

# Collectivity in small systems — Initial state vs. final state effects

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# Outline

- General perspective on initial state vs. final state effects as origin of azimuthal correlations high-multiplicity p+p/A
  - Hydrodynamic description of p+p/A
  - Initial state momentum correlations

State of the art of phenomenological calculations

Reviews: Dusling, Li, Schenke, Int.J.Mod.Phys. E25 (2016) no.01, 1630002  
Schlichting, Tribedy, Adv. High Energy Phys. Vol. 2016 (2016), 8460349

- New developments to quantify rel. importance of Initial state & final state effects

Based on Greif, Greiner, Schenke, SS, Xu arXiv:1708.02076

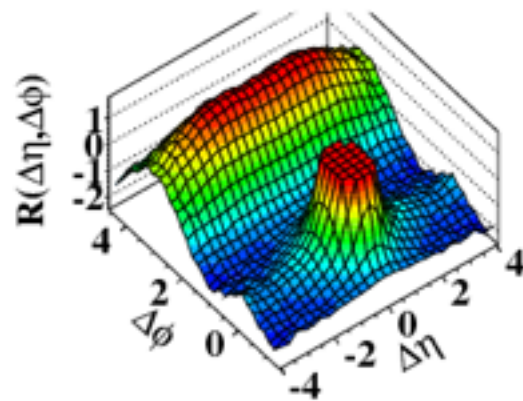
- Conclusions & Perspectives

# Long-range azimuthal correlations

↑  
— high multiplicity  
— low multiplicity  
↓

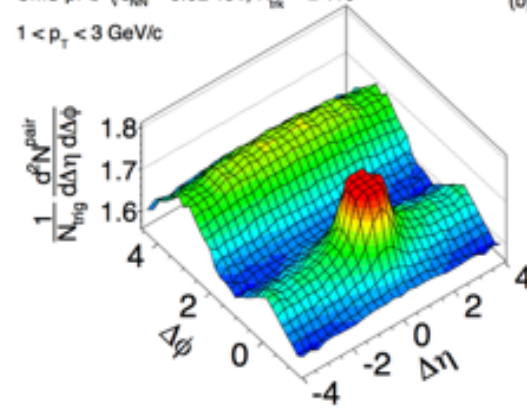
p+p  
7 TeV

(d) CMS  $N \geq 110$ ,  $1.0 \text{ GeV}/c < p_T < 3.0 \text{ GeV}/c$



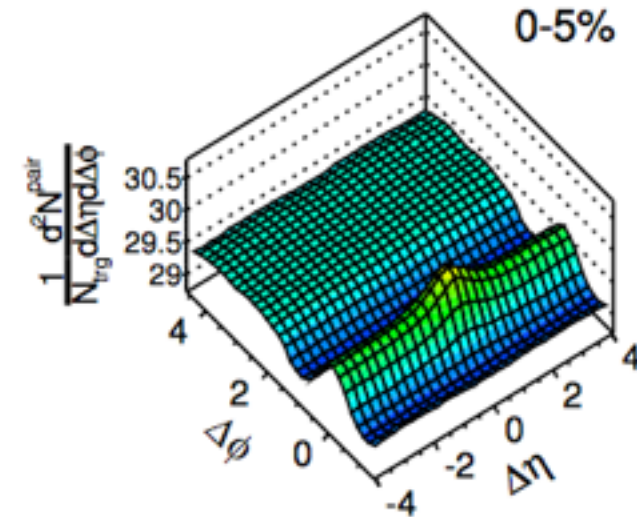
p+Pb  
5.02 TeV

CMS pPb  $\sqrt{s_{NN}} = 5.02 \text{ TeV}$ ,  $N_{ch}^{offline} \geq 110$   
 $1 < p_T < 3 \text{ GeV}/c$

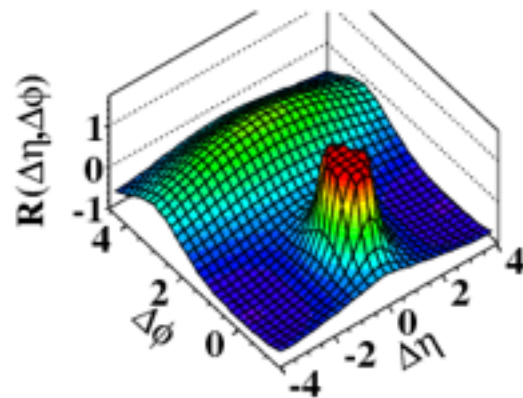


Pb+Pb  
2.76 TeV

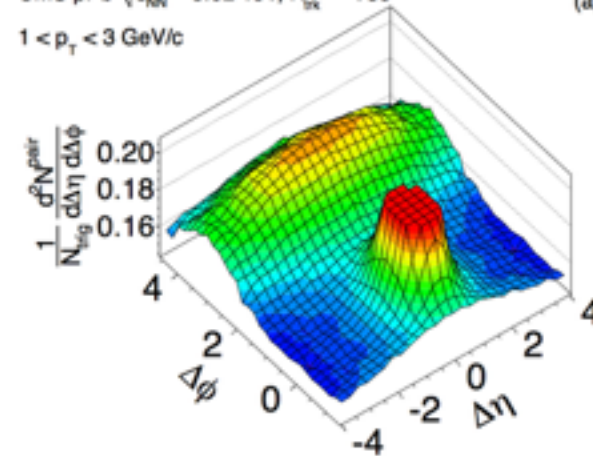
0-5%



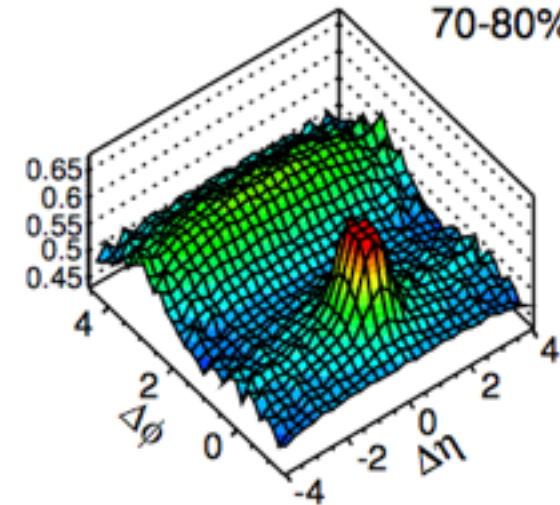
(b) CMS MinBias,  $1.0 \text{ GeV}/c < p_T < 3.0 \text{ GeV}/c$



CMS pPb  $\sqrt{s_{NN}} = 5.02 \text{ TeV}$ ,  $N_{ch}^{offline} < 35$   
 $1 < p_T < 3 \text{ GeV}/c$



70-80%



Surprising similarities as conventionally p+p/A provide background measurements for A+A

# Collectivity in small systems

Even though many features of near-side ridge in  $p+p/A$  are similar to observations in  $A+A$  collisions,

- > correlations between many ( $n > 2$ ) particles
- > dependence on hadron species (mass ordering)

there are also important differences

- > unambiguous observations in  $p+p/A$  only in high-multiplicity events
- > so far no observation of jet-quenching in  $p+p/A$

Different theoretical explanations developed in terms of

final state response to initial state geometry

and/or

initial state momentum correlations



# Nature of high-multiplicity p+p/A events

High-multiplicity events exhibit exceptionally large parton densities in the initial state



If parton densities in high-multiplicity events are sufficiently large, interaction between produced partons can be significant

-> Creation of small droplet of QGP?  
Space-time dynamics similar to A+A collision?

# Hydrodynamic description of p+p/A

Generating azimuthal correlations as a response to initial state geometry requires a non-trivial event geometry

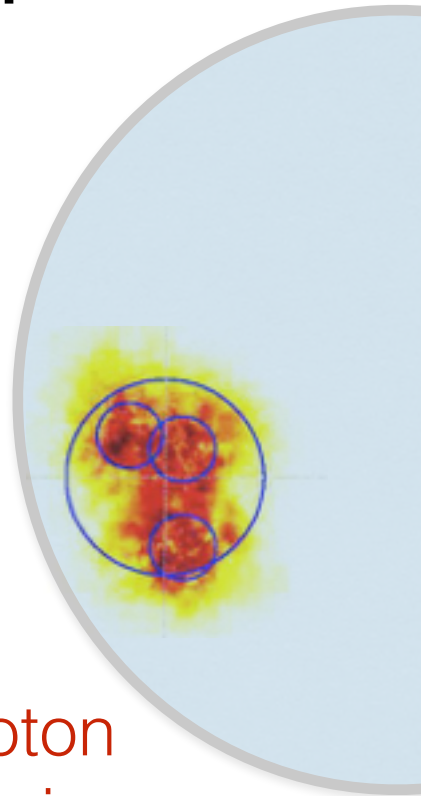
Event geometry in p+p/A collisions closely reflects impact parameter dependence of gluon distribution in proton

Schenke, Venugopalan PRL 113 (2014) 102301

SS, Schenke PLB 739 (2014) 313-319

Mäntysaari, Schenke, Shen, Tribedy arXiv:1705.03177

-> event-by-event fluctuation of the proton  
necessary to generate sizable anisotropies



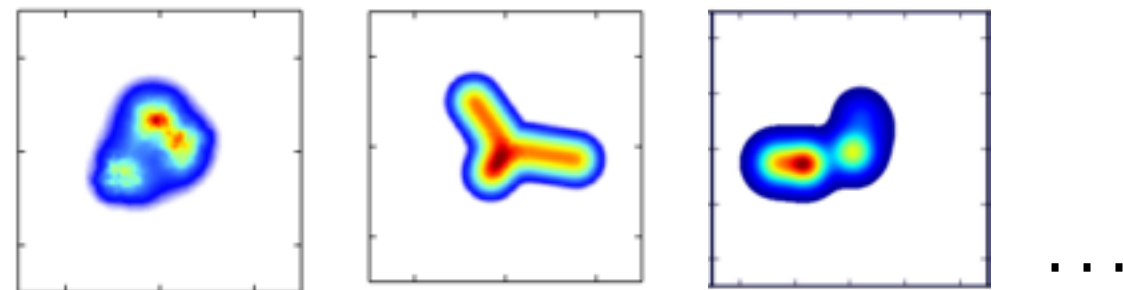
Various models of fluctuating proton sub-structure emerging

Mäntysaari, Schenke PRD 94 (2016) no.3, 034042

Bozek, Broniowski, Rybczynski PRC 94 (2016) no.1, 014902

Habich, Miller, Romatschke, Xiang EPJ. C76 (2016) no.7, 408

Welsh, Singer, Heinz PRC 94 (2016) no.2, 024919

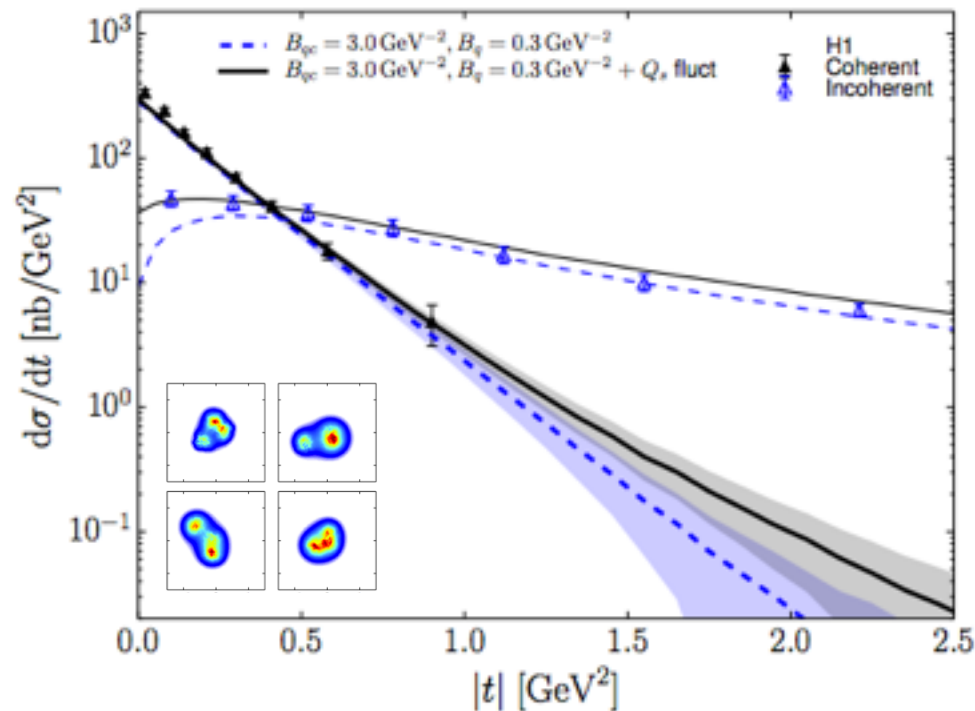


need to be independently constrained to be of predictive value

# Hydrodynamic description of p+p/A

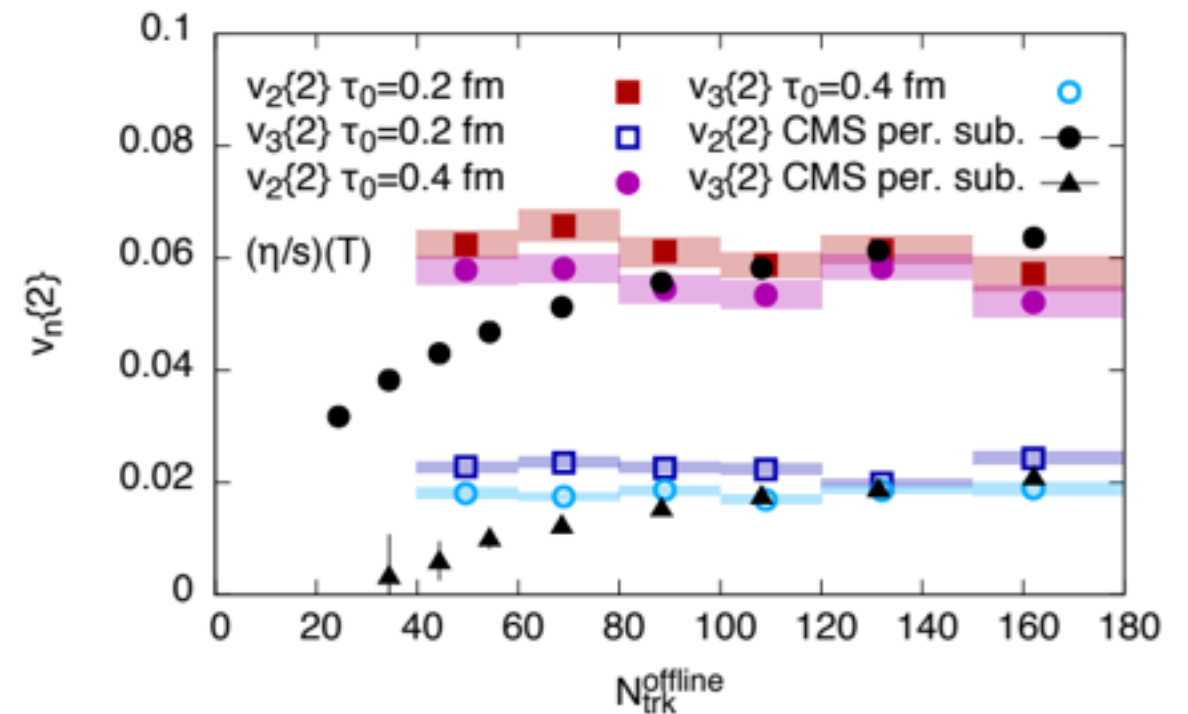
Constrain geometric fluctuations from incoh. diff. J/ $\Psi$  production  
as an input for event-geometry in p+Pb collisions

e+p  $\rightarrow$  e+p\*+J/ $\Psi$



Mäntysaari, Schenke PRD94 (2016) no.3, 034042

p+Pb

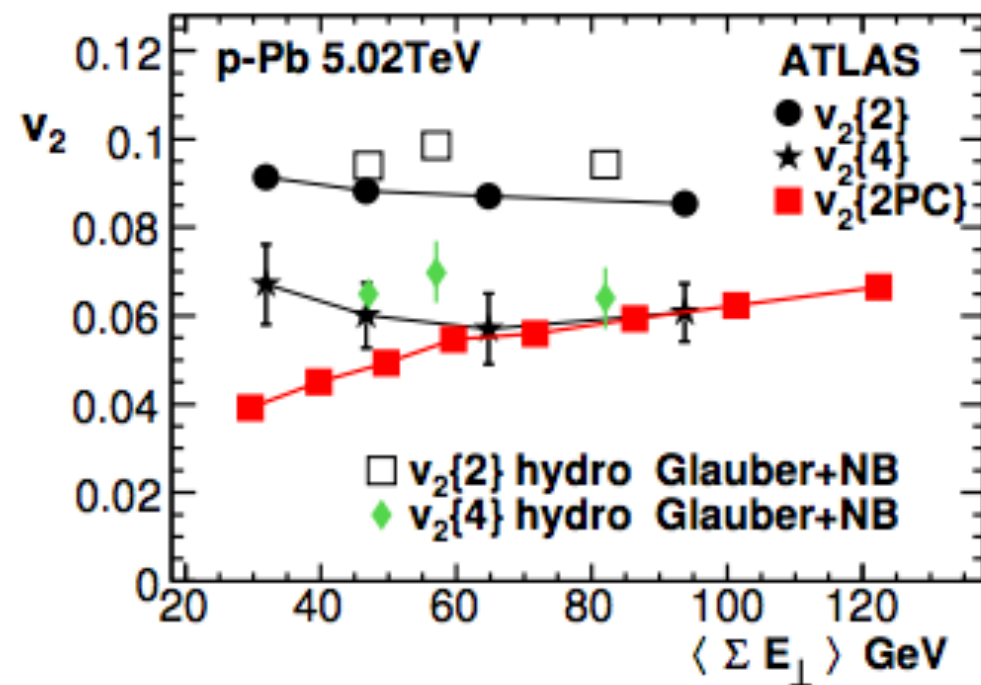


Mäntysaari, Schenke, Shen, Tribedy PLB772 (2017) 681-686

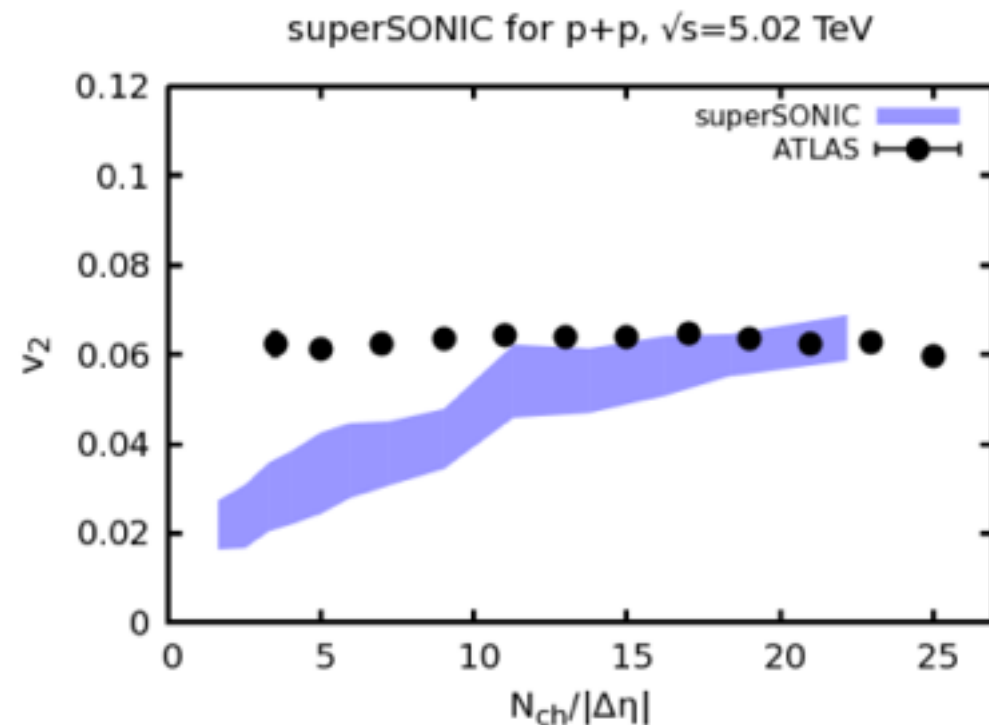
Consistent amount of geometric fluctuations of the proton  
needed to describe e+p and p+Pb data

# Hydrodynamic description of p+p/A

Various calculations by different groups



P. Bozek, W. Broniowski, G. Torrieri, PRL 111 (2013) 172303.



Weller, Romatschke 1701.07145

Generally provide successful phenomenological description of azimuthal correlations in high-multiplicity p+p/A

Caveats: viscous corrections? pre-equilibrium?, ...



# Validity of hydrodynamics in p+p/A?

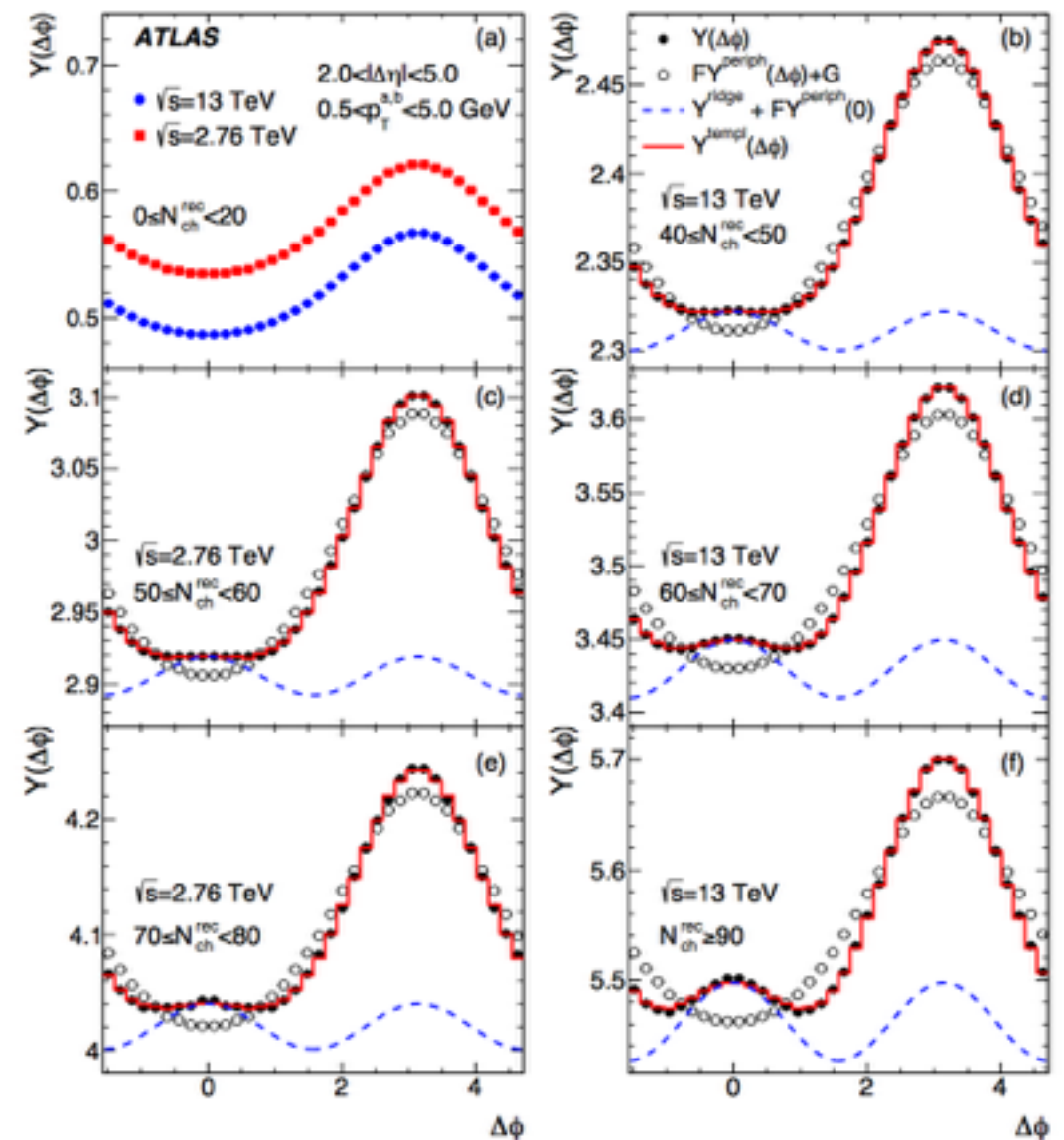
Hydrodynamic description of hadronic collisions only becomes applicable once the system is sufficiently close to local thermal equilibrium

Based on current understanding of pre-equilibrium dynamics

Initial state of hadronic collisions described by collection of mini-jets with typical momenta  $Q_s \sim 2$  GeV

Hydrodynamic description requires significant quenching of mini jets  $\sim Q_s$

Experimental results in high-multiplicity p+p reveal little to no change of the away side (mini-) jet peak

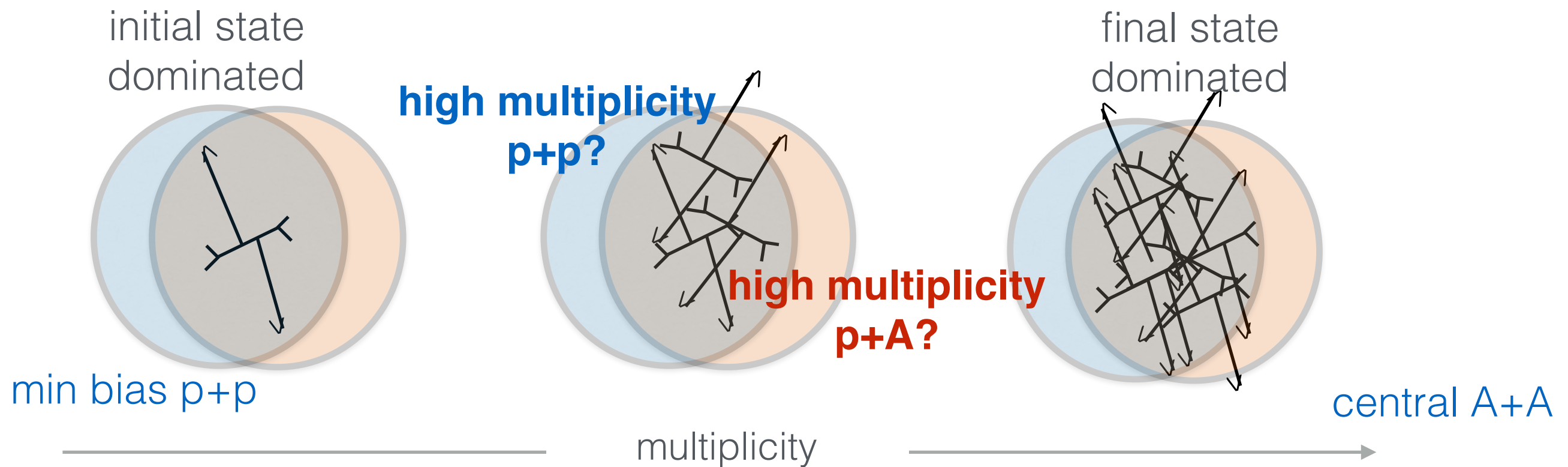


ATLAS  
PRL 116 (2016) no.17, 172301

**Challenge:** Strongly interacting QGP vs. no evidence of (mini-) jet-quenching?

# Collectivity in small systems w/o hydrodynamics?

Even though final state effects will eventually dominate at very high multiplicity, whether or not this point is reached in p+p/A collisions at RHIC and LHC



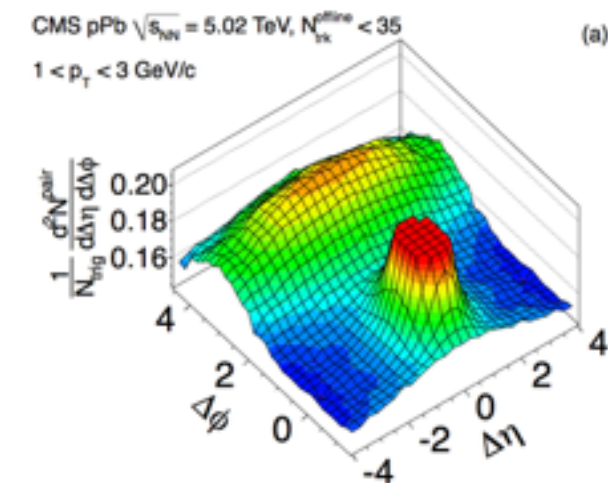
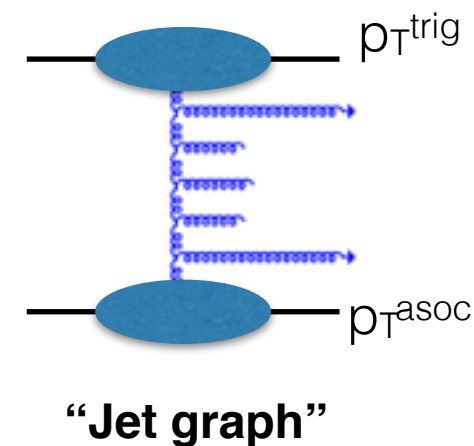
Experimentally observed correlations could also reflect modifications of initial state/early time dynamics in regime of high parton densities

# Initial state correlations

QCD multi-particle production gives rise to intrinsic momentum space correlations present in the initial state

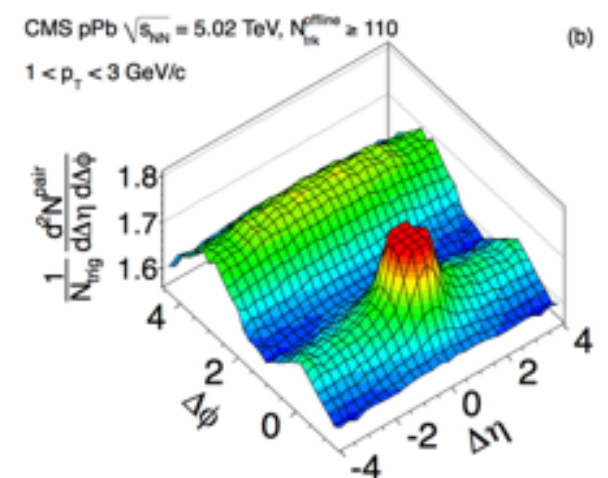
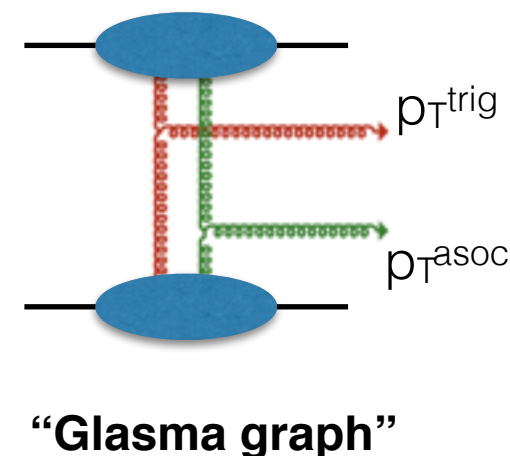
Di-jet like correlations dominate at high  $p_T$  and low mult.

long range ( $\Delta\eta$ ) back-to-back ( $\Delta\phi \sim \pi$ )



Bose-enhancement of small  $x$  gluons gives rise to intrinsic multi-parton correlation for  $p_T \sim Q_s$  in high mult. events

long range ( $\Delta\eta$ ) symmetric ( $\Delta\phi \sim 0, \pi/2$ )



Several calculations point to the fact that initial state effects can be sizable in small systems (p+p, p+A, a+A)

# Phenomenological calculations

## Initial state multi-particle production

### $k_T$ factorization

Dumitru, Dusling, Dusling, Venugopalan  
Gelis, Jalilian-Marian, PRD 87 (2013) 5, 051502,  
Lappi, Venugopalan PRD 87 (2013) 5, 054014,  
PLB 697 (2011) 21-25 PRD 87 (2013) 9, 094034

Dusling, Tribedy, Venugopalan  
PRD 93 (2016) 1 014034

### Hybrid formalism

Dumitru, Giannini Dumitru, McLerran, Skokov  
NPA933 (2015) 212-228 PLB 743 (2015) 134-137  
Lappi Lappi, Schenke, SS, Venugopalan  
PLB 744 (2015) 315-319 JHEP 1601 (2016) 061  
McLerran, Skokov Dusling, Mace, Venugopalan  
NPA 947 (2016) 142-154 arXiv:1705.00745

### Event-by-event classical Yang-Mills simulations

Schenke, SS, Venugopalan  
PLB 747 (2015) 76-82  
Schenke, SS, Tribedy, Venugopalan  
PRL 117 (2016) no.16, 162301

## Hadronization

### Fragmentation functions

N/A

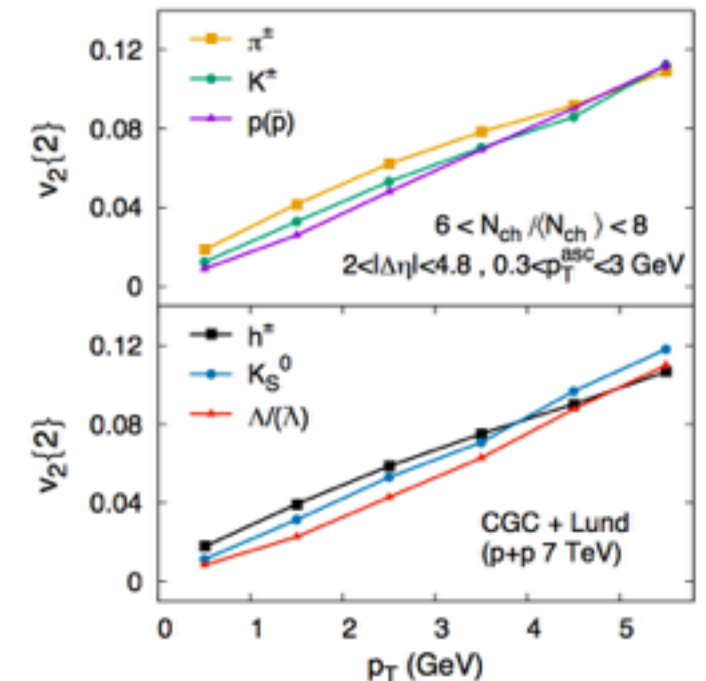
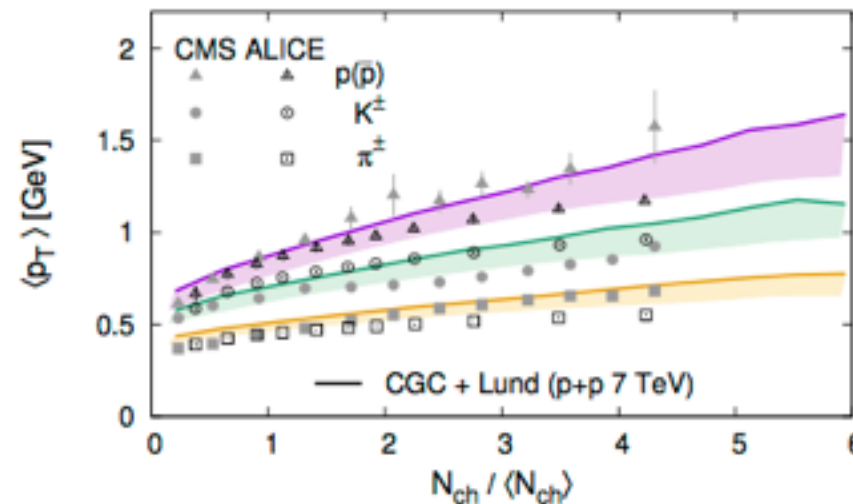
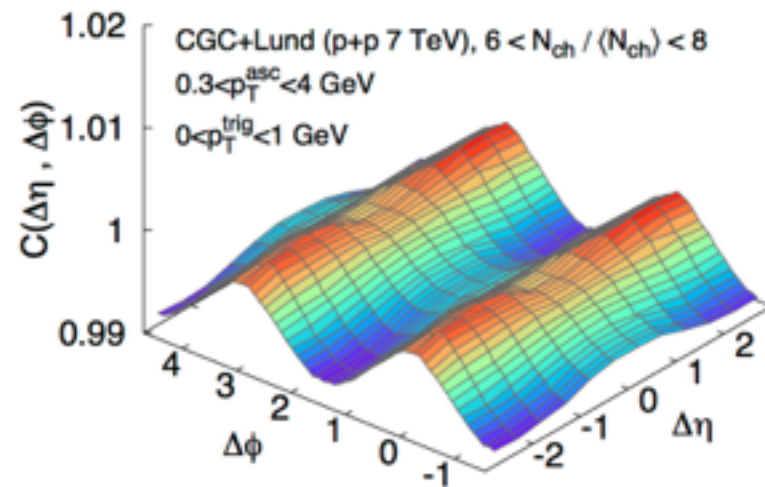
### Monte-Carlo scheme (PYTHIA HSA)

Generally the correlation is  $\sim 1/N_c^2$ , long range in rapidity  
and strongest when  $p_T^1, p_T^2, \dots \sim Q_s$ ,



# Phenomenological calculations

Event-by-event simulations in classical-Yang Mills theory  
+ MC Lund string fragmentation



(Schenke,SS,Tribedy, Venugopalan PRL 117 (2016) no.16, 162301)

Various phenomenologically important aspects have been addressed in different calculations

$v_2/v_3$  , higher-cumulants ,  $v_2 / \langle p_T \rangle$  mass ordering, ...

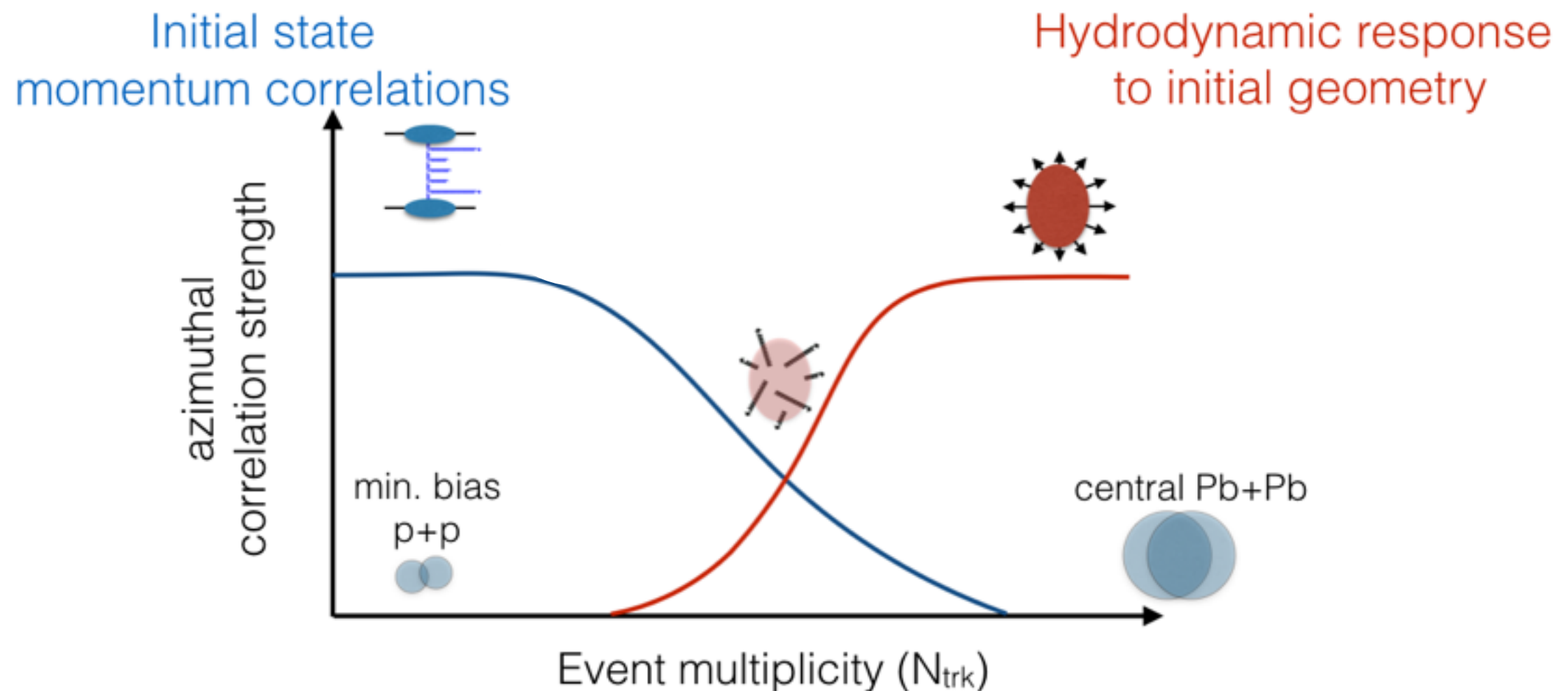
showing that characteristic features of the data can be reproduced.

**Challenge:** Even though sizable correlations are expected to be present in the initial state, so far these calculations do not take into account possible modifications due to final state effects



# Qualitative picture of dynamics

Generally speaking to understand the dynamics over the full range of multiplicities from low multiplicity p+p to central A+A collisions we eventually expect to see a transition from initial state to final state dominance



SS, Quark Matter 2015, NPA 956 (2016) 216-221; SS, Tribedy Adv. High Energy Phys. Vol. 2016 (2016), 8460349

# Initial state vs. final state effects

Based on recent progress in understanding of pre-equilibrium dynamics at weak coupling, one can attempt to estimate the transition region

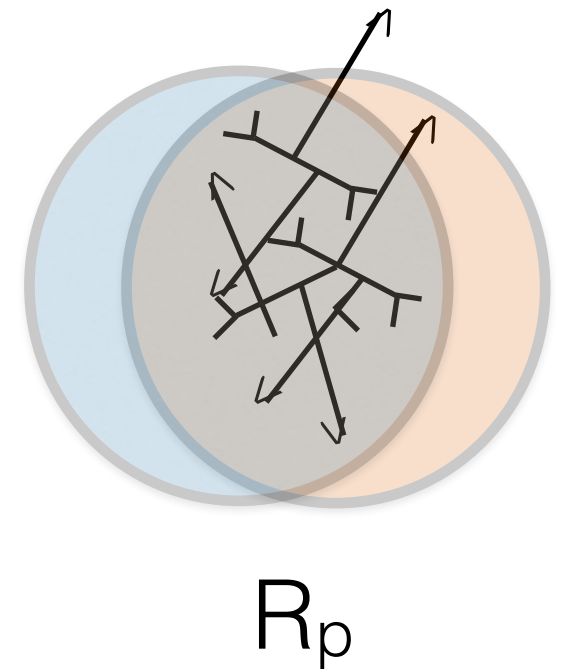
D.Teaney Initial Stages 2016 | SS, Tribedy Adv. High Energy Phys. Vol. 2016 (2016), 8460349

Criterion: mini-jet equilibration time < system size

Kurkela, Zhu PRL 115 (2015) no.18, 182301

$$Q_s \tau_{eq} \simeq 10(\eta/s)^{4/3} (g^2 N_c)^{1/3} \simeq 6 \quad (\eta/s = 5/4\pi \mid \lambda = 10)$$

$$\frac{dN}{dy} \simeq \frac{1}{4} Q_s^2 \pi R_p^2 \quad \frac{\tau_{eq}}{R_p} \simeq \sqrt{\frac{50}{dN/dy}}$$



Ball-park estimate for transition from initial state to final state regime indicates that a lot of the interesting dynamics observed in high-multiplicity p+p/A collisions could well be in the transition region

Development of new theoretical approaches crucial to describe the relevant physics across wide kinematic range probed in RHIC/LHC experiments

# Non-equilibrium description of initial state & final state effects

## Event-by-event classical-Yang Mills + parton cascade

- 1 Simulate particle production and early time dynamics ( $\tau < 0.2$  fm) in classical Yang-Mills theory, based on IP-Glasma framework

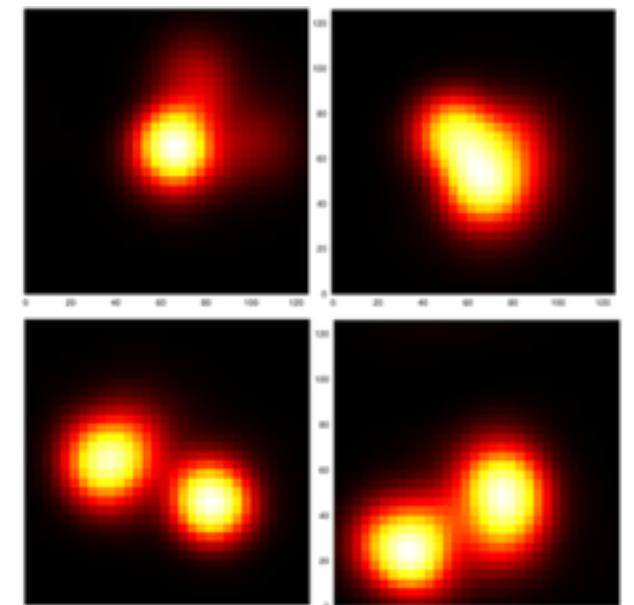
hadronic structure input constrained by DIS

- 2 Extract phase-space distribution  $dN/d^2x d^2p$  of gluons from classical Yang-Mills simulations, which contains full information on

- initial state momentum correlations
- non-trivial event geometry

- 3 Simulate final state dynamics in parton cascade (BAMPS) including pQCD  $2 \leftrightarrow 2$  and  $2 \leftrightarrow 3$  processes

Event geometry

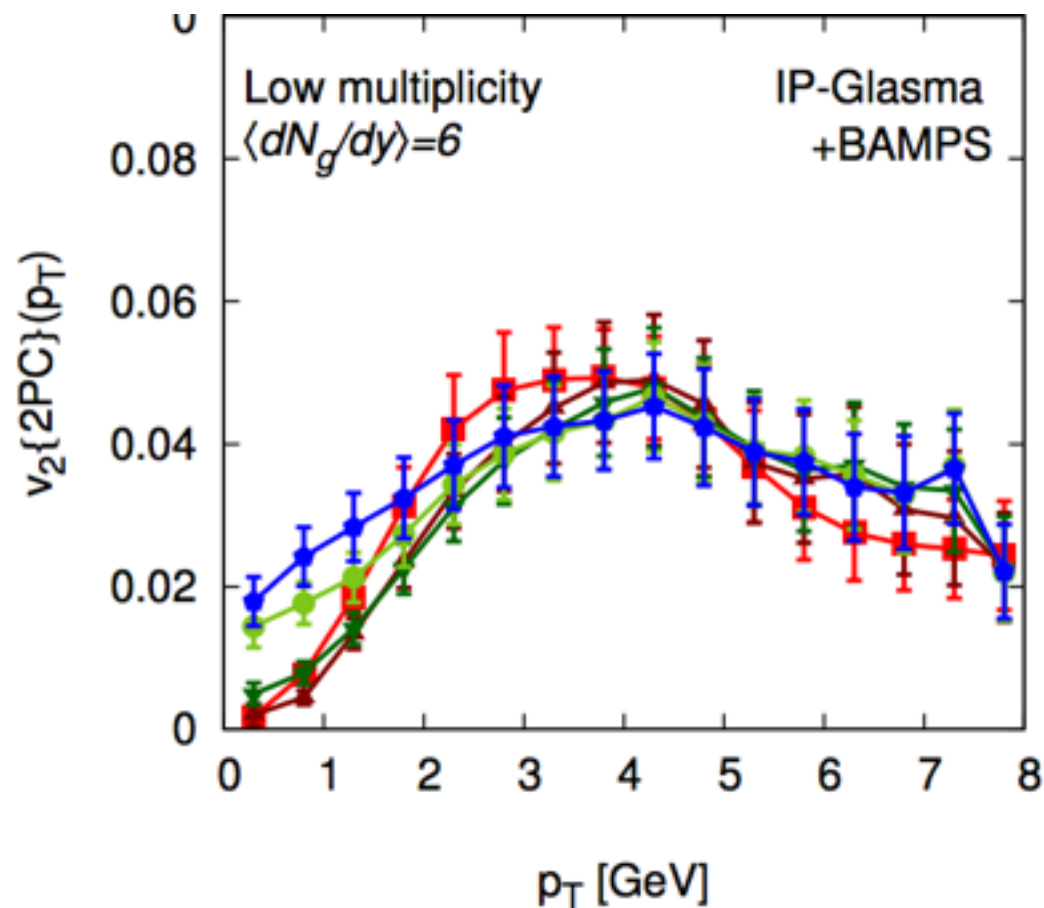


-> Extract time evolution of partonic  $v_2$  to assess the relative importance of initial state & final state effects in small systems

# High multiplicity vs. low multiplicity

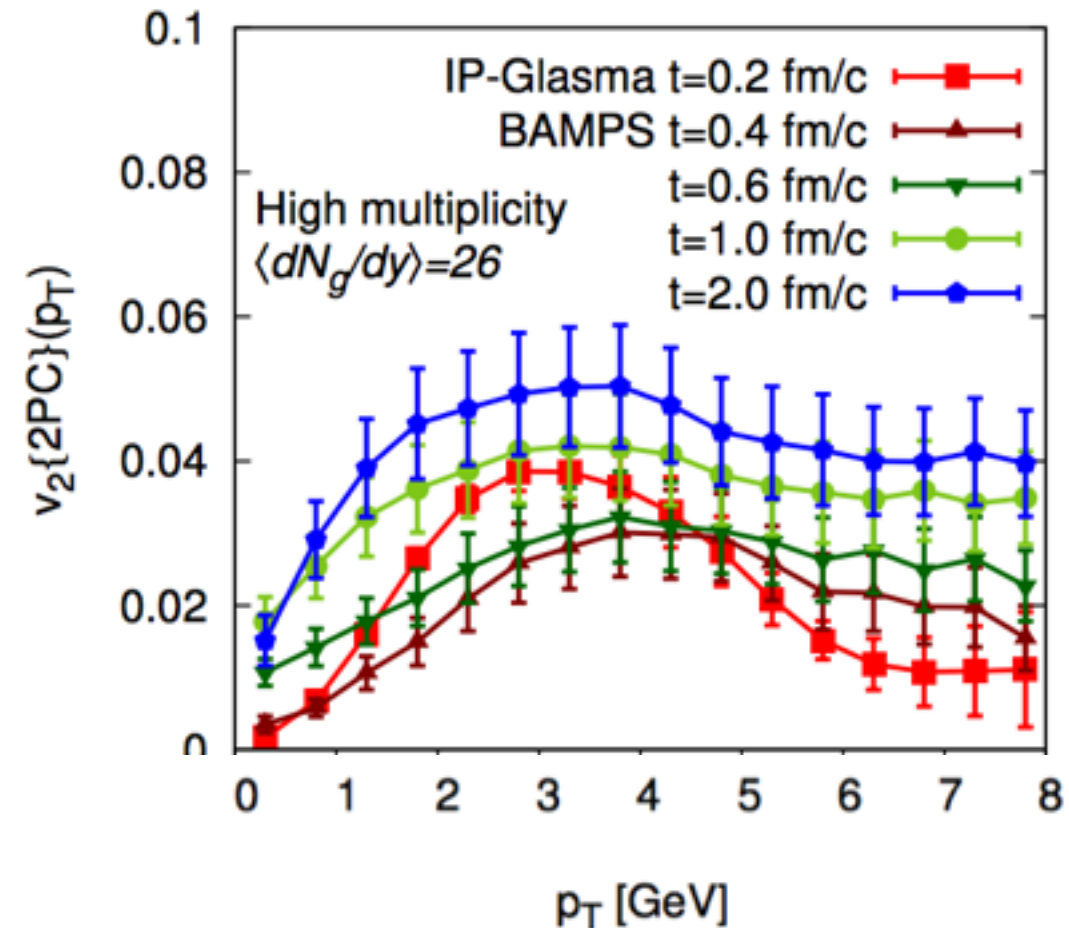
(Greif, Greiner, Schenke, SS, Xu arXiv:1708.02076)

low mult. p+Pb



Very little modification of initial state correlations

high mult. p+Pb



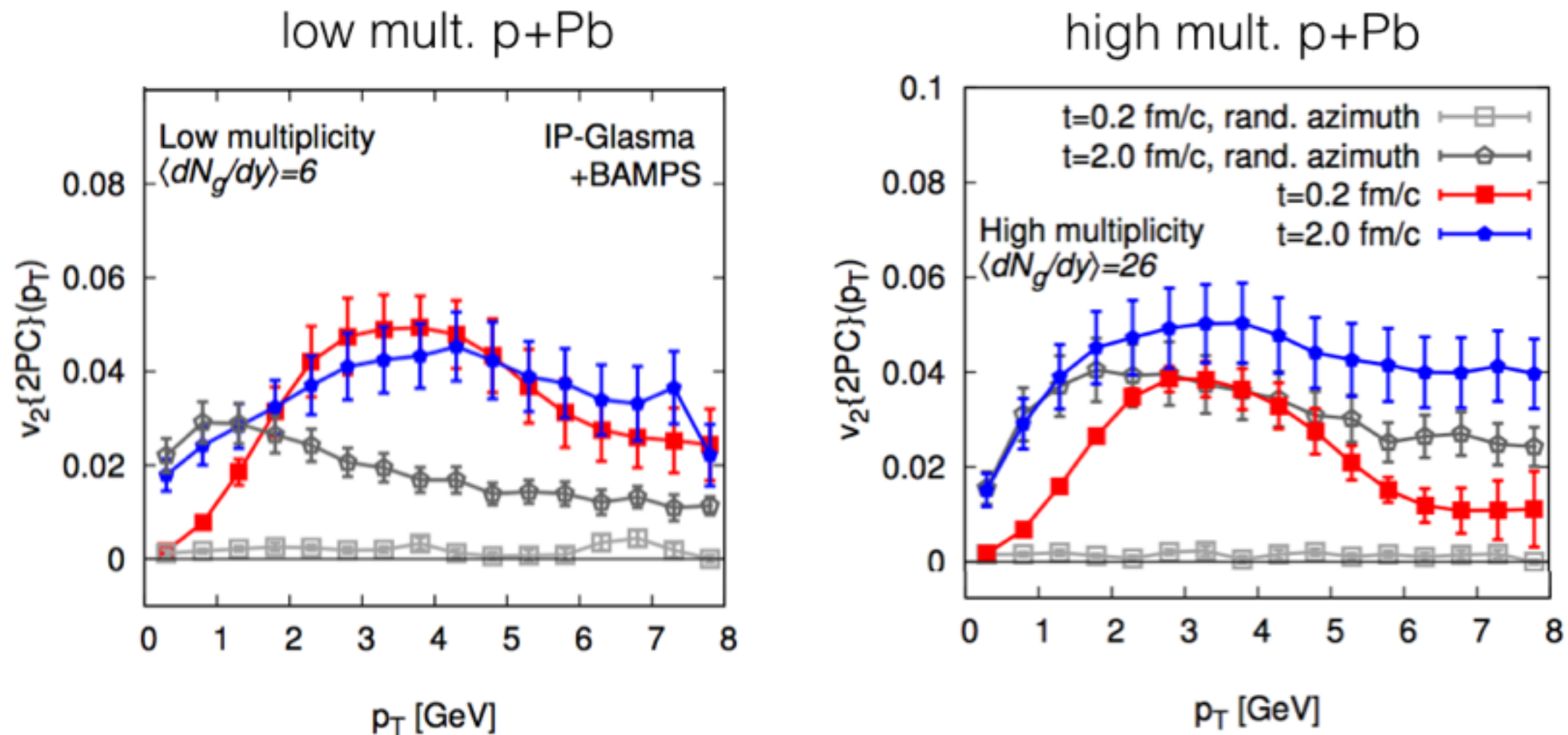
Strong modification of initial state correlations

Significant difference between low and high-multiplicity events, due to larger number of large angle scatterings

# Initial state vs. final state effects

(Greif, Greiner, Schenke, SS, Xu arXiv:1708.02076)

Isolate different effects by manually removing initial state momentum correlations



low  $p_T$  ( $<2$  GeV): dominance of final state effects

high  $p_T$  ( $>2$  GeV): competition of initial & final state

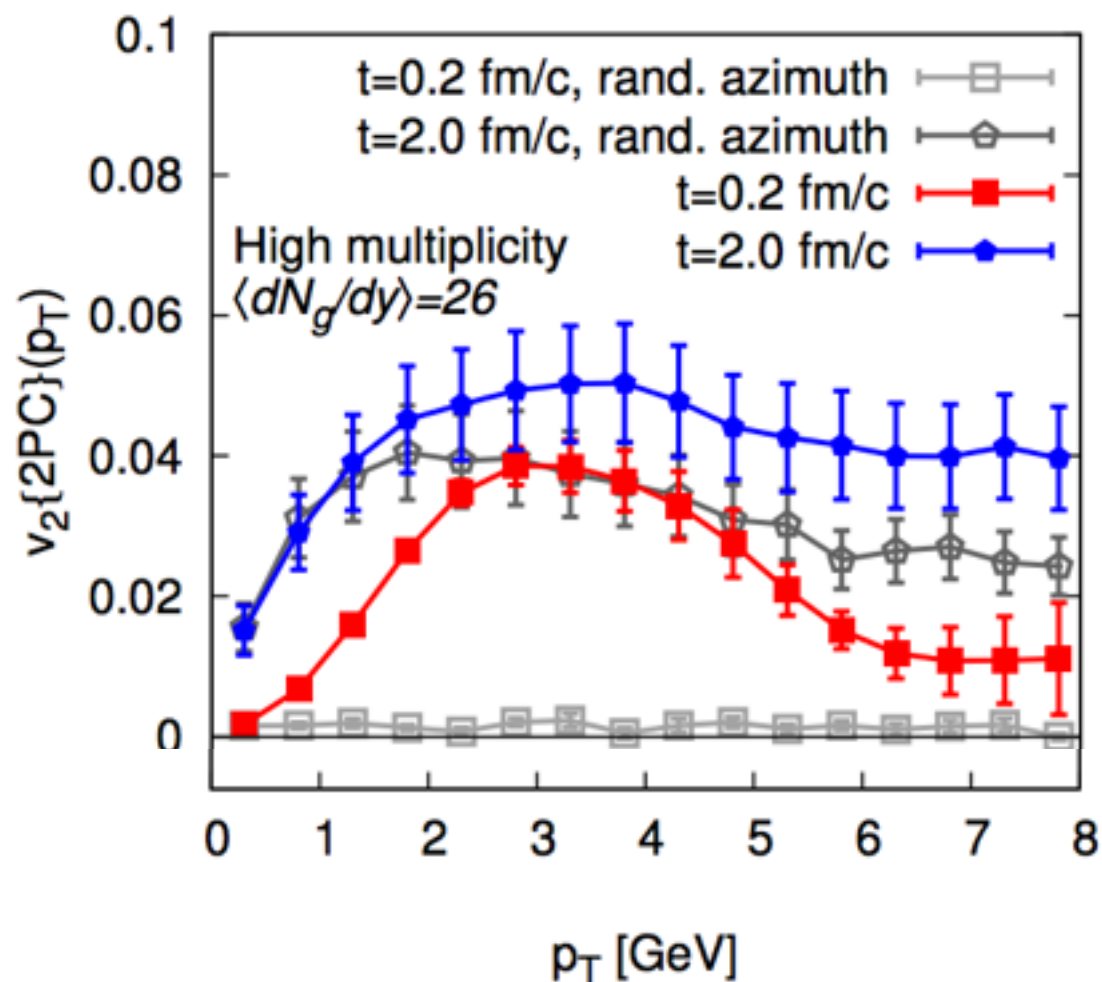


# Initial state vs. final state effects

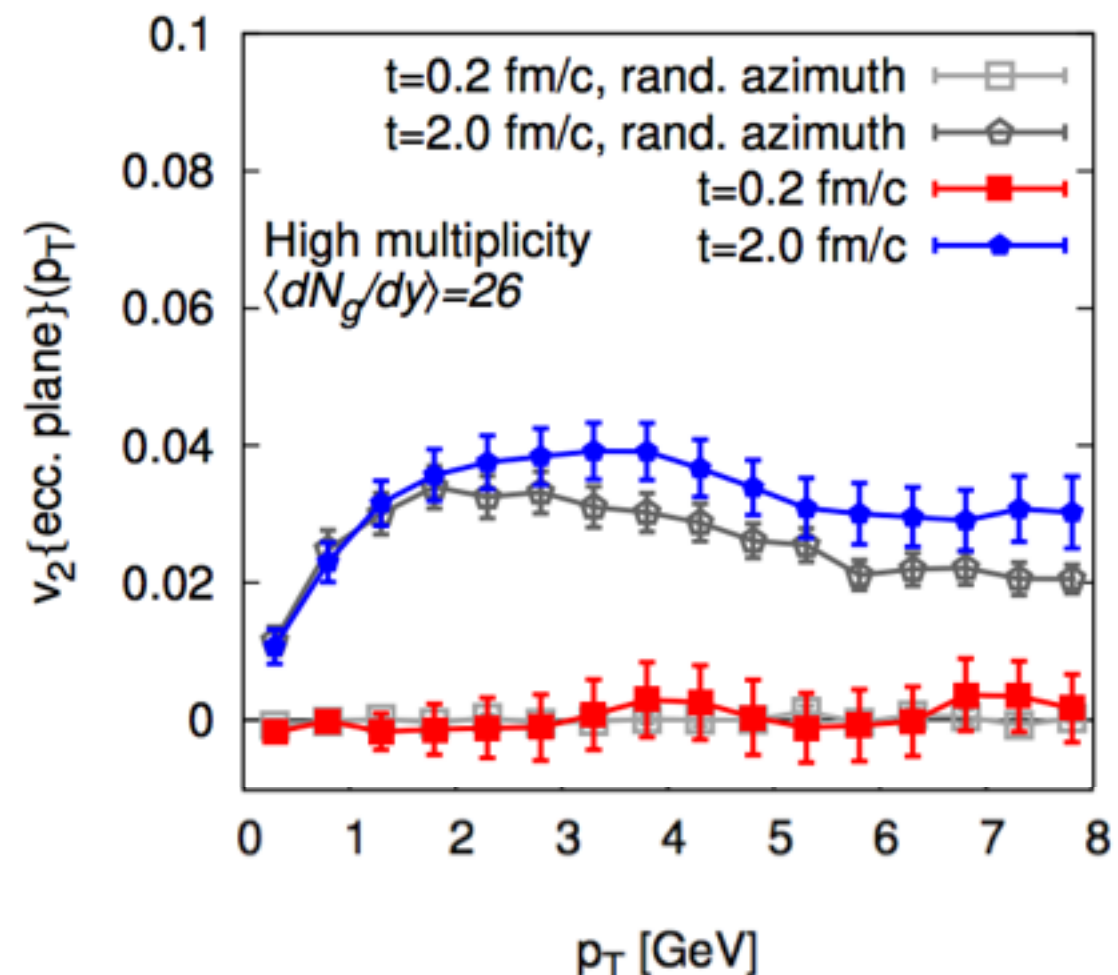
(Greif, Greiner, Schenke, SS, Xu arXiv:1708.02076)

Compare  $v_2\{2\}$  with correlation w.r.t to geometric eccentricity plane

2-PC



Ecc. plane



Even though average number of scatterings per particle is quite small ( $N_{\text{Scat}} = 5.6 \pm 1.1$ ) with only large angle scatterings ( $N_{\text{large angle}} = 1 \pm 0.18$ ), low momentum  $v_2$  in high multiplicity events is of geometric origin

# Initial state vs. final state effects

(Greif, Greiner, Schenke, SS, Xu arXiv:1708.02076)

## Evolution of azimuthal correlations

$t \sim 0 - 0.2$  fm:

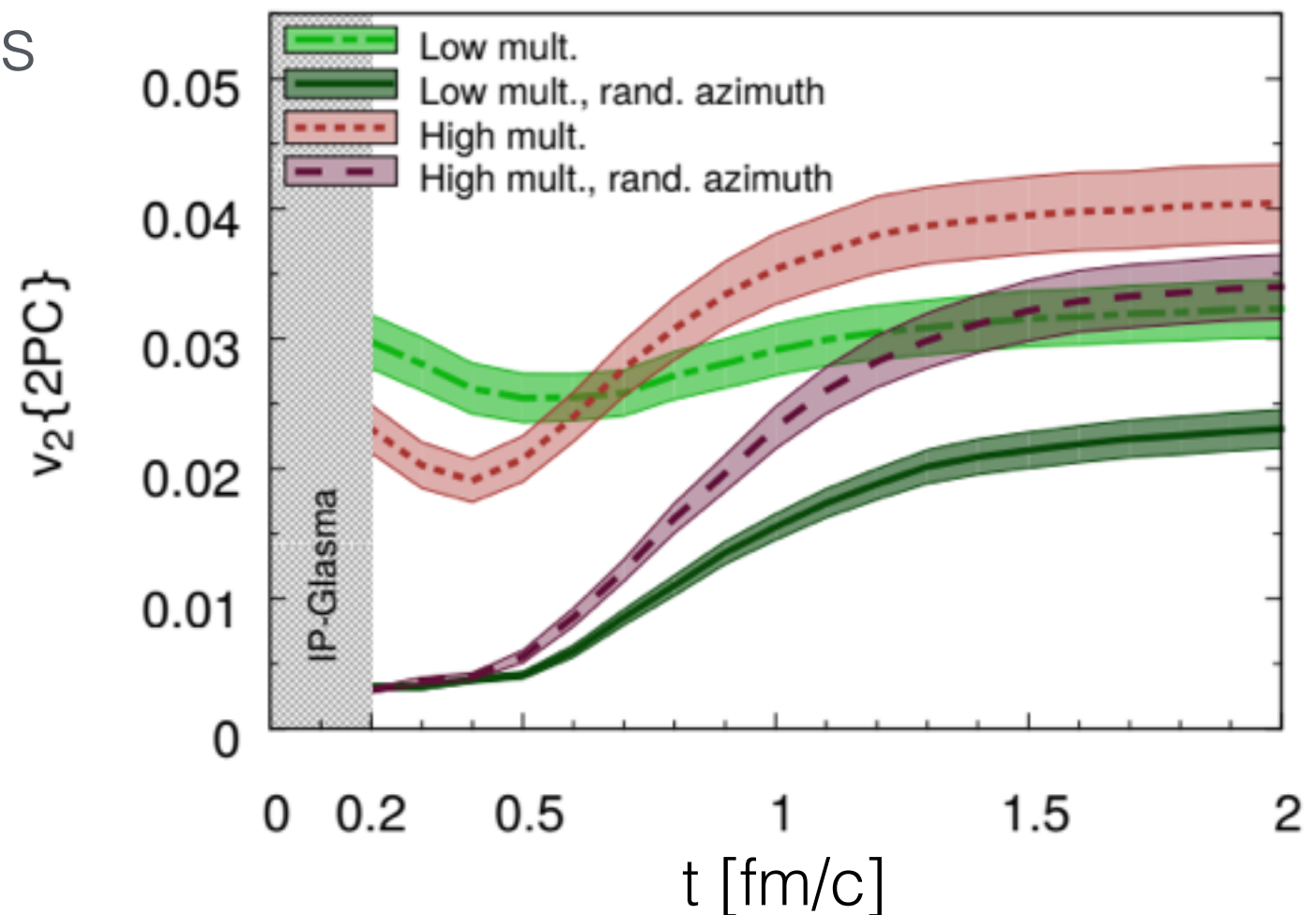
Dominated by initial state

$t \sim 0.2 - 0.5$  fm:

Scatterings partially destroy initial state correlation.

$t \sim 0.5 - 1.0$  fm:

New correlations build up in response to geometry



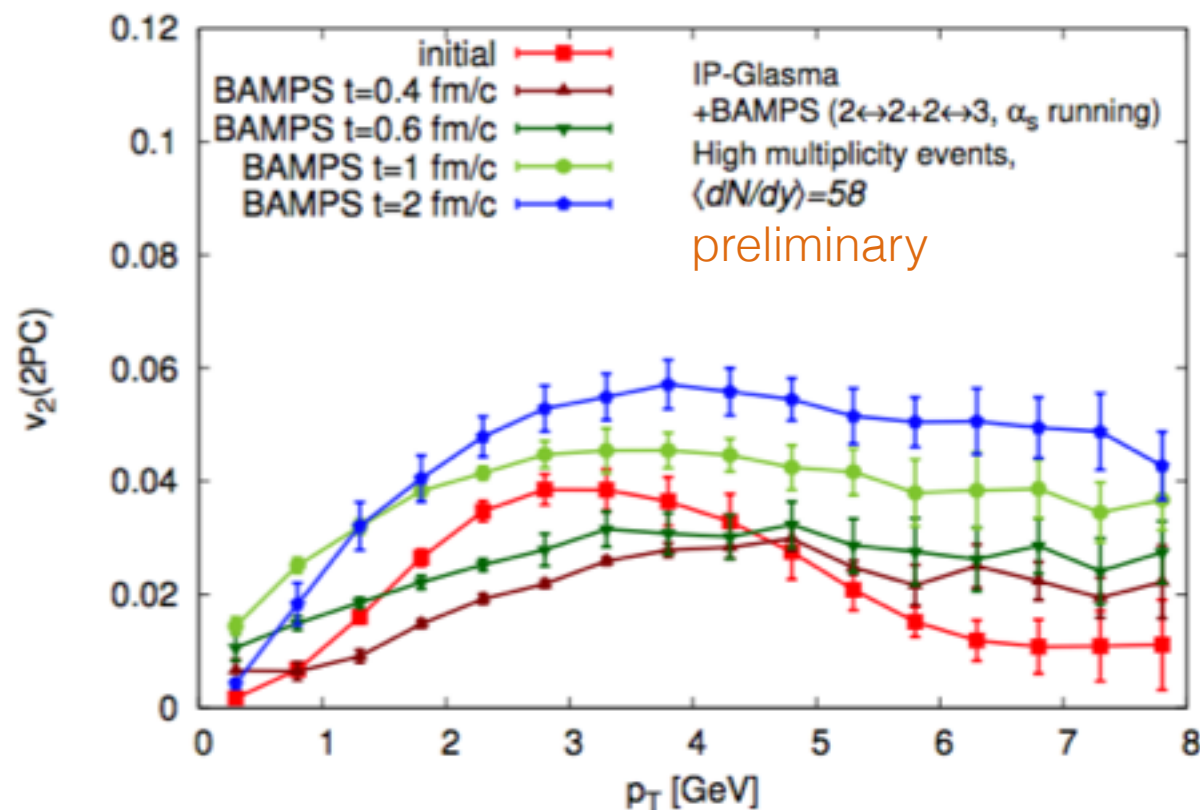
Even though geometric response ultimately dominates at low  $p_T$ , there are still sizable effects of initial state correlations even on the  $p_T$  integrated  $v_2$  ( $\sim 25\%$  for high.mult. and  $\sim 50\%$  for low mult.)

# Sensitivity to pre-equilibrium dynamics

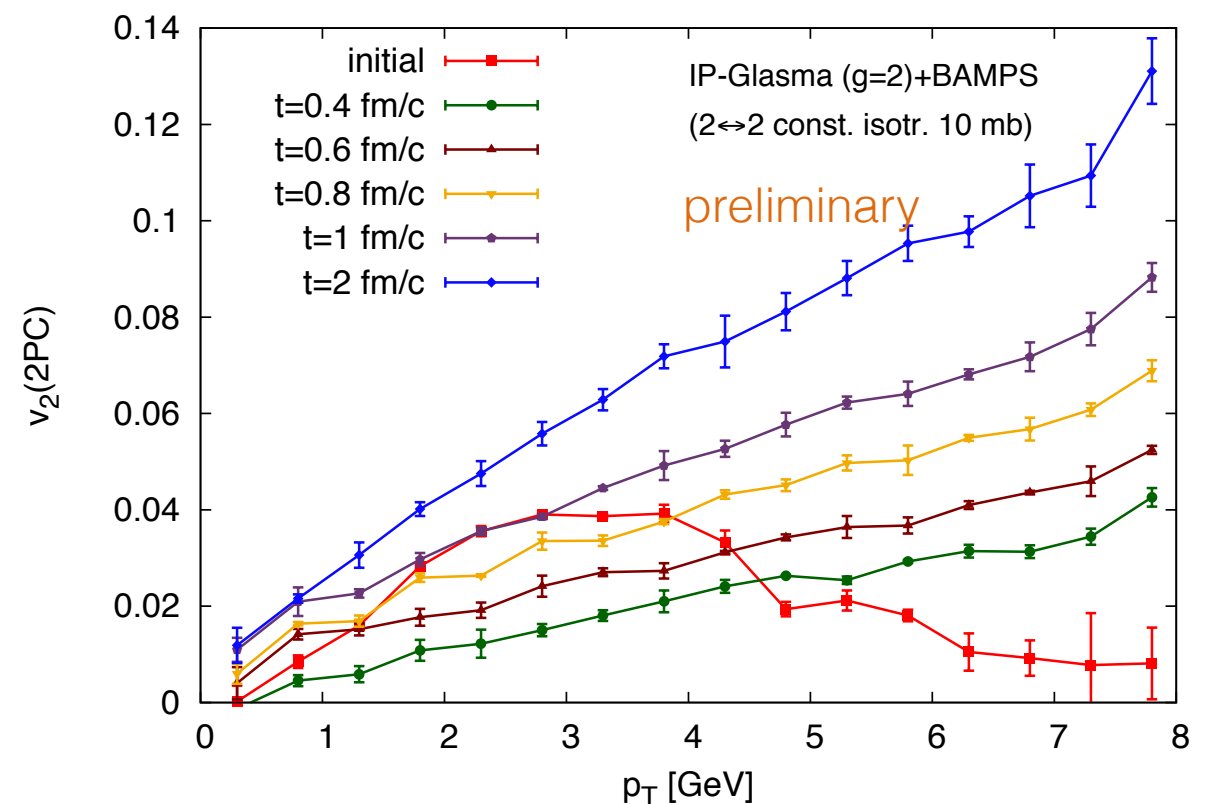
(Greif, Greiner, Schenke, SS, Xu work in progress)

Quantitative features of evolution is quite sensitive to pre-equilibrium dynamics — initial state correlations never washed out completely

pQCD



const. isotropic cross-section



Clear discrepancy between  $2\leftrightarrow 2$  and  $2\leftrightarrow 3$  pQCD processes and naive toy model with const. isotropic cross-section (at least at high  $p_T$ )

Prove of principle that azimuthal correlations in small systems can provide sensitivity to pre-equilibrium dynamics

# Collective behavior?

Higher order cumulants ( $m > 2$ ) provide clear evidence that (some of) correlations are between many particles

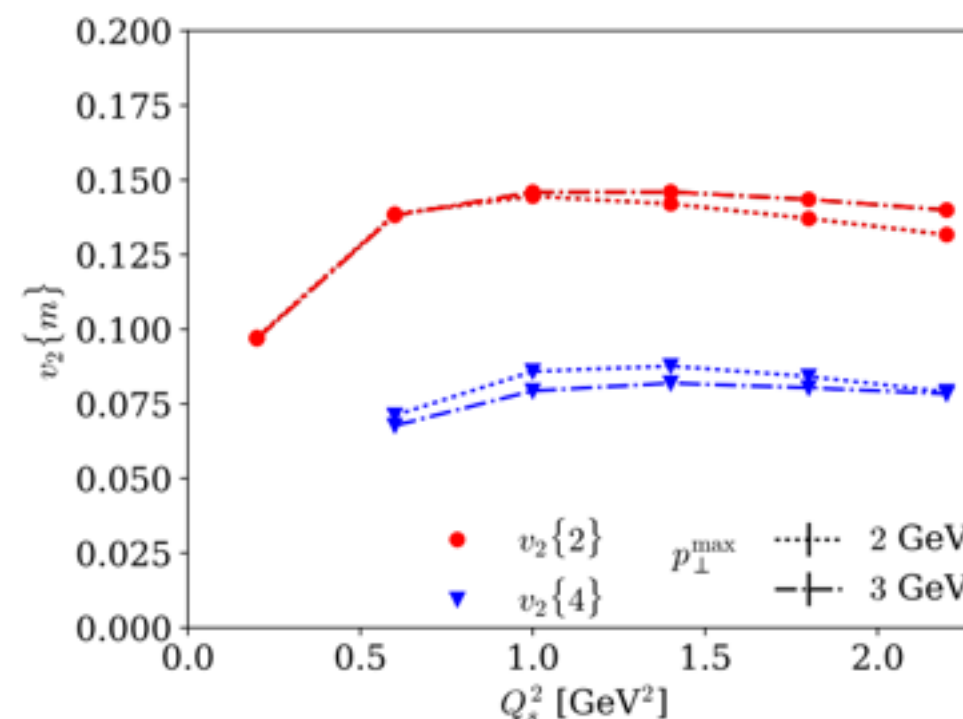
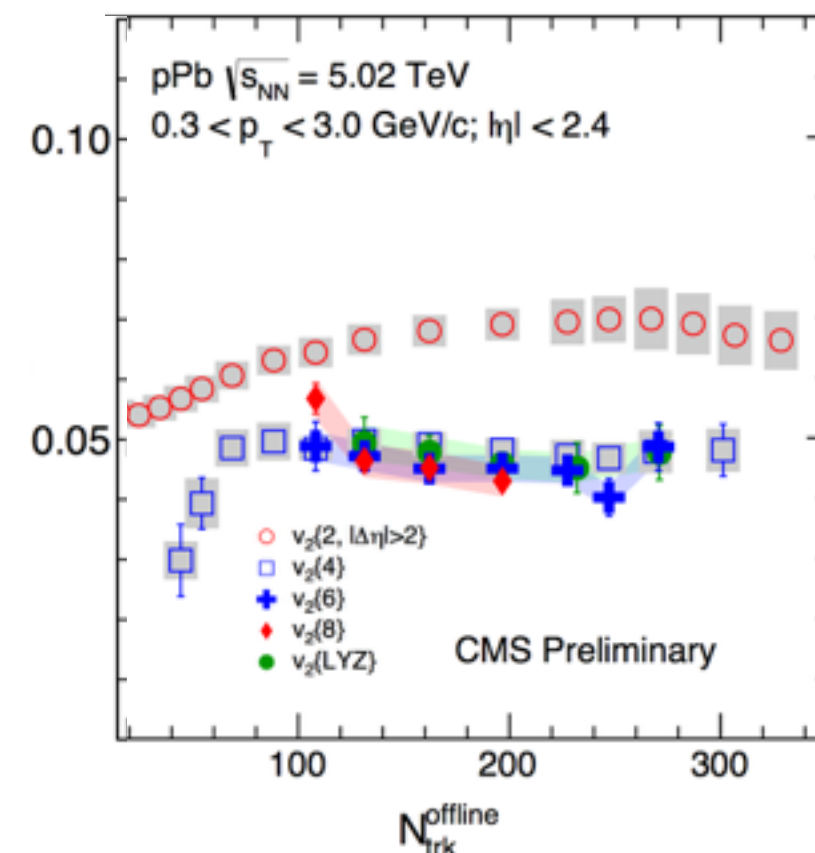
Clearly geometric correlations with the event geometry carry over to all (low  $p_T$ ) particles

-> naturally expect sizable  $v_n\{m\}$  ( $m > 2$ ) in microscopic non-equilibrium framework

Genuine multi particle correlations also present in initial state

Dusling, Mace, Venugopalan arXiv:1705.00745

Should expect contributions from both; important to clarify dominant effects within combined framework



Dusling, Mace, Venugopalan arXiv:1705.00745

# Conclusions & Perspectives

Observation of long. range azimuthal correlations in small systems are challenging us to develop a unified picture of the space-time evolution of hadronic collisions

-> Exciting connections with unresolved problems in A+A  
(equilibration, intermediate  $p_T$  physics)

Showed first calculation including both initial state and final state effects, based on weak-coupling description ( class. YM + pQCD transport)

-> Clear demonstration that both initial state & final state effects are important with relative strength dependent on multiplicity & transverse momentum

## ***Change of paradigm:***

Consistent theoretical description across experimental range of multiplicities and transverse momenta requires both initial state and final state effects

Still lots of work to be done concerning in particular  
interplay soft physics <-> high- $p_T$ /jets



# Backup

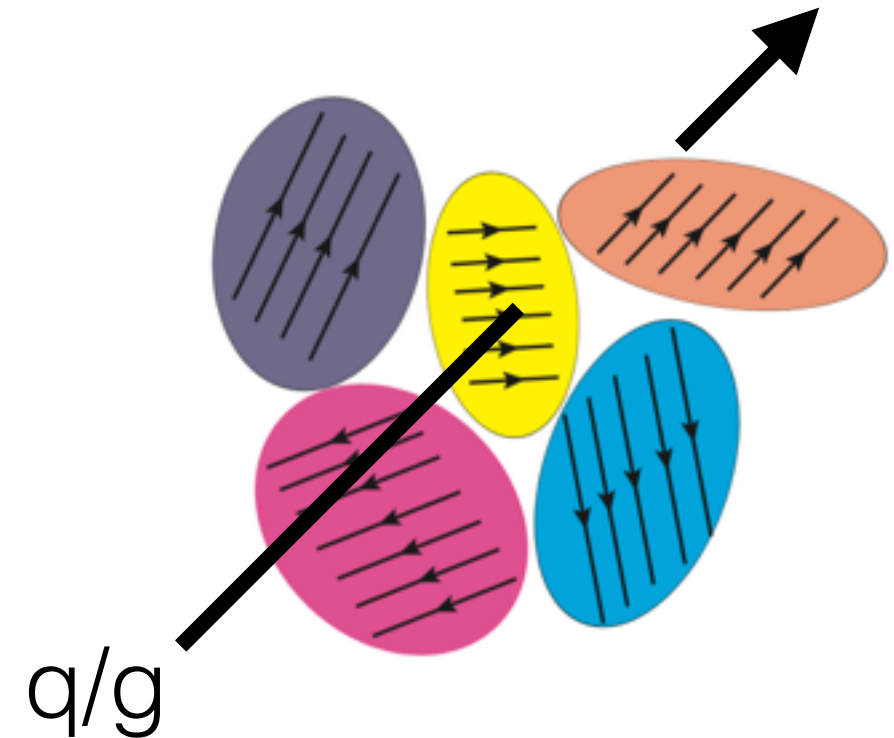
# Initial state correlations in high-multiplicity events

Intuitive picture at small  $x$ :

Bose enhancement of small  $x$  gluons in wave function allows treatment as a classical color field

Scattering amplitude of projectile parton

$$V_x = \mathcal{P} e^{-ig \int dx^- A^+}$$



Distribution of scattered partons

$$\frac{dN_{q/g}}{d^2\mathbf{k}_T} = \int_{\mathbf{p}_T, \mathbf{b}_T, \mathbf{r}_T} W_{q/g}(\mathbf{p}_T, \mathbf{b}_T) e^{-i(\mathbf{k}_T - \mathbf{p}_T) \cdot \mathbf{r}_T} \text{tr}_{f/a} V(\mathbf{b}_T + \mathbf{r}_T/2) V^\dagger(\mathbf{b}_T - \mathbf{r}_T/2)$$

Short-distance expansion: Each parton receives a momentum kick in the direction of the light-cone electric field

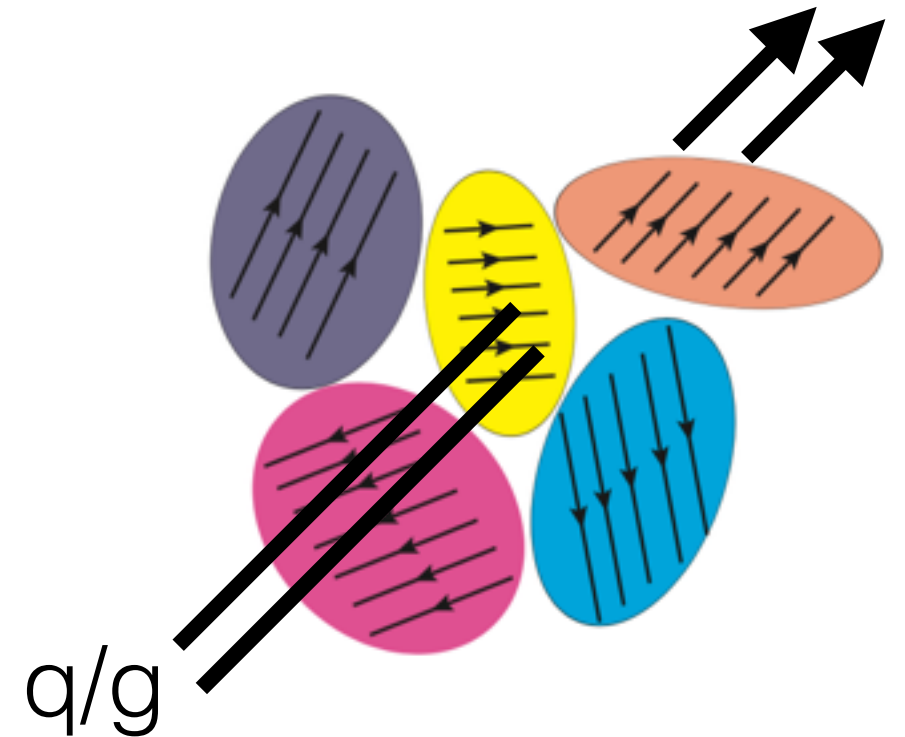
$$E^i(\mathbf{b}_T) = \frac{i}{g} V(\mathbf{b}_T) \partial^i V^\dagger(\mathbf{b}_T)$$

# Initial state correlations in high-multiplicity events

Intuitive picture at small  $x$ :

Each parton scattering off the same domain receives a kick in the direction of the chromo-electric field which leads to a correlation in azimuthal angle

$$\left\langle \frac{dN_{q/g}}{d^2\mathbf{k}_1 d^2\mathbf{k}_2} \right\rangle = \int_{\mathbf{p}_1, \mathbf{b}_1, \mathbf{r}_1}^{\mathbf{p}_2, \mathbf{b}_2, \mathbf{r}_2} W_{q/g}(\mathbf{p}_1, \mathbf{b}_1) e^{-i(\mathbf{k}_1 - \mathbf{p}_1)\mathbf{r}_1} W_{q/g}(\mathbf{p}_2, \mathbf{b}_2) e^{-i(\mathbf{k}_2 - \mathbf{p}_2)\mathbf{r}_2} \\ \left\langle \text{tr}_{f/a} V(\mathbf{b}_1 + \mathbf{r}_1/2) V^\dagger(\mathbf{b}_1 - \mathbf{r}_1/2) \text{tr}_{f/a} V(\mathbf{b}_2 + \mathbf{r}_2/2) V^\dagger(\mathbf{b}_2 - \mathbf{r}_2/2) \right\rangle$$



-> Near-side ( $\Delta\phi \sim 0$ ) azimuthal correlation  $\sim 1/(N_c^2 Q_s^2 S_T)$

Since the decoration of color fields inside nucleus is slow ( $\Delta\eta_{\text{corr}} \sim 1/\alpha_s$ ) correlations are naturally long range in rapidity