{-2}$	$(6.9 \pm 3.6) \times 10^{-2}$
$\Lambda_c^+ \rightarrow p\phi$	$(1.81 \pm 0.33 \pm 0.13) \times 10^{-2}$	$(1.64 \pm 0.32) \times 10^{-2}$
$\Lambda_c^+ \rightarrow pK^+K^-$ (non- ϕ)	$(9.36 \pm 2.22 \pm 0.71) \times 10^{-3}$	$(7 \pm 2 \pm 2) \times 10^{-3}$
-	$\mathcal{B}_{\text{mode}}$ (This work)	$\mathcal{B}_{\text{mode}}$ (PDG average)
$\Lambda_c^+ \rightarrow p\pi^+\pi^-$	$(3.91 \pm 0.28 \pm 0.15 \pm 0.24) \times 10^{-3}$	$(3.5 \pm 2.0) \times 10^{-3}$
$\Lambda_c^+ \rightarrow p\phi$	$(1.06 \pm 0.19 \pm 0.08 \pm 0.06) \times 10^{-3}$	$(8.2 \pm 2.7) \times 10^{-4}$
$\Lambda_c^+ \rightarrow pK^+K^-$ (non- ϕ)	$(5.47 \pm 1.30 \pm 0.41 \pm 0.33) \times 10^{-4}$	$(3.5 \pm 1.7) \times 10^{-4}$

- ▶ Single tag method is used
- ▶ Using the decay $pK^-\pi^+$ as the reference mode

- First observation of the singly Cabibbo suppressed decay $\Lambda_c^+ \rightarrow p\pi^+\pi^-$
- precision of decays $\Lambda_c \rightarrow pK^+K^-$ (non- ϕ) and $\Lambda_c \rightarrow p\phi$ improved

Decay $\Lambda_c^+ \rightarrow nK_S\pi^+$

- A precision test for the **isospin symmetry** and final states interaction
- DT method: $M_{miss}^2 \equiv E_{miss}^2/c^4 - |\vec{p}_{miss}|^2/c^2$

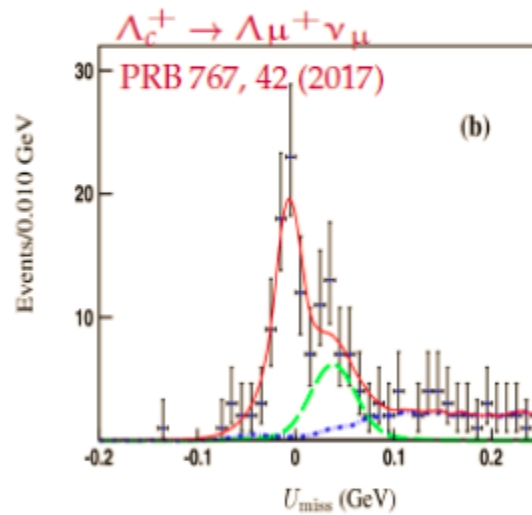
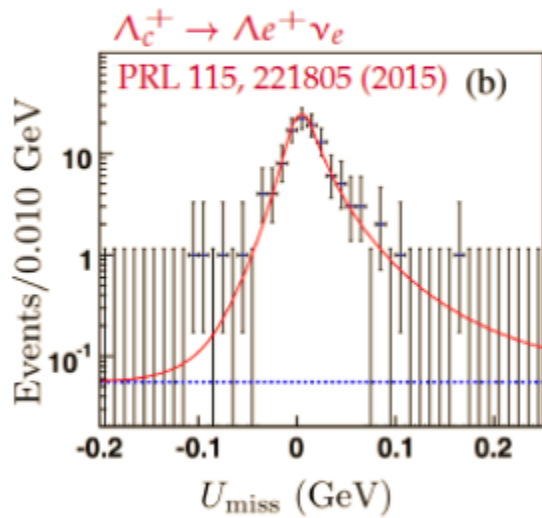


- $\mathcal{B}(\Lambda_c^+ \rightarrow nK_S^0\pi^+) = (1.82 \pm 0.23 \pm 0.11)\%$
- $\mathcal{B}(\Lambda_c^+ \rightarrow n\bar{K}^0\pi^+)/\mathcal{B}(\Lambda_c^+ \rightarrow pK^-\pi^+) = 0.62 \pm 0.09$
- $\mathcal{B}(\Lambda_c^+ \rightarrow n\bar{K}^0\pi^+)/\mathcal{B}(\Lambda_c^+ \rightarrow p\bar{K}^0\pi^0) = 0.97 \pm 0.16$

The first direct measurement of Λ_c^+ decay involving neutron in final state

Decay $\Lambda_c^+ \rightarrow \Lambda l^+ \nu_l$

- A stringent test for **nonperturbative aspects** of strong interaction theory
- The key ingredient in **calibrating Lattice QCD** calculations
- There is no absolute measurement of Λ_c^+ semi-leptonic decay yet
- Mutually confirm and test the leptonic universality



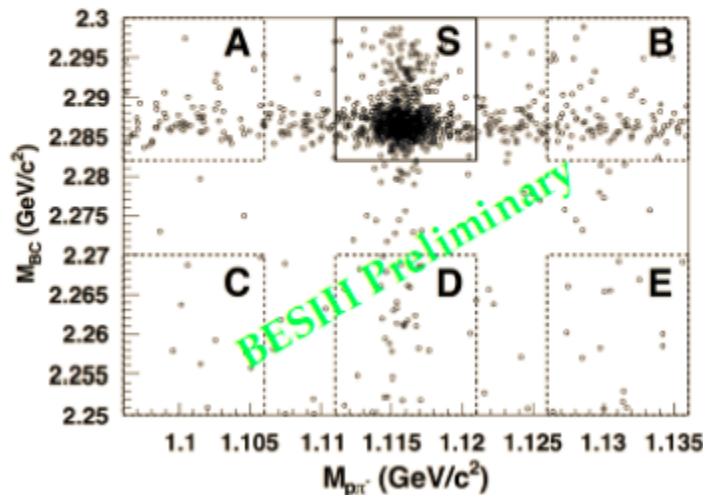
- ▶ DT method is used, 11 modes are tagged
- ▶ missing mass technique at threshold
- ▶ $U_{\text{miss}} = E_{\text{miss}} - c|\vec{p}_{\text{miss}}|$

- ▶ $\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e) = (3.63 \pm 0.38 \pm 0.20)\%$
- ▶ $\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda \mu^+ \nu_\mu) = (3.49 \pm 0.46 \pm 0.27)\%$
- ▶ $\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e) / \mathcal{B}(\Lambda_c^+ \rightarrow \Lambda \mu^+ \nu_\mu) = 0.96 \pm 0.16 \pm 0.04$

The first direct measurement of Λ_c^+ semi-leptonic decay

Decay $\Lambda_c^+ \rightarrow \Lambda X$

- This decay is mediated by $c \rightarrow s$ and dominates the lifetime of Λ_c^+
- Help to understand the quark structure and decay dynamics of Λ_c^+
- Provide an essential input for decays of b-flavored hadrons



▶ DT method is used, modes $\bar{p}K^+\pi^-$ and $\bar{p}K_S^0$ are singly tagged.

▶
$$\mathcal{A}_{cp} \equiv \frac{\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda + X) - \mathcal{B}(\bar{\Lambda}_c^- \rightarrow \bar{\Lambda} + X)}{\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda + X) + \mathcal{B}(\bar{\Lambda}_c^- \rightarrow \bar{\Lambda} + X)}$$

Preliminary result:

$$\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda + X) = (38.2_{-2.2}^{+2.8} \pm 0.6)\% \text{ and } \mathcal{A}_{cp} = (2.1_{-6.6}^{+7.0} \pm 1.1)\%$$

- Sum of known exclusive decays $\Lambda_c^+ \rightarrow \Lambda X_i$ is $(24.5 \pm 2.1)\%$, which means other unknown decays
- No CPV is observed at current precision

Summary

◆ Proton pairs

- The effective form factors are measured with improved errors
- The ratio $|G_E/G_M|$ are extracted with uncertainty of 25% – 30%
- The ratio $|G_E/G_M|$ are close to unity between 2.2 – 3.08 GeV

◆ Pion pairs

- The cross section and form factor are measured with ISR return
- The difference of Δa_μ between experiments and theory is confirmed
- Systematic uncertainty ($\sim 0.9\%$) still dominant.

◆ $\Lambda_c^+ \Lambda_c^-$ pairs

- Cross section and form factor close to threshold are measured
- Absolute branch ratio of Λ_c decays are studied